

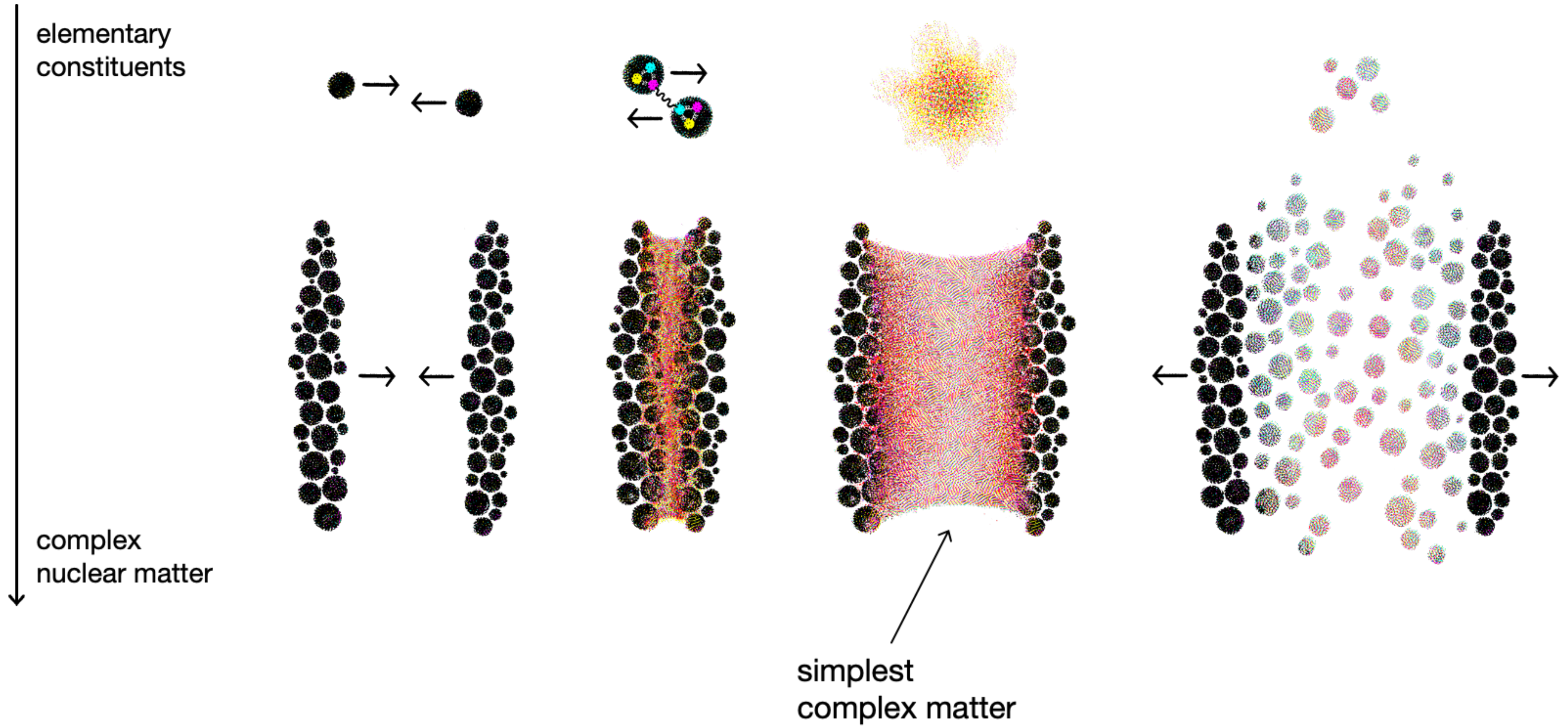
Jet quenching in anisotropic flowing matter

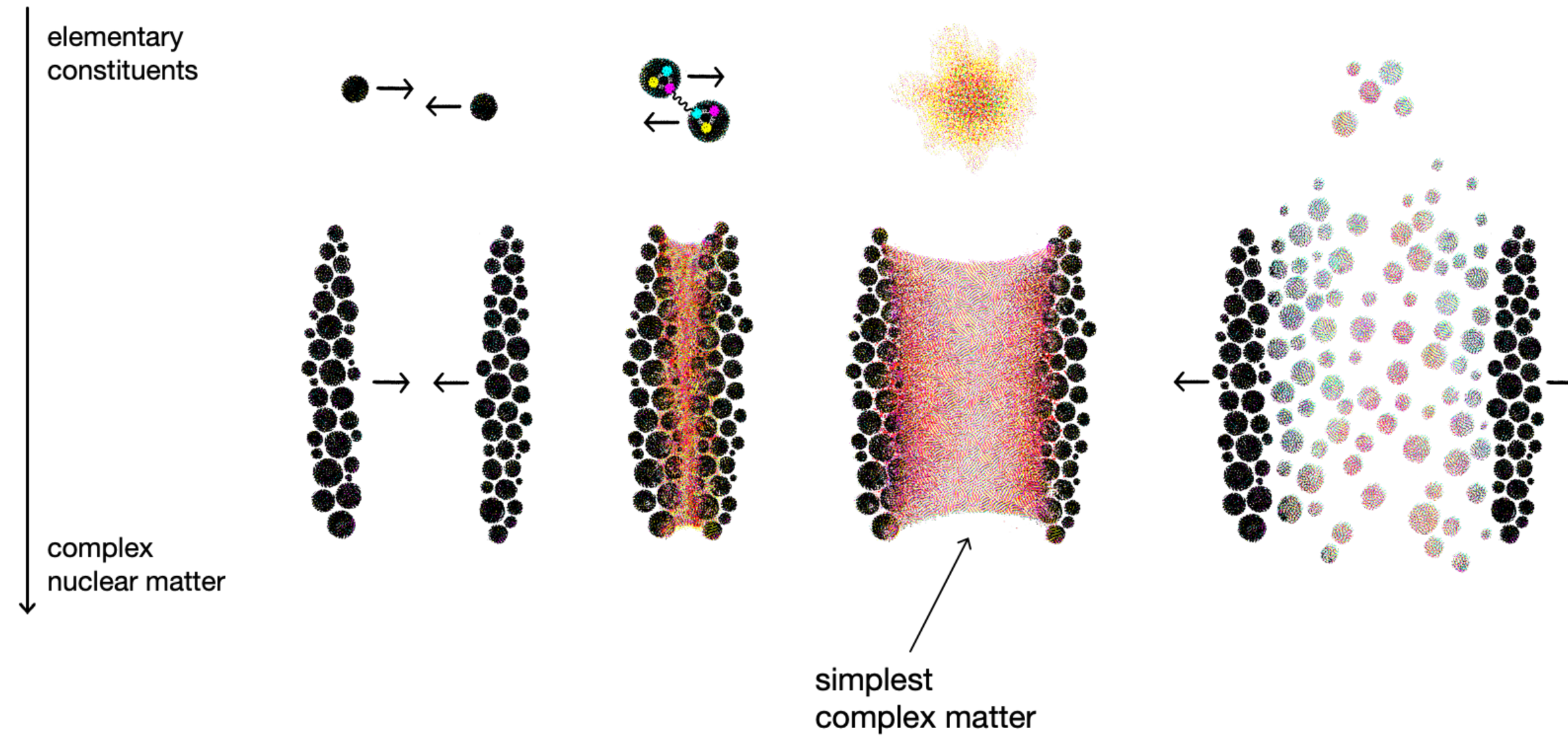
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17th October 2023, Seattle

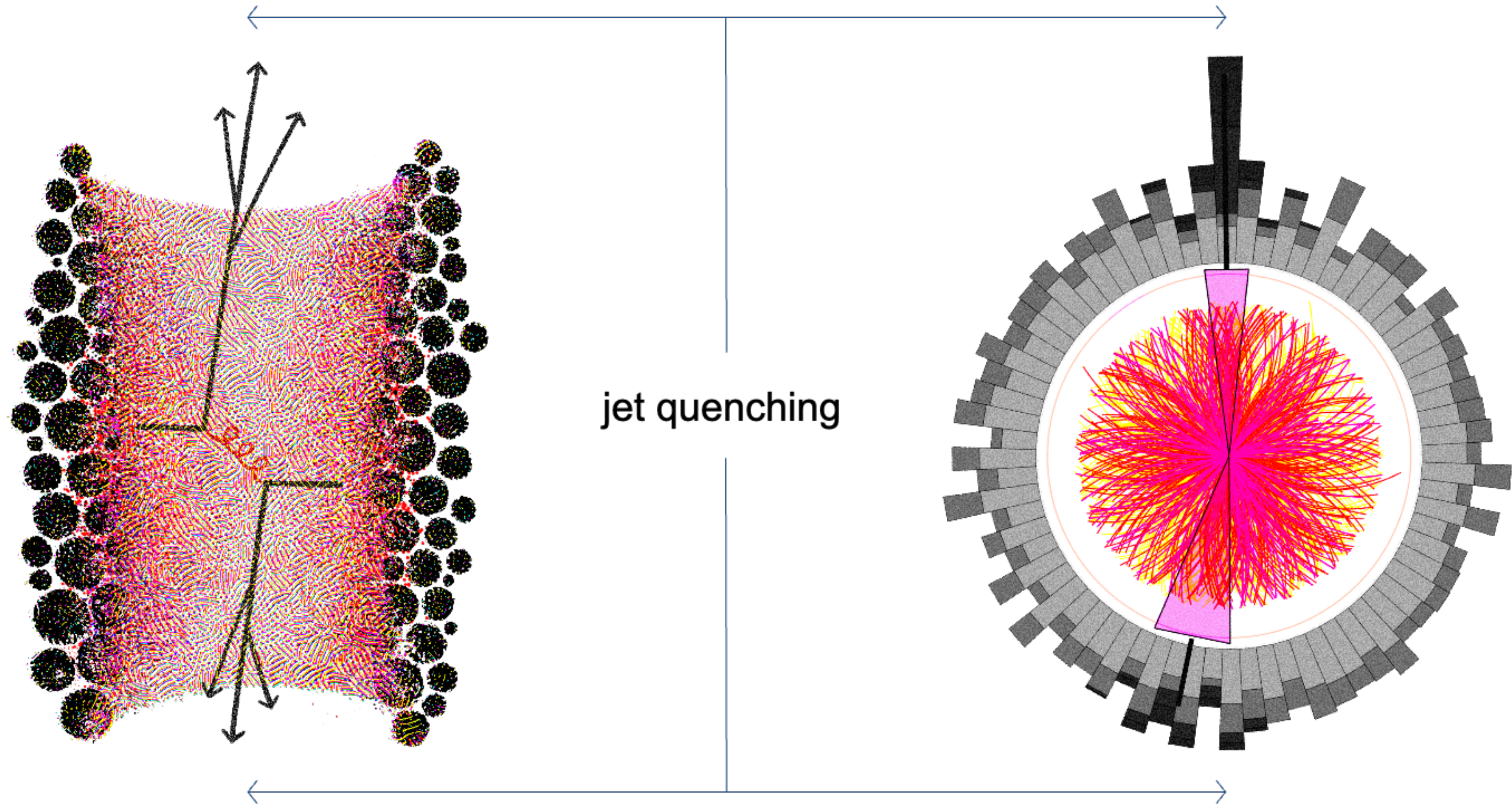
Mainly based on [2309.00683](#)



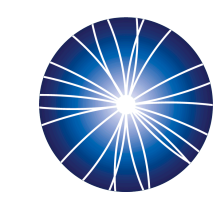


Two main sources of information:

- **Soft particle** coming from the thermal matter
- **Hard particle: jets, quarkonia...**



jets interact with the medium while propagating through it



Jet tomography

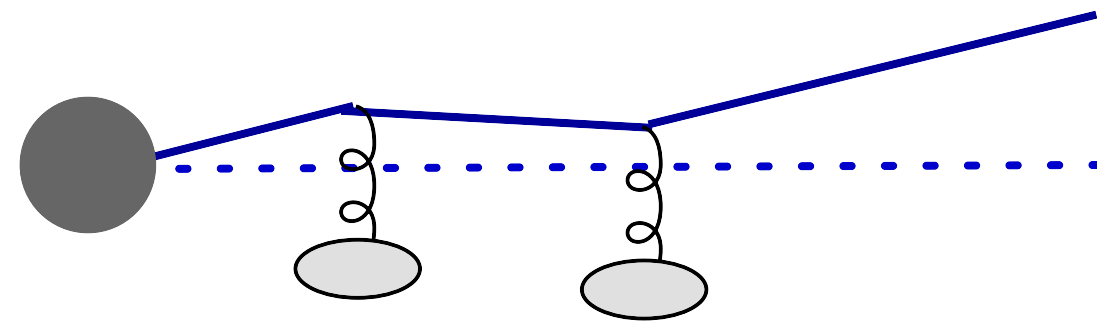
- Jet tomography: Jets as differential probes of the spatio-temporal structure of the thermal matter created in HIC
- Modification of jet properties throughout their flight encodes information about the QGP characteristics and evolution
- Most approaches to jet-medium interaction are either empirical or based on multiple simplifying assumptions

Do jets feel the transverse flow and anisotropies of the QGP?

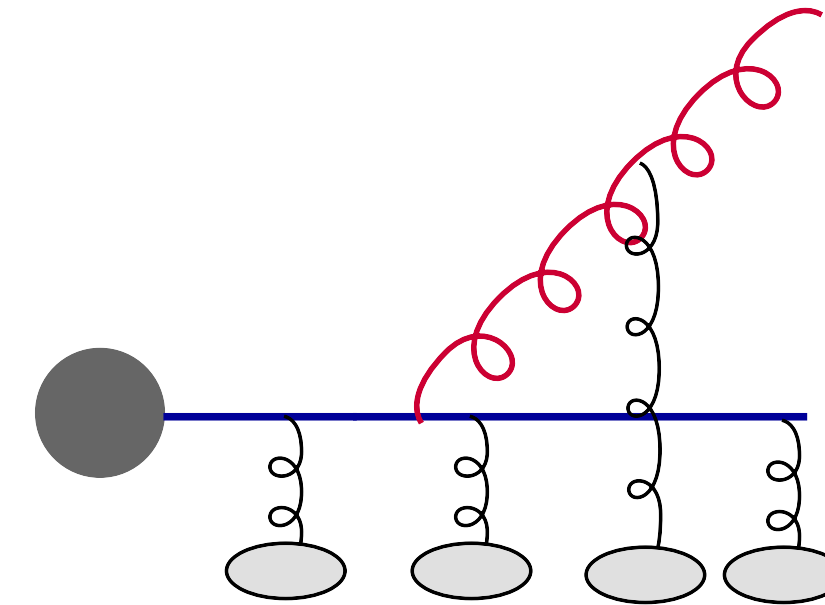


Focus on leading perturbative processes: Two processes that modify jets.

Single particle broadening



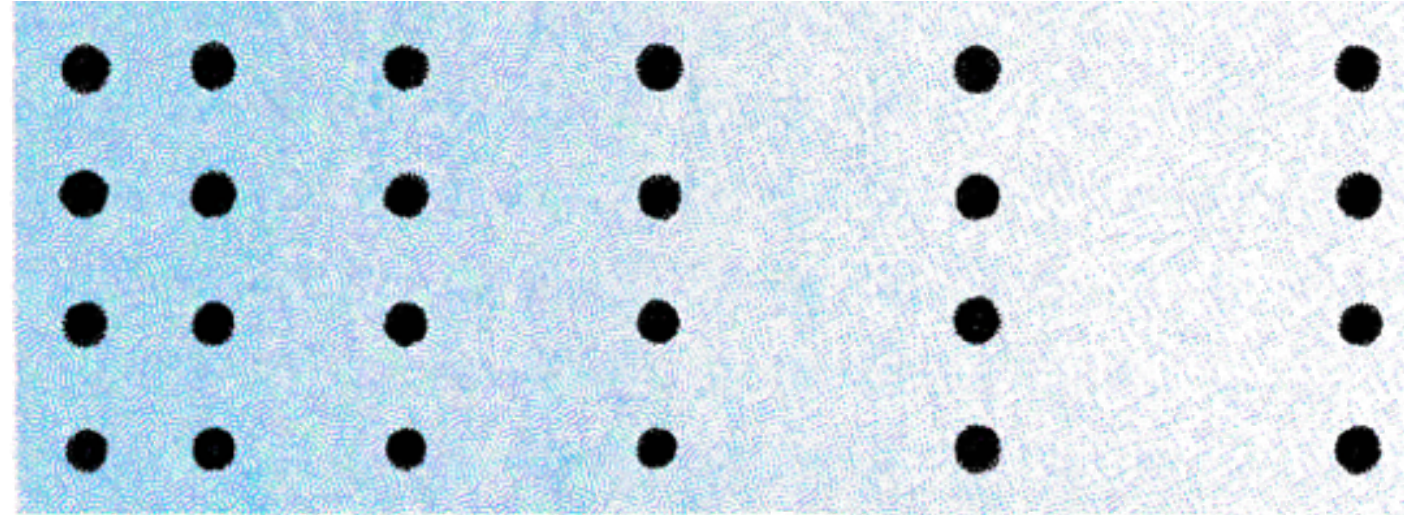
Medium induced gluon radiation



Theoretical formulation of jet quenching requires several assumptions to make it tractable. Some of the are

- Eikonal expansion; only sub-eikonal length enhanced terms are kept
- Medium is modeled by a background field
- In the simplest scenario the medium is **static** and **homogeneous**

The medium is modeled by a field created by a classical current of sources



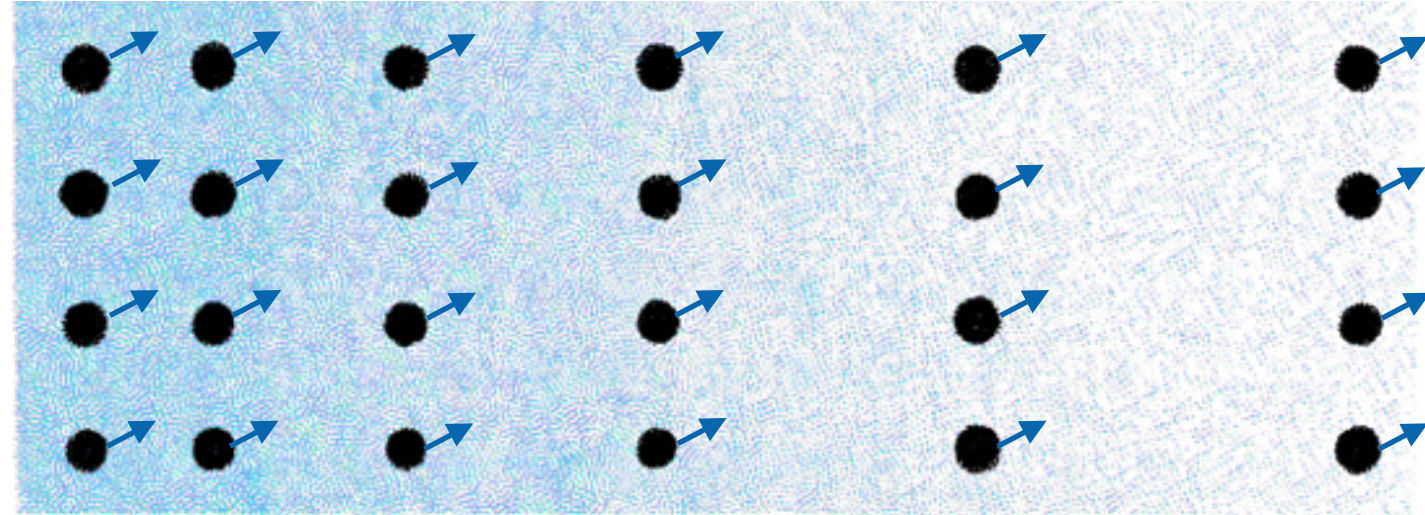
Heavy sources

The stochastic field can be written as

$$gA^{a\mu}(q) = \sum_i g^{\mu 0} e^{-iq \cdot x_i} t_i^a v_i(q) (2\pi) \delta(q_0)$$

- controls the jet-medium interaction
- controls de inhomogeneity

The medium is modeled by a field created by a classical current of sources



Heavy sources

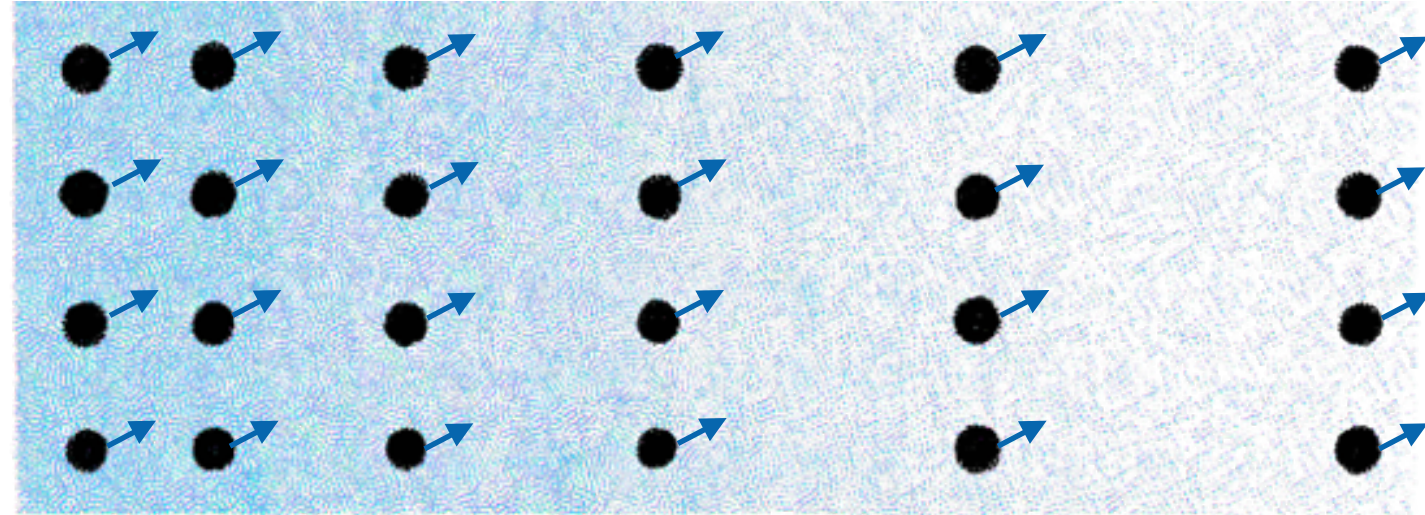
$$u_\mu = (1, \mathbf{u}, u_z)_\mu$$

The stochastic field can be written as

$$gA^{a\mu}(q) = \sum_i u_i^\mu e^{-iq \cdot x_i} t_i^a v_i(q) (2\pi) \delta(q_0 - \mathbf{q} \cdot \mathbf{u} - q_z u_z)$$

- controls the jet-medium interaction
- controls de inhomogeneity
- velocity of the sources

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Heavy sources

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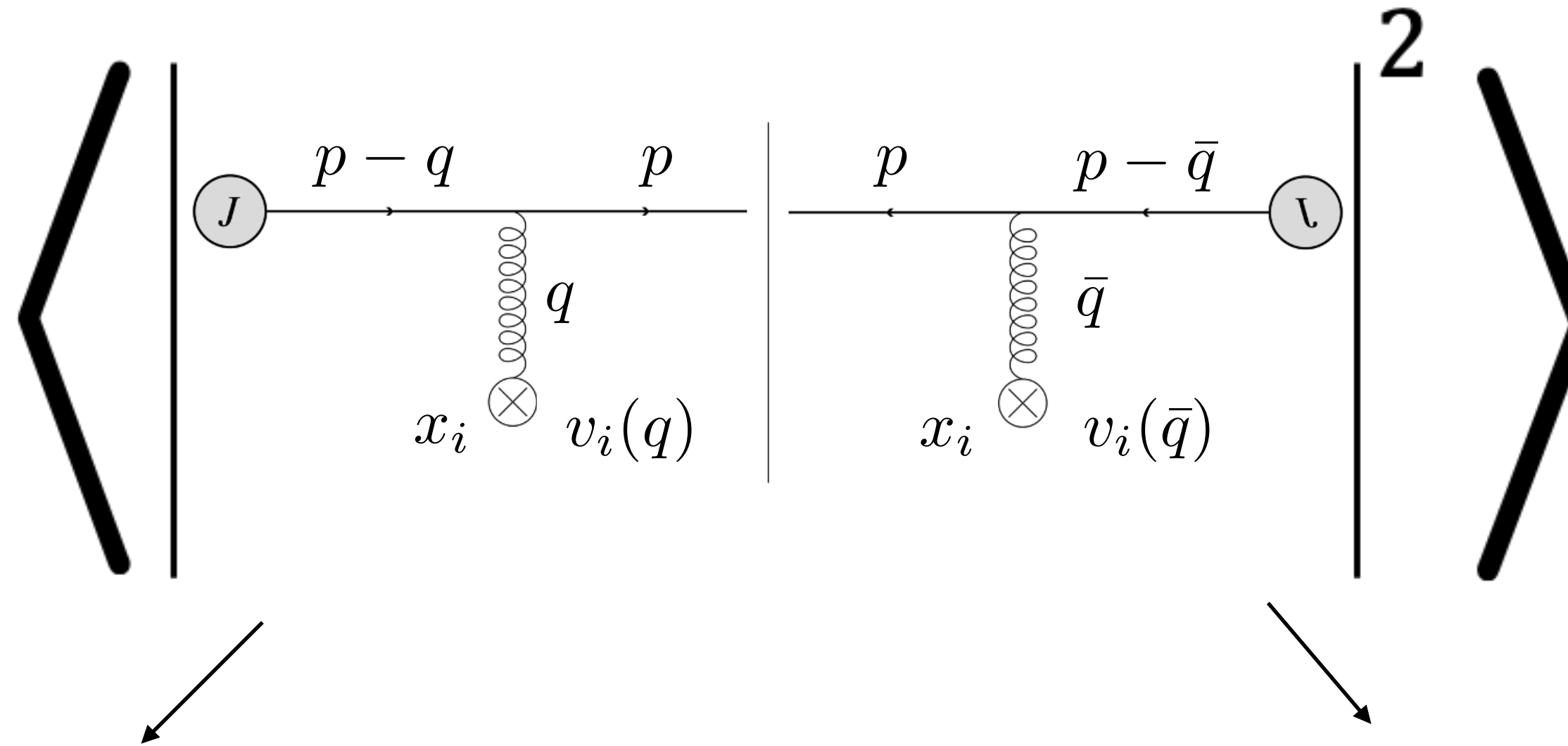
$$gA^{a\mu}(q) = \sum_i u_i^\mu e^{-iq \cdot x_i} t_i^a v_i(q) (2\pi) \delta(q_0 - \mathbf{q} \cdot \mathbf{u} - q_z u_z)$$

$$v_i(q) = \frac{g^2}{q^2 - \mu^2 + i\epsilon}$$

- controls the jet-medium interaction
- controls de inhomogeneity
- velocity of the sources

Stochastic field \longrightarrow need to specify the average over its configurations \longrightarrow Gaussian statistics

$$gA^{a\mu}(q) = \sum_i u_i^\mu e^{-iq \cdot x_i} t_i^a v_i(q) (2\pi) \delta(q_0 - \mathbf{q} \cdot \mathbf{u} - q_z u_z)$$



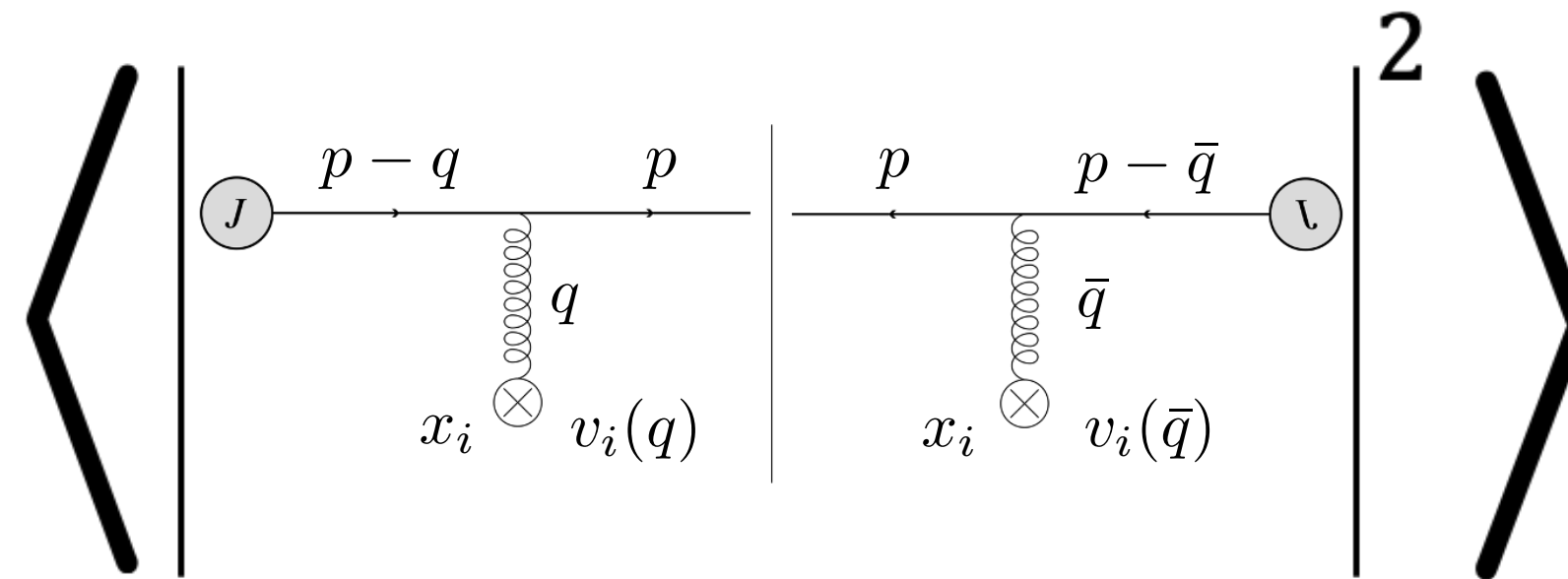
Colour neutrality

$$\langle A^a(q) A^b(\bar{q}) \rangle \sim \langle t_i^a t_j^b \rangle = C \delta_{ij} \delta^{ab}$$

Source averaging

$$\sum_i = \int d^2 \mathbf{x} dz \rho(\mathbf{x}, z)$$

Hydrodynamic variables, $g(\mathbf{x}, z)$, encode the matter structure: $g(\mathbf{x}, z) \equiv \rho(\mathbf{x}, z) \quad \mu^2(\mathbf{x}, z) \quad \mathbf{u}(\mathbf{x}, z) \quad u_z(\mathbf{x}, z)$



Transversely homogeneous matter :

$$g(\mathbf{x}, z) \simeq g(z)$$

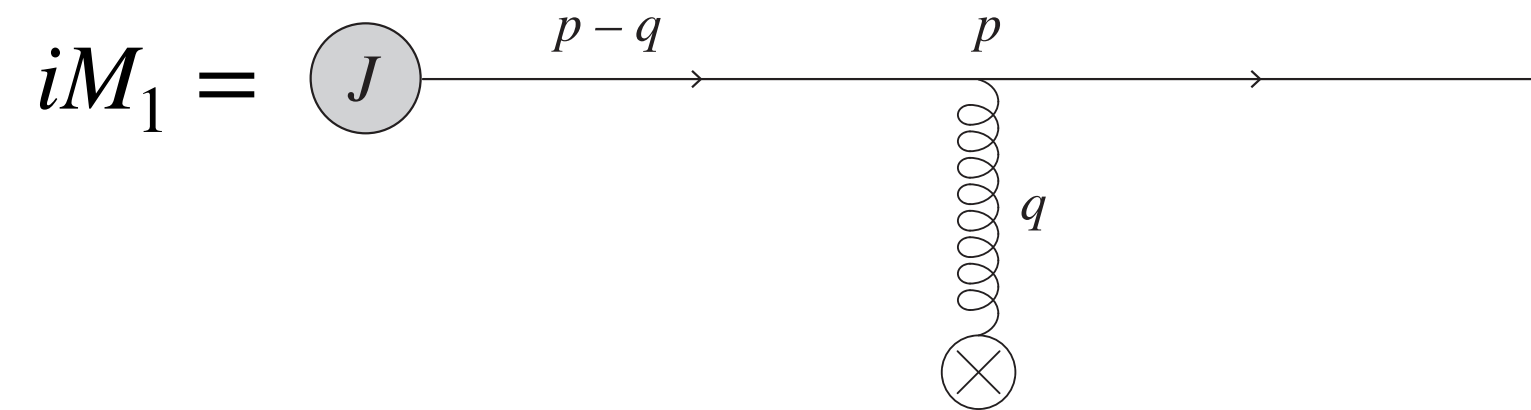
$$\int_{\mathbf{x}} g(z) e^{-i(\mathbf{q} \pm \bar{\mathbf{q}}) \cdot \mathbf{x}} = g(z) (2\pi)^2 \delta^{(2)}(\mathbf{q} \pm \bar{\mathbf{q}})$$

Transversely inhomogeneous matter :

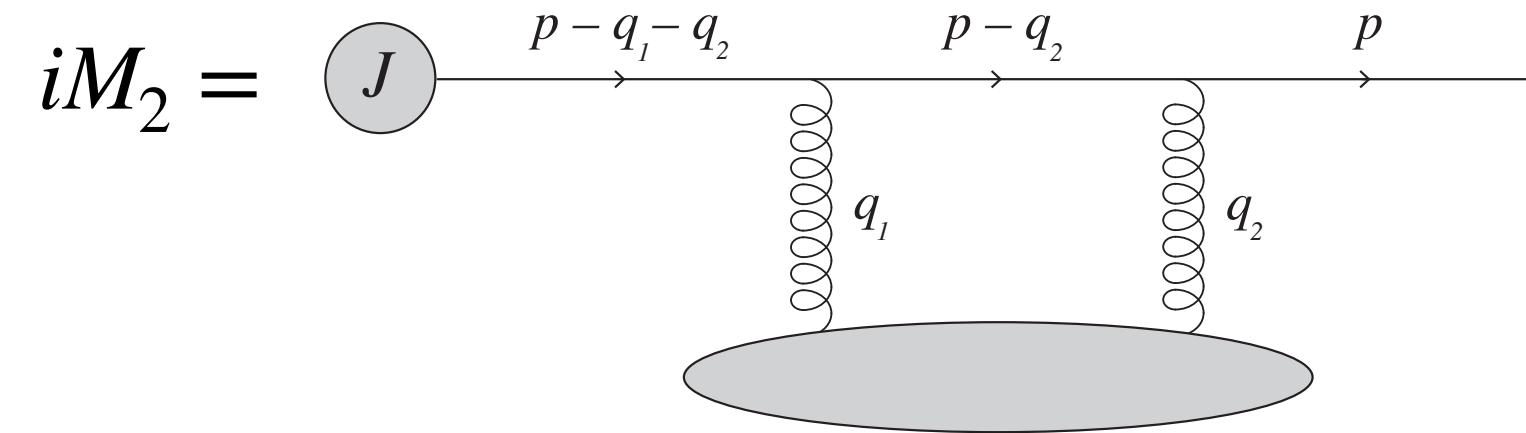
$$g(\mathbf{x}, z) \simeq g(z) + \nabla_{\alpha} g(z) \mathbf{x}_{\alpha}$$

$$\int_{\mathbf{x}} \nabla_{\alpha} g(z) \mathbf{x}_{\alpha} e^{-i(\mathbf{q} \pm \bar{\mathbf{q}}) \cdot \mathbf{x}} = i \nabla_{\alpha} g(z) (2\pi)^2 \frac{\partial}{\partial (\mathbf{q} \pm \bar{\mathbf{q}})_{\alpha}} \delta^{(2)}(\mathbf{q} \pm \bar{\mathbf{q}})$$

Two diagrams to compute



Single-Born contribution



Double-Born contribution

$$\langle |M|^2 \rangle = \langle |M_0|^2 \rangle + \langle |M_1|^2 \rangle + \langle M_2 M_0^* \rangle + \langle M_2^* M_0 \rangle$$

Some assumption

- Only first subeikonal corrections are kept
- Dilute and extended medium $\mu \Delta z \gg 1$

The final state parton distribution

$$E \frac{d\mathcal{N}}{d^2pdE} \equiv \frac{1}{2(2\pi)^3} \langle |M|^2 \rangle$$

The final state parton distribution

$$\begin{aligned}
 E \frac{d\mathcal{N}}{d^2p dE} = & E \frac{d\mathcal{N}^{(0)}}{d^2p dE} + \mathcal{C} \int_0^L dz \int_{\mathbf{q}} \left\{ \left[1 - \hat{\mathbf{g}}_\alpha \frac{(\mathbf{u}E - \mathbf{p} + \mathbf{q})_\alpha z}{(1 - u_z)E} \right] [1 + \mathbf{u} \cdot \mathbf{\Gamma}(\mathbf{q})] E \frac{d\mathcal{N}^{(0)}}{d^2(p - \mathbf{q}) dE} \right. \\
 & - \left[1 - \hat{\mathbf{g}}_\alpha \frac{(\mathbf{u}E - \mathbf{p})_\alpha z}{(1 - u_z)E} \right] [1 + \mathbf{u} \cdot \mathbf{\Gamma}_{DB}(\mathbf{q})] E \frac{d\mathcal{N}^{(0)}}{d^2p dE} \\
 & \left. - \frac{1}{2} \hat{\mathbf{g}}_\alpha \frac{\partial}{\partial p_\alpha} E \frac{d\mathcal{N}^{(0)}}{d^2p dE} \frac{\pi g^4 \sqrt{1 - \mathbf{u}^2 - u_z^2}}{2\mu(1 - u_z)E} \frac{\delta^{(2)}(\mathbf{q})}{[v(\mathbf{q}^2)]^2} \right\} \rho(z) [v(\mathbf{q}^2)]^2
 \end{aligned}$$

Initial distribution

$$E \frac{d\mathcal{N}^0}{d^2p dE} \equiv \frac{1}{2(2\pi)^3} |J(E, \mathbf{p})|^2$$

The final state parton distribution

Flow corrections

Gradient corrections

$$\begin{aligned}
 E \frac{d\mathcal{N}}{d^2p dE} = & E \frac{d\mathcal{N}^{(0)}}{d^2p dE} + \mathcal{C} \int_0^L dz \int_{\mathbf{q}} \left\{ \left[1 - \hat{g}_\alpha \frac{(\mathbf{u}E - \mathbf{p} + \mathbf{q})_\alpha z}{(1 - u_z)E} \right] \left[1 + \mathbf{u} \cdot \boldsymbol{\Gamma}(\mathbf{q}) \right] E \frac{d\mathcal{N}^{(0)}}{d^2(p - \mathbf{q}) dE} \right. \\
 & - \left[1 - \hat{g}_\alpha \frac{(\mathbf{u}E - \mathbf{p})_\alpha z}{(1 - u_z)E} \right] \left[1 + \mathbf{u} \cdot \boldsymbol{\Gamma}_{DB}(\mathbf{q}) \right] E \frac{d\mathcal{N}^{(0)}}{d^2p dE} \\
 & \left. - \frac{1}{2} \hat{g}_\alpha \frac{\partial}{\partial p_\alpha} E \frac{d\mathcal{N}^{(0)}}{d^2p dE} \frac{\pi g^4 \sqrt{1 - \mathbf{u}^2 - u_z^2}}{2\mu(1 - u_z)E} \frac{\delta^{(2)}(\mathbf{q})}{[v(\mathbf{q}^2)]^2} \right\} \rho(z) [v(\mathbf{q}^2)]^2
 \end{aligned}$$

Initial distribution

$$E \frac{d\mathcal{N}^0}{d^2p dE} \equiv \frac{1}{2(2\pi)^3} |J(E, \mathbf{p})|^2$$

The final state parton distribution

- Flow corrections
- Gradient corrections

$$\hat{g}_\alpha = \sum_g \left(\nabla_\alpha g \frac{\delta}{\delta g} \right)$$

$$E \frac{d\mathcal{N}}{d^2p dE} = E \frac{d\mathcal{N}^{(0)}}{d^2p dE} + \mathcal{C} \int_0^L dz \int_{\mathbf{q}} \left\{ \left[1 - \hat{g}_\alpha \frac{(\mathbf{u}E - \mathbf{p} + \mathbf{q})_\alpha z}{(1 - u_z)E} \right] \left[1 + \mathbf{u} \cdot \boldsymbol{\Gamma}(\mathbf{q}) \right] E \frac{d\mathcal{N}^{(0)}}{d^2(p - \mathbf{q}) dE} \right. \\ \left. - \left[1 - \hat{g}_\alpha \frac{(\mathbf{u}E - \mathbf{p})_\alpha z}{(1 - u_z)E} \right] \left[1 + \mathbf{u} \cdot \boldsymbol{\Gamma}_{DB}(\mathbf{q}) \right] E \frac{d\mathcal{N}^{(0)}}{d^2p dE} \right. \\ \left. - \frac{1}{2} \hat{g}_\alpha \frac{\partial}{\partial p_\alpha} E \frac{d\mathcal{N}^{(0)}}{d^2p dE} \frac{\pi g^4 \sqrt{1 - \mathbf{u}^2 - u_z^2}}{2\mu(1 - u_z)E} \frac{\delta^{(2)}(\mathbf{q})}{[v(\mathbf{q}^2)]^2} \right\} \rho(z) [v(\mathbf{q}^2)]^2$$

■ Initial distribution

$$E \frac{d\mathcal{N}^0}{d^2p dE} \equiv \frac{1}{2(2\pi)^3} |J(E, \mathbf{p})|^2$$

Definition of the moments

$$\langle \mathbf{p}_{\alpha_1} \cdots \mathbf{p}_{\alpha_n} \rangle \equiv \frac{\int_{\mathbf{p}} (\mathbf{p}_{\alpha_1} \cdots \mathbf{p}_{\alpha_n}) E \frac{d\mathcal{N}}{d^2p dE}}{\int_{\mathbf{p}} E \frac{d\mathcal{N}^{(0)}}{d^2p dE}}$$

and

$$E \frac{d\mathcal{N}^{(0)}}{d^2p dE} = \frac{f(E)}{2\pi w^2} e^{-\frac{\mathbf{p}^2}{2w^2}}$$

Definition of the moments $\langle \mathbf{p}_{\alpha_1} \dots \mathbf{p}_{\alpha_n} \rangle \equiv \frac{\int_{\mathbf{p}} (\mathbf{p}_{\alpha_1} \dots \mathbf{p}_{\alpha_n}) E \frac{d\mathcal{N}}{d^2p dE}}{\int_{\mathbf{p}} E \frac{d\mathcal{N}^{(0)}}{d^2p dE}}$ and $E \frac{d\mathcal{N}^{(0)}}{d^2p dE} = \frac{f(E)}{2\pi w^2} e^{-\frac{\mathbf{p}^2}{2w^2}}$

• Leading odd moments

$$\langle \mathbf{p}_\alpha \rangle = -\frac{1}{2} \mathcal{C} \int_0^L dz \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \rho(z) \frac{u_\alpha}{(1 - u_z) E} \int_{\mathbf{q}} \mathbf{q}^2 \left[E \frac{f'(E)}{f(E)} + \mathbf{q}^2 \frac{\partial}{\partial \mathbf{q}^2} \right] [v(\mathbf{q}^2)]^2$$

$$+ \mathcal{C} \int_0^L dz \hat{\mathbf{g}}_\alpha \frac{\pi g^4 \rho(z) \sqrt{1 - \mathbf{u}^2 - u_z^2}}{4\mu(1 - u_z) E}$$

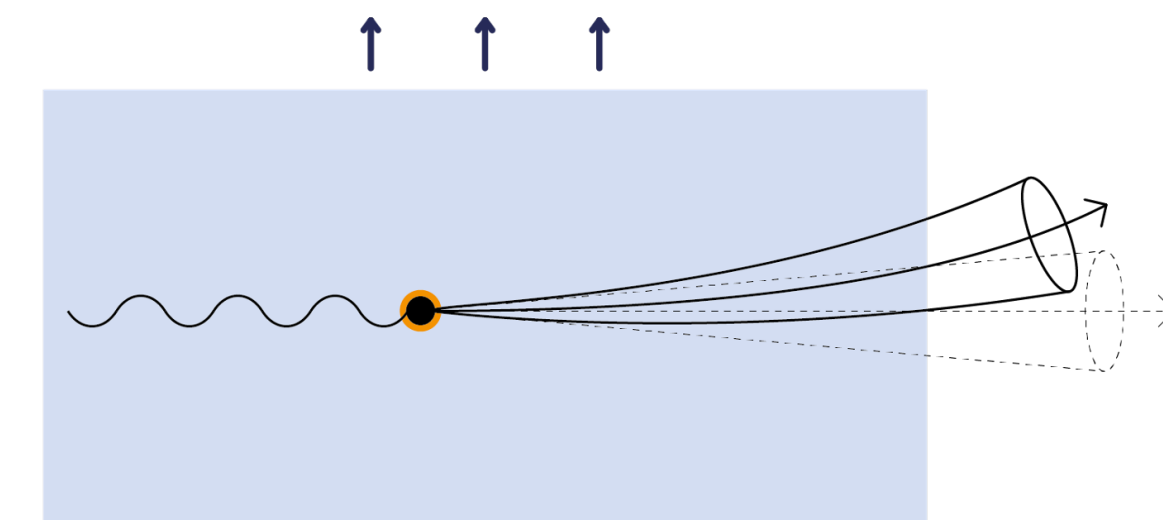
$$\langle \mathbf{p}_\alpha \mathbf{p}^2 \rangle = \mathcal{C} \int_0^L dz \int_{\mathbf{q}} \left\{ \hat{\mathbf{g}}_\alpha 2w^2 \left[z \frac{\mathbf{q}^2}{(1 - u_z) E} + \frac{\delta^{(2)}(\mathbf{q})}{[v(\mathbf{q}^2)]^2} \frac{\pi g^4 \sqrt{1 - \mathbf{u}^2 - u_z^2}}{2\mu(1 - u_z) E} \right] \right.$$

$$- \frac{1}{2} \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \frac{u_\alpha}{(1 - u_z) E}$$

$$\left. \times \mathbf{q}^2 \left[8w^2 + (10w^2 + \mathbf{q}^2) \mathbf{q}^2 \frac{\partial}{\partial \mathbf{q}^2} + (4w^2 + \mathbf{q}^2) E \frac{f'(E)}{f(E)} \right] \right\} \rho(z) [v(\mathbf{q}^2)]^2$$

Along the flow

Along the gradients



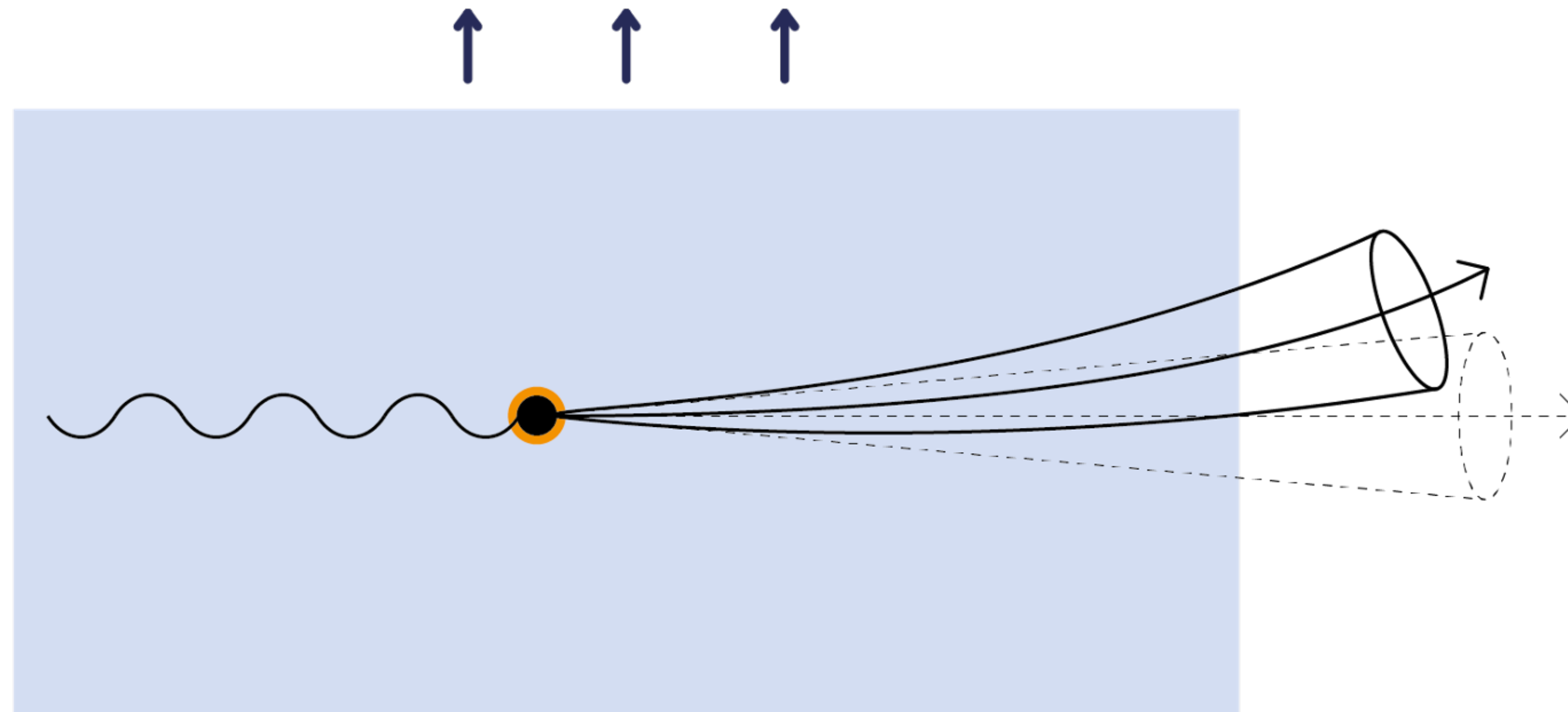
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and

$$E \frac{d\mathcal{N}^{(0)}}{d^2p dE} = \frac{f(E)}{2\pi w^2} e^{-\frac{\mathbf{p}^2}{2w^2}}$$

- Leading odd moments



Jets do feel flow and anisotropies

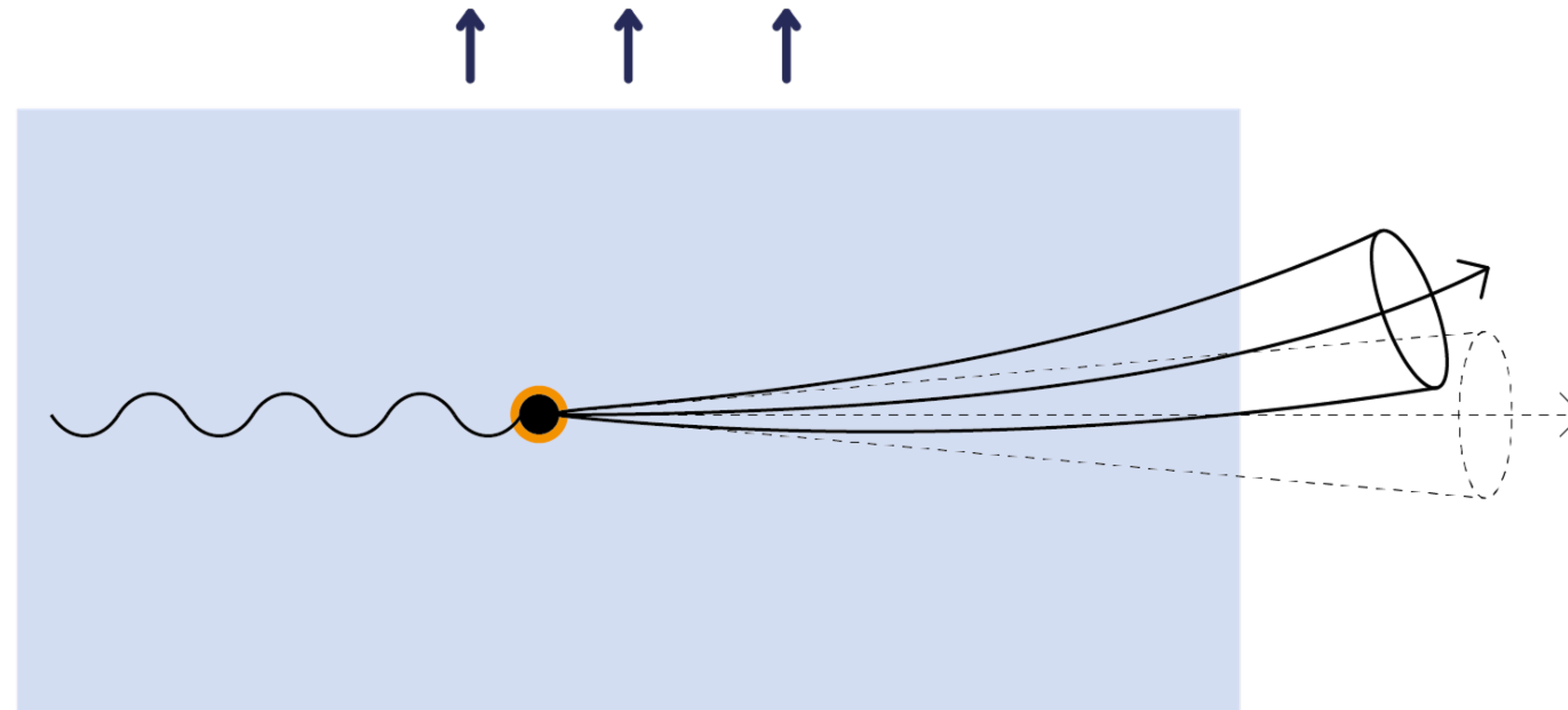
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- Leading odd moments



Agreement with previous results

Sadofyev et al. [2104.09513](#)
Barata et al. [2202.08847](#)
Andres et al. [2207.07141](#)

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- Quadratic moment of the distribution

$$\langle \mathbf{p}^2 \rangle = 2w^2 + \mathcal{C} \int_0^L dz \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \rho(z) \int_{\mathbf{q}} \mathbf{q}^2 [v(\mathbf{q}^2)]^2$$

$$\frac{\delta}{\delta L} \downarrow$$

$$\hat{q}(z) = \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \mathcal{C} \rho(z) \int_{\mathbf{q}} \mathbf{q}^2 [v(\mathbf{q}^2)]^2$$

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$$\frac{\delta}{\delta L} \downarrow$$

$$\hat{q}(z) = \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \hat{q}_0(z)$$

Rough estimation of the effect

$$\hat{q}(z) = \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \hat{q}_0(z)$$

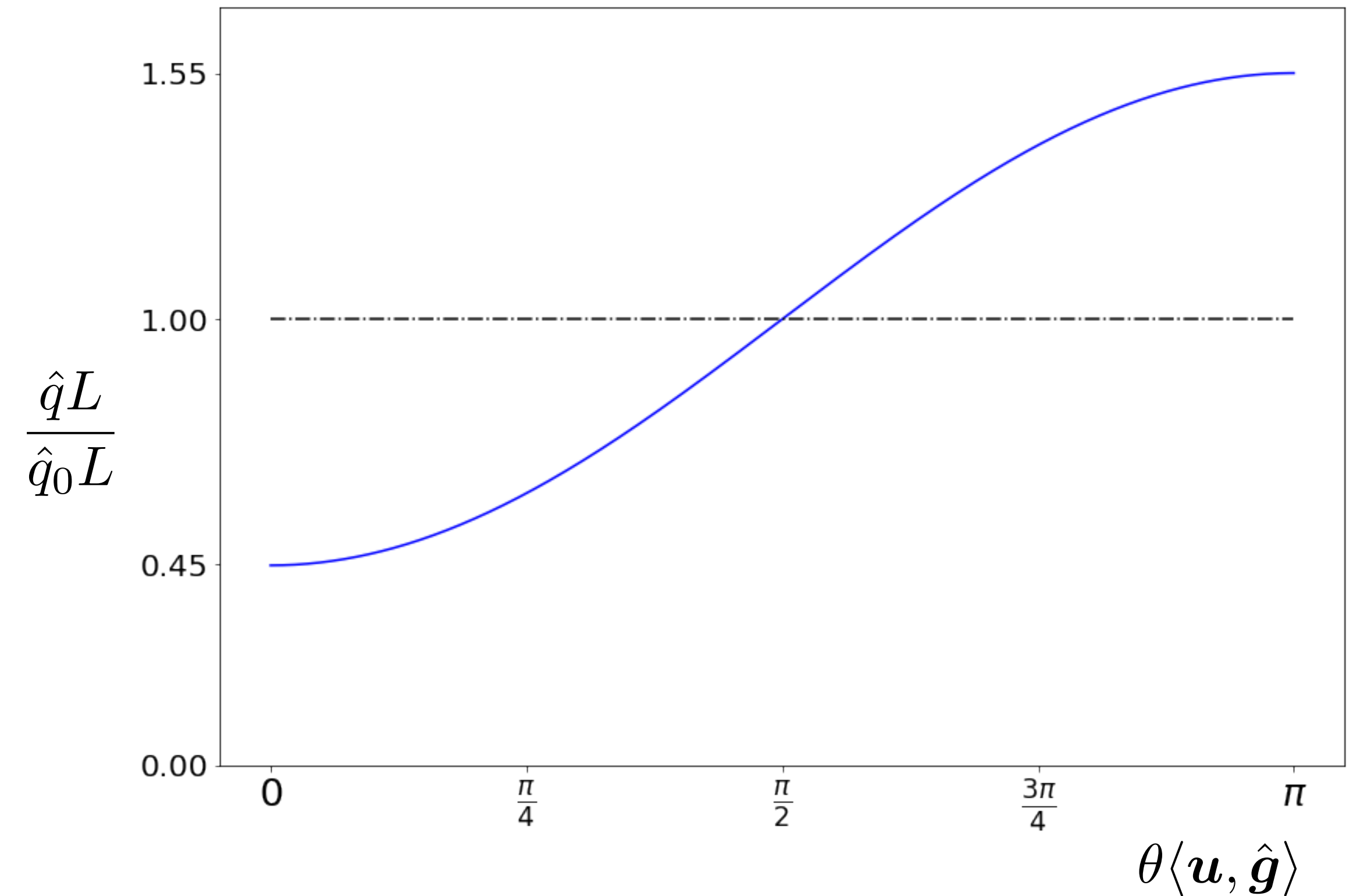
- Only gradients of temperature to leading logarithm
- Everything z - independent

$$\hat{q}L = \left[1 - \frac{L}{2} \frac{\nabla \rho}{\rho} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \hat{q}_0 L$$

Chosen parameters

$$L \simeq 5 \text{ fm} \quad \left| \frac{\nabla T}{T^2} \right| \simeq 0.05$$

$$T \simeq 0.3 \text{ GeV} \quad u \simeq 0.7 c \quad \text{about } \frac{\pi}{4} \text{ to the z-axis}$$



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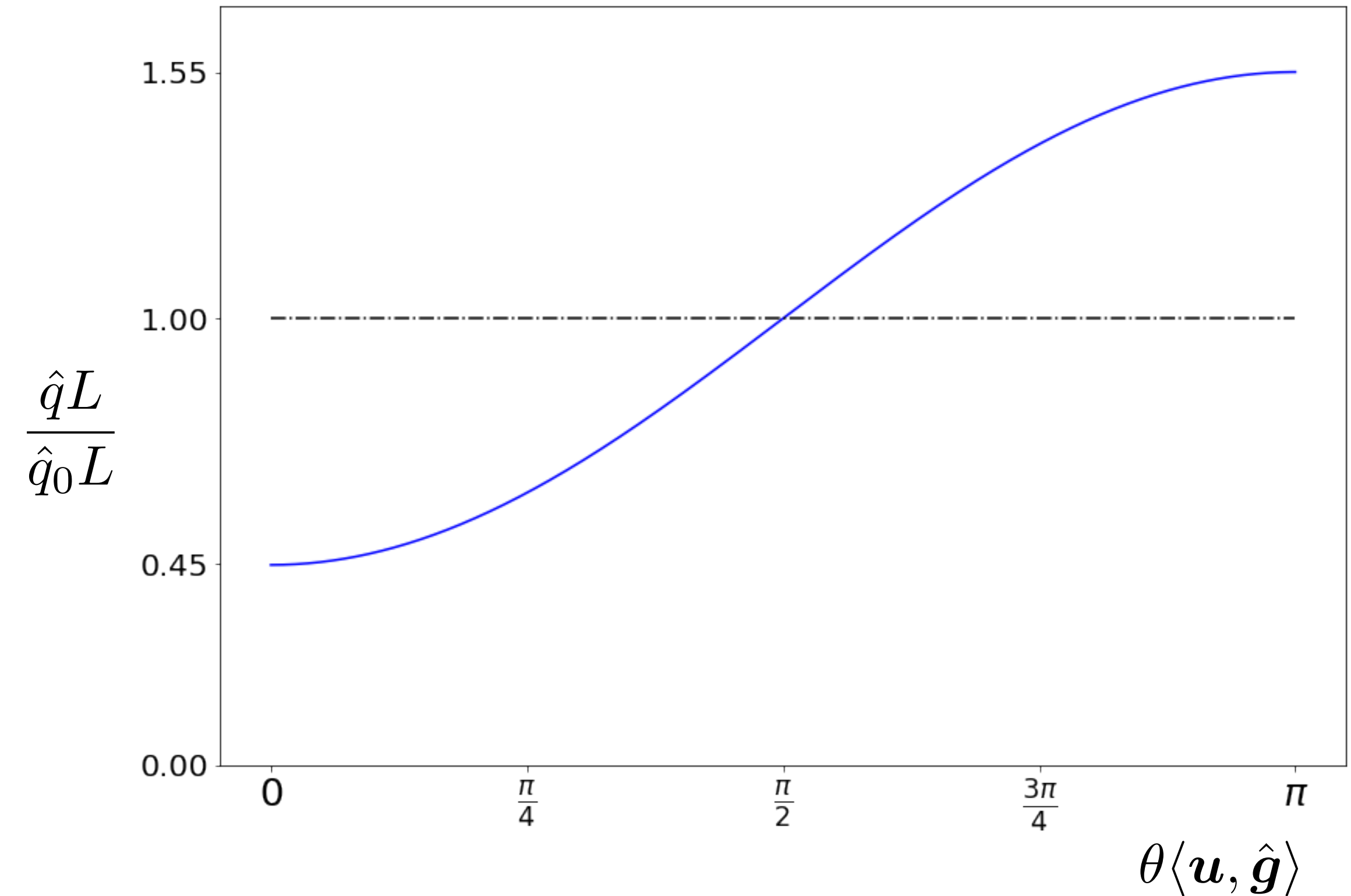
- Only gradients of temperature to leading logarithm
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$$\hat{q}L = \left[1 - \frac{L}{2} \frac{3 \left| \frac{\nabla T}{T^2} \right| T |\mathbf{u}| \cos(\theta)}{1 - u_z} \right] \hat{q}_0 L$$

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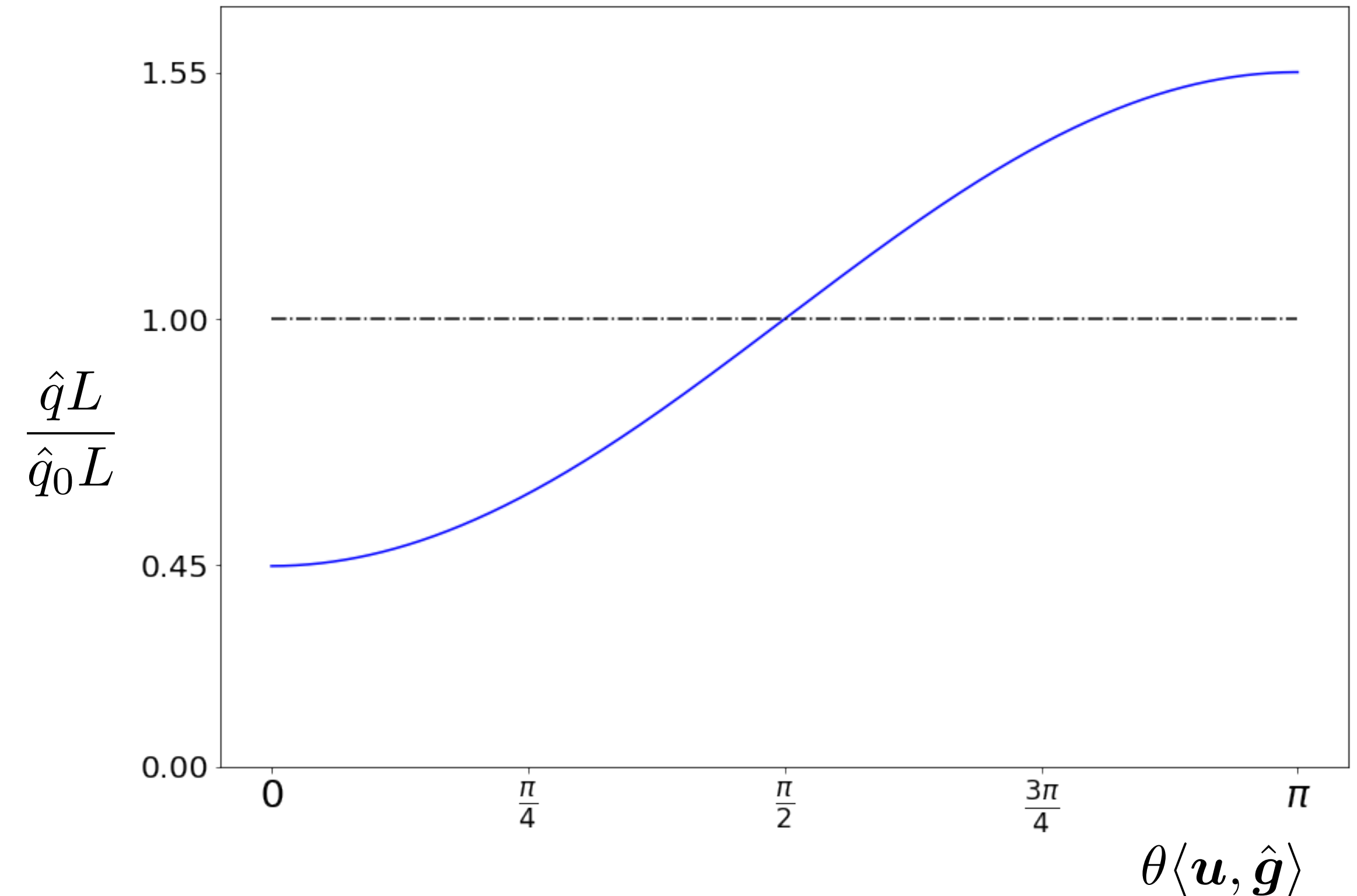
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- Full dependence $\rho \equiv \rho(T)$
- Other gradients contribute in non trivial way
- z-dependence must be taken into account

The jet quenching parameter is positive

$$\left| z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right| < 1 \quad \text{or gradient expansion brakes} \quad \longrightarrow \quad \hat{q}(z) = \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \hat{q}_0(z)$$

Keeping full dependence \mathbf{x} on in a crude estimate

$$\rho(\mathbf{x}, z) \longrightarrow \rho\left(-\frac{\mathbf{u}}{1 - u_z} z, z\right) \simeq \left[1 - z \frac{\nabla \rho}{\rho} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \rho(z)$$

Flowing anisotropic medium \Rightarrow anisotropic broadening

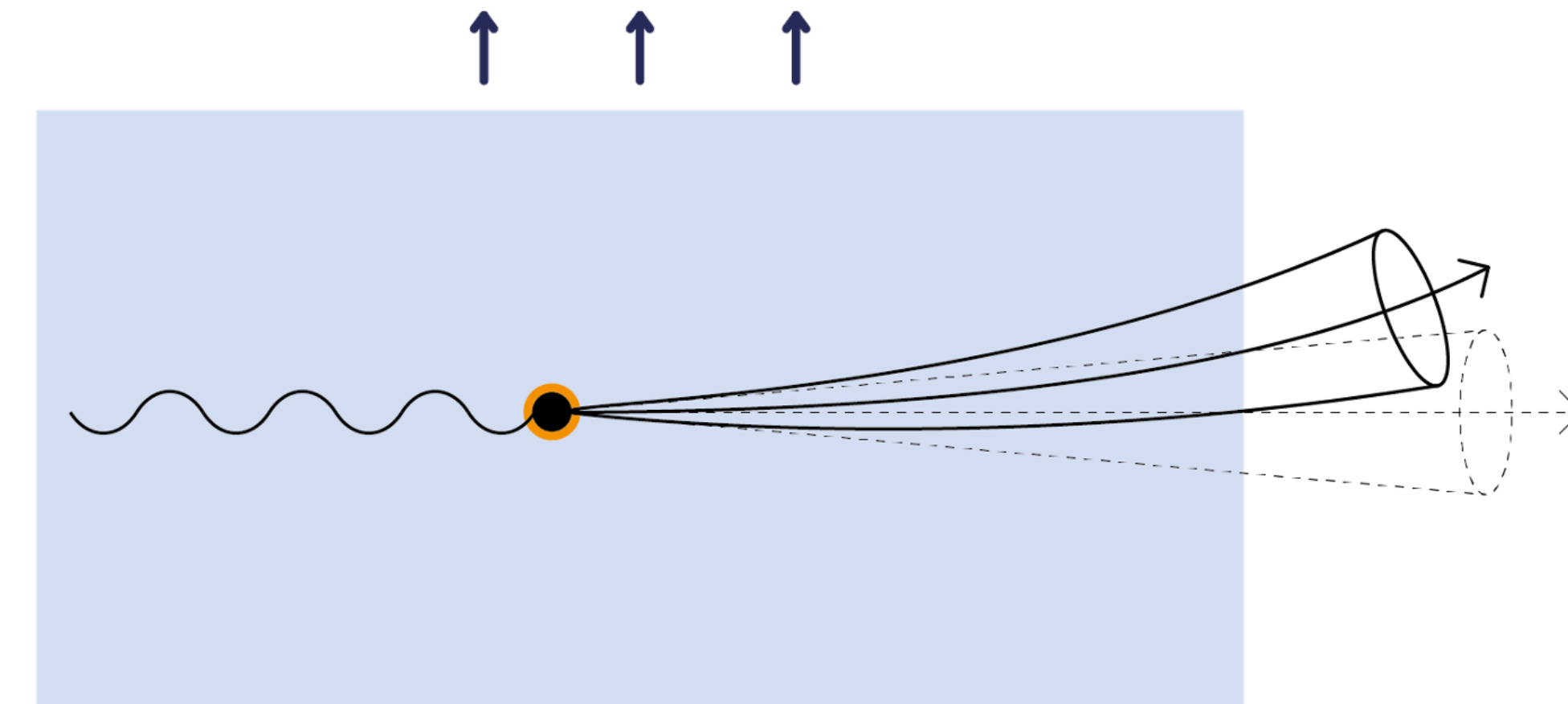
Directional effects due to transverse gradient and flow

- Odd moments of the distribution are non-zero and along gradients and flow
- (potentially lower background but smaller effect)

Novel multiplicative effect on even moments not energy suppressed

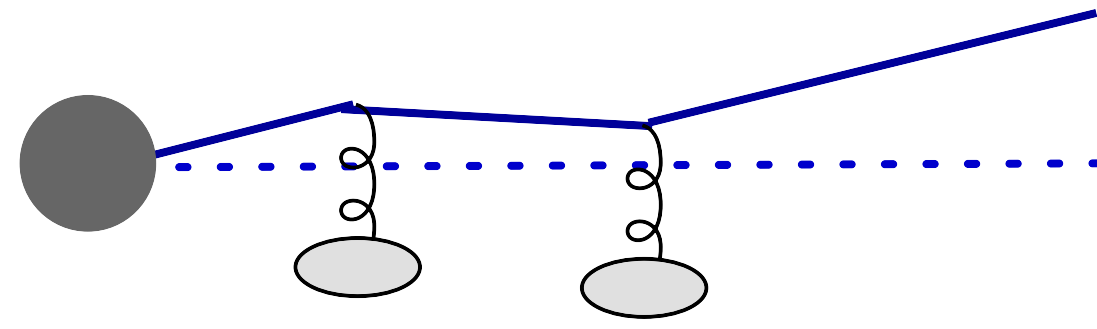
- The jet quenching parameter gets a multiplicative correction

$$\hat{q}(z) = \left[1 - z \hat{\mathbf{g}} \cdot \frac{\mathbf{u}}{1 - u_z} \right] \hat{q}_0(z)$$

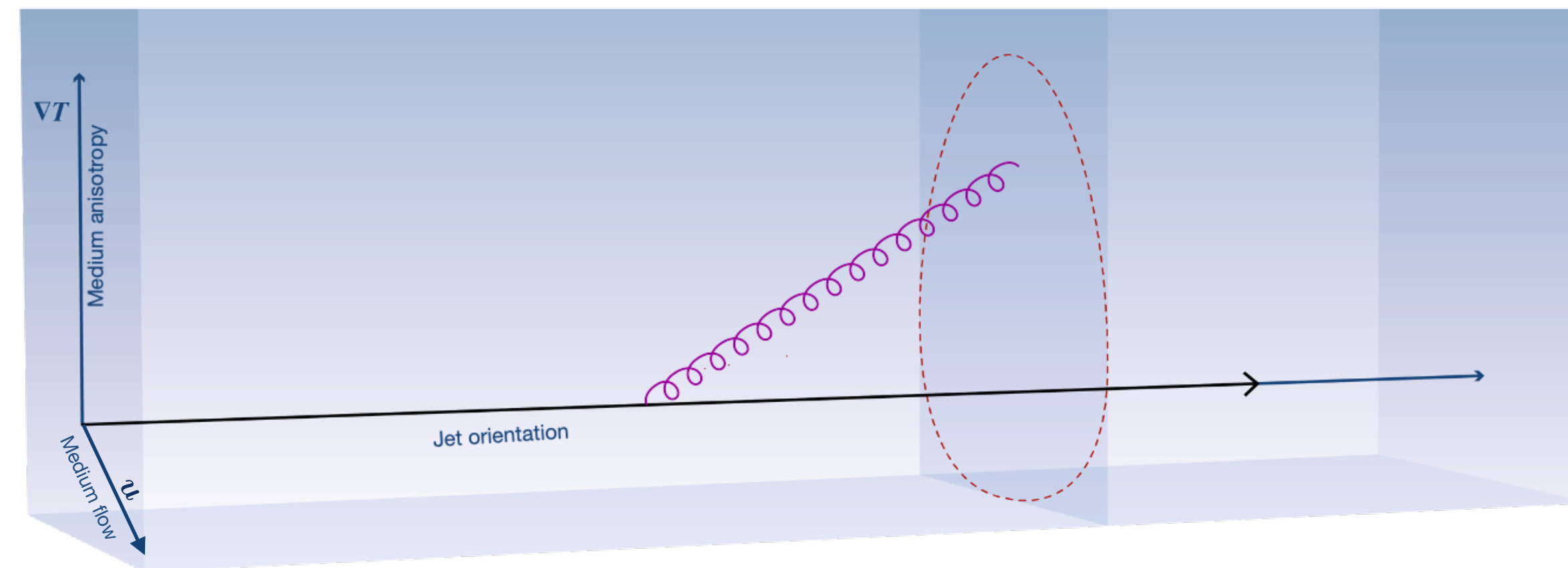
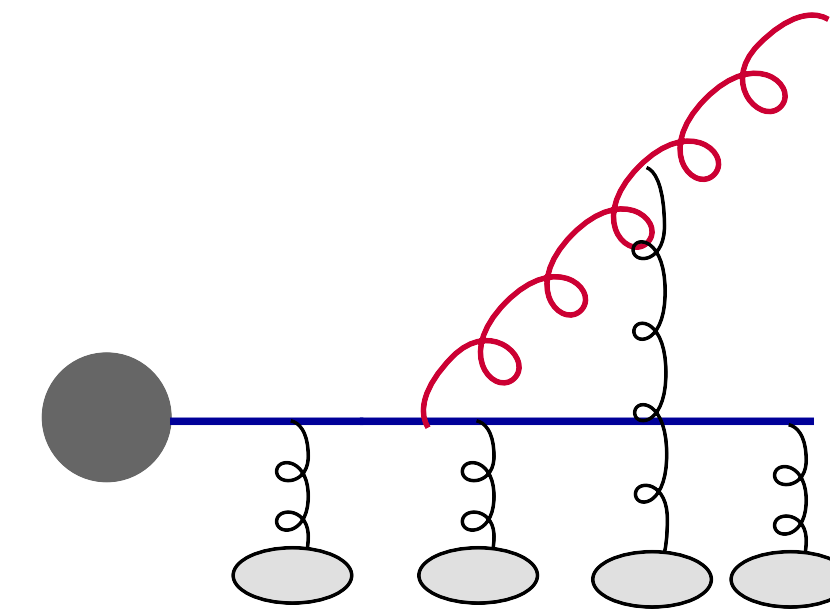


Focus on leading perturbative processes: Two processes that modify jets.

Single particle broadening ✓



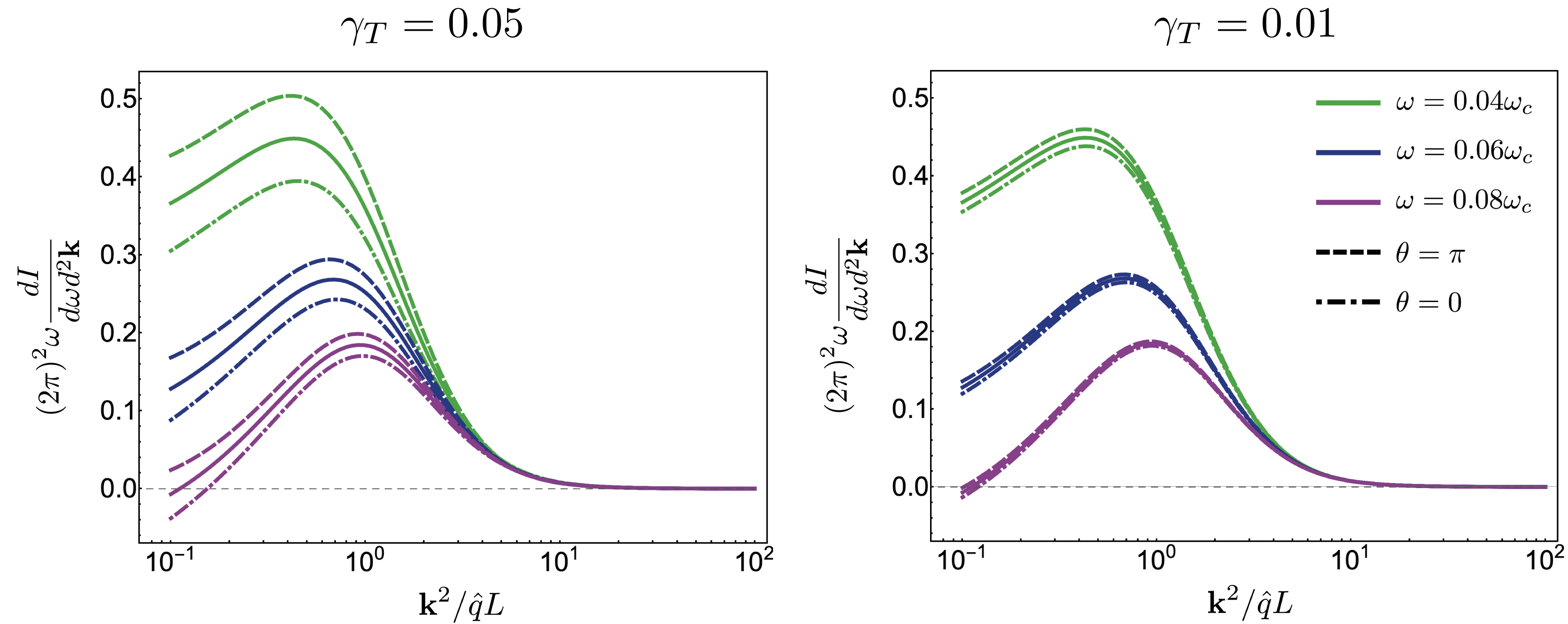
Medium induced gluon radiation



Ressummed spectrum with transverse gradients

Barata et al. [2304.03712](#)

- Asymmetric medium-induced gluon spectrum



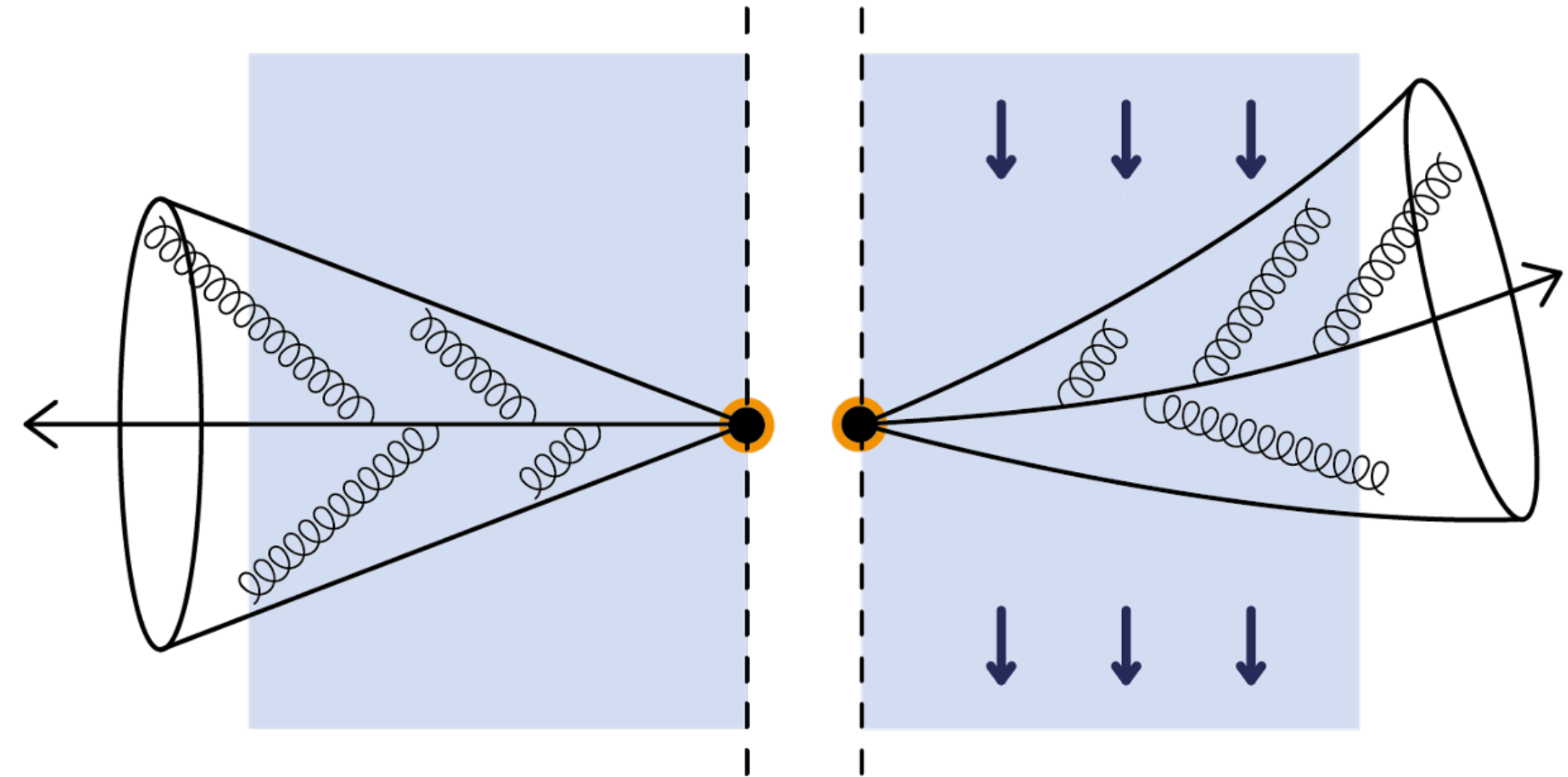
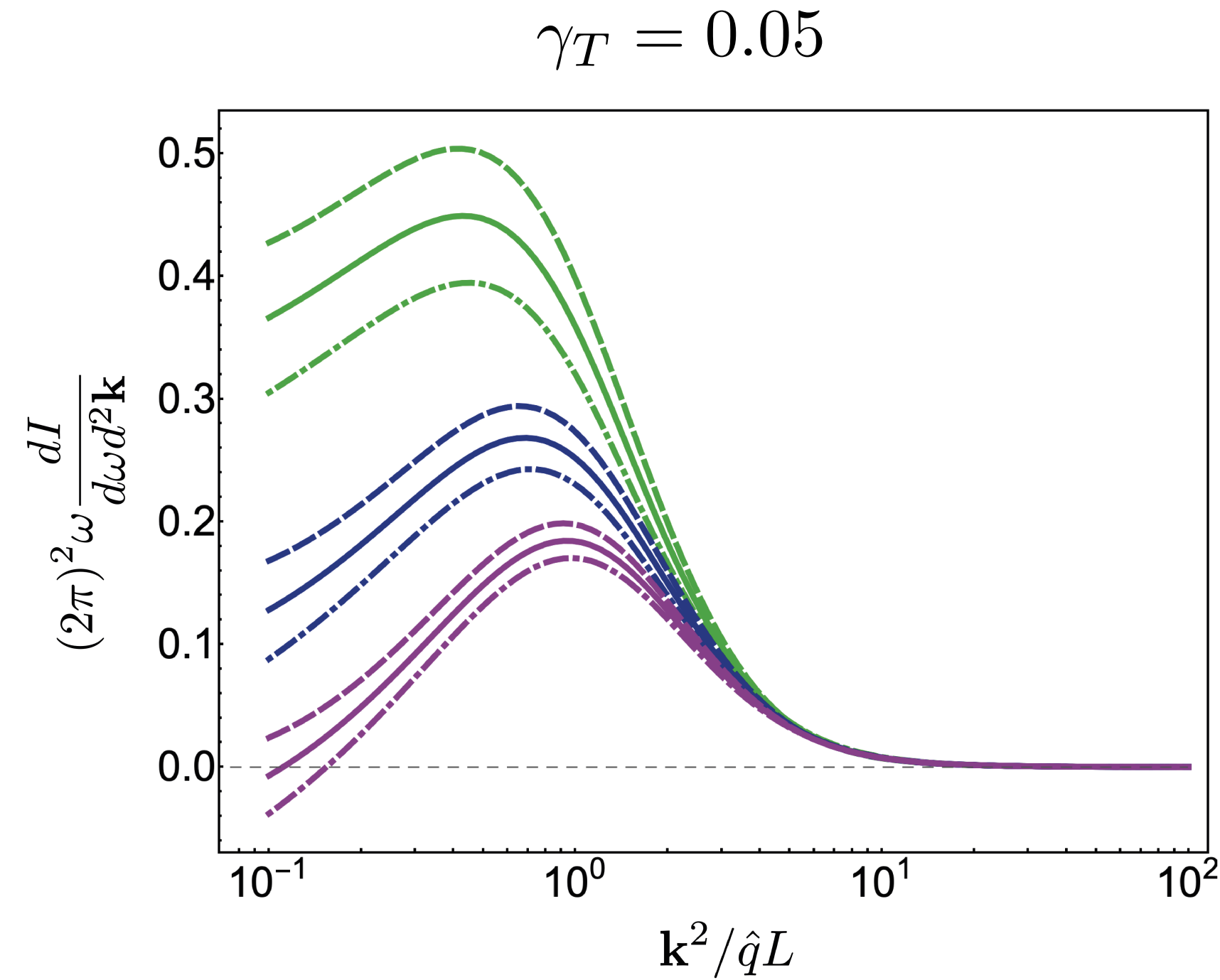
Ressummed spectrum with transverse flow

Coming soon

Ressummed spectrum with transverse gradients

Barata et al. [2304.03712](#)

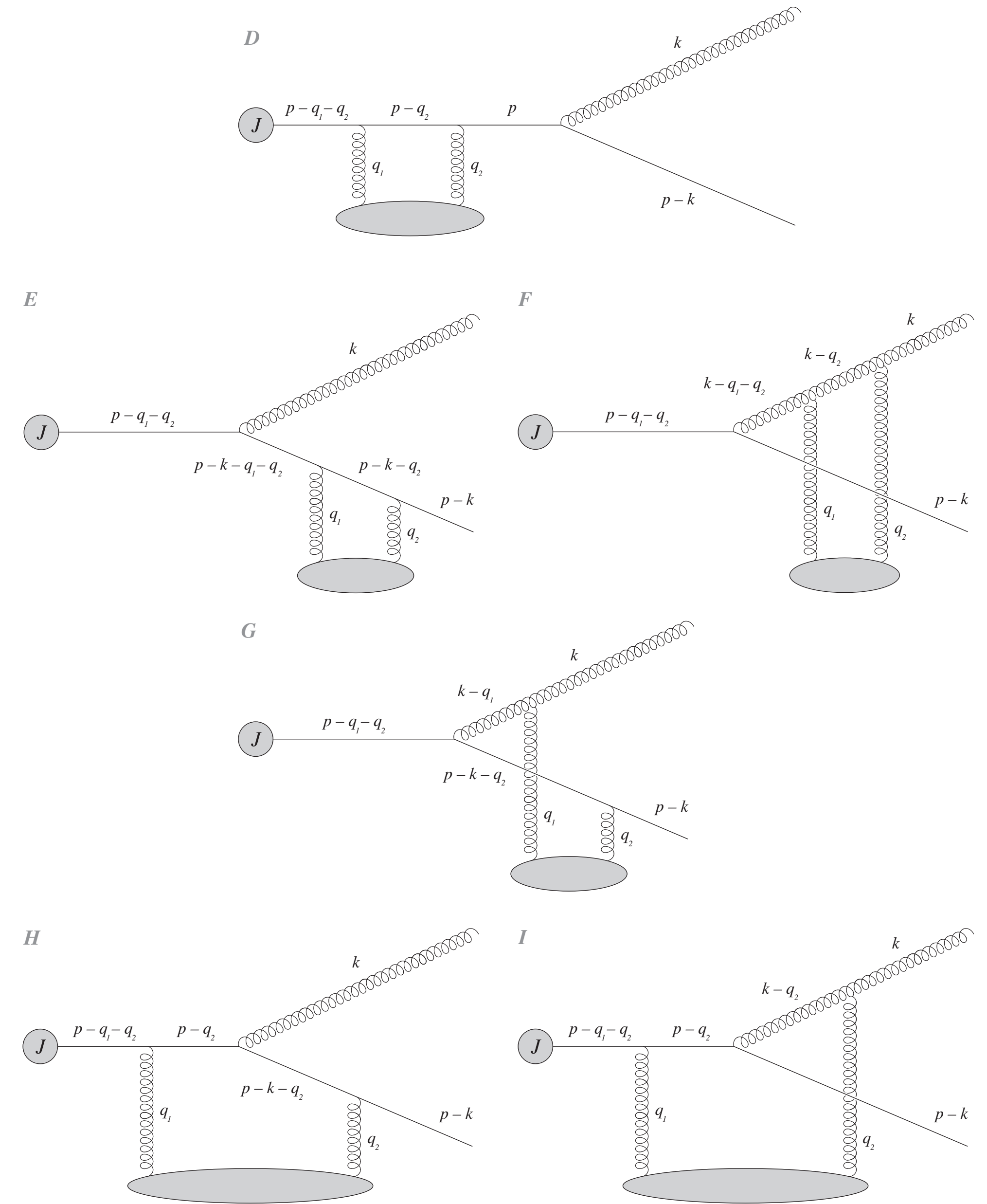
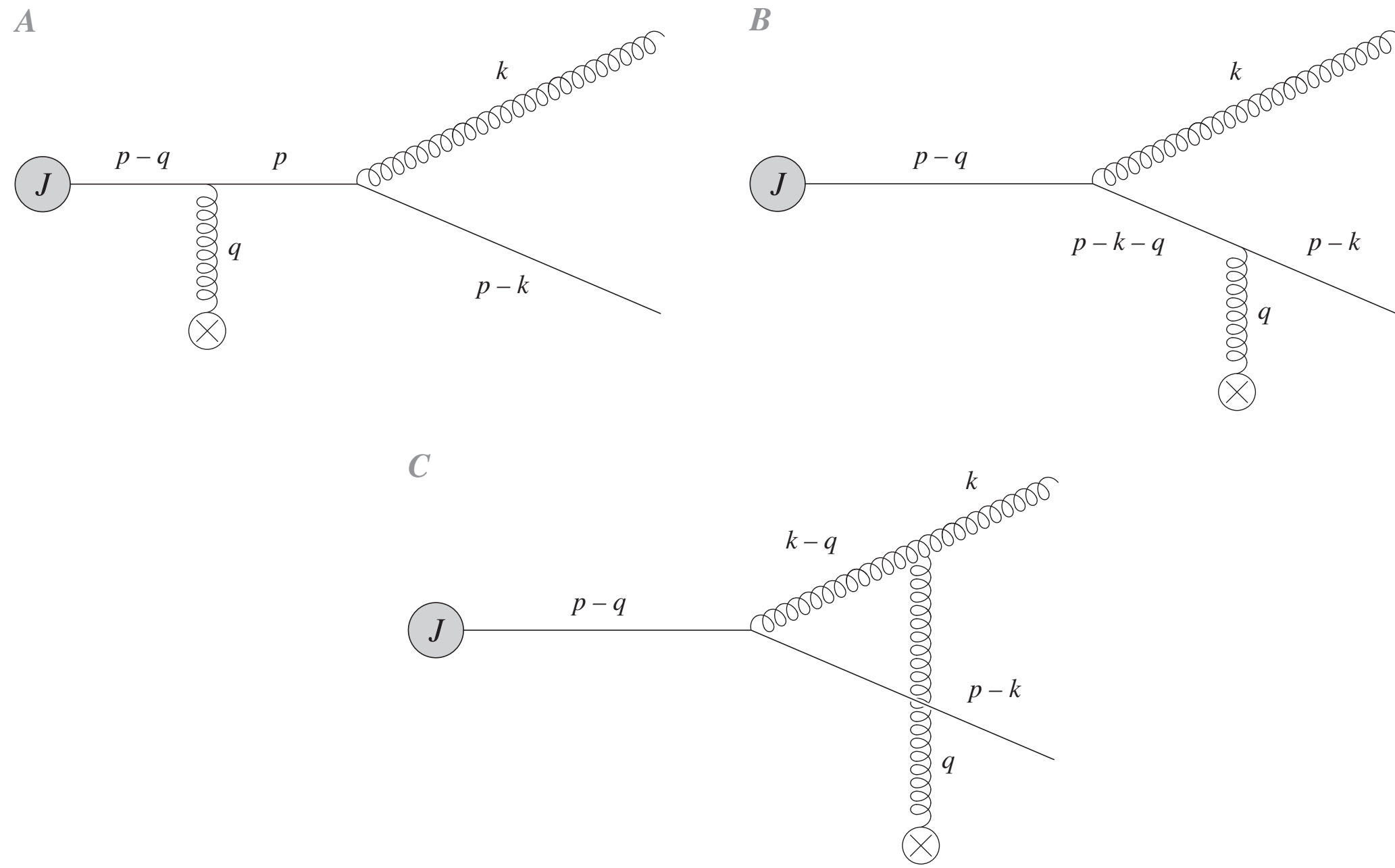
- Asymmetric medium-induced gluon spectrum



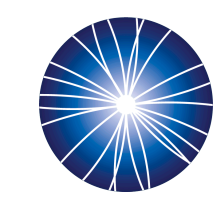
Ressummed spectrum with transverse flow

Coming soon

There are 9 possible diagrams



SB and DB diagrams add up to 12 different contributions



The final state parton distribution

$$E \frac{d\mathcal{N}^{(1)}}{d^2k dx d^2p dE} \equiv \frac{1}{[2(2\pi)^3]^2} \frac{1}{x(1-x)} \langle |\mathcal{R}_{N=1}|^2 \rangle$$

- Static matter with full gluon kinematics

Extending the previous result to hard gluon emissions

Without resummation of the interactions

Both agree on the correspondent limit

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- GLV spectrum
- Gradients corrections

$$E \frac{d\mathcal{N}^{(1)}}{d^2k dx d^2p dE} = \frac{g^2 C_F}{(2\pi)^3 x} \left(E \frac{d\mathcal{N}^{(0)}}{d^2p dE} \right) \int_0^L dz \int_{\mathbf{q}} \rho(z) [v(\mathbf{q}^2)]^2$$

$$\times \left\{ \frac{2 \mathbf{k} \cdot \mathbf{q}}{\mathbf{k}^2 (\mathbf{k} - \mathbf{q})^2} \left(1 - \cos \left(\frac{(\mathbf{k} - \mathbf{q})^2 z}{2xE} \right) \right) \left(1 + \frac{\hat{\mathbf{g}} \cdot (\mathbf{k} - \mathbf{q})}{2xE} z \right) - \frac{\hat{\mathbf{g}} \cdot \mathbf{k}}{\mathbf{k}^2} \left[\frac{z}{xE} - \frac{1}{\mathbf{k}^2} \sin \left(\frac{\mathbf{k}^2 z}{2xE} \right) \right] \right.$$

$$\left. + \frac{\mathbf{k} \cdot (\mathbf{k} - \mathbf{q})}{\mathbf{k}^2 (\mathbf{k} - \mathbf{q})^2} \left[\frac{\hat{\mathbf{g}} \cdot (\mathbf{k} - \mathbf{q})}{xE} z - \hat{\mathbf{g}} \cdot \left(2 \frac{\mathbf{k} - \mathbf{q}}{(\mathbf{k} - \mathbf{q})^2} - \frac{\mathbf{k}}{\mathbf{k} \cdot (\mathbf{k} - \mathbf{q})} \right) \sin \left(\frac{(\mathbf{k} - \mathbf{q})^2 z}{2xE} \right) \right] \right\}$$

The final state parton distribution

$$E \frac{d\mathcal{N}^{(1)}}{d^2k dx d^2p dE} \equiv \frac{1}{[2(2\pi)^3]^2} \frac{1}{x(1-x)} \langle |\mathcal{R}_{N=1}|^2 \rangle$$

- Flow-gradient mixture effect

Leading correction to the spectrum

 GLV spectrum

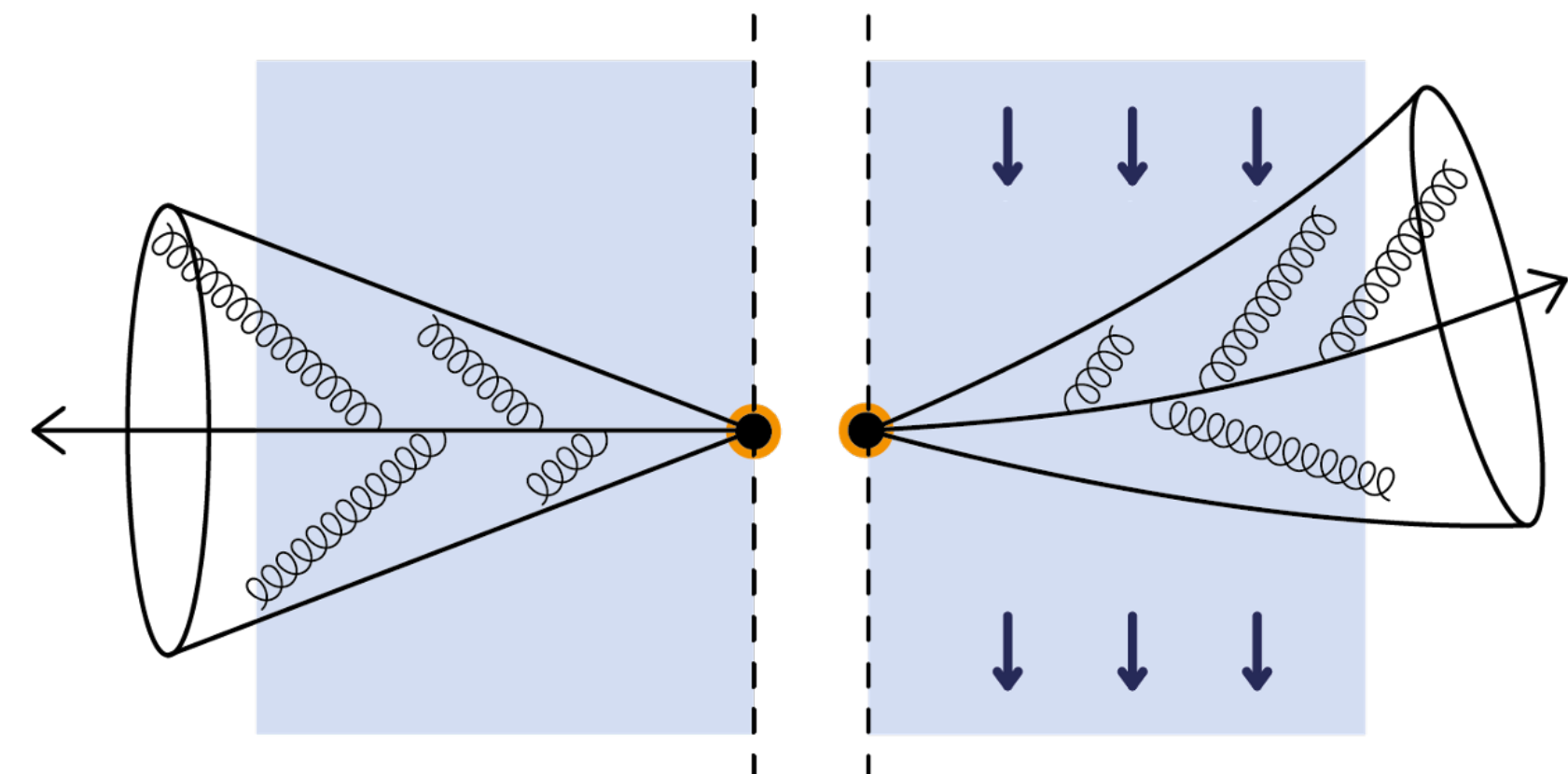
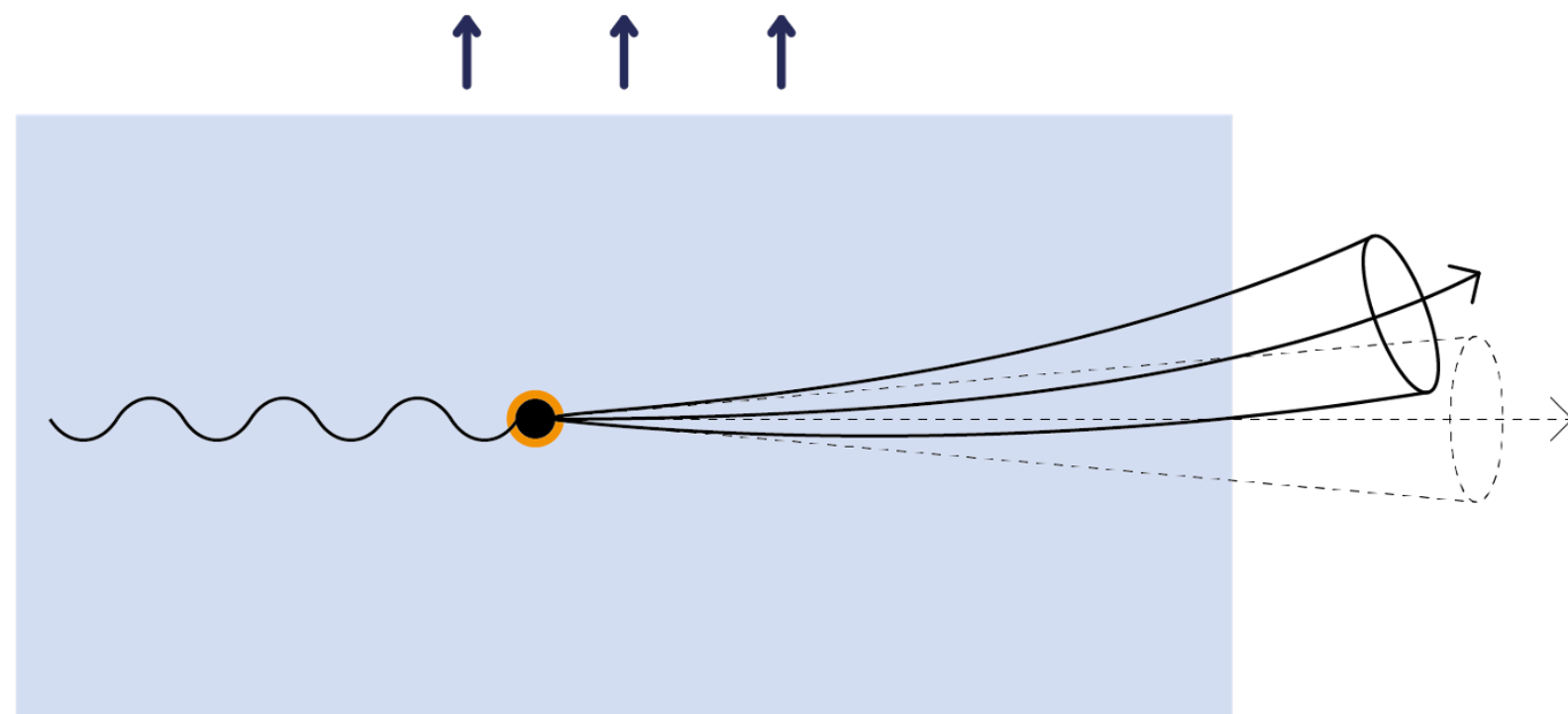
 Gradient x flow corrections

$$\omega \frac{dI}{d^2k d\omega} = \frac{g^2 C_F}{(2\pi)^2} \int_0^L dz \int_{\mathbf{q}} [1 - \hat{\mathbf{g}} \cdot \mathbf{u} z] \frac{2 \mathbf{k} \cdot \mathbf{q}}{\mathbf{k}^2 (\mathbf{k} - \mathbf{q})^2} \left[1 - \cos \left(\frac{(\mathbf{k} - \mathbf{q})^2}{2xE} z \right) \right] \rho(z) [v(\mathbf{q}^2)]^2$$

Multiplicative modification of the radiation rate \Rightarrow Modification of the induced energy loss

To take home

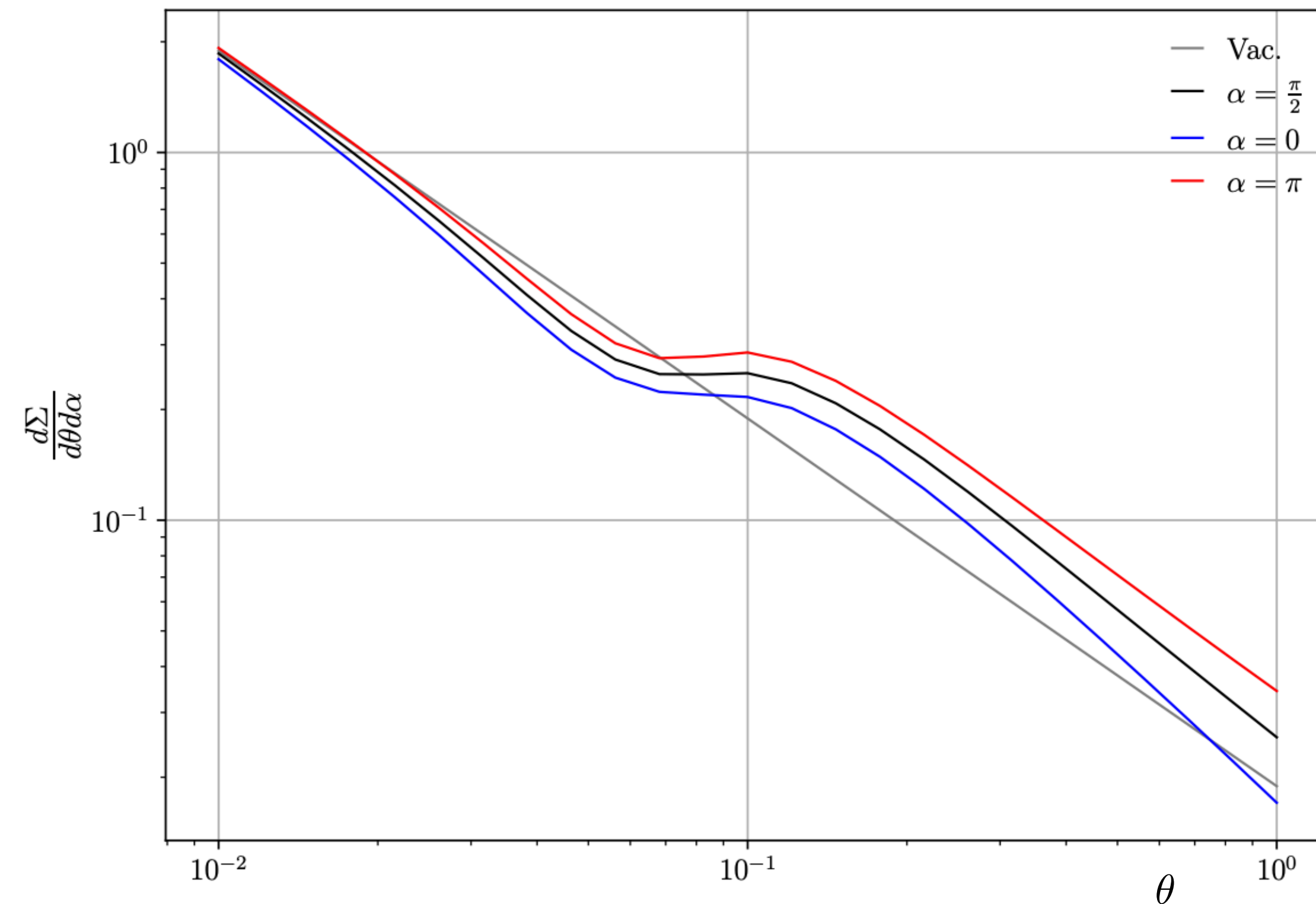
- Jets do feel the transverse flow and anisotropy, and get bended and distorted
- The transverse flow and anisotropy do affect the medium-induced radiation, modifying the jet substructure
- The interplay between flow and anisotropies modify the amount of quenching of a jet
- These effects can be probed in experiment, leading towards actual jet tomography



To take home

- These effects can be probed in experiment, leading towards actual jet tomography

They may be accessible with different substructure techniques, e.g. EECs [Barata et al. 2308.01294](#)



Thanks