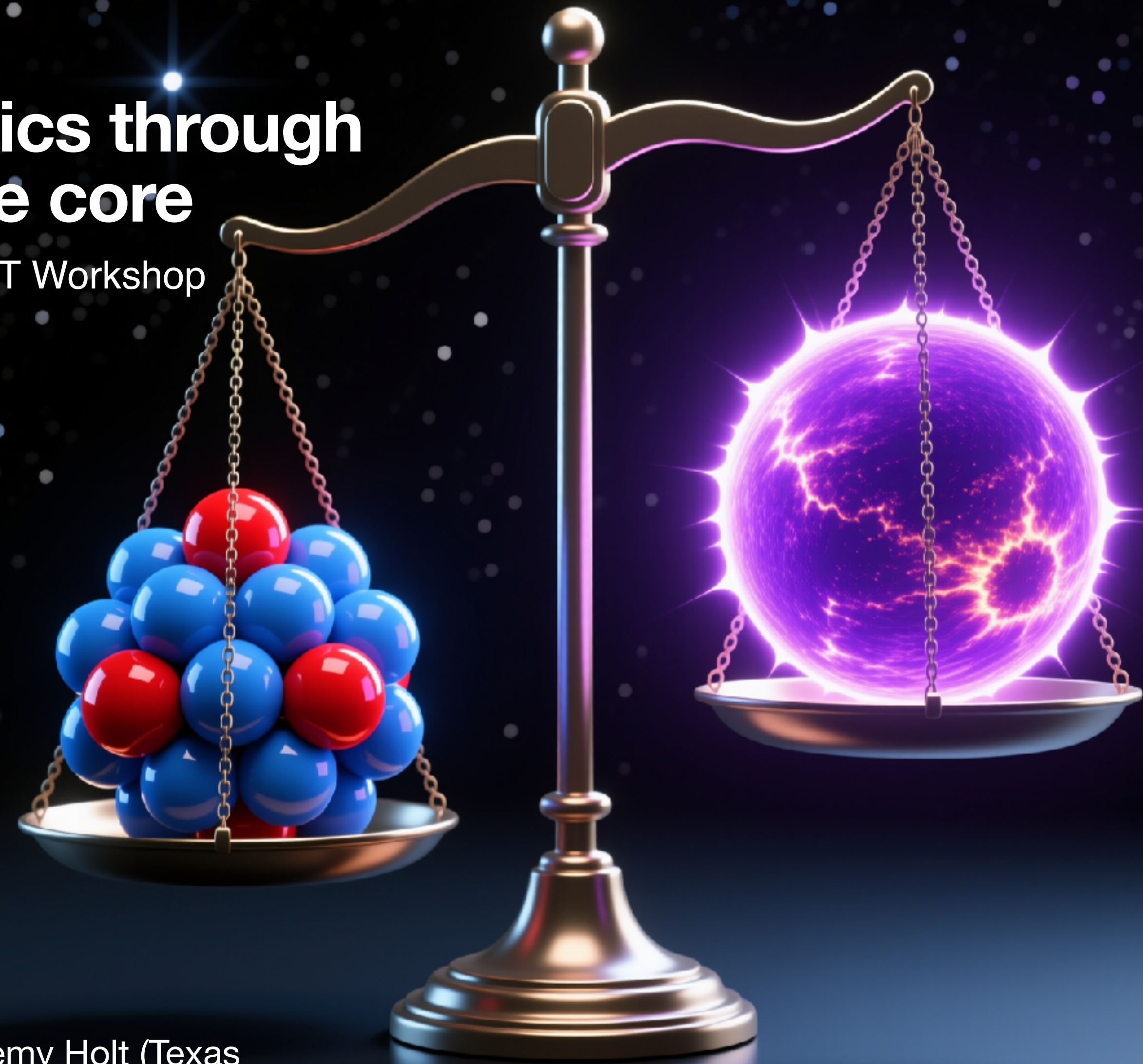


Geometric radius measurement during NS mergers

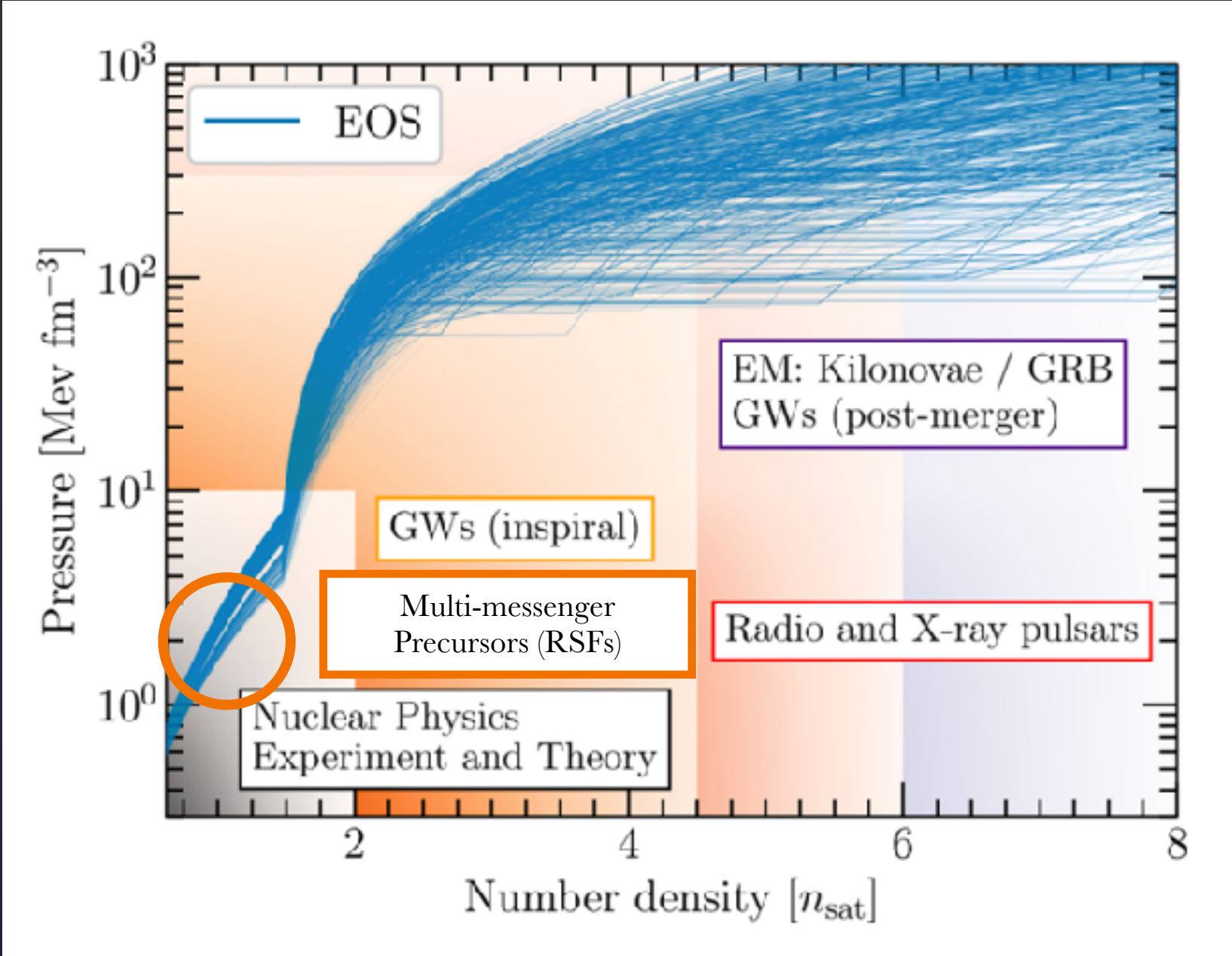
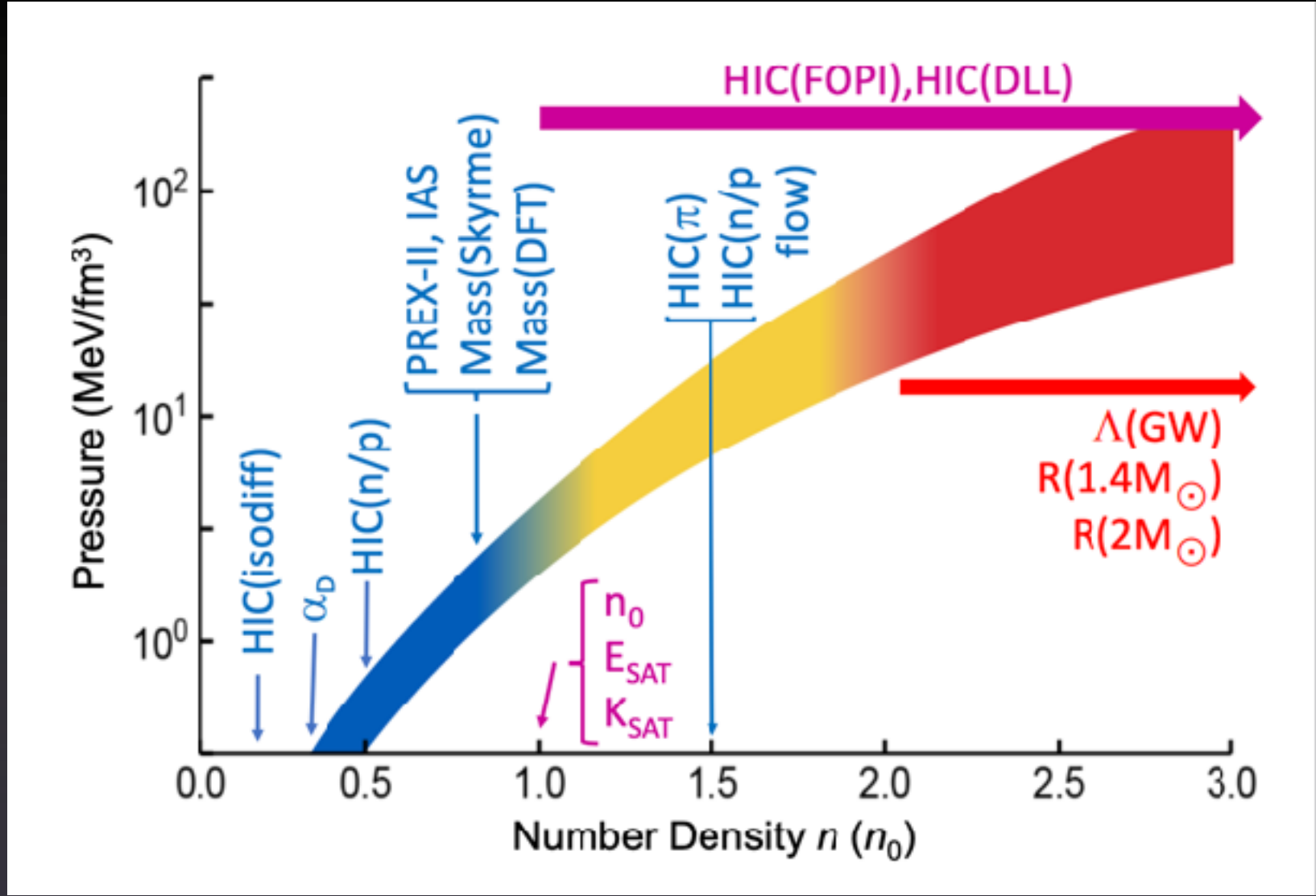
Leveraging low-density nuclear physics through dynamical resonance to constrain the core

Nuclear Physics in Mergers - Going Beyond the Equation of State INT Workshop
25-94W, University of Washington,
Wednesday 10 September 2025



David Tsang, University of Bath

With **Duncan Neill** (University of Bath), Will Newton (East Texas A&M), Jeremy Holt (Texas A&M), Christian Drischler (Ohio University/FRIB) & Jérôme Margueron (CNRS/FRIB)



C.Y. Tsang et al., 2023 arXiv:231011588

Adapted from Pang et al., (2023) Nature Comm, 14:8352

Important Physics

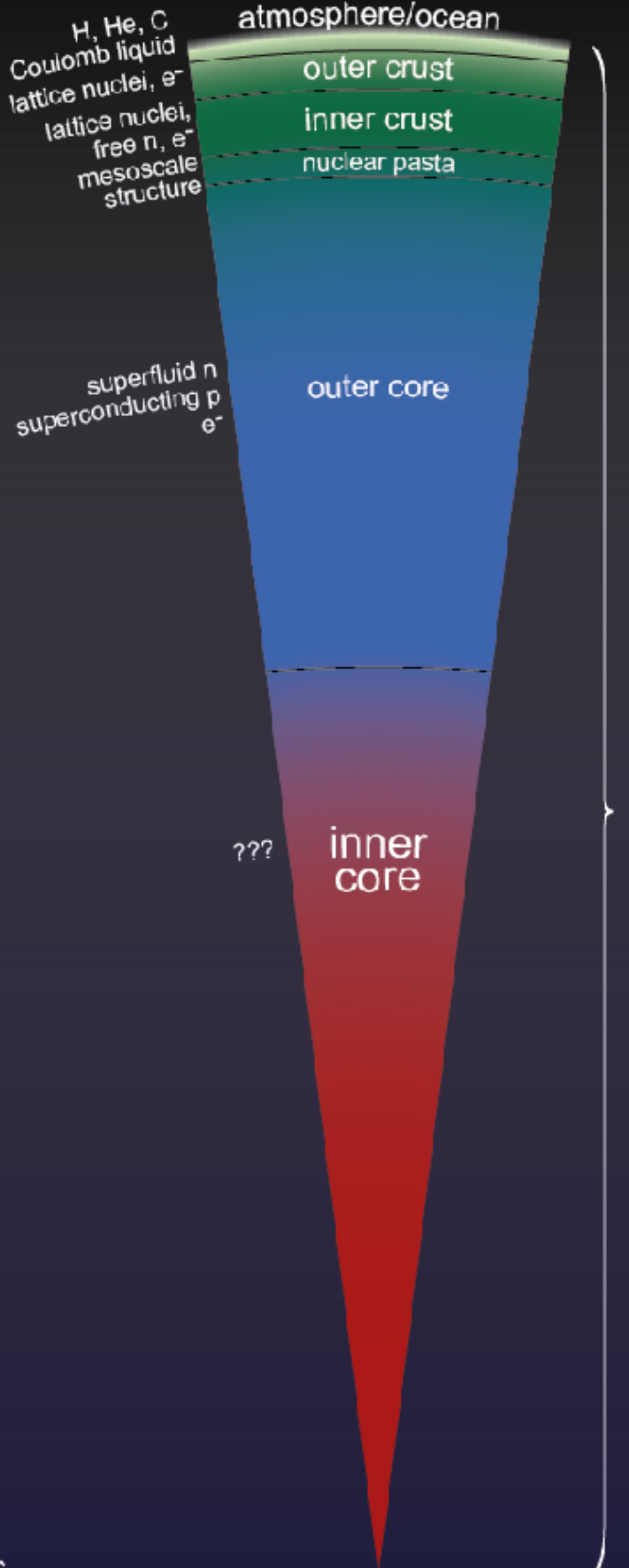
shear modulus

superfluidity, superconductivity

Nucleonic Physics (e.g. χ EFT, nucleonic meta-models)

exotic physics? (e.g. phase transitions, quark gluon plasma, quarkyonic matter, hyperons, kaon condensate)

NS Structure



Astro Observables

ocean modes

toroidal shear modes

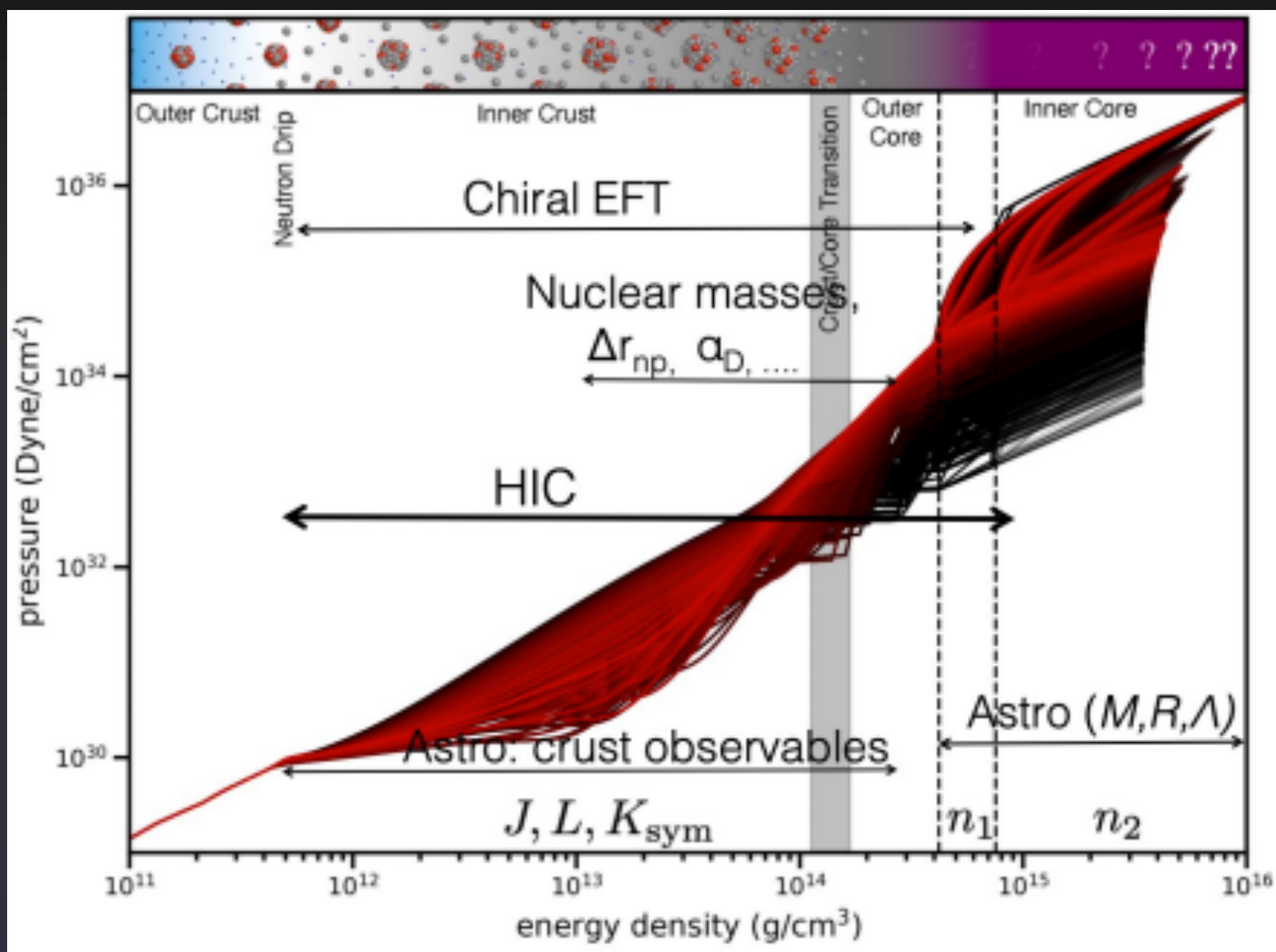
RSFs

i-mode

g-modes

r-modes

tidal deformability, f-mode, M_{lov}



Adapted from Neill et al, 2022

Important Physics

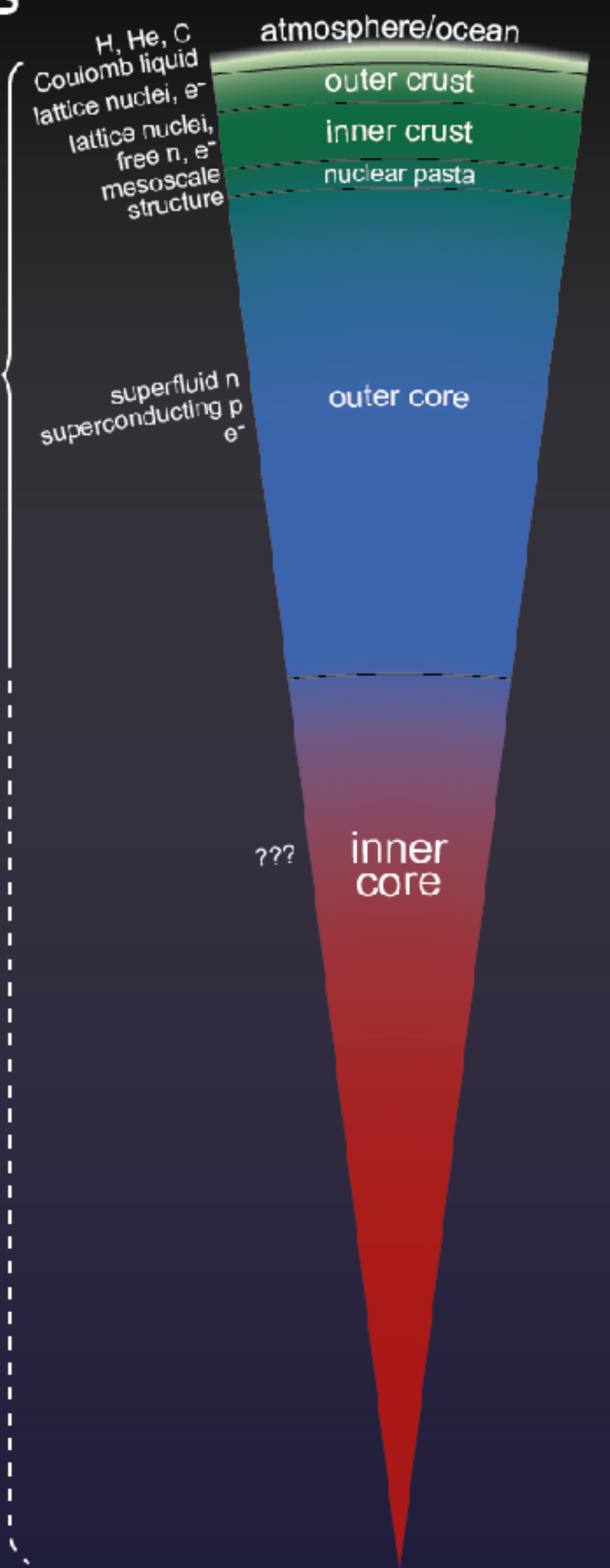
superfluidity,
superconductivity

shear
modulus

Nucleonic
Physics
(e.g. χ EFT,
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meta-models)

exotic physics?
(e.g. phase transitions,
quark gluon plasma,
quarkyonic matter,
hyperons,
kaon condensate)

NS Structure



Astro Observables

ocean modes
toroidal shear modes

RSFs
i-mode

g-modes
r-modes

tidal
deformability,
f-mode,
 M_{lov}

Nuclear Matter Physics

FOR
~~DUMMIES~~

Astrophysicists

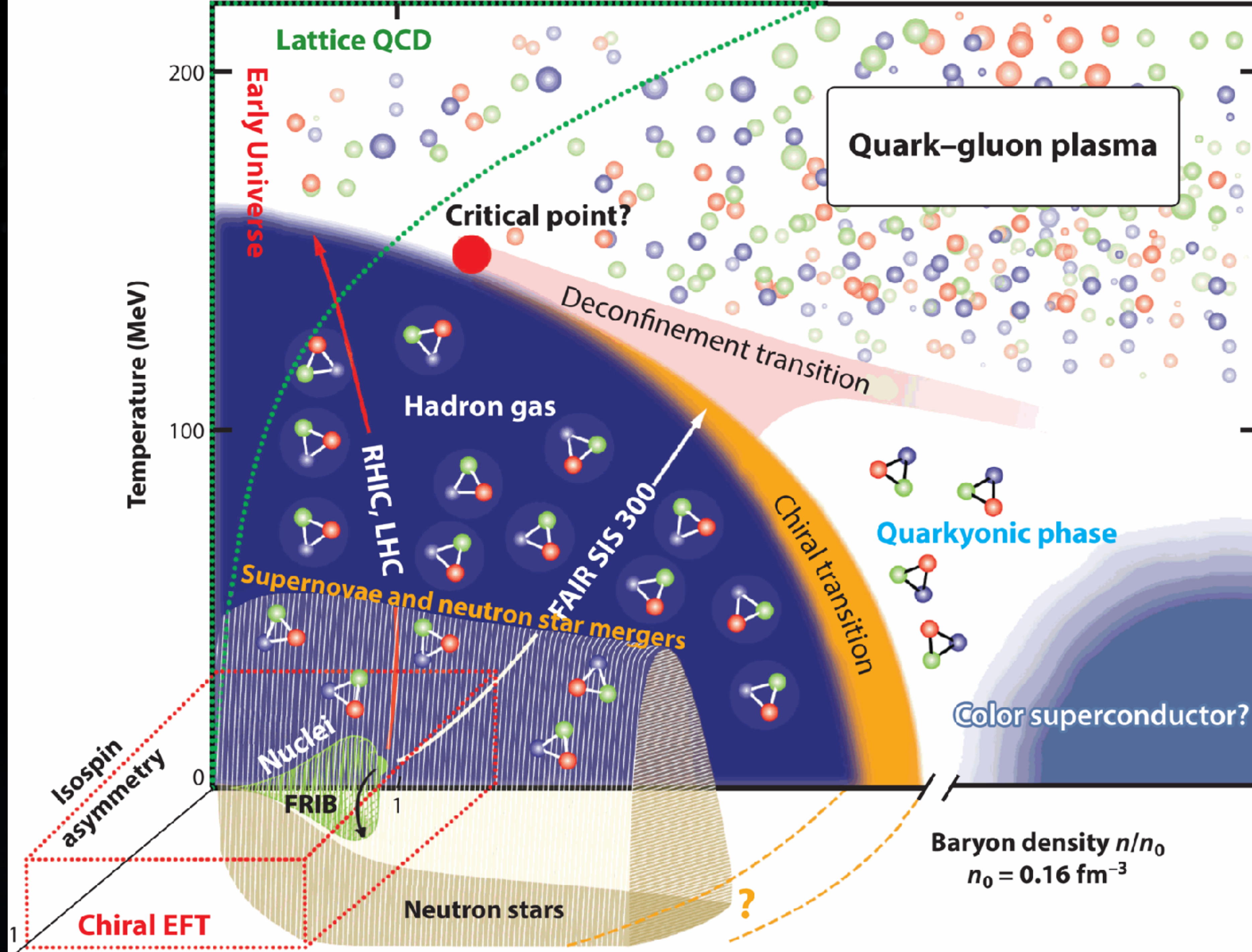
*A Reference
for the
Rest of Us!*

FREE eTips at dummies.com

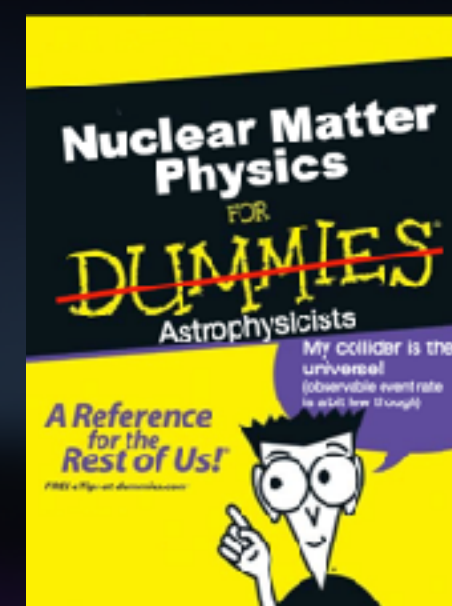


My collider is the
universe!
(observable event rate
is a bit low though)





Drischler, Holt, & Wellenhofer (2021), Ann. Rev. of Nucl., 71, 403



(Cold) Infinite Nuclear Matter Equation of State

Energy per baryon

$$K \propto \left. \frac{\partial^2 E_{\text{sym}}}{\partial n^2} \right|_{n=n_o}$$

$$L \propto \left. \frac{\partial E_{\text{sym}}}{\partial n} \right|_{n=n_o}$$

$$J = E_{\text{sym}}(n_o)$$

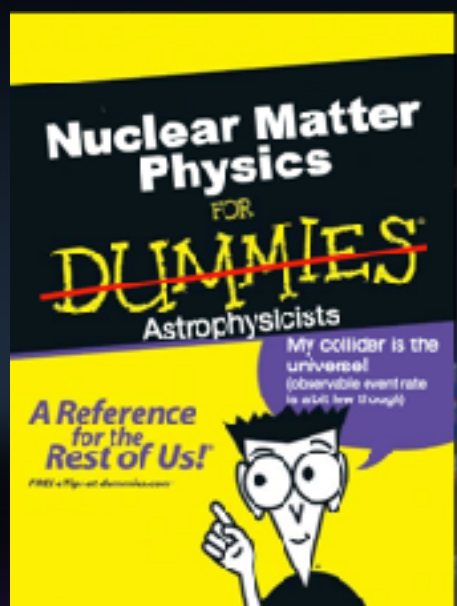
Saturation Density
 $n_o \simeq 0.16 \text{ fm}^{-3}$

n
Baryon Density

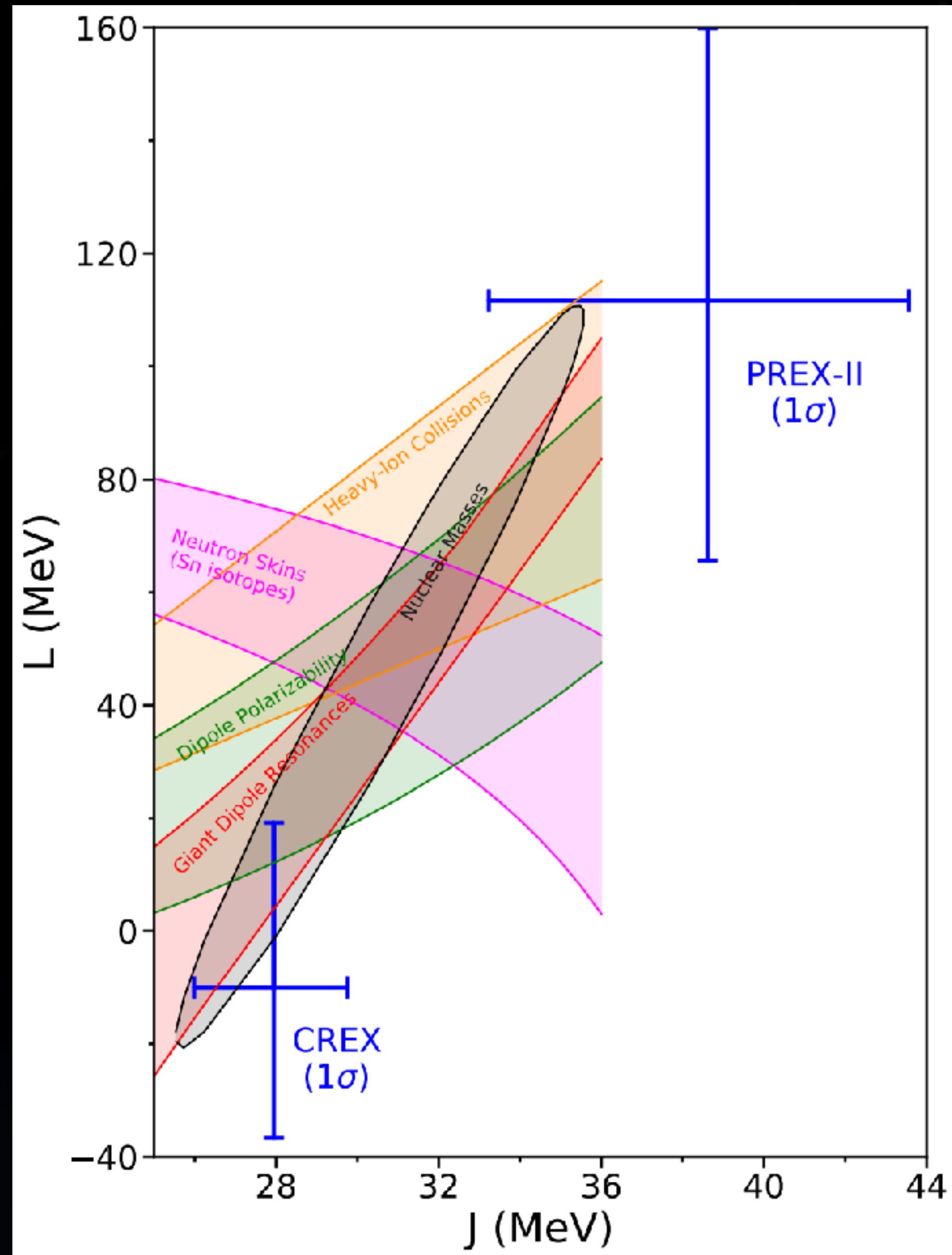
Pure Neutron Matter (PNM)

“isovector”
Nuclear Symmetry
Energy:
 $E_{\text{sym}}(n)$

Symmetric Nuclear Matter (SNM)
(Equal Protons and Neutrons)
“isoscalar”

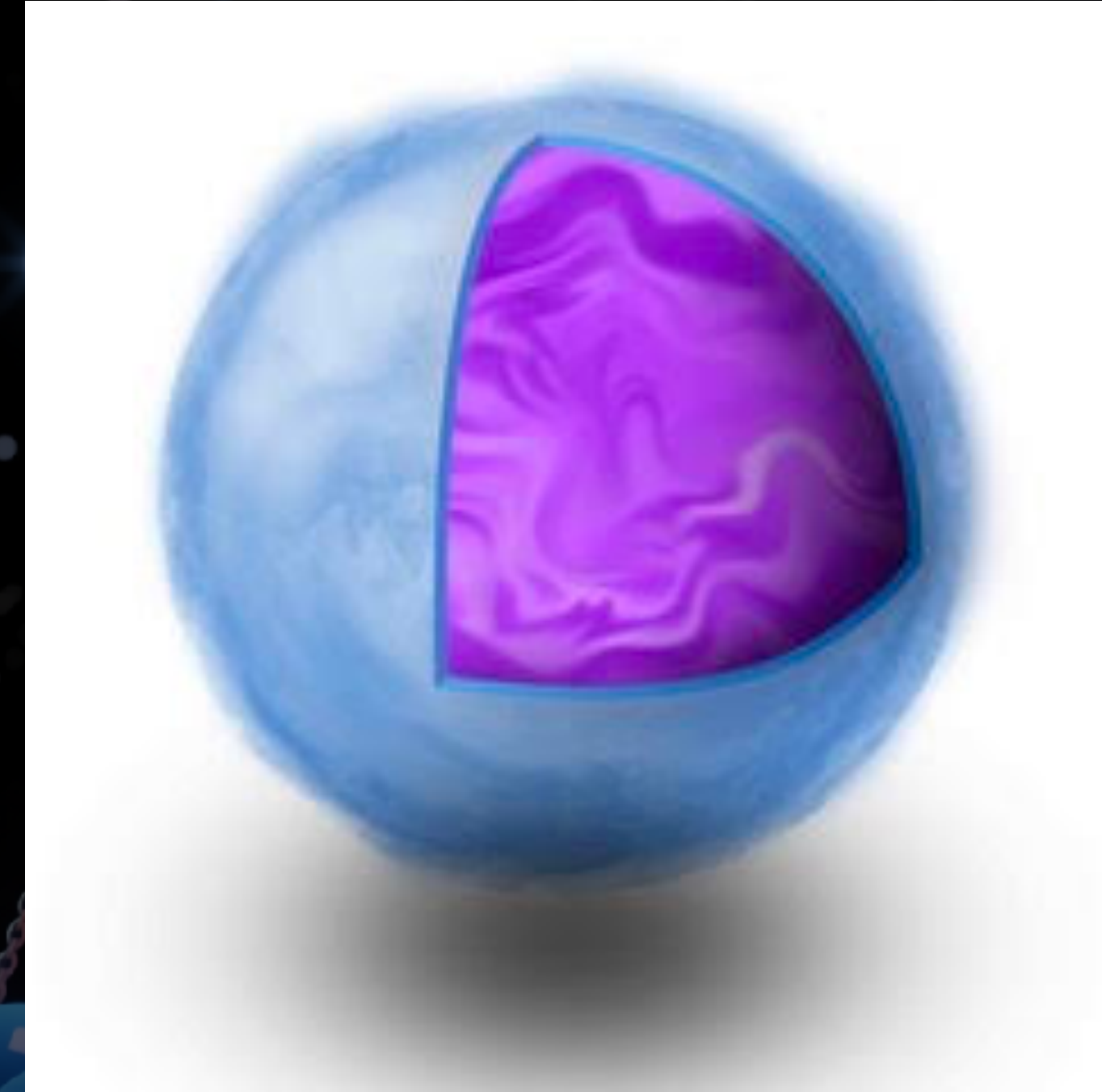


Experimental Constraints on J-L



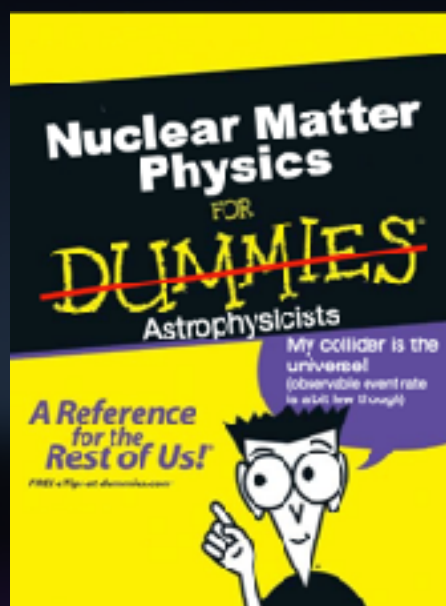
Adapted by D. Neill (2023 Thesis) from Lattimer & Lim 2013 including (Skryme dependent) J-L constraints on PREX and CREX from Zhang & Chen (2023) Phys Rev C, 108, 2, 024317

$^{208}\text{Pb}/^{48}\text{Ca}$ Neutron “Skin” thickness



https://www.stonybrook.edu/commcms/physics/research/archive/2022/0217_neutronskin

Experimental constraints
of symmetry energy
and nucleonic physics



Nuclear Effective Field Theories

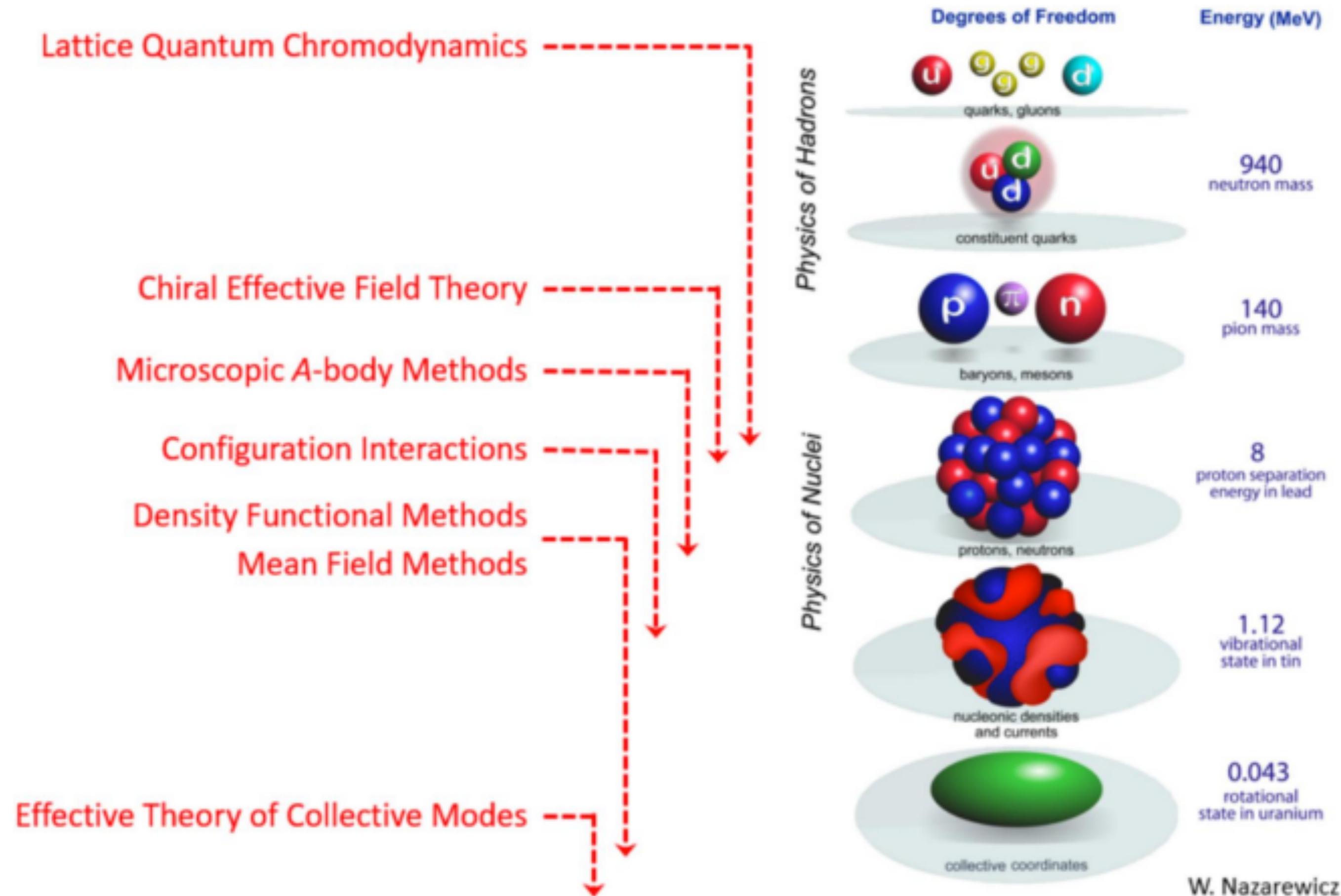
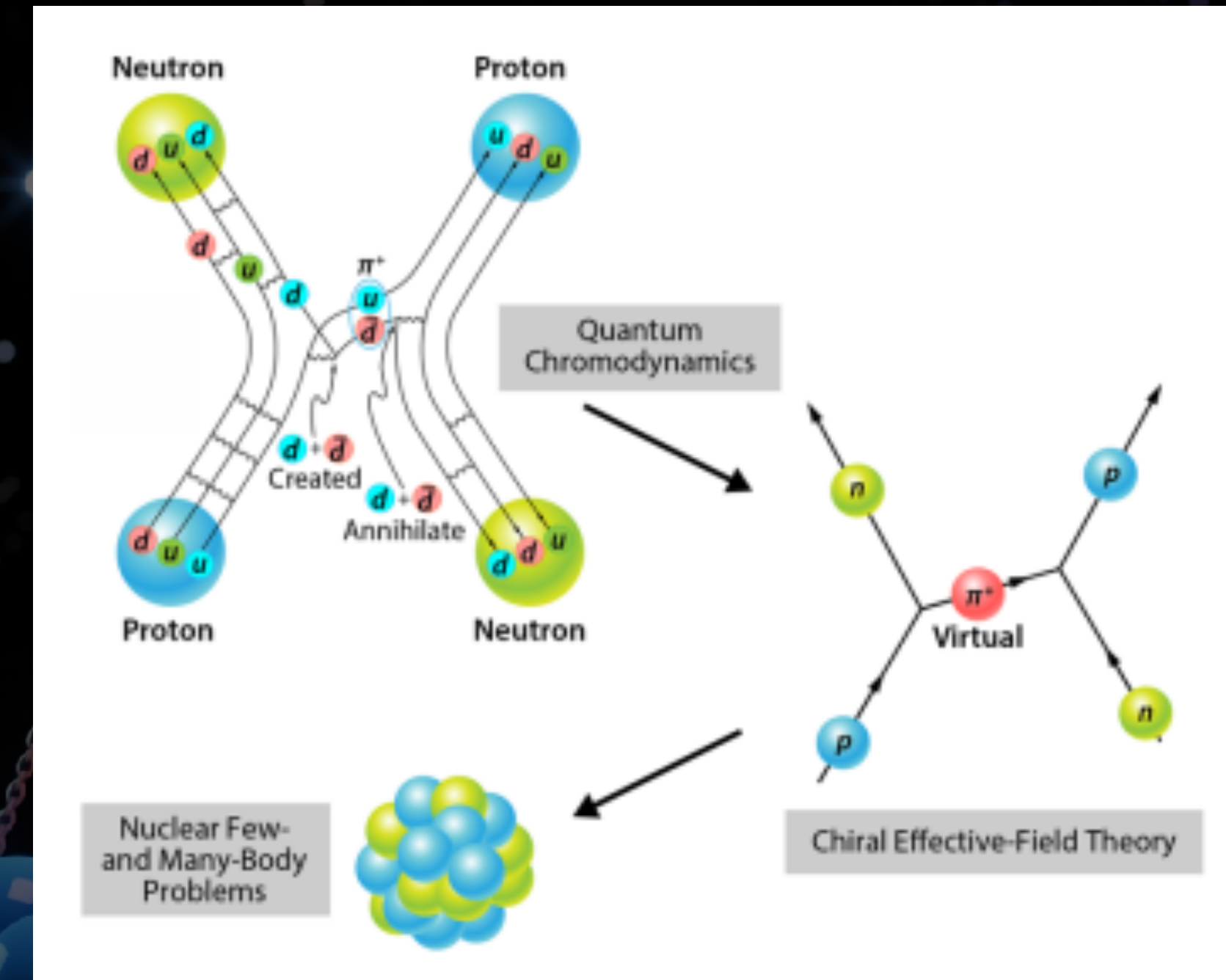
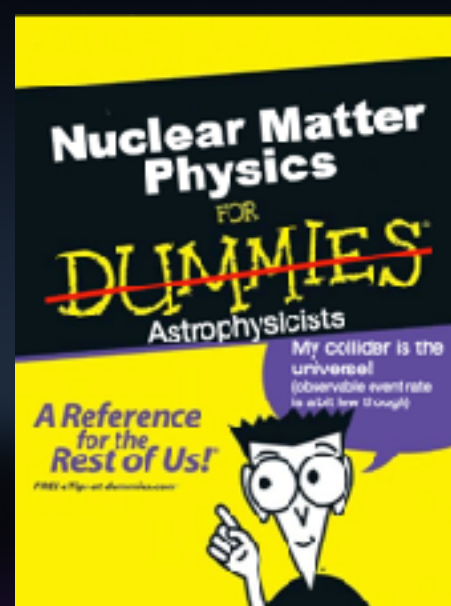


Illustration from https://indico-tdli.sjtu.edu.cn/event/2821/attachments/5277/8738/20241210_SJTU_bnlu.pdf



Hjorth-Jensen, Physics 10, 72, 2017 (APS/Alan Stonebraker)

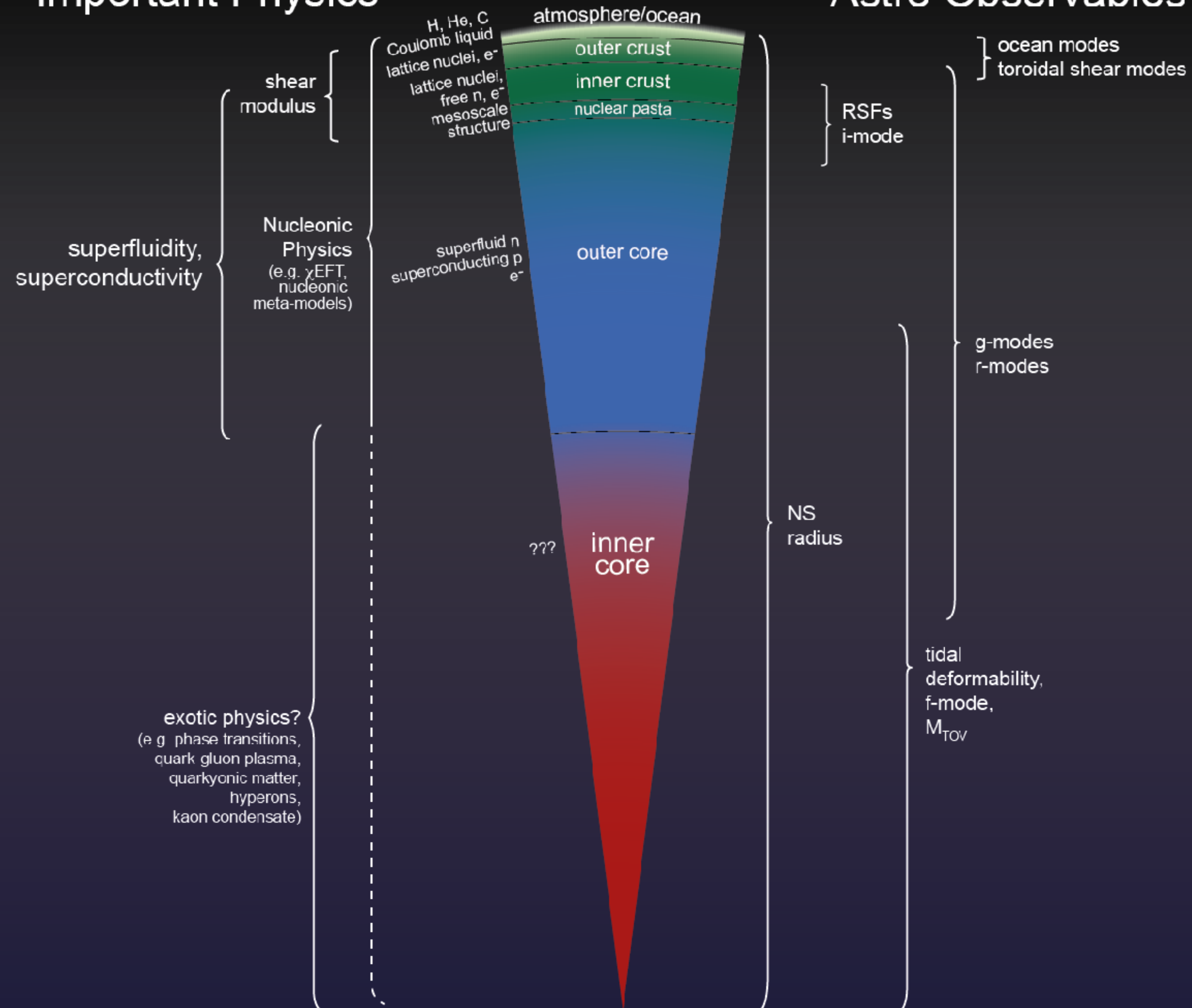
Theoretical models of nuclear matter



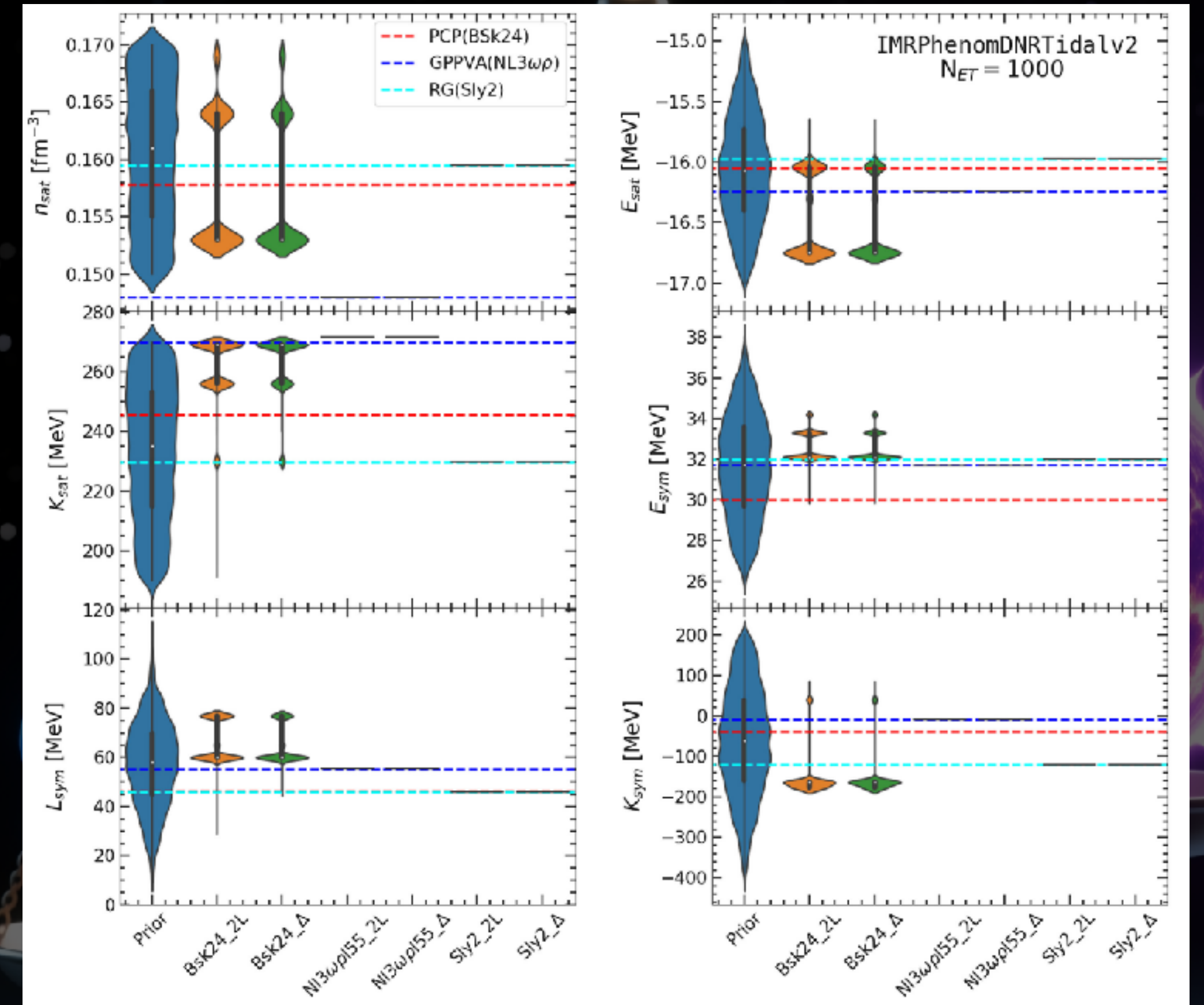
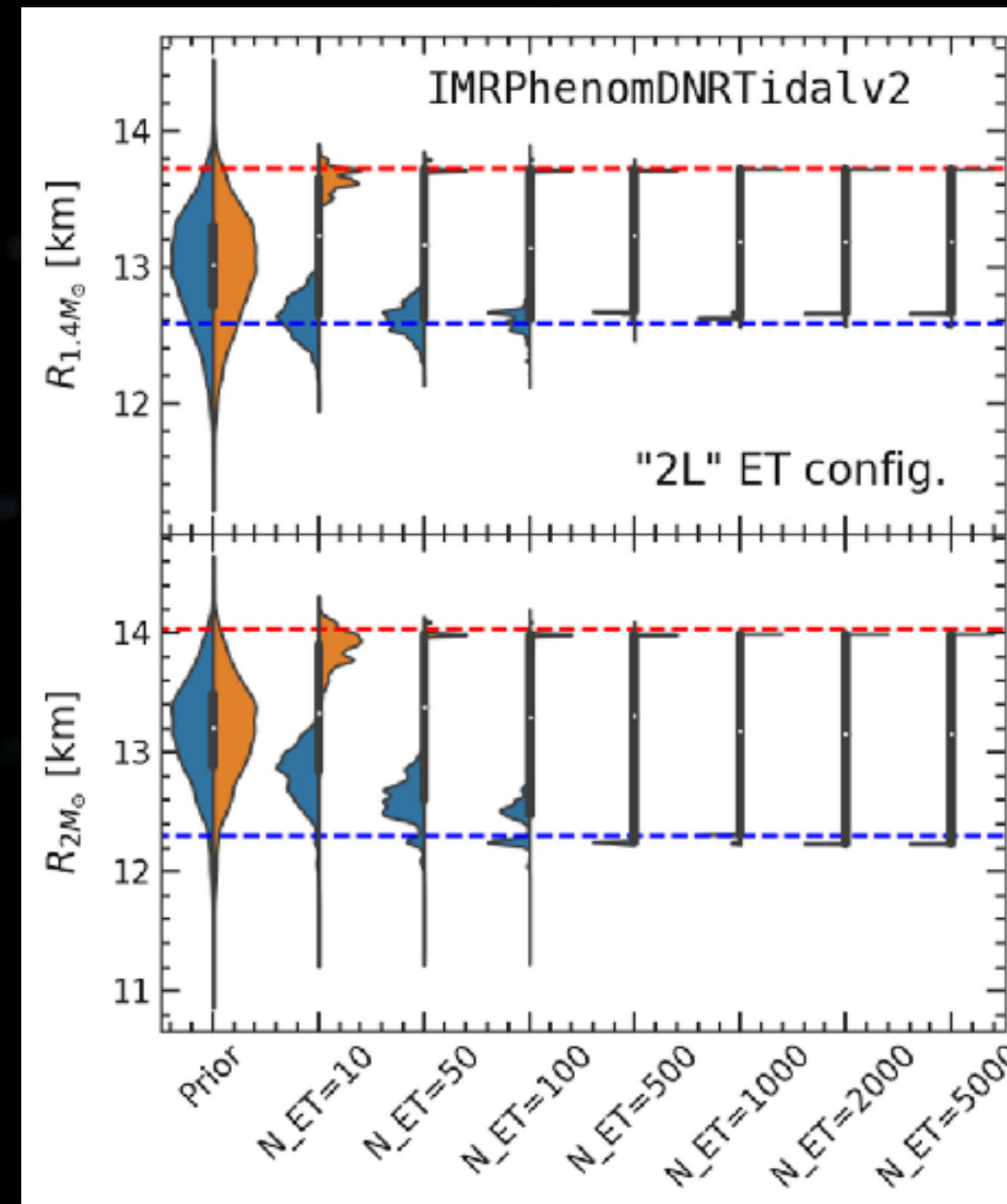
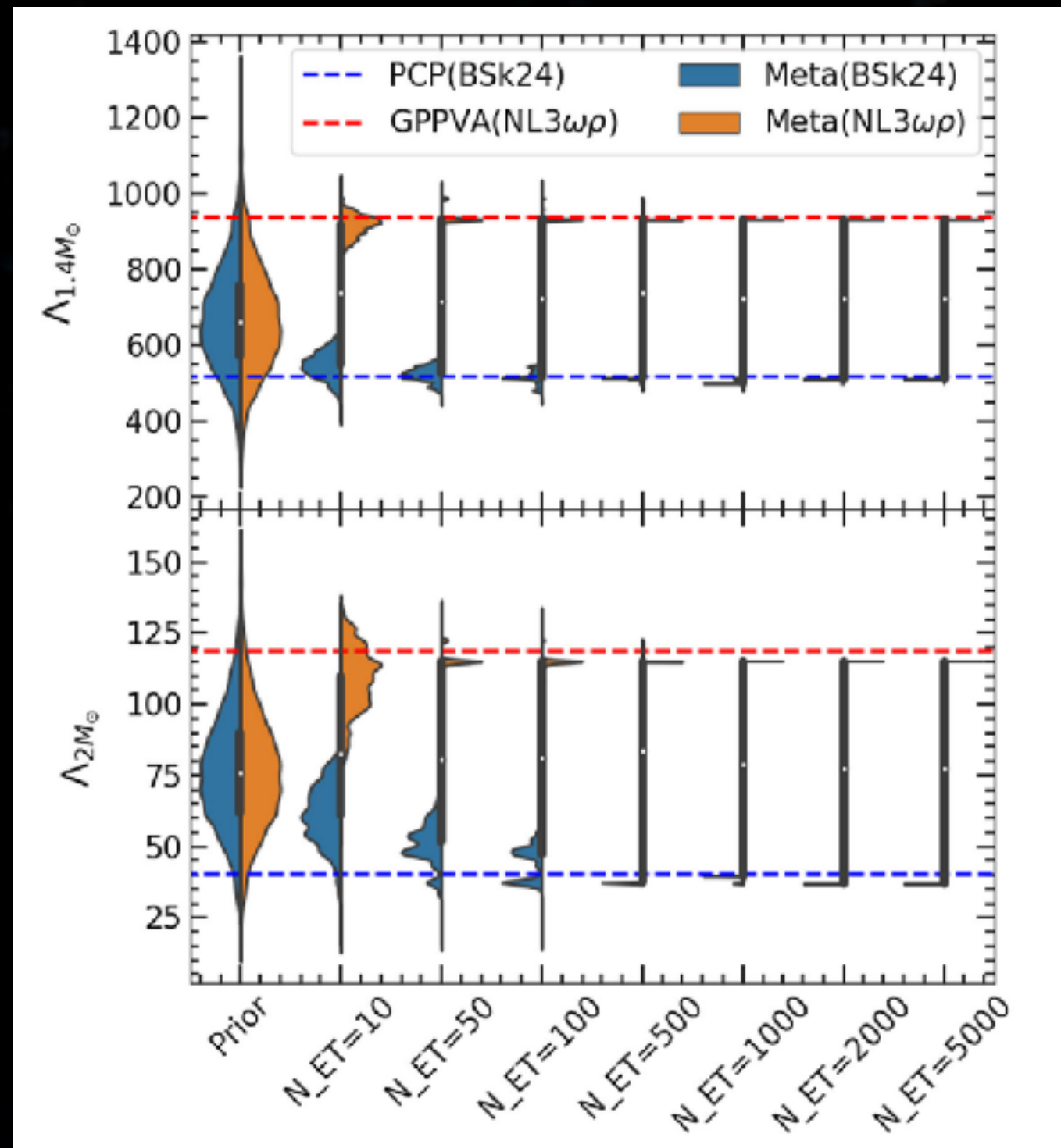
NS Structure

Important Physics

Astro Observables



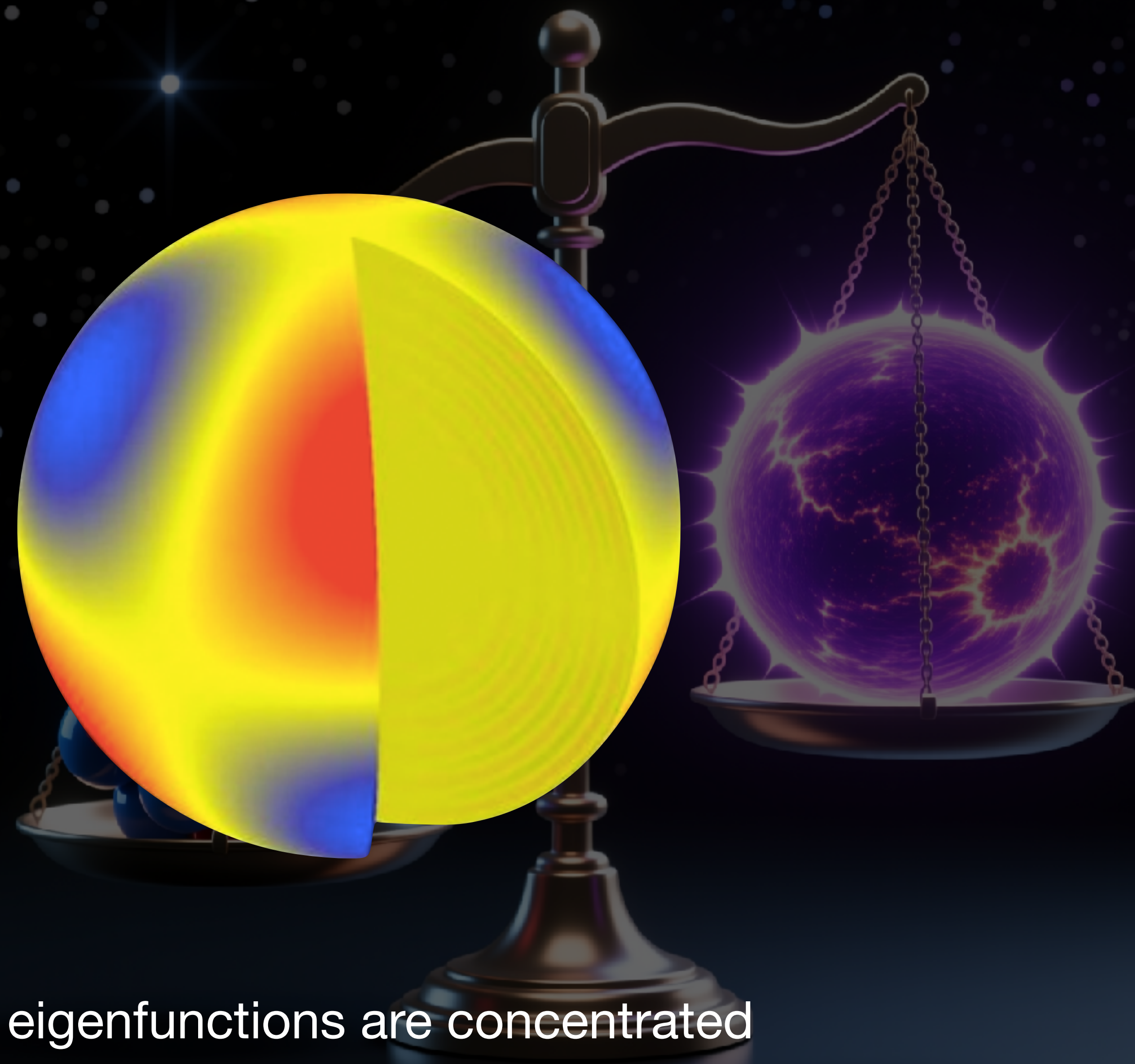
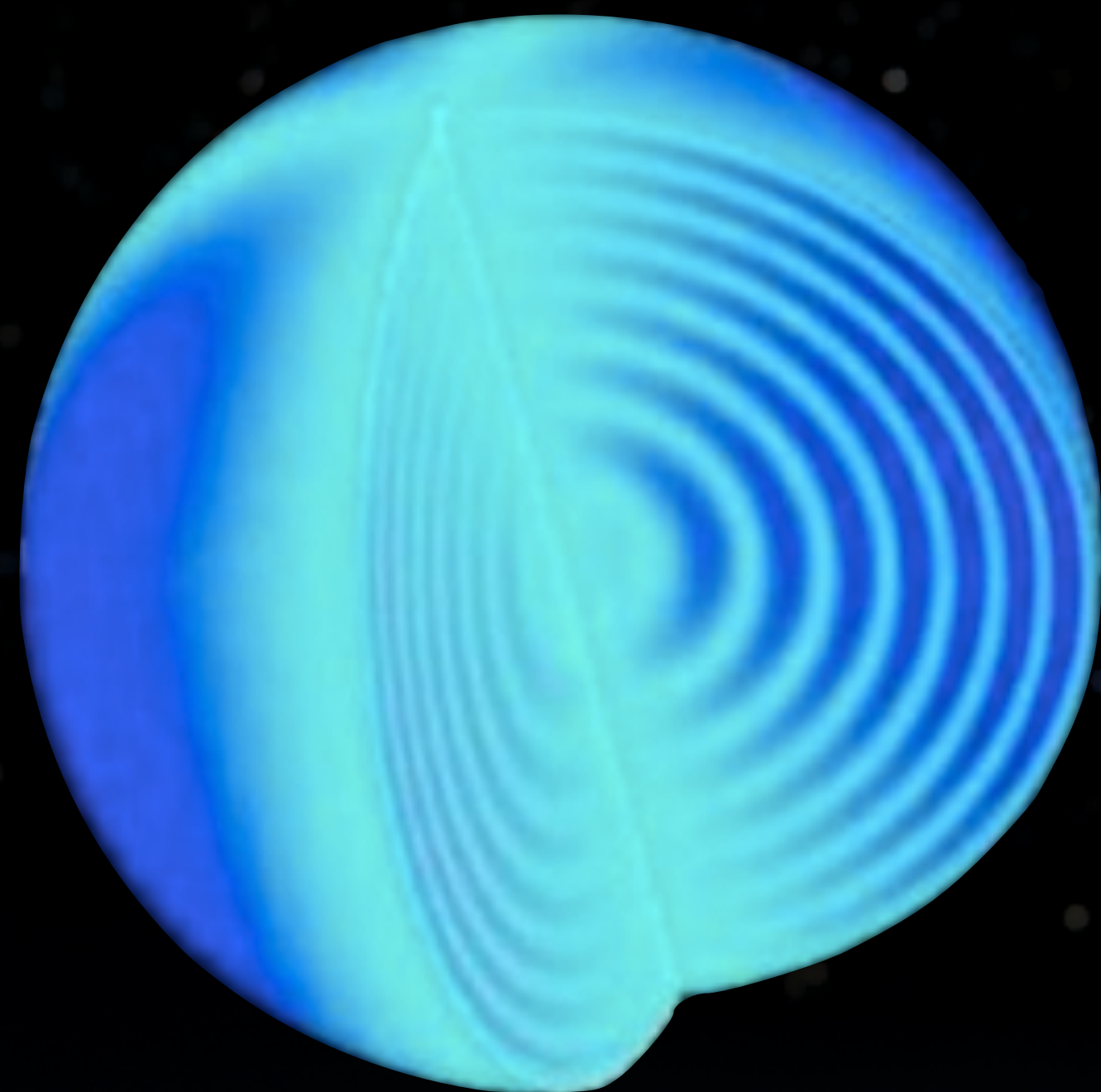
GW Bulk Observables



If you assume the entire star is nucleonic then constraints can be placed on the radius and isovector/isoscalar parameters from the GW tidal deformability, particularly with the next gen observatories. However, this isn't necessarily a good assumption.

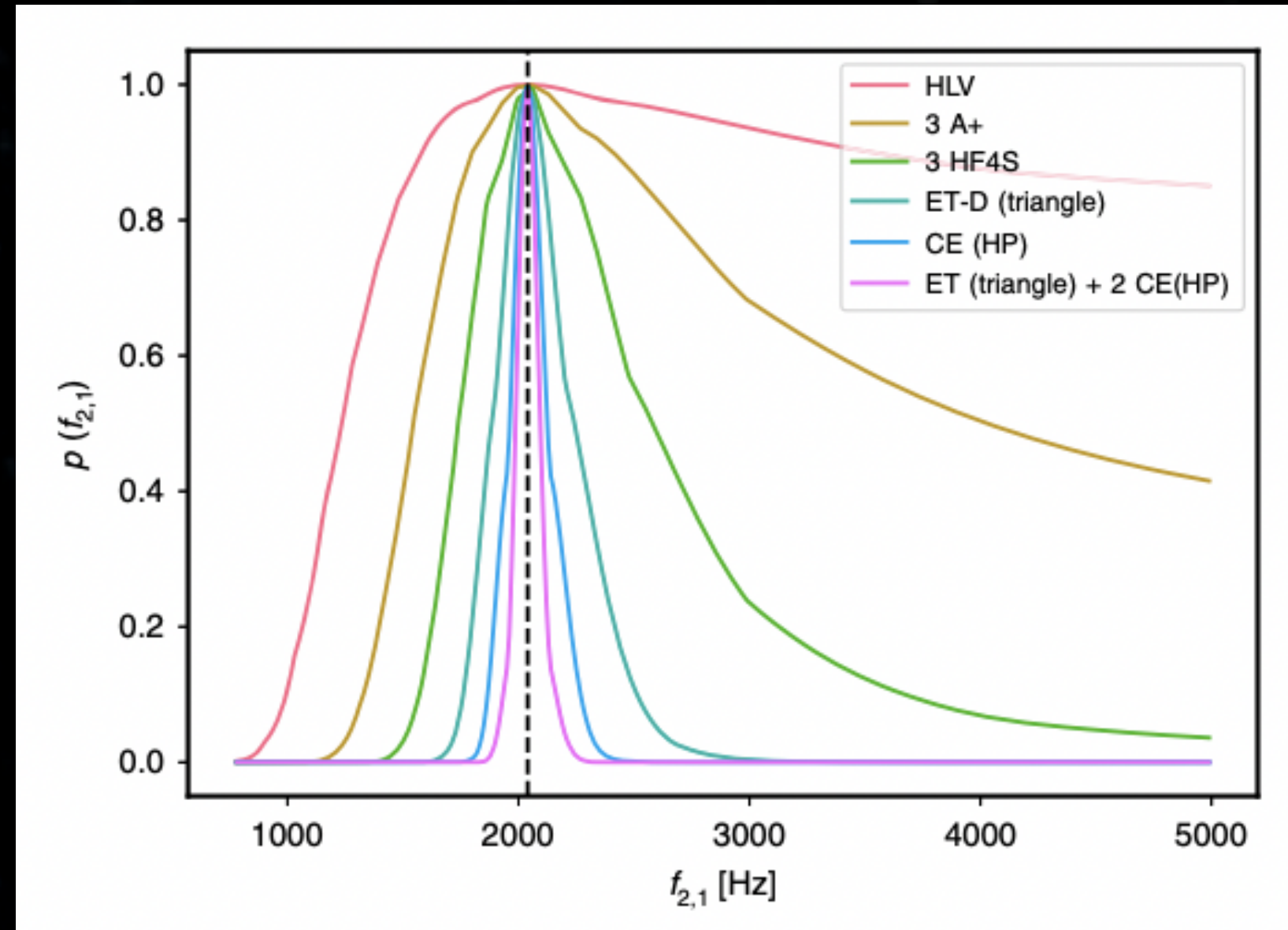
See Legred et al (2025) arXiv:2505.07677, or Isaac's entire talk on Monday

Asteroseismology!



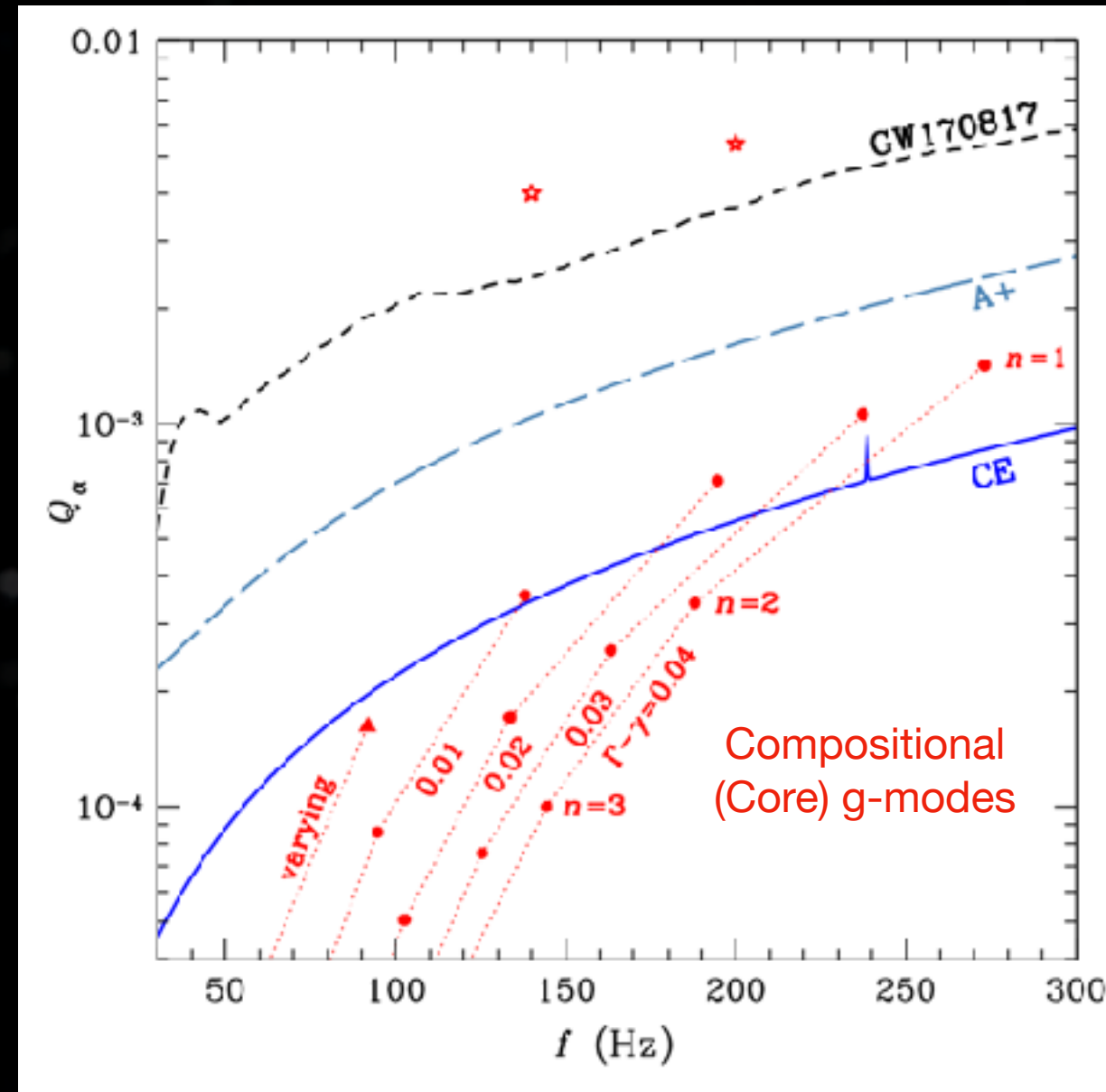
Modes probe the dynamics where their eigenfunctions are concentrated

Asteroseismology!



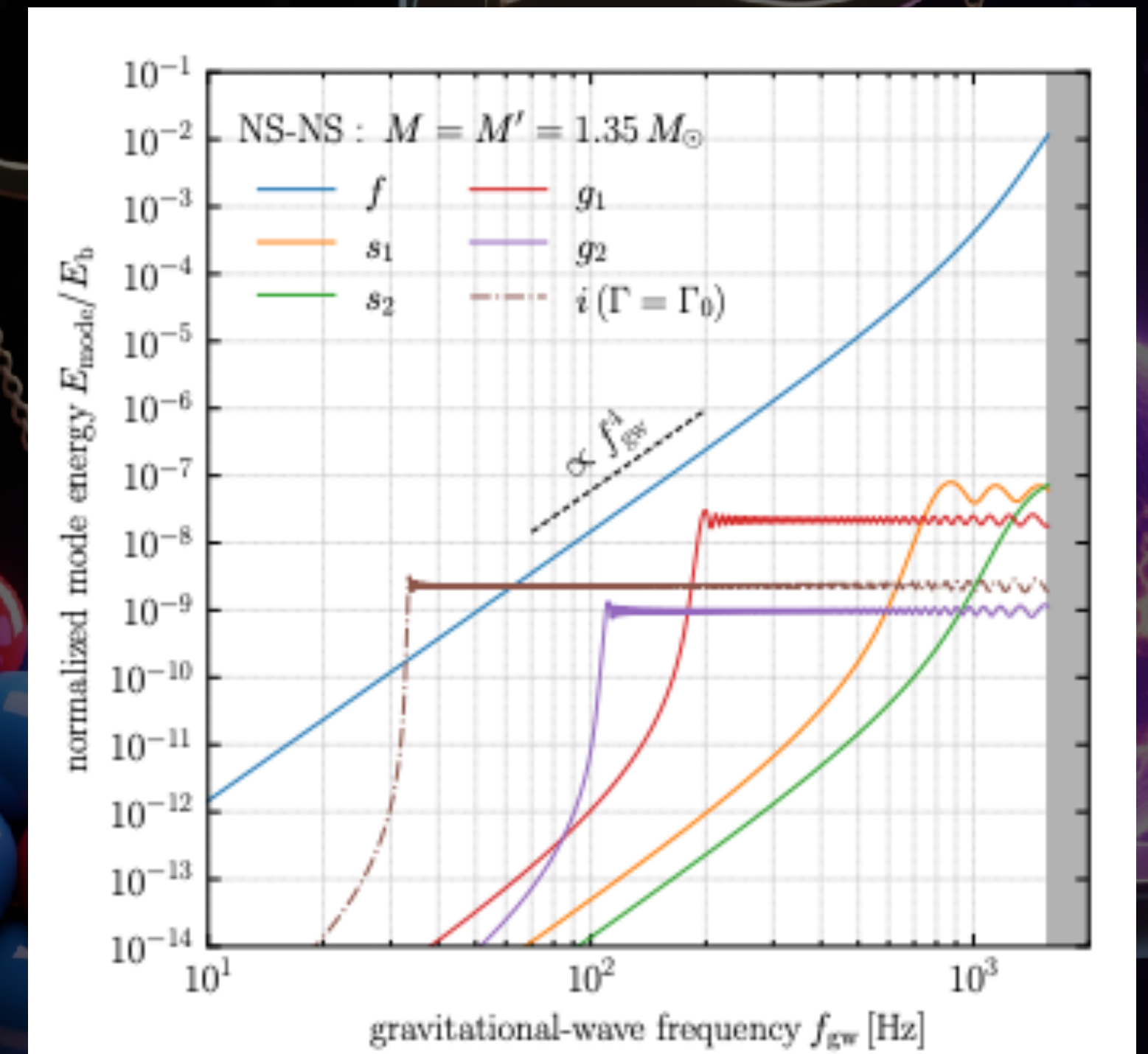
Fundamental modes (same EOS info as Λ)
(non-resonant during inspiral)

Pratten, Schmidt, & Hinderer (2020) Nature Comm., 11, 2553

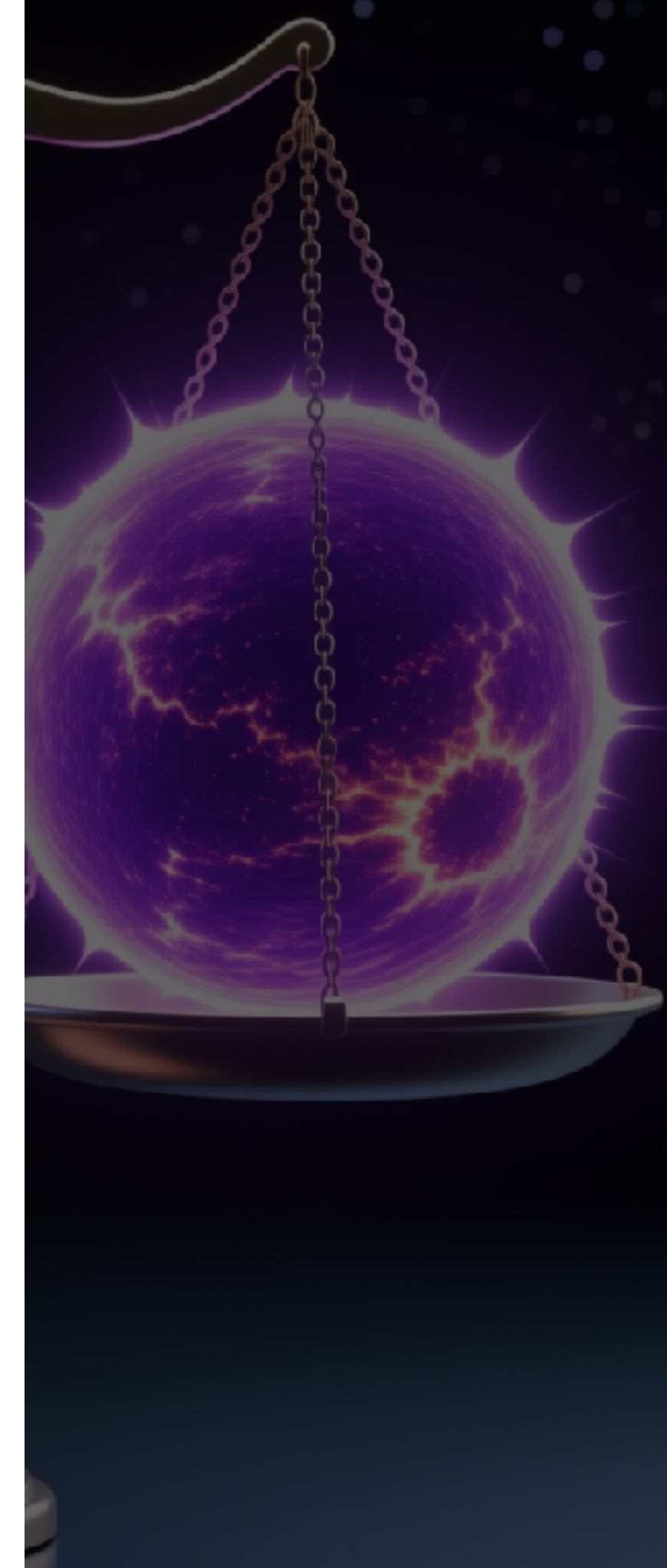
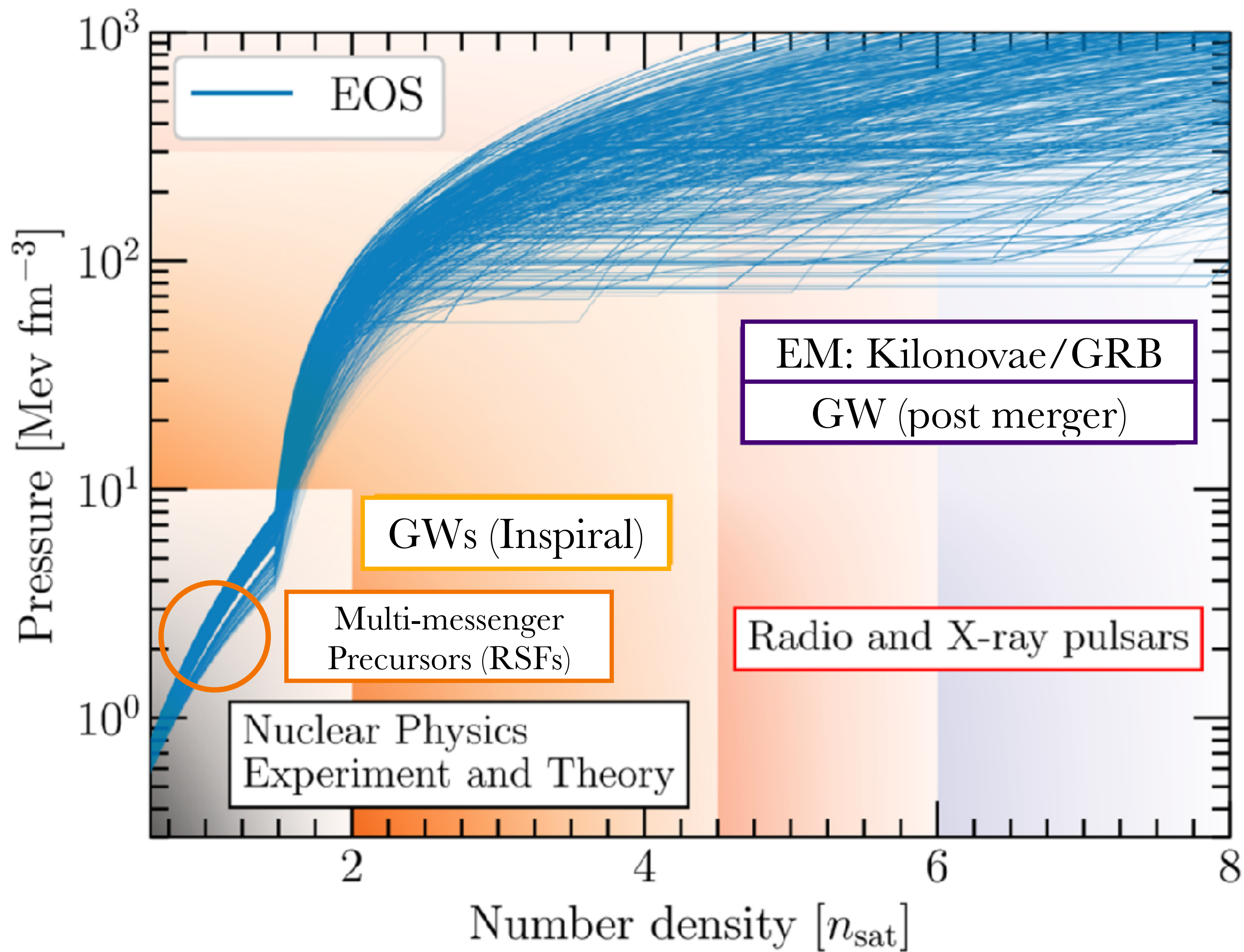


Other asteroseismic modes
(resonant during inspiral)

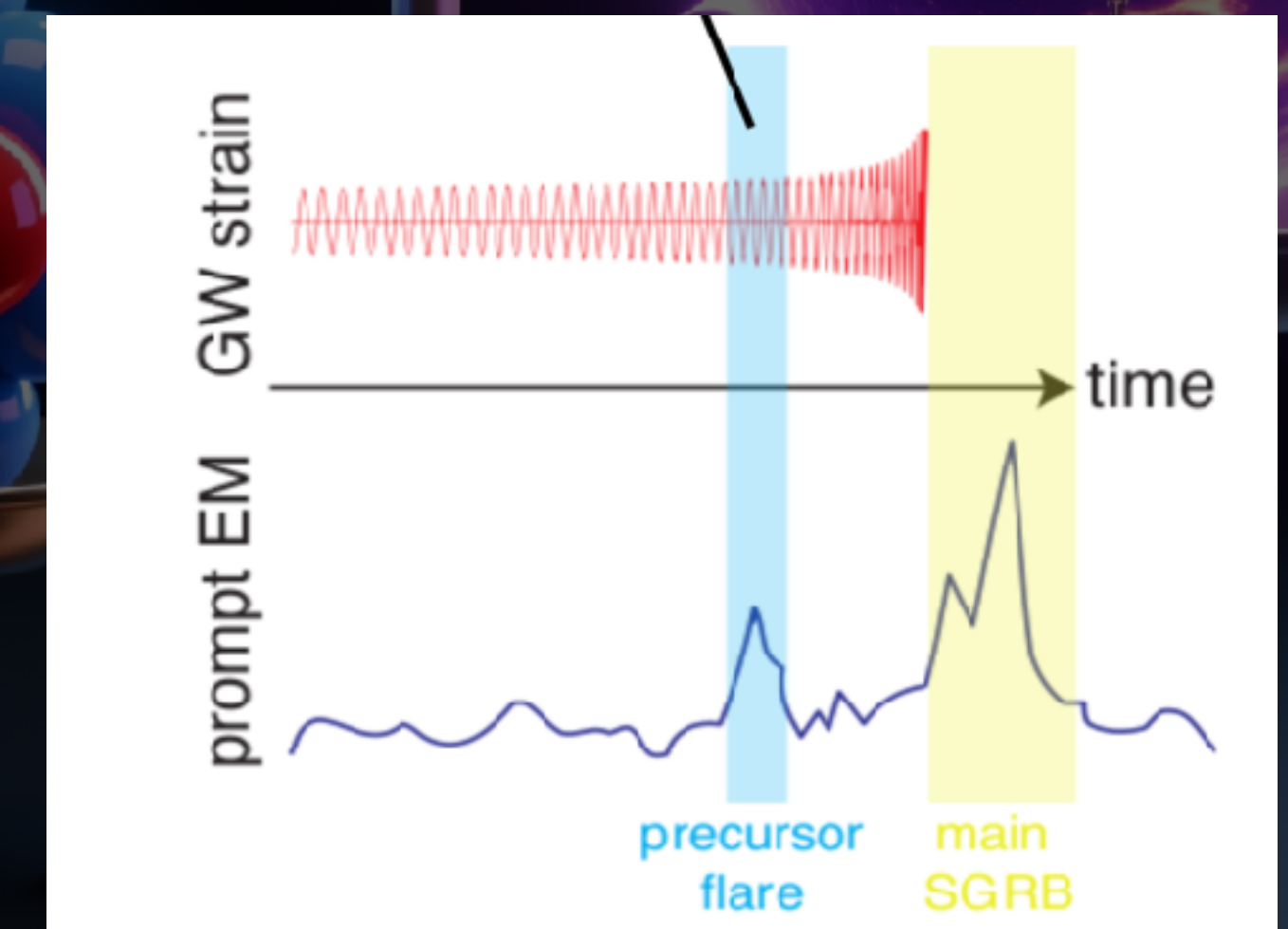
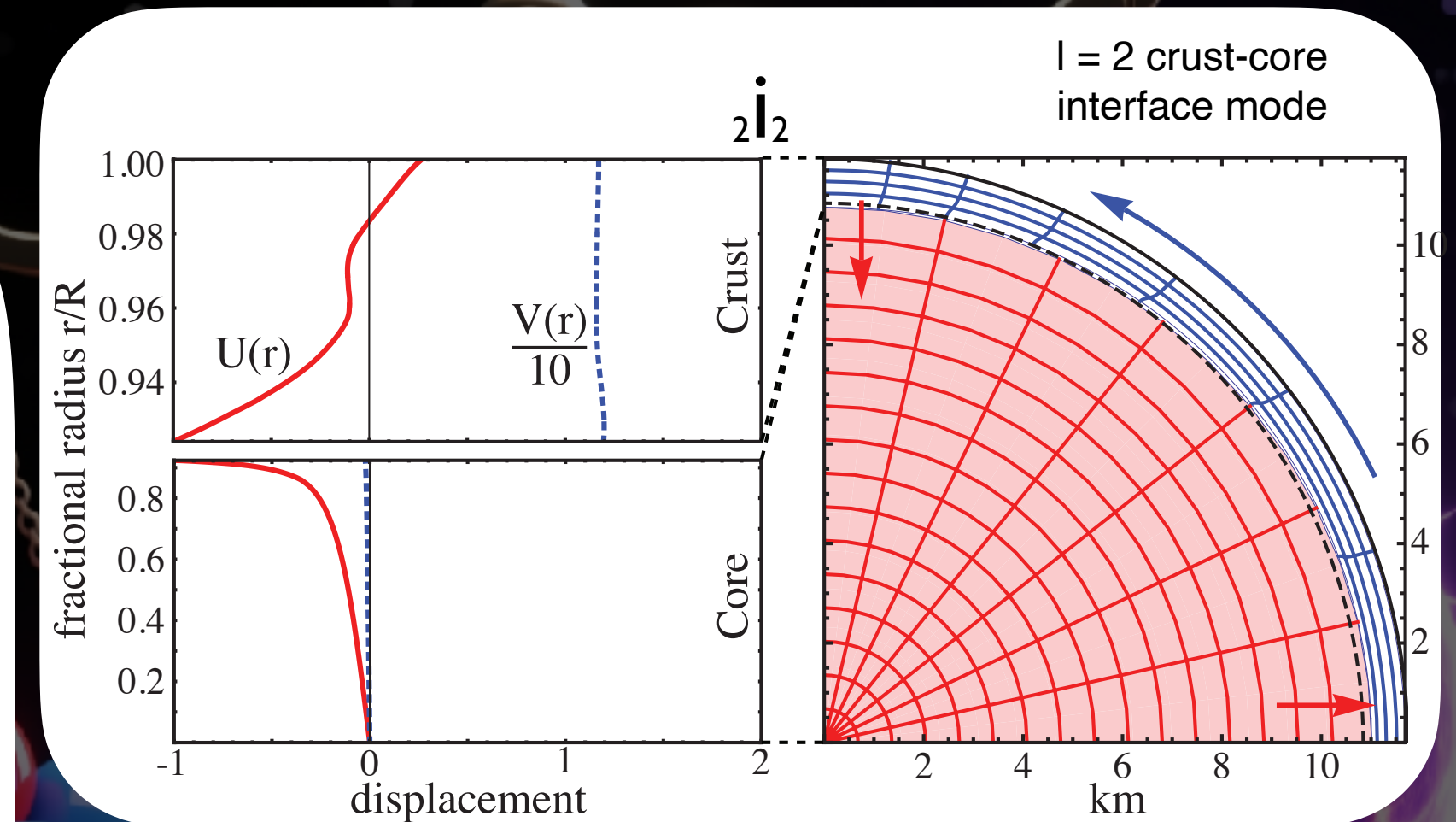
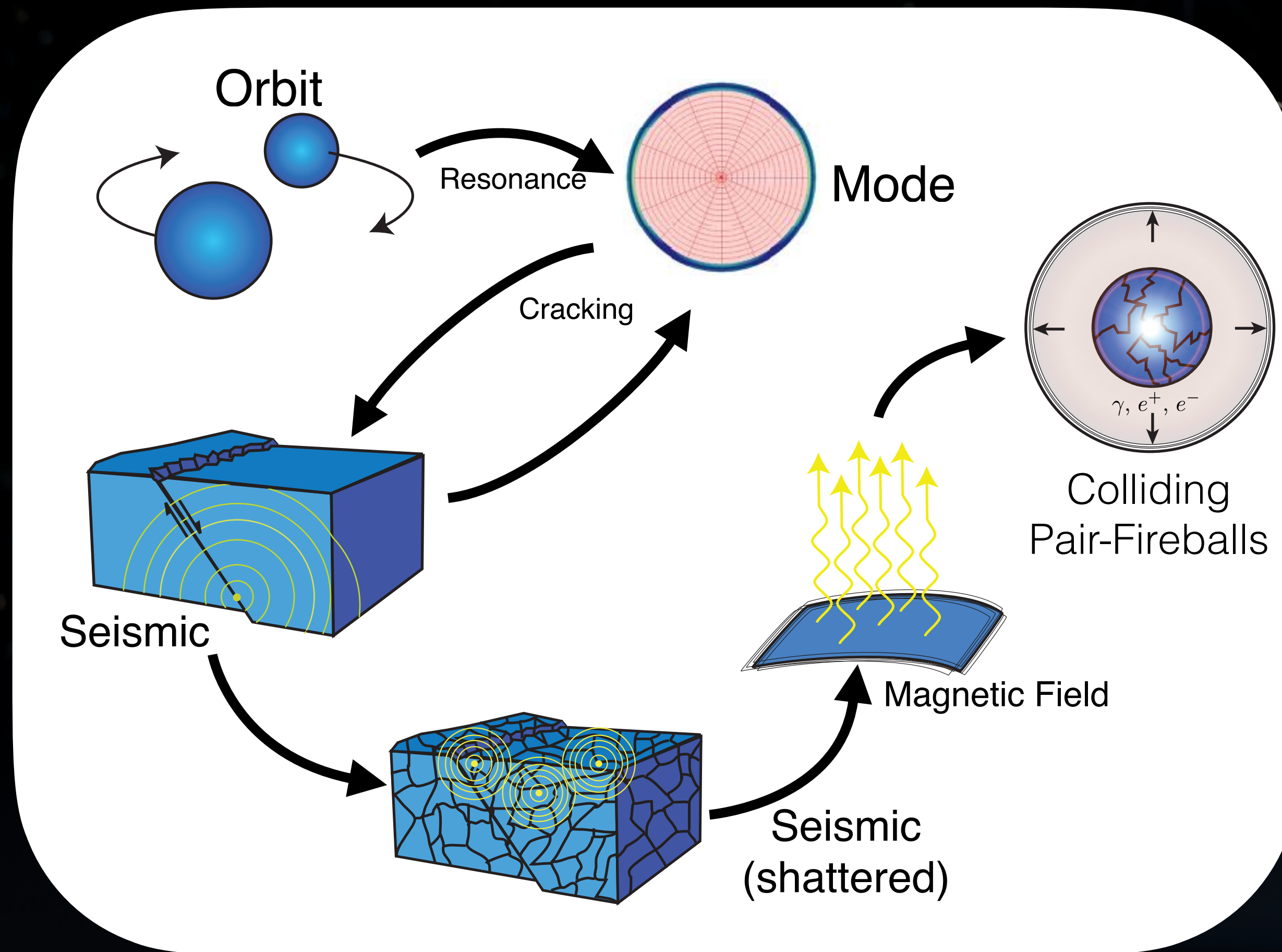
Ho & Andersson (2023), PRD 108, 043003



Gao et al (2025) arXiv:2509.00257v1



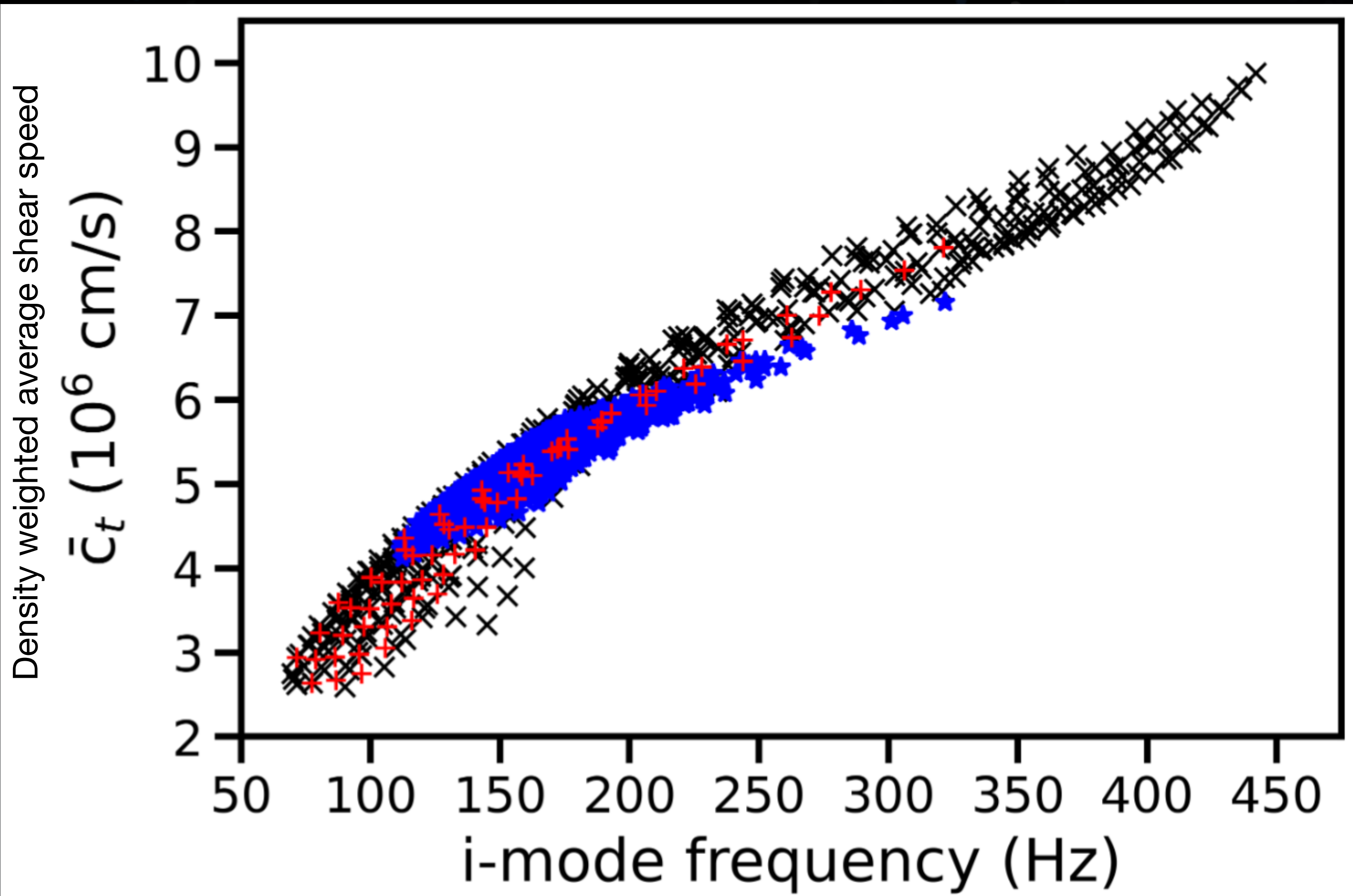
Multi-messenger Precursors (RSFs)

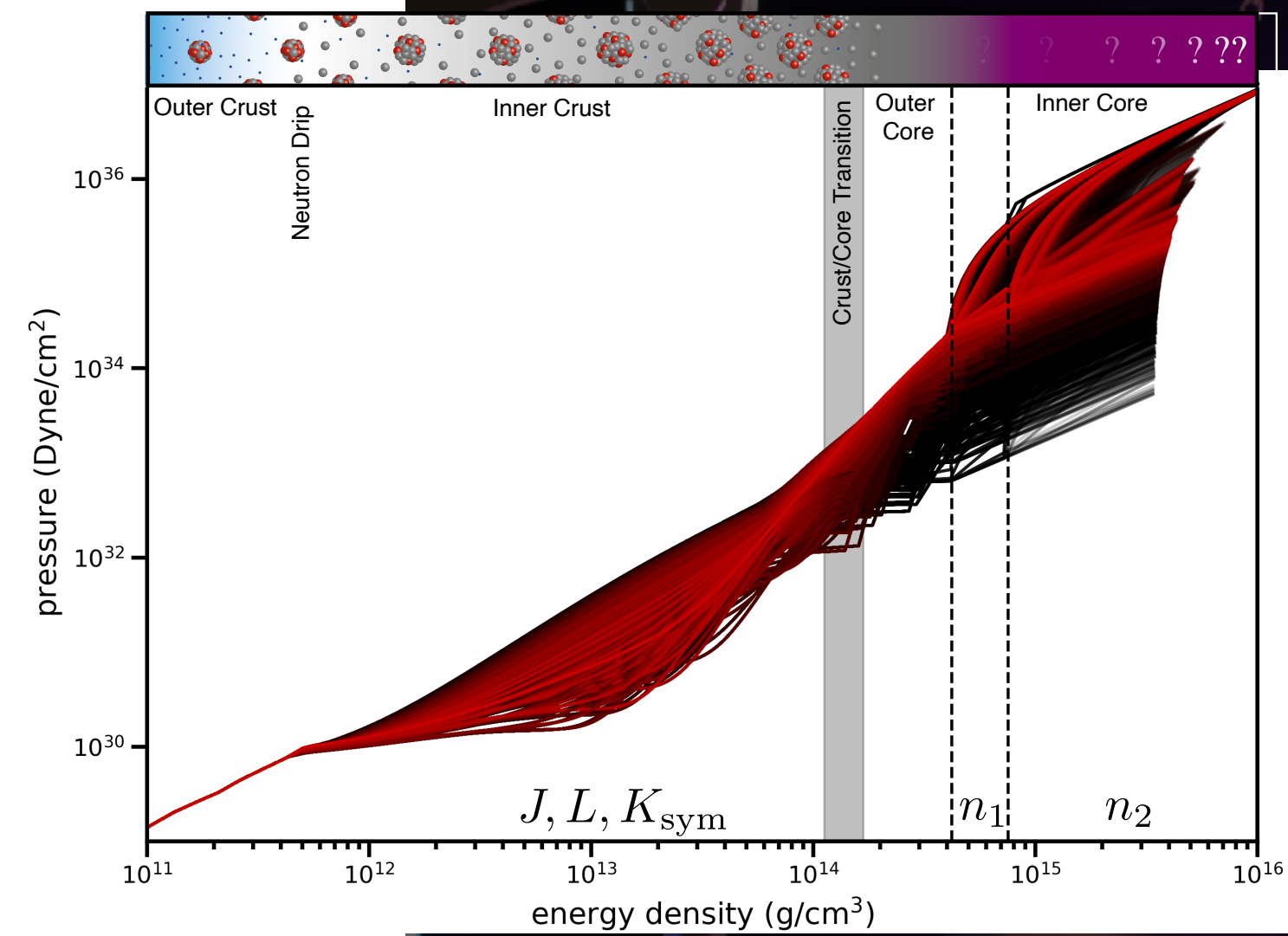
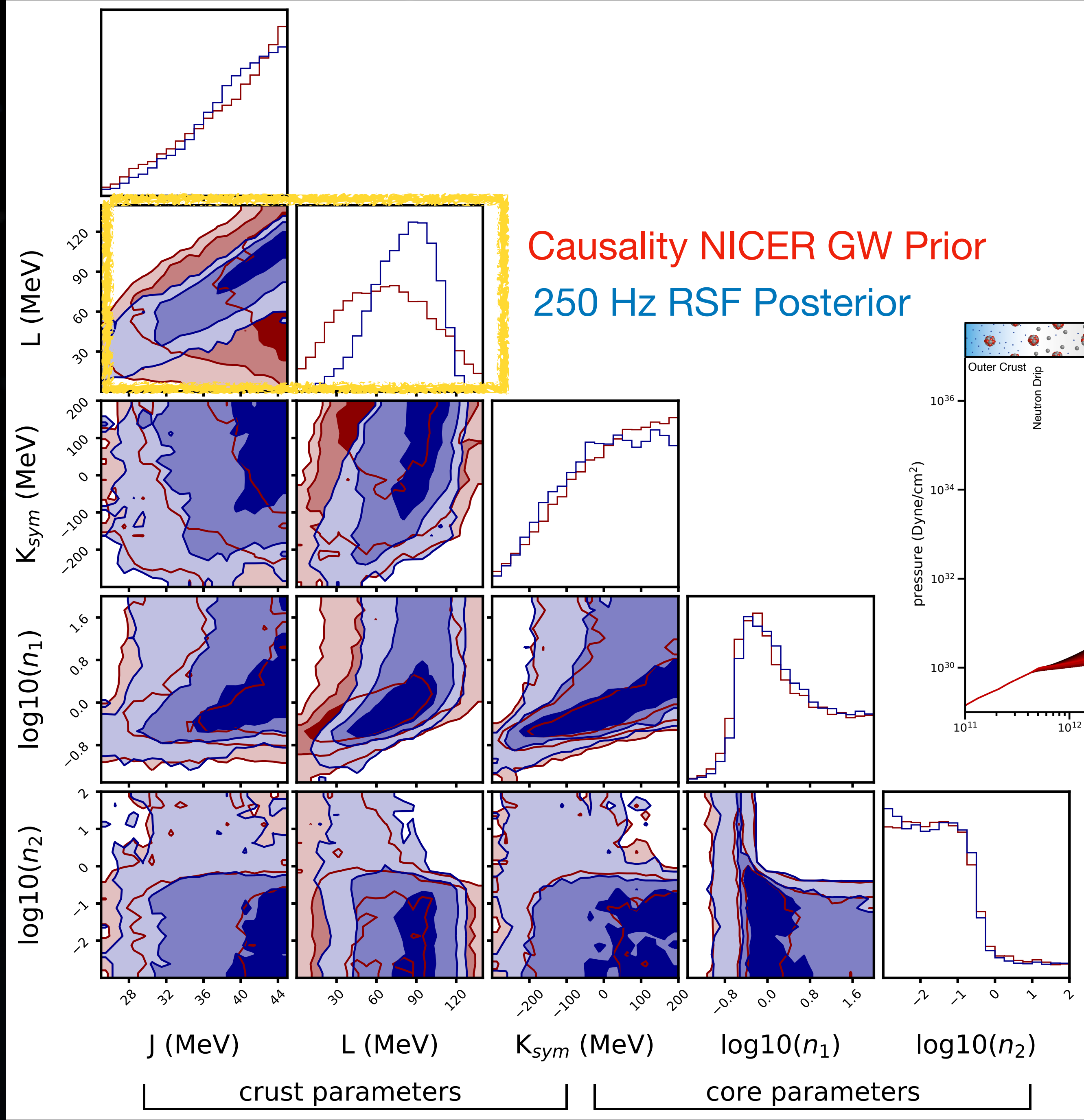


See also Kuan, Suvorov, & Kokkatos (2021),
Suvorov, Kuan, & Kokkatos (2024)
Gao, Kuan, Xia, Silva, & Shibata (2025)

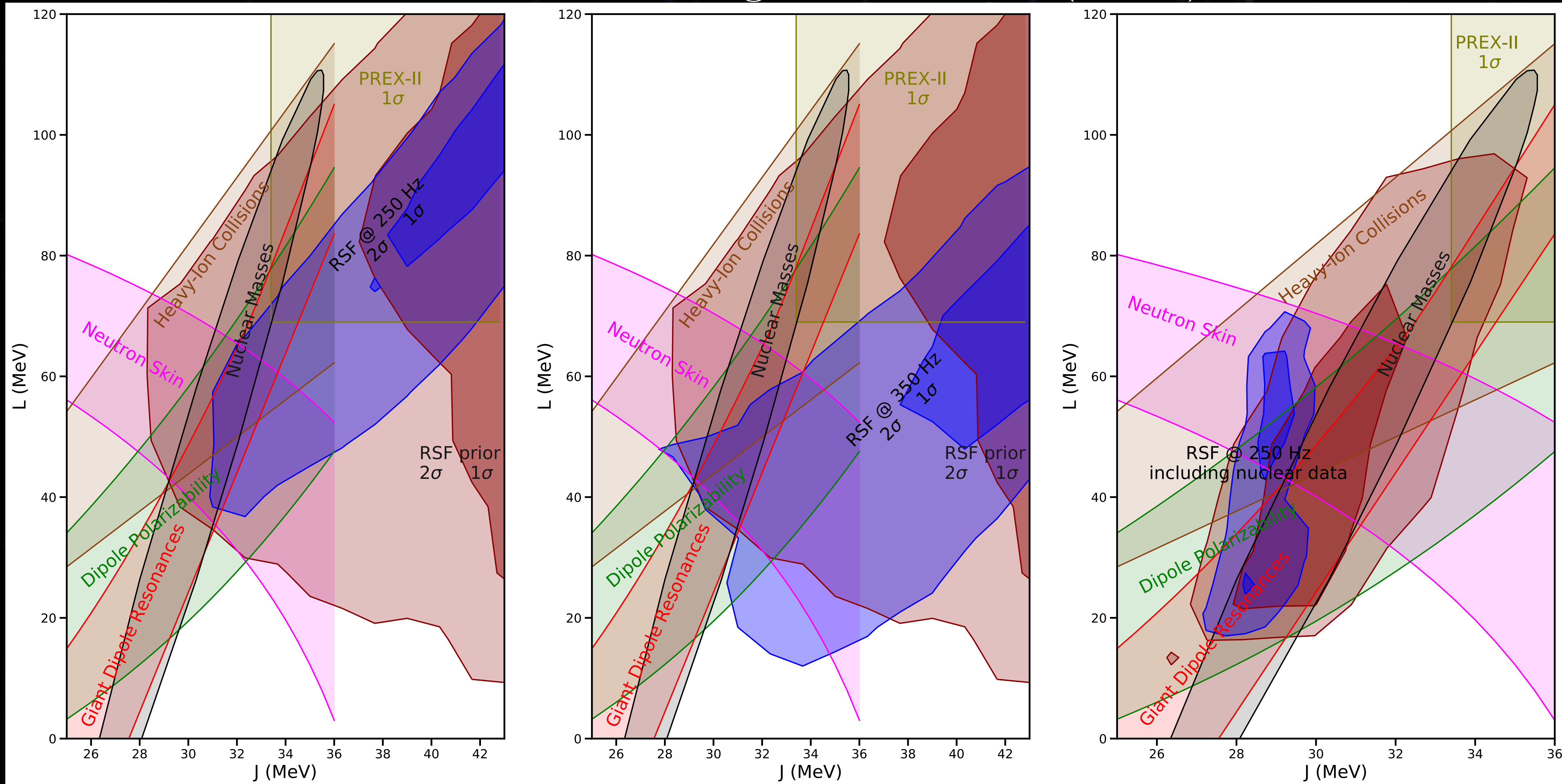
DT, et al. (2012) PRL 108, 011102
DT (2013) ApJ 777, 103
Neill, DT, Van Eerten, Ryan, & Newton (2022) MNRAS, 514, 4

Multi-messenger Precursors (RSFs)





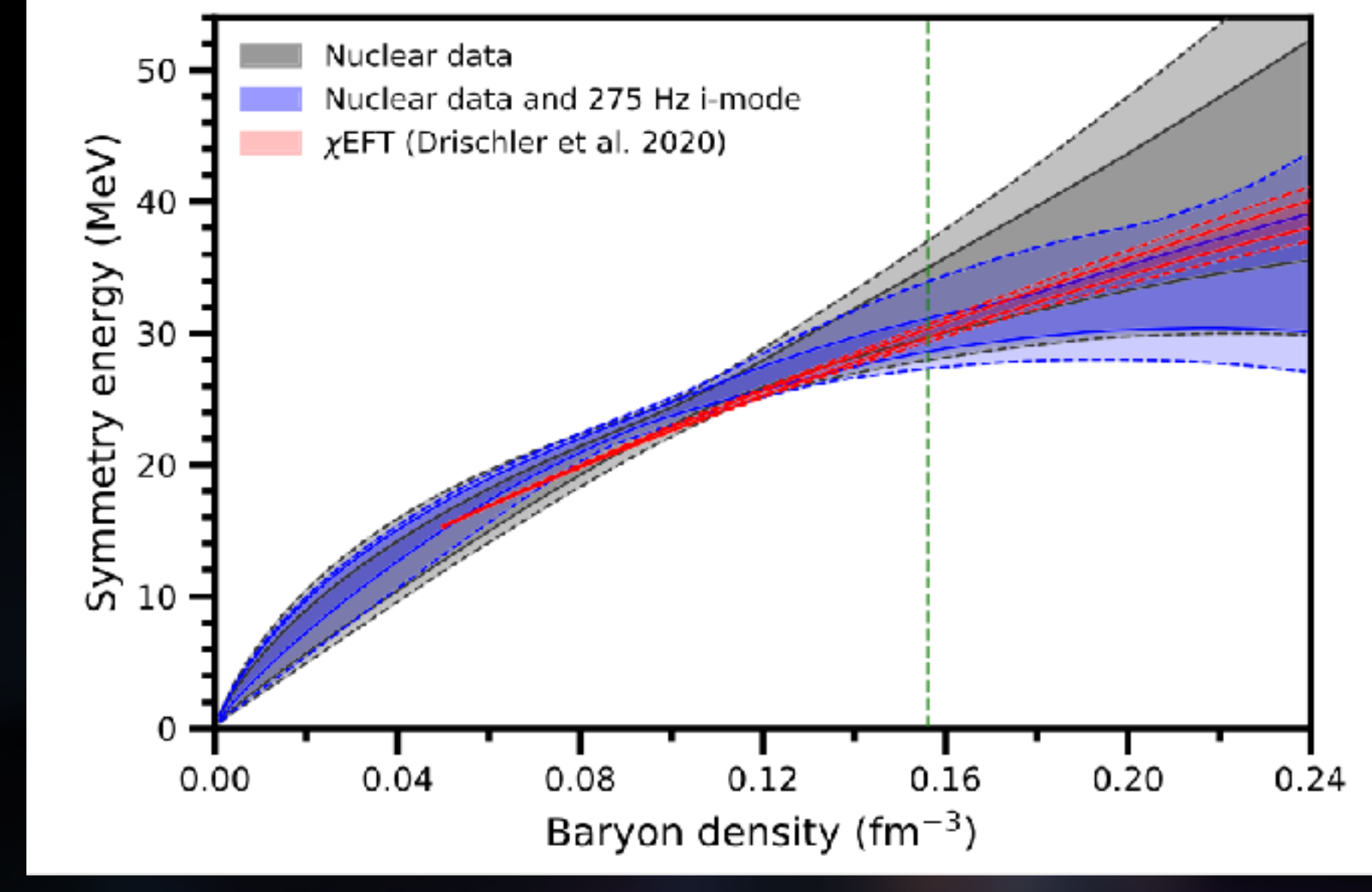
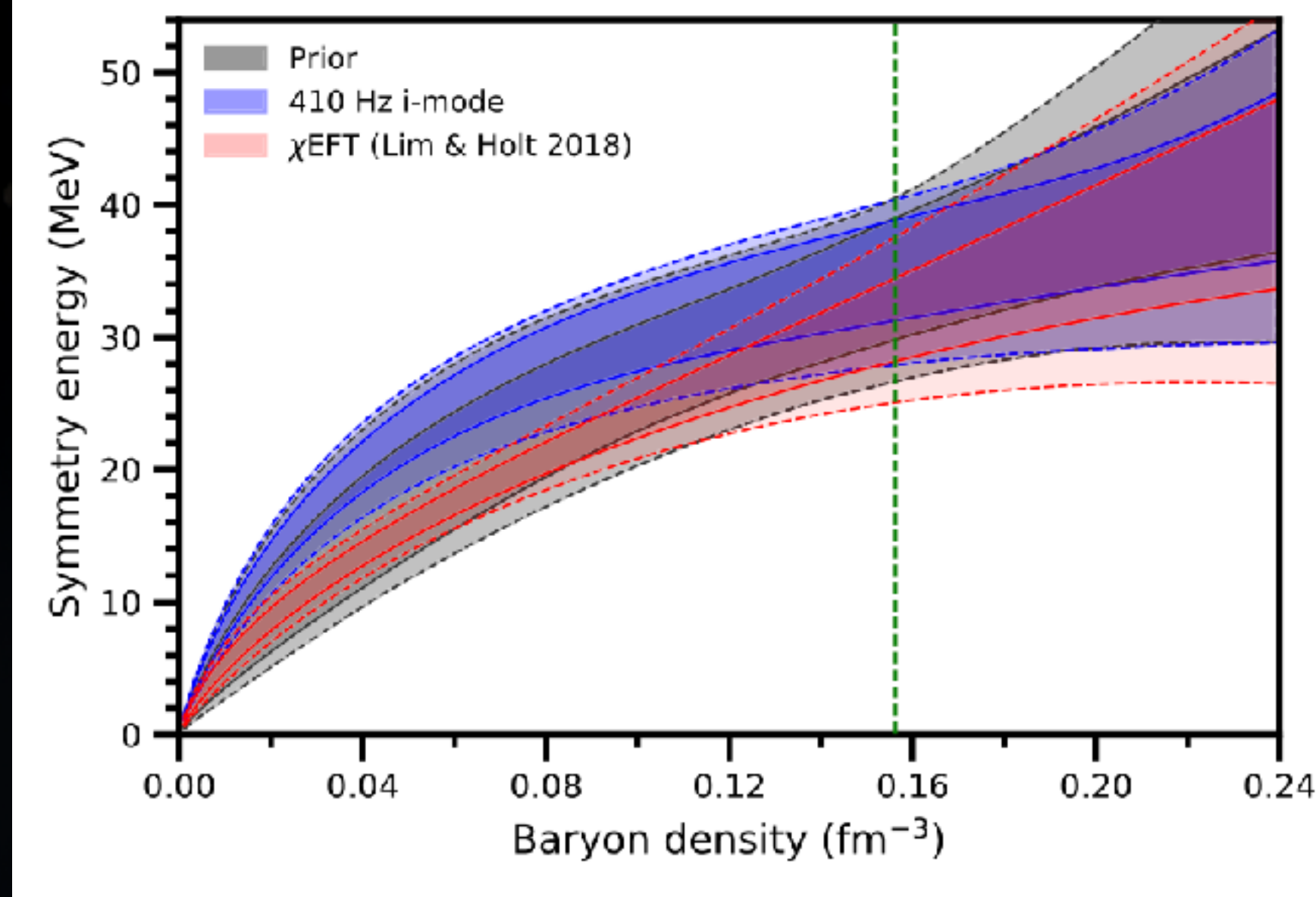
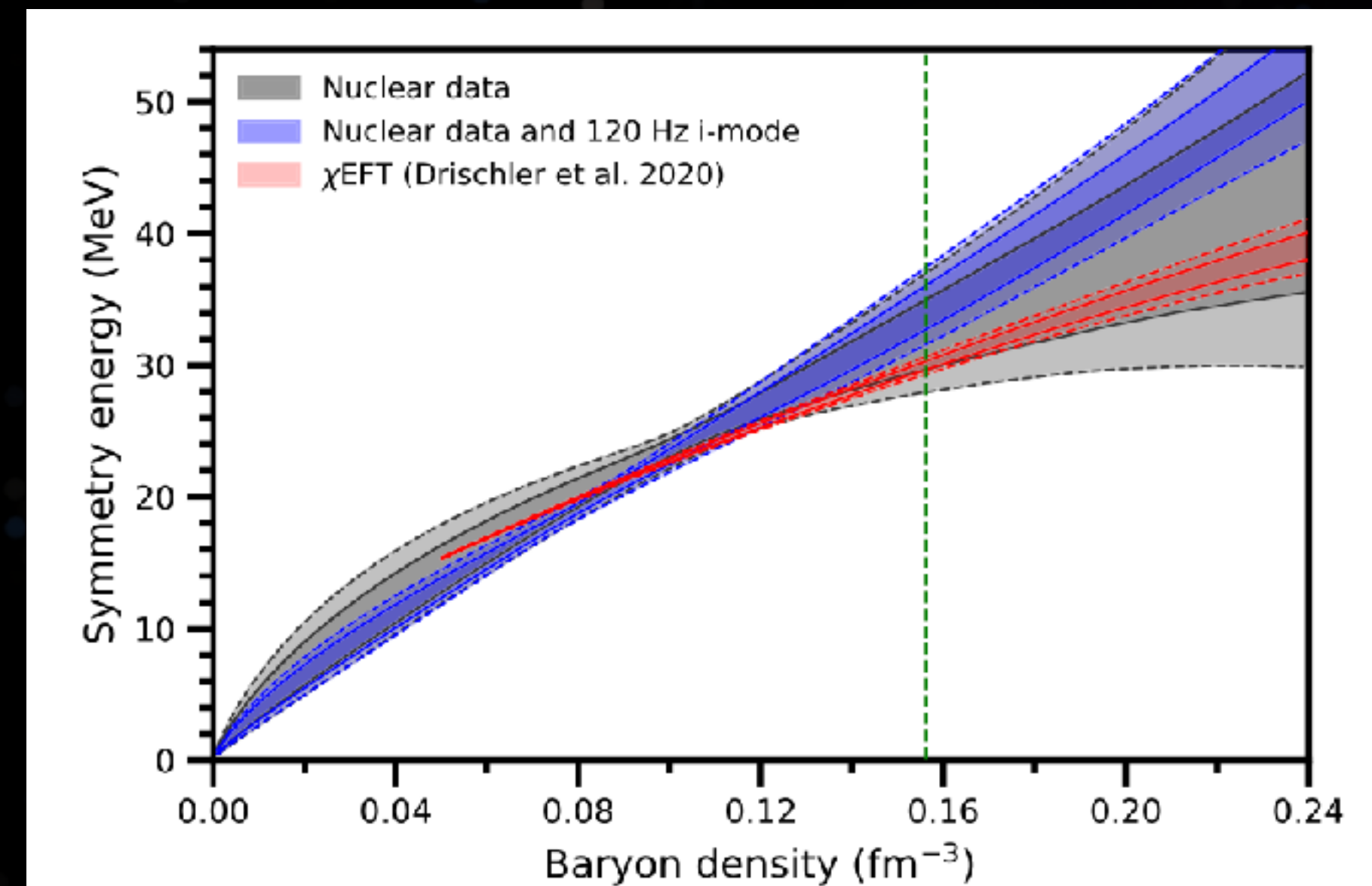
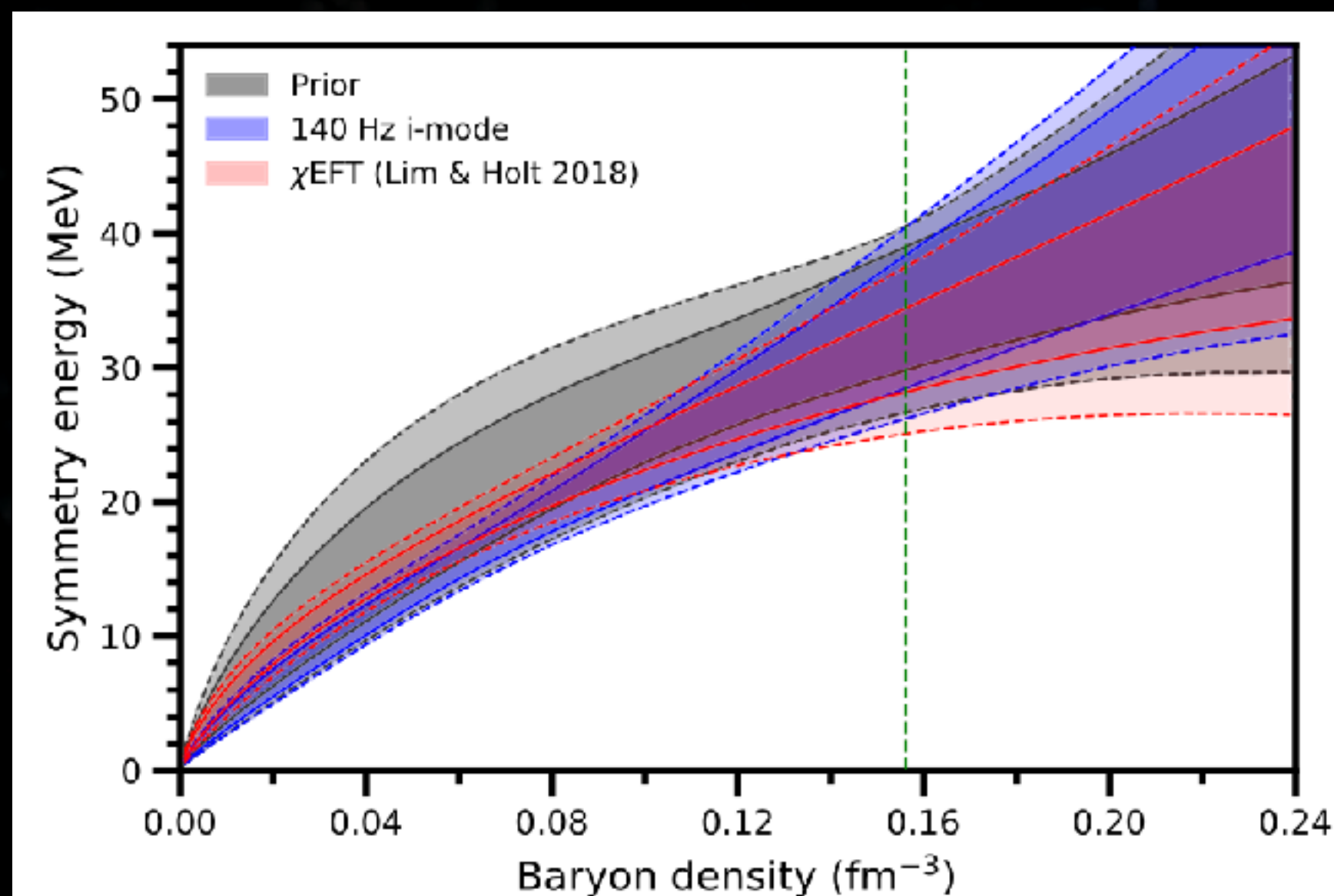
Multi-messenger Precursors (RSFs)



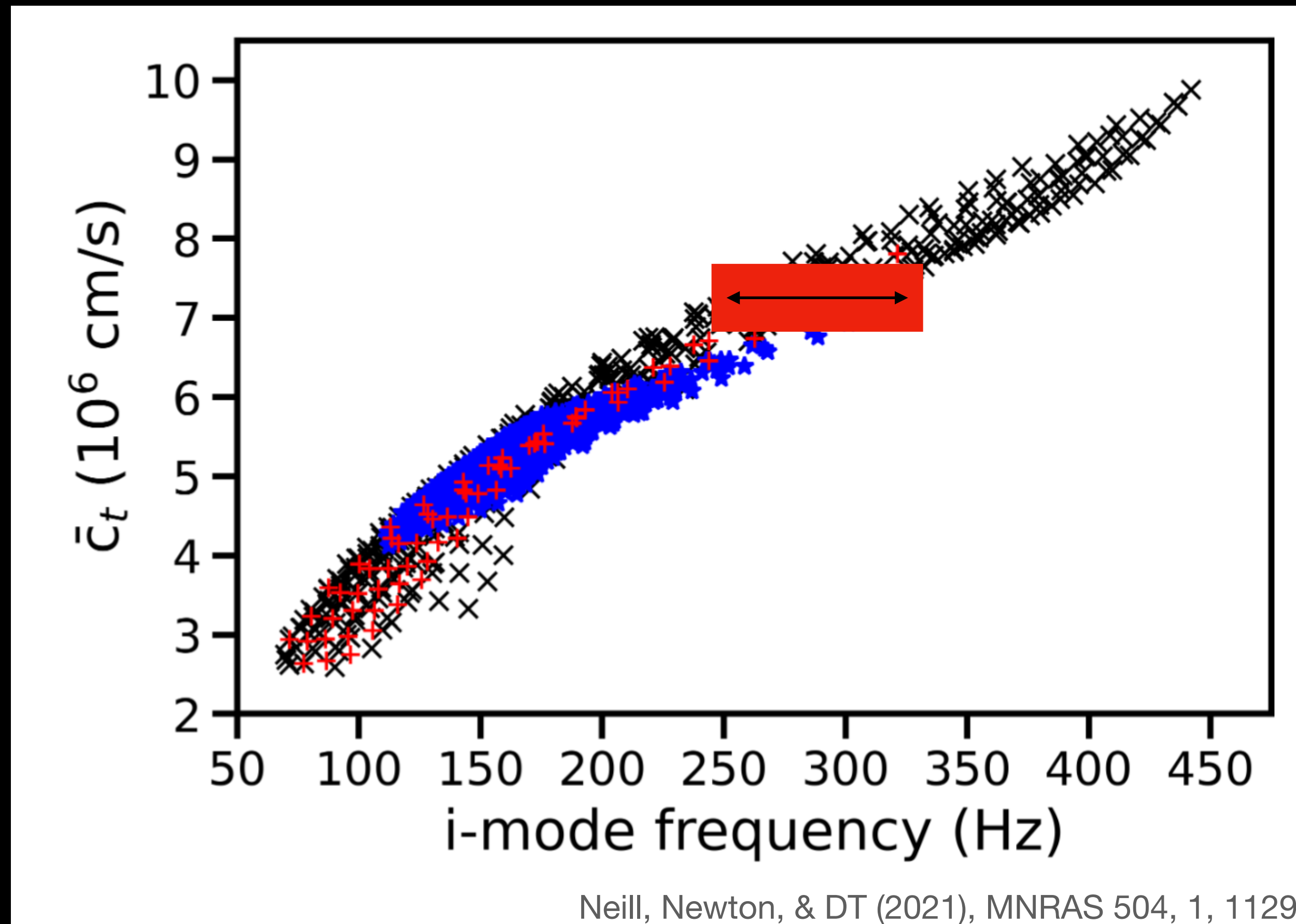
Neill, Preston, Newton & DT (2023), PRL, 130, 112701

See also Neill, DT, & Newton(2024) MNRAS 532, 1, 82

Testing Chiral Effective Field Theory with RSFs



But wait!

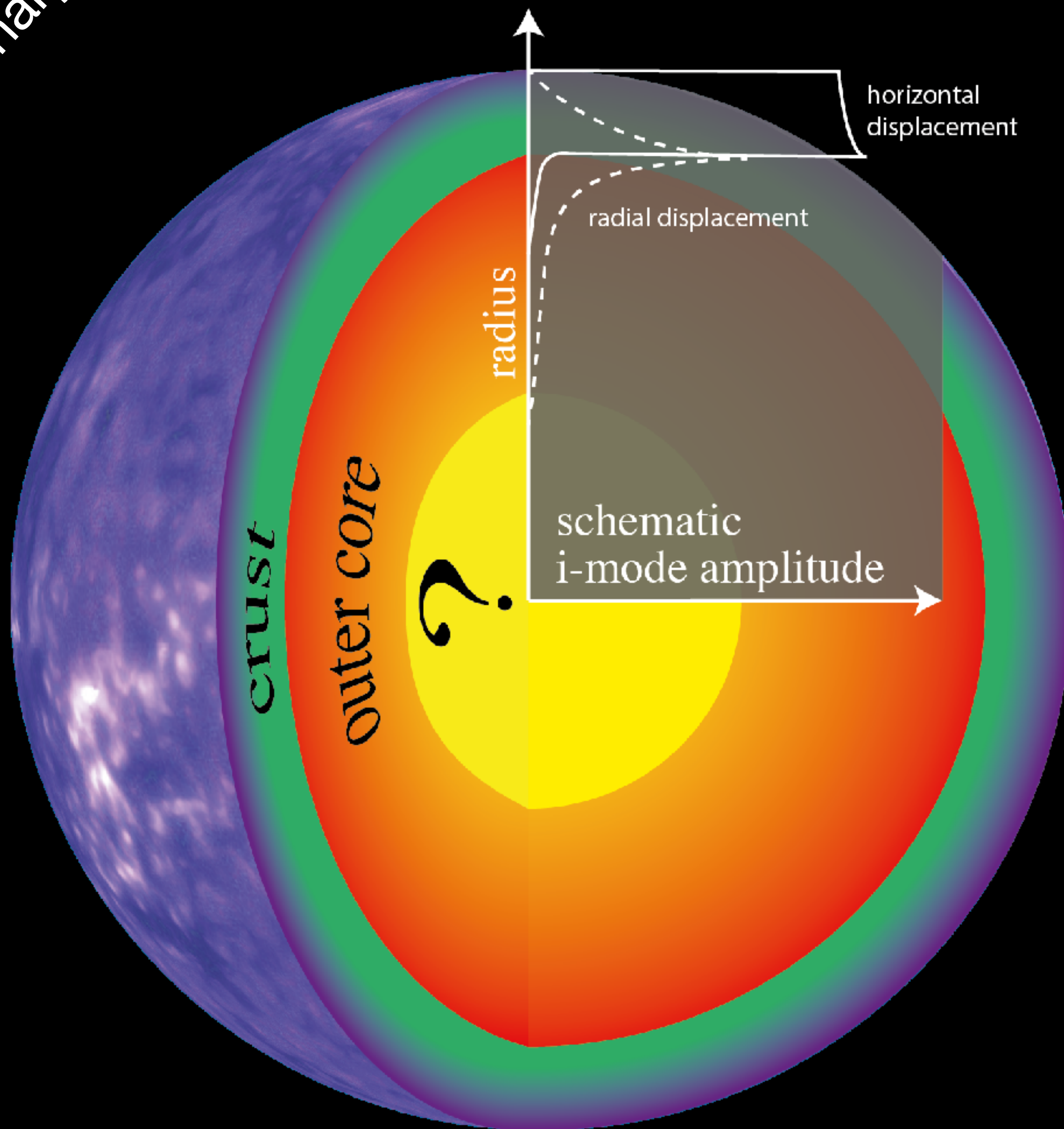


If we fix the crust/outer core physics...

What determines the spread of i-mode frequencies?

Preliminary

What determines the spread of i-mode frequencies?



frequency
fit
including

NS mass

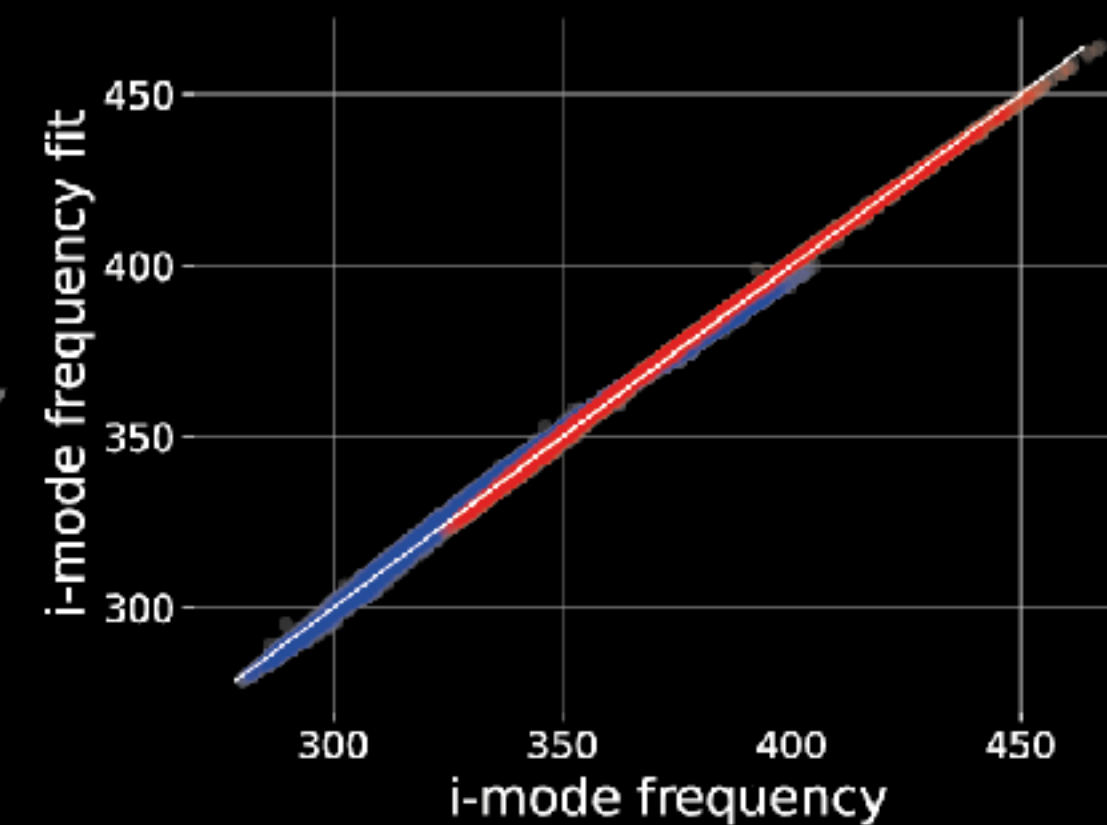
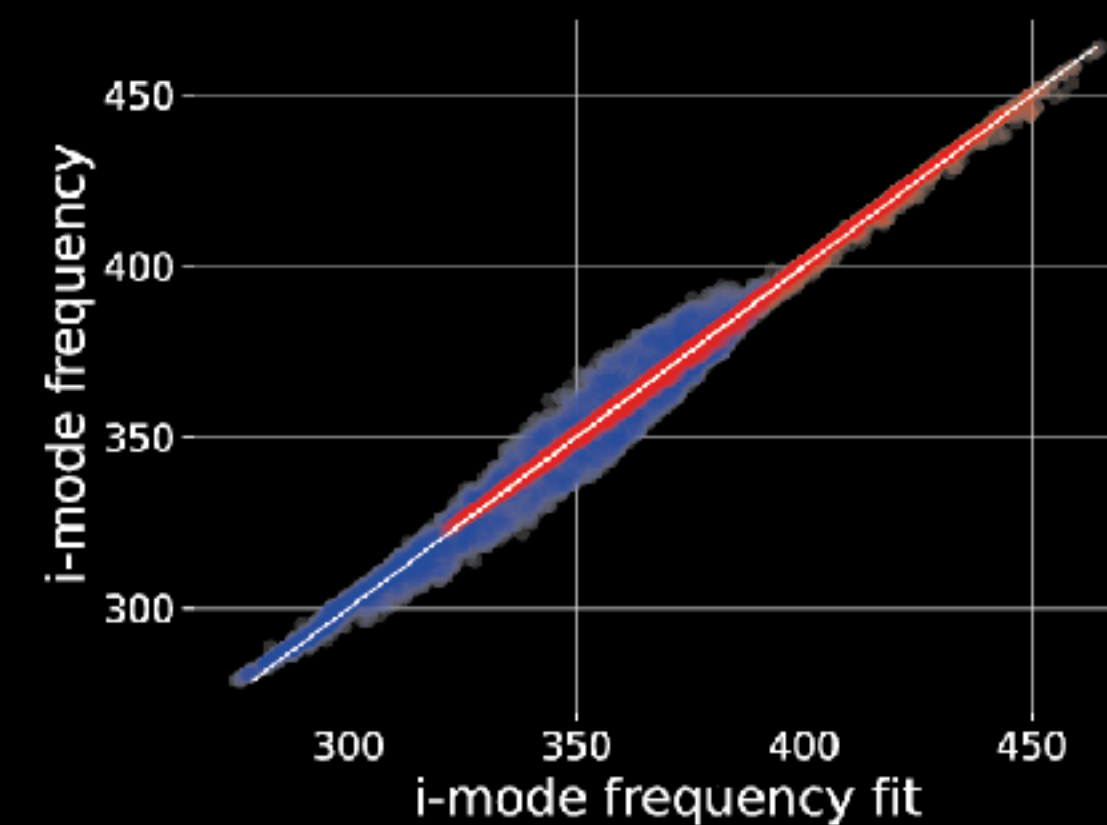
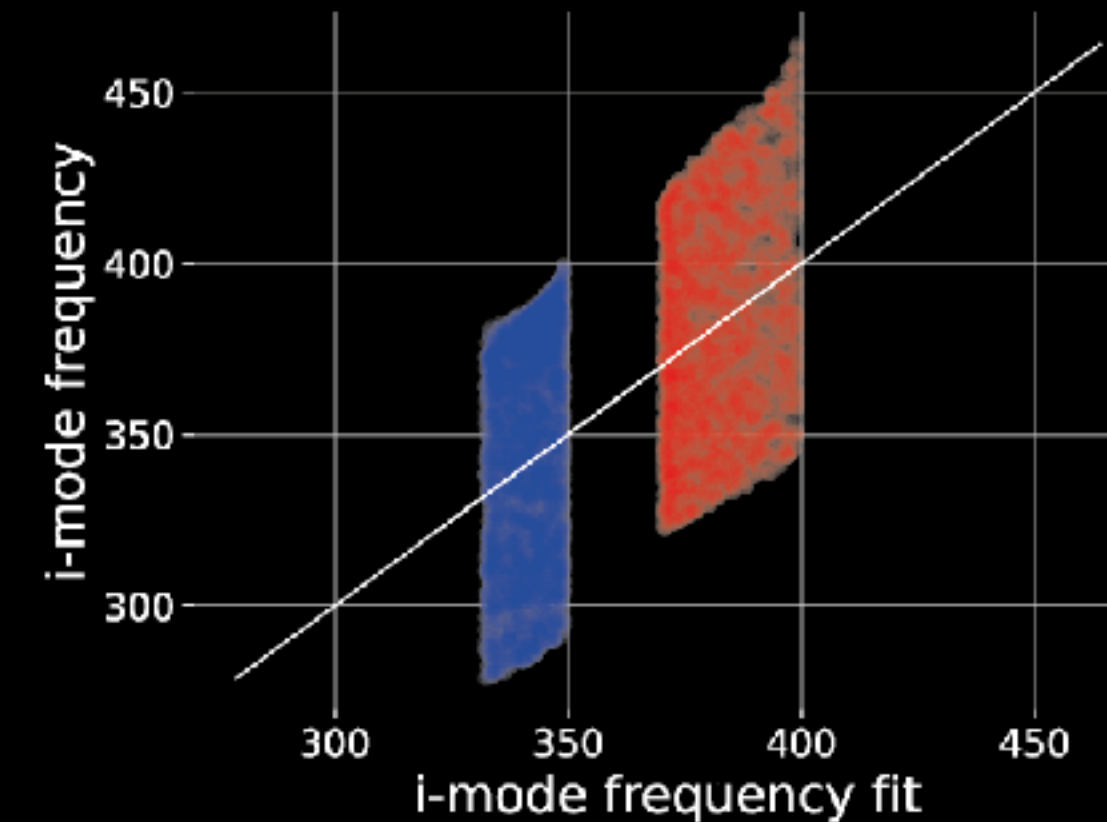
+

NS radius

+

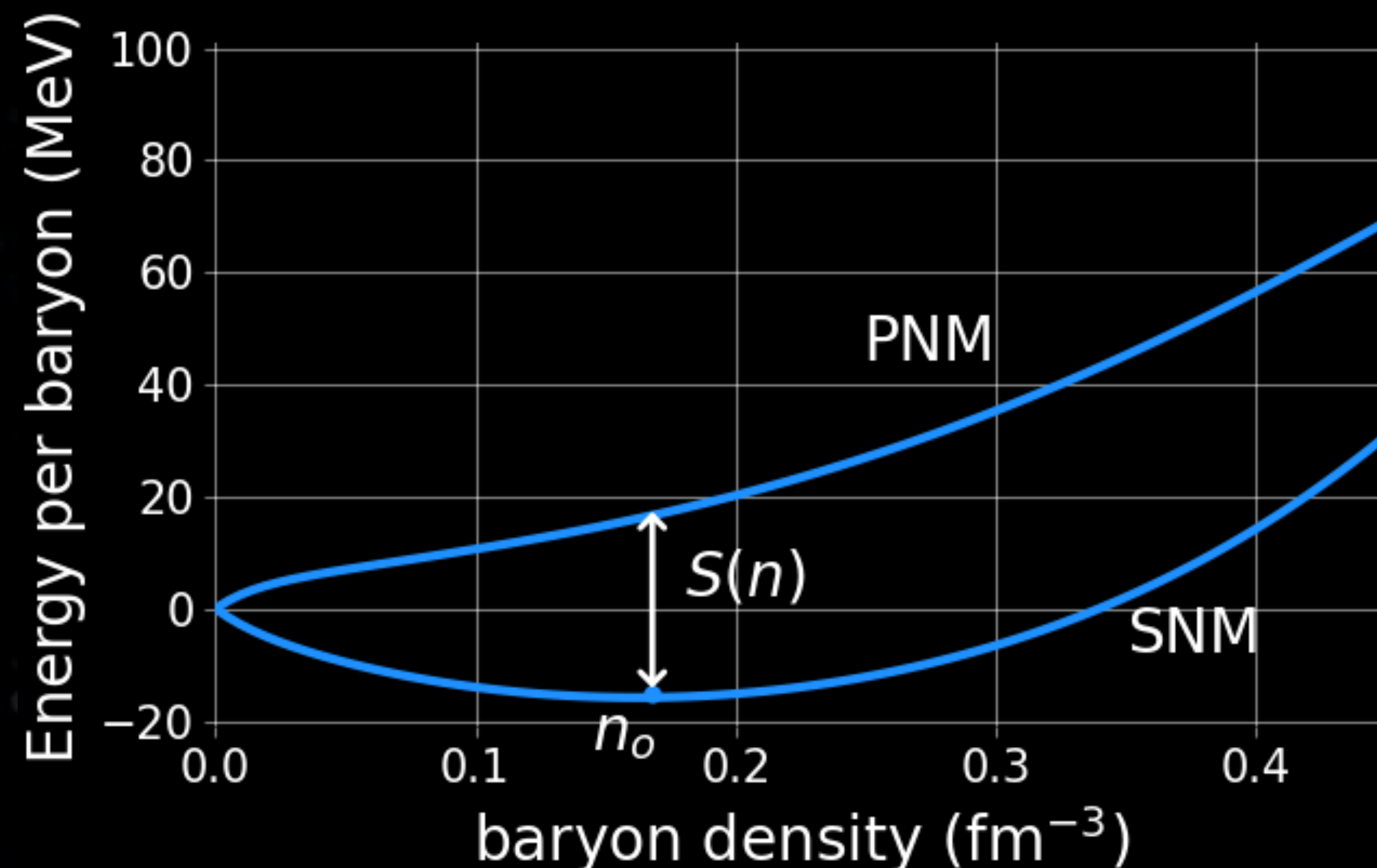
average
bouyancy

fixing nucleonic
(low density) physics

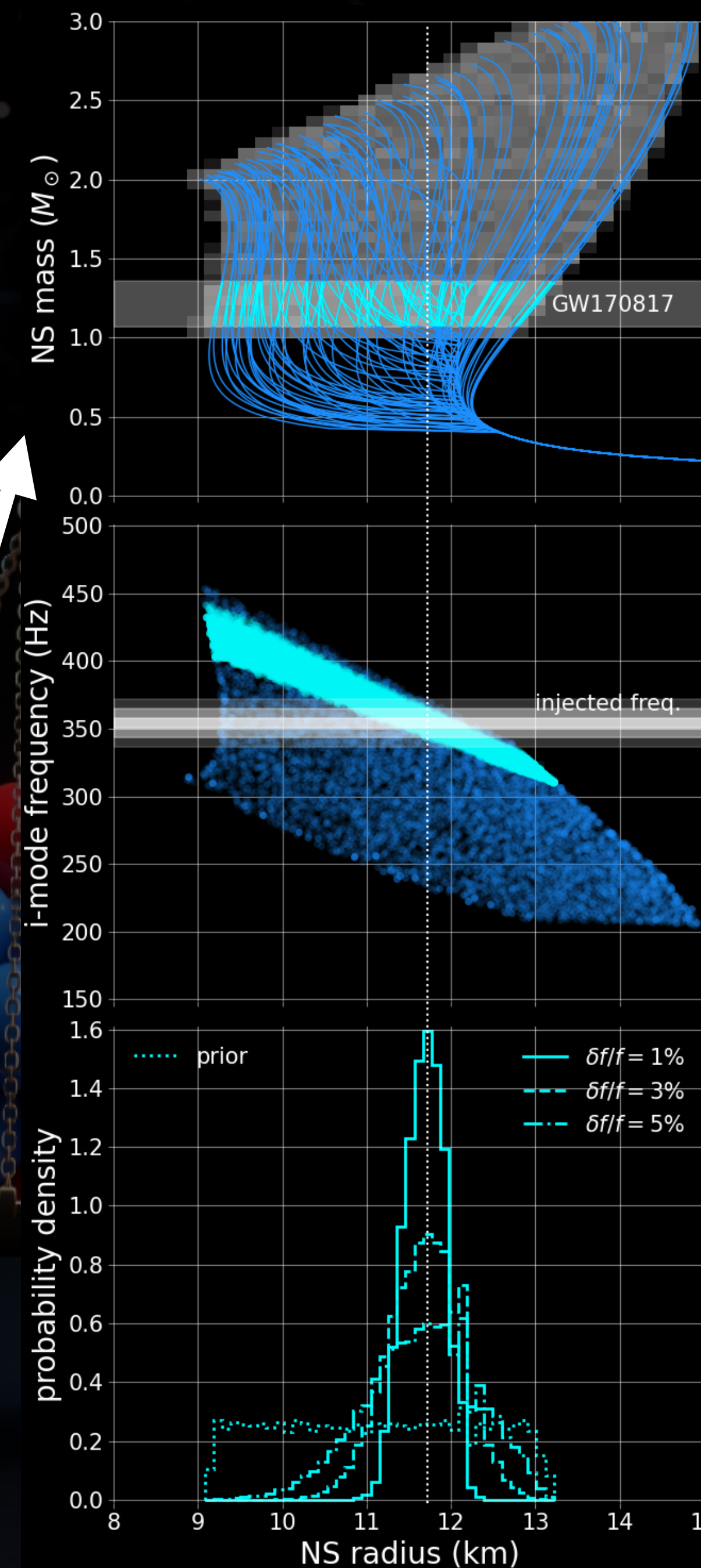


Preliminary

Fixed Nucleonic Physics



Fix a metamodel from Margueron et al (2017), add arbitrary phase transition to linear sound speed to vary the bulk core properties. Generate random samples of $(n_{\text{PT}}, \Delta n_{\text{PT}}, c_s^2, dc_s^2/dn)$ for spread in M-R plane.



Sampled with uniform prior in M-R within masses between $1-3M_{\text{sun}}$

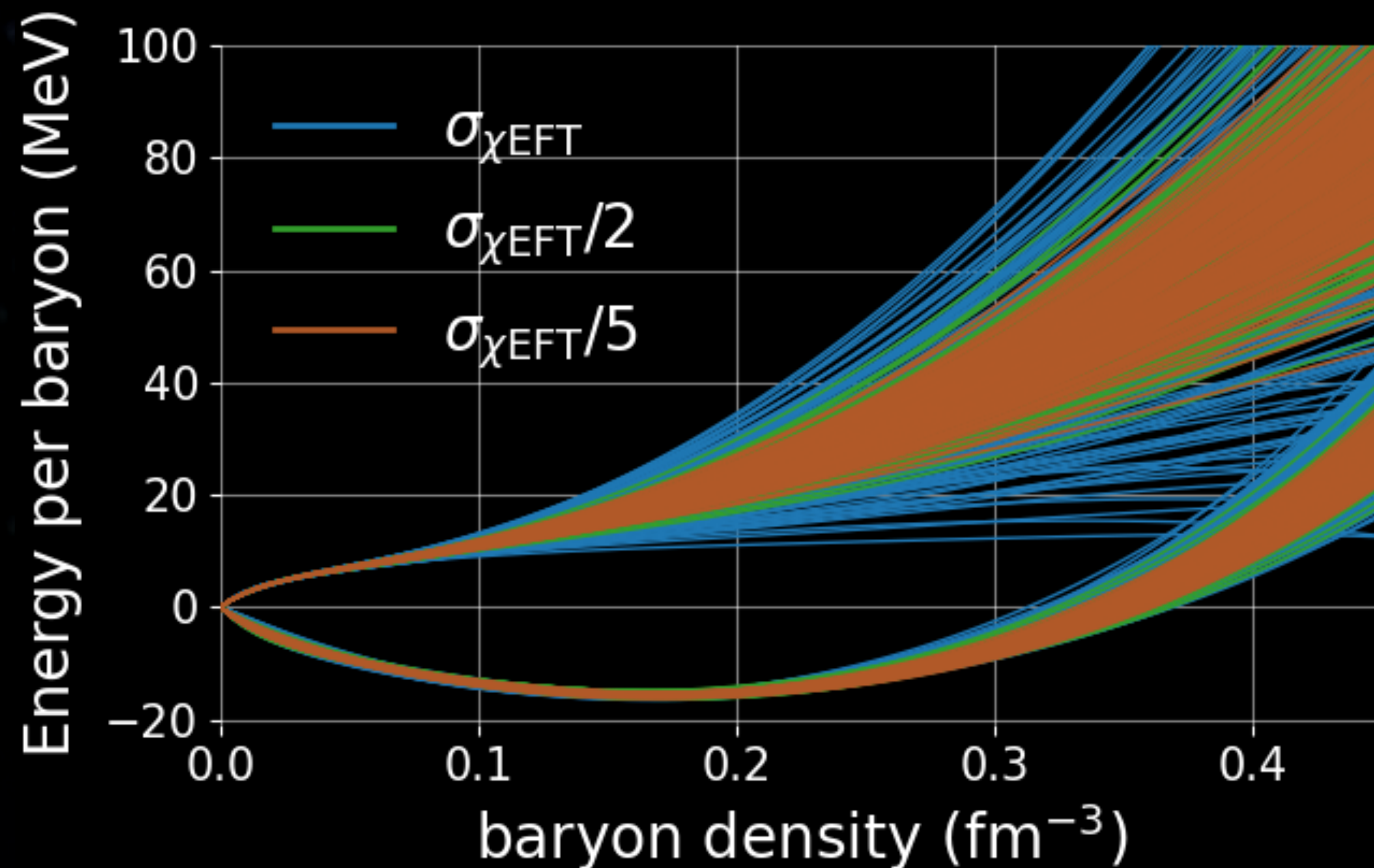
Inject mass data taken to be consistent with GW170817

Injected i-mode frequency with different uncertainties

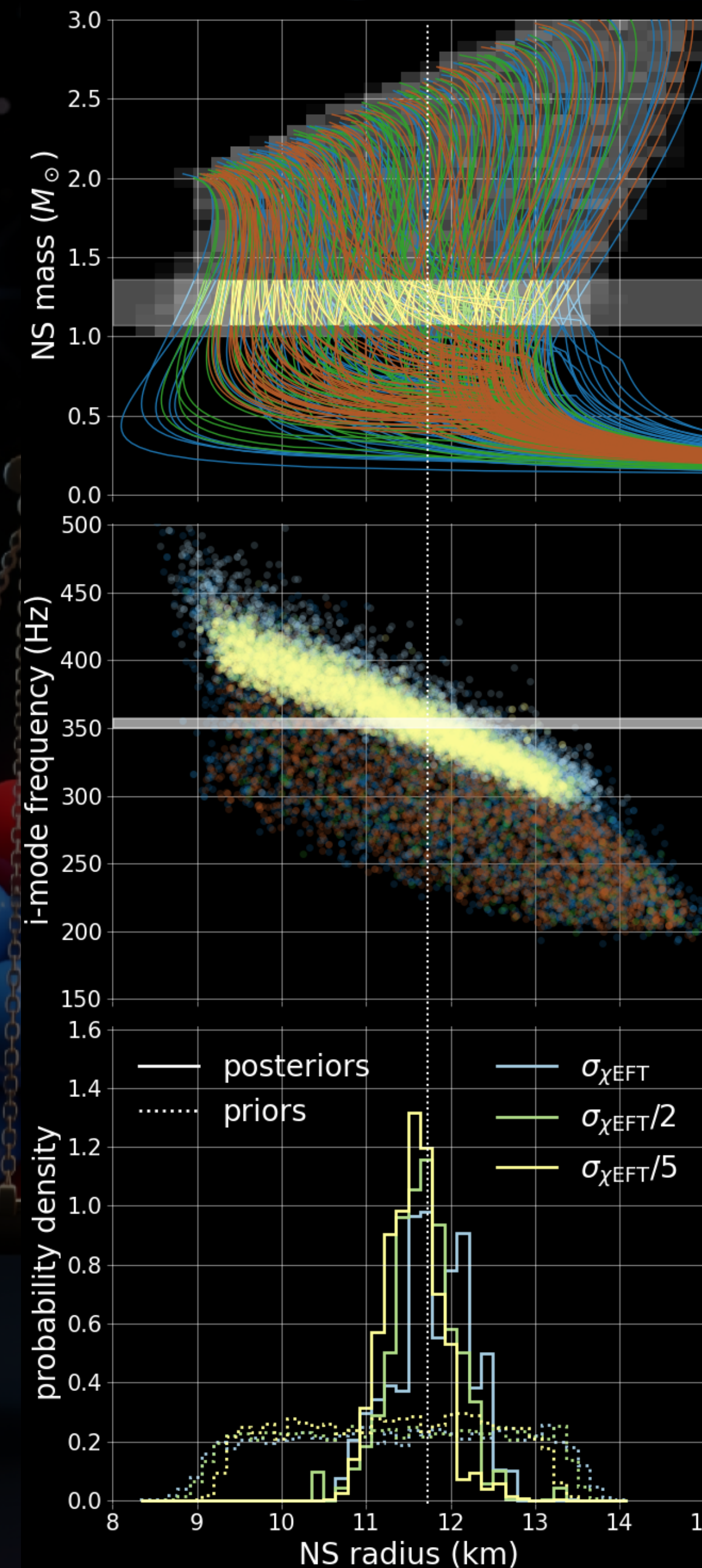
Geometric radius measurement with precision down to $\sim \pm 0.5 \text{ km}$

Preliminary

χ EFT Nucleonic Physics



Same as before, but allowing nucleonic model to vary with uncertainty range consistent with χ EFT from Lim & Holt (2018), with with covariance matrix scaled by constant factor to get estimates for “improved” constraints.



Sampled with uniform prior in M-R within masses between 1-3 M_{sun}

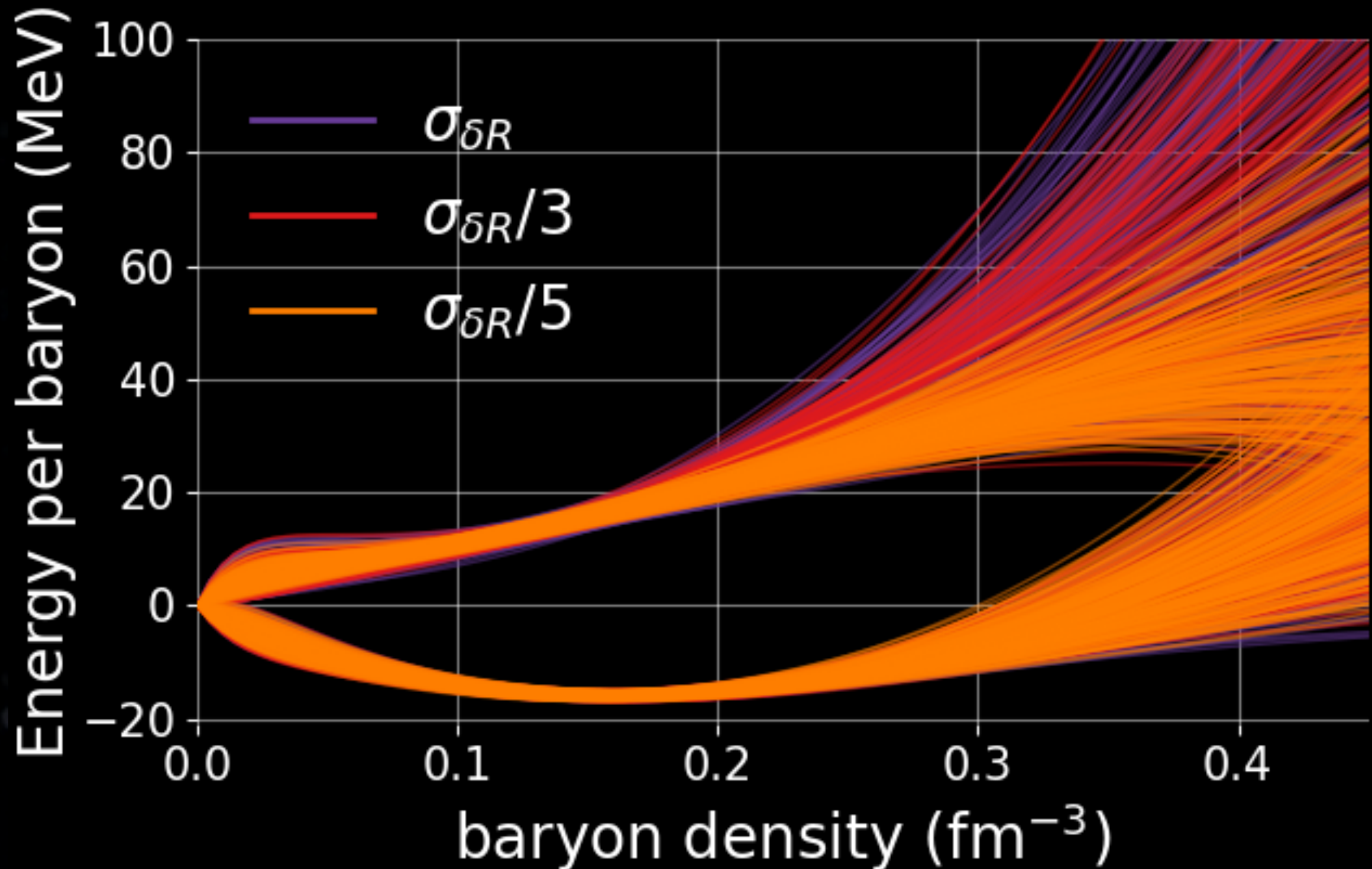
Inject mass data taken to be consistent with GW170817

Injected i-mode frequency with 1% uncertainty (mostly mass uncertainty dominated)

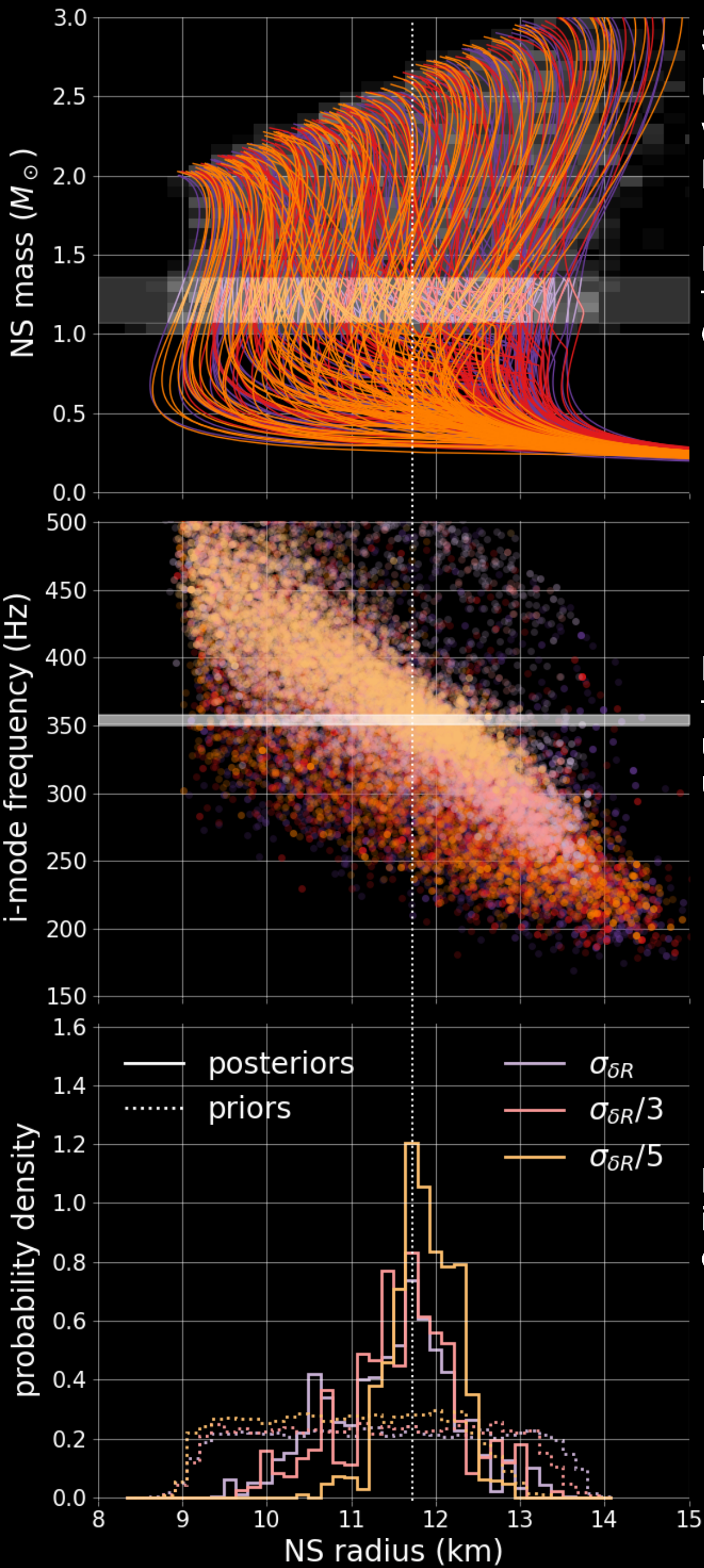
Radius precision improves with better theoretical constraints

Preliminary

Experimental Nucleonic Constraints



Using Newton & Crocombe (2021) isoscalar/isovector parameters, into meta-model. Varying only δR neutron skin depth from experimental results (effected through Skyrme EDF).



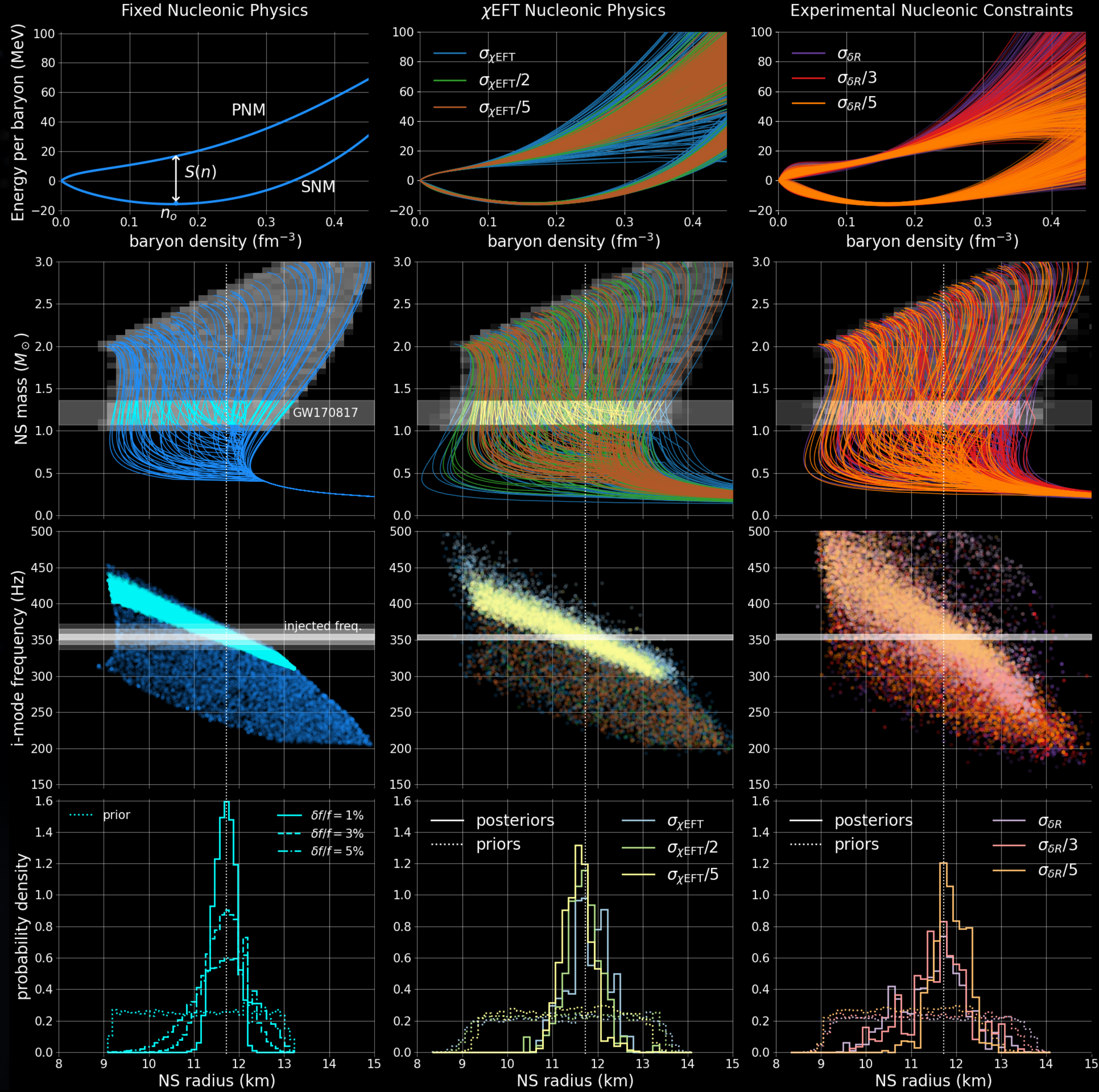
Sampled with uniform prior in M-R within masses between 1-3 M_{sun}

Inject mass data taken to be consistent with GW170817

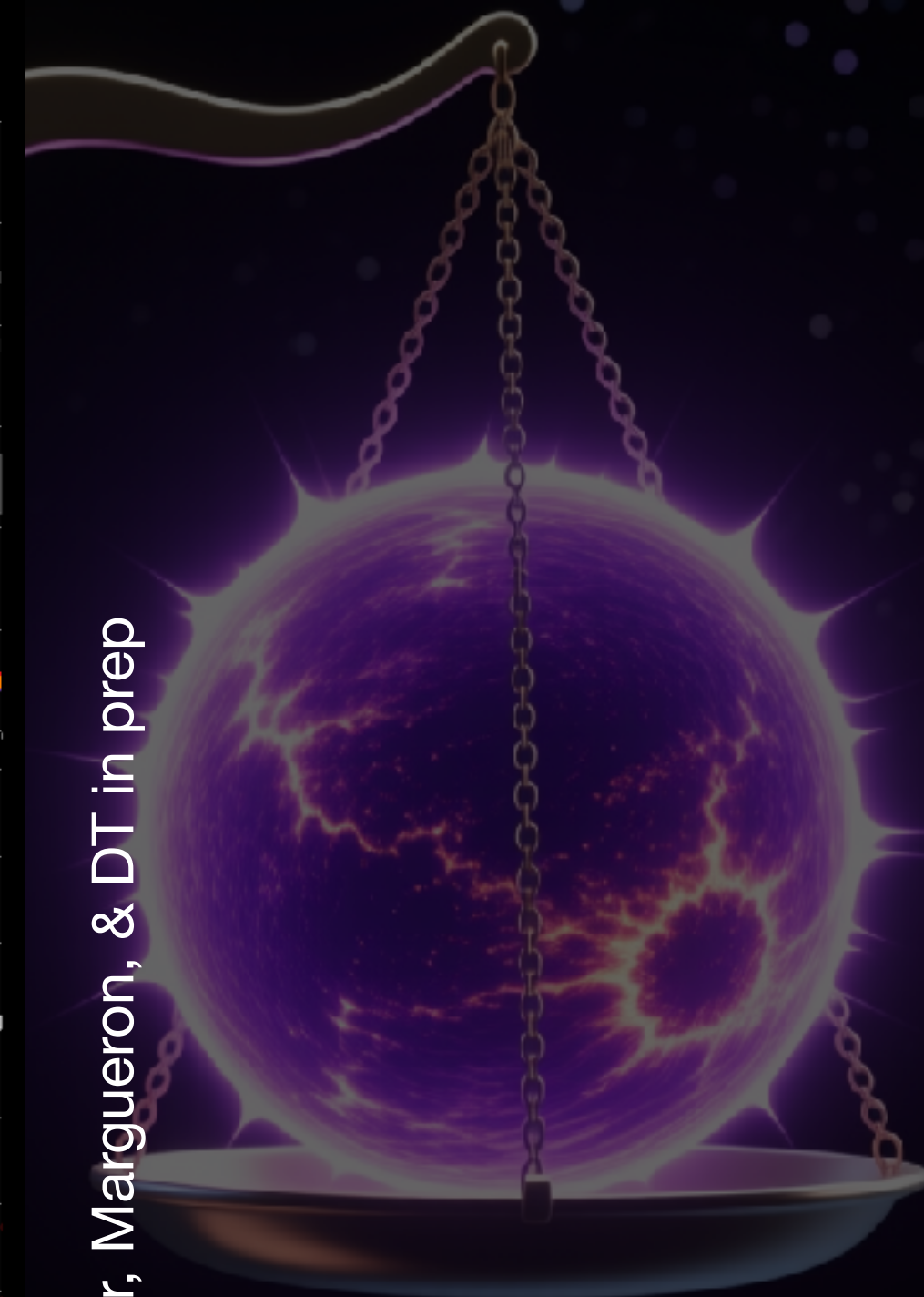
Injected i-mode frequency with 1% uncertainty (mostly mass uncertainty dominated)

Radius precision improves with better experimental constraints

Preliminary



Neill, Newton, Holt, Drischler, Margueron, & DT in prep

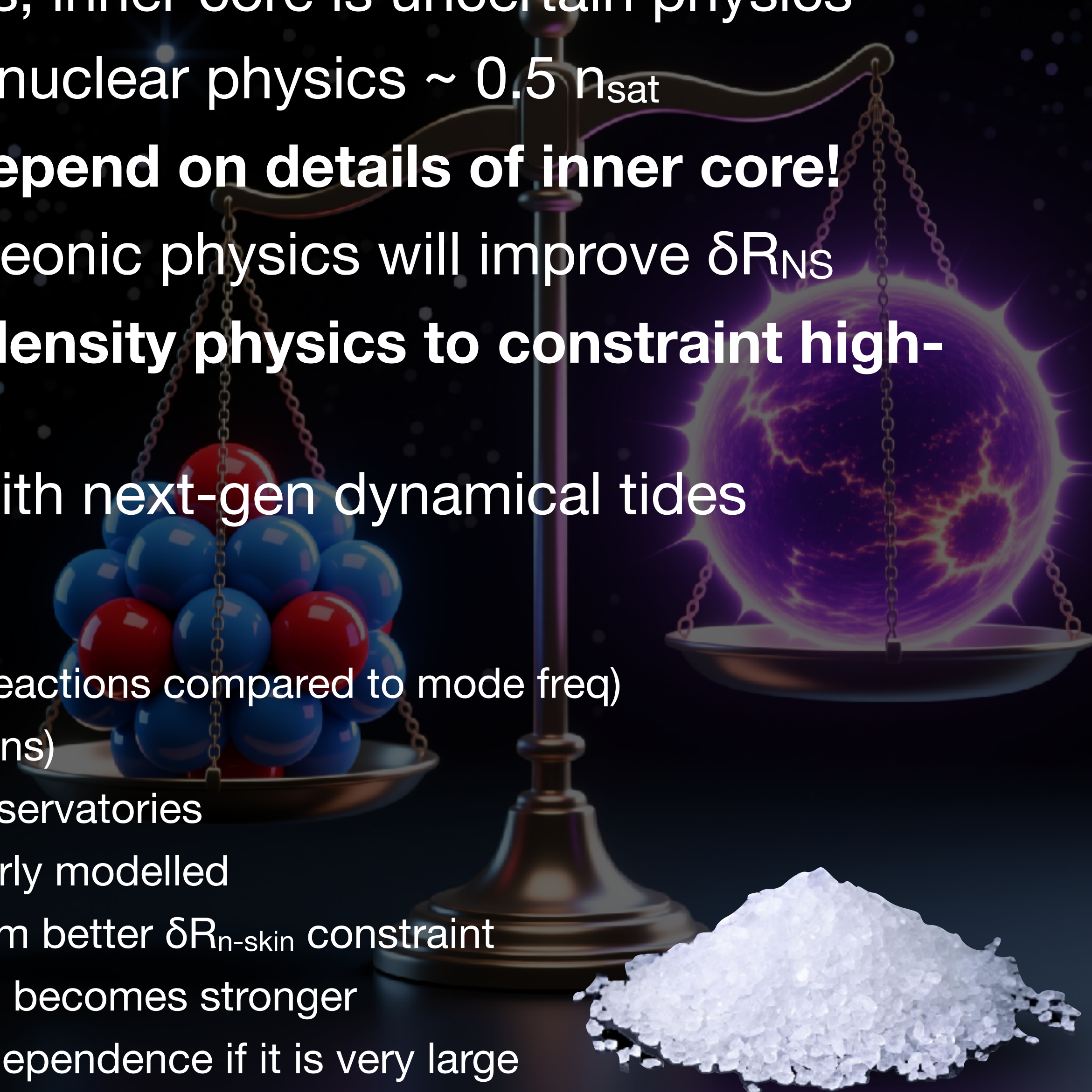


Summary:

- Different observables probe different regions, inner core is uncertain physics
- i-mode probes crust-core transition region, nuclear physics $\sim 0.5 n_{\text{sat}}$
- Geometric measure of R_{NS} **that does not depend on details of inner core!**
- Improving uncertainties for low-density nucleonic physics will improve δR_{NS}
- **Uses asteroseismology to leverage low-density physics to constraint high-density physics**
- i-mode detectable with RSFs (this gen) or with next-gen dynamical tides

Caveats:

- Post phase-transition buoyancy is assumed to be zero (fast reactions compared to mode freq)
- Pasta effects not fully included (just CLDM in these calculations)
- Mass uncertainty will definitely improve with next gen GW observatories
- Our estimate of “experimental” uncertainty is not really properly modelled
 - key take-away is to see improvement in R_{NS} constraint from better $\delta R_{\text{n-skin}}$ constraint
- Mixing of i and first g-mode when compositional stratification becomes stronger
 - Included in the calculation, but can weaken geometric R dependence if it is very large



Acknowledgements:



Duncan Neill (University of Bath)
(Currently applying for jobs/fellowships)



Will Newton (East Texas A&M)



Jeremy Holt (Texas A&M)



Christian Drischler (Ohio University/FRIB)



Jérôme Margueron (CNRS/MSU)

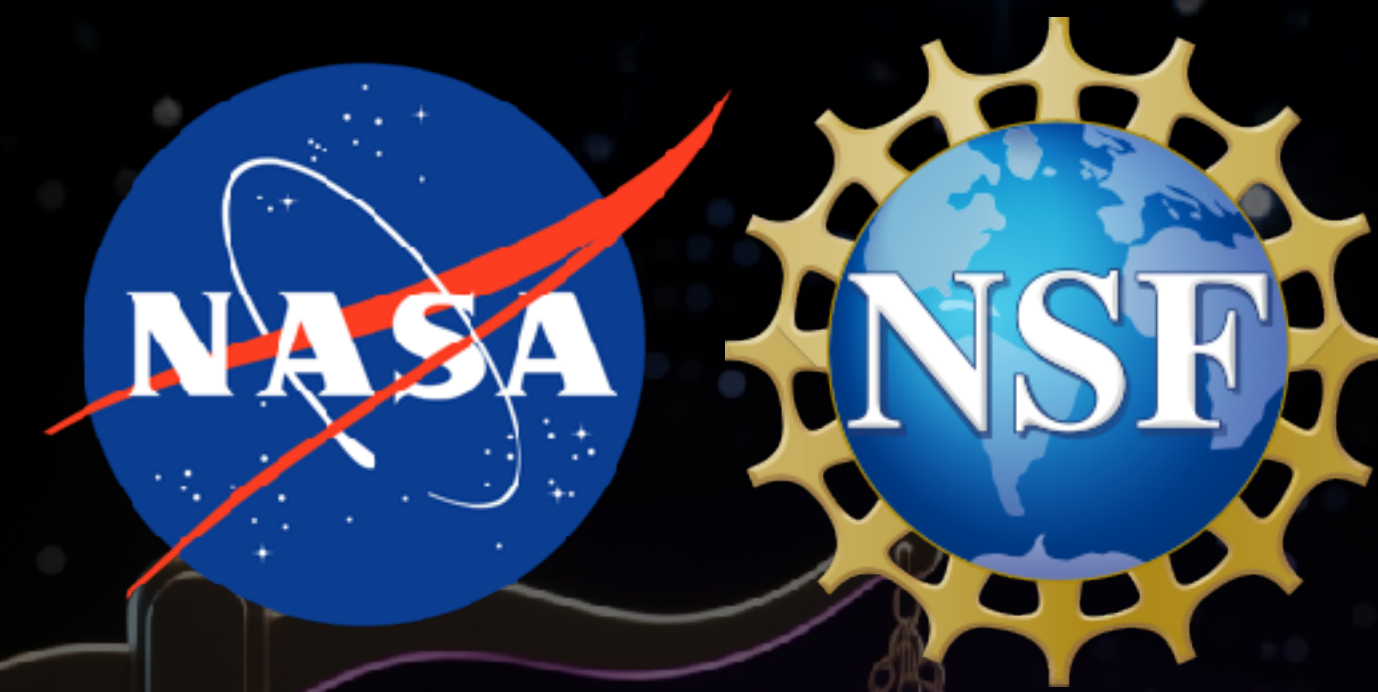
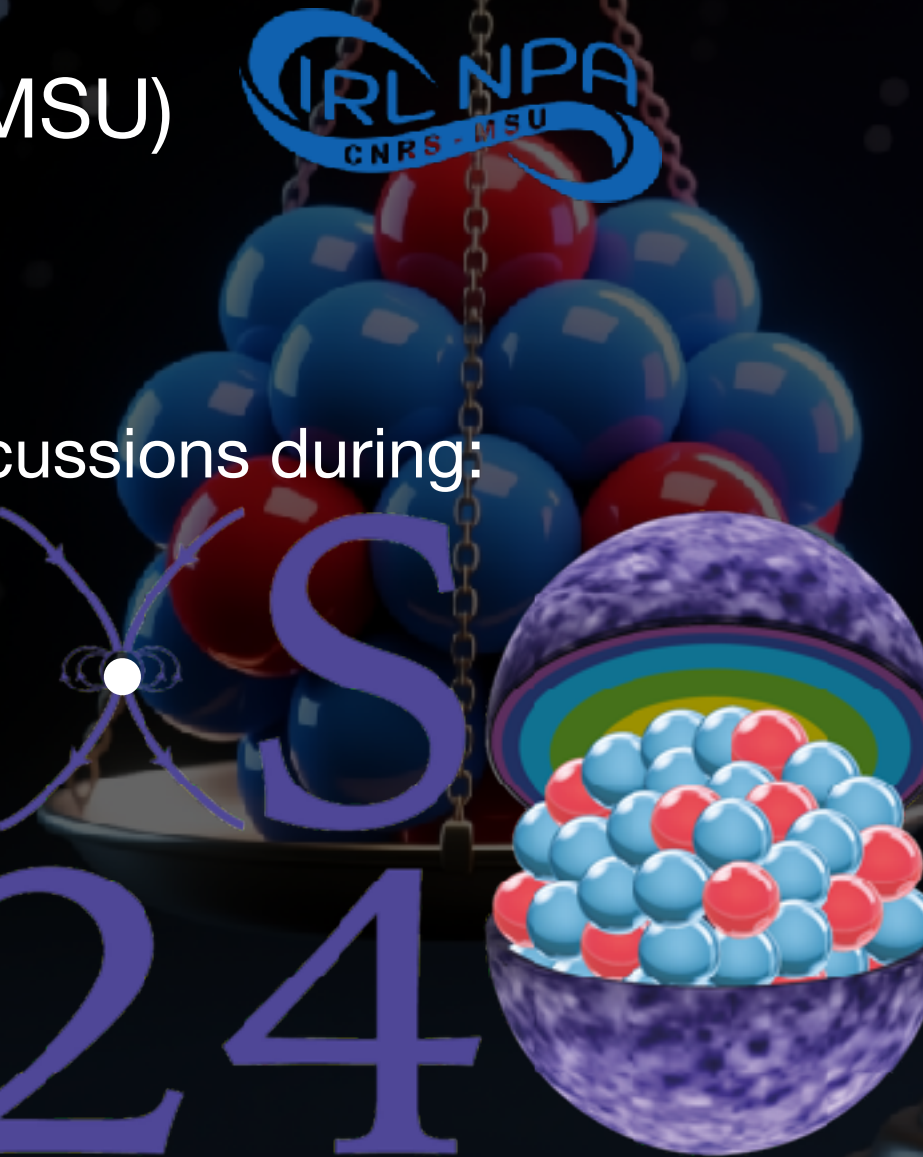


UNIVERSITY OF
BATH

Generated from discussions during:

XMAS
2024

eXtreme Matter in eXtreme Stars
Lorentz Center, Netherlands
Sept 23-27, 2024



Science and
Technology
Facilities Council