

Fundamental Physics with Nuclei

S@INT Seminar

2 June 2022 Saori Pastore

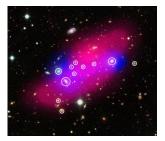
https://physics.wustl.edu/quantum-monte-carlo-group

Quantum Monte Carlo Group @ WashU Lorenzo Andreoli (PD) Jason Bub (GS) Garrett King (GS) Maria Piarulli and Saori Pastore

Computational Resources awarded by the DOE ALCC and INCITE programs

Fundamental Physics with Nuclei





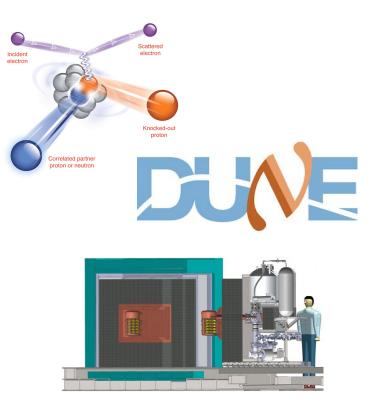
ESA, XMM-Newton, Gastaldello, CFHTL



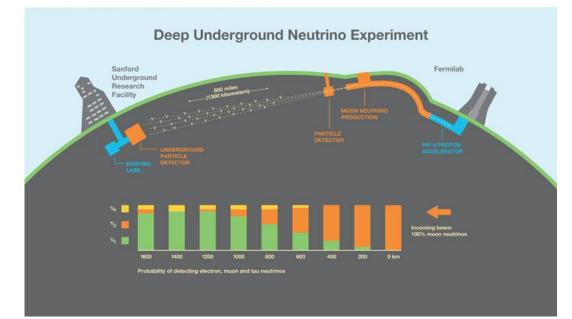
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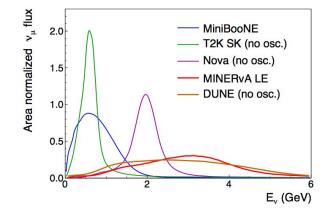
To an arrow, electrone range around the mechan at domains repeating up to 10,000 mms; the muchan Zhanisers (the channes cloud were shown to acids, this chart would move a small some.





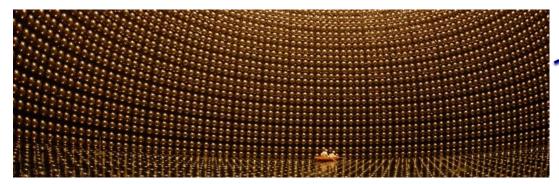
Accelerator Neutrinos' Experiments



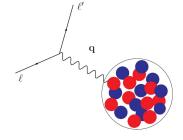


DUNE - Fermilab

Nuclei for Neutrino Oscillations' Experiments

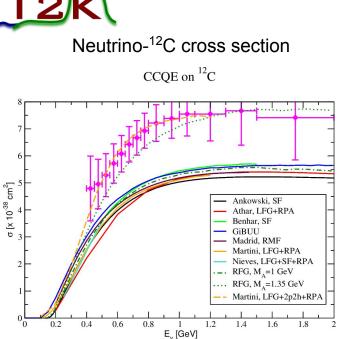


$$P(\mathbf{v}_{\mu} \to \mathbf{v}_{e}) = \sin^{2}2\theta \sin^{2}\left(\frac{\Delta m_{21}^{2}L}{2\mathbf{E}_{v}}\right)$$



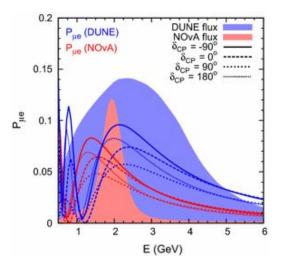
Nuclei are the active material in

the detector. The energy of the incident neutrino is reconstructed from the observed final states using **neutrino event generators** that require **theoretical cross-sections**.



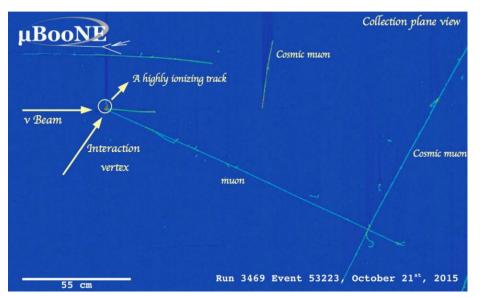
Alvarez-Ruso arXiv:1012.3871

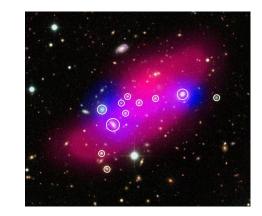
The needs of the experimental programs



The range of challenges is extreme;

ultimately we would like to be able to predict both inclusive and **exclusive cross sections across a wide range of kinematics**. The experimental neutrino program is in need of accurate **theoretical calculations of neutrino-nucleus cross-sections with quantified theoretical errors** to ensure a robust implementation of interaction models in experiments

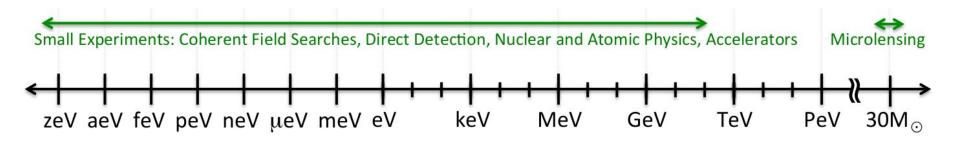




Candidates

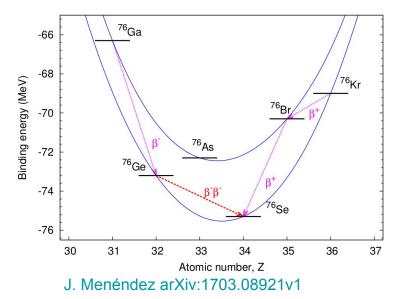
Dark Matter

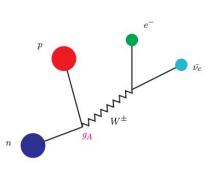
ESA, XMM-Newton, Gastaldello, CFHTL



US cosmic vision 2017

Single and Double Beta Decays







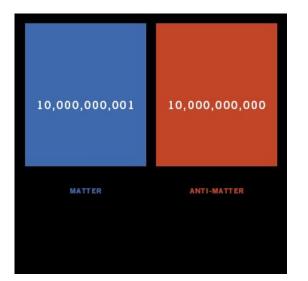
Maria Goeppert-Mayer

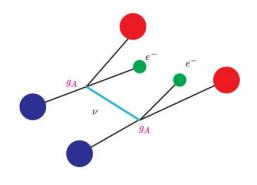
Single beta decay

 $(\mathbf{Z}, \mathbf{N}) \rightarrow (\mathbf{Z}+1, \mathbf{N}-1) + e + \bar{\mathbf{v}}_e$ Double beta decay $(Z, N) \rightarrow (Z+2, N-2) + 2e + 2\bar{v}_e$

Here the lepton number is conserved

Neutrinoless double beta decay







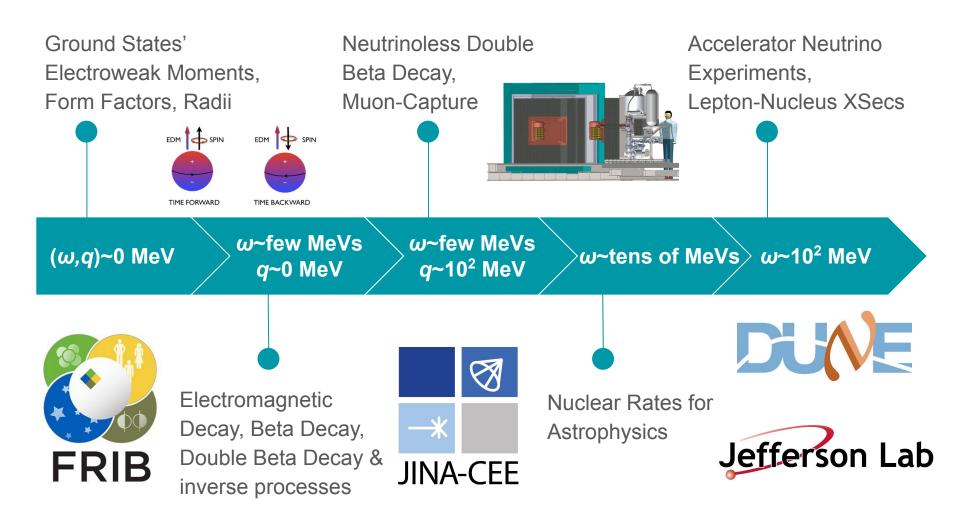
Ettore Majorana

 $(\mathbf{Z}, \mathbf{N}) \rightarrow (\mathbf{Z} + \mathbf{2}, \mathbf{N} - \mathbf{2}) + 2e$

Hitoshi Murayama



Lepton number is not conserved Decay Rate \propto (nuclear matrix element)² x (m_{BB})²



Strategy

Validate the Nuclear Model against available data for strong and electroweak observables

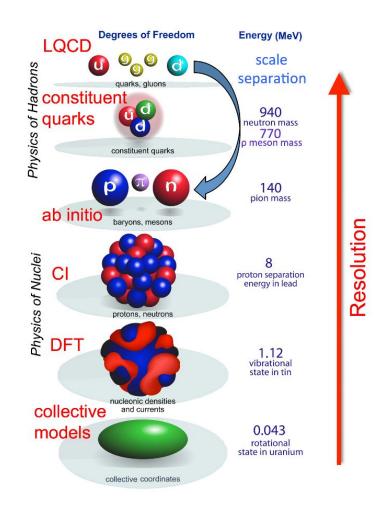
- Energy Spectra, Electromagnetic Form Factors, Electromagnetic Moments, ...
- Electromagnetic and Beta decay rates, ...
- Muon Capture Rates, ...
- Electron-Nucleus Scattering Cross Sections, ...

Use attained information to make (accurate) predictions for BSM searches and precision tests

- EDMs, Hadronic PV, ...
- BSM searches with beta decay, ...
- Neutrinoless double beta decay, ...
- Neutrino-Nucleus Scattering Cross Sections, ...
- ...

From Quarks to Nuclei

- Nuclei are complex systems made of interacting protons and neutrons, which in turns are composite objects made of interacting constituent quarks.
- All fundamental forces are at play in nuclei.
- **EFTs** low-energy approximations of QCD whose d.o.f. are bound states of QCD (e.g., protons, neutrons, pions, ...)
- **EFTs** are used to construct many-nucleon interactions and currents



Microscopic (or ab initio) Description of Nuclei

Comprehensive theory that describes quantitatively and predictably nuclear structure and reactions

Requirements:

- Accurate understanding of the interactions/correlations between nucleons in **paris**, **triplets**, ... (two- and three-nucleon forces)
- Accurate understanding of the electroweak interactions of external probes (electrons, neutrinos, photons) with nucleons, correlated nucleon-pairs, ... (one- and two-body electroweak currents)
- **Computational methods** to solve the many-body nuclear problem of strongly interacting particles



Erwin Schrödinger

 $H\Psi = E\Psi$

Many-body Nuclear Problem

Nuclear Many-body Hamiltonian

$$H = T + V = \sum_{i=1}^{A} t_i + \sum_{i < j} v_{ij} + \sum_{i < j < k} V_{ijk} + \dots$$

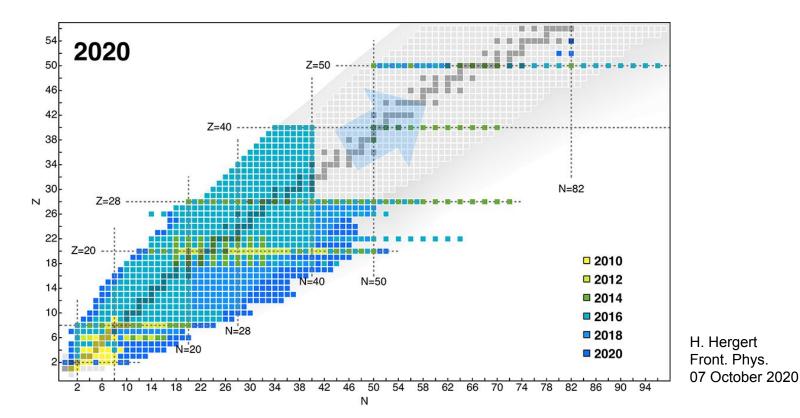
$$\Psi(\mathbf{r}_1,\mathbf{r}_2,...,\mathbf{r}_A,\mathbf{s}_1,\mathbf{s}_2,...,\mathbf{s}_A,\mathbf{t}_1,\mathbf{t}_2,...,\mathbf{t}_A)$$



$$\Psi$$
 are spin-isospin vectors in 3A dimensions with $2^A \times \frac{A!}{Z!(A-Z)!}$ components
⁴He : 96
⁶Li : 1280
⁸Li : 14336
¹²C : 540572

(numerically) exactly or within approximations that are under control the many-body nuclear problem

Current Status

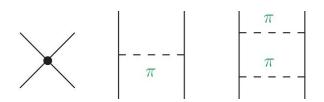


Many-body Nuclear Interactions

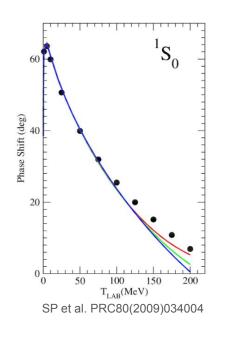
Many-body Nuclear Hamiltonian

$$H = T + V = \sum_{i=1}^{A} t_i + \sum_{i < j} v_{ij} + \sum_{i < j < k} V_{ijk} + \dots$$

 v_{ij} and V_{ijk} are two- and three-nucleon operators based on experimental data fitting; fitted parameters subsume underlying QCD dynamics



Contact term: short-range Two-pion range: intermediate-range $r\propto (2\,m_\pi)^{-1}$ One-pion range: long-range $r\propto m_\pi^{-1}$



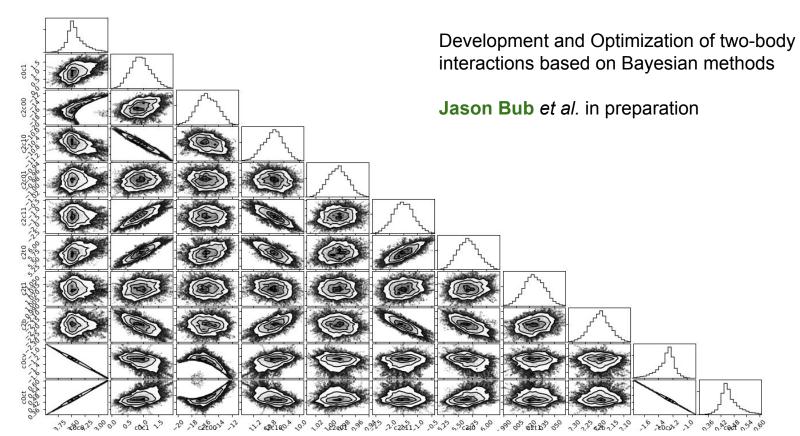


Hideki Yukawa

AV18+UIX; AV18+IL7 Wiringa, Schiavilla, Pieper *et al.*

chiral πNΔ N3LO+N2LO Piarulli *et al.* Norfolk Models

Optimization of Nuclear Two-body Interactions



Quantum Monte Carlo Methods

Minimize the expectation value of the nuclear Hamiltonian: $H = T + v_{ii} + V_{iik}$

$$E_V = \frac{\langle \Psi_V | H | \Psi_V \rangle}{\langle \Psi_V | \Psi_V \rangle} \ge E_V$$

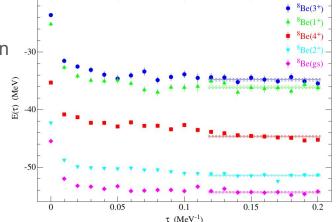
using the trial wave function:

$$|\Psi_V\rangle = \left[\mathcal{S}\prod_{i< j} (1 + U_{ij} + \sum_{k\neq i,j} U_{ijk})\right] \left[\prod_{i< j} f_c(r_{ij})\right] |\Phi_A(JMTT_3)\rangle$$

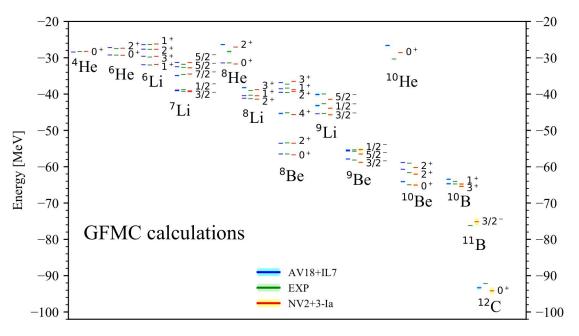
Further improve the trial wave function by eliminating spurious contaminations via a Green's Function Monte Carlo propagation in imaginary time

$$\Psi(\tau) = \exp[-(H - E_0)\tau]\Psi_V = \sum_n \exp[-(E_n - E_0)\tau]a_n\psi_n$$
$$\Psi(\tau \to \infty) = a_0\psi_0$$

Carlson, Wiringa, Pieper et al.

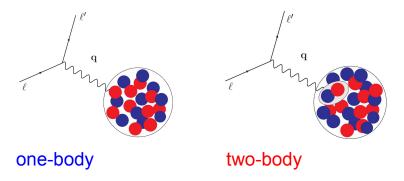


Energies



Piarulli et al. PRL120(2018)052503

Many-body Nuclear Electroweak Currents



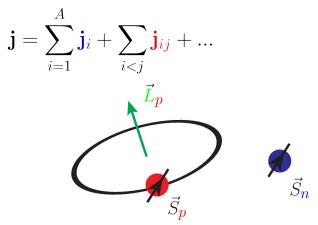
- Two-body currents are a manifestation of two-nucleon correlations
- Electromagnetic two-body currents are required to satisfy current conservation

$$\mathbf{q} \cdot \mathbf{j} = [H, \rho] = [t_i + v_{ij} + V_{ijk}, \rho]$$

Nuclear Charge Operator

$$\rho = \sum_{i=1}^{A} \rho_i + \sum_{i < j} \rho_{ij} + \dots$$

Nuclear (Vector) Current Operator



Magnetic Moment: Single Particle Picture

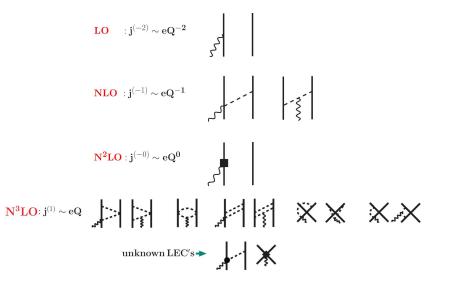
Many-body Currents

• Meson Exchange Currents (MEC)

Constrain the MEC current operators by imposing that the current conservation relation is satisfied with the given two-body potential

Chiral Effective Field Theory Currents

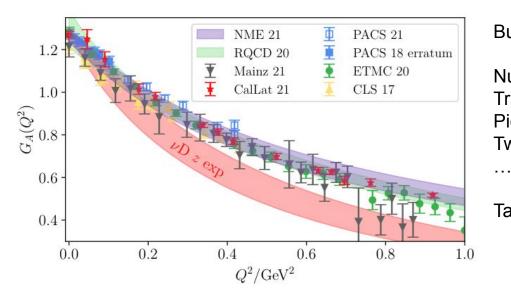
Are constructed consistently with the two-body chiral potential; Unknown parameters, or Low Energy Constants (LECs), need to be determined by either fits to experimental data or by Lattice QCD calculations



Electromagnetic Current Operator

SP *et al.* PRC78(2008)064002, PRC80(2009)034004, PRC84(2011)024001, PRC87(2013)014006 Park *et al.* NPA596(1996)515, Phillips (2005) Kölling *et al.* PRC80(2009)045502 & PRC84(2011)054008

LCQD inputs for neutrino-nucleus scattering



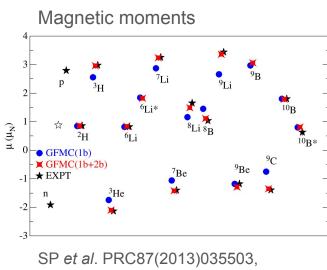
Snowmass WP: Theoretical tools for neutrino scattering: interplay between lattice QCD, EFTs, nuclear physics, phenomenology, and neutrino event generators; arXiv:2203.09030

Building blocks of ab initio nuclear approaches:

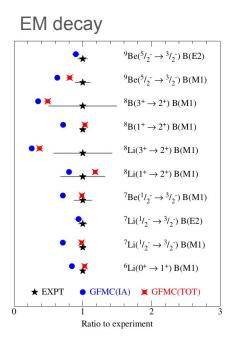
Nucleonic form factors Transition form factors Pion production amplitudes Two-nucleon couplings (strong and EW)

Taken from data where available, or from theory

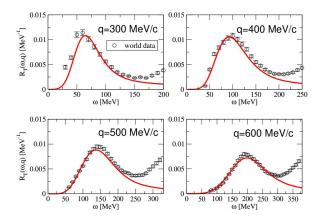
Electromagnetic Observables



PRC101(2020)044612



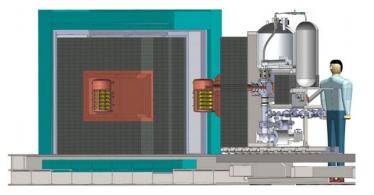
e-⁴He particle scattering



Nuclear Physics for Neutrinoless Double Beta Programs



EXO-200 Collaboration

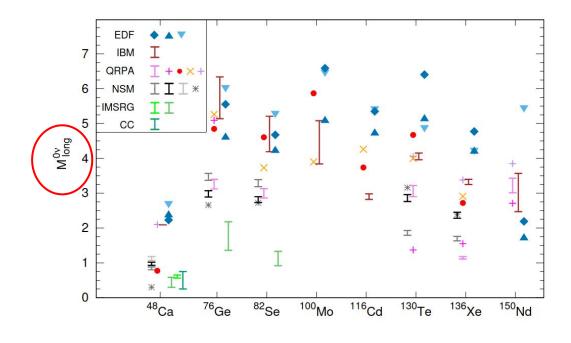


Majorana Demonstrator

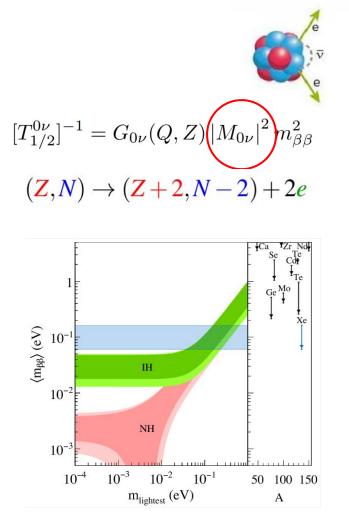
Neutrinoless double beta decay half-life $T_{1/2} \gtrsim 10^{25}$ years (age of the universe 1.4 x 10^{10} years) 1 ton of material is required to see few events per year

Decay Rate \propto (nuclear matrix element)² x (m_{BB})²

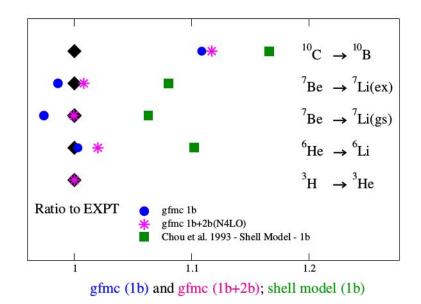
Neutrinoless Double Beta Decay



Agostini, Menendez et al, arXiv:2202.01787 (2022)



Beta decay



SP et al. PRC97(2018)022501

Beta Decay and Electron Capture in Light Nuclei

0.96 1 1.04	0.96 1 1.04	0.96 1 1.04	0.96 1 1.04
³ H β-decay	⁶ He β-decay	⁷ Be ε -cap(gs)	⁷ Be ε -cap(ex)
0	()	0.	0
⁸ Li β-decay	⁸ B β-decay	⁸ He β-decay	¹⁰ C β-decay
0 •	0•	0	••
■ NV2+3-Ia NV2+3-Ia* NV2+3-Ia* NV18+IL7			
0.4 0.6 0.8 1	0.4 0.6 0.8 1	0.4 0.6 0.8 1	1 1.1

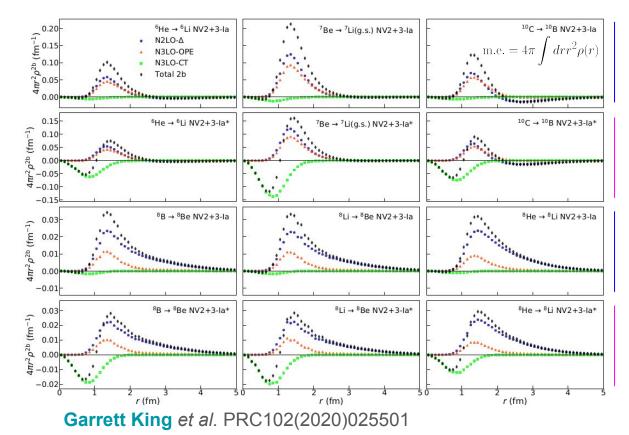
Garrett King et al. PRC102(2020)025501

Calculations based on

- chiral interactions and currents NV2+3-la Norfolk unstarred NV2+3-la* Norfolk* starred Piarulli *et al.* PRL120(2018)052503 Baroni *et al.* PRC98(2018)044003
- phenomenological AV18+IL7 potential and chiral axial currents (hybrid calculation)

Two-body currents are small/negligible; Results for A=6-7 are within 2% of data; Results for A=8 are off by a 30-40%; Results for A=10 are affected by the second J^{π} =(1⁺) state in ¹⁰B

Axial Two-body Transition Density



NV2+3-la; NV2+3-la*

enhanced contribution from contact current in the starred model gives rise to nodes in the two-body transition density

Two-body axial currents

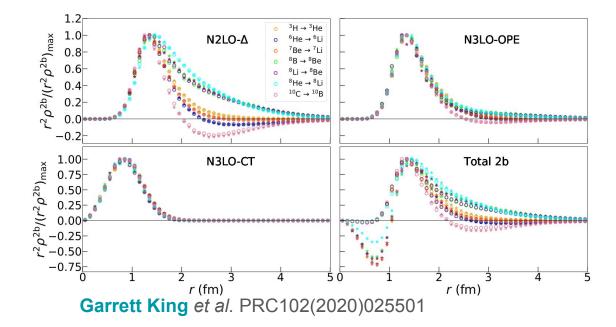


long-range at N2LO and N3LO



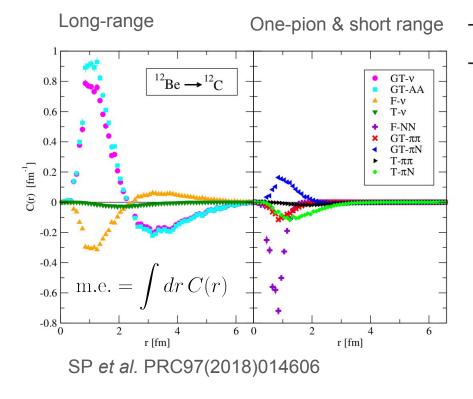
contact current at N3LO

Scaling & Universality of Short-Range Dynamics



NV2+3-Ia empty circles; NV2+3-Ia* stars Different colors refer to different transitions

Neutrinoless Double Beta Decay Matrix Elements

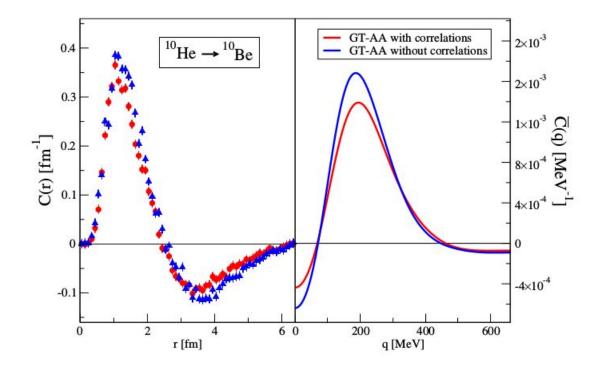


 ν π $\pi\pi$ NN

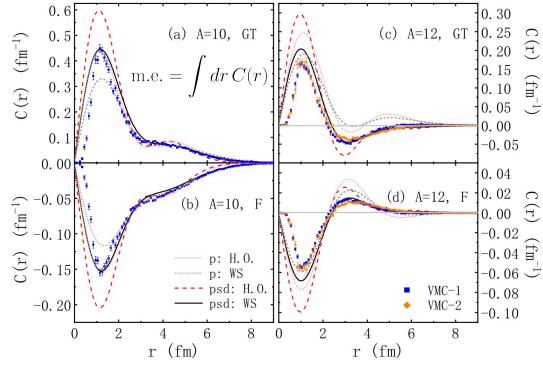
Cirigliano Dekens DeVries Graesser Mereghetti *et al.* PLB769(2017)460, JHEP12(2017)082, PRC97(2018)065501

- Leading operators in neutrinoless double beta decay are two-body operators
- These observables are particularly sensitive to short-range and two-body physics
- Transition densities calculated in momentum space indicate that the momentum transfer in this process is of the order of q ~ 200 MeV

Correlations in neutrinoless double beta decay ME



Comparison with Shell-Model Calculations



X. Wang et al. PLB798(2019)134974

Closer agreement between Shell-Model calculations with Variational Monte Carlo results is reached by

- Increasing the size of the model space
- Wood-Saxon single particle wave functions are superion in describing the tails of the densities wrt harmonic oscillator wave functions
- Phenomenological Short-Range-Correlations functions further improve the agreement

Partial muon capture rates: VMC calculations

$\Gamma_{VMC}(avg.) = 1495 \text{ s}^{-1} \pm 19 \text{ s}^{-1}$ $\Gamma_{expt} = 1496.0 \text{ s}^{-1} \pm 4.0 \text{ s}^{-1}$

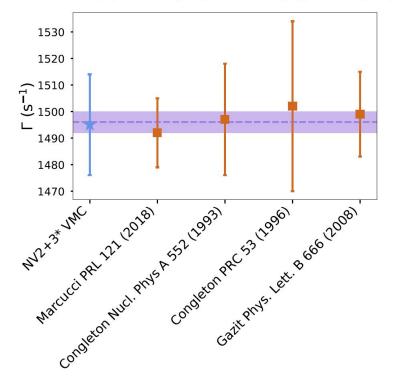
Ackerbauer et al. PLB417, 224(1998)

Momentum transfer q~ 100 MeV

Two-body correction is \sim 8% of total rate on average for A=3

Garrett King et al. PRC2022

 ${}^{3}\text{He}(1/2^{+};1/2) \rightarrow {}^{3}\text{H}(1/2^{+};1/2)$



Partial muon capture rates: VMC calculations

$$\Gamma_{VMC}(avg.) = 1235 \text{ s}^{-1} \pm 101 \text{ s}^{-1}$$

$$\Gamma_{GFMC}(IIa^*) = 1171 \text{ s}^{-1} \pm 164 \text{ s}^{-1}$$

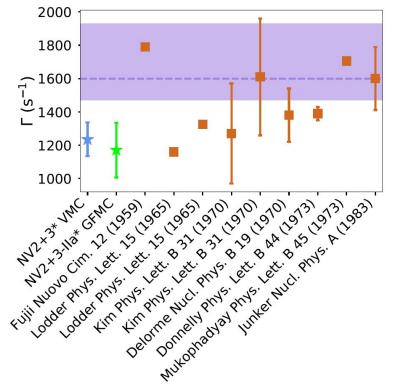
$$\Gamma_{expt} = 1600 \text{ s}^{-1} + 330/-129 \text{ s}^{-1}$$

Deutsch *et al.* PLB26(1968)315

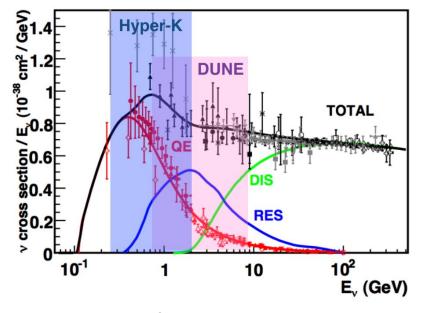
Garrett King et al. PRC2022

Outlook at FRIB: extraction of the Gamow-Teller strength A=11, A=12

$${}^{6}\mathrm{Li}(1^{+};0) \rightarrow {}^{6}\mathrm{He}(0^{+};1)$$



Neutrino cross section anatomy



Formaggio & Zeller

Quasi-elastic: dominated by single-nucleon knockout

Resonance: excitation to nucleonic resonant states which decay into mesons

Deep-inelastic scattering: where the neutrino resolves the nucleonic quark content

Each of these regimes requires knowledge of both the **nuclear ground state** and the **electroweak coupling** and **propagation of the struck nucleons, hadrons, or partons**

A challenge for achieving precise neutrino-nucleus cross-section is **reliably bridging the transition regions which use different degrees of freedom**

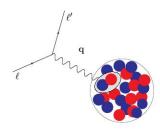
Lepton-Nucleus scattering: Inclusive Processes

Electromagnetic Nuclear Response Functions

$$R_{\alpha}(q,\omega) = \sum_{f} \delta\left(\omega + E_0 - E_f\right) |\langle f|O_{\alpha}(\mathbf{q})|0\rangle|^2$$

Longitudinal response induced by the charge operator $O_L = \rho$ Transverse response induced by the current operator $O_T = j$ 5 Responses in neutrino-nucleus scattering

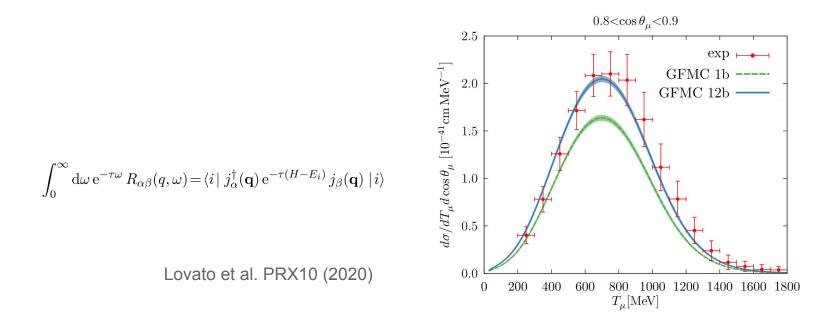
$$\frac{d^2 \sigma}{d \,\omega d \,\Omega} = \sigma_M \left[v_L \, R_L(\mathbf{q}, \omega) + v_T \, R_T(\mathbf{q}, \omega) \right]$$



For a recent review on QMC, SF methods see Rocco Front. In Phys.8 (2020)116

Inclusive Cross Sections with Integral Transforms

Exploit integral properties of the response functions and closure to avoid explicit calculation of the final states (Lorentz Integral Transform **LIT**, **Euclidean**, ...)

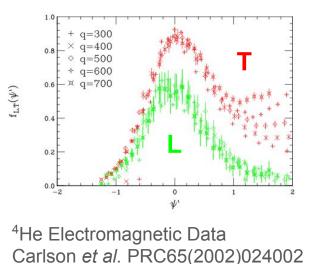


Lepton-Nucleus scattering: Data

5

Transverse Sum Rule

 $S_T(q) \propto \langle 0 | \mathbf{j}^{\dagger} \mathbf{j} | 0 \rangle \propto \langle 0 | \mathbf{j}_{1b}^{\dagger} \mathbf{j}_{1b} | 0 \rangle + \langle 0 | \mathbf{j}_{1b}^{\dagger} \mathbf{j}_{2b} | 0 \rangle + \dots$



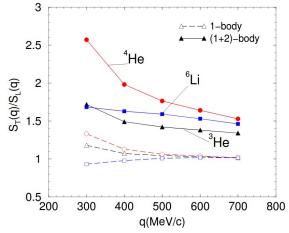
Observed transverse enhancement explained by the combined effect of two-body correlations and currents in the interference term

$$\langle \mathbf{j}_{1b}^{\dagger} \ \mathbf{j}_{1b} \rangle > 0$$

Leading one-body term

$$\langle \mathbf{j}_{1b}^{\dagger} \; \mathbf{j}_{2b} \; v_{\pi} \rangle \propto \langle v_{\pi}^2 \rangle > 0$$

Interference term

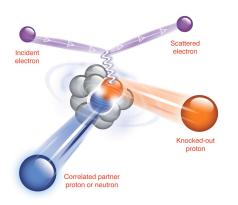


Transverse/Longitudinal Sum Rule Carlson *et al.* PRC65(2002)024002

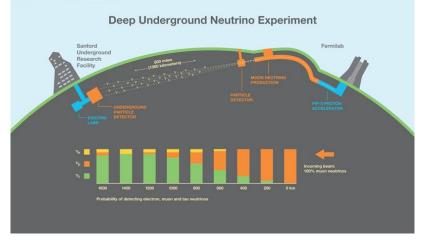
Beyond Inclusive: Short-Time-Approximation

Short-Time-Approximation Goals:

- Describe electroweak scattering from
 A > 12 without losing two-body physics
- Account for exclusive processes
- Incorporate relativistic effects



Subedi et al. Science320(2008)1475



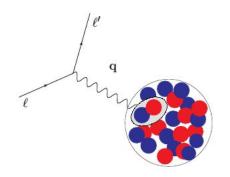
Stanford Lab article



Short-Time-Approximation

Short-Time-Approximation:

- Based on Factorization
- Retain two-body physics
- Correctly accounts for interference



$$R(q,\boldsymbol{\omega}) = \int_{-\infty}^{\infty} \frac{dt}{2\pi} e^{i(\boldsymbol{\omega}+E_0)t} \langle 0|O^{\dagger} e^{-iHt} O|0\rangle$$

$$O_i^{\dagger} e^{-iHt} O_i + O_i^{\dagger} e^{-iHt} O_j + O_i^{\dagger} e^{-iHt} O_{ij} + O_{ij}^{\dagger} e^{-iHt} O_{ij}$$

$$H \sim \sum_i t_i + \sum_{i < j} v_{ij}$$

Factorization Schemes

Short-Time-Approximation:

- Based on Factorization
- Retains two-body physics
- Response functions are given by the scattering from pairs of fully interacting nucleons that propagate into a correlated pair of nucleons
- Allows to retain both two-body correlations and currents at the vertex
- Provides "more" exclusive information in terms of nucleon-pair kinematics via the Response Densities

Response Functions ∝ Cross Sections

$$R_{\alpha}(q,\omega) = \sum_{f} \delta\left(\omega + E_0 - E_f\right) |\langle f|O_{\alpha}(\mathbf{q})|0\rangle|^2$$

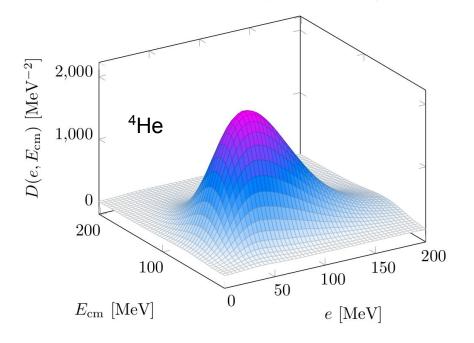
Response *Densities*

$$R(q,\omega) \sim \int \delta \left(\omega + E_0 - E_f\right) dP' dp' \mathcal{D}(p',P';q)$$

P' and *p*' are the CM and relative momenta of the struck nucleon pair

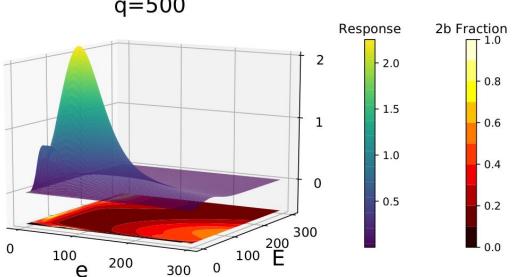
Transverse Response Density: *e*-⁴He scattering

Transverse Density q = 500 MeV/c



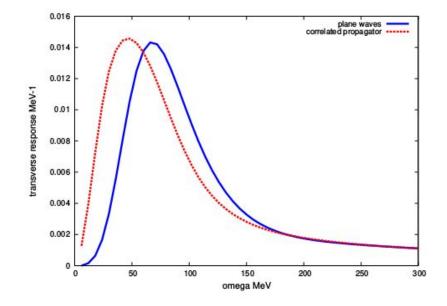
SP et al. PRC101(2020)044612

Transverse Response Density: two-body physics



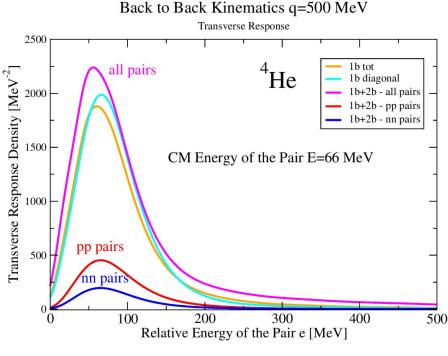
q=500

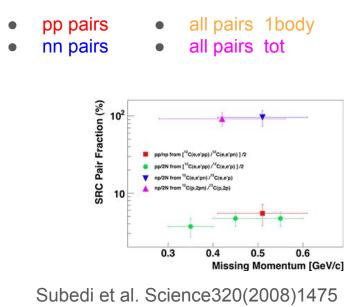
Correlated pairs vs uncorrelated pairs



Scattering from uncorrelated vs correlated nucleon pairs

e-⁴He scattering in the back-to-back kinematic

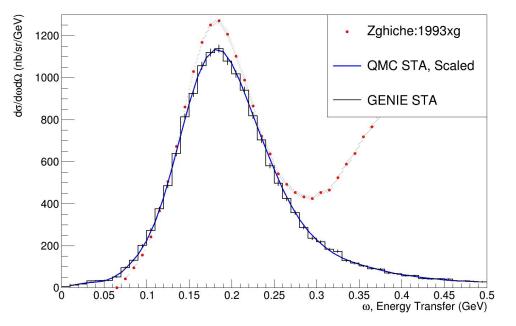




SP et al. PRC101(2020)044612

GENIE validation using e-scattering

Z = 2, A = 4, Beam Energy = 0.64 GeV, Angle = $60^{\circ} \pm 0.25^{\circ}$

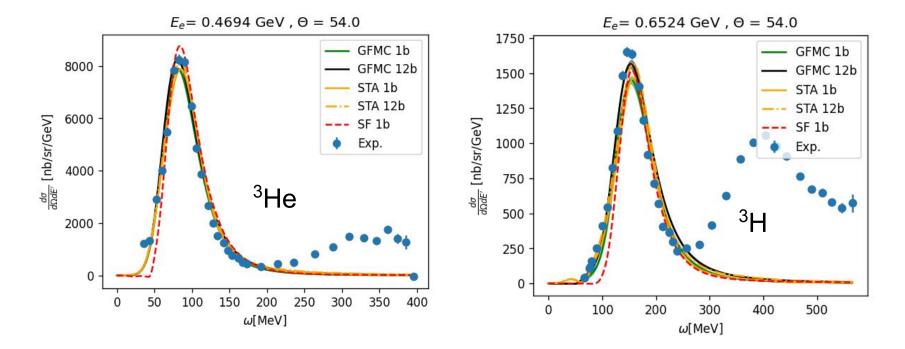


Barrow Gardiner Betancourt SP et al. PRD 103 (2021) 5, 052001 Ongoing work

- Implementation of moment-morphin interpolation techniques
- Implementations of response Densities in GENIE
- ¹²C response densities with Lorenzo Andreoli

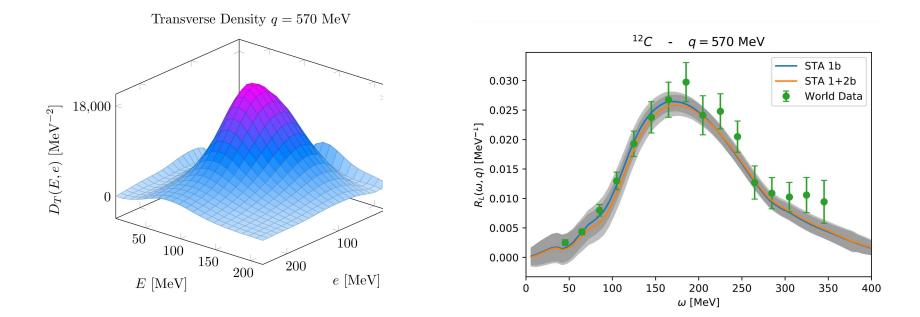
$$\frac{d^2 \sigma}{d \,\omega d \,\Omega} = \sigma_M \left[v_L \, R_L(\mathbf{q}, \omega) + v_T \, R_T(\mathbf{q}, \omega) \right]$$

GFMC SF STA: Benchmark & error estimate



Andreoli, Rocco et al. submitted to PRC

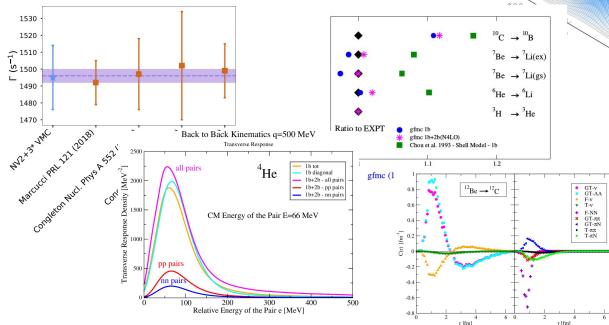
STA for Carbon 12: Preliminary results



Lorenzo Andreoli et al. in preparation

Summary

Ab initio calculations of light nuclei yield a picture of nuclear structure and dynamics where many-body effects play an essential role to explain available data.



200150100 500 $e \, [MeV]$ Close collaborations between NP, LQCD, Pheno, Hep, Comp, Expt, ... are required to progress e.g., NP is represented in the Snowmass process

Transverse Density q = 500 MeV/c

2,000

1.000

It's a very exciting time!

Collaborators

WashU: Andreoli Bub King Piarulli

LANL: Baroni Carlson Cirigliano Gandolfi Hayes Mereghetti JLab+ODU: Schiavilla ANL: Lovato Rocco Wiringa UCSD/UW: Dekens Pisa U/INFN: Kievsky Marcucci Viviani Salento U: Girlanda Huzhou U: Dong Wang Fermilab: Gardiner Betancourt MIT: Barrow





Theory Alliance facility for rare isotope beams

















