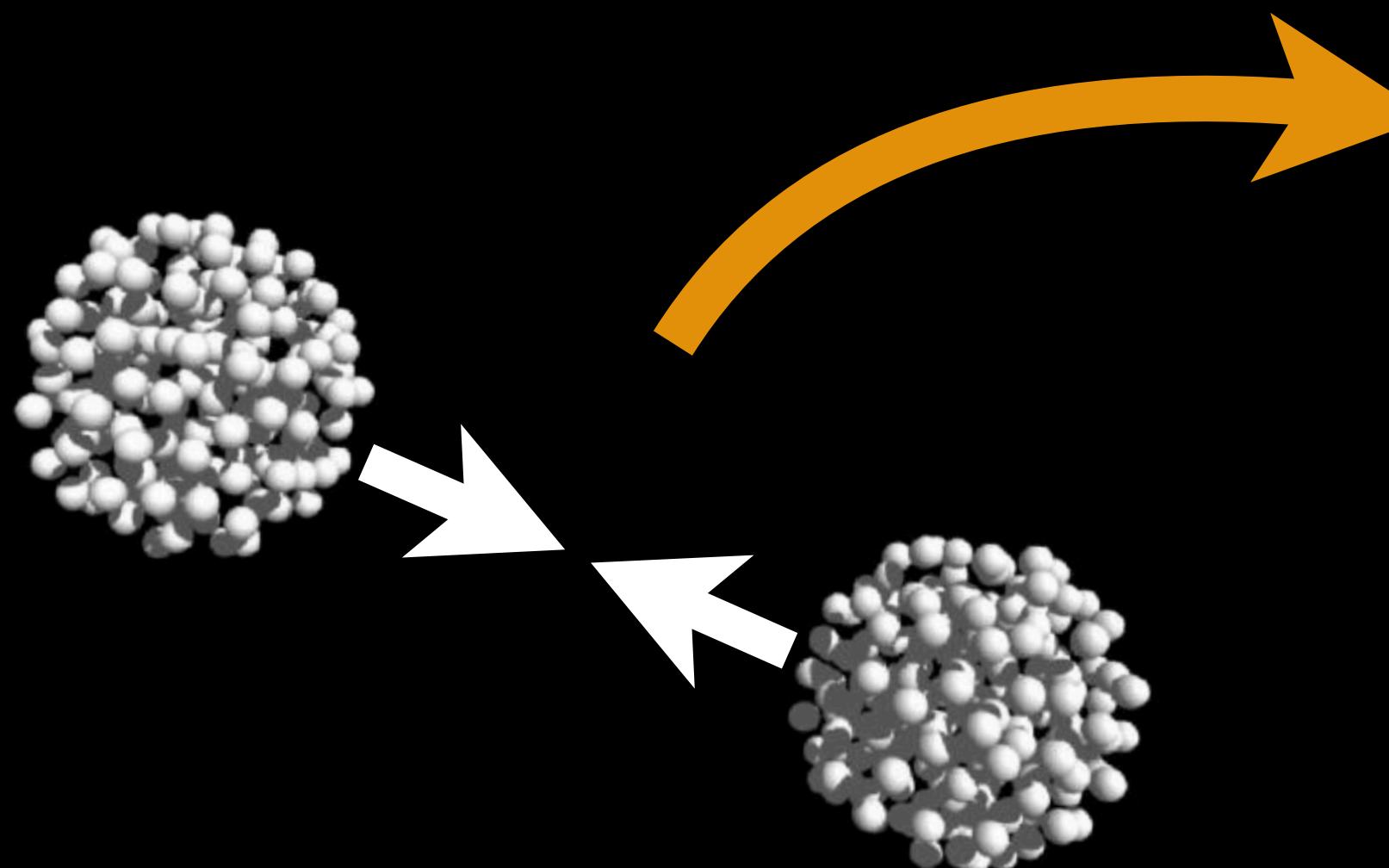


Transport simulations for extracting the properties of dense nuclear matter

Agnieszka Sorensen

Institute for Nuclear Theory, University of Washington



July 30, 2024

INT PROGRAM INT-24-2B

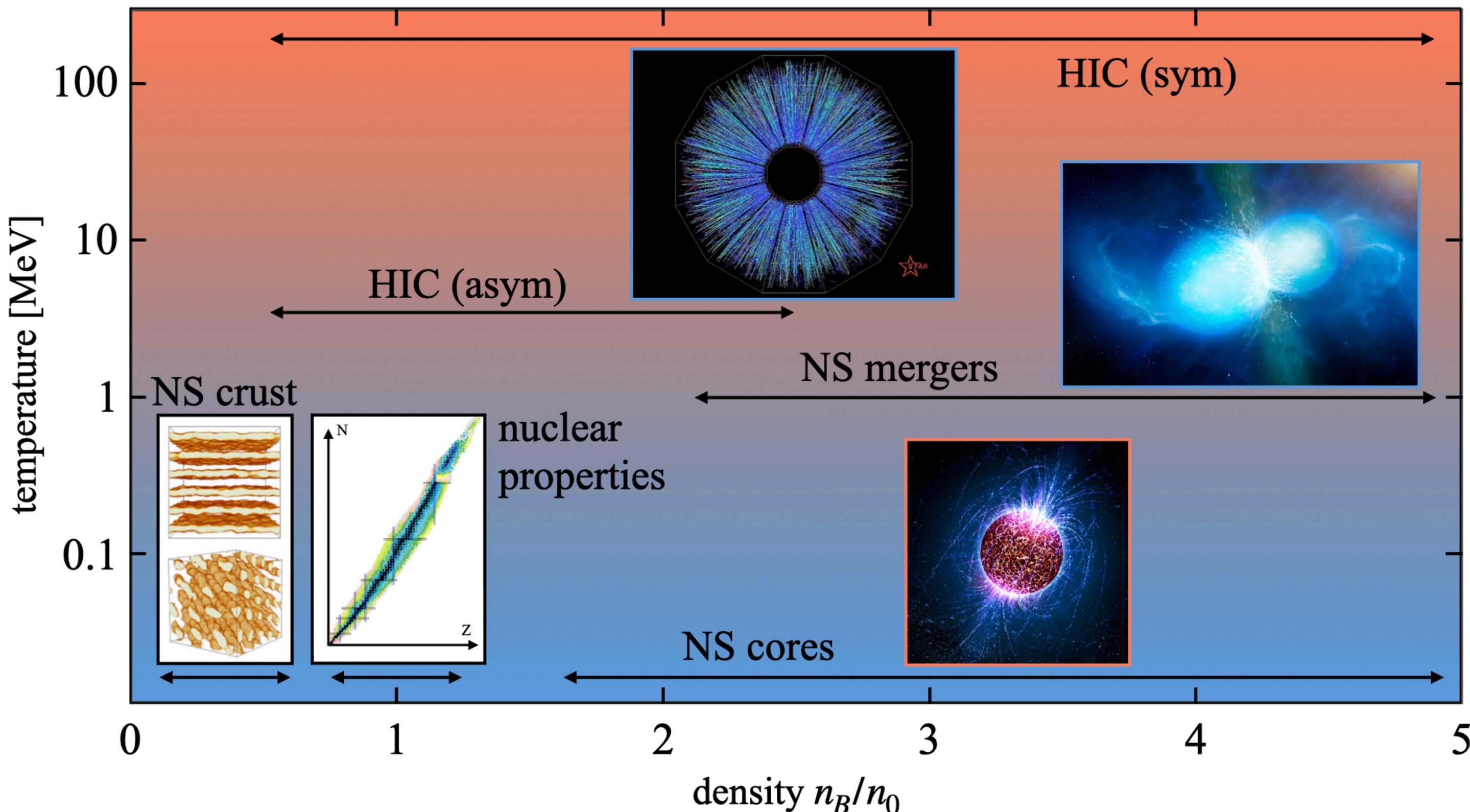
“Heavy Ion Physics in the EIC Era”

Transport simulations for extracting the properties of dense nuclear matter

Outline:

1. Introduction
2. Results: historic & recent
3. Future opportunities

Dense nuclear matter properties = common interest in nuclear physics

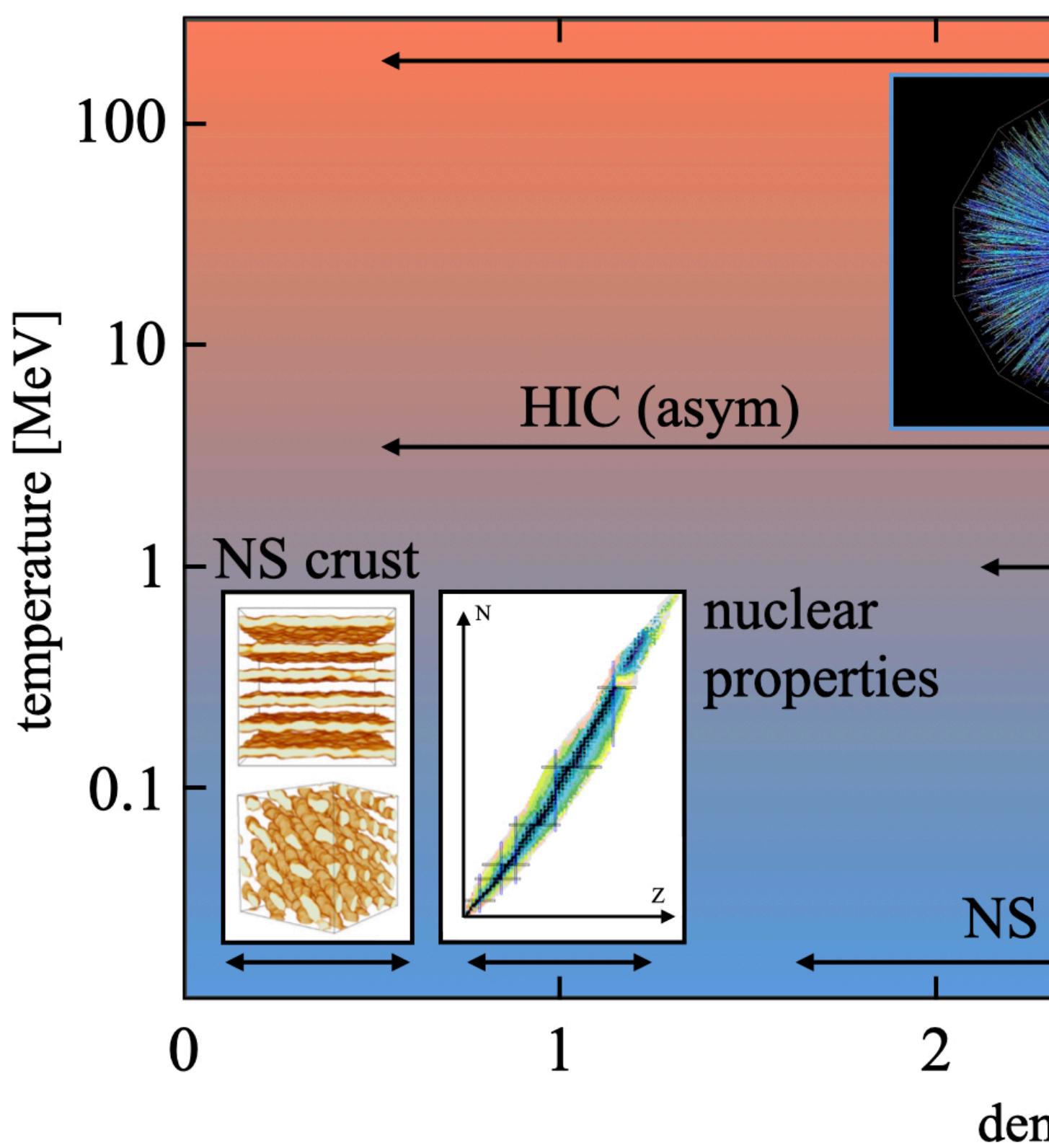


Properties of dense nuclear matter:

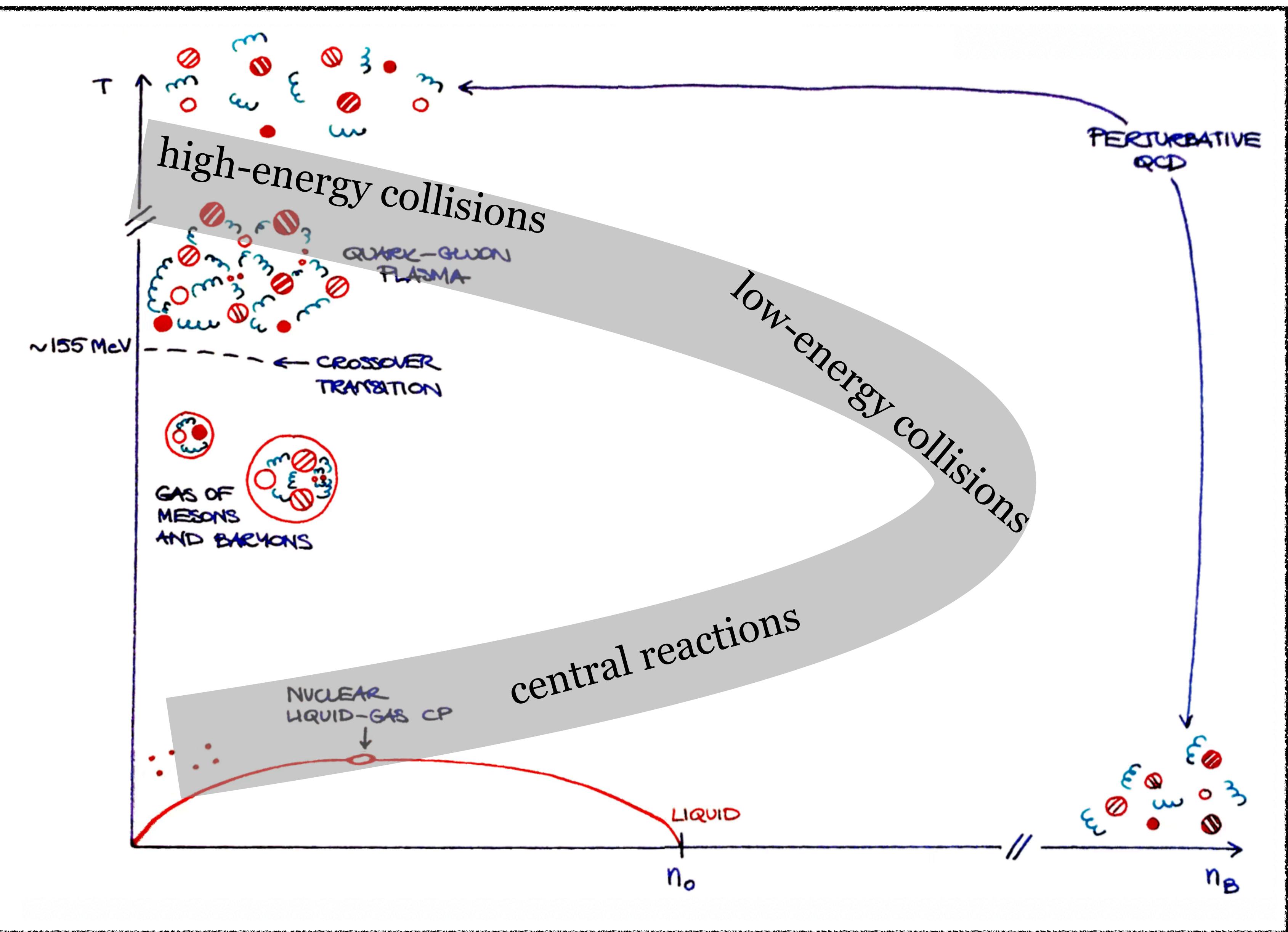
- necessary input to studies of neutron stars & their mergers, supernovae
- reflected in the structure of heavy nuclei
- necessary input to simulations of heavy-ion collisions
- test beds for theories & models
- conveniently “summarized” in the equation of state (EOS)

A. Sorensen et al., Prog. Part. Nucl. Phys. **134**, 104080 (2024)
arXiv:2301.13253

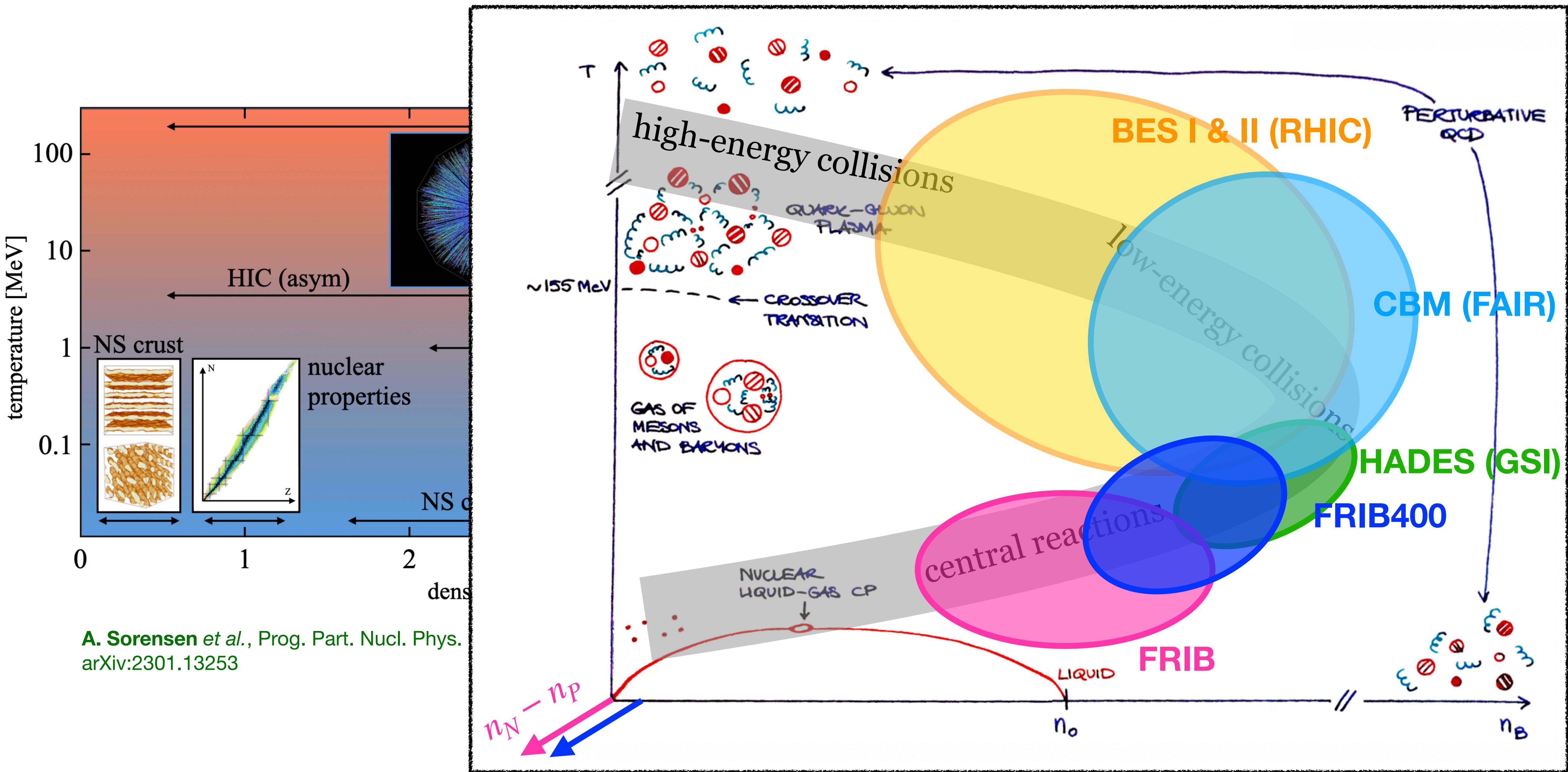
Dense nuclear matter properties = common interest in nuclear physics



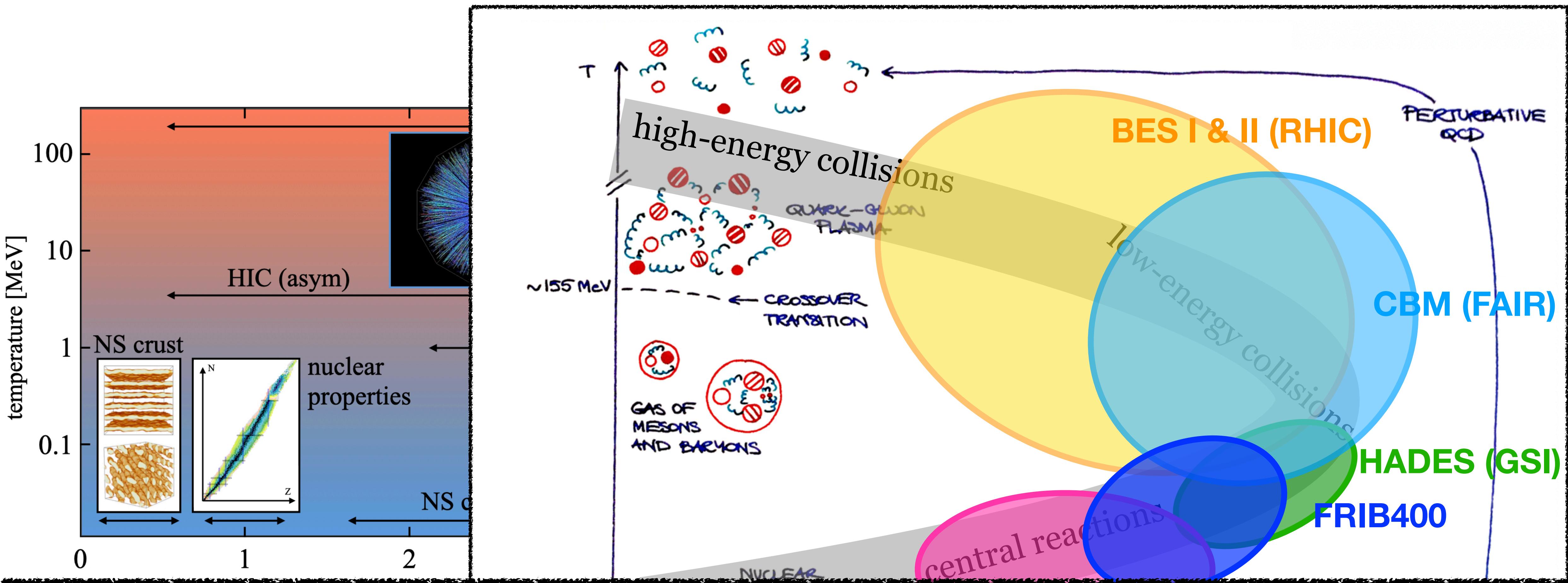
A. Sorensen et al., Prog. Part. Nucl. Phys.
arXiv:2301.13253



Dense nuclear matter properties = common interest in nuclear physics



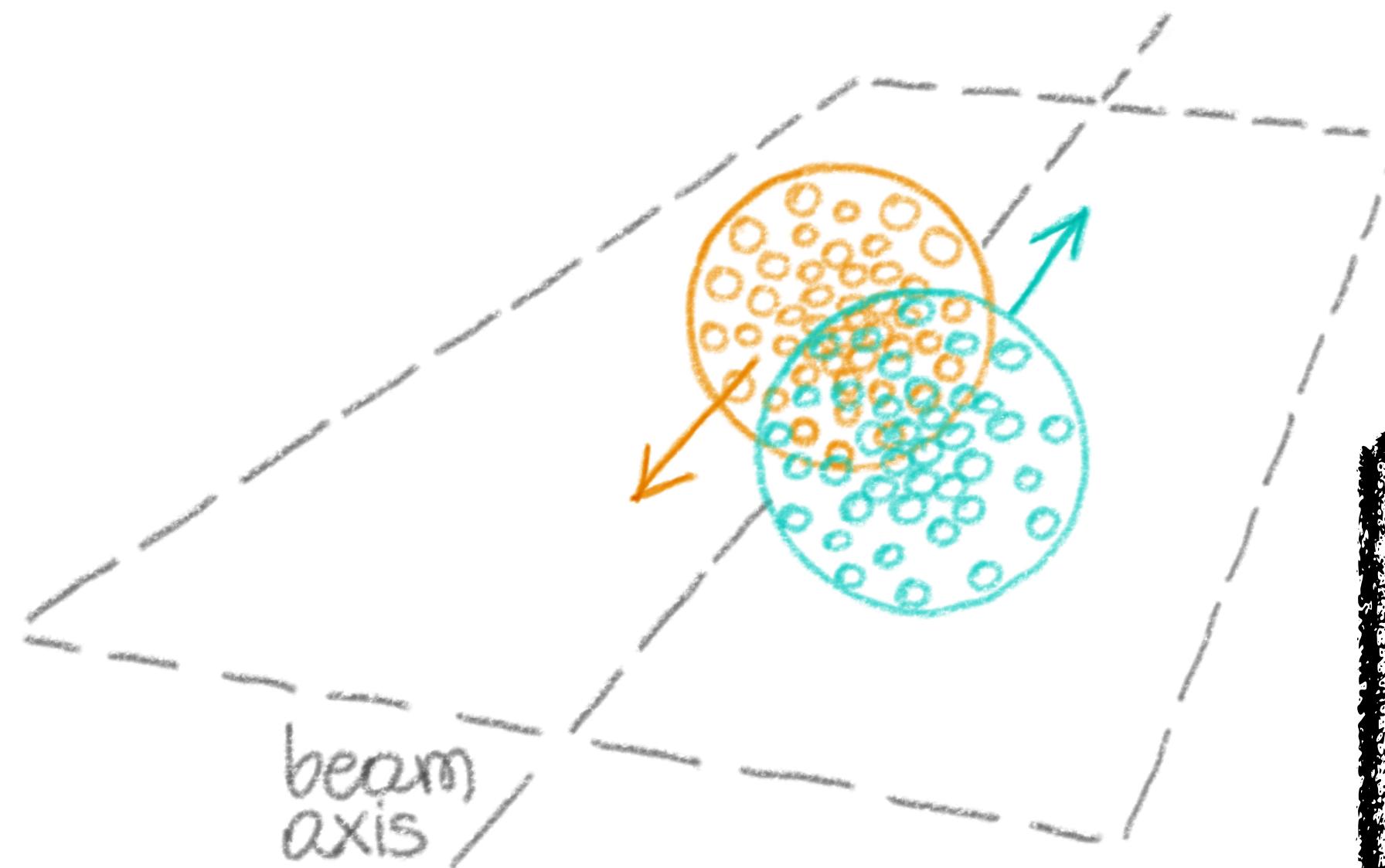
Dense nuclear matter properties = common interest in nuclear physics



- HICs = the **only** means to probe densities above n_0 in controlled terrestrial experiments
- EOS extracted from comparison to dynamical simulations
- At low energies, prolonged initial state and out-of-equilibrium evolution: **microscopic transport**

Microscopic transport model simulations of heavy-ion collisions

- 2 types of models:
 - Boltzmann-Uehling-Uhlenbeck (BUU): evolve the distribution function of the system
 - Quantum Molecular Dynamics (QMD): evolve wave packets associated with particles
 - forces:
 - 2-body interactions (“pure” QMD)
 - gradients of single-particle energies = mean-field (BUU, QMD)
 - collisions:
 - based on measured cross sections for scatterings and decays
 - cross sections may be modified in the medium

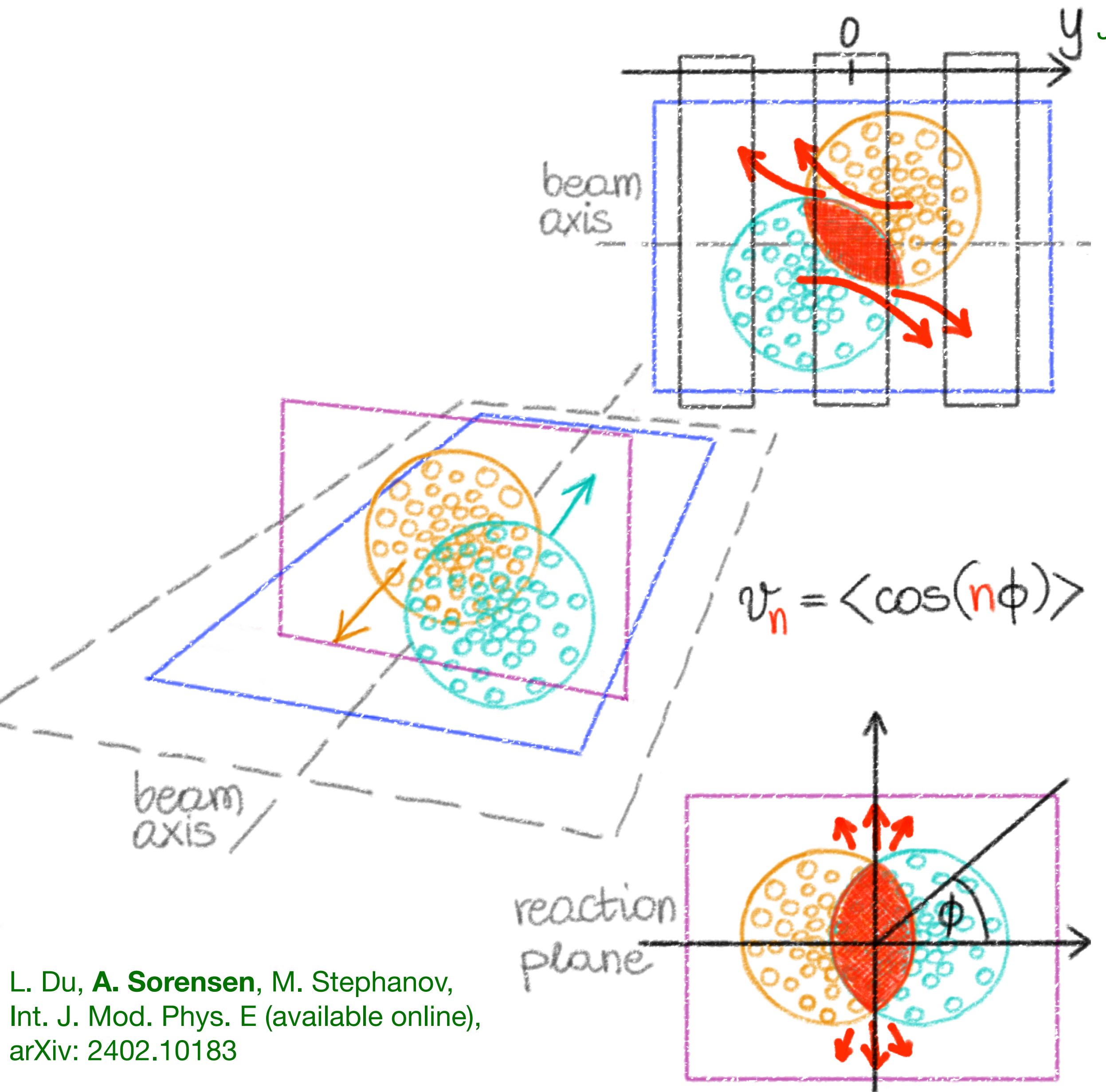


General idea:

- take nucleons from the initial state (nuclei about to collide)
- evolve them in time
- compute observables and compare with experiment

Chapter on “Microscopic transport description of dense nuclear matter dynamics” in a recent review:
L. Du, **A. Sorensen**, M. Stephanov, “The QCD phase diagram and Beam Energy Scan physics: a theory overview”,
Quark-Gluon Plasma 6, Int. J. Mod. Phys. E (available online), arXiv: 2402.10183

Sketch of a heavy-ion collision evolution and development of flow

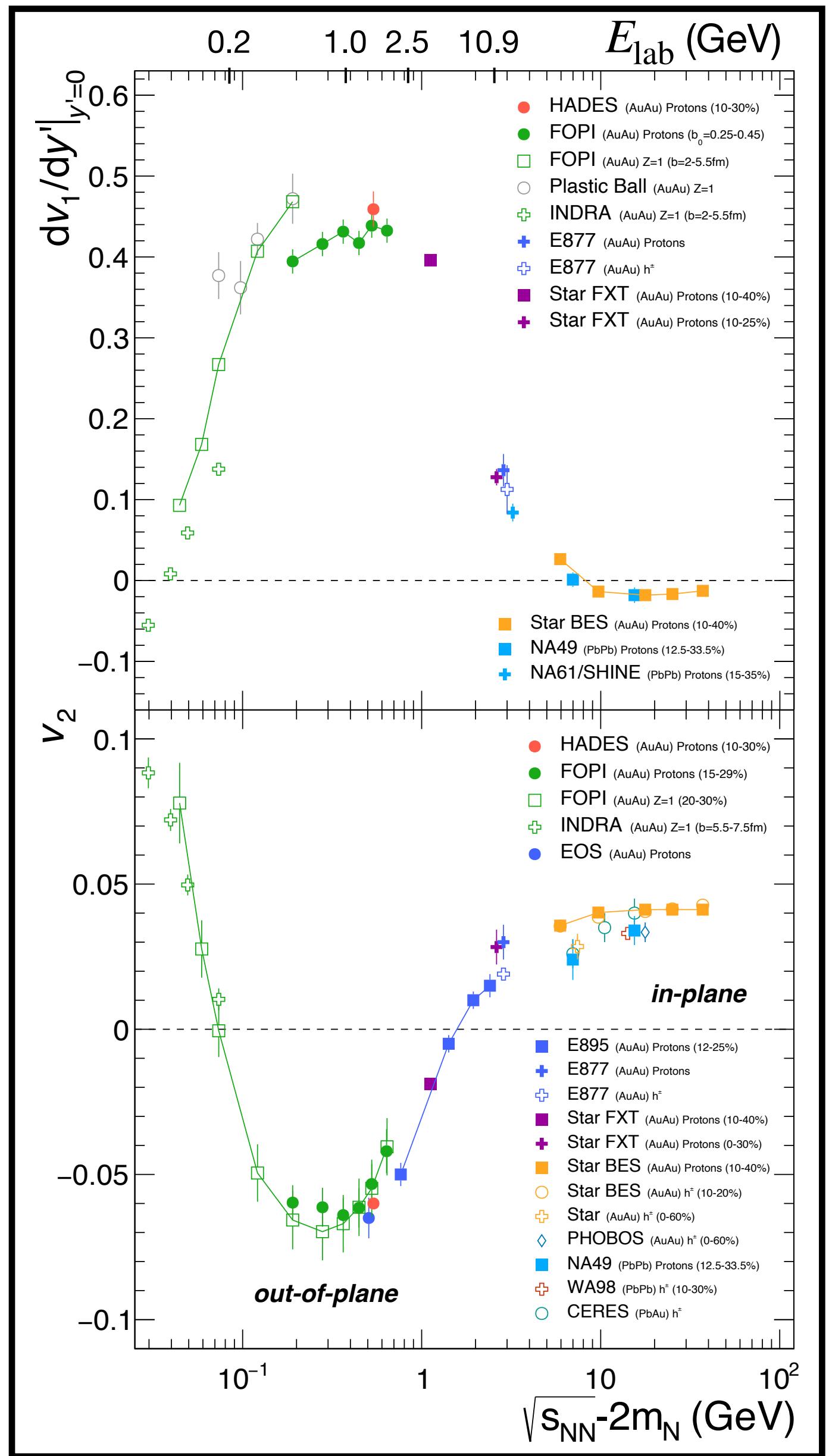


J. Adamczewski-Musch *et al.* (HADES),
Eur.Phys.J.A 59 (2023) 4, 80,
arXiv:2208.02740

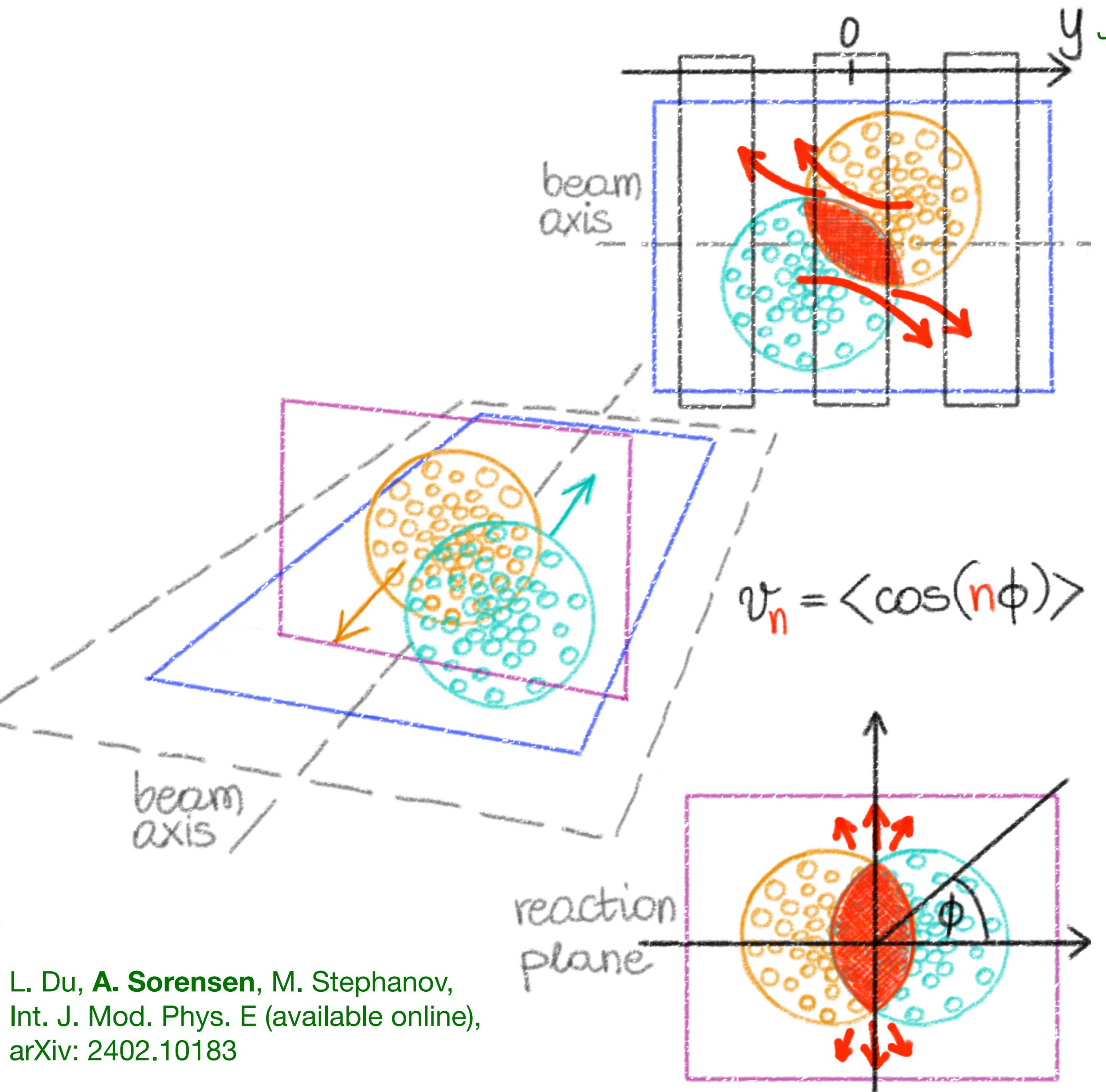
v_1 = directed flow

stiffer EOS
=
more pushing

v_2 = elliptic flow



Sketch of a heavy-ion collision evolution and development of flow

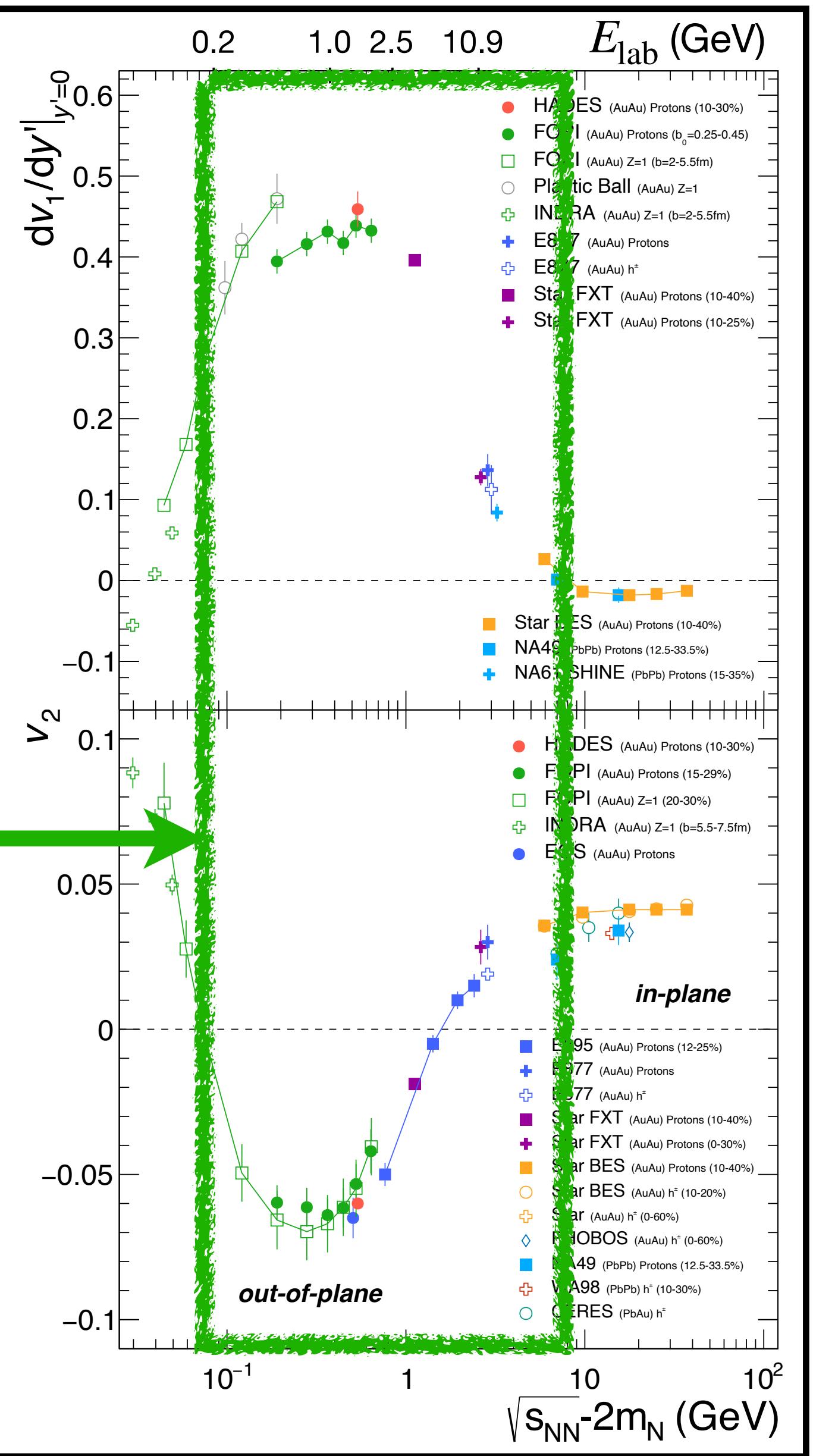


J. Adamczewski-Musch *et al.* (HADES),
Eur.Phys.J.A 59 (2023) 4, 80,
arXiv:2208.02740

v_1 = directed flow

Experiments:
FRIB & FRIB400,
BES FXT,
HADES, CBM, ...

v_2 = elliptic flow



Transport simulations for extracting the properties of dense nuclear matter

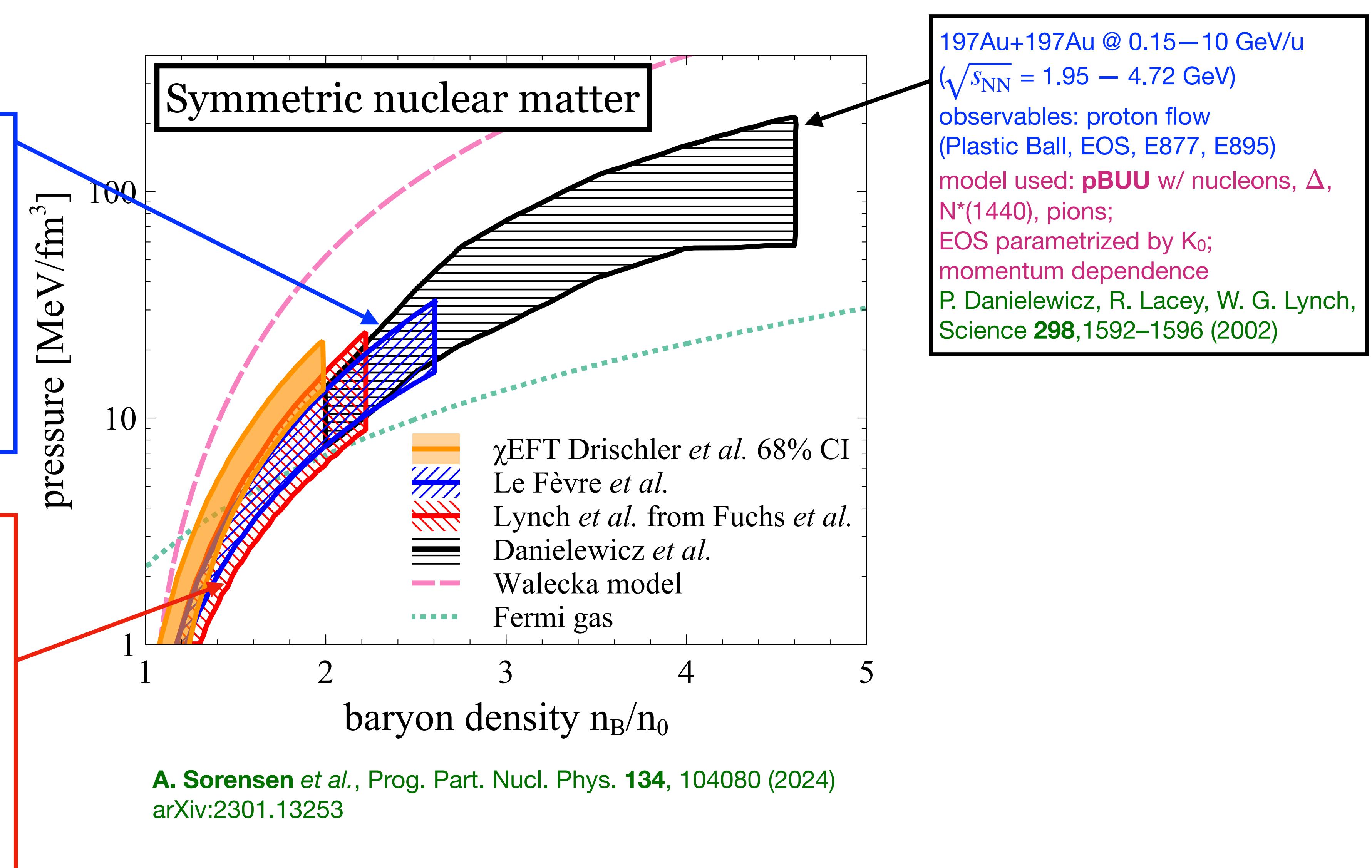
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Constraints on the EOS come from comparisons to transport models

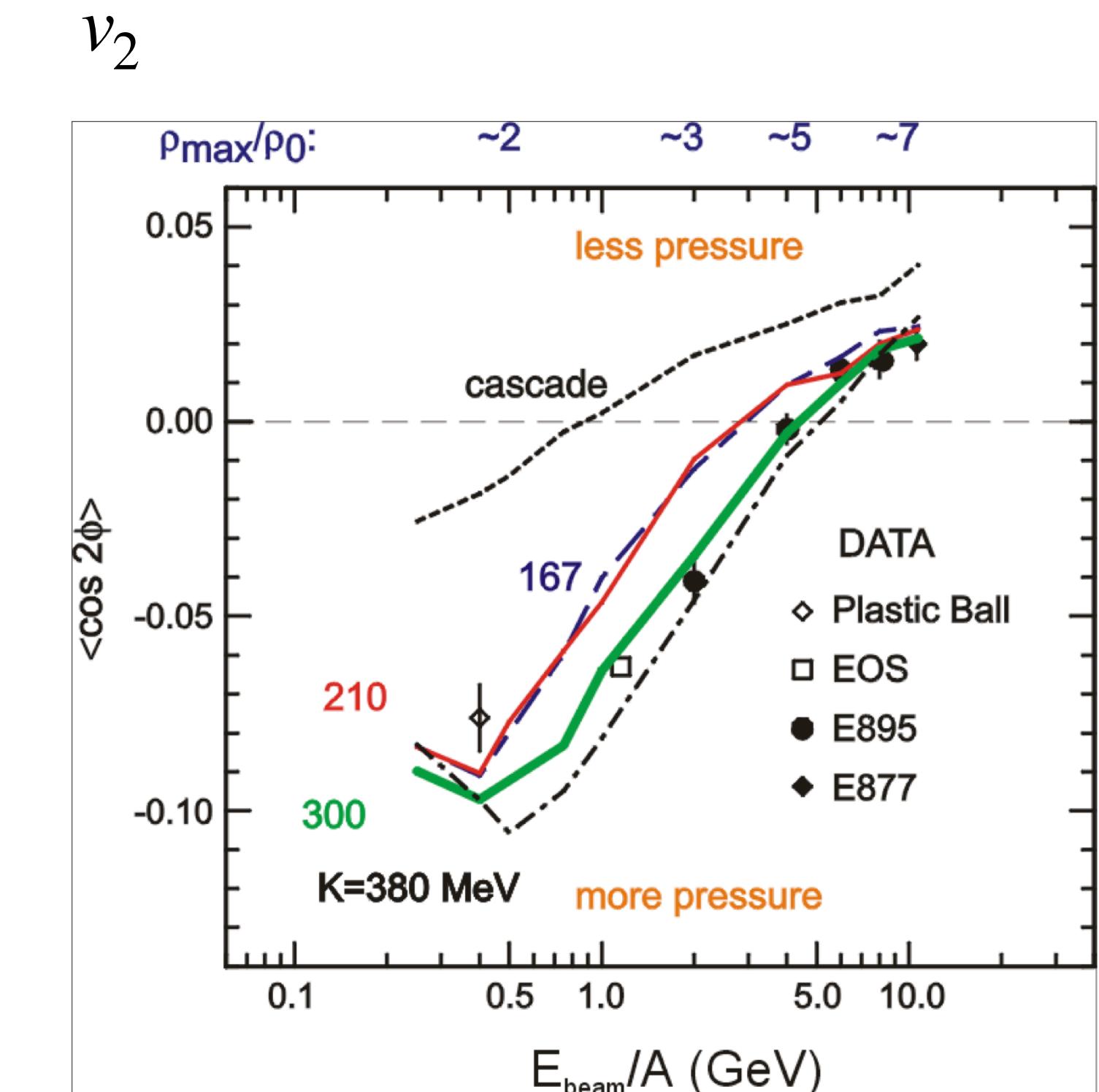
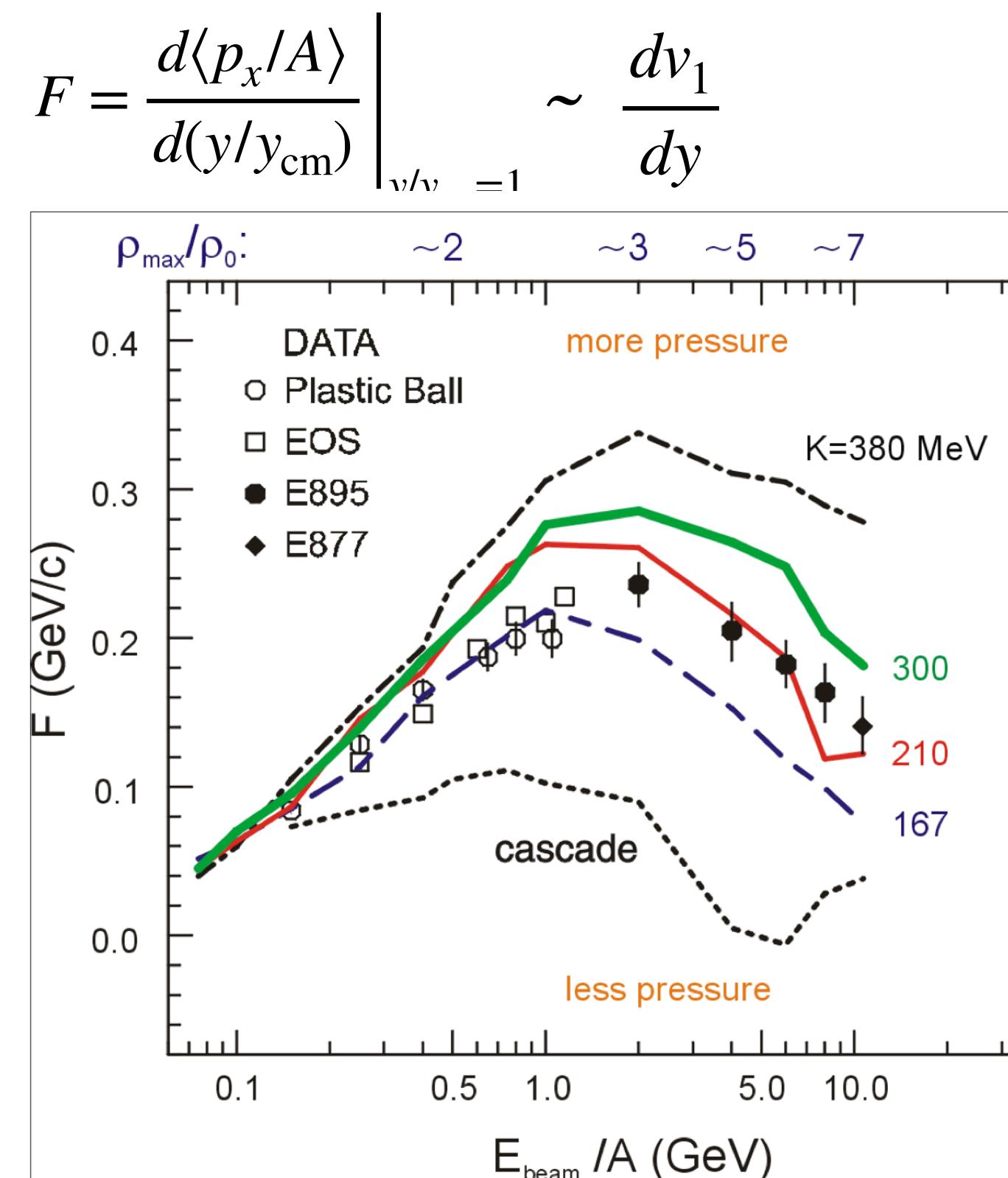
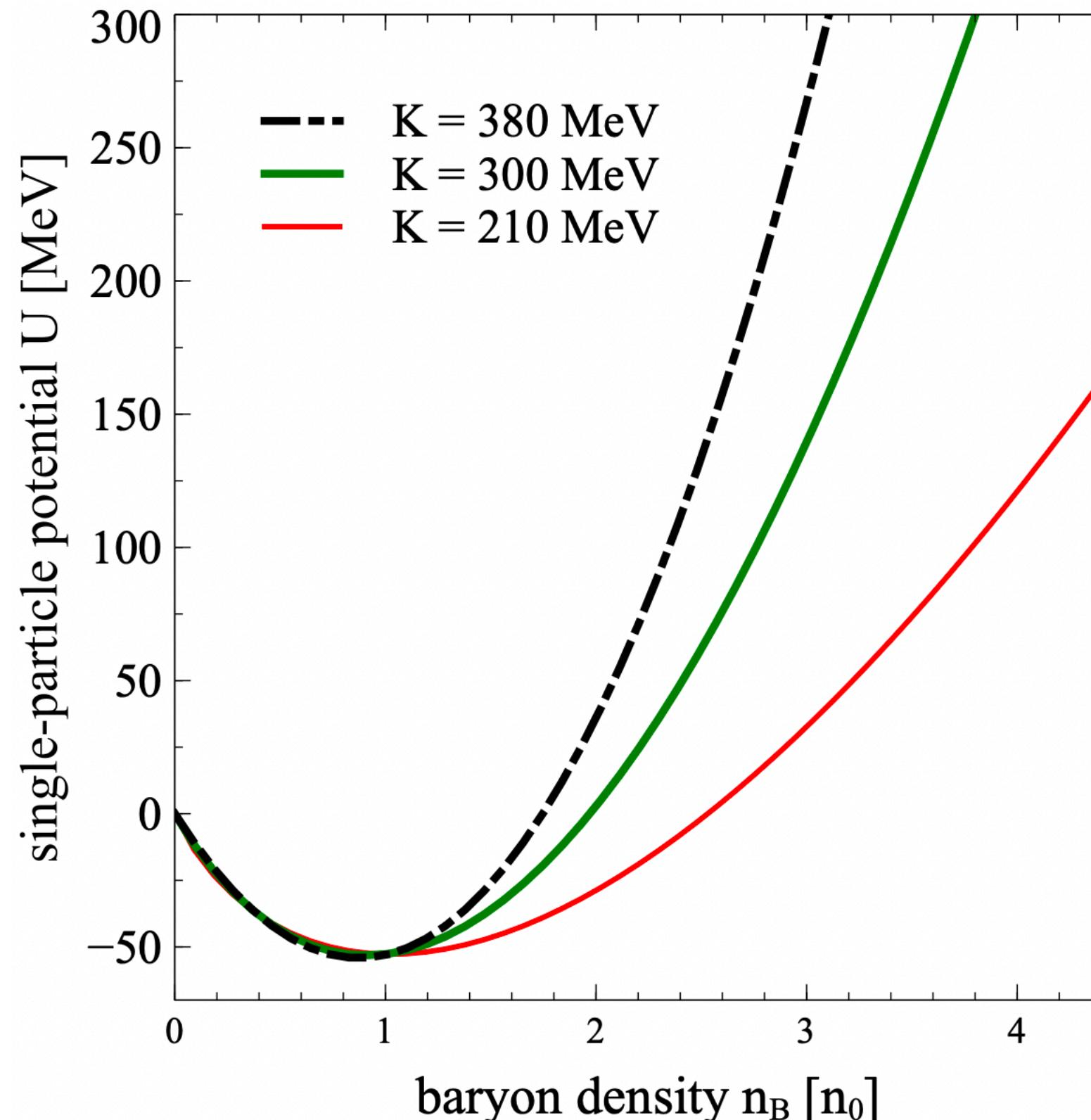
197Au+197Au @ 0.4–1.5 GeV/u
($\sqrt{s_{NN}} = 2.07 - 2.52$ GeV)
observables: proton flow (FOPI)
model used: **isospin QMD (IQMD)** w/
nucleons, Δ , $N^*(1440)$, deuterons, tritons;
EOS parametrized by K_0 ;
momentum dependence
A. Le Fèvre, Y. Leifels, W. Reisdorf, J.
Aichelin, C. Hartnack, Nucl. Phys. A 945,
112 (2016), arXiv:1501.05246

197Au+197Au & 12C+12C @ < 1.5 GeV/u
($\sqrt{s_{NN}} < 2.5$ GeV)
observables: subthreshold kaon production
(KaoS)
model used: **QMD** w/ nucleons, Δ ,
 $N^*(1440)$, pions, kaons;
EOS parametrized by K_0 ;
kaon potentials, momentum dependence
C. Fuchs *et al.*, Prog. Part. Nucl. Phys. **53**,
113–124 (2004) arXiv:nucl-th/0312052



Standard way of modeling the EOS: Skyrme potential

The most common form of the EOS is the “Skyrme potential”: $U(n_B) = A\left(\frac{n_B}{n_0}\right) + B\left(\frac{n_B}{n_0}\right)^{\tau}$

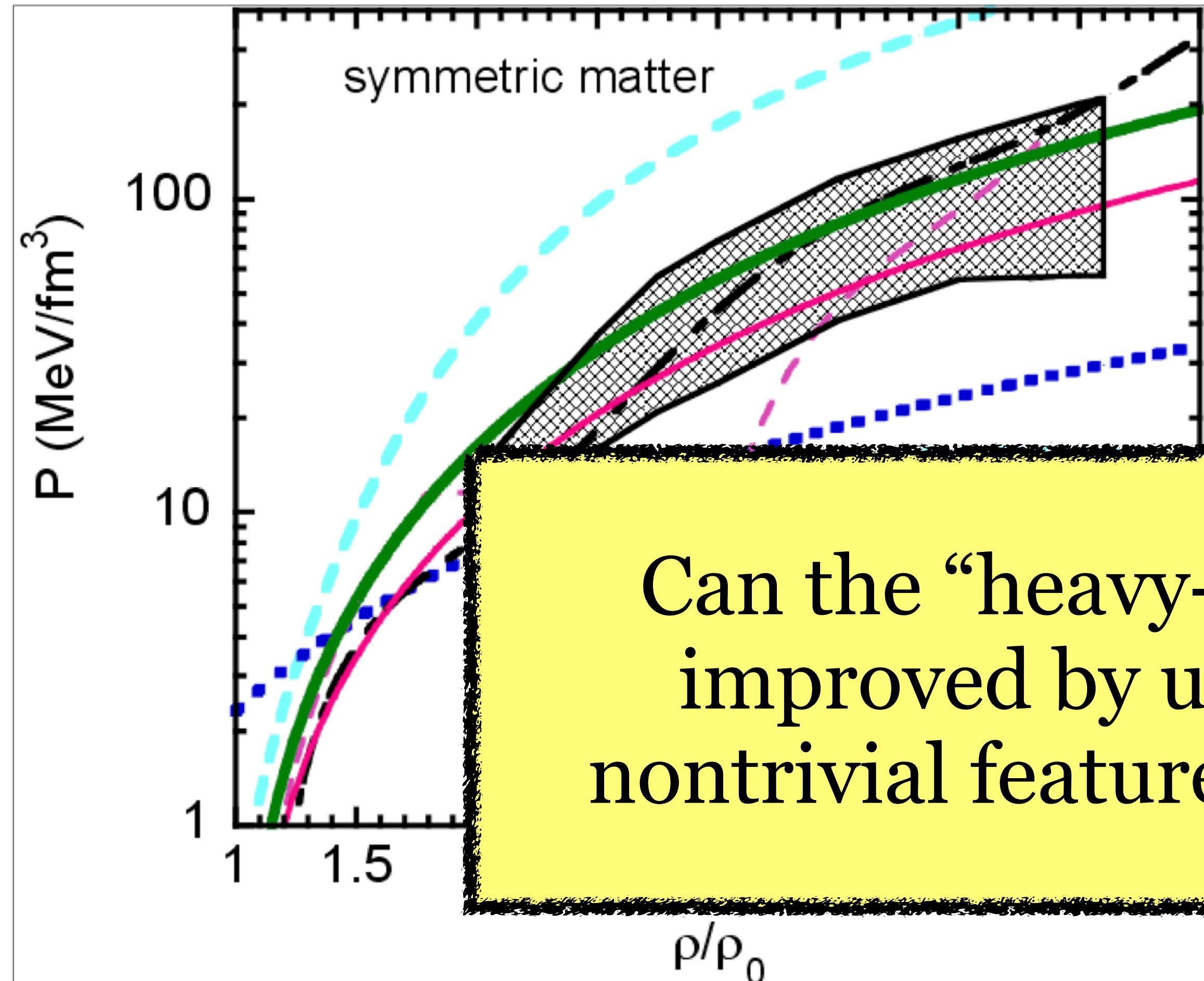


P. Danielewicz, R. Lacey, W. G. Lynch,
Science **298**, 1592–1596 (2002), arXiv:nucl-th/0208016

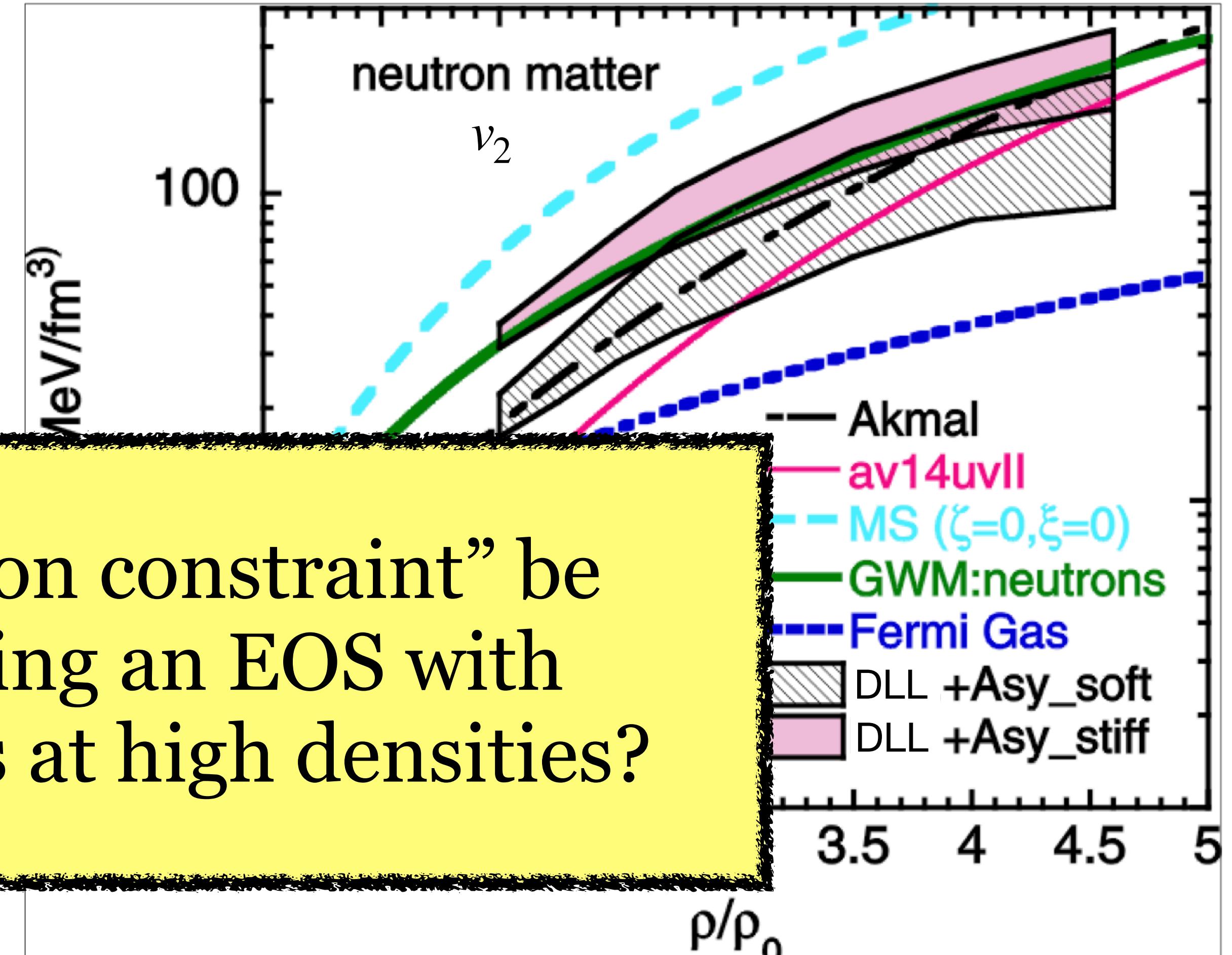
Standard way of modeling the EOS: Skyrme potential

P. Danielewicz, R. Lacey, W. G. Lynch,
Science 298, 1592–1596 (2002), arXiv:nucl-th/0208016

“the heavy-ion constraint”

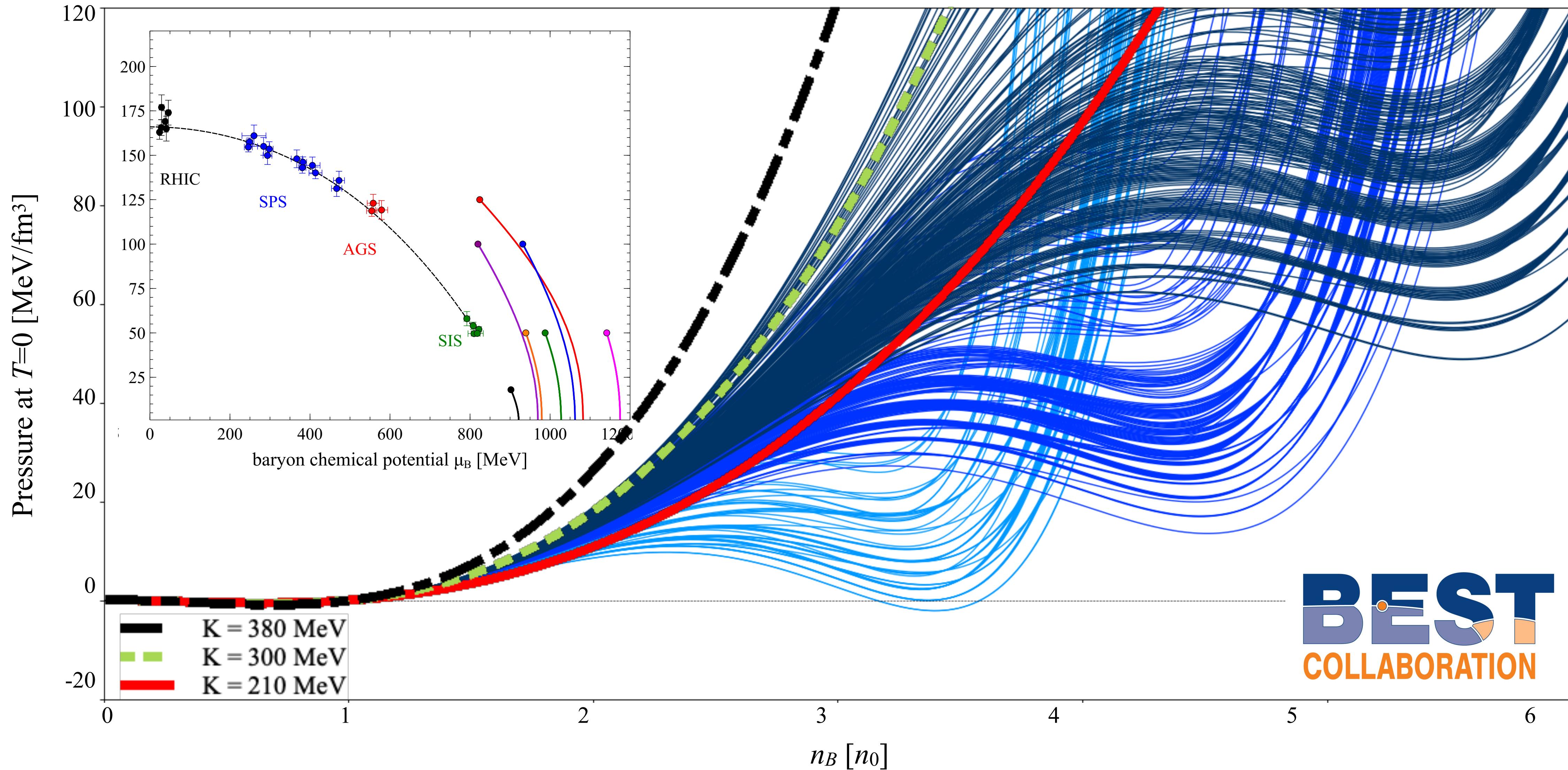


Can the “heavy-ion constraint” be improved by using an EOS with nontrivial features at high densities?



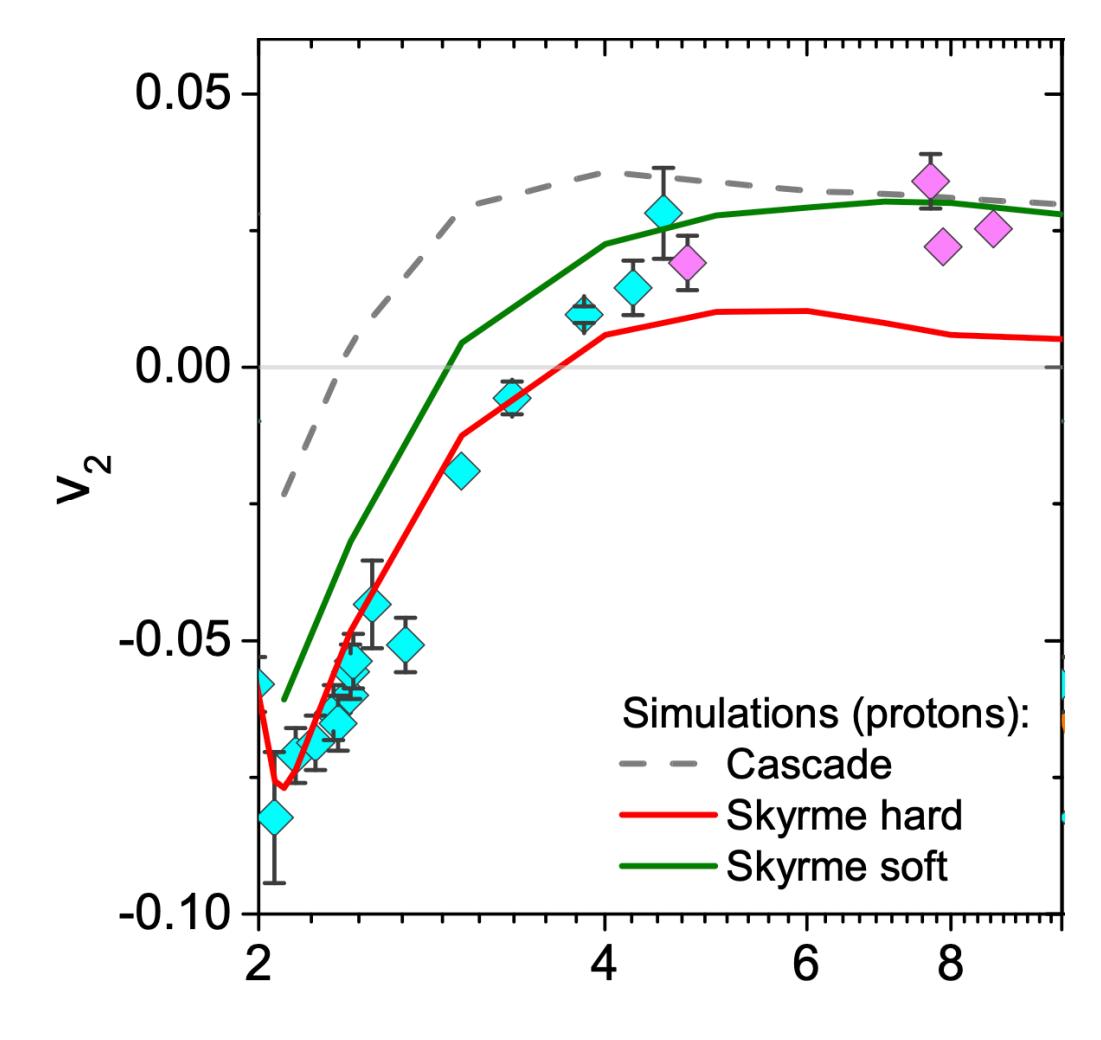
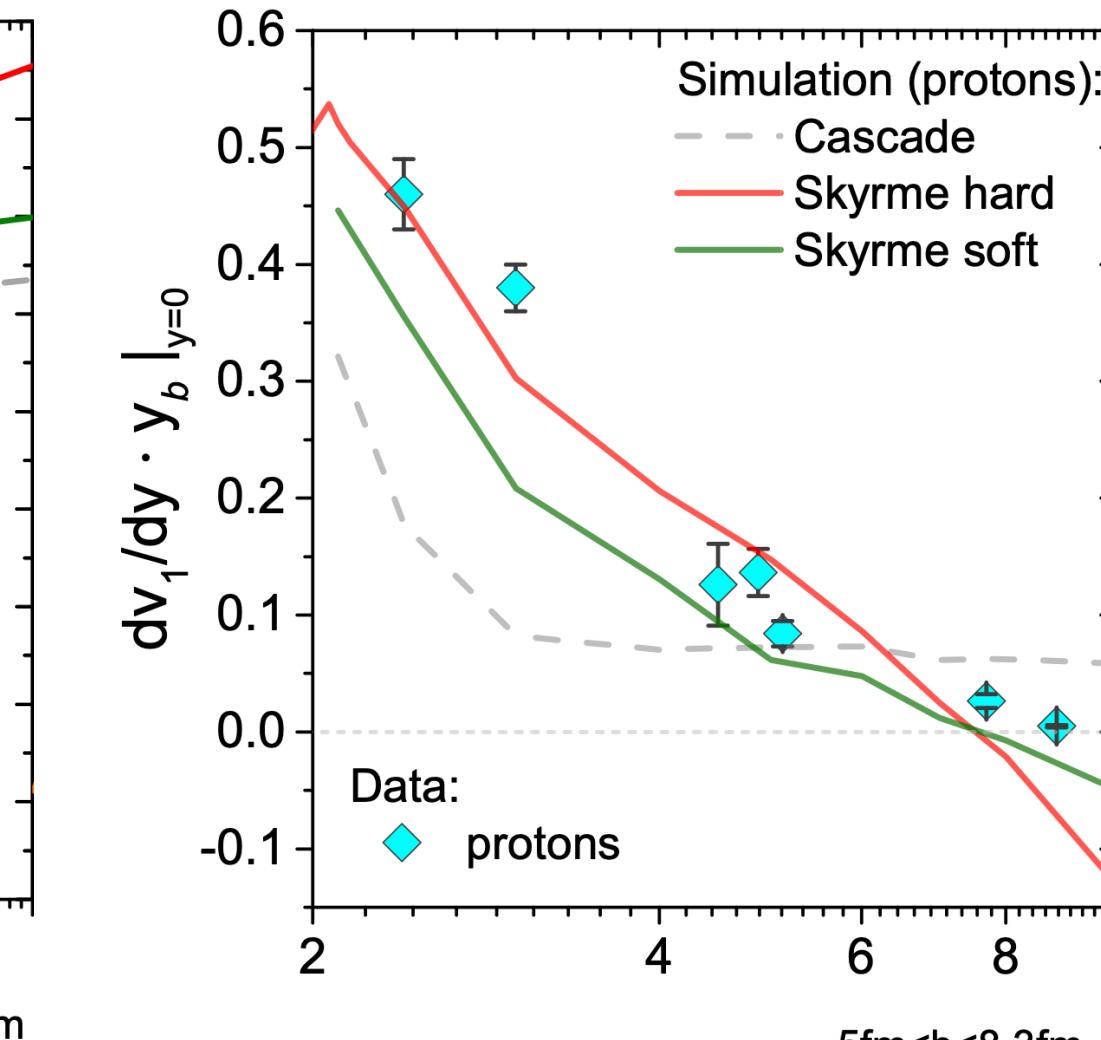
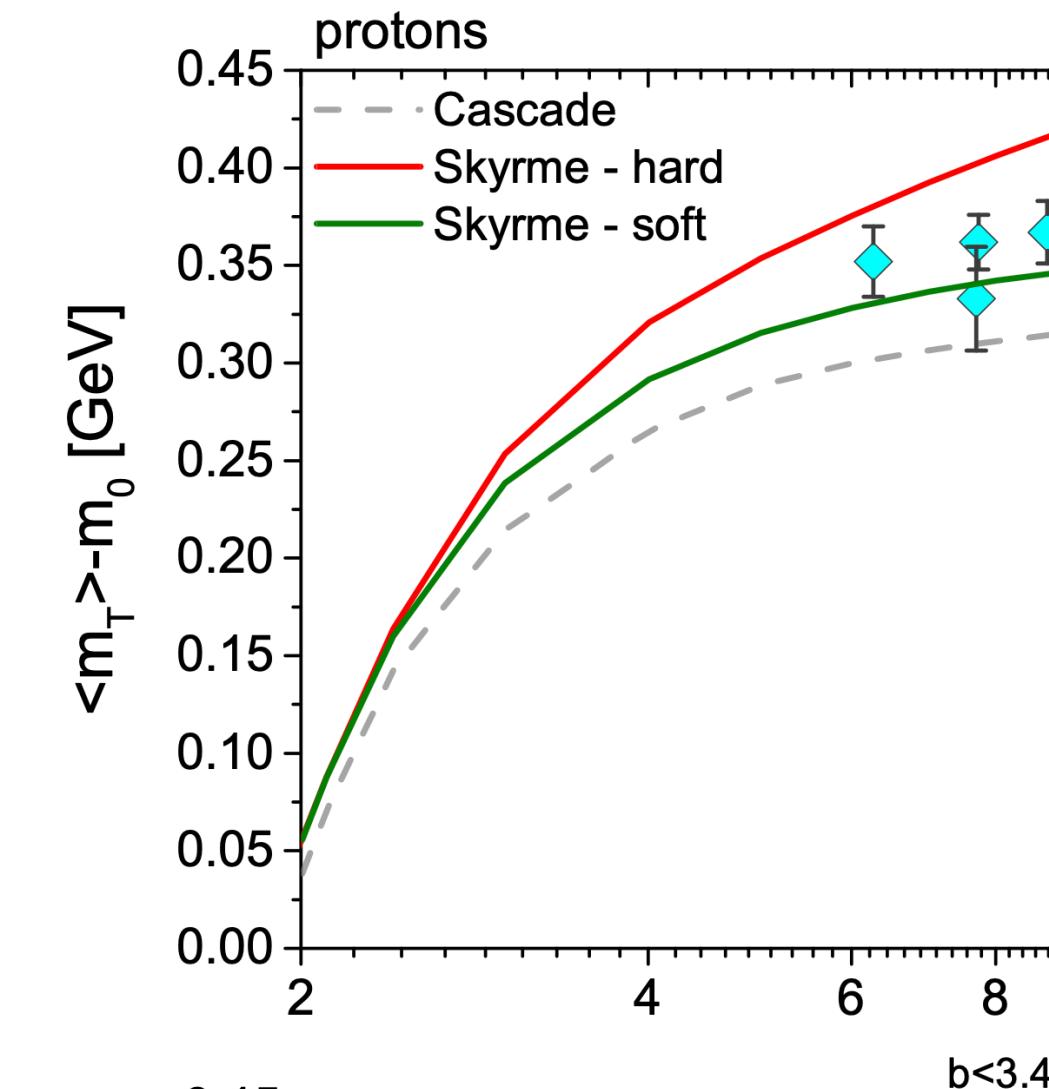
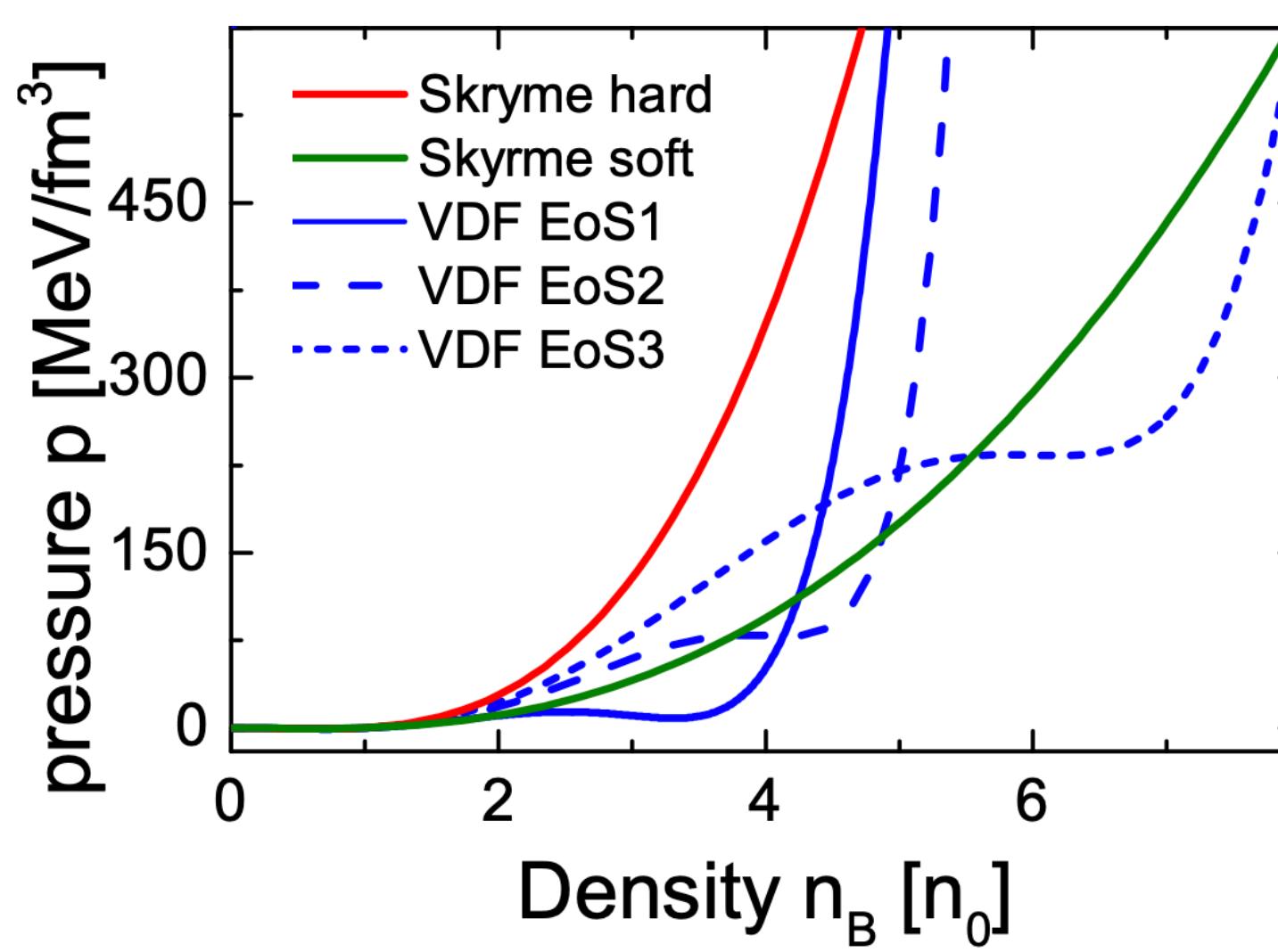
VDF model: relativistic potentials with two 1st order phase transitions

A. Sørensen, V. Koch, Phys. Rev. C 104 (2021) 3, 034904, arXiv:2011.06635



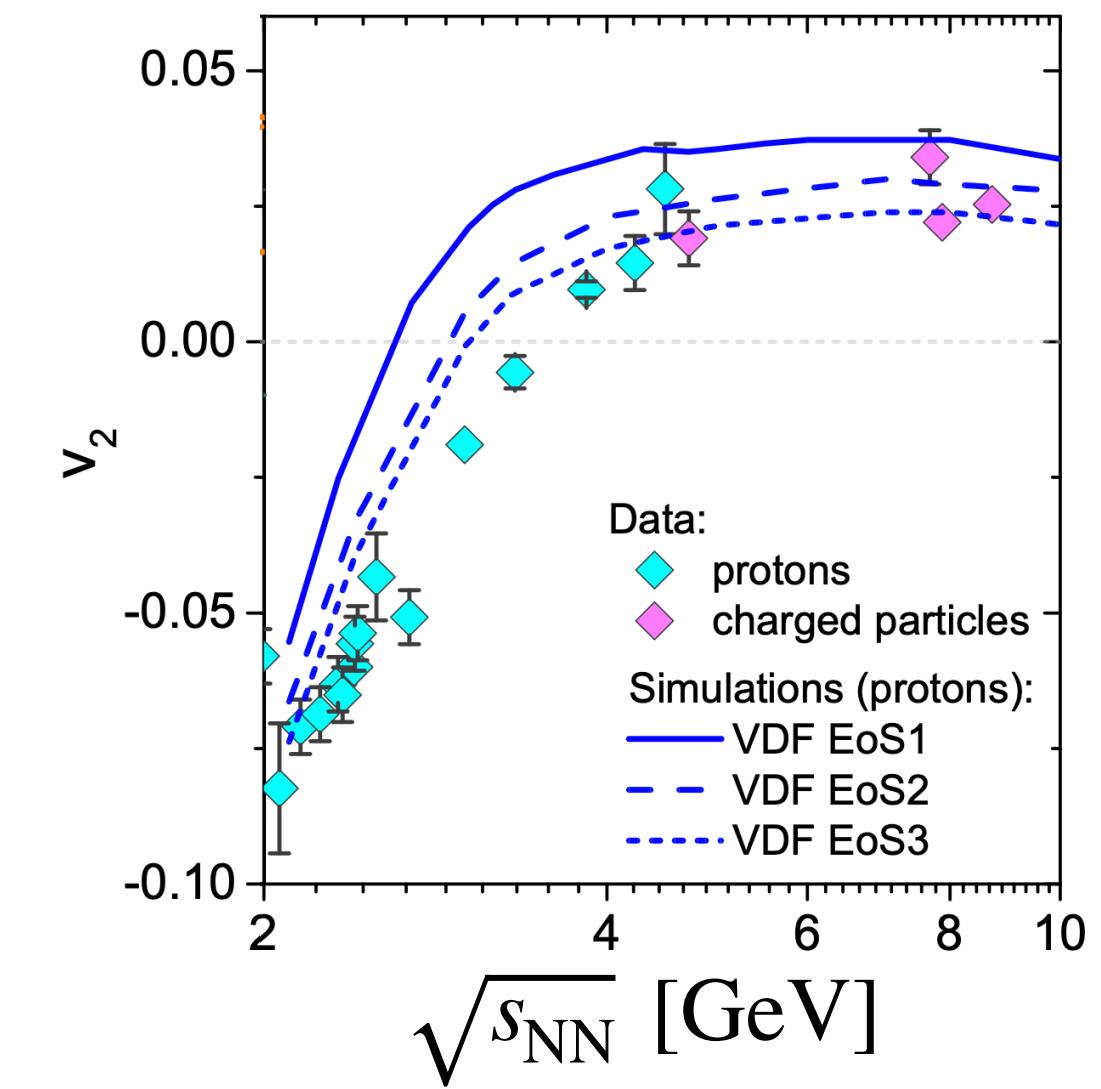
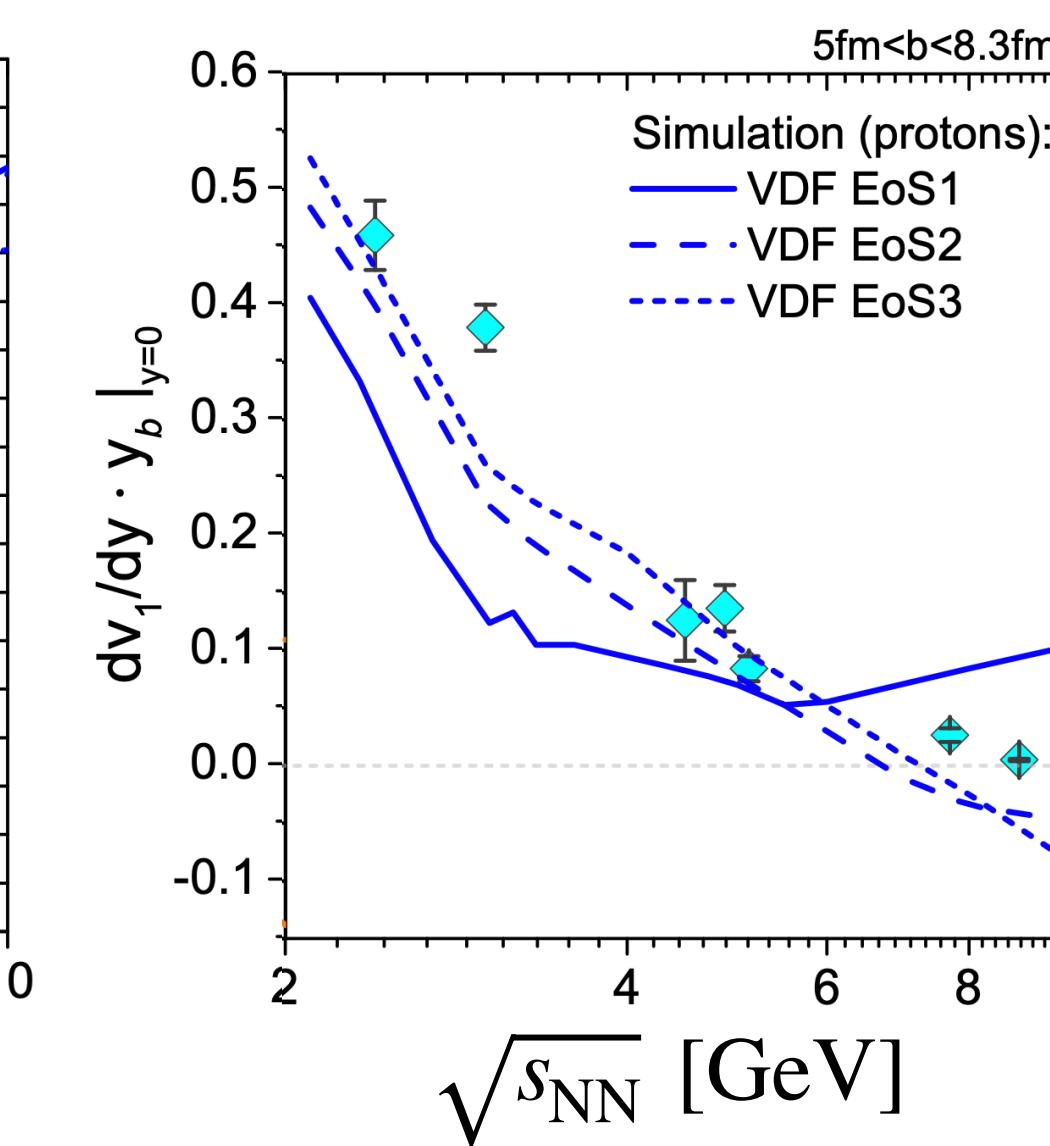
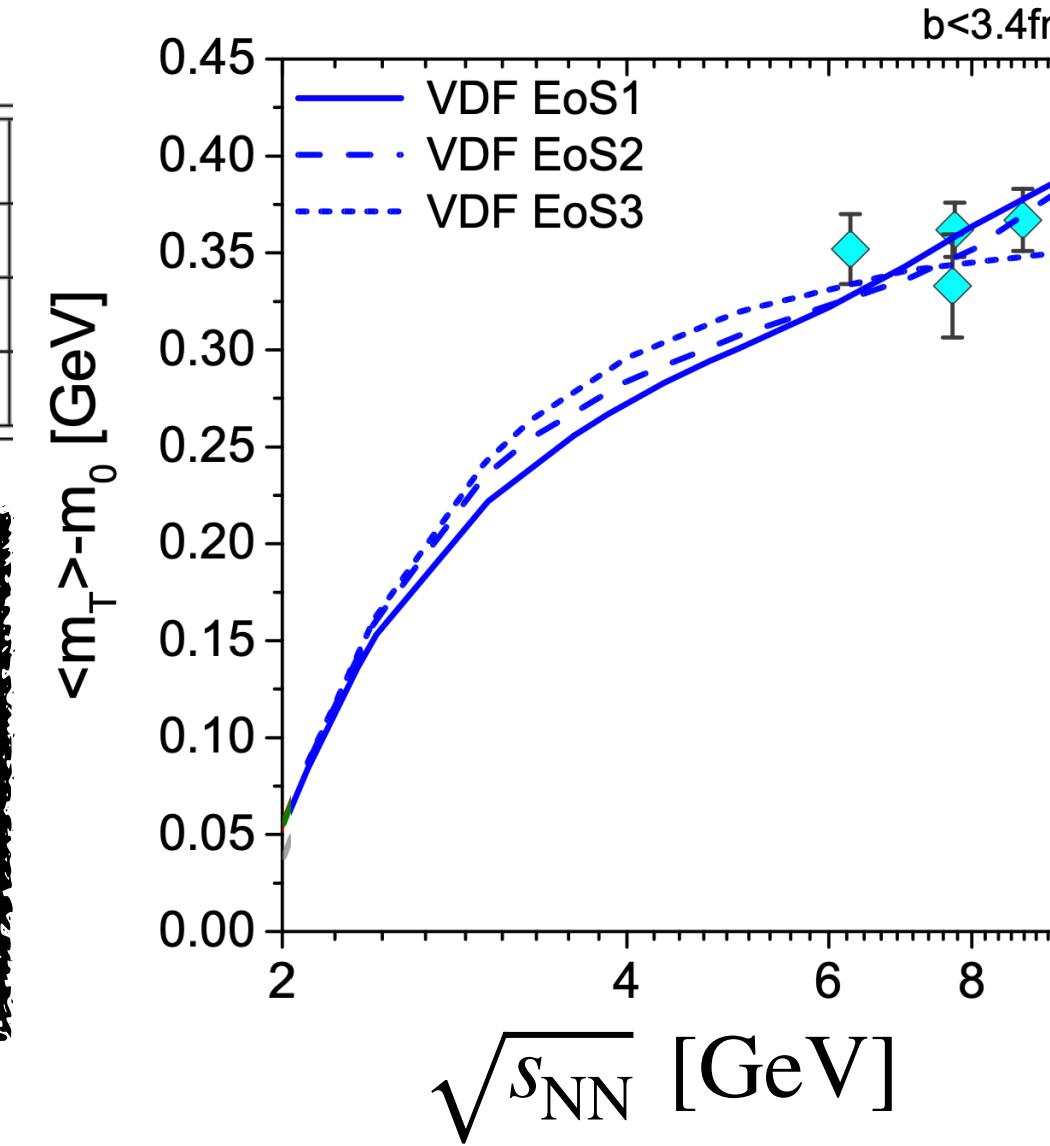
Results from UrQMD with (non-relativistic) VDF

J. Steinheimer, A. Motornenko, **A. Sorensen**, Y. Nara, V. Koch, M. Bleicher,
Eur. Phys. J. C **82**, 10, 911 (2022) arXiv:2208.12091



EoS	$T_c^{(N)}$ [MeV]	$n_c^{(Q)}$ [n_0]	$T_c^{(Q)}$ [MeV]	K_0 [MeV]
VDF1	18	3.0	100	261
VDF2	18	4.0	50	279
VDF3	22	6.0	50	356

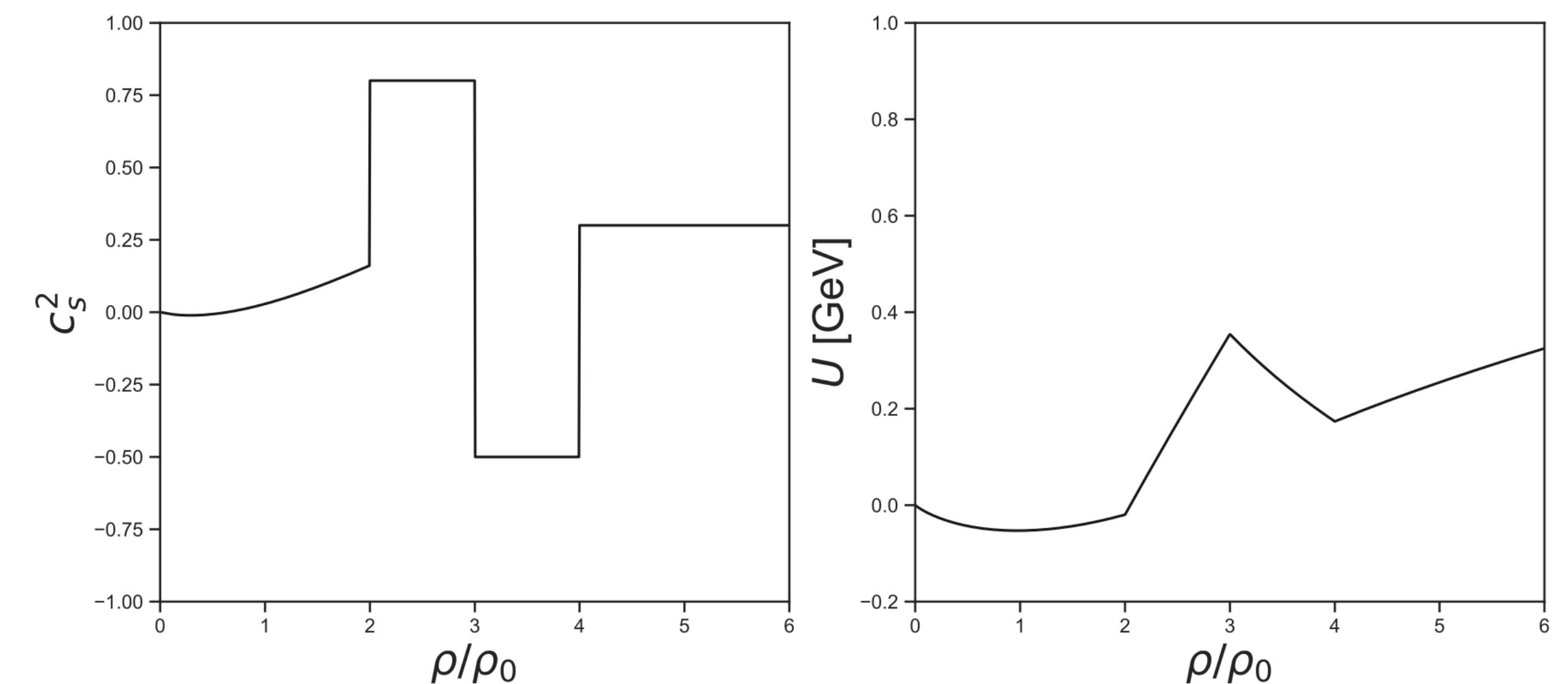
Very soft EOS at $n_B \in (2,3)n_0$
not supported in VDF+UrQMD



Better suited for Bayesian analyses: piecewise parametrization of c_s^2

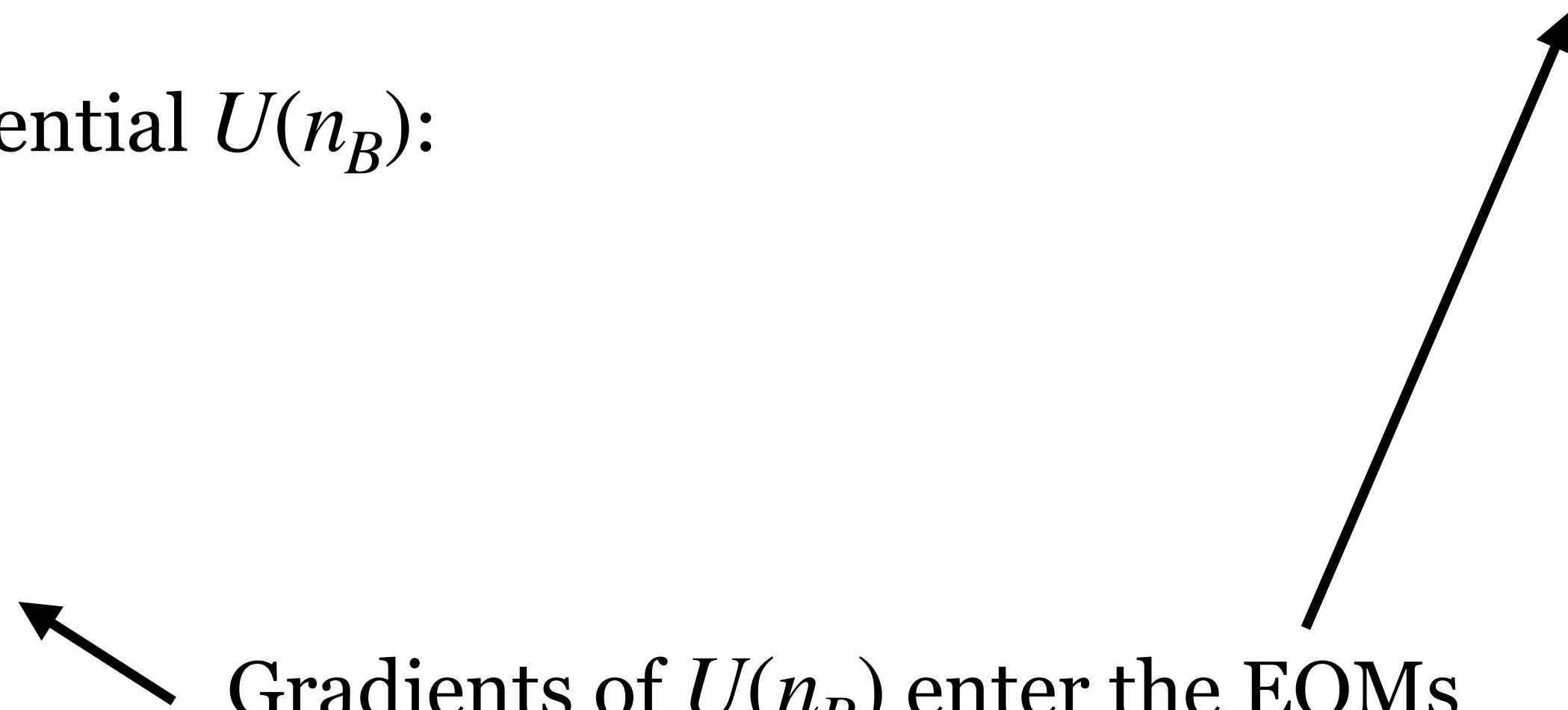
Piecewise parametrization of $c_s^2(n_B)$:

$$c_s^2(n_B) = \begin{cases} c_s^2(\text{Skyrme}), & n_B < n_1 = 2n_0 \\ c_1^2, & n_1 < n_B < n_2 \\ c_2^2, & n_2 < n_B < n_3 \\ \dots \\ c_m^2, & n_m < n_B \end{cases}$$



1-to-1 relation to the single-particle potential $U(n_B)$:

$$U(n_B) = \begin{cases} U_{\text{Sk}}(n_B) & n_B < n_1 = 2n_0 \\ U_1(n_B) & n_1 < n_B < n_2 \\ \dots \\ U_k(n_B) & n_k < n_B < n_{k+1} \end{cases}$$



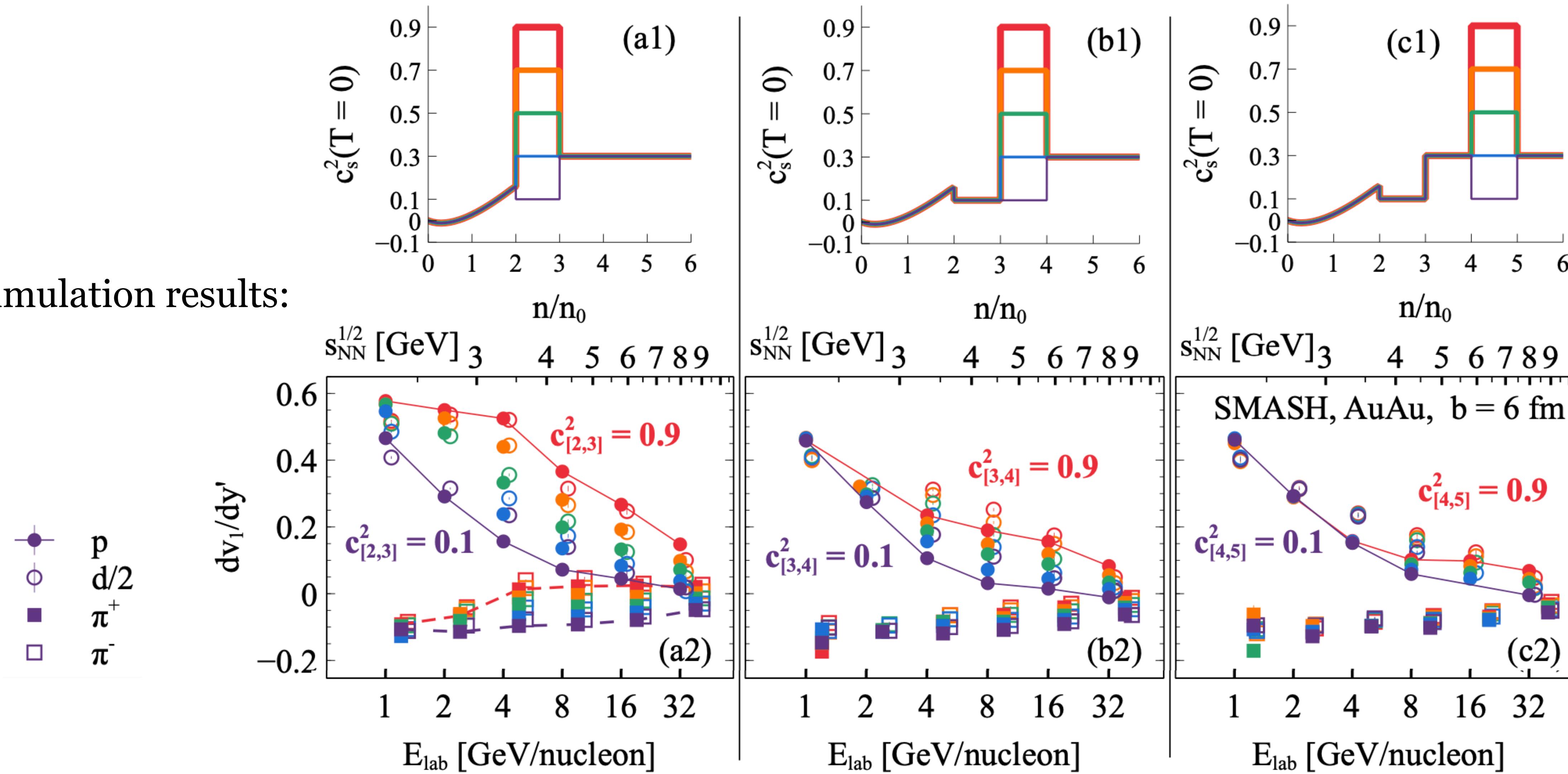
Gradients of $U(n_B)$ enter the EOMs
= directly affect the evolution in simulations

Sensitivity of HIC observables to the EOS at different beam energies

Mean-field piecewise-parametrized by values of c_s^2 for $n_i < n_B < n_j$:

D. Oliinychenko, A. Sorensen, V. Koch, L. McLerran,
Phys. Rev. C **108**, 3, 034908 (2023), arXiv:2208.11996

Simulation results:

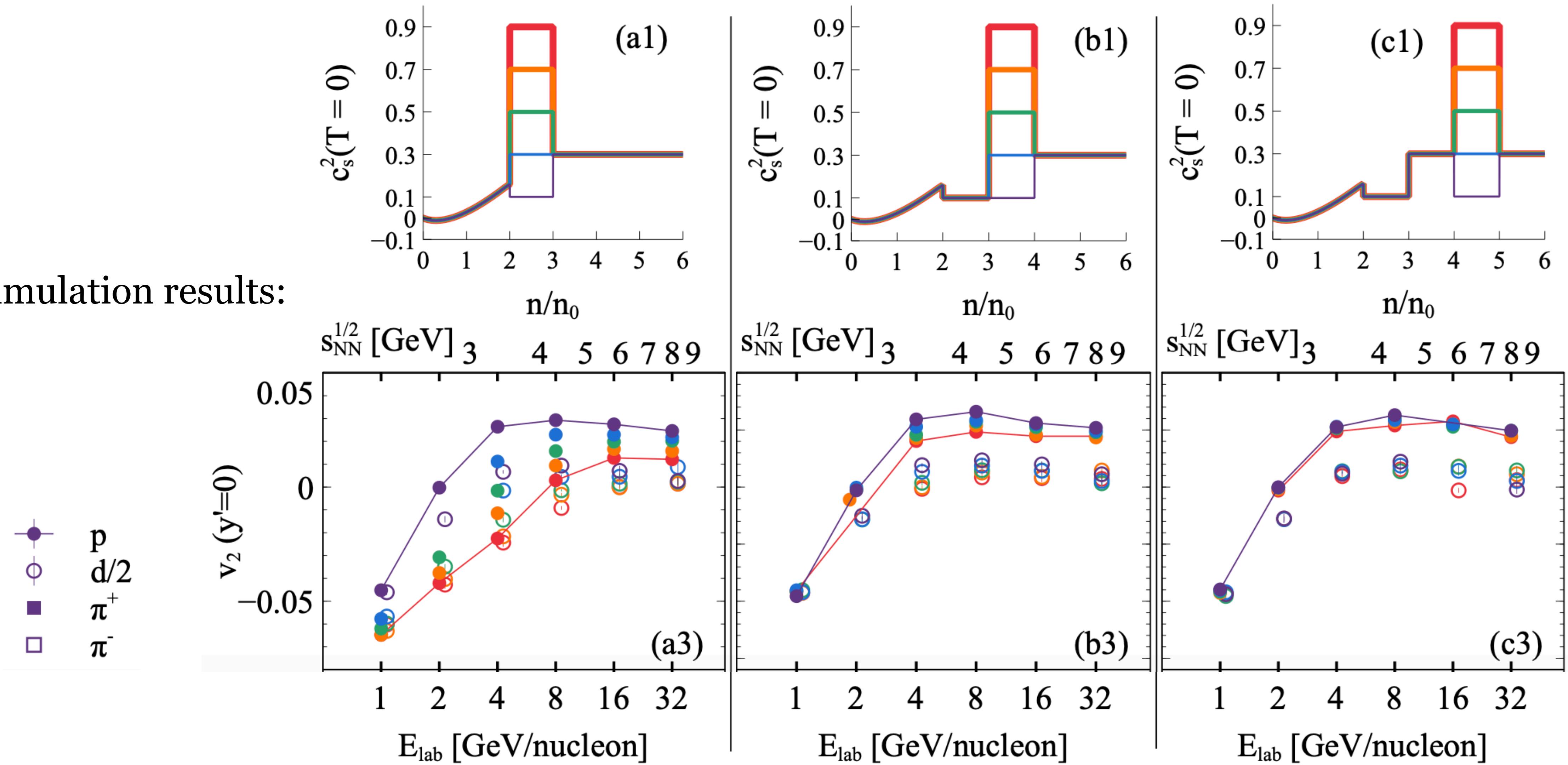


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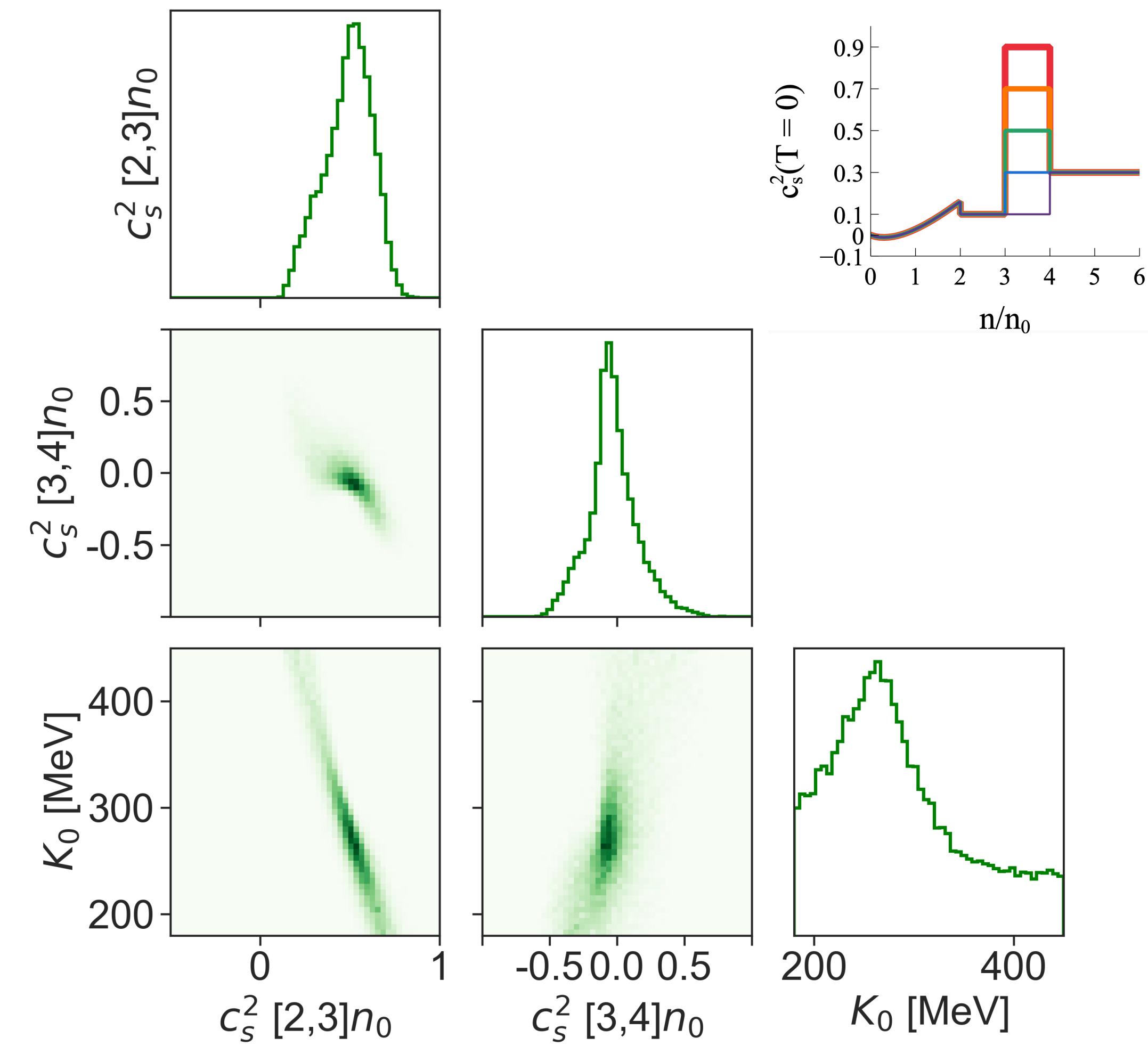
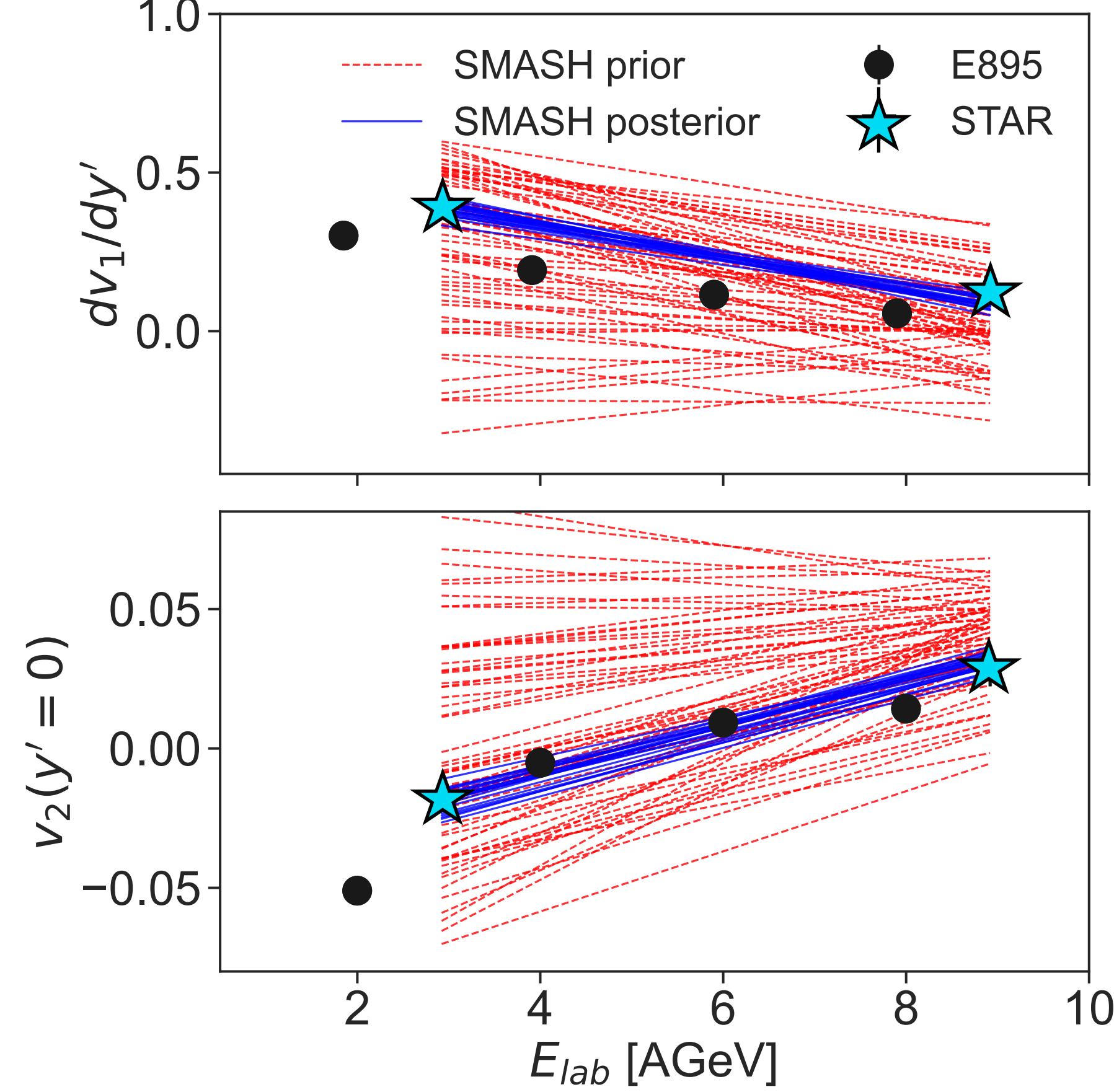
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Bayesian analysis of BES FXT flow in BUU with varying K_0 , $c_{[2,3]n_0}^2$, $c_{[3,4]n_0}^2$

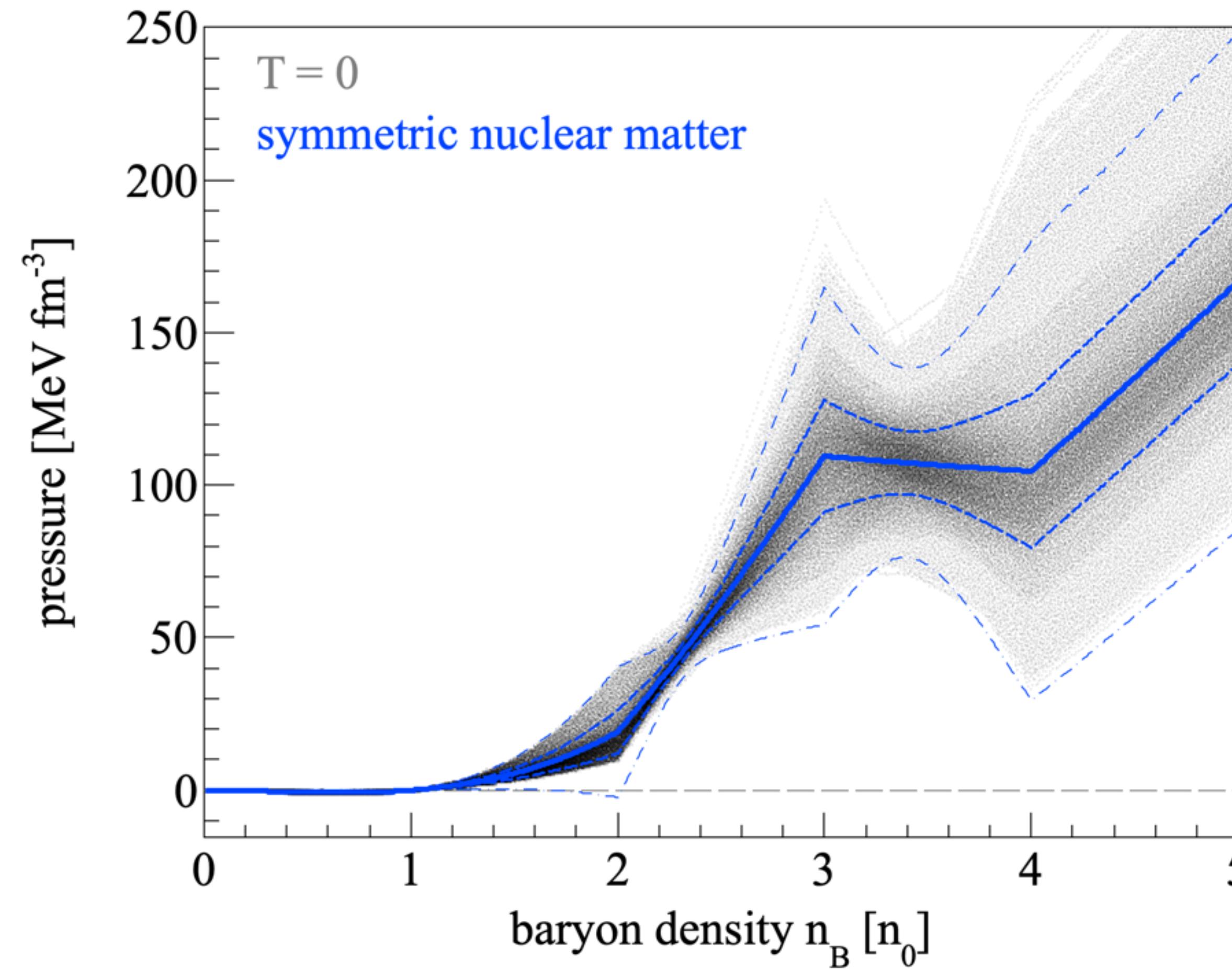


The maximum a posteriori probability (MAP) parameters are

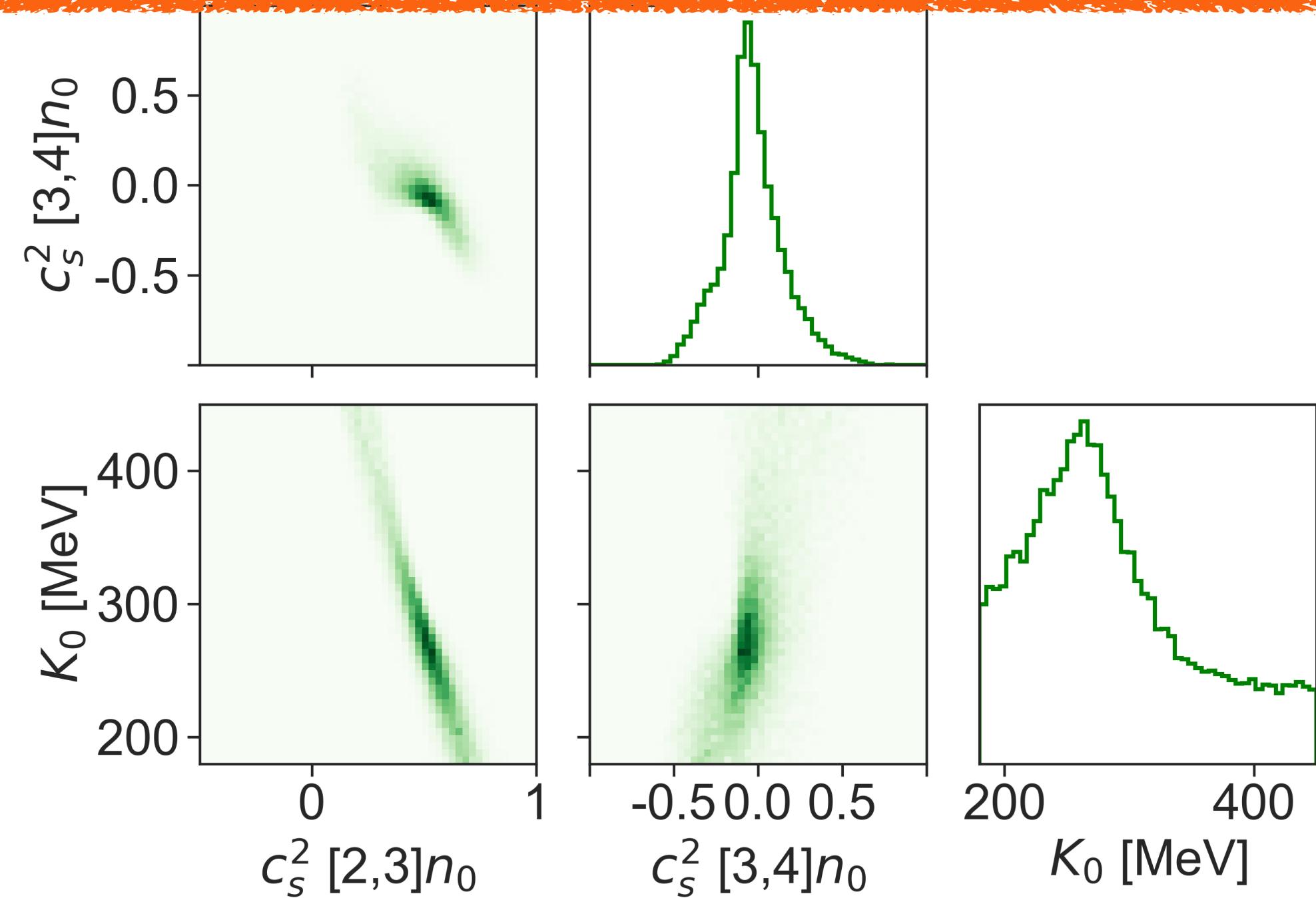
$$K_0 = 285 \pm 67 \text{ MeV}, \quad c_{[2,3]n_0}^2 = 0.49 \pm 0.13, \quad c_{[3,4]n_0}^2 = -0.03 \pm 0.15$$

D. Oliinychenko, A. Sorensen, V. Koch, L. McLellan,
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Bayesian analysis of BES FXT flow in BUU with varying K_0 , $c_{[2,3]n_0}^2$, $c_{[3,4]n_0}^2$



The constrained EOS is very stiff at $n_B \in (2,3)n_0$ and very soft at $n_B \in (3,4)n_0$



The maximum a posteriori probability (MAP) parameters are

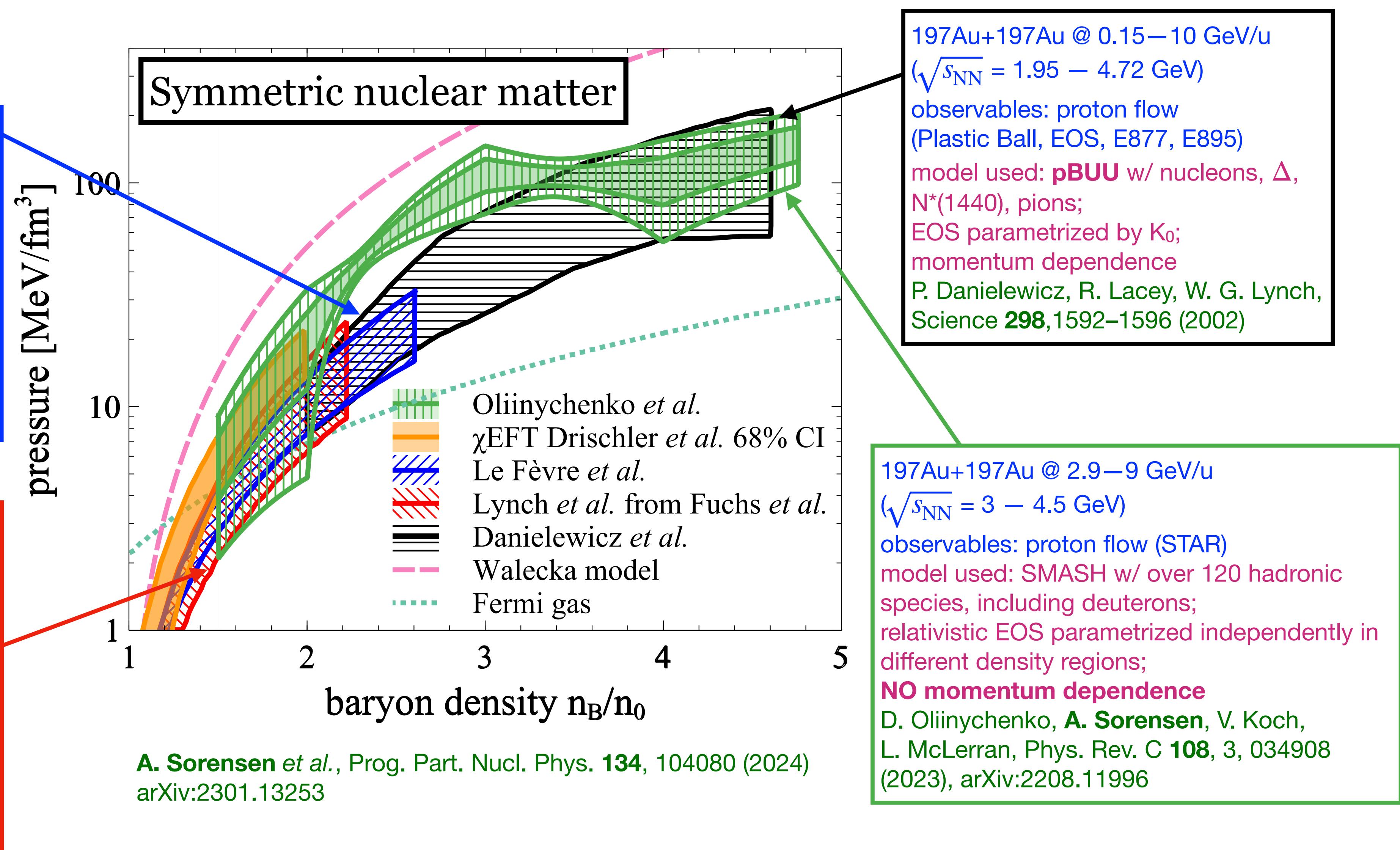
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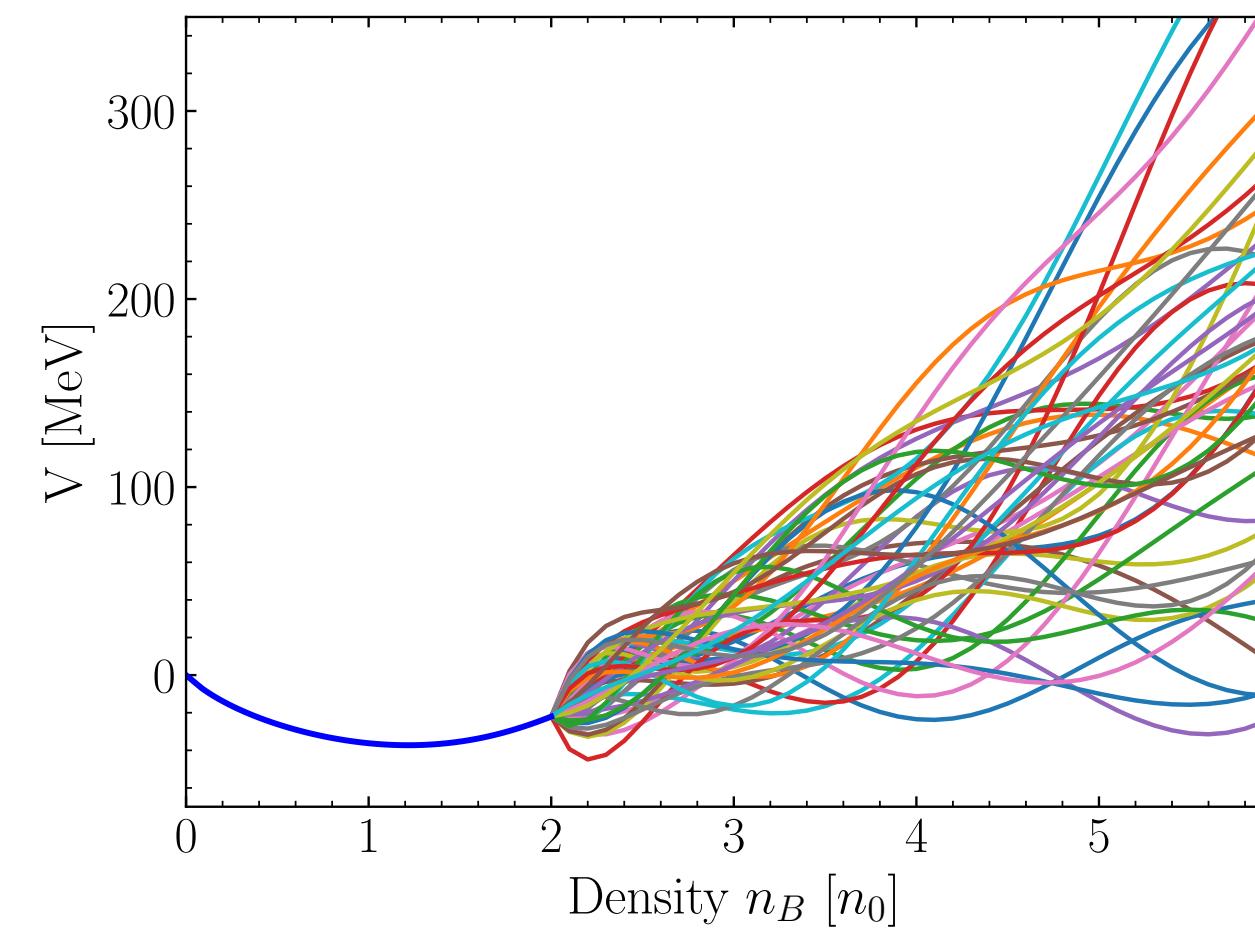
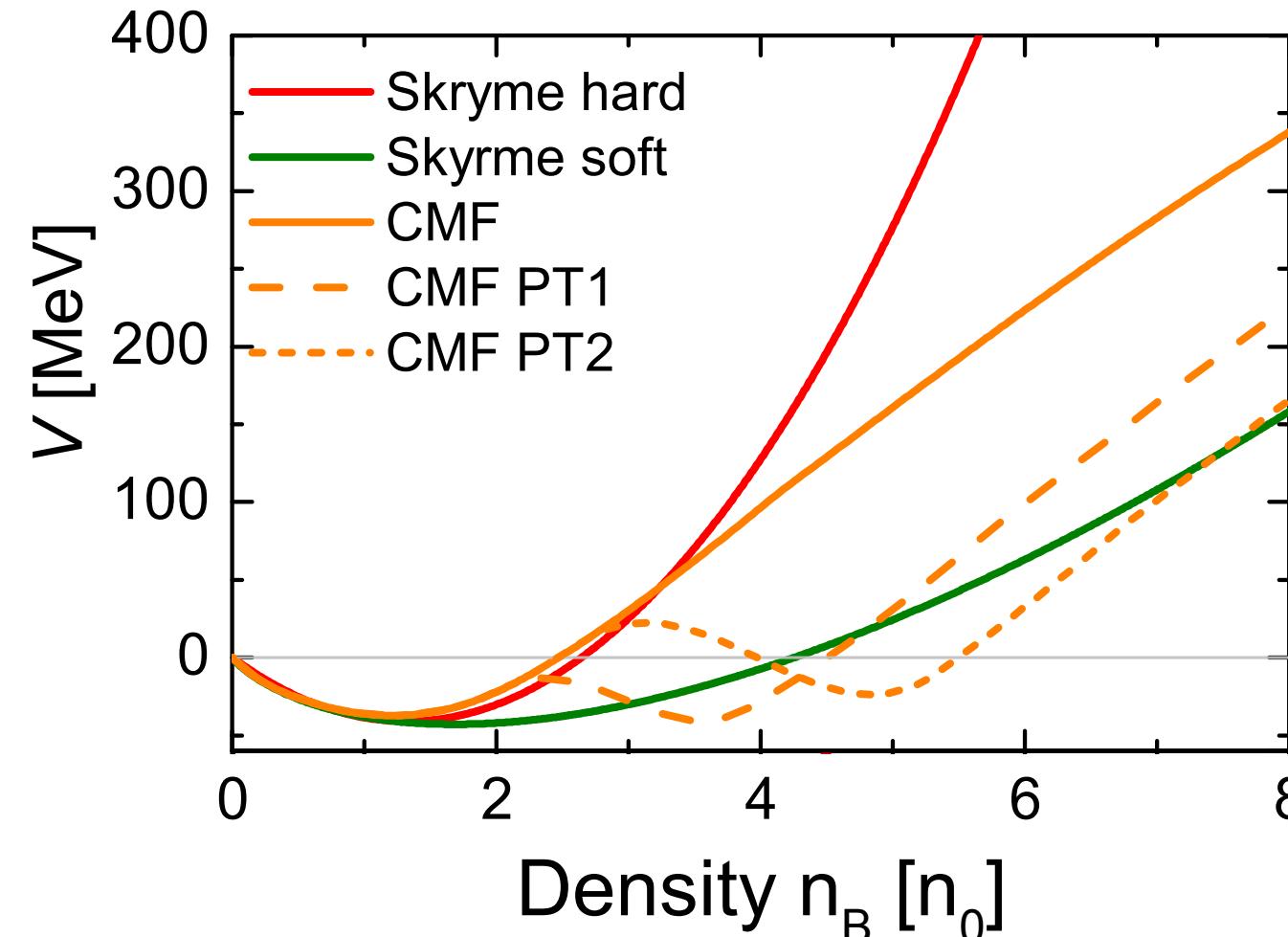
EOS of symmetric nuclear matter: selected (*few*) results

197Au+197Au @ 0.4–1.5 GeV/u
($\sqrt{s_{NN}} = 2.07 - 2.52$ GeV)
observables: proton flow (FOPI)
model used: **isospin QMD (IQMD)** w/
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EOS parametrized by K_0 ;
kaon potentials, momentum dependence
C. Fuchs *et al.*, Prog. Part. Nucl. Phys. **53**,
113–124 (2004) arXiv:nucl-th/0312052



Bayesian analysis of flow data in UrQMD



M. Omana Kuttan, J. Steinheimer, K. Zhou, H. Stoecker,
Phys. Rev. Lett. **131** 20, 202303 (2023)
arXiv:2211.11670

$$V(n_B) = \begin{cases} V_{\text{CMF}} & \\ \sum_{i=1}^7 \theta_i \left(\frac{n_B}{n_0} - 1 \right)^i + C & \end{cases}$$

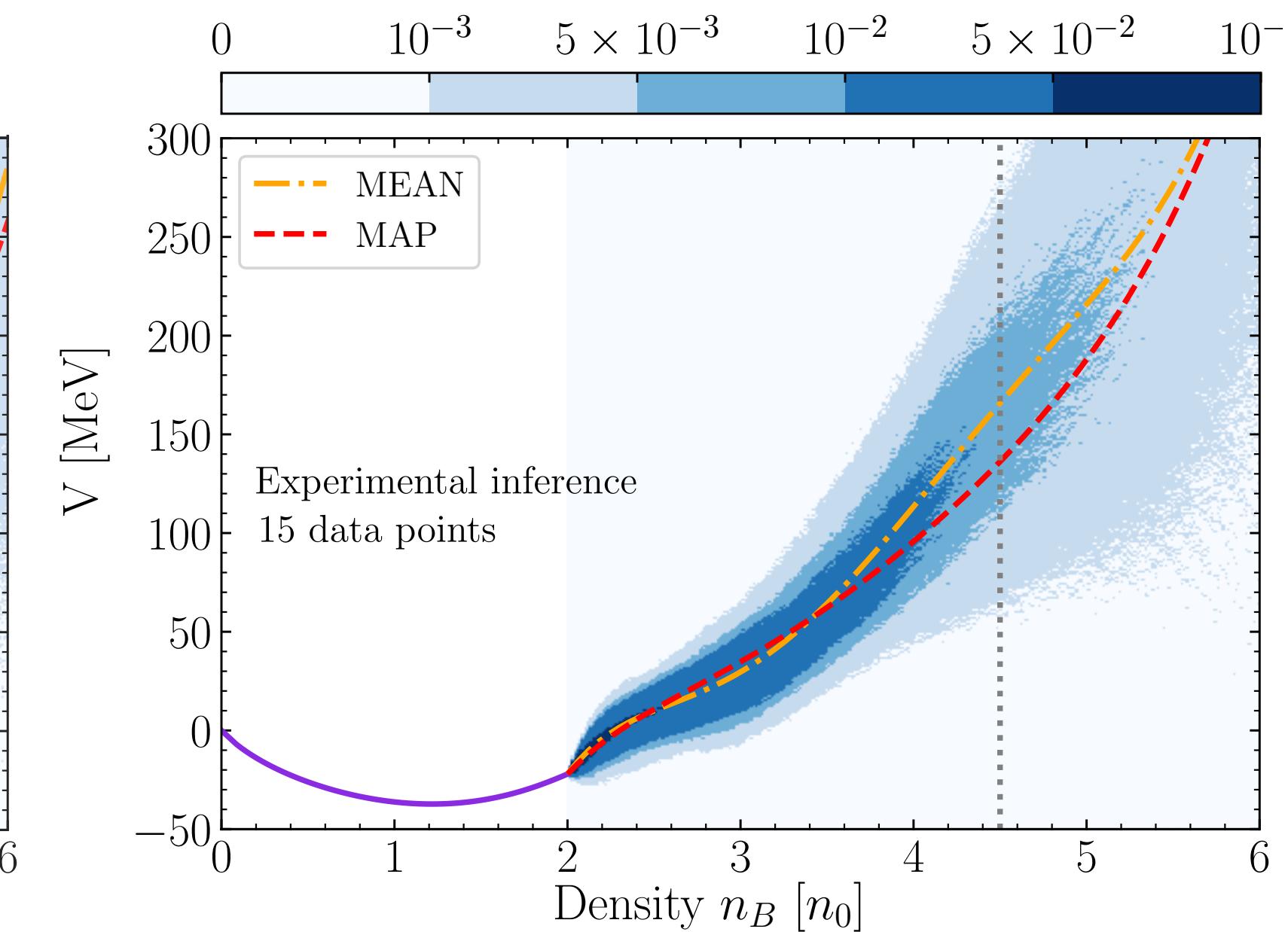
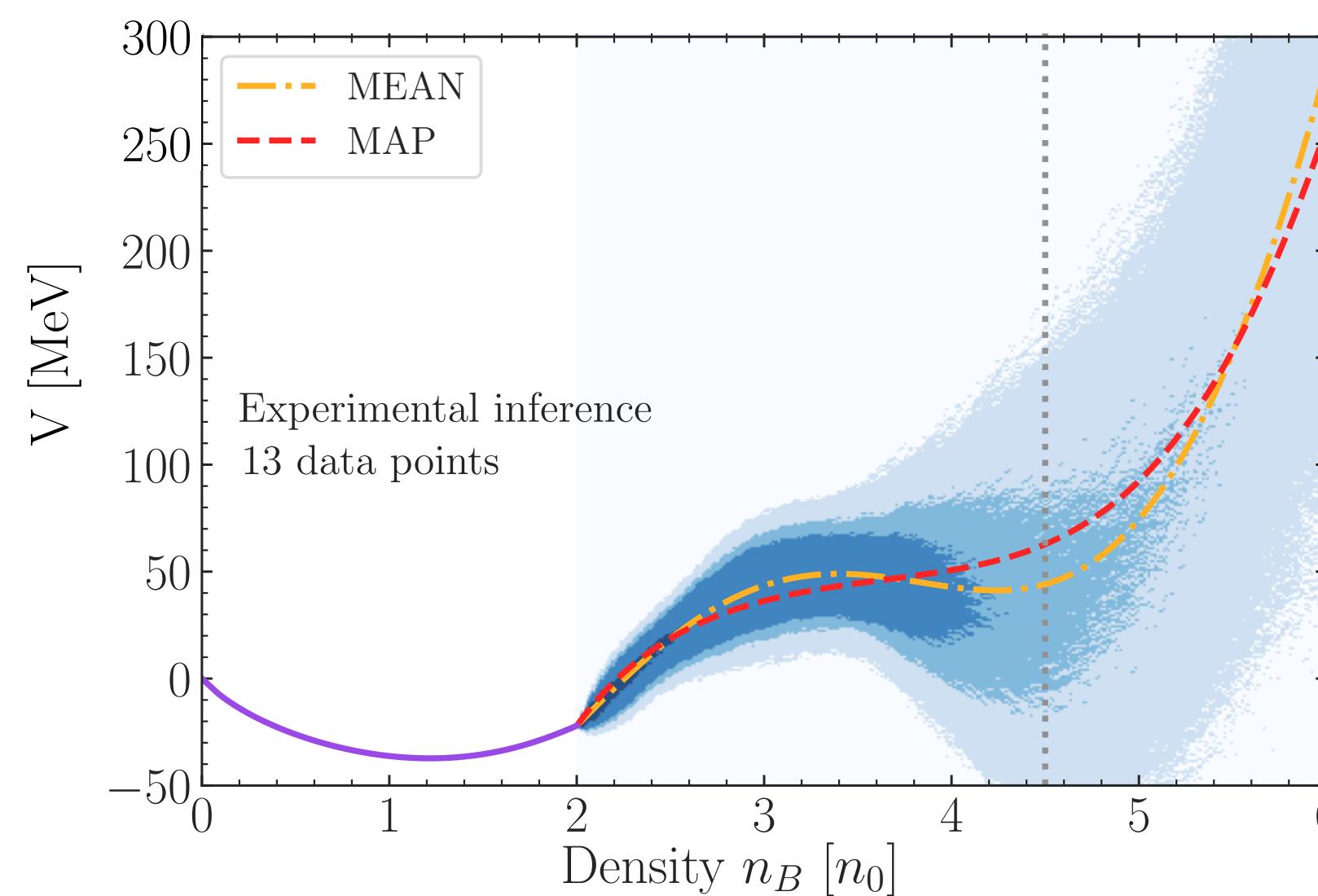
$$n_B \leq 2n_0$$

$$n_B > 2n_0$$

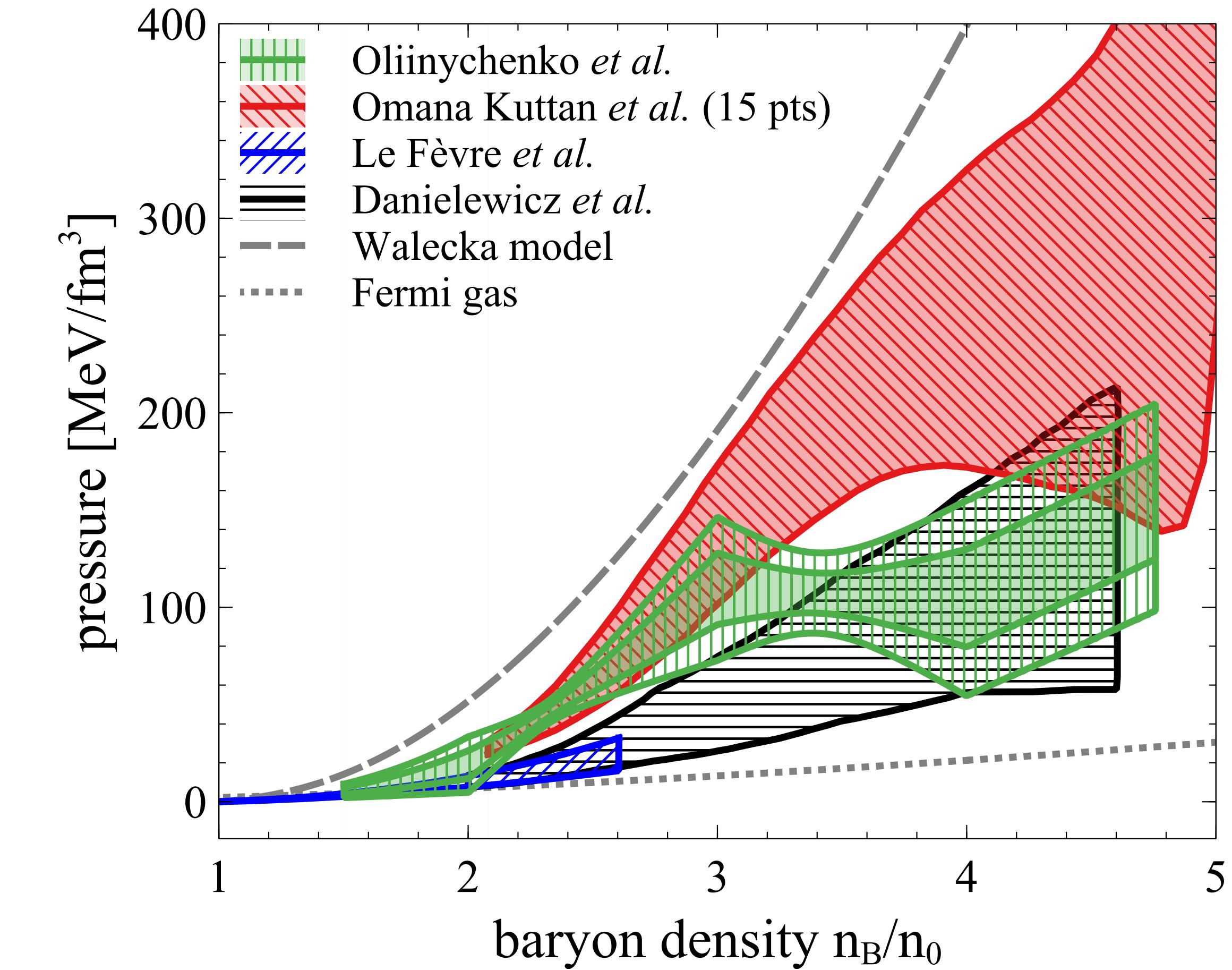
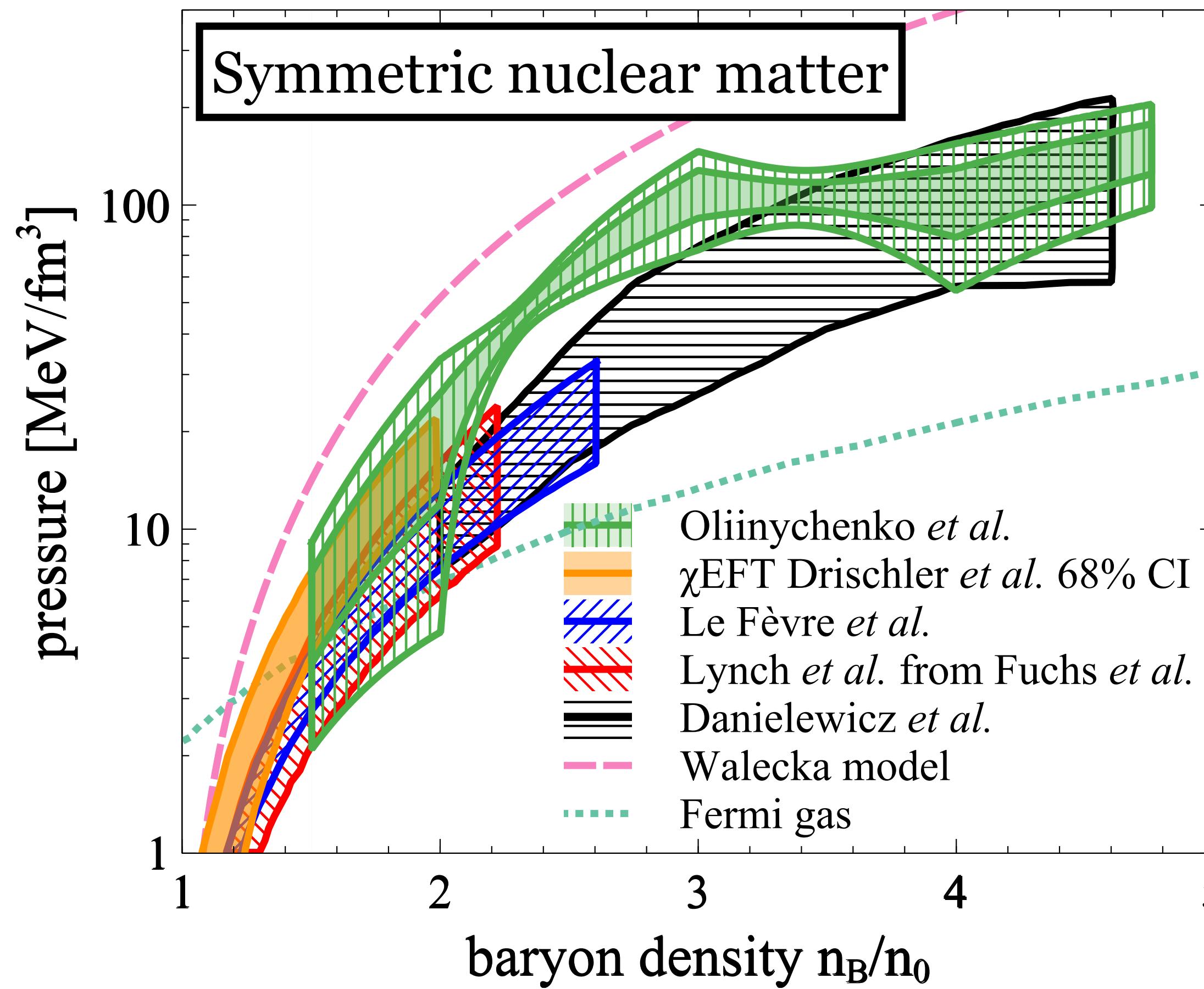
proton mean transverse kinetic energy $\langle m_T \rangle - m_0$:
 $\sqrt{s_{\text{NN}}} \in [3.83, 8.86]$ GeV

proton elliptic flow v_2 at midrapidity:
 $\sqrt{s_{\text{NN}}} \in [2.24, 4.72]$ GeV

13 points = excluding $\langle m_T \rangle - m_0$ at the two lowest collision energies
 $\sqrt{s_{\text{NN}}} = 3.83, 4.29$ GeV



EOS of symmetric nuclear matter: selected (*few*) results



A. Sorensen *et al.*, Prog. Part. Nucl. Phys. **134**, 104080 (2024)
arXiv:2301.13253

L. Du, A. Sorensen, M. Stephanov, Int. J. Mod. Phys. E
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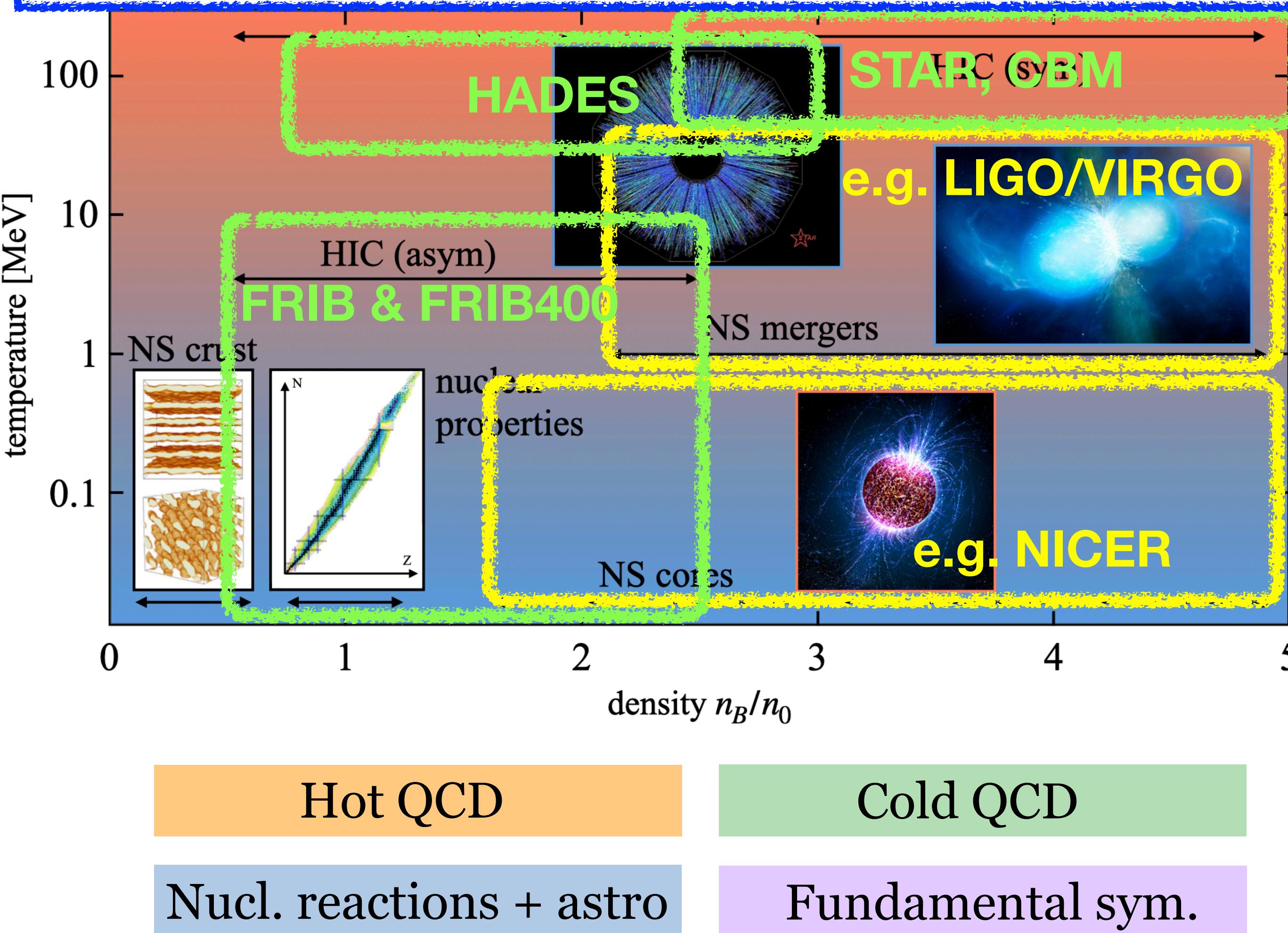
Transport simulations for extracting the properties of dense nuclear matter

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1. Introduction
2. Results: historic & recent
3. Future opportunities:
 - momentum-dependence of nuclear matter interactions
 - in-medium scattering cross-sections
 - cluster production

Golden age for studies of the EOS

- EOS is of interest to multiple diverse communities
- opportunity to study in-medium properties of nuclear matter & address outstanding problems



Dense Nuclear Matter Equation of State from Heavy-Ion Collisions *

Agnieszka Sorensen¹, Kshitij Agarwal², Kyle W. Brown^{3,4}, Zbigniew Chajecki⁵, Paweł Danielewicz^{3,6}, Christian Drischler⁷, Stefano Gandolfi⁸, Jeremy W. Holt^{9,10}, Matthias Kaminski¹¹, Che-Ming Ko^{9,10}, Rohit Kumar³, Bao-An Li¹², William G. Lynch^{3,6}, Alan B. McIntosh¹⁰, William G. Newton¹², Scott Pratt^{3,6}, Oleh Savchuk^{3,13}, Maria Stefanaki¹⁴, Ingo Tews⁸, ManYee Betty Tsang^{3,6}, Ramona Vogt^{15,16}, Hermann Wolter¹⁷, Hanna Zbroszczyk¹⁸

Endorsing authors:

Navid Abbasi¹⁹, Jörg Aichelin^{20,21}, Anton Andronic²², Steffen A. Bass²³, Francesco Becattini^{24,25}, David Blaschke^{26,27,28}, Marcus Bleicher^{29,30}, Christoph Blume³¹, Elena Bratkovskaya^{14,29,30}, B. Alex Brown^{3,6}, David A. Brown³², Alberto Camaiani³³, Giovanni Casini²⁵, Katerina Chatzioannou^{34,35}, Abdelouahad Chbihi³⁶, Maria Colonna³⁷, Mircea Dan Cozma³⁸, Veronica Dexheimer³⁹, Xin Dong⁴⁰, Travis Dore⁴¹, Lipei Du⁴², José A. Dueñas⁴³, Hannah Elfner^{14,21,29,30}, Wojciech Florkowski⁴⁴, Yuki Fujimoto¹, Richard J. Furnstahl⁴⁵

highest cited of all* WPs for the 2023 LRP!

*published (arXiv, journal, etc.)

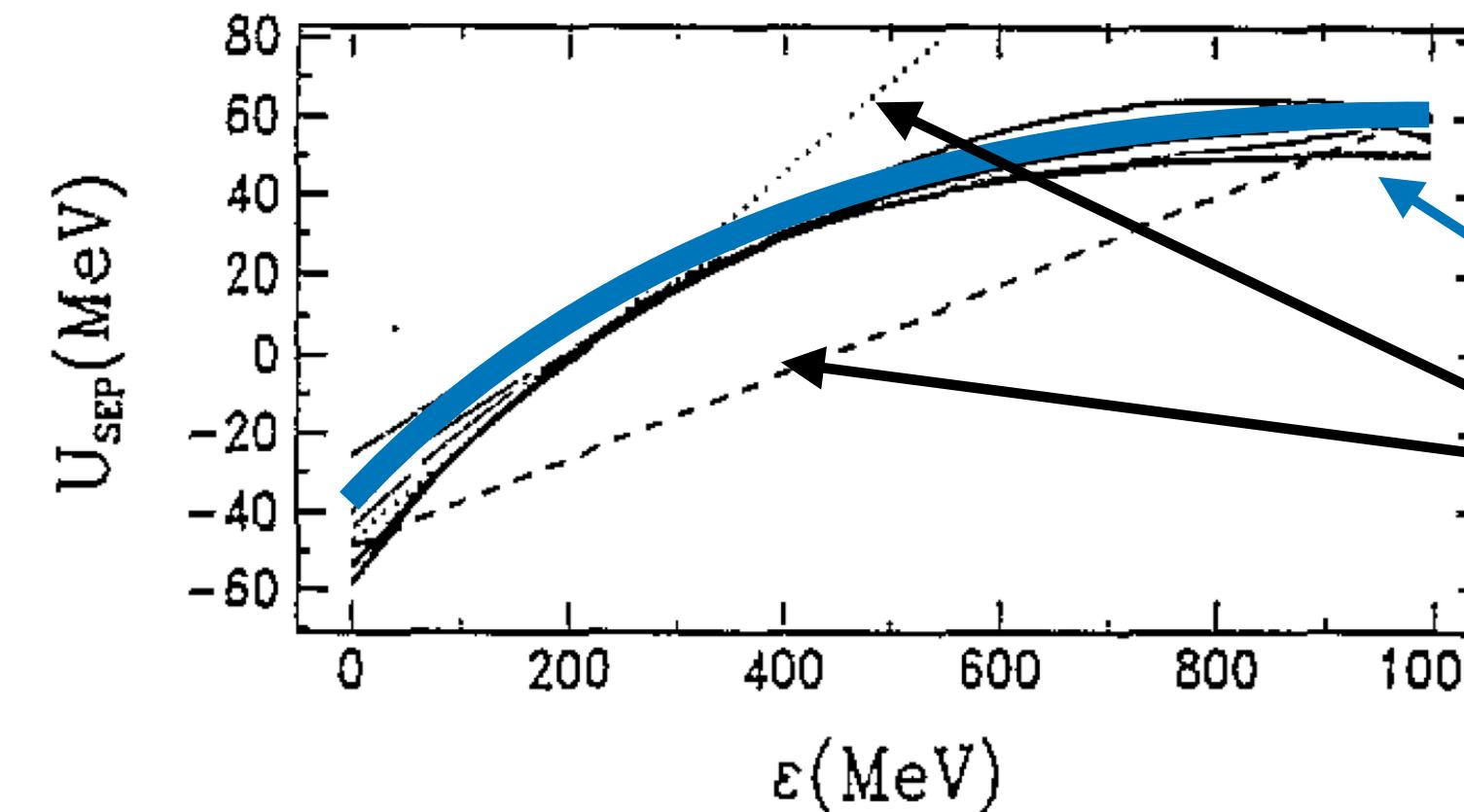
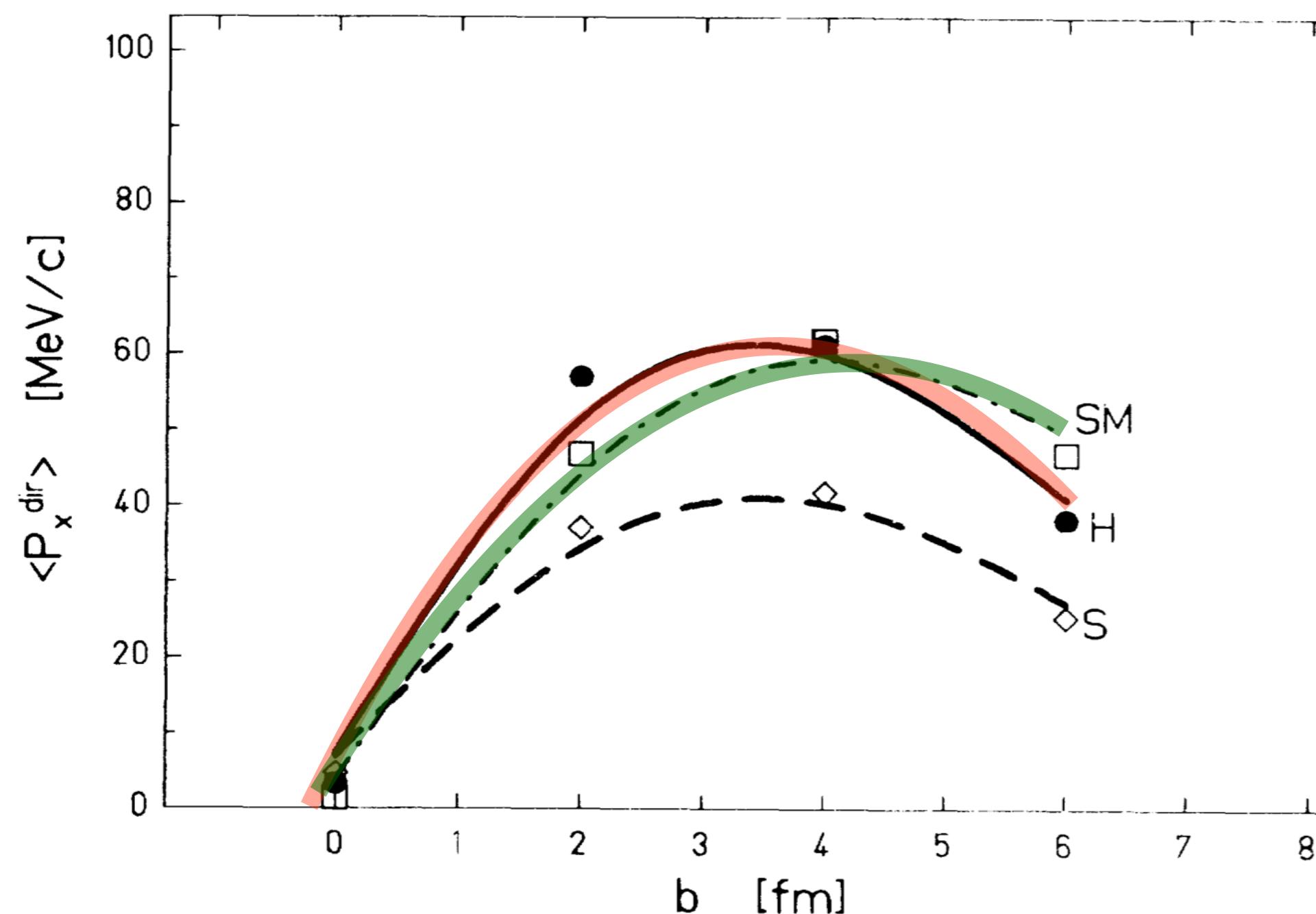
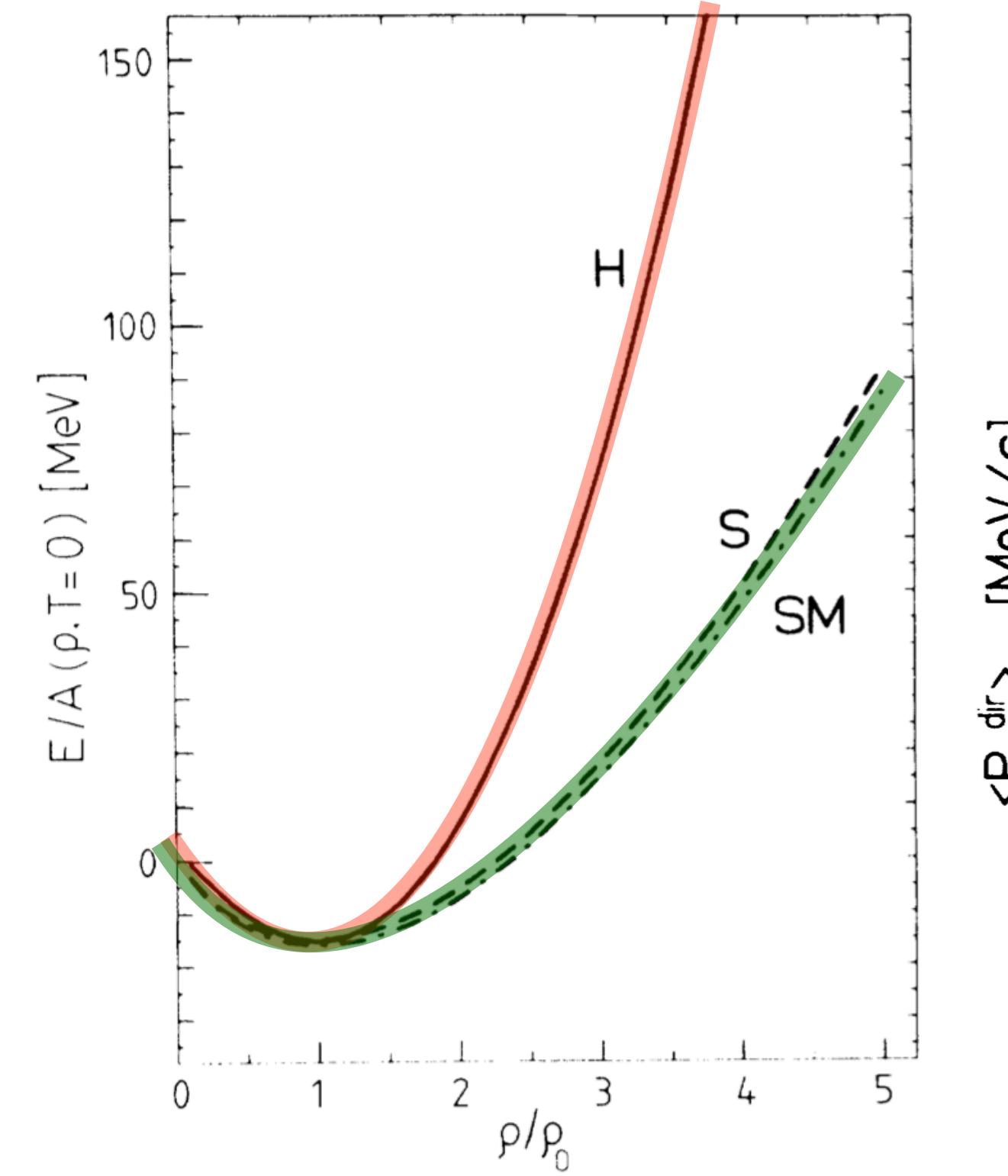
José C. Jiménez⁶¹, Joseph Kapusta⁶², Behruz Kardan³¹, Iurii Karpenko⁶³, Declan Keane³⁹, Dmitri Kharzeev^{60,64}, Andrej Kugler⁶⁵, Arnaud Le Fèvre¹⁴, Dean Lee^{3,6}, Hong Liu⁶⁶, Michael A. Lisa⁴⁵, William J. Llope⁶⁷, Ivano Lombardo⁶⁸, Manuel Lorenz³¹, Tommaso Marchi⁶⁹, Larry McLerran¹, Ulrich Mosel⁷⁰, Anton Motornenko²¹, Berndt Müller²³, Paolo Napolitani⁷¹, Joseph B. Natowitz¹⁰, Witold Nazarewicz^{3,6}, Jorge Noronha⁷², Jacquelyn Noronha-Hostler⁷², Grażyna Odyniec⁴⁰, Panagiota Papakonstantinou⁷³, Zuzana Paulínyová⁷⁴, Jorge Piekarewicz⁷⁵, Robert D. Pisarski⁶⁰, Christopher Plumberg⁷⁶, Madappa Prakash⁷, Jørgen Randrup⁴⁰, Claudia Ratti⁷⁷, Peter Rau¹, Sanjay Reddy¹, Hans-Rudolf Schmidt^{2,14}, Paolo Russotto³⁷, Radosław Ryblewski⁷⁸, Andreas Schäfer⁷⁹, Björn Schenke⁶⁰, Srimoyee Sen⁸⁰, Peter Senger⁸¹, Richard Seto⁸², Chun Shen^{67,83}, Bradley Sherrill^{3,6}, Mayank Singh⁶², Vladimir Skokov^{83,84}, Michał Spaliński^{85,86}, Jan Steinheimer²¹, Mikhail Stephanov⁸⁷, Joachim Stroth^{14,31}, Christian Sturm¹⁴, Kai-Jia Sun⁸⁸, Aihong Tang⁶⁰, Giorgio Torrieri^{89,90}, Wolfgang Trautmann¹⁴, Giuseppe Verde⁹¹, Volodymyr Vovchenko⁷⁷, Ryoichi Wada¹⁰, Fuqiang Wang⁹², Gang Wang⁵⁴, Klaus Werner²⁰, Nu Xu⁴⁰, Zhangbu Xu⁶⁰, Ho-Ung Yee⁸⁷, Sherry Yennello^{9,10,93}, Yi Yin⁹⁴

Momentum-dependence of nuclear matter interactions

Momentum-dependence of interactions is a necessary component

Measured in scattering experiments (at n_0):

Influence: flow from a hard EOS looks like flow from a soft EOS with p -dependence!

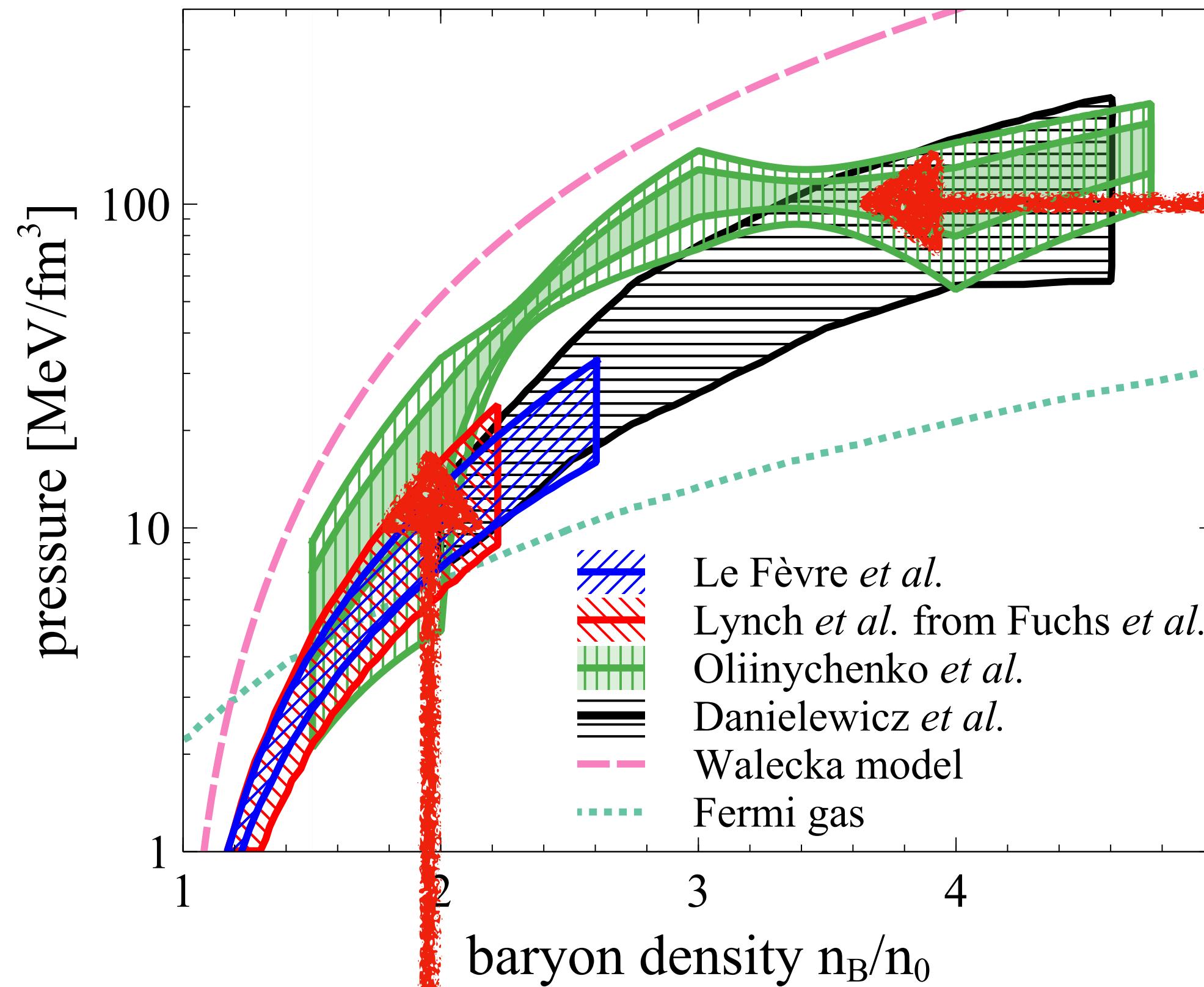


B. Blaettel, V. Koch, U. Mosel,
Rept. Prog. Phys. **56**, 1–62 (1993)

fits to data
parametrizations of
the Walecka model

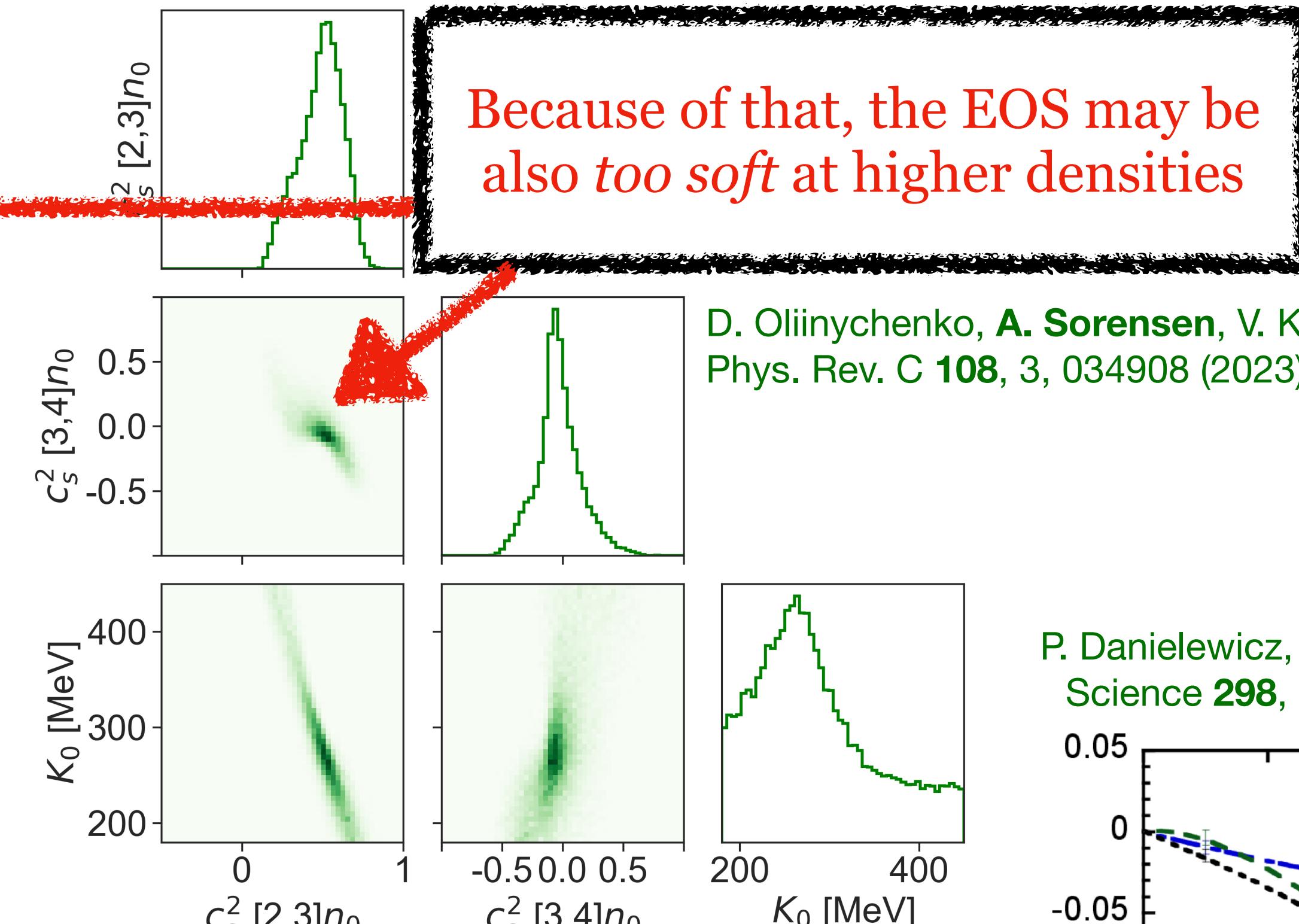
J. Aichelin, A. Rosenhauer, G. Peilert,
H. Stoecker, W. Greiner,
Phys. Rev. Lett. **58** 1926–1929 (1987)

Momentum-dependence of nuclear matter interactions



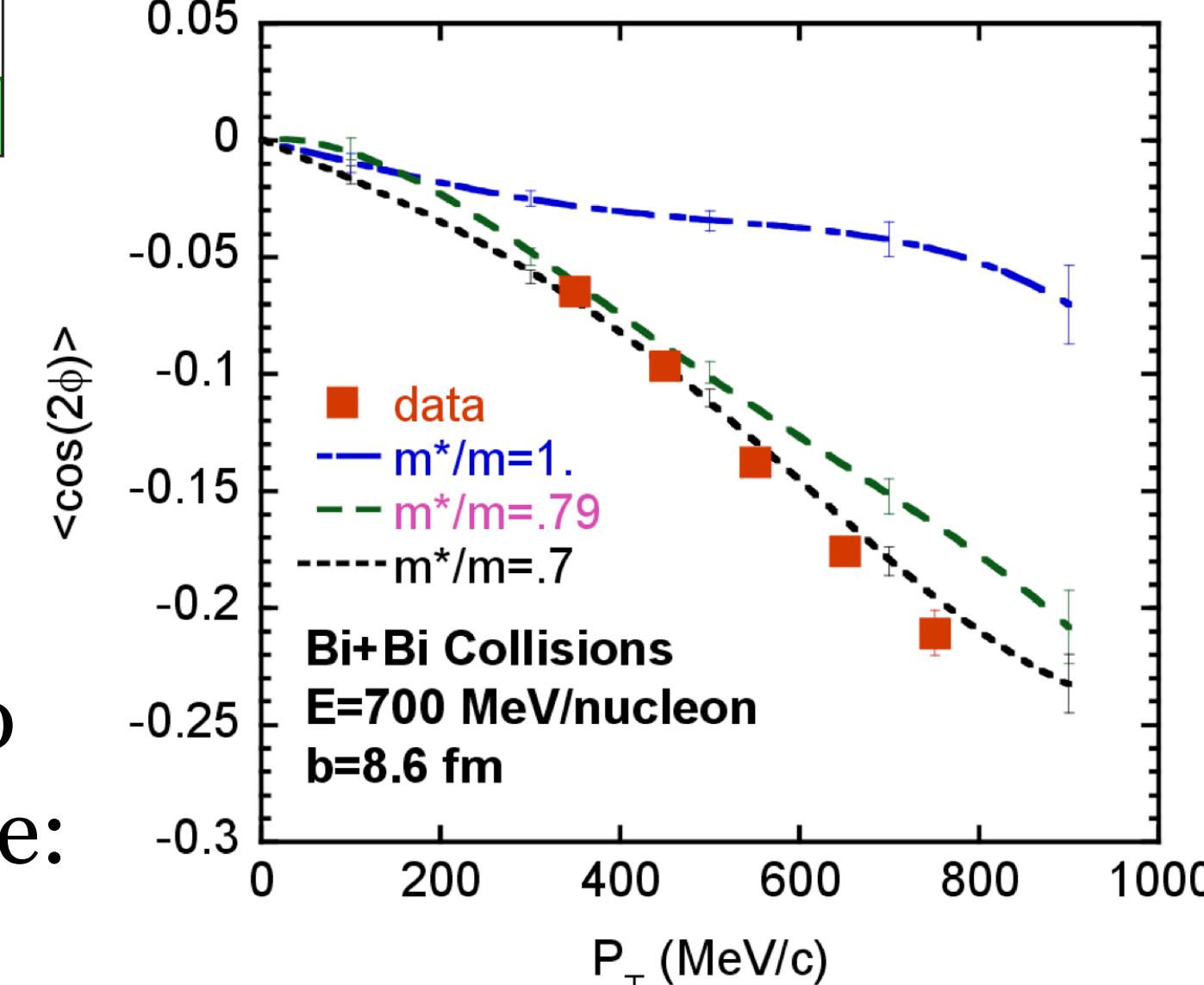
A. Sorensen *et al.*, Prog. Part. Nucl. Phys. **134**, 104080 (2024)
arXiv:2301.13253

Without momentum dependence, “artificial” additional source of repulsion is needed = the extracted EOS is too stiff?



Because of that, the EOS may be also *too soft* at higher densities

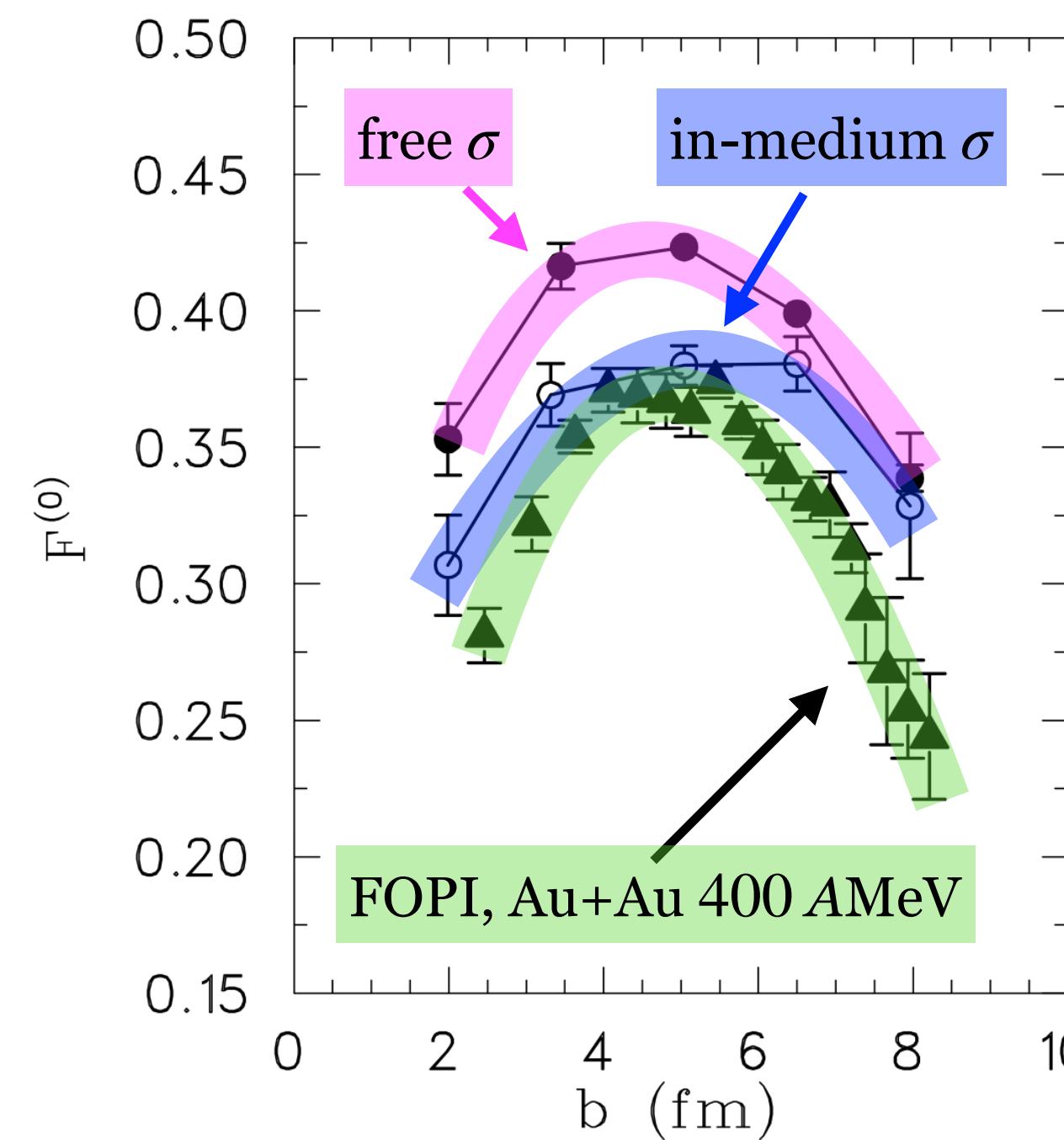
P. Danielewicz, R. Lacey, and W. G. Lynch,
Science **298**, 1592 (2002), arXiv:0208016



Use peripheral collisions to constrain the p -dependence:

In-medium scattering cross-sections

- free nucleon cross sections (σ 's) lead to excessive stopping
- microscopic calculations: N-N σ is reduced in the medium
- isospin dependence of in-medium σ 's generally unknown
- S π RIT experiment data indicate in-medium σ 's need further studies
- particle-particle scatterings contribute $\approx 30\text{-}50\%$ to flow observables

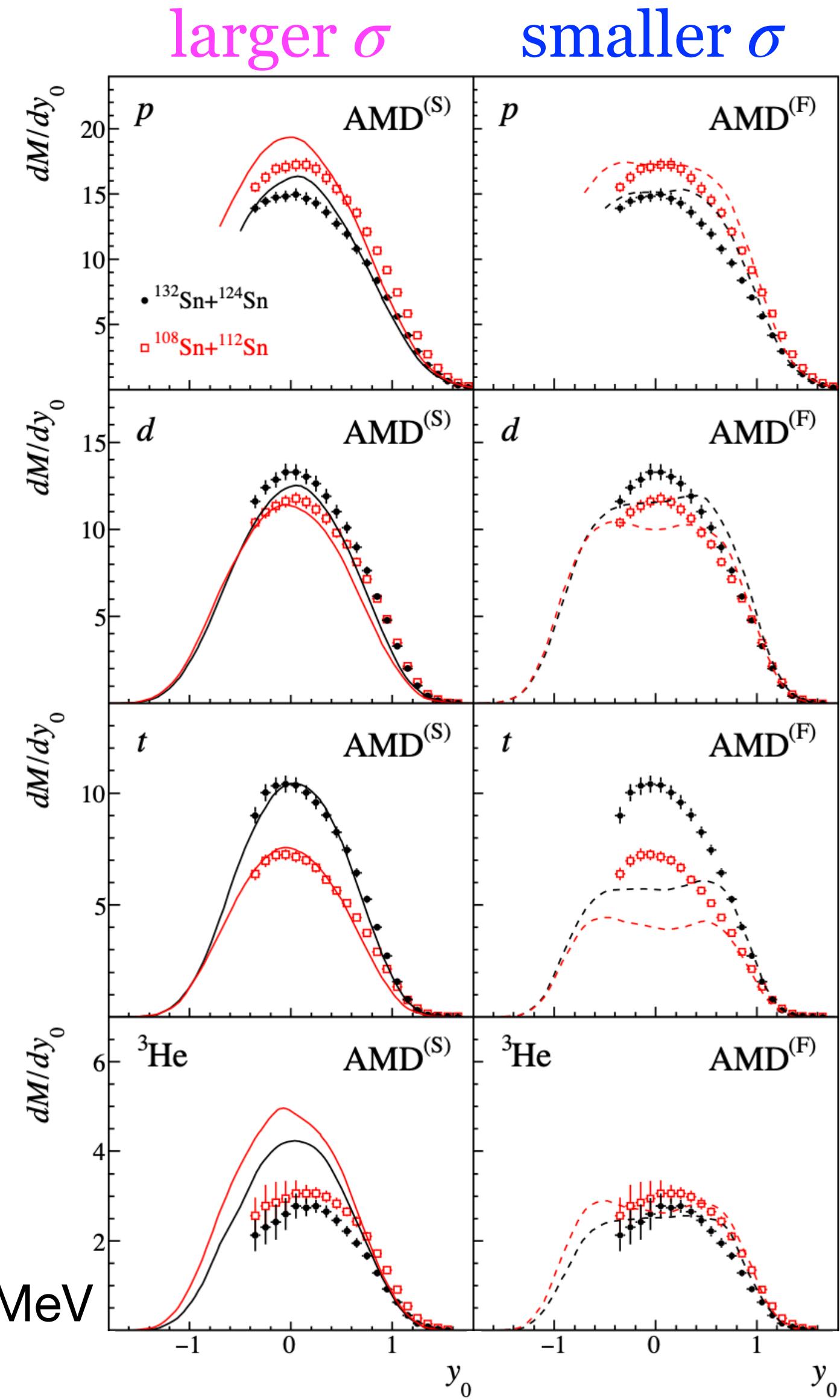


D. Persson, C. Gale, Phys. Rev. C **65**, 064611 (2002), arXiv:nucl-th/0111035

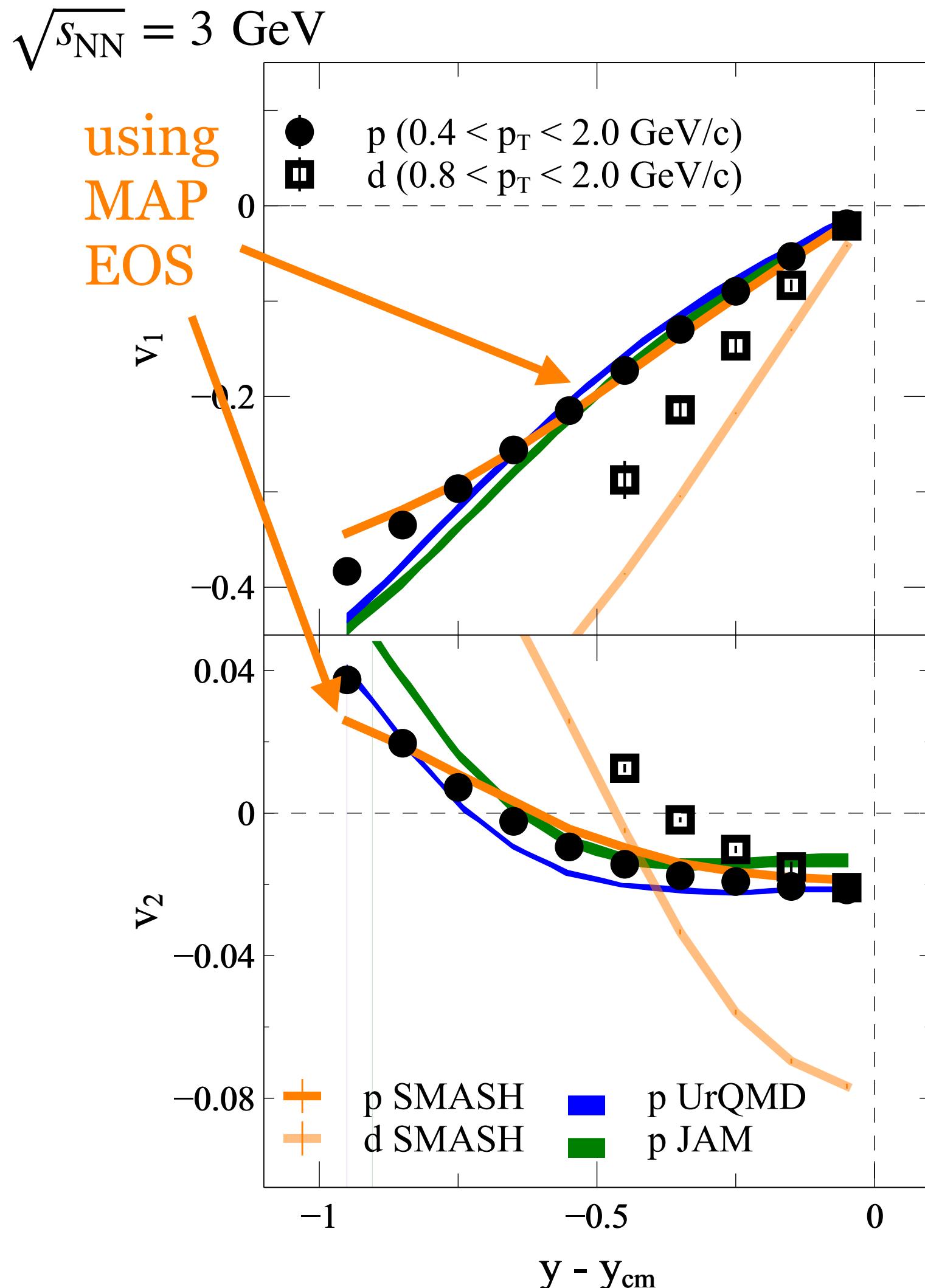
- cross sections and mean-fields should be consistent
- opportunity to collaborate w/ theory, *ab initio* calculations, ...

270 AMeV

J. W. Lee et al. (SpiRIT), Eur. Phys. J. A **58**, 201 (2022), arXiv:2211.02837

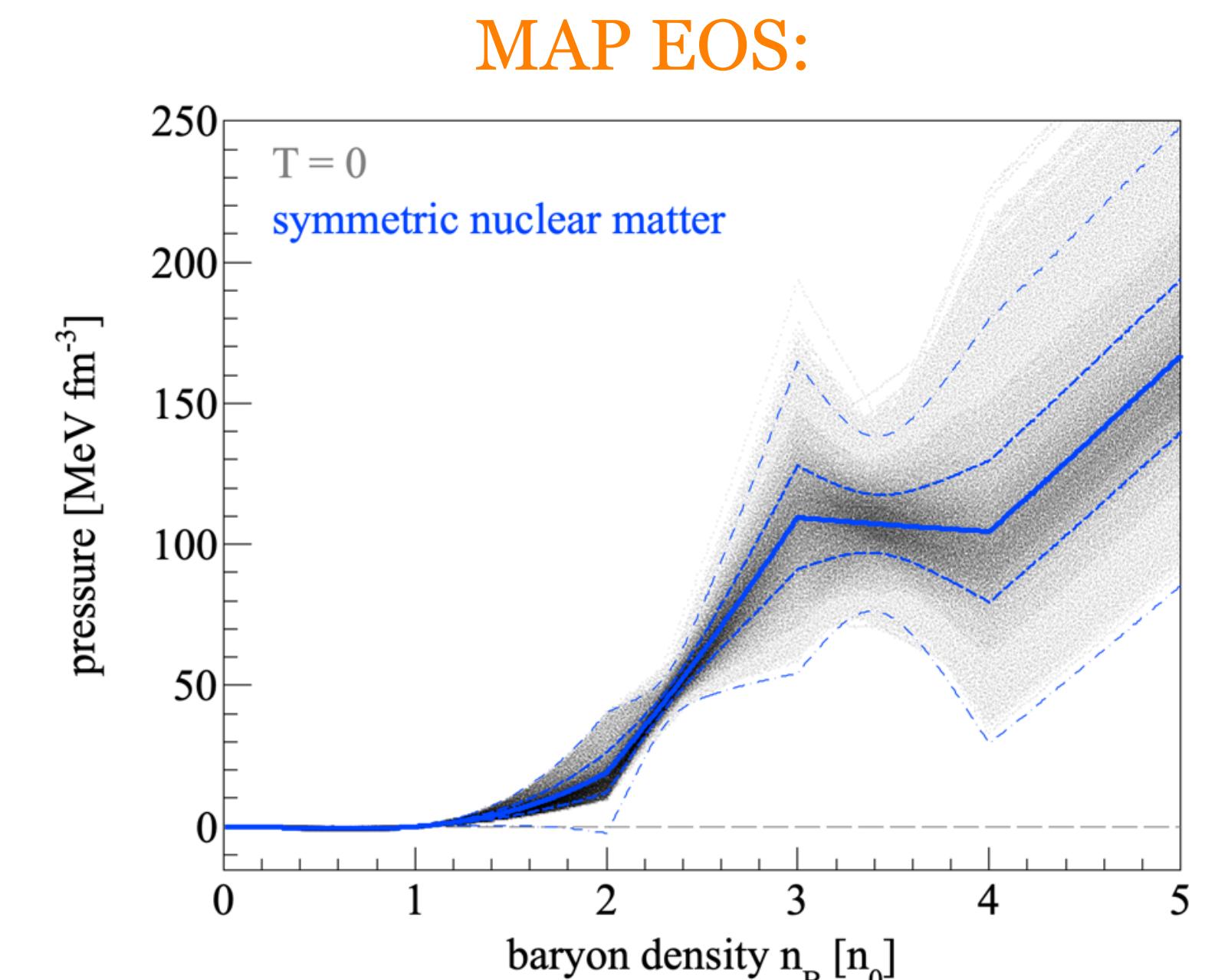


Cluster production



Description of light cluster production needed:

- coalescence/clustering: doesn't take into account the dynamic role of light clusters throughout the evolution
- dynamic nucleon/pion catalysis: consider as separate degrees of freedom, produced through N or π collisions
- dynamical production through potentials???

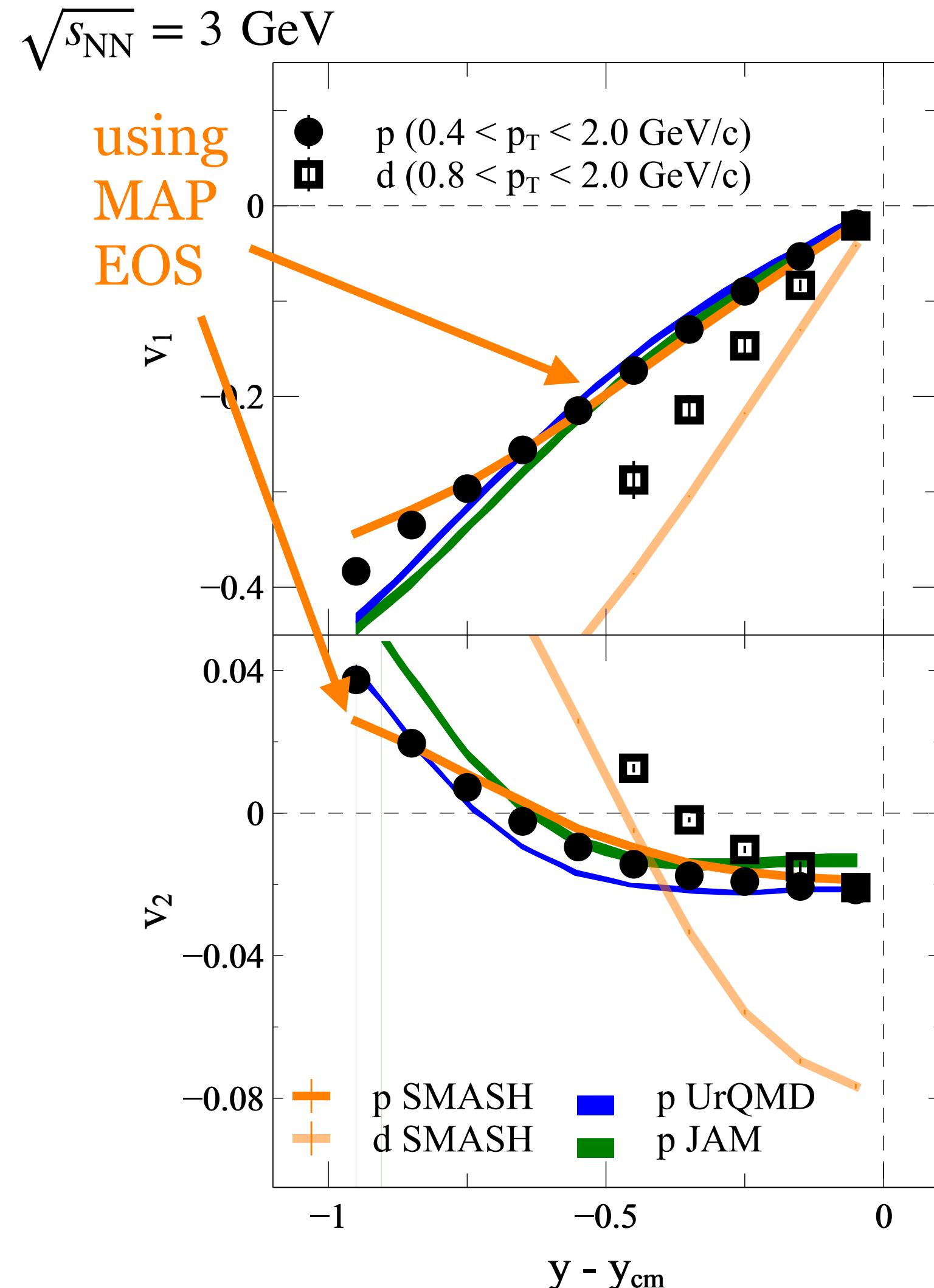


STAR, Phys. Lett. B **827**, 137003 (2022), arXiv:2108.00908

D. Oliinychenko, A. Sorensen, V. Koch, L. McLerran, Phys. Rev. C **108**, 3, 034908 (2023), arXiv:2208.11996

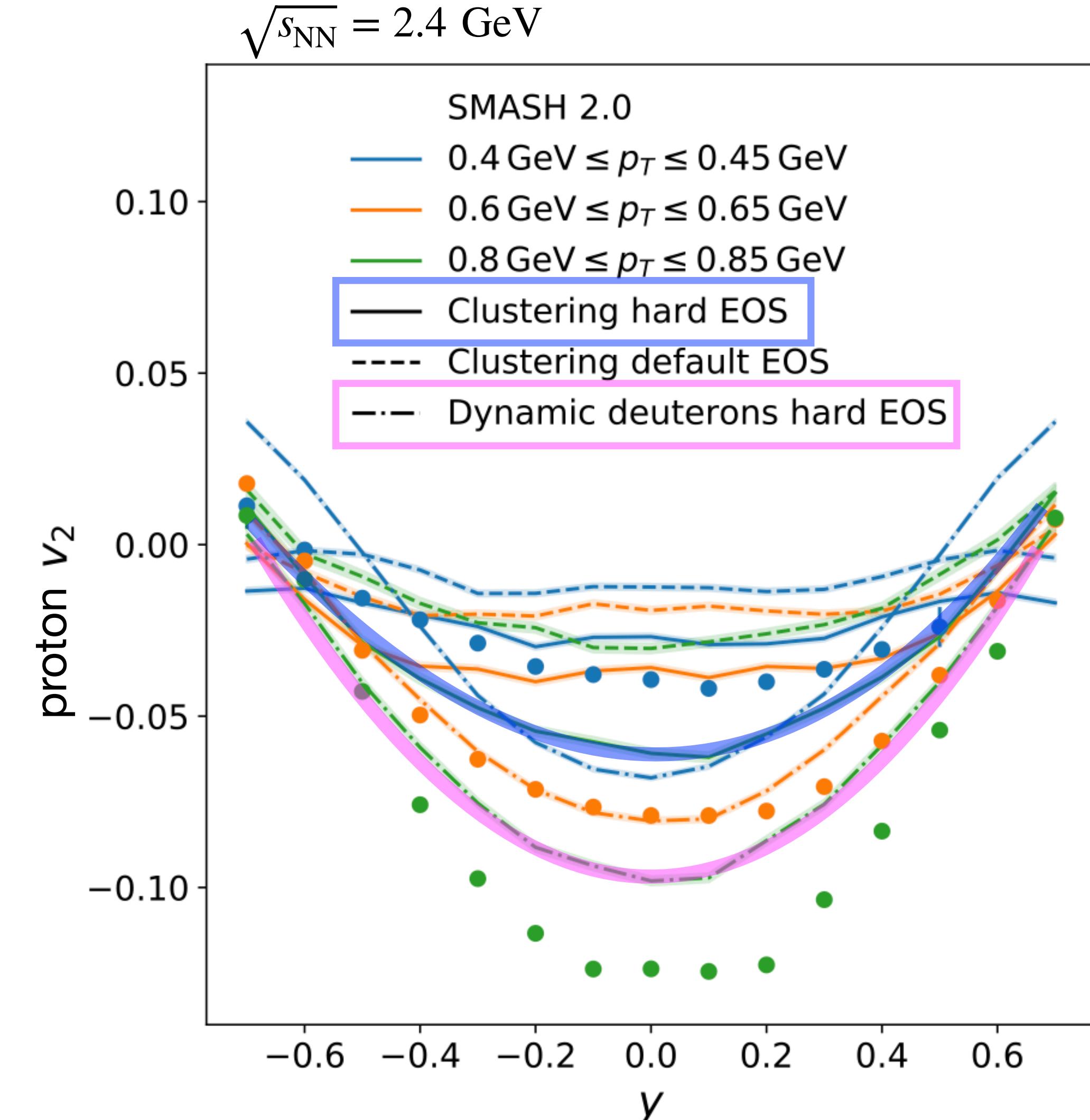
A. Sorensen et al., Prog. Part. Nucl. Phys. **134**, 104080 (2024), arXiv:2301.13253

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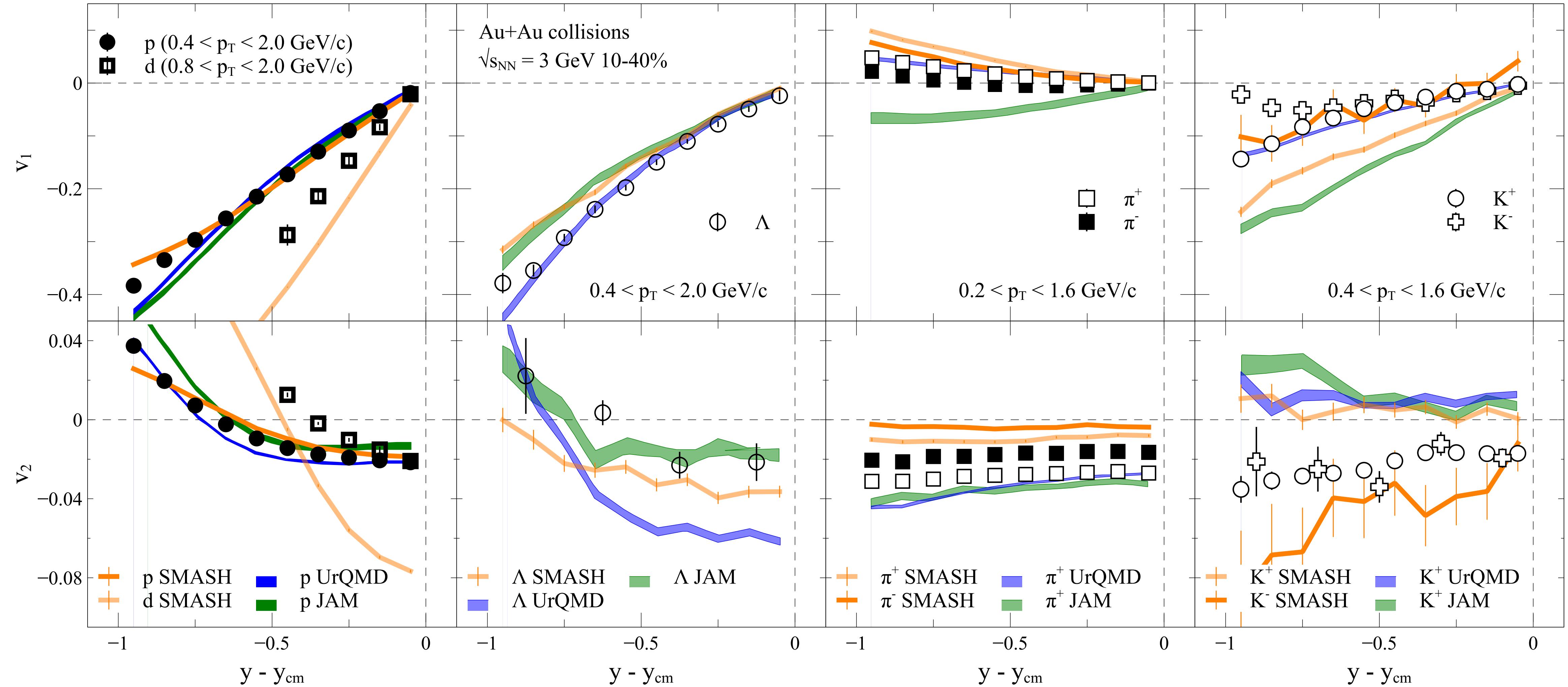
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A. Sorensen et al., Prog. Part. Nucl. Phys. **134**, 104080 (2024), arXiv:2301.13253

J. Mohs, M. Ege, H. Elfner, M. Mayer, Phys. Rev. C **105** 3, 034906 (2022), arXiv:2012.11454

Describing proton flow is not enough

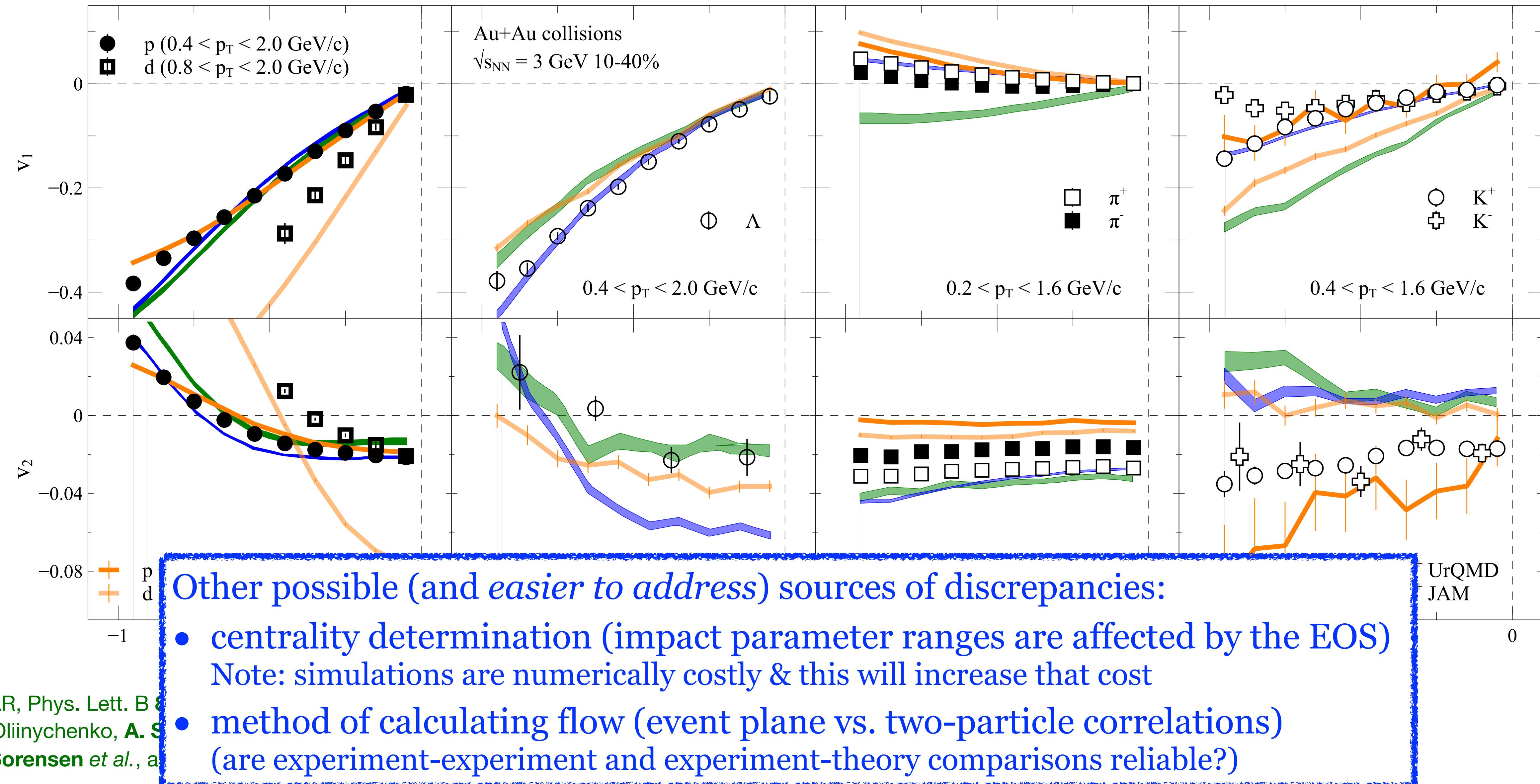


STAR, Phys. Lett. B 827, 137003 (2022) arXiv:2108.00908

D. Oliinychenko, A. Sorensen, V. Koch, L. McLerran, Phys. Rev. C 108, 3, 034908 (2023), arXiv:2208.11996

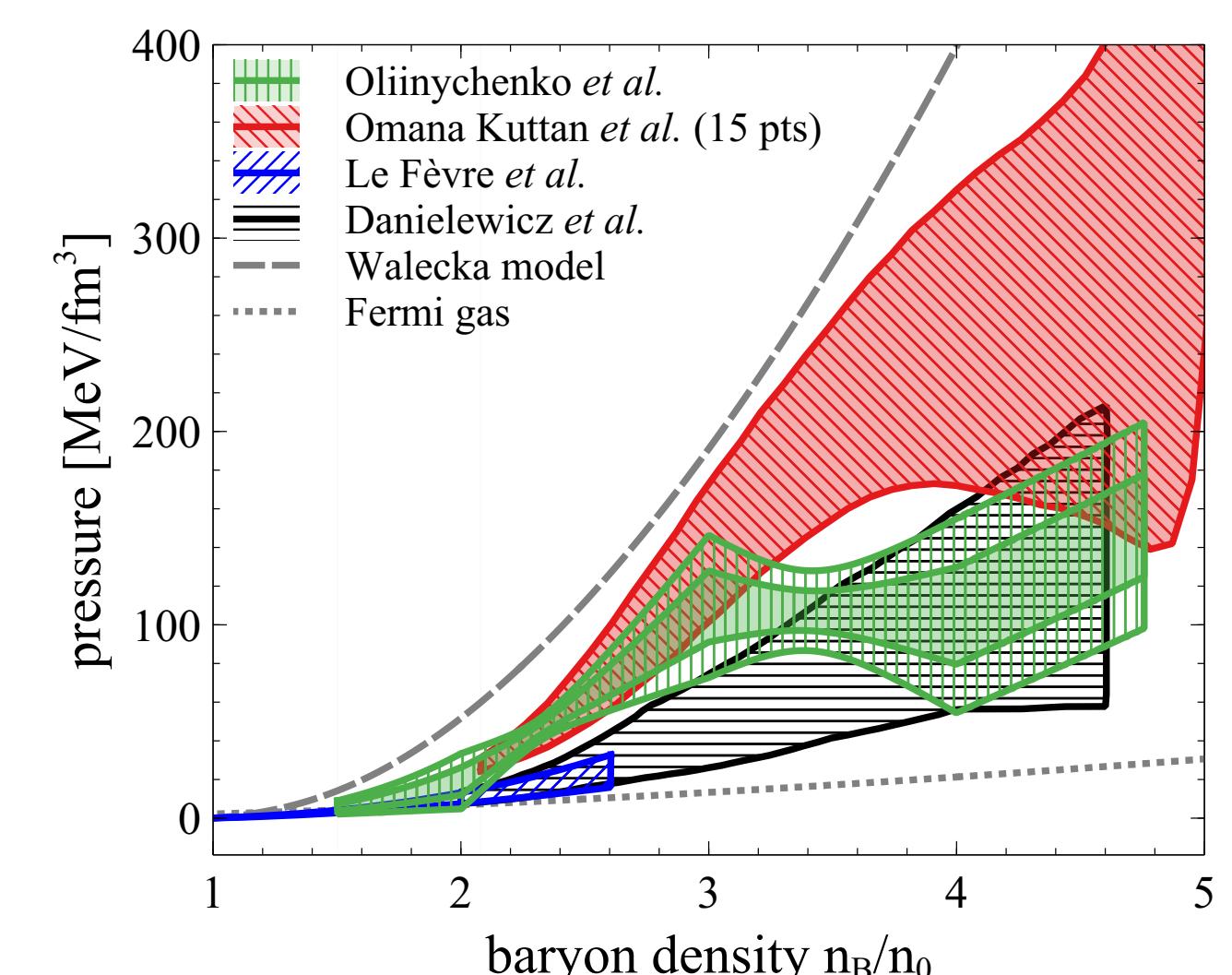
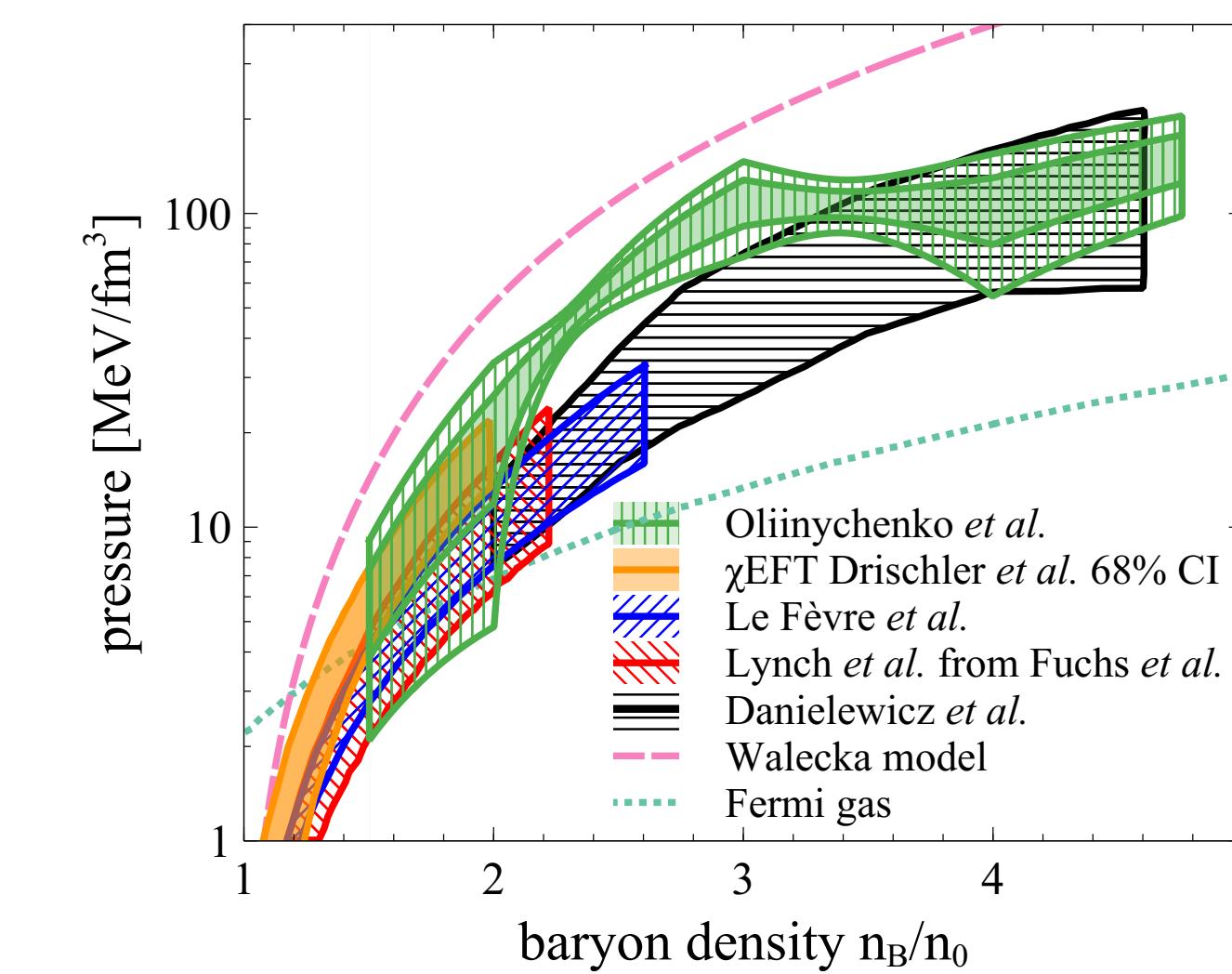
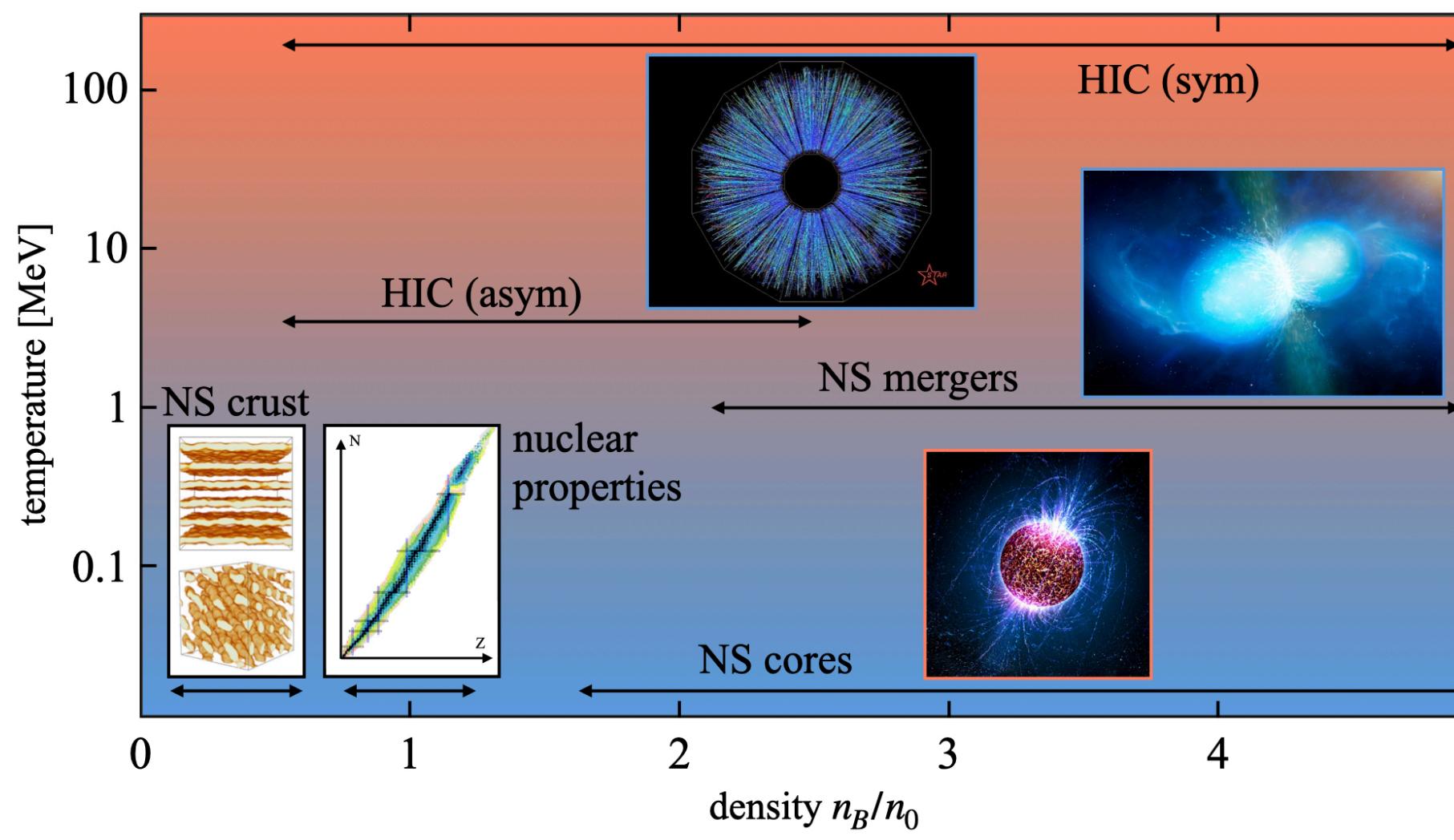
A. Sorensen et al., arXiv:2301.13253, to appear in JPPNP

Describing proton flow is not enough



Summary

- Description of heavy-ion collisions at low energies constrains multiple **fundamental properties of nuclear matter**:
 - density, isospin, and momentum dependence of nuclear interactions
 - in-medium cross sections
 - cluster production mechanisms
 - ...
- Needed for interpreting low- \sqrt{s}_{NN} experiments (**STAR FXT, HADES, FRIB, CBM, FRIB400**)



Open questions

- How to reconcile various effects affecting the extraction of the EOS?
(momentum dependence, in-medium cross sections, cluster production...)
Can we move away from phenomenology and toward clear guidance from theory?

Some ideas in

[A. Sorensen et al., Prog. Part. Nucl. Phys. **134**, 104080 \(2024\)](#)
[arXiv:2301.13253](#)

Dense Nuclear Matter Equation of State from Heavy-Ion Collisions *

Agnieszka Sorensen¹, Kshitij Agarwal², Kyle W. Brown^{3,4}, Zbigniew Chajecki⁵,
Paweł Danielewicz^{3,6}, Christian Drischler⁷, Stefano Gandolfi⁸, Jeremy W. Holt^{9,10},
Matthias Kaminski¹¹, Che-Ming Ko^{9,10}, Rohit Kumar³, Bao-An Li¹², William G. Lynch^{3,6},
Alan B. McIntosh¹⁰, William G. Newton¹², Scott Pratt^{3,6}, Oleh Savchuk^{3,13}, Maria Stefaniak¹⁴,
Ingo Tews⁸, ManYee Betty Tsang^{3,6}, Ramona Vogt^{15,16}, Hermann Wolter¹⁷, Hanna Zbroszczyk¹⁸

- What are the limits of microscopic transport?
(dense systems, change of degrees of freedom, short-range correlations, etc.)
- Besides the extraction of the EOS, how can low energy studies / transport inform other sub-fields in nuclear physics? (e.g., strangeness interactions important for physics of neutron stars)
- Could any of that be of use for physics at the EIC?