



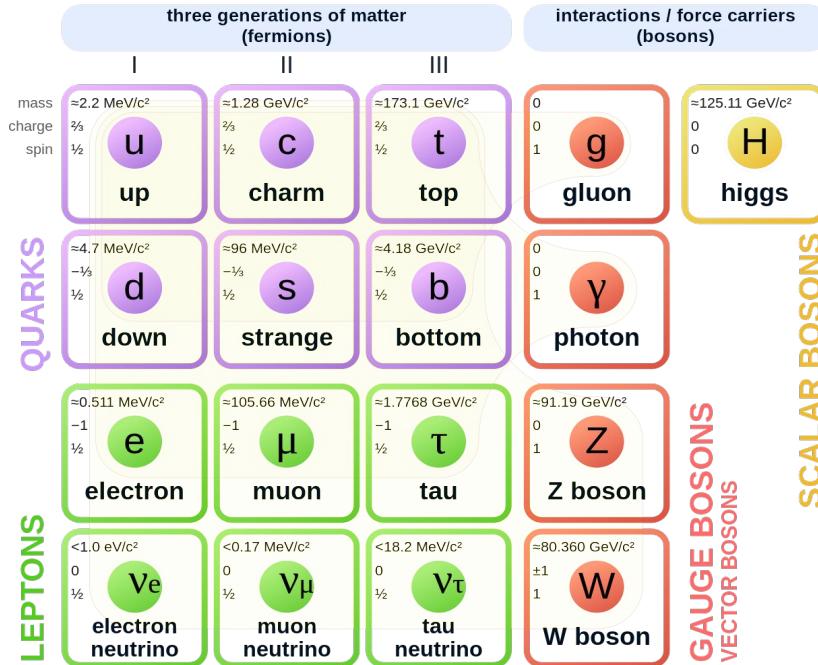
Low-energy nuclear physics for fundamental science

Garrett King

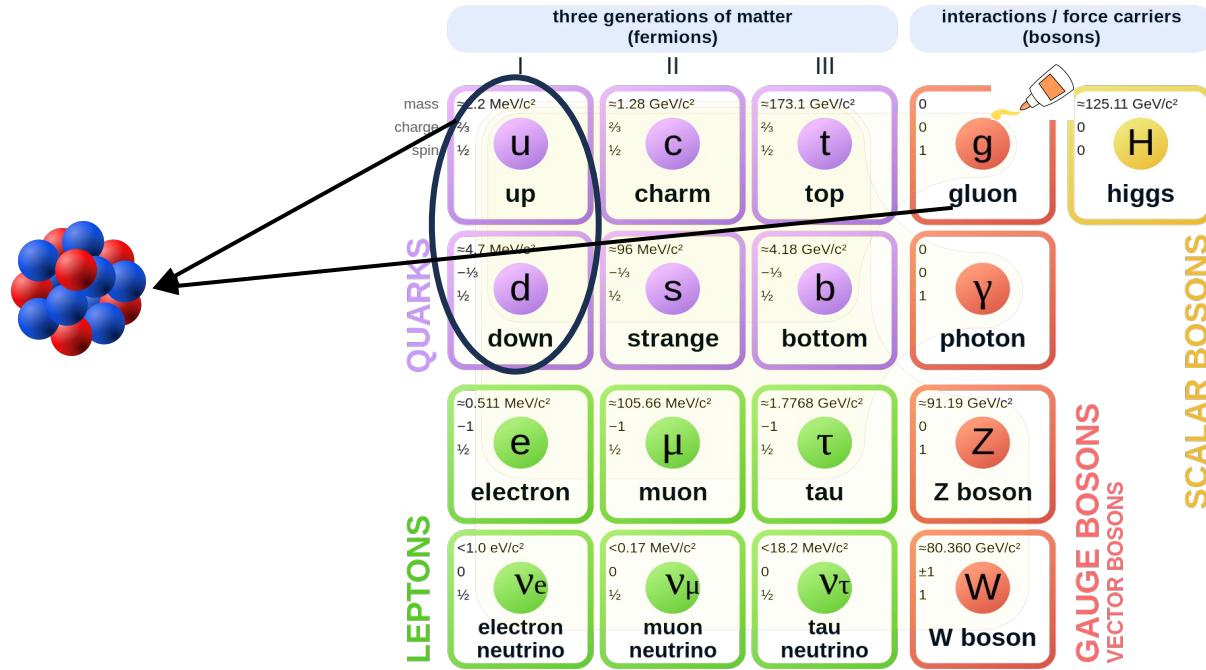
Dehmelt Seminar
University of Washington
1/8/2026

LA-UR-25-32298

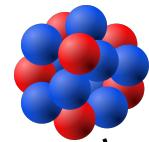
The Standard Model



The Standard Model

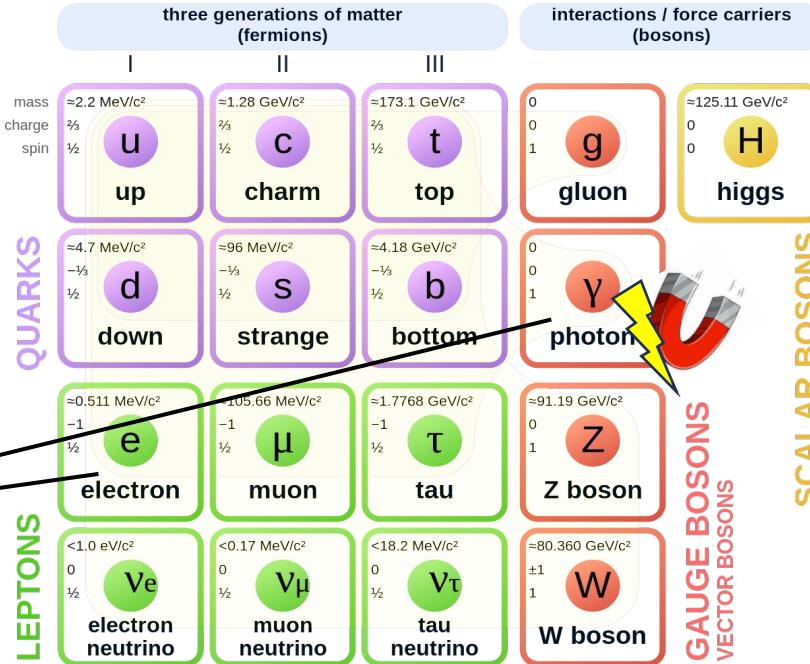


The Standard Model

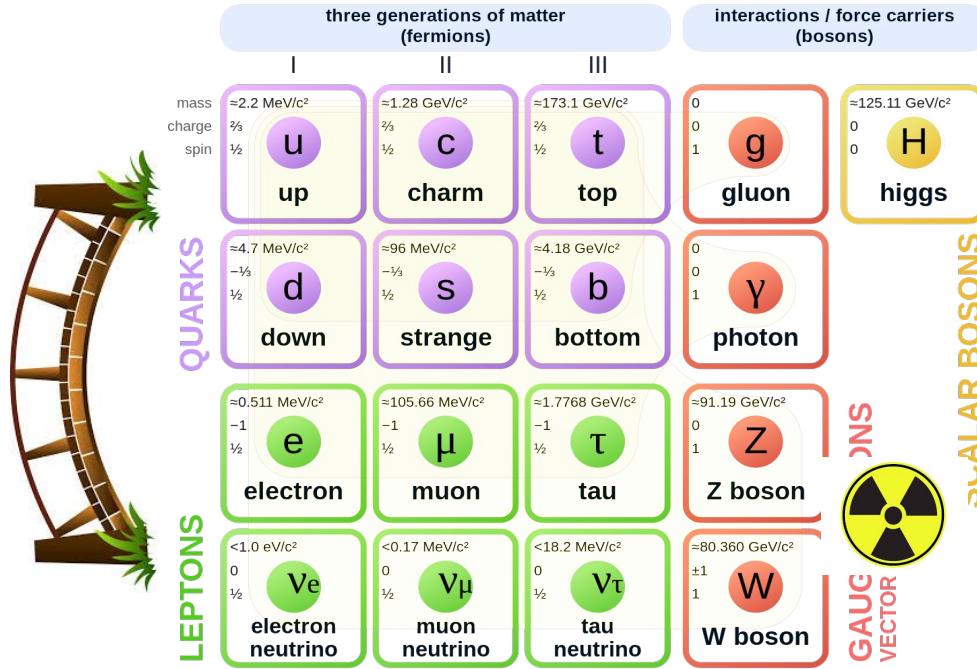


Group	Period	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
	1	H																	
2	2	He	Li	B															
3	3		Be																
4	4																		
5	5																		
6	6																		
7	7																		

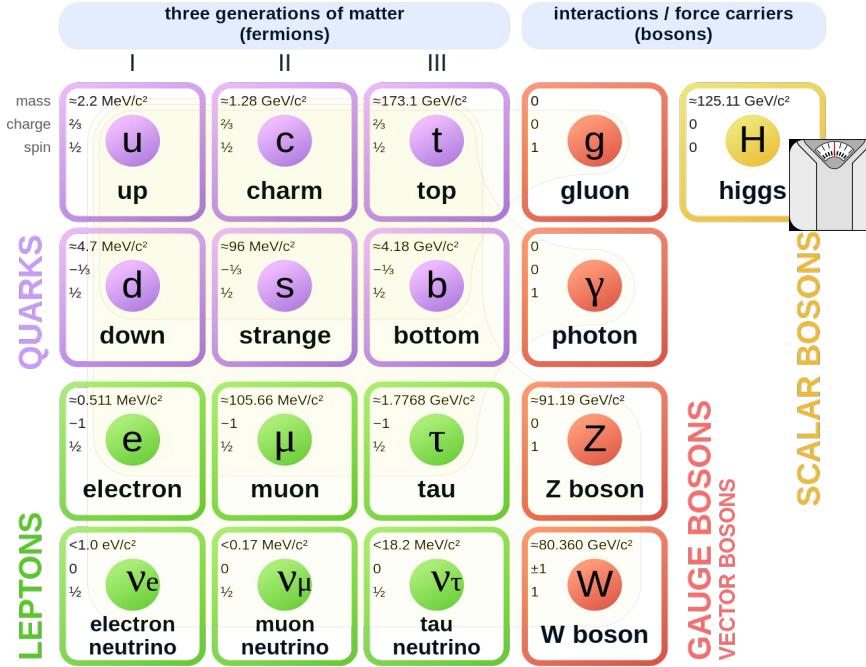
Periodic Table of Elements showing groups and periods. The first column (H) is Group 1, the second (He) is Group 2, and so on. The first period (H) is Period 1, the second (He) is Period 2, and so on.



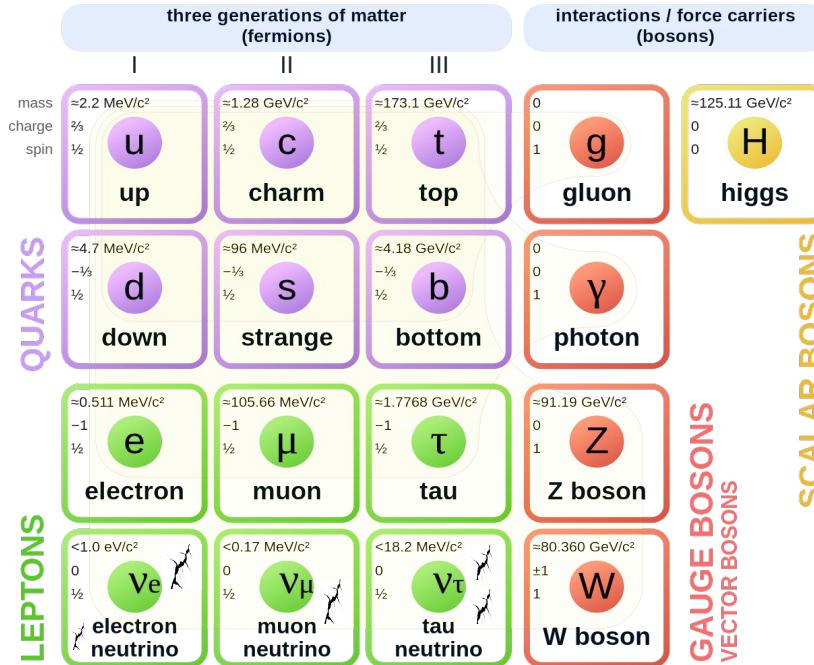
The Standard Model



The Standard Model



The Standard Model



Neutrino oscillations



Fermilab / Sandbox Studio, Chicago

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

↑
Flavors

↑
Mass

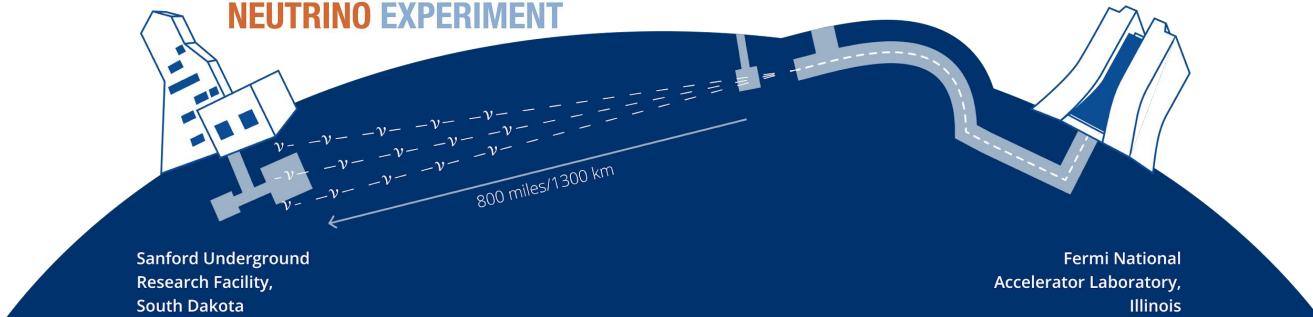
Neutrino searches



Fermilab / Sandbox Studio, Chicago

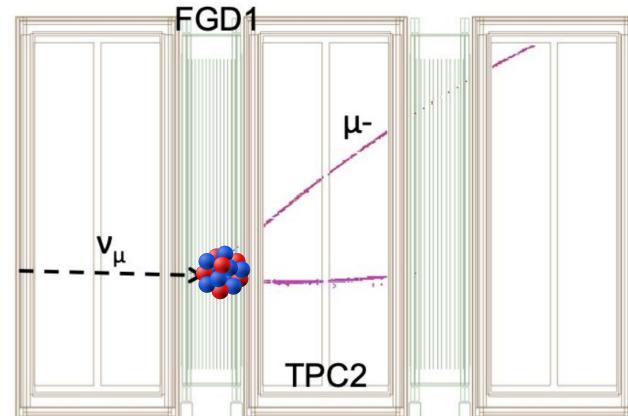


DEEP UNDERGROUND
NEUTRINO EXPERIMENT



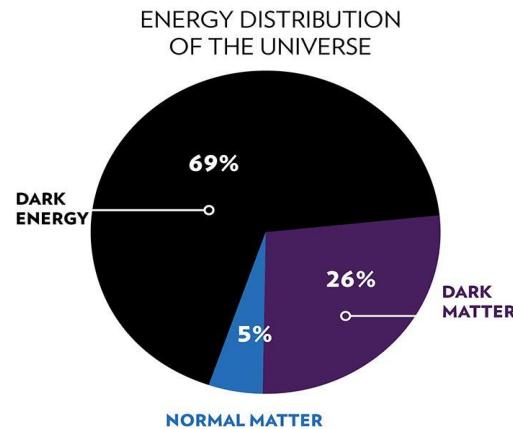
Sanford Underground
Research Facility,
South Dakota

Fermi National
Accelerator Laboratory,
Illinois

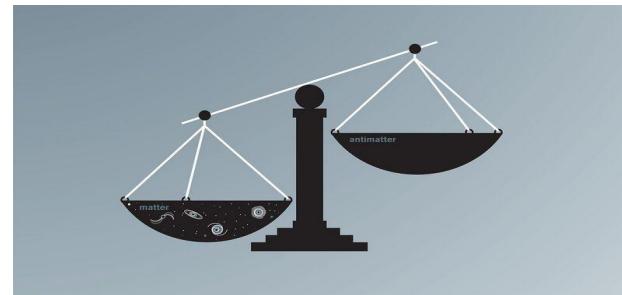


Adapted from K. Mahn,
“The Theoretical Cross Section Needs of Future Long Baseline Experiments”
at INT WORKSHOP INT-23-86W

Why beyond Standard Model (BSM) physics?

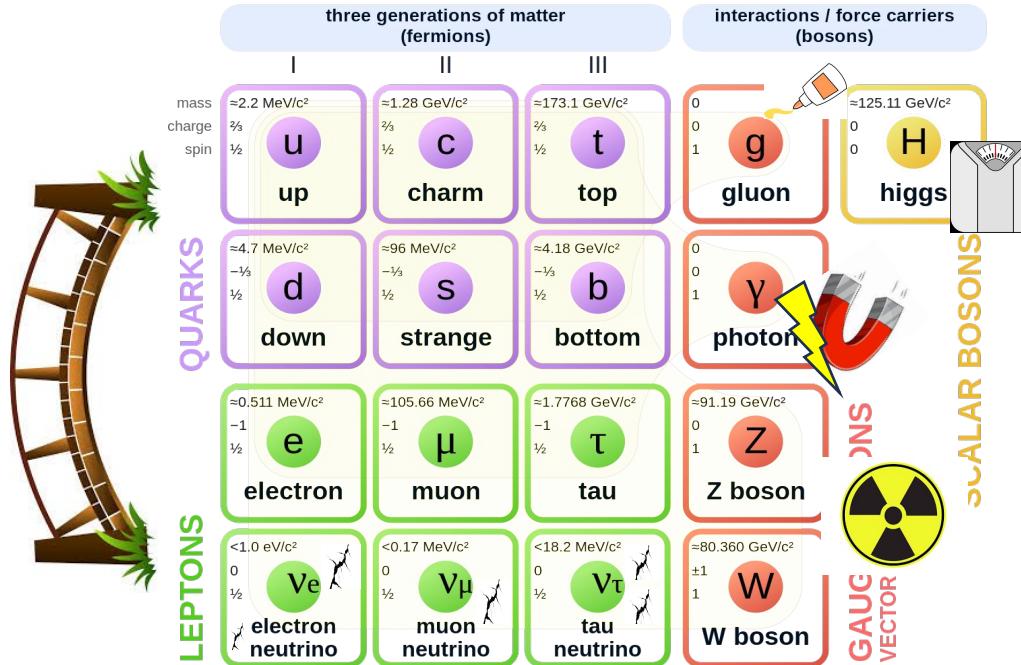


NASA / Chandra X-ray Center/ K. Divona

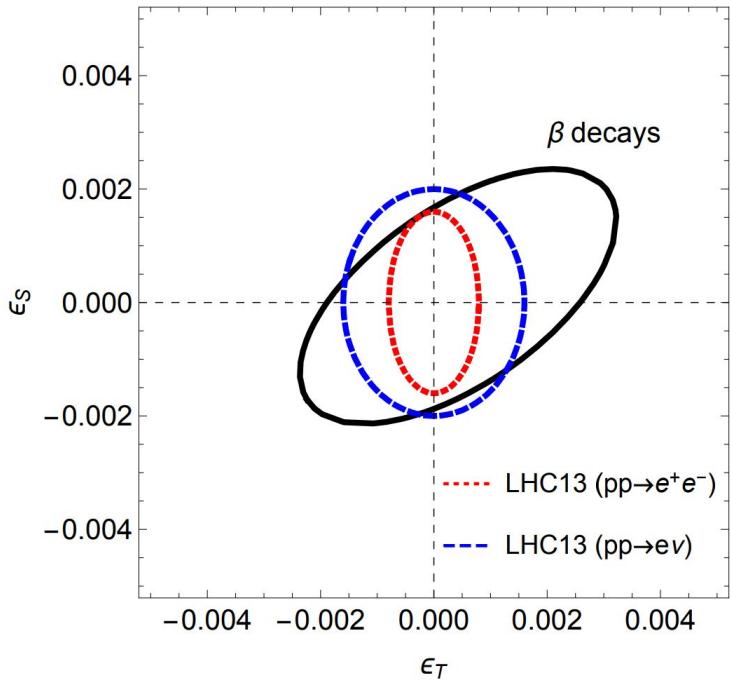


Symmetry Magazine / Sandbox Studio, Chicago

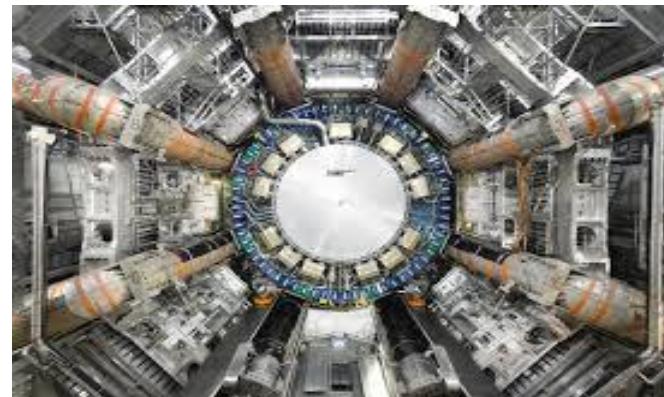
Nuclei as laboratories for new physics



New physics impact of nuclear β -decays

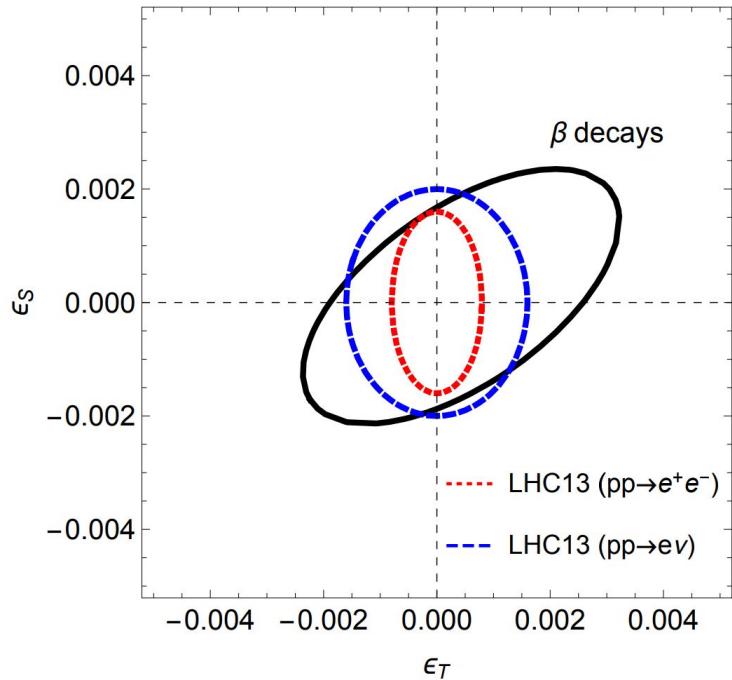


Competitive bounds on BSM currents that complement high-energy searches



Falkowski et al, JHEP04 (2021) 126

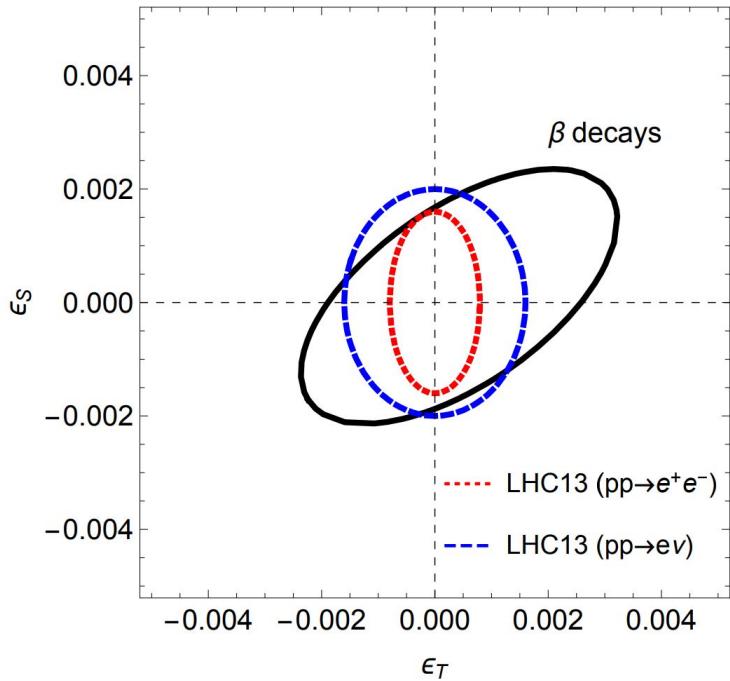
New physics impact of nuclear β -decays



Question: How reliable are the estimates of nuclear uncertainties?

Falkowski et al, JHEP04 (2021) 126

New physics impact of nuclear β -decays



Question: How reliable are the estimates of nuclear uncertainties?

To answer, we need *precise and accurate* calculations of nuclear observables

Falkowski et al, JHEP04 (2021) 126

Understanding structure and dynamics

Validate on available data



Predict relevant quantities

Understanding structure and dynamics

Validate on available data



Predict relevant quantities

Decay rates, magnetic moment



Precision decays, moments

Electron scattering



Neutrino scattering

Understanding structure and dynamics

Validate on available data



Predict relevant quantities

Decay rates, magnetic moment



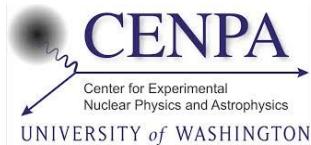
Precision decays, moments

Electron scattering



Neutrino scattering

Connection to nuclear science



FRIB



GANIL

GSI

ISOLDE

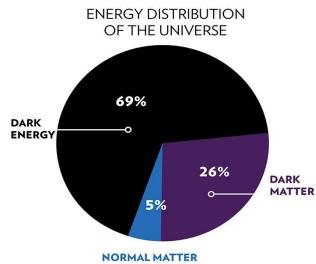
TRIUMF

To benefit new physics searches, we must understand...

- How structure changes near the limit of stability
- What role clustering plays in exotic systems
- The nature of the nuclear force
- How nuclei interact with external probes

Strong global capabilities to validate models of nuclear structure used for BSM predictions

Bridging new physics and nuclear science



Nuclear Theory



Microscopic description of the nucleus

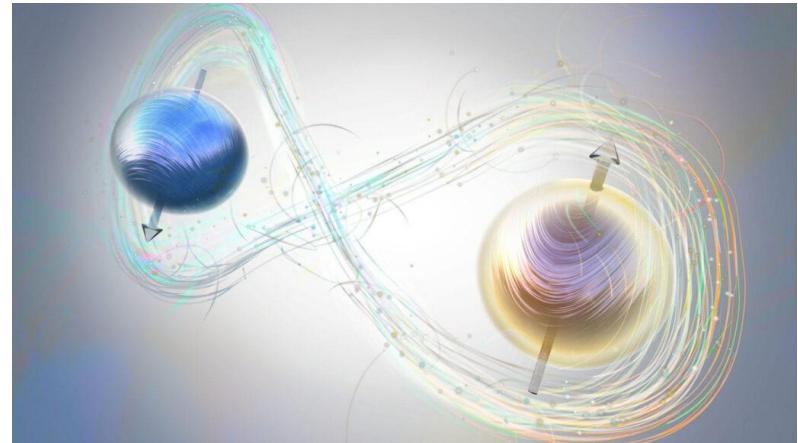


The quantum many-body problem

Interaction generates *entanglement* in solution of the Schrödinger equation

$$H|\Psi\rangle = E|\Psi\rangle$$

Goal: Model the nucleus in terms of interacting proton and neutron (nucleon) degrees of freedom



The quantum many-body problem

Wave function of A nucleons containing information about *coordinates, spins, and isospins*

$$\Psi(r_1, r_2, \dots, r_A; s_1, s_2, \dots, s_A; t_1, t_2, \dots, t_A)$$

$$\dim(\Psi) = 3A \times 2^A \times \frac{A!}{N!Z!}$$

$$\dim(^4\text{He}) = 1152$$

$$\dim(^6\text{Li}) \approx 2.3 \times 10^4$$

$$\dim(^{12}\text{C}) \approx 1.4 \times 10^8$$



NERSC



ALCF



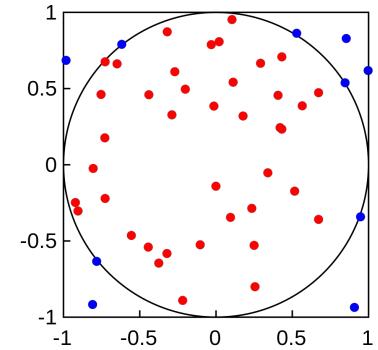
LANL IC

Quantum Monte Carlo (QMC) methods

Stochastic approaches to solve the Schrödinger Equation

Allows you to solve large-dimensional integrals via random sampling

In this talk: **Variational and Green's function**
(or Diffusion) Monte Carlo



MC Example: Estimating π

100 samples = 3.28000
(4.4%)

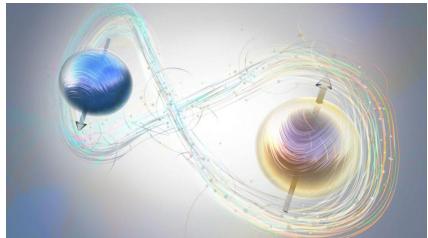
1,000 samples = 3.16400
(0.71%)

1,000,000 samples =
3.14216 (0.02%)

```
1 import numpy as np
2
3 exact = 4.*np.arctan(1.)
4
5 nsamp = 10**2
6
7 accepted = 0
8
9 for i in range(nsamp):
10
11     x,y = np.random.rand(2)
12     if ( (x**2. + y**2.) < 1. ):
13         accepted += 1
14
15 area = 4.* (accepted/nsamp)
16
17 acc = 100.*np.abs(area-exact)/exact
18
19 print("pi = %.8f" % area )
20 print("accuracy = %.8f %%" % acc)
```

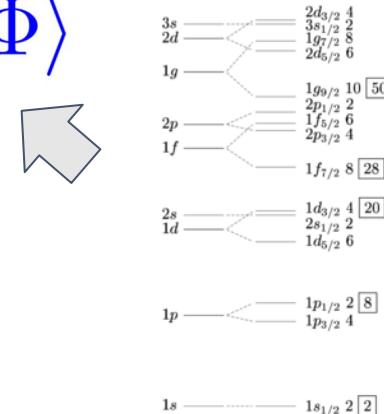
Variational Monte Carlo for correlated Fermions

$$|\Psi_T\rangle = \hat{F}(\{\mathbf{r}_i\}, \{\mathbf{s}_i\}, \{\mathbf{t}_i\}) |\Phi\rangle$$



Encodes entanglement between nucleons

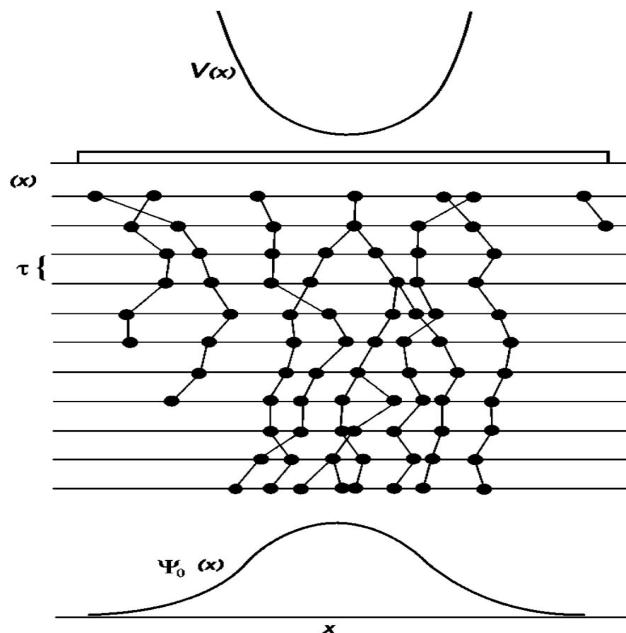
Contains the variational parameters



Mean-field description

Encodes long-range structure, quantum numbers

Green's Function (or Diffusion) Monte Carlo



Can recast the Schrödinger Equation as a Diffusion equation

Sample the path integral with Monte Carlo

$$\lim_{\tau \rightarrow \infty} |\Psi_T\rangle \rightarrow c_0 \psi_0$$

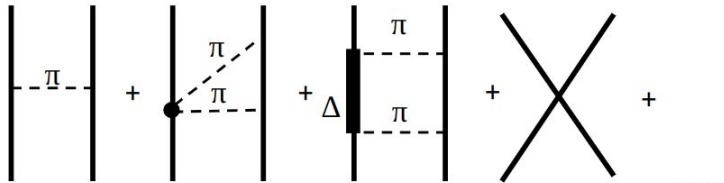
Non-perturbative approach to obtain exact solution

Nuclear interactions

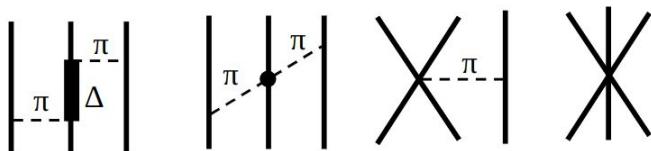
$$H = \sum_i T_i + \sum_{ij} v_{ij} + \sum_{ijk} V_{ijk} + \dots$$

Contains **kinetic energies**, plus **two-body** and **three-body** interactions

Long-range attraction mediated by the lightest meson, the pion (π)



Intermediate range attraction involving two pions, and sometimes excitation of nucleons (ex: the Δ)



Short-range repulsion from heavier intermediaries represented by “contact” terms

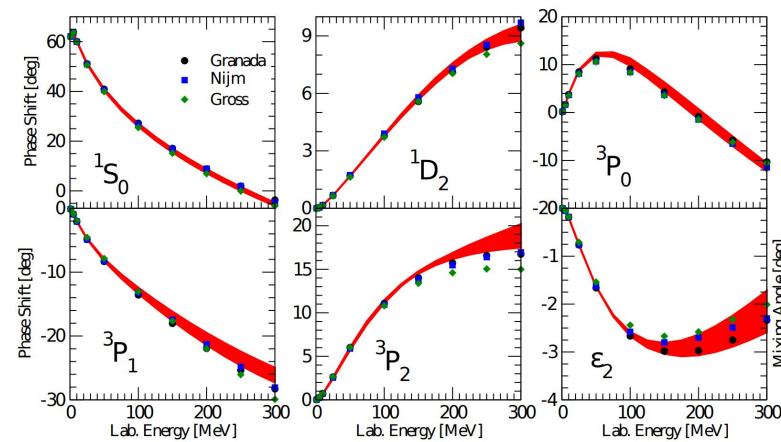
Need for three-body forces to bind light systems

Systematic uncertainty

Interaction between nucleons is not fundamental

Phenomenological models available that must fit to data, but have uncertainties

Systematic expansions as effective theory of fundamental theory exist, but work remains to study convergence



Piarulli et al. PRC 91, 024003 (2014)

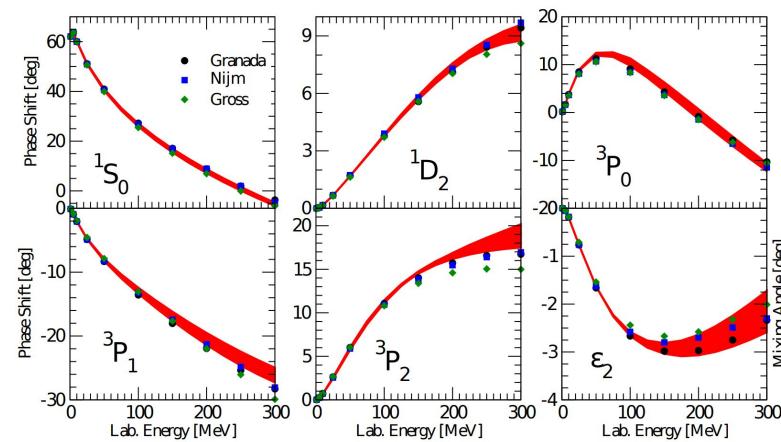
Systematic uncertainty

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Phenomenological models available that must fit to data, but have uncertainties

Systematic expansions as effective theory of fundamental theory exist, but work remains to study convergence

This systematic has to be accounted for in calculations



Piarulli et al. PRC 91, 024003 (2014)

Nuclear matrix elements

Use QMC to compute

$$M = \langle \Psi_\beta | \mathcal{O} | \Psi_\alpha \rangle$$

Related to physics quantities of interest

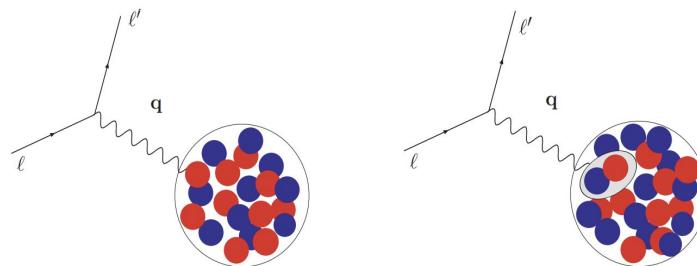
$$|M|^2 \propto \Gamma, \tau_{1/2}^{-1}, d\sigma/d\Omega, \dots$$

Electroweak charge and current operators

Schematically:

$$\rho = \sum_{i=1}^A \rho_i + \sum_{i < j} \rho_{ij} + \dots$$
$$\mathbf{j} = \sum_{i=1}^A \mathbf{j}_i + \sum_{i < j} \mathbf{j}_{ij} + \dots$$

External field interacts with **single nucleons** and **correlated pairs** of nucleons

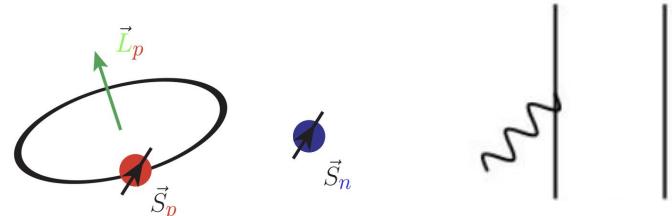


Pastore et al. PRC 80, 034004 (2009), Pastore et al. PRC 84, 024001 (2011), Piarulli et al. PRC 87, 014006 (2013), Schiavilla et al. PRC 99, 034005 (2019), Baroni et al. PRC 93, 049902 (2016), ...

Two-body currents intuition (magnetic moments)

We know that it will arise from charges moving in the system

Expect proton orbital, proton spin, and neutron spin contributions



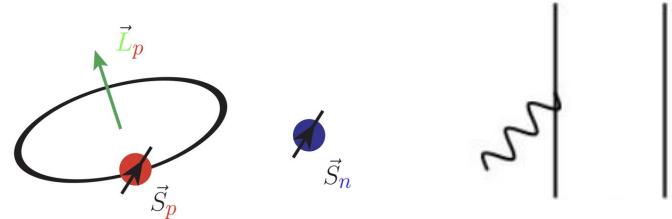
Two-body currents intuition (magnetic moments)

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Expect proton orbital, proton spin, and neutron spin contributions

Protons are not the only charged objects (pions, Δ 's, heavier mesons,...)

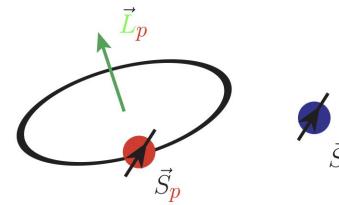
Ex: Pion couplings to an external electromagnetic field



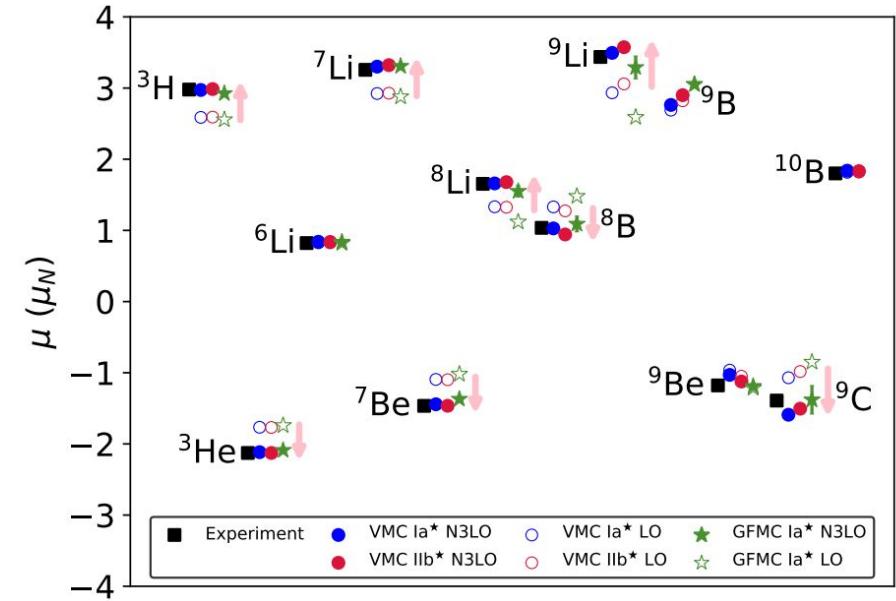
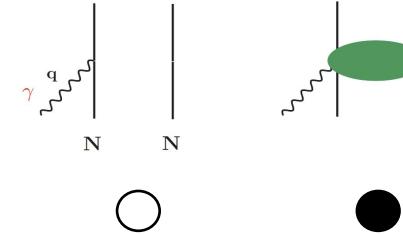
Magnetic moments

One-body picture:

$$\mu^{LO} = \sum_i (\vec{L}_{i,z} + g_p \vec{S}_{i,z}) \frac{1 + \tau_{3,i}}{2} + g_n \vec{S}_{i,z} \frac{1 - \tau_{3,i}}{2}$$

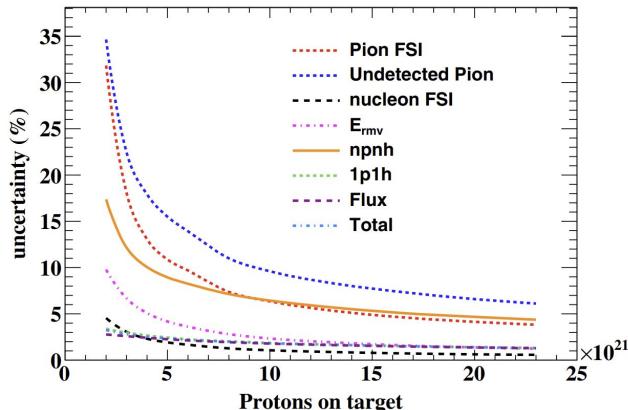


Two-body currents can play a large role (up to $\sim 33\%$) in describing magnetic dipole moments



Chambers-Wall, King, et al. PRL 133, 212501 (2024)
 Chambers-Wall, King, et al. PRC 110, 054316 (2024)

Importance of two-body physics for neutrino physics



Dolan et al. PRD 105, 032010 (2022)

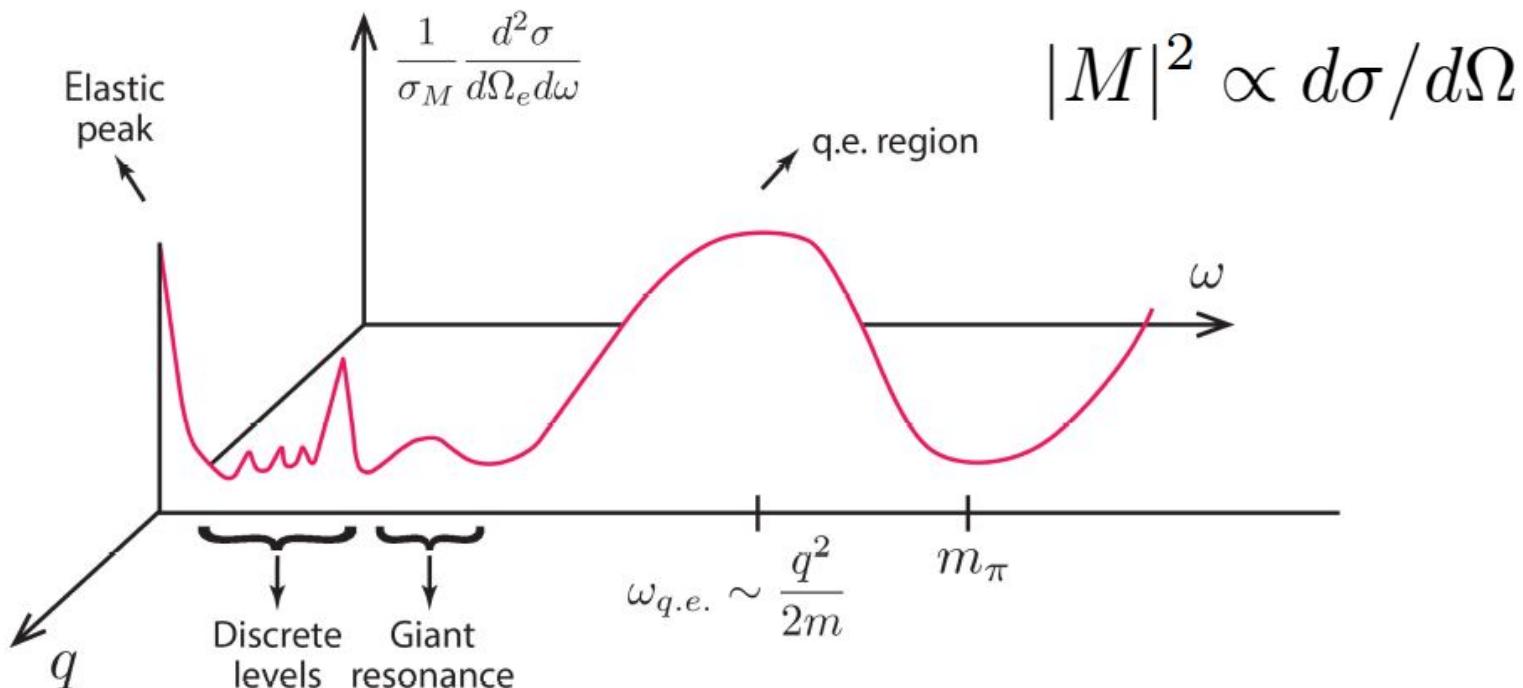
Two-body physics and beyond mean-field effects are dominant contribution to experimental uncertainty

Need to know cross sections at \sim 100s MeV to GeV energies

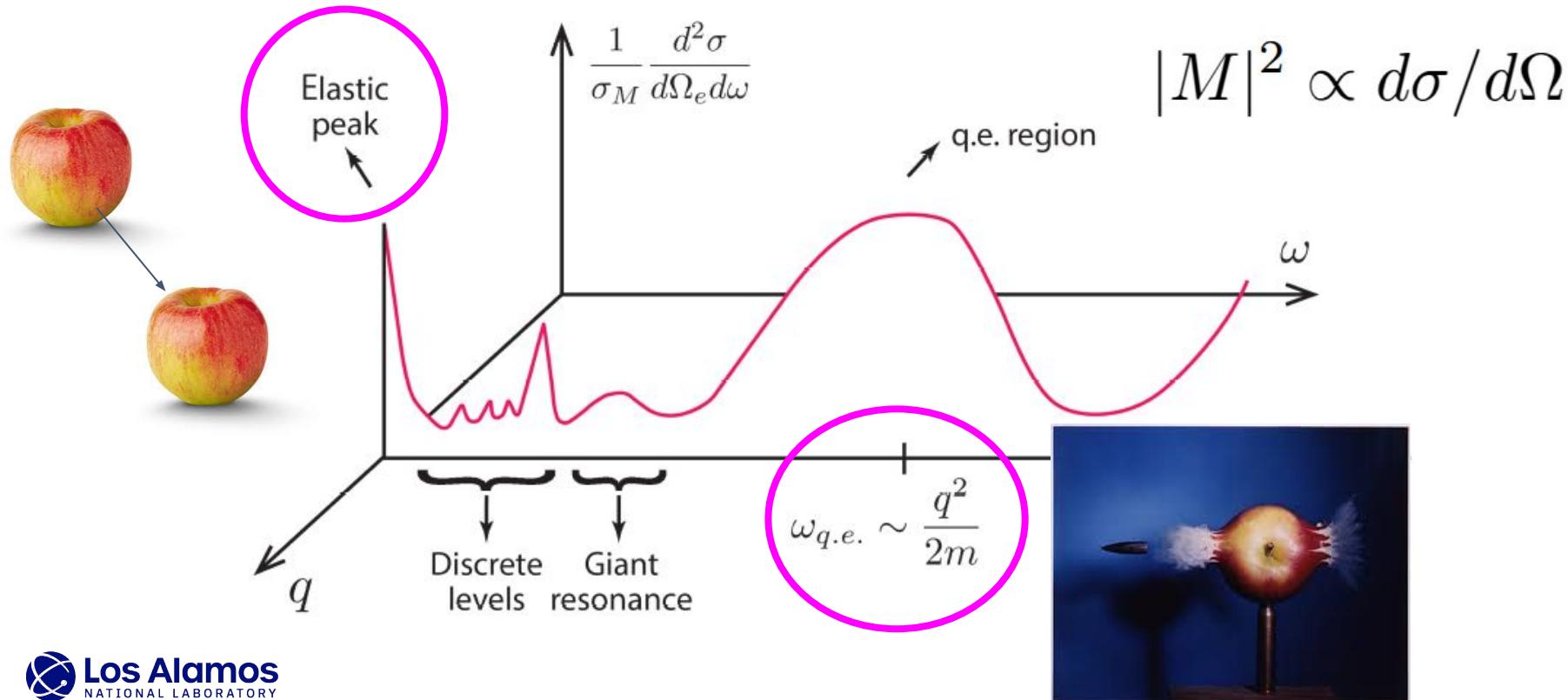


Can benchmark models with *electron scattering*

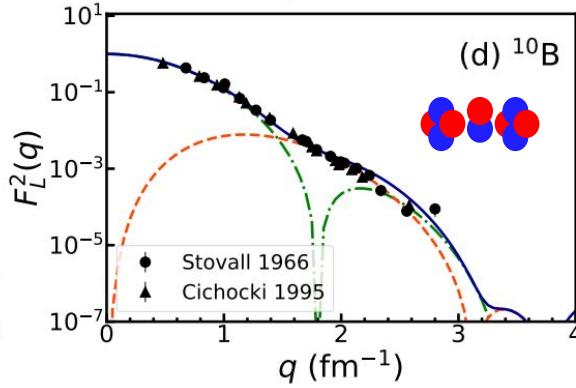
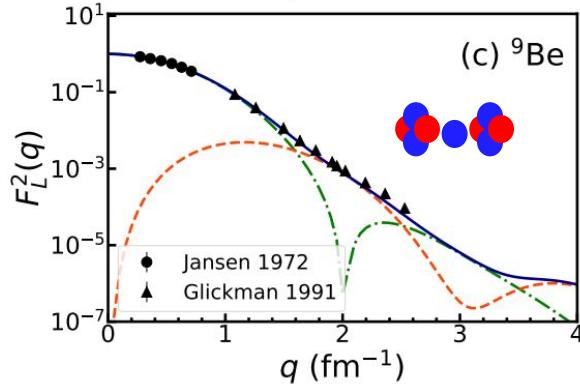
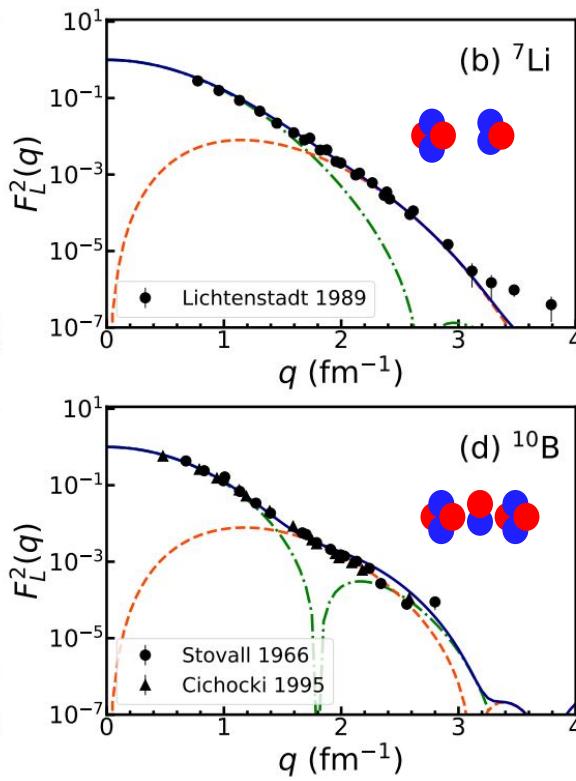
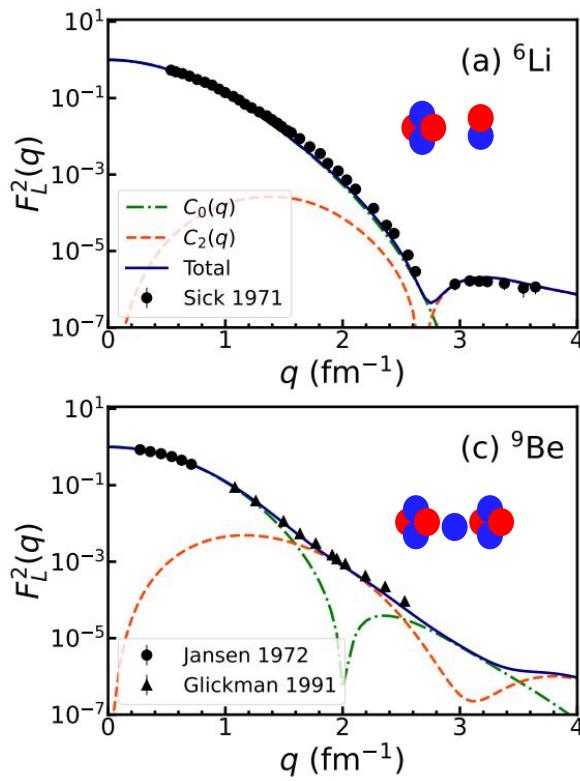
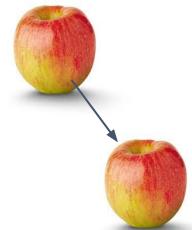
The kinematic regimes of lepton scattering



The kinematic regimes of lepton scattering



Elastic electron scattering form factors

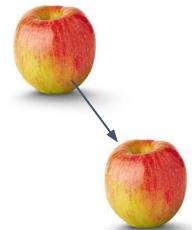


Charge form factor depends on sum of excited “multipolarities”

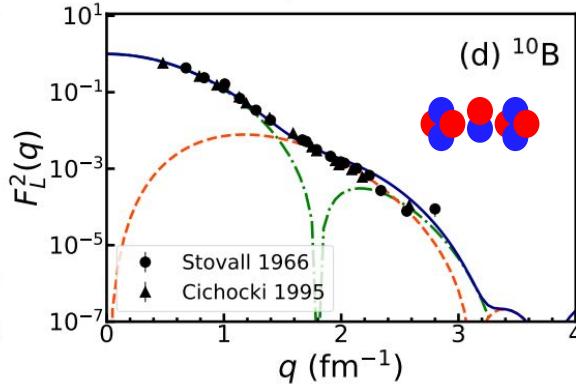
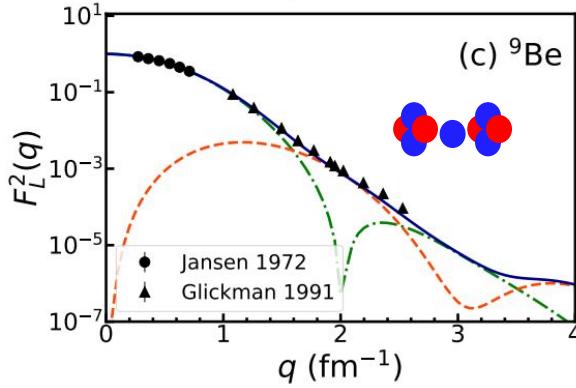
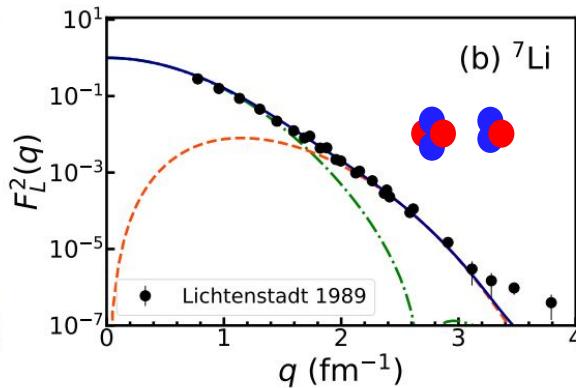
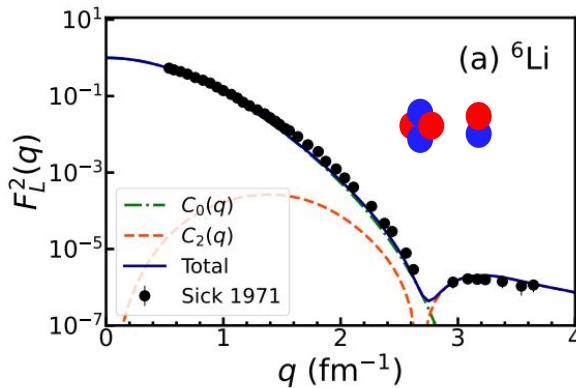
The $I=0$ term is related to spherically averaged charge density

$I=2$ is sensitive to quadrupole deformation of the nucleus

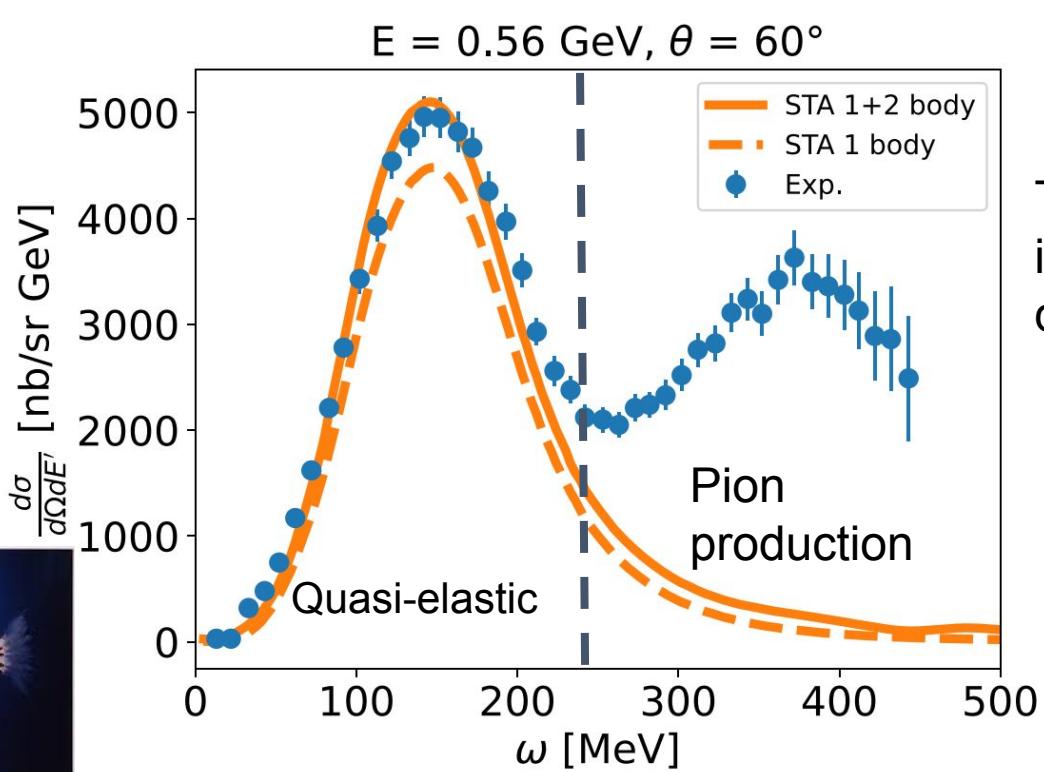
Elastic electron scattering form factors



Capturing shape gives insight into the *clustering* and the *nature of the nuclear force*



Quasi-elastic electron scattering on ^{12}C

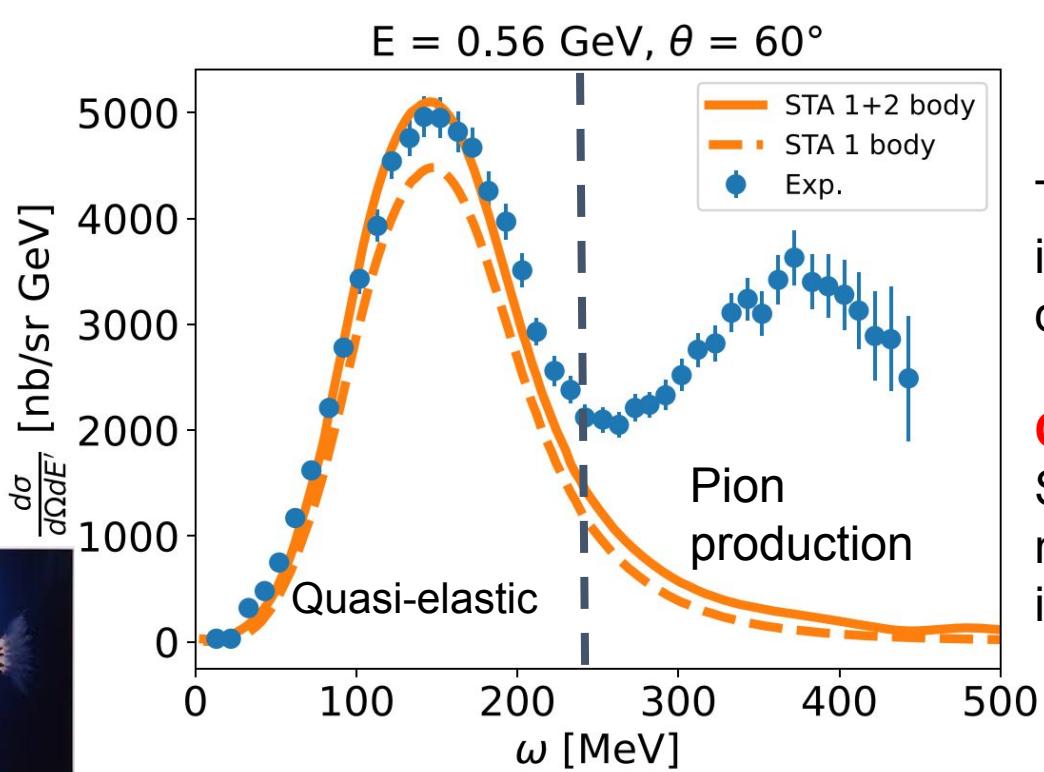


$$\frac{d\sigma}{d\Omega dE'} \propto \sum_i K_i | \langle \Psi | \mathcal{O}_i | \Psi \rangle |^2$$

Two-body physics plays an important role in describing quasi-elastic cross sections



Quasi-elastic electron scattering on ^{12}C



$$\frac{d\sigma}{d\Omega dE'} \propto \sum_i K_i | \langle \Psi | \mathcal{O}_i | \Psi \rangle |^2$$

Two-body physics plays an important role in describing quasi-elastic cross sections

Outlook:

Study of quasi-elastic neutrino scattering and inclusion of pion production



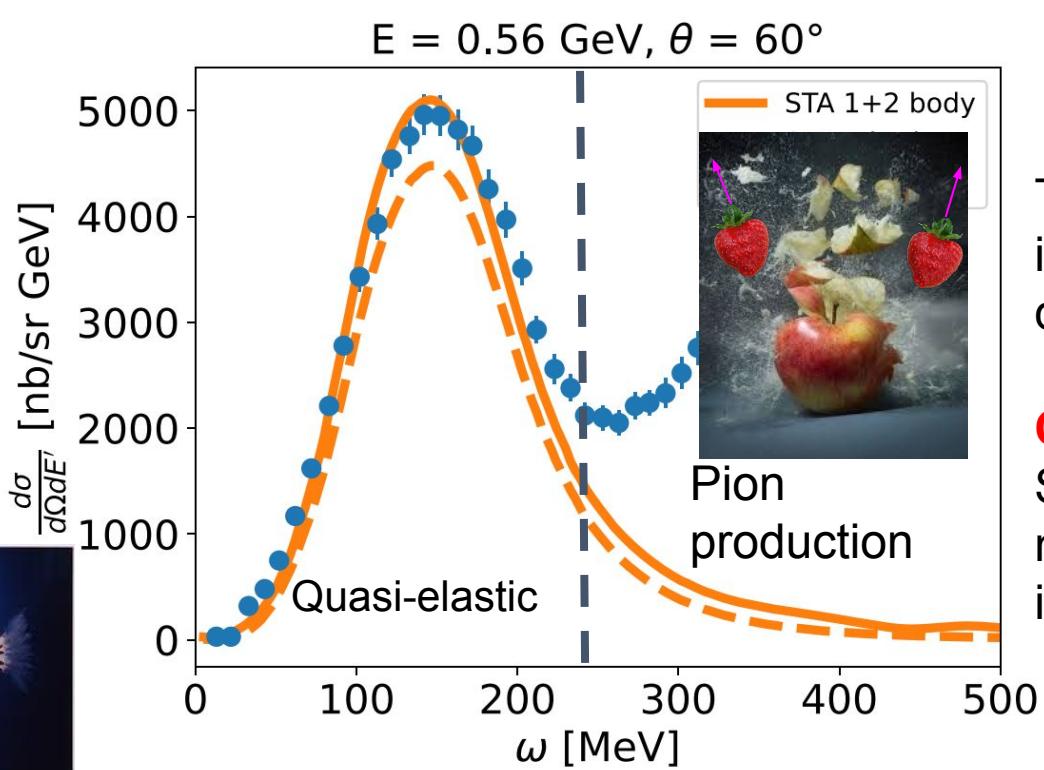
Los Alamos
NATIONAL LABORATORY

Andreoli, King, et al. PRC 110, 064004 (2024)

DUNE
DEEP UNDERGROUND
NEUTRINO EXPERIMENT



Quasi-elastic electron scattering on ^{12}C



Los Alamos
NATIONAL LABORATORY

Andreoli, King, et al. PRC 110, 064004 (2024)

$$\frac{d\sigma}{d\Omega dE'} \propto \sum_i K_i | \langle \Psi | \mathcal{O}_i | \Psi \rangle |^2$$

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NEUTRINO EXPERIMENT



Nuclear β -decay



β -decays as a bridge to new physics



Neutron is converted into a **proton**, **electron**, and an **electron antineutrino**

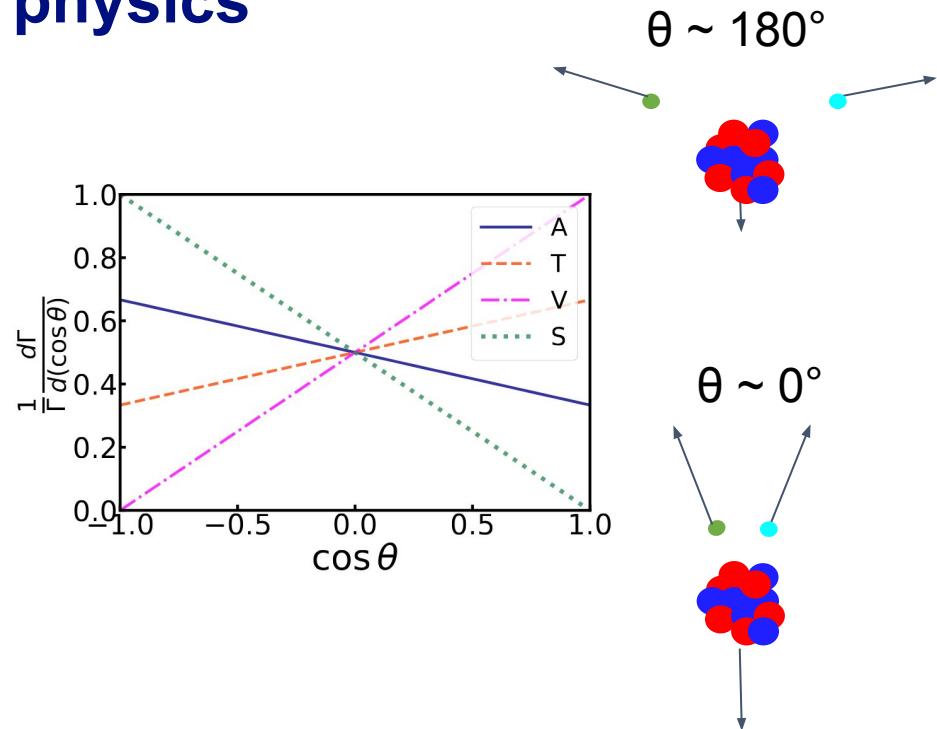
β -decays as a bridge to new physics

Weak currents with different transformation properties prefer different lepton angles

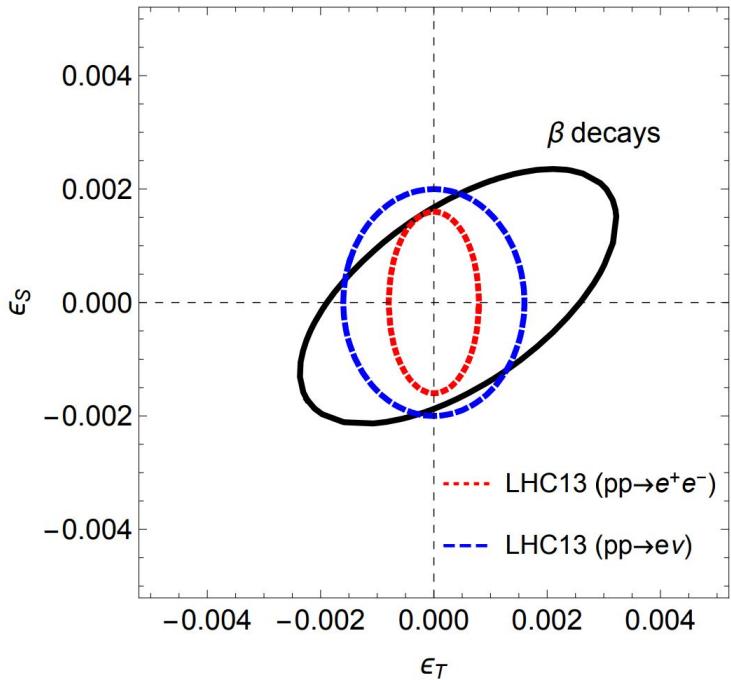
Standard Model is a **vector** minus **axial** theory

BSM **tensor** and **scalar** currents could interfere with standard current, changing kinematics

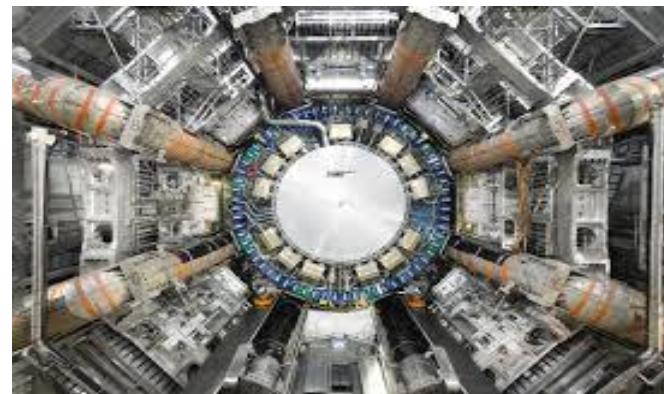
Neutrino mass would remove some phase space for the outgoing electron



New physics impact of nuclear β -decays

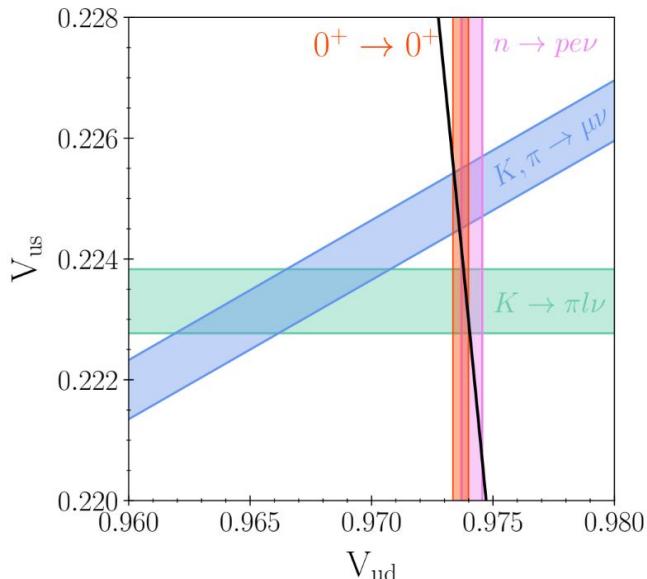


Competitive bounds on BSM currents that complement high-energy searches



Falkowski et al, JHEP04 (2021) 126

New physics impact of nuclear β -decays



Competitive bounds on BSM currents that complement high-energy searches

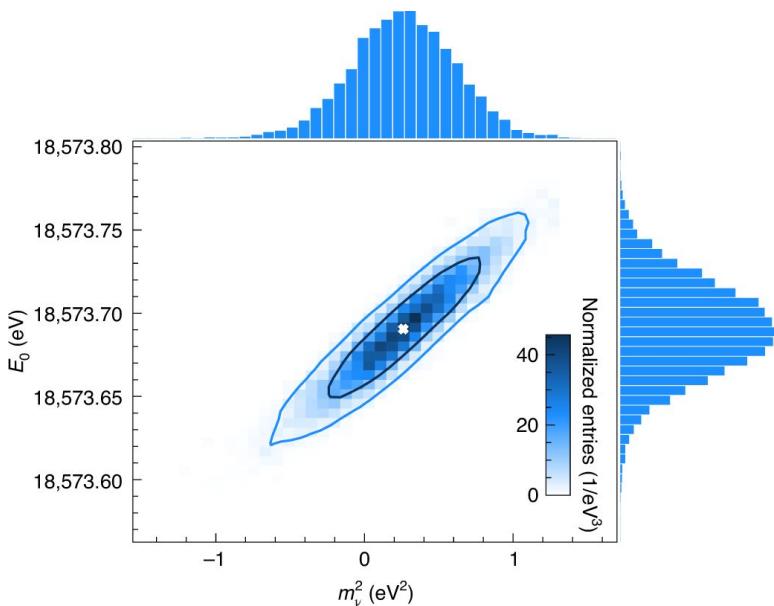
Tests of CKM unitarity

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

Cirigliano et al., PLB 838 (2023) 137748

New physics impact of nuclear β -decays



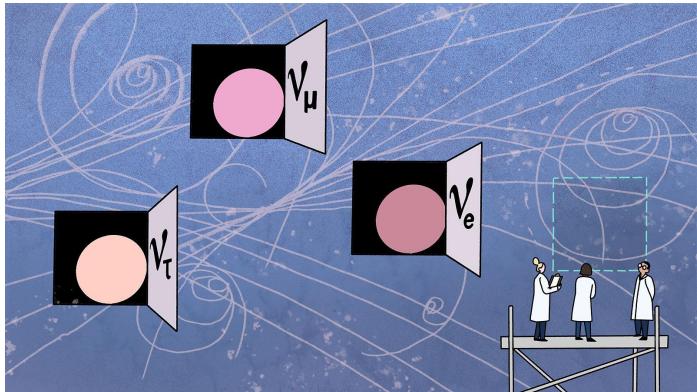
Competitive bounds on BSM currents that complement high-energy searches

Tests of CKM unitarity

Access to the scale of neutrino masses

The KATRIN Collaboration, Nature Phys. 18, 160–166 (2022)

New physics impact of nuclear β -decays



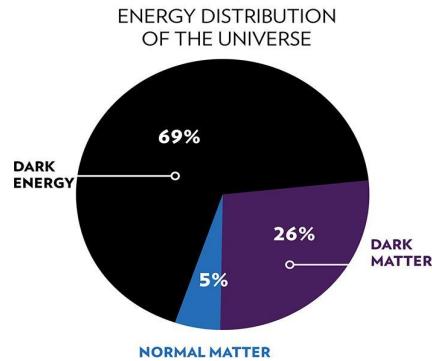
Competitive bounds on BSM currents that complement high-energy searches

Tests of CKM unitarity

Access to the scale of neutrino masses

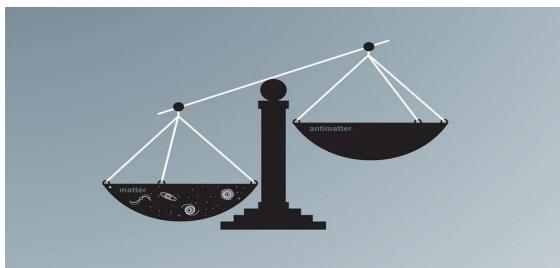
Bounds on sterile neutrinos

New physics impact of nuclear β -decays



Competitive bounds on BSM currents that complement high-energy searches

Tests of CKM unitarity



Access to the scale of neutrino masses

Bounds on sterile neutrinos

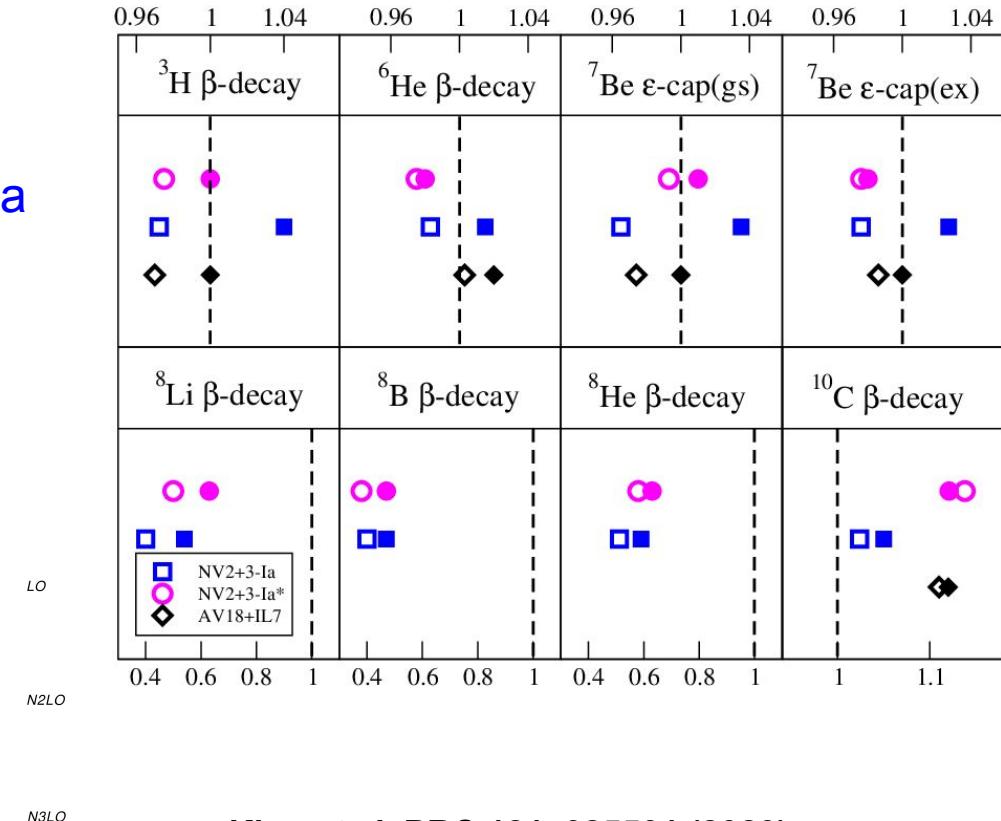
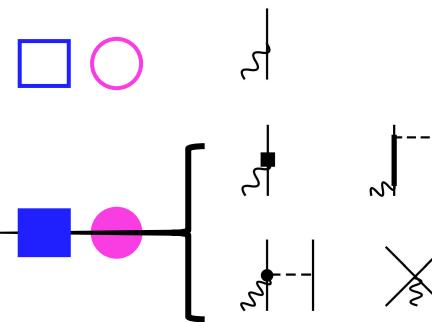
β -decay rates

Computed with two models:

Fit to 3H beta decay or purely strong data

Many-body correlations important

Two-body can be ~few % to several %



^6He β -decay spectrum: Overview

Differential rate without recoil:

$$\frac{d\Gamma}{dE_e} = |M|^2 G_\beta(E)$$

New physics can distort this:

$$\frac{d\Gamma}{dE_e} = \frac{d\Gamma_0}{dE_e} [1 + \Delta(E_e)]$$

Similar distortions can be generated when accounting for nuclear recoil

Performed calculation with recoil corrections and two-body physics effects

Vector
Scalar

 Fermi

Axial
Tensor
Pseudoscalar

 GT

${}^6\text{He}$ β -decay spectrum: Multipoles

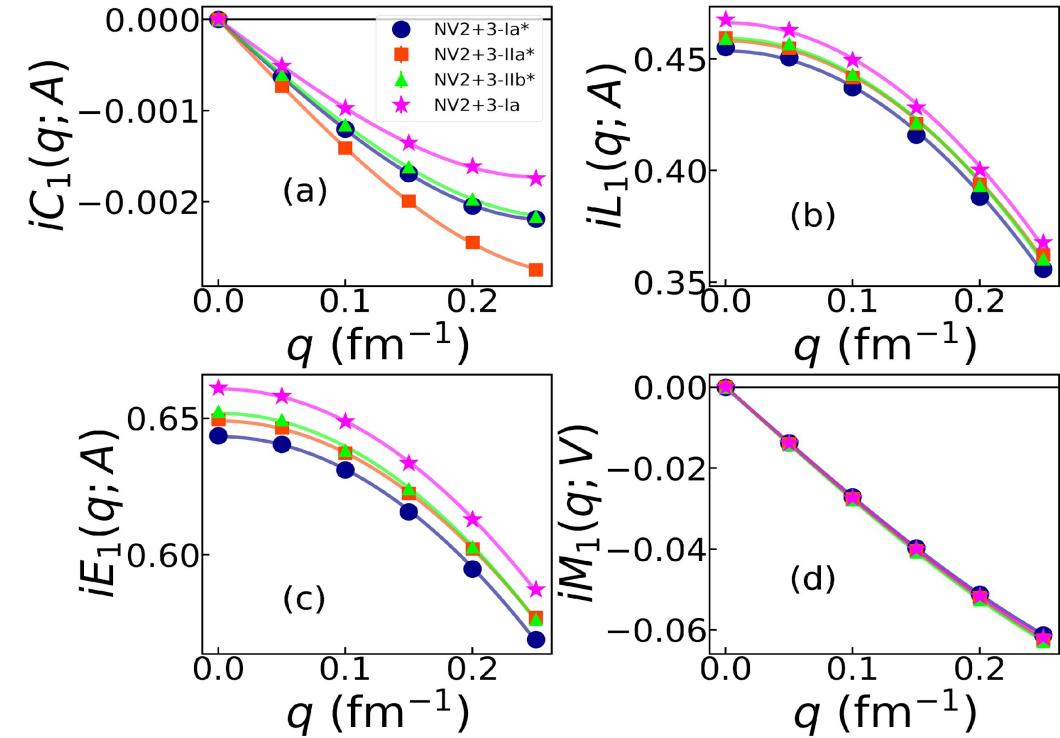
Distortion term is a function of four nuclear matrix elements:

$$C_1(q; A) = \frac{i}{\sqrt{4\pi}} \langle {}^6\text{Li}, 10 | \rho_+^\dagger(q\hat{\mathbf{z}}; A) | {}^6\text{He}, 00 \rangle$$

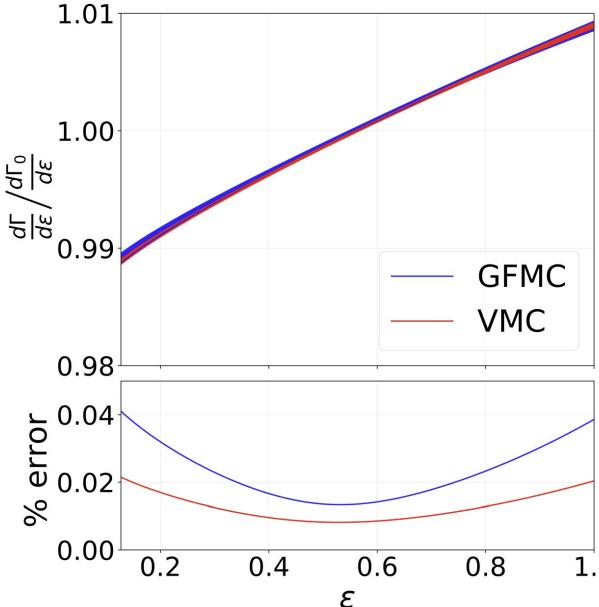
$$L_1(q; A) = \frac{i}{\sqrt{4\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{z}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{z}}; A) | {}^6\text{He}, 00 \rangle$$

$$E_1(q; A) = -\frac{i}{\sqrt{2\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{z}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{x}}; A) | {}^6\text{He}, 00 \rangle$$

$$M_1(q; V) = -\frac{1}{\sqrt{2\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{y}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{x}}; V) | {}^6\text{He}, 00 \rangle$$



${}^6\text{He}$ β -decay spectrum: Standard Model results



$$\varepsilon = \frac{E_e}{\omega}$$

Model uncertainty plus two-body contribution
brings theory precision within needs of experiment

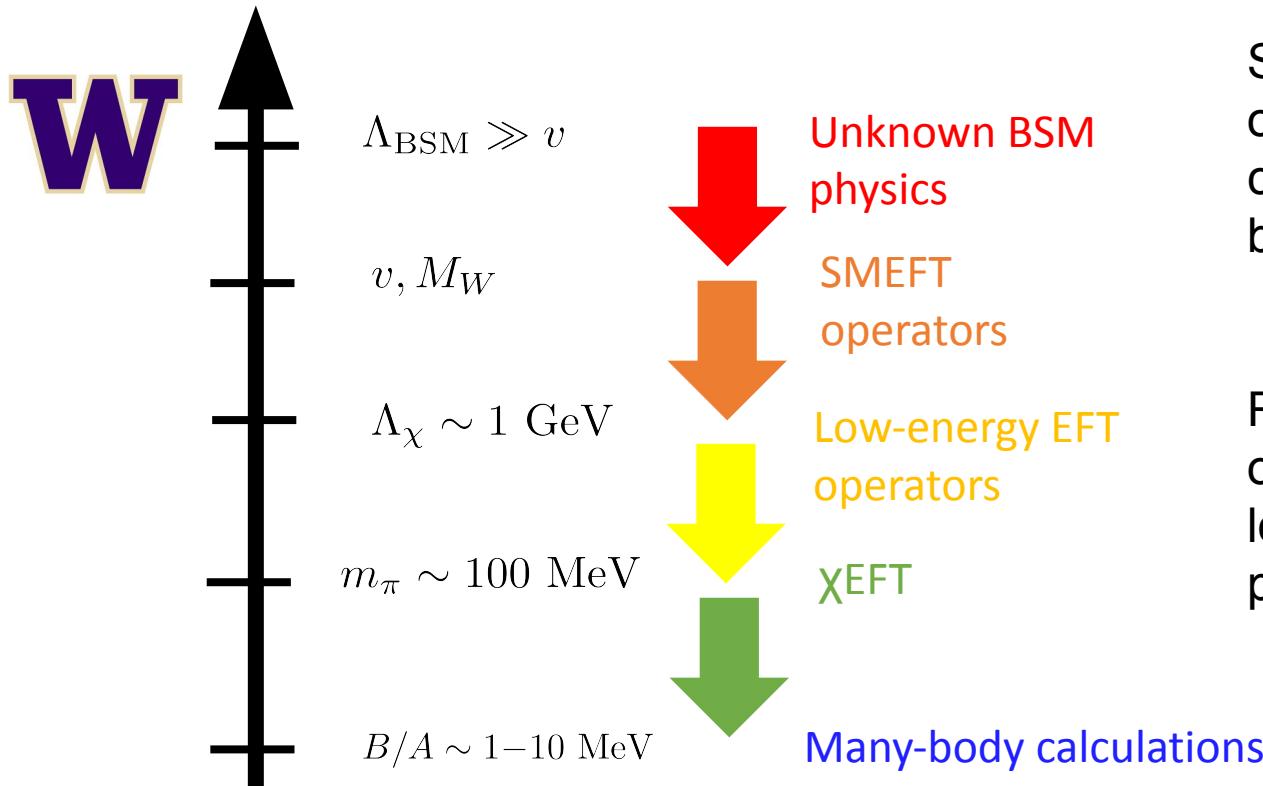
$$T_{\text{VMC}} = 762 \pm 11 \text{ ms}$$

$$T_{\text{GFMC}} = 808 \pm 24 \text{ ms}$$

$$T_{\text{Expt.}} = 807.25 \pm 0.16 \pm 0.11 \text{ ms}$$

[Kanafani et al. PRC 106, 045502 (2022)]

${}^6\text{He}$ β -decay spectrum: SMEFT



Start with most general operators in SMEFT that can contribute to GT beta decay

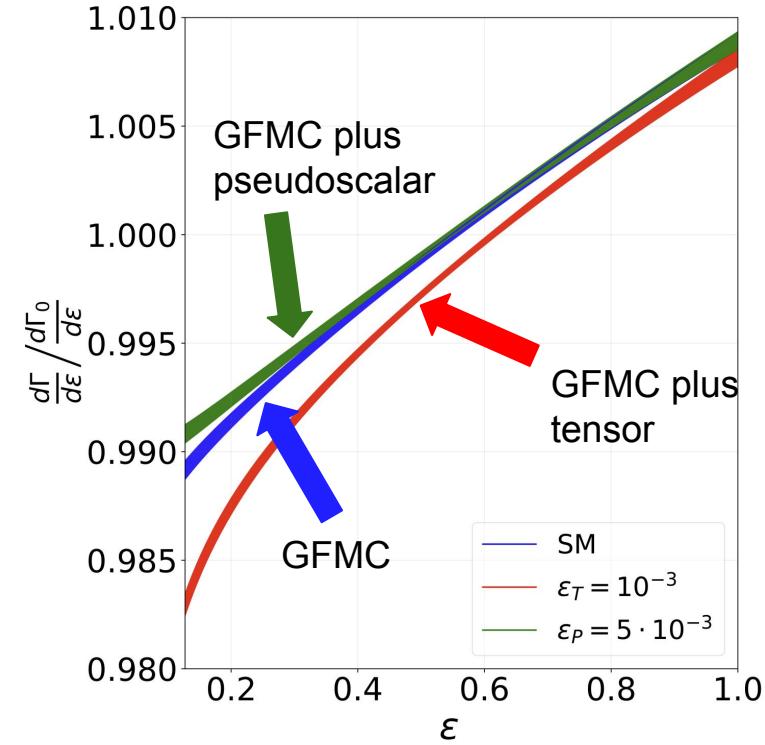
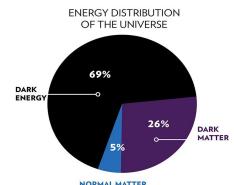
Run the coupling and obtain operators at the low-energy nuclear physics scale

${}^6\text{He}$ β -decay spectrum: Probing new forces

Included transition operators associated with new physics

With permille precision, it will be possible to further constrain new physics

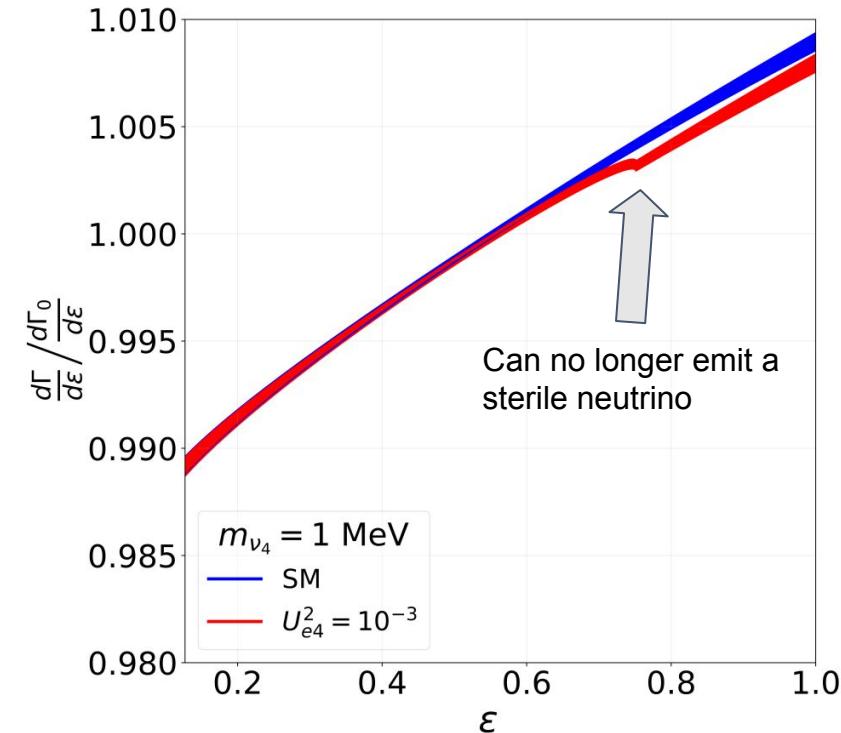
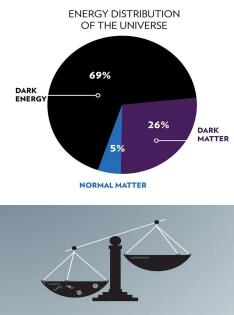
$$\Lambda_{\text{BSM}} \sim \frac{\Lambda_{\text{EW}}}{\sqrt{\epsilon_i}} \sim 1-10 \text{ TeV}$$



${}^6\text{He}$ β -decay spectrum: Probing neutrino physics

Can also investigate impacts from production of ~ 1 MeV sterile neutrinos

The shape of the decay endpoint can exclude some parameter space and probe BSM scenarios



Superallowed $0^+ \rightarrow 0^+$ decays

Under good isospin $M_F = \langle TT_z \pm 1 | T_\pm | TT_z \rangle = \sqrt{(T \mp T_z)(T \pm T_z + 1)}$

For T=1 triplets

$$M_F = \sqrt{2}$$

“ft” value should also be constant

$$ft = \frac{K}{2G_F^2 V_{ud}^2}$$

Hardy and Towner PRC 102, 045501 (2020)

Superallowed $0^+ \rightarrow 0^+$ decays

$$\mathcal{F}t = \frac{K}{2G_F^2 V_{ud}^2 (1 + \boxed{\Delta_R^V})} = ft(1 + \boxed{\delta'_R})(1 + \boxed{\delta_{\text{NS}}} - \boxed{\delta_{\text{C}}})$$

Transition-independent single-nucleon corrections

Correction sensitive to charge and electron energy

Sensitive to internal structure of the nucleus

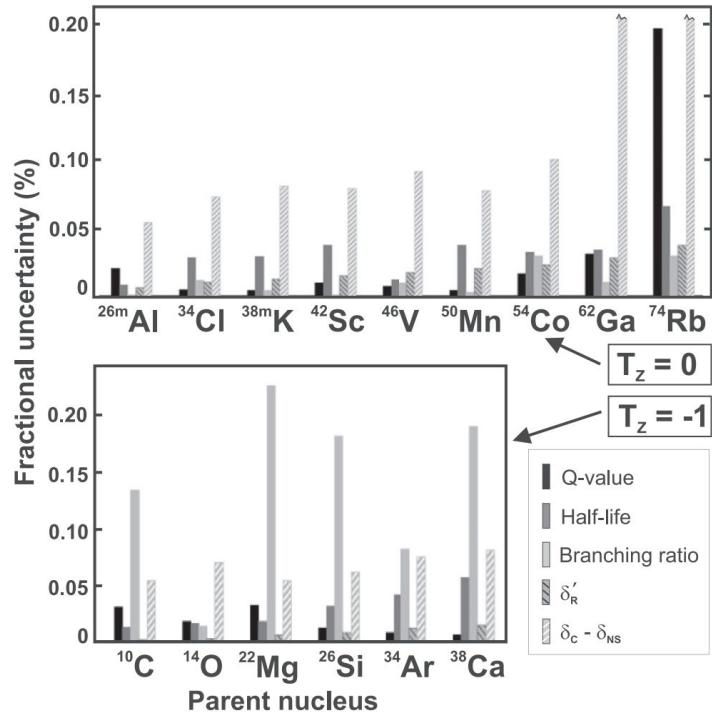
Broken isospin symmetry between protons and neutrons

Superallowed $0^+ \rightarrow 0^+$ decays

Corrections must be accounted for in real decay

$$\mathcal{F}t = \frac{K}{2G_F^2 V_{ud}^2 (1 + \Delta_R^V)} = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C)$$

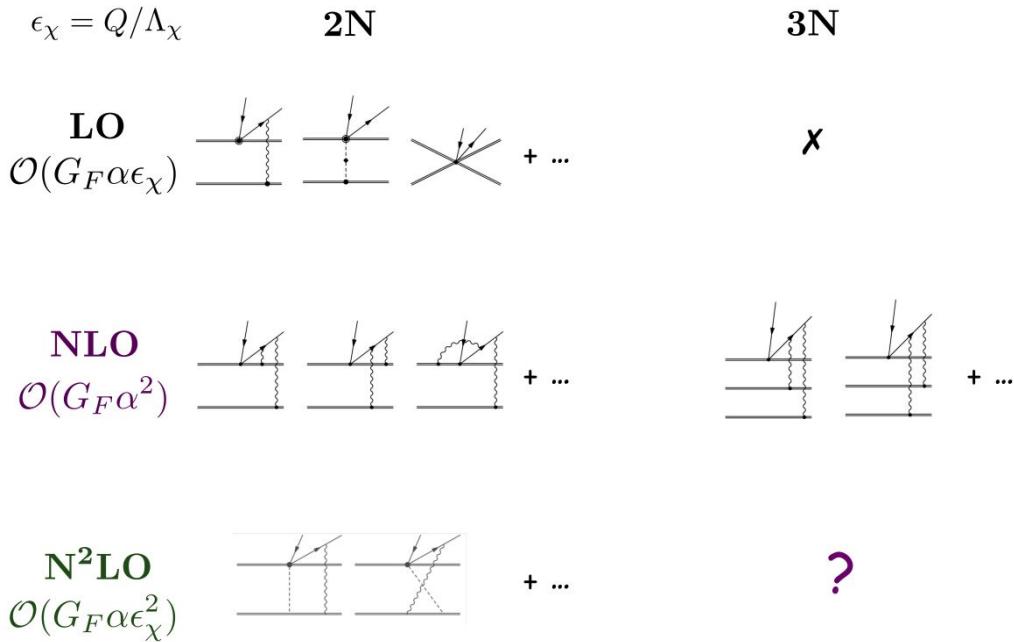
Dominant uncertainty is nuclear theory



EFT approach to radiative corrections

$$\epsilon_\chi = Q/\Lambda_\chi$$

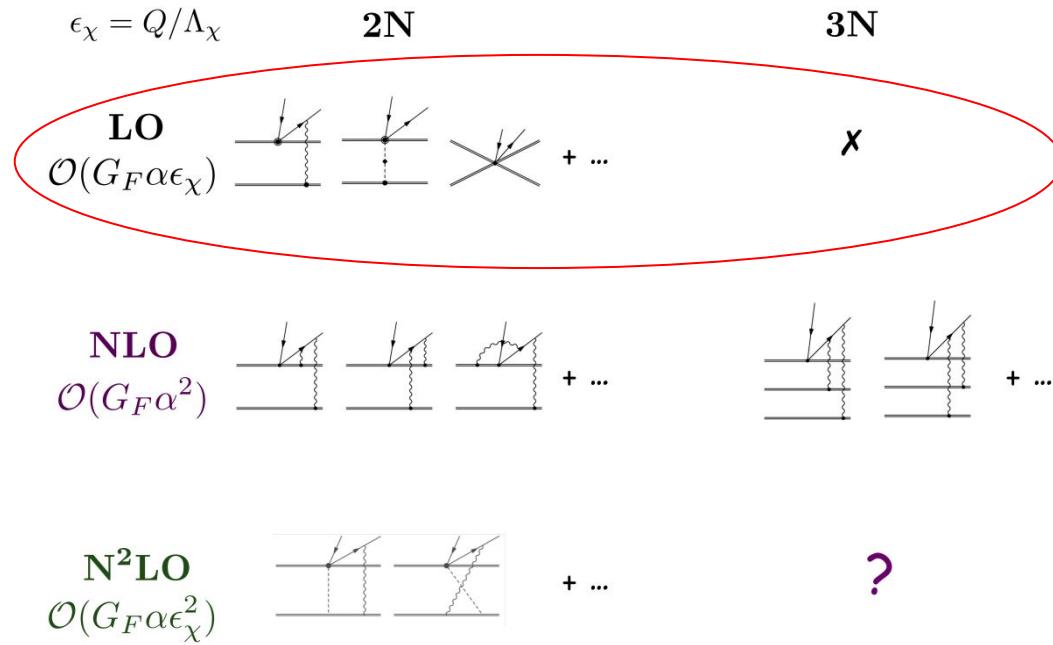
*Cirigliano,
Dekens,
Hoferichter,
Mereghetti,
Tomalak, + ...*



Cirigliano et al. PRL 133, 211801 (2024)

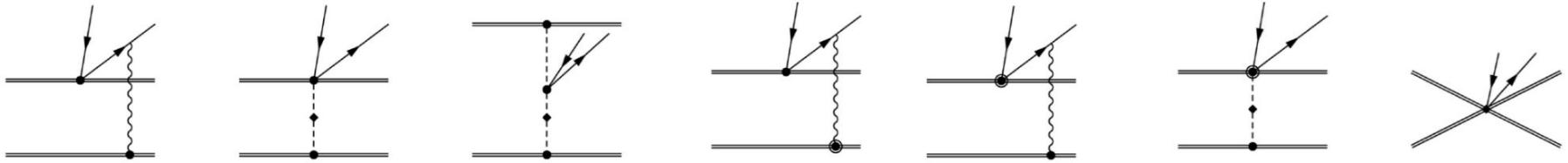
EFT approach to radiative corrections

*Cirigliano,
Dekens,
Hoferichter,
Mereghetti,
Tomalak, + ...*

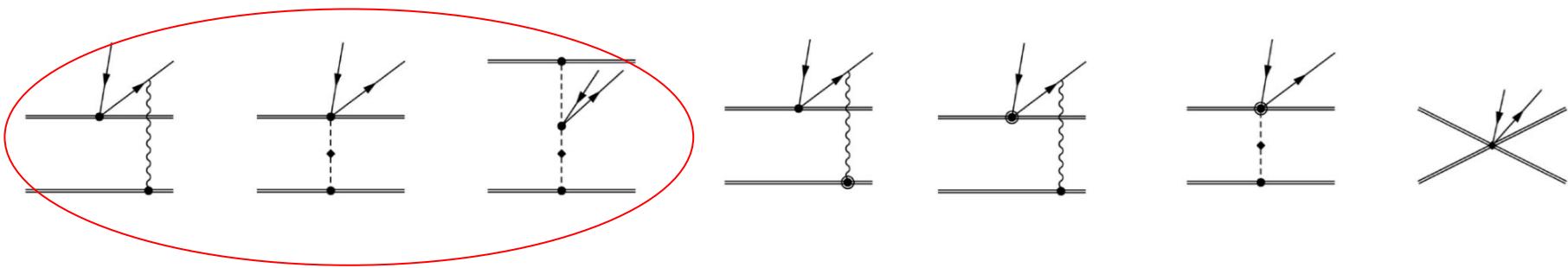


Cirigliano et al. PRL 133, 211801 (2024)

EFT approach to radiative corrections



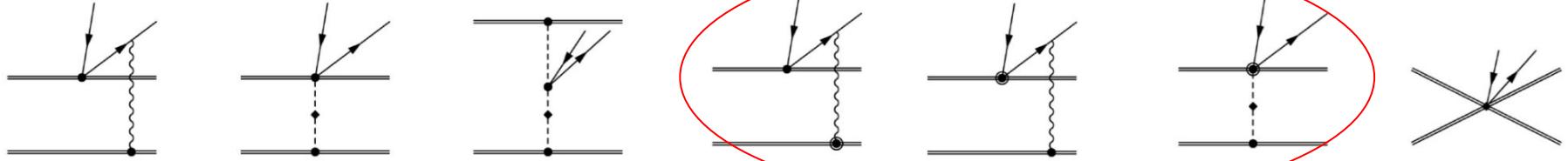
EFT approach to radiative corrections



Energy-dependent terms, proportional to the external momentum

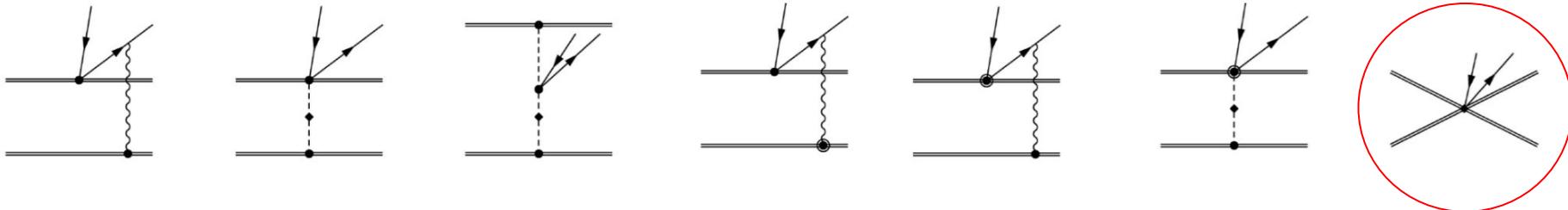
Grows with the size of the system

EFT approach to radiative corrections



Energy-independent terms arising from magnetic moment and recoil effects

EFT approach to radiative corrections



Absorbs the cutoff dependence of the long-range terms

Introduces two unknown parameters that must be fit or modelled

LEC is taken as an uncertainty in individual calculations

$^{10}\text{C}(0^+) \rightarrow {}^{10}\text{B}(0^+)$ β -decay

In an effective field theory approach:

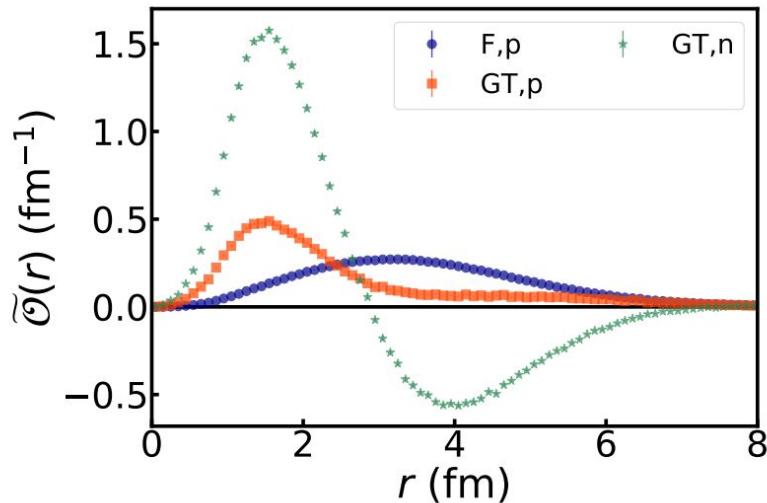
$$\delta_{\text{NS}} = \sum_{m,n,i} \alpha^m E_0^n c_{m,n} M_{m,n}^i$$

Can also evaluate: $M = \int dr C(r) \tilde{\mathcal{O}}(r)$

GFMC: $\delta_{\text{NS}} = -4.46(48) \times 10^{-3} - -4.64(77) \times 10^{-3}$

Hardy and Towner: $\delta_{\text{NS}} = -4.0(5) \times 10^{-3}$

Gennari et al PRL 134, 012501: $\delta_{\text{NS}} = -4.22(32) \times 10^{-3}$



King et al., arXiv:2509.07310v1

Outlook: Benchmark QMC + Coupled-cluster

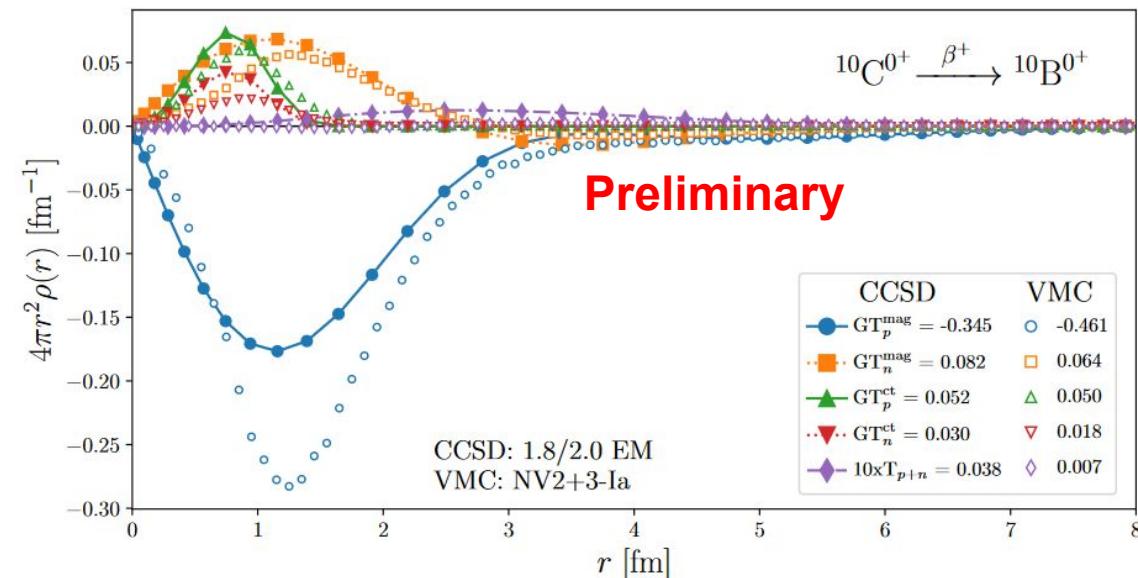


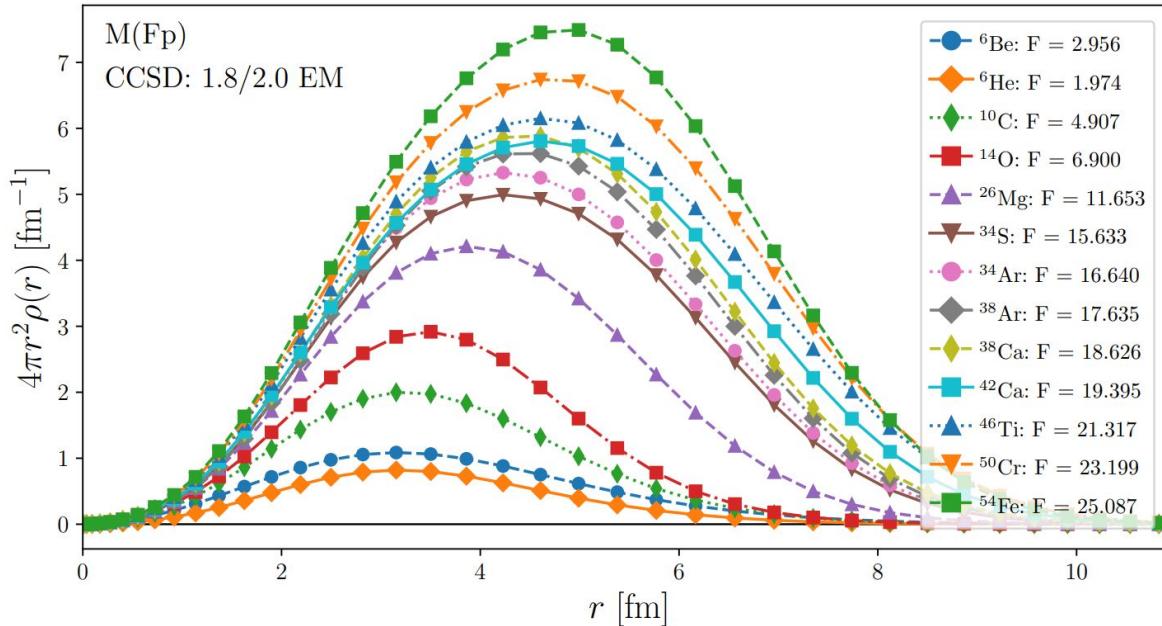
Figure courtesy of Sam Novario

Benchmarking different models, methods in first step toward global analysis

Qualitative agreement, but further analysis necessary

Outlook: Global analysis Coupled-cluster

Preliminary



S. J. Novario, "Nuclear-Structure Corrections in Superallowed Beta Decay" (2025)

Outlook: Higher-order EFT operators

$$\epsilon_\chi = Q/\Lambda_\chi$$

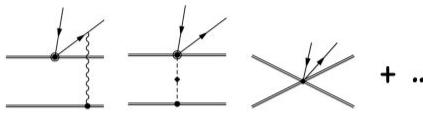
2N

3N

G. Chambers-Wall,

LO

$$\mathcal{O}(G_F \alpha \epsilon_\chi)$$



+ ...

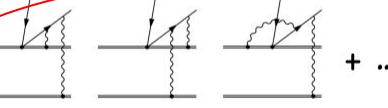
x

Cirigliano, Dekens,
Hoferichter,
Mereghetti, Tomalak,

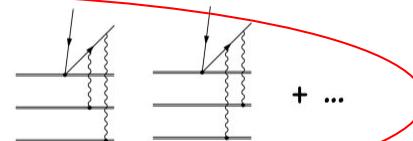
+ ...



NLO
 $\mathcal{O}(G_F \alpha^2)$

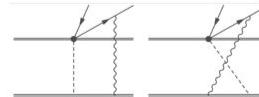


+ ...



+ ...

$\mathcal{O}(G_F \alpha \epsilon_\chi^2)$

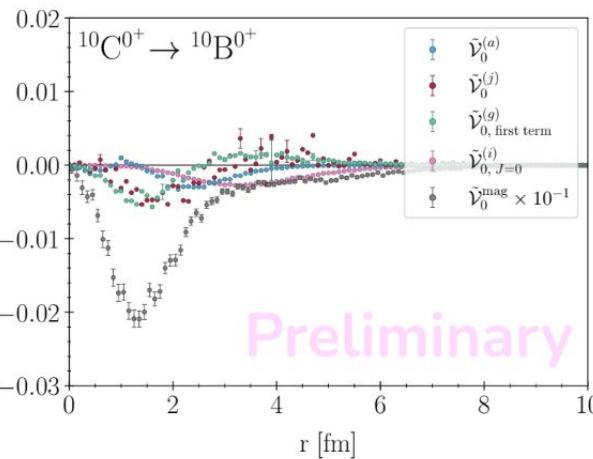
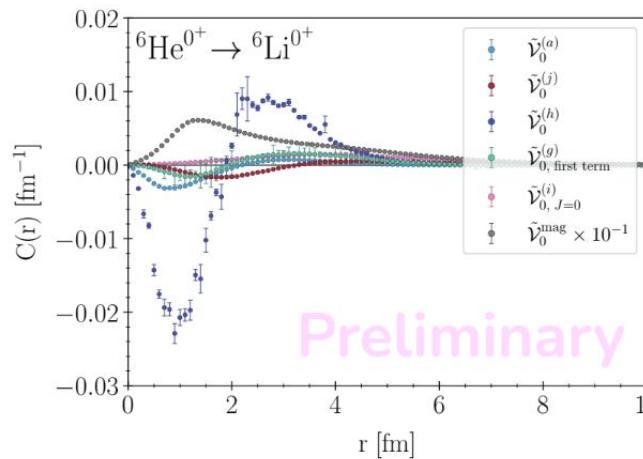


+ ...

?

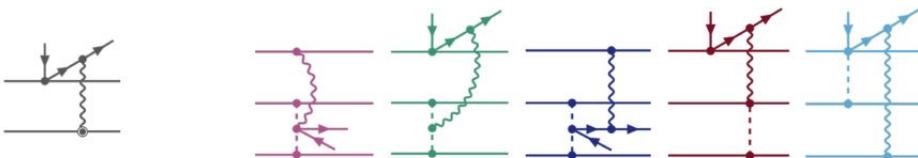
Outlook: Higher-order EFT operators

G. Chambers-Wall



Preliminary calculation
of NLO contributions

~5% corrections to LO
two-body from NLO



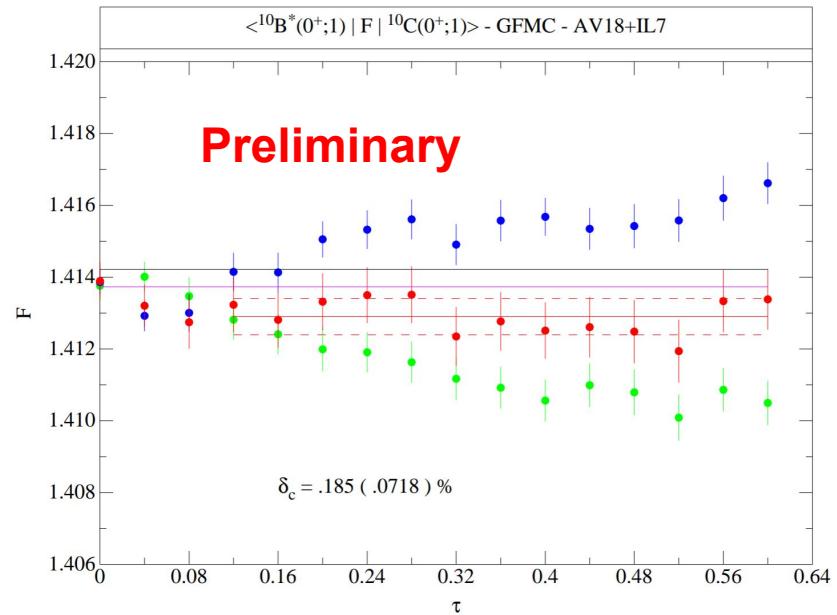
Future directions

Isospin breaking corrections with GFMC

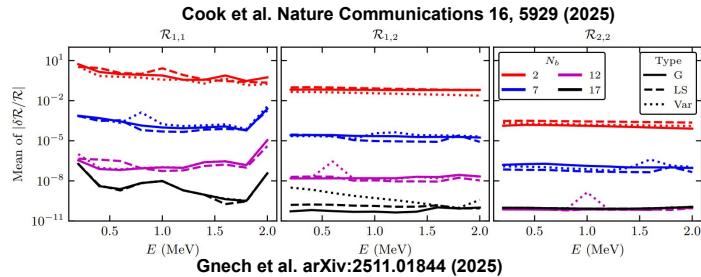
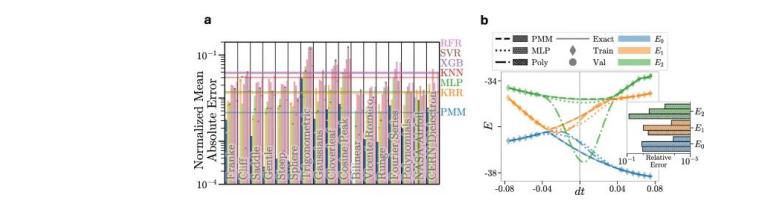
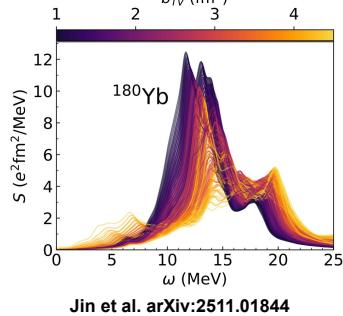
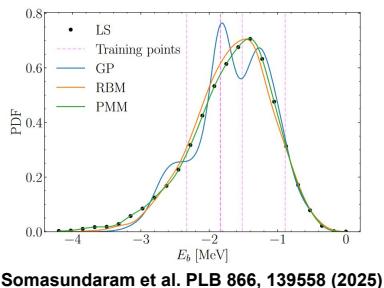
Fermi matrix element evaluated using wave functions with isospin breaking correlations

AV18+IL7 results consistent with shell model with ~ 2.6 times smaller error bar

Chiral interaction predicts ~ 1.4 times larger correction than AV18+IL7, ~ 1.3 times smaller error than shell model



Quantifying uncertainties to connect with precision



Bayesian UQ requires sampling many times from parameter space

QMC calculations are costly, sampling is computationally prohibitive

Emulators replace full-order model with low-order approximation

Pushing to Heavier nuclei with Auxiliary Field Diffusion Monte Carlo (AFDMC)

Use the single particle basis:

$$\langle S | \Psi \rangle \propto \xi_{\alpha_1}(s_1) \xi_{\alpha_2}(s_2) \dots \xi_{\alpha_A}(s_A)$$

Advantage of a polynomial scaling with A

Technically more complicated to operate on wave function

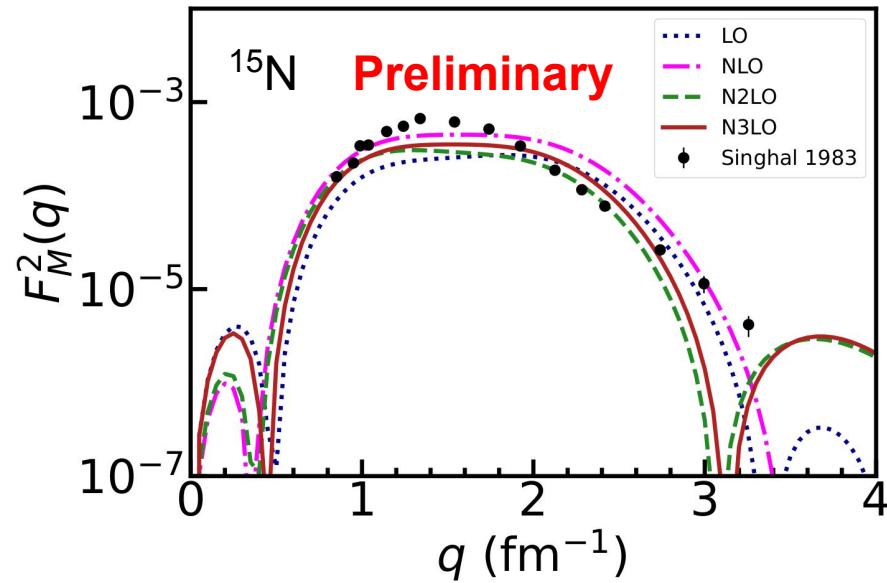
Cost is a simpler correlation structure in the wave function

Quasi-elastic neutrino scattering with AFDMC

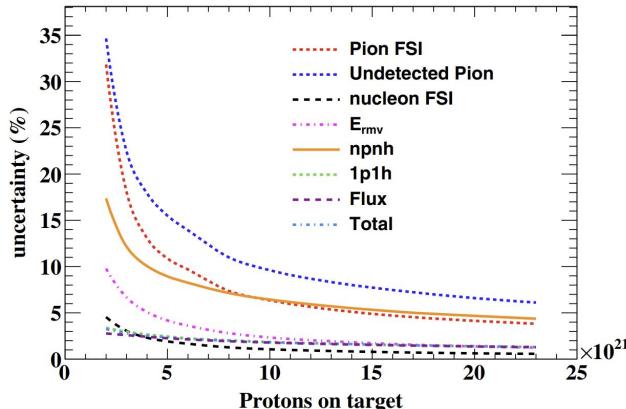
QMC quasi-elastic responses so far for scattering on $A \leq 12$ nuclei

AFDMC basis would allow the study of heavier nuclei

Present: Elastic scattering using the AFDMC basis



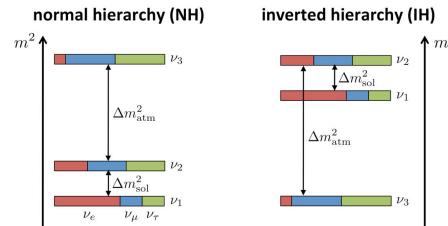
Quasi-elastic neutrino scattering outlook



Dolan et al. PRD 105, 032010 (2022)

AFDMC allows for consistent treatment of two-body currents in heavy nuclei

Two-body current processes represent one of the largest systematic uncertainties for DUNE experiment



Information from DUNE complementary to neutrinoless double beta decay and neutrino mass efforts at UW

Beta decay spectra

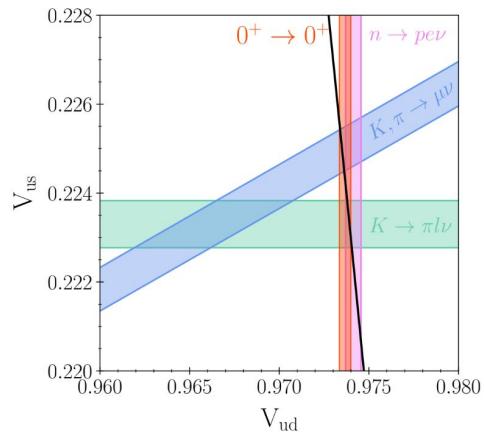
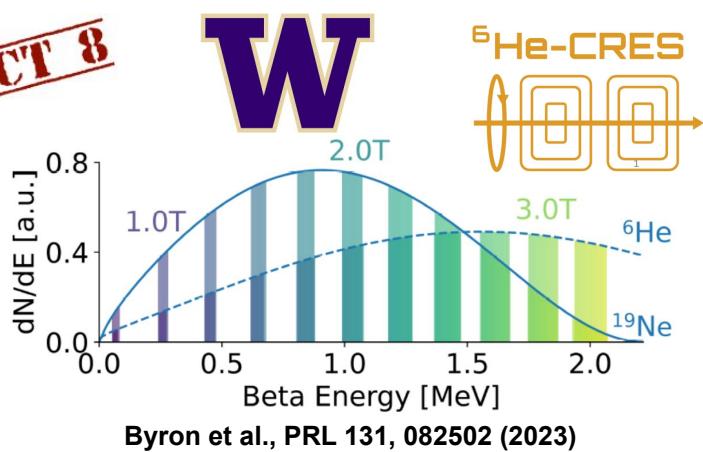
PROJECT 8

Spectra of nuclei heavier than ${}^6\text{He}$ also important for BSM physics

${}^{19}\text{Ne}$ important for the ${}^6\text{He}$ -CRES experiment

Recoil spectra up to $A = 41$ important for constraining V_{ud}

AFDMC makes these cases accessible



What will this require?

Better understanding of model dependence in nuclear interaction (supported by EFT expertise at UW)

Identifying impactful beta decay spectra (UW and INT collaboration)

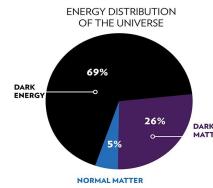
Computational resources (UW Research Computing and external)

Conclusions

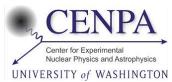
Accurate many-body calculations of interacting nucleons provide a powerful way to understand the impact of the nuclear dynamics on electroweak structure

QMC allows for *understanding* and *interpretation* of these impacts

Future directions will help bridge precision searches and nuclear physics



QMC @ 



Acknowledgements

WUSTL: Chambers-Wall, Pastore, Piarulli

ANL: Wiringa

JLab+ODU: Andreoli, Gnech, Schiavilla

LANL: Carlson, Gandolfi, Mereghetti

LPC Caen: Hayen

ORNL: Baroni

UW: Cirigliano



**Funding from DOE/NNSA Stewardship Science Graduate Fellowship and the
LDRD Project 20240742PRD1**

Computational resources provided by Argonne ALCF and NERSC

Additional slides

Variational Monte Carlo

$$|\Psi_T\rangle = \left[\mathcal{S} \prod_{i < j} (1 + \textcolor{red}{U}_{ij} + \sum_{k \neq i, j} \textcolor{blue}{U}_{ijk}) \right] \left[\sum_{i < j} \textcolor{green}{f}_c(r_{ij}) \right] |\Phi_A(JMTT_z)\rangle$$

Slater determinant of nucleons in s- and p-shell coupled to the appropriate quantum numbers

Pair correlation operator encoding appropriate cluster structure

Two- and three-body correlation operator to reflect impact of nuclear interaction at short distances

Optimize when you minimize:

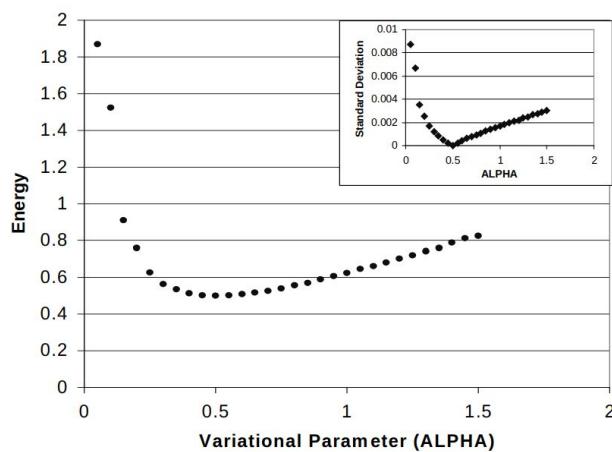
$$E_V = \frac{\langle \Psi_V | H | \Psi_V \rangle}{\langle \Psi_V | \Psi_V \rangle} \geq E_0$$

Variational Monte Carlo: 1D Example

$$V(x) = \frac{1}{2}x^2$$

$$\Psi_0(x) = \left(\frac{1}{\pi}\right)^{1/4} e^{-x^2/2}$$

$$E_0 = \frac{1}{2}$$



Use Monte Carlo to compute:

$$\frac{\langle \Psi_T | H | \Psi_T \rangle}{\langle \Psi_T | \Psi_T \rangle} = \frac{\int d\mathbf{R} |\Psi_T(\mathbf{R})|^2 E_L(\mathbf{R})}{\int d\mathbf{R} |\Psi_T(\mathbf{R})|^2}; \quad E_L(\mathbf{R}) = \frac{H\Psi_T(\mathbf{R})}{\Psi_T(\mathbf{R})}$$

Can tune $\Psi_T = \left(\frac{2\alpha}{\pi}\right)^{1/4} e^{-\alpha x^2}$ to solve

Pottorf et al, Eur. J. Phys. 20 205 (1999)

Green's function Monte Carlo

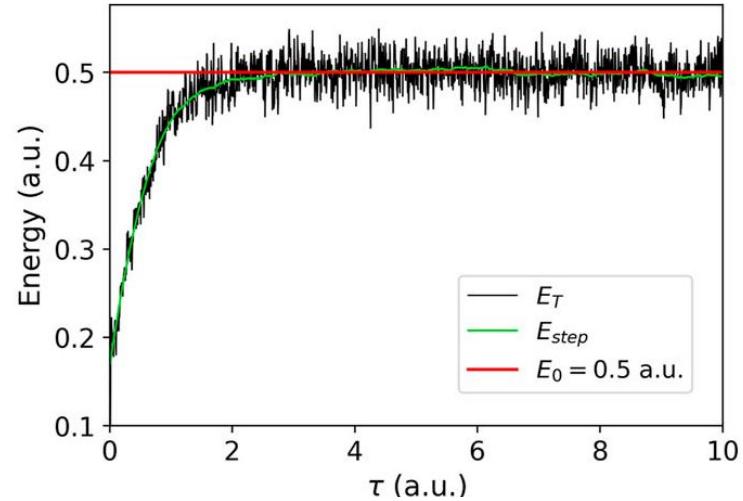
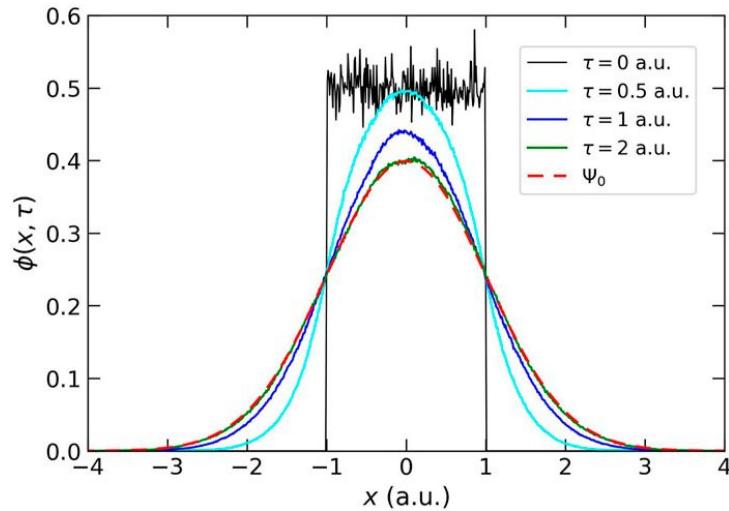
Recast $i\frac{\partial}{\partial t} |\Psi(t)\rangle = (H - E_T) |\Psi(t)\rangle$ as $-\frac{\partial}{\partial \tau} |\Psi(\tau)\rangle = (H - E_T) |\Psi(\tau)\rangle$

Solution: $|\Psi(\tau)\rangle = e^{-(H - E_T)\tau} |\Psi(0)\rangle$

Recall $|\Psi(0)\rangle = \sum_i c_i |\psi_i\rangle$ and note $e^{-(H - E_0)\tau} |\Psi(0)\rangle = c_0 \psi_0 + \sum_i e^{-\alpha_i \tau} c_i |\psi_i\rangle$; $\alpha_i > 0$

For a proper offset $\lim_{\tau \rightarrow \infty} e^{-(H - E_0)\tau} |\Psi(0)\rangle \rightarrow c_0 \psi_0$

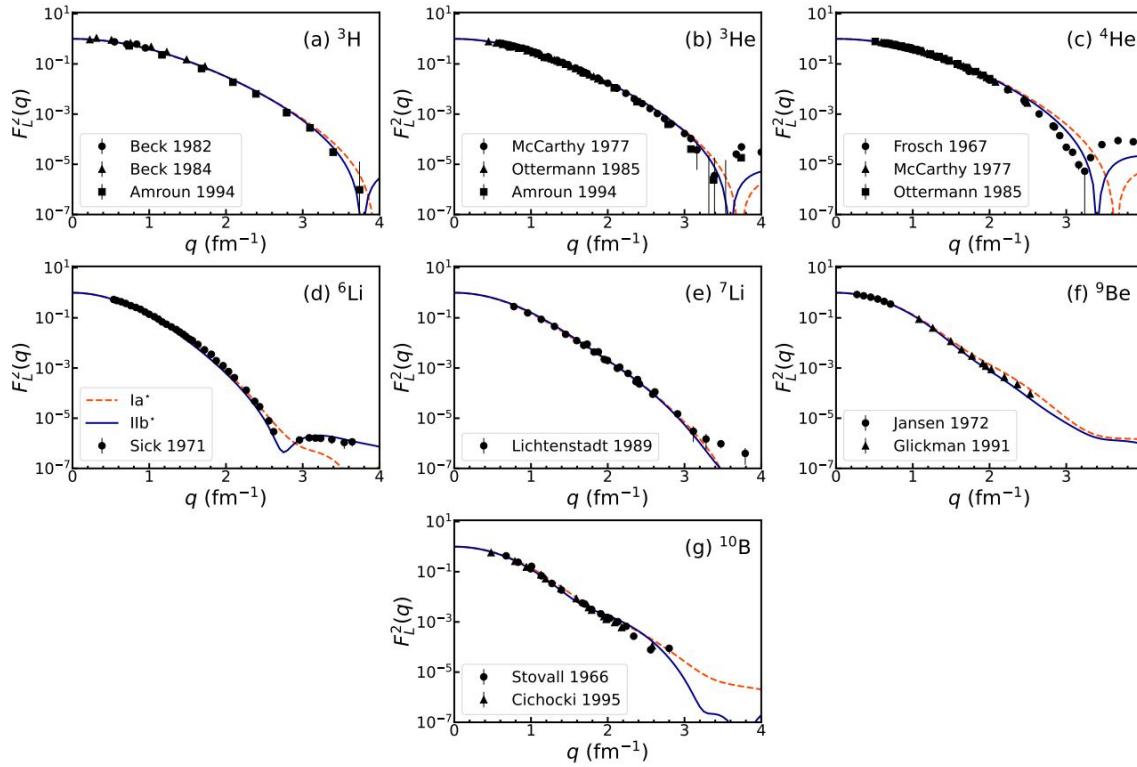
Green's function Monte Carlo: 1D example



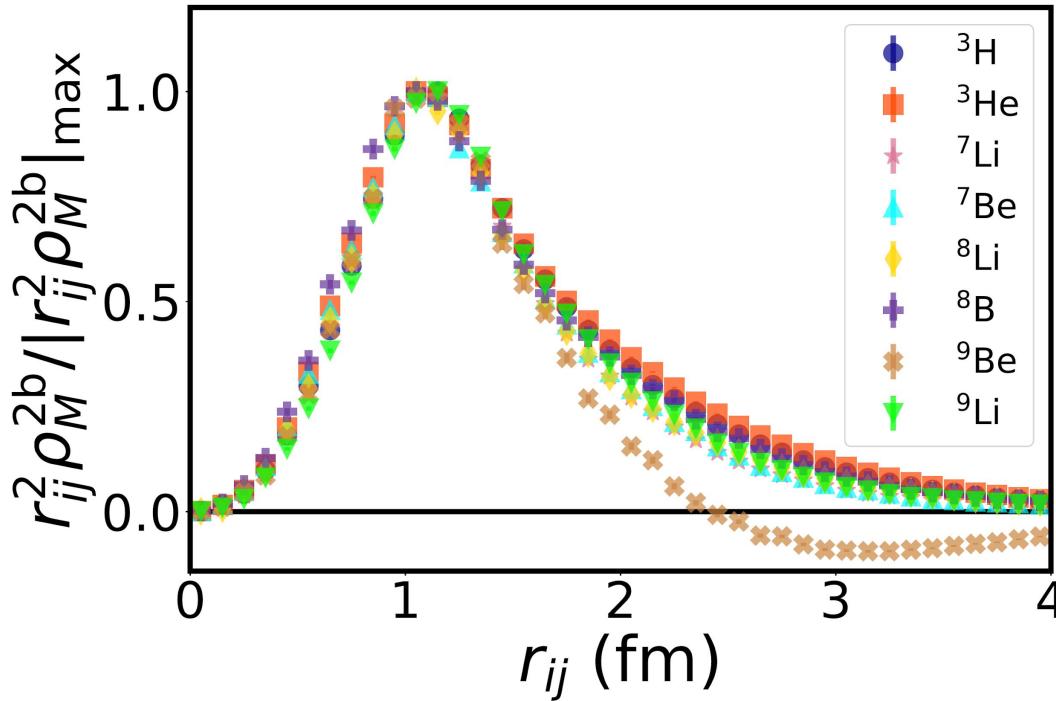
$$G(\mathbf{R}', \mathbf{R}) = \langle \mathbf{R}' | e^{-(H - E_0)\Delta\tau} | \mathbf{R} \rangle$$

$$\Psi(\mathbf{R}_N; \tau) = \int d\mathbf{R}_{N-1} \dots d\mathbf{R}_1 d\mathbf{R}_0 G(\mathbf{R}_N, \mathbf{R}_{N-1}) \dots G(\mathbf{R}_2, \mathbf{R}_1) G(\mathbf{R}_1, \mathbf{R}_0) \Psi(\mathbf{R}_0; 0)$$

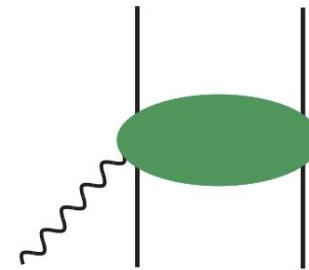
Model variation of charge form factors



Universality in magnetic densities



NV2+3-IIb*



$$\mu^{2b} = \int dr_{ij} 4\pi r_{ij}^2 \rho_M^{2b}(r_{ij})$$

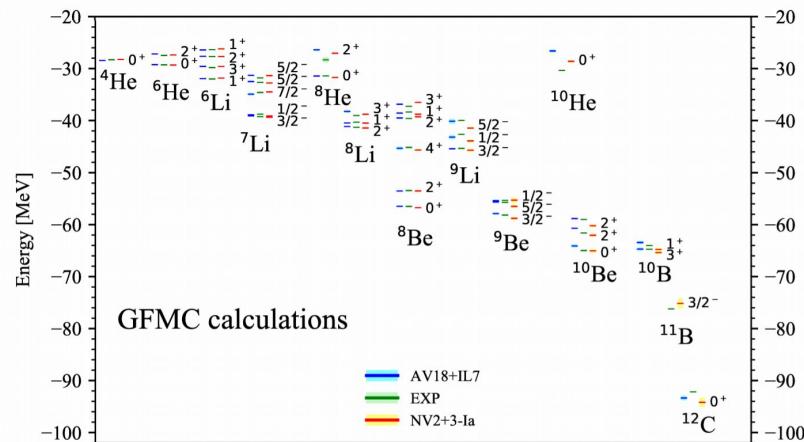
The Norfolk (NV2+3) interactions

Semi-phenomenological model based on xEFT with pion, nucleon, and delta degrees of freedom by Piarulli et al. [PRL 120, 052503 (2018)]

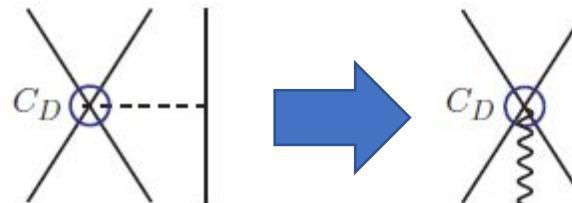
NV2 contains 26 unknown LECs in contacts, two more from the NV3

Eight model classes arrived at from different procedures to constrains the unknown LECs

$$H = \sum_i K_i + \sum_{i < j} v_{ij} + \sum_{i < j < k} V_{ijk}$$



Three-body LECs and sub-leading contact



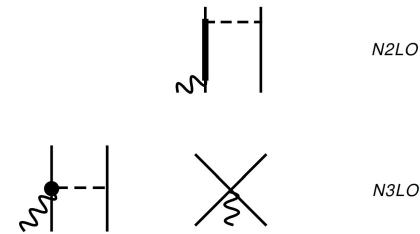
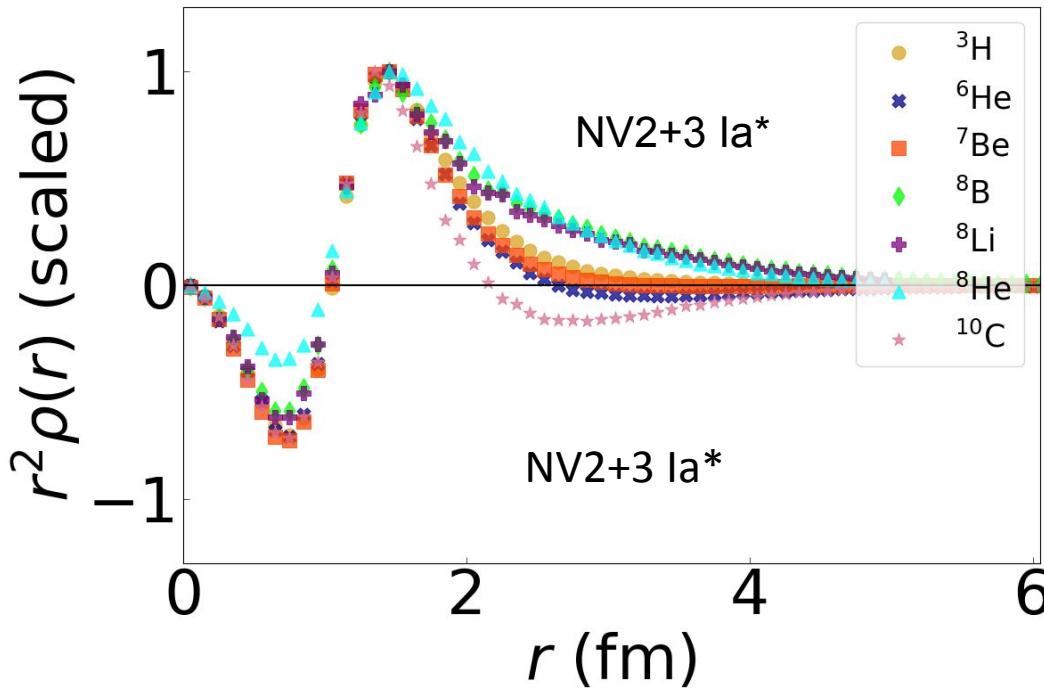
$$\mathbf{j}_{5,a}^{\text{N}3\text{LO}}(\mathbf{q}; \text{CT}) = z_0 \mathcal{O}_{ij}(\mathbf{q})$$

$$z_0 \propto (c_D + \text{known LECs})$$

Specific parameter in the **three-nucleon force** is **connected to** a parameter in the **two-body weak transition operator**

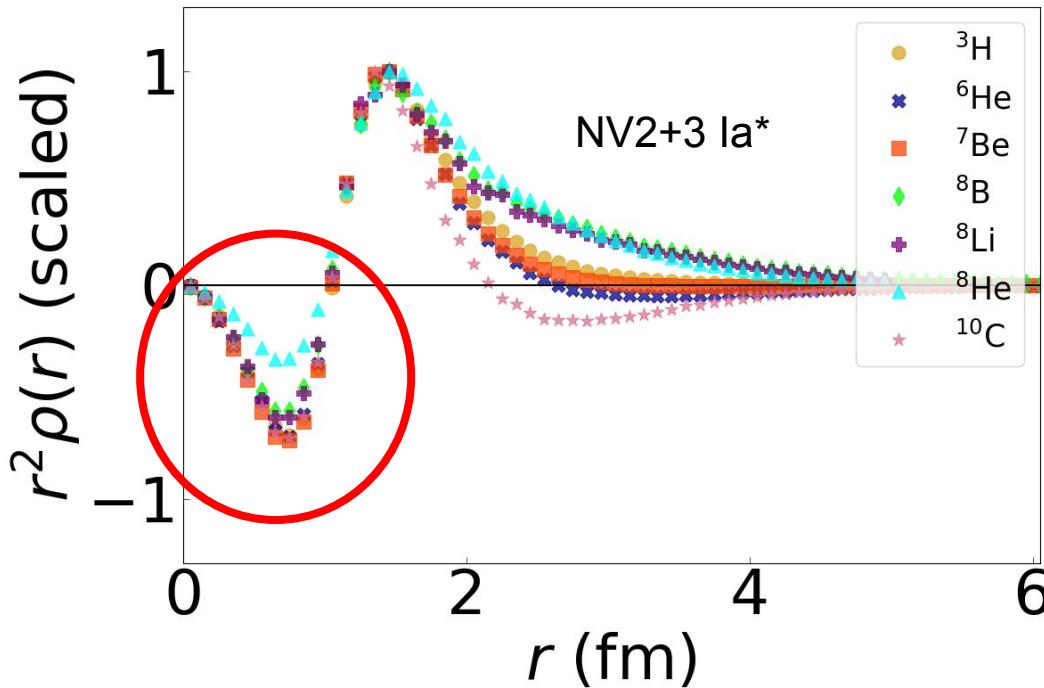
Short-range dynamics will depend on these values, influenced by fit

Scaled total two-body transition densities



$$M_{\text{GT}}^{2\text{b}} = \int dr_{ij} 4\pi r_{ij}^2 \rho_{\text{GT}}^{2\text{b}}(r_{ij})$$

Scaled total two-body transition densities

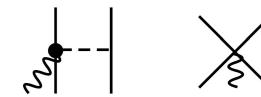


We can isolate the short-range contact piece

$$M_{\text{GT}}^{2\text{b}} = \int dr_{ij} 4\pi r_{ij}^2 \rho_{\text{GT}}^{2\text{b}}(r_{ij})$$

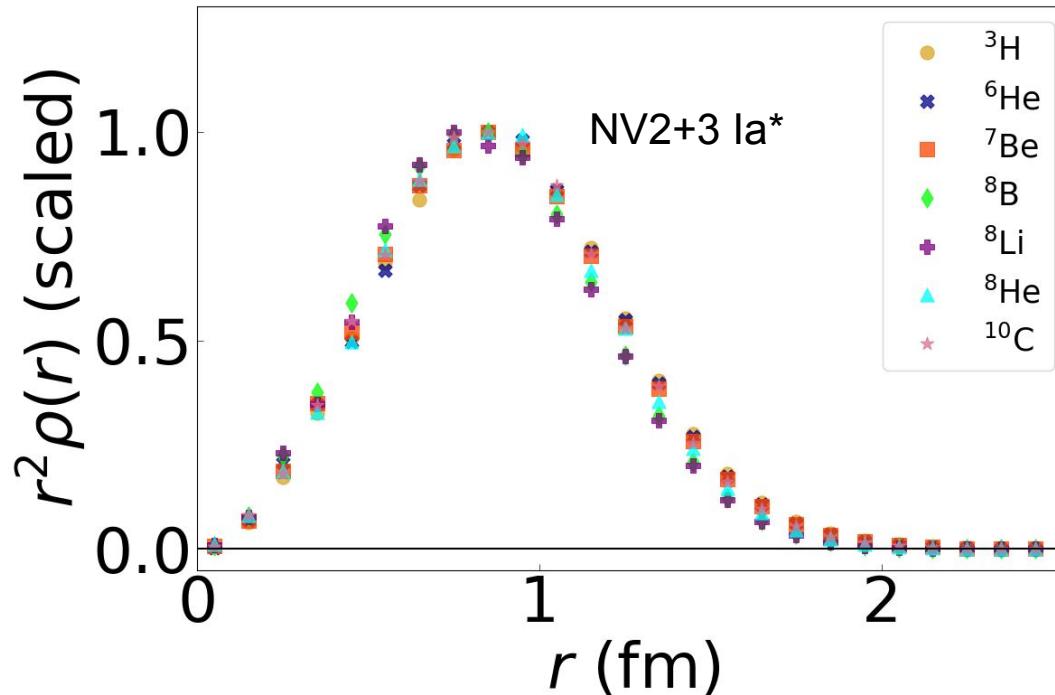


$N2\text{LO}$



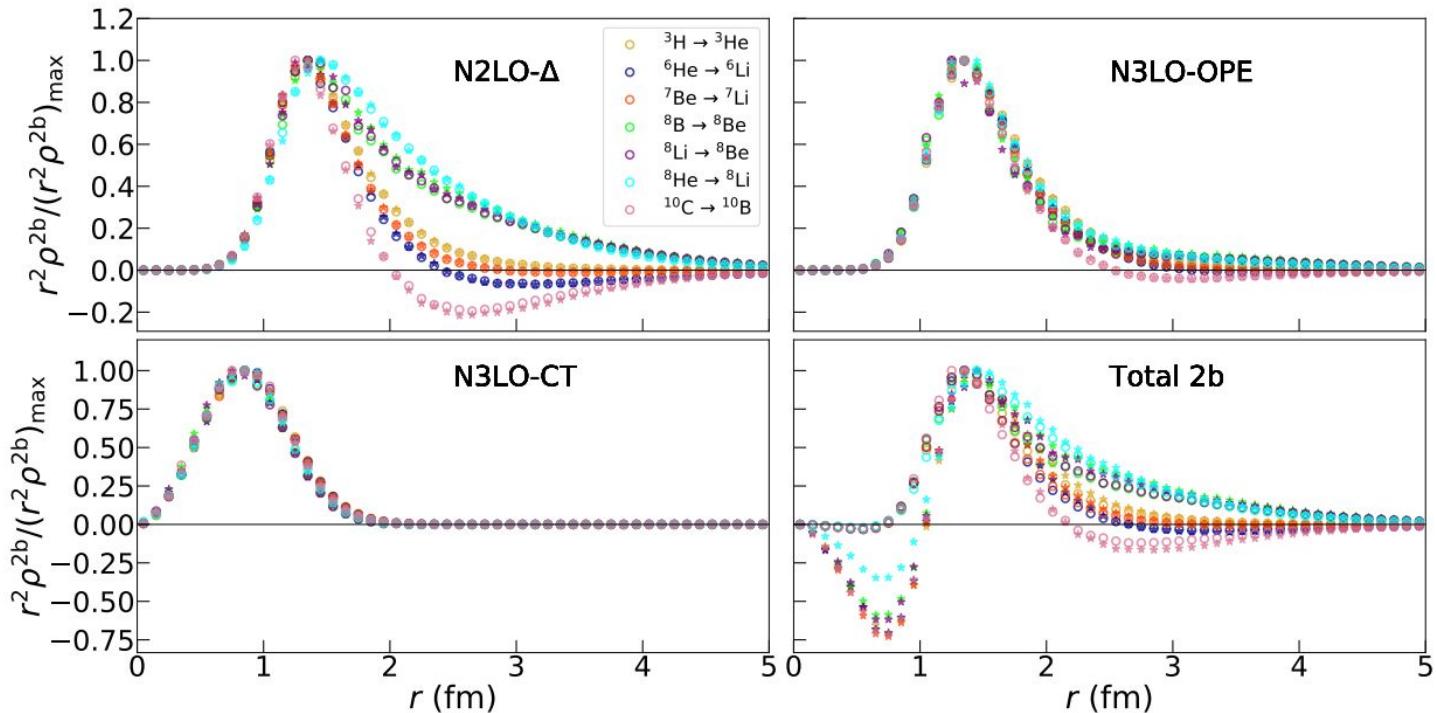
$N3\text{LO}$

Scaled contact two-body transition densities



$$M_{\text{GT}}^{\text{CT}} = \int dr_{ij} 4\pi r_{ij}^2 \rho_{\text{GT}}^{\text{CT}}(r_{ij})$$

Universal behavior in GT densities



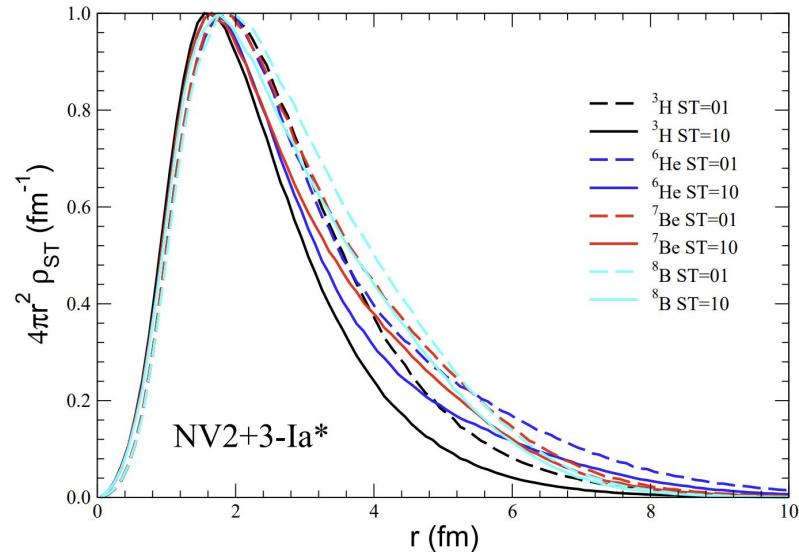
Interpreting universal and tail behaviors

Decay takes nn/np (ST=01/10) pair to an np/pp (ST=10/01) pair

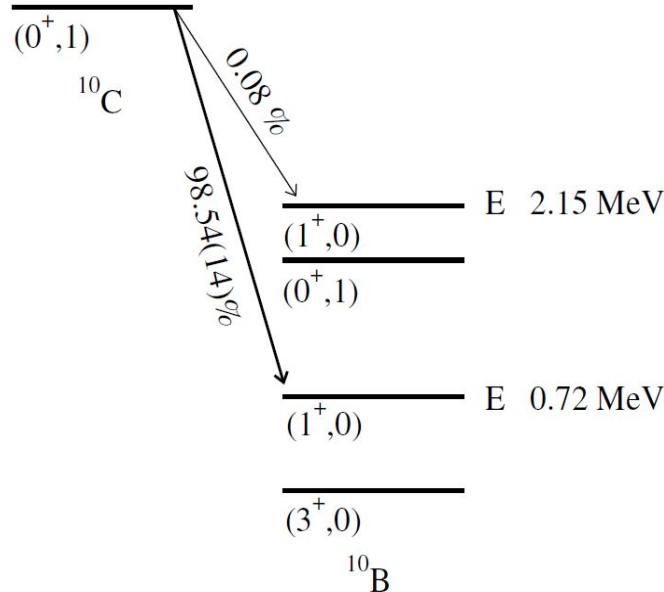
The ST=01 and 10 pair densities at short distances scale

Consequence of how pairs form in the nucleus

$$N_{ST} = \int dr_{ij} 4\pi r_{ij}^2 \rho_M^{2b}(r_{ij})$$



^{10}B β -decay



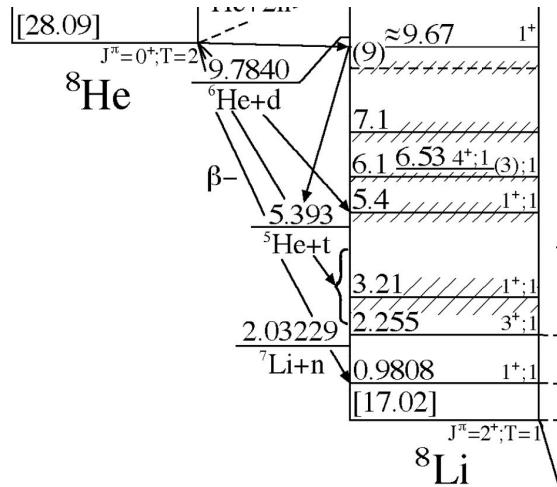
Two states of the same quantum numbers nearby

The result depends strongly on the LS mixing of the p -shell

Particularly sensitive to the 3S_1 and 3D_1 mixing because S to S produces a larger m.e. and ^{10}C is predominantly S wave

<https://nucldata.tunl.duke.edu/>

^8He β -decay



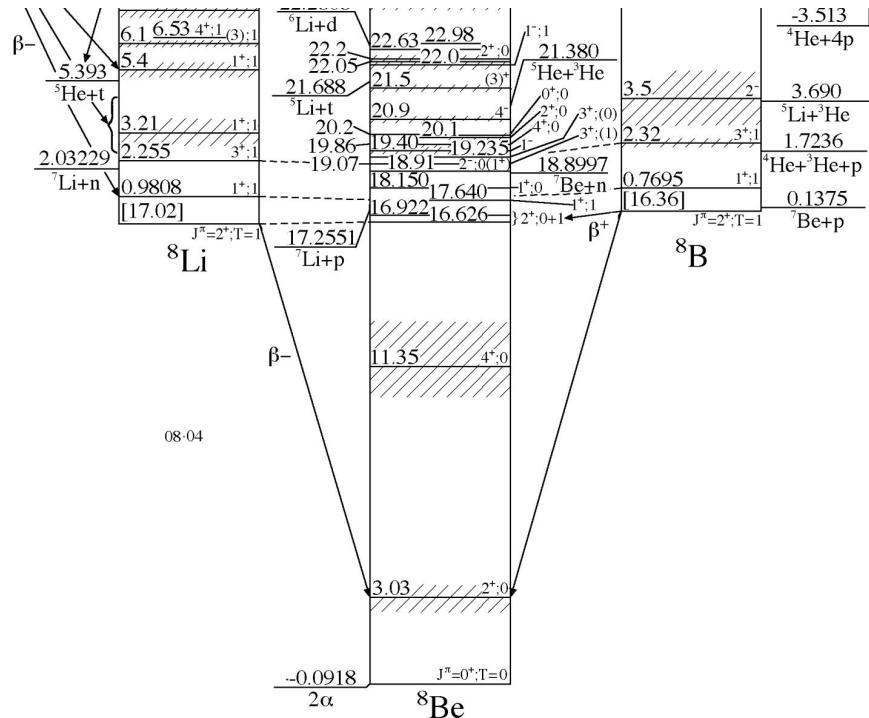
Three ($1^+; 1$) states within a few MeV

Different dominant spatial symmetries → sensitivity to the precise mixing of small components in the wave function

Improving the mixing of the small components in the ($1^+; 1$) states is crucial to getting an improved m.e.

<https://nucldata.tunl.duke.edu/>

A=8 level scheme



Computation of reduced multipoles

Reduced multipoles are defined by **[Carlson and Schiavilla RMP 70 (1998)]**:

$$\langle J_f M | \rho^\dagger(q) | J_i M \rangle = (-1)^{J_i - M} \sum_L \sqrt{4\pi} (-i)^L P_L(\cos \theta) c_{J_f J_i L}^M C_L(q),$$

$$\langle J_f M | \hat{e}_\lambda^* \cdot \mathbf{j}^\dagger(q) | J_i M \rangle = (-1)^{J_i - M + 1} \sum_{L \geq 1} \sqrt{8\pi^2} \frac{(-i)^L}{\sqrt{2L + 1}} Y_{LM}^*(\theta, \phi) c_{J_f J_i L}^M M_L(q)$$

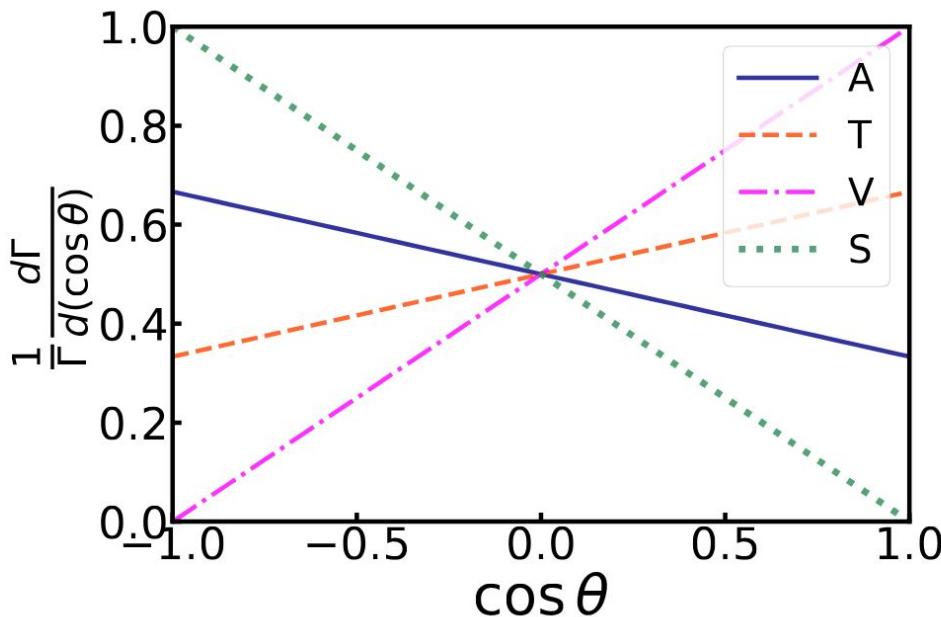
Cross section

$$\frac{d\sigma}{d\Omega} = 4\pi\sigma_M f_{\text{rec}}^{-1} \left[\frac{Q^4}{q^4} F_L^2(q) + \left(\frac{Q^2}{2q^2} + \tan^2 \theta_e/2 \right) F_T^2(q) \right]$$

In elastic scattering:

$$F_T^2(q) = F_M^2(q) = \frac{1}{2J_i + 1} \sum_{L=1}^{\infty} |\langle J_f || M_L(q) || J_i \rangle|^2 \quad F_L^2(q) = \frac{1}{2J_i + 1} \sum_{L=0}^{\infty} |\langle J_f || C_L(q) || J_i \rangle|^2$$

BSM current effects on decay correlations

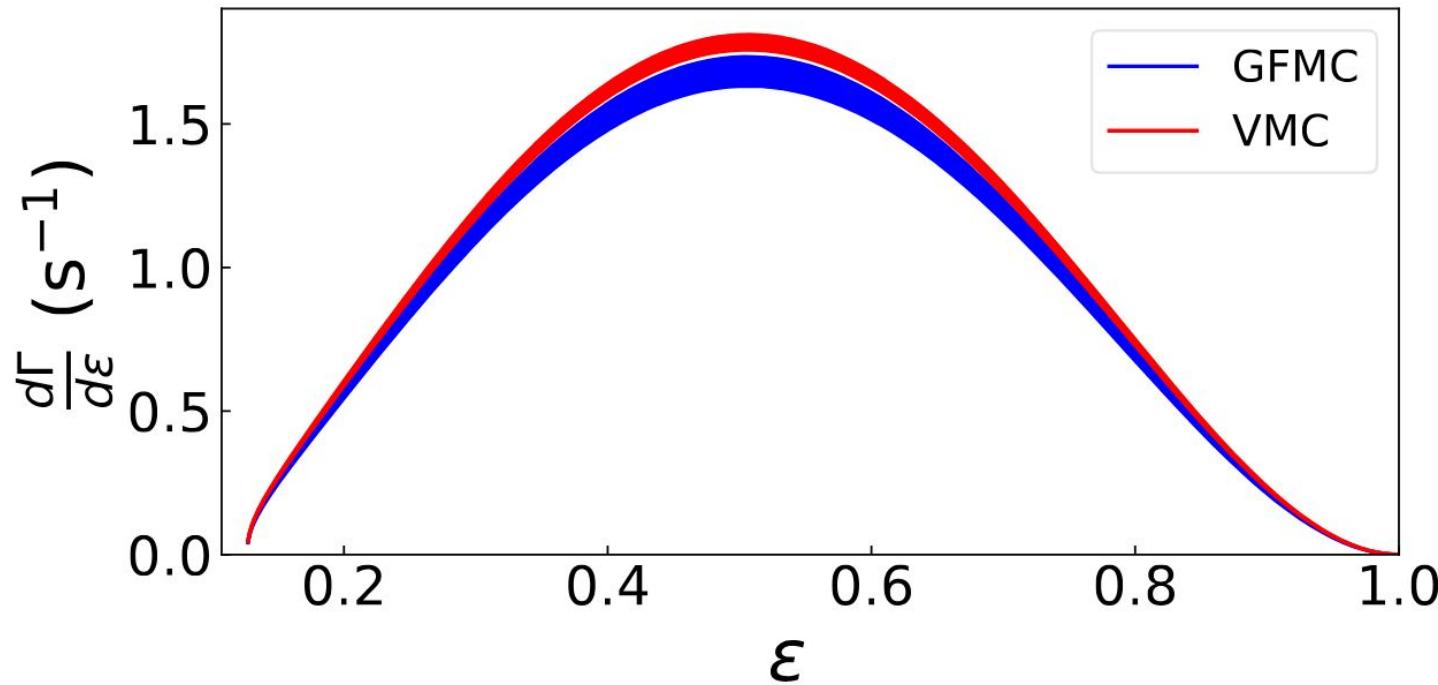


Axial, tensor, vector, and scalar currents preferentially emit electrons at certain angles

A/T, V/S interfere with one another in BSM scenarios

Tensor operator flips electron chirality \rightarrow interference at low energy, coherently sums with axial at large energy

${}^6\text{He}$ β -decay spectrum: Absolute spectrum



^6He β -decay spectrum: SM corrections

