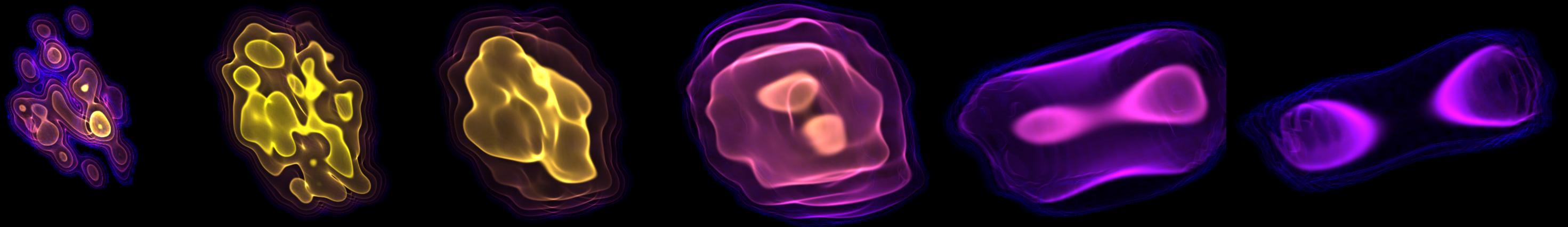




# 3D MODELING FOR THE RHIC ISOBAR COLLISIONS

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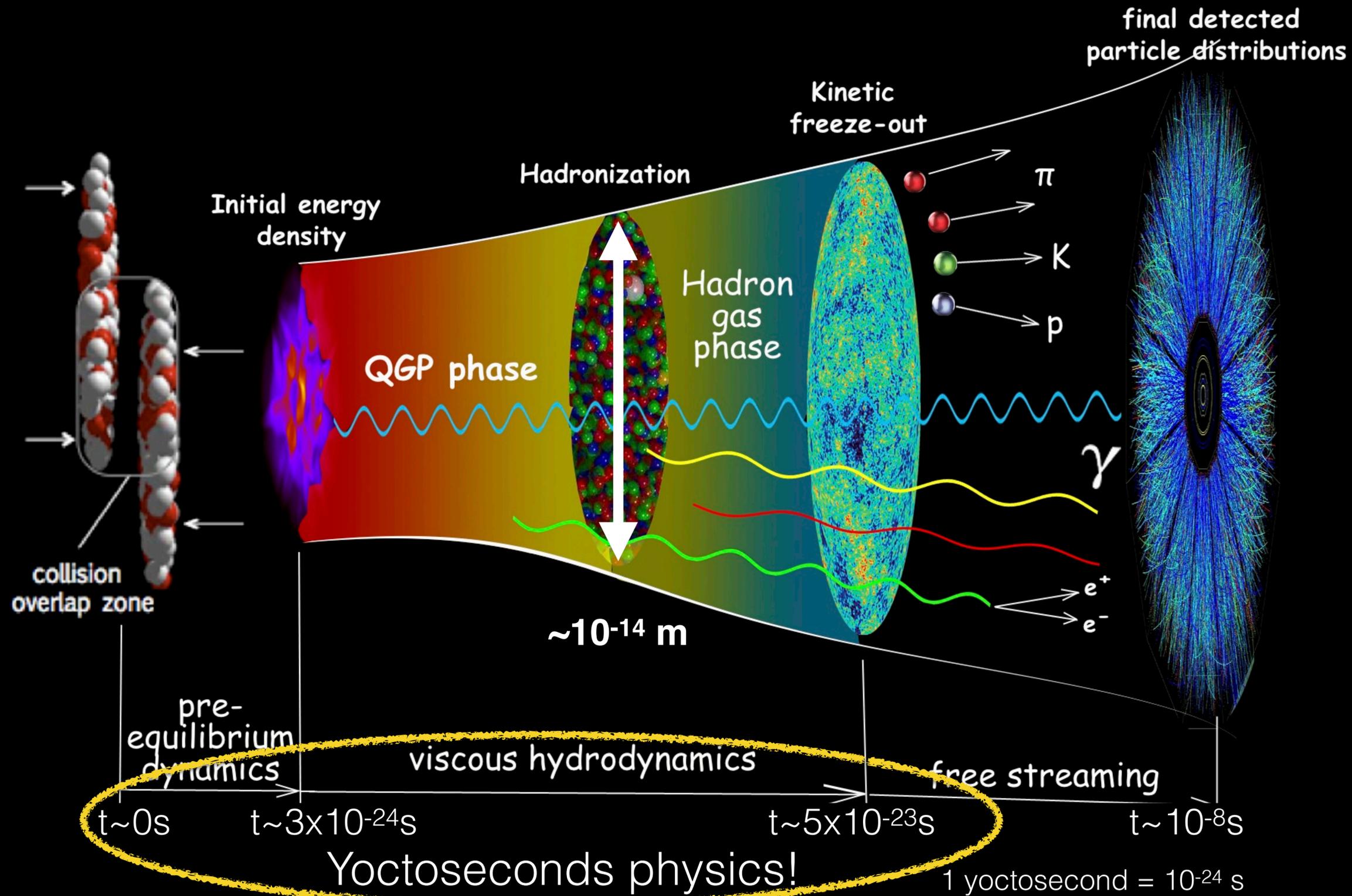
CHUN SHEN



Intersection of nuclear structure and  
high-energy nuclear collisions

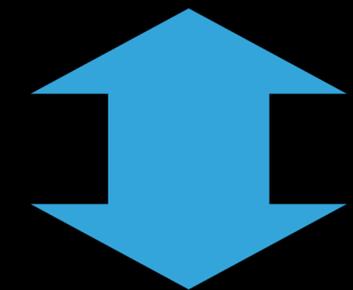
Feb. 17, 2023

# NUCLEAR MATTER UNDER EXTREME CONDITIONS



Heavy-ion collisions are tiny and have ultra-fast dynamics

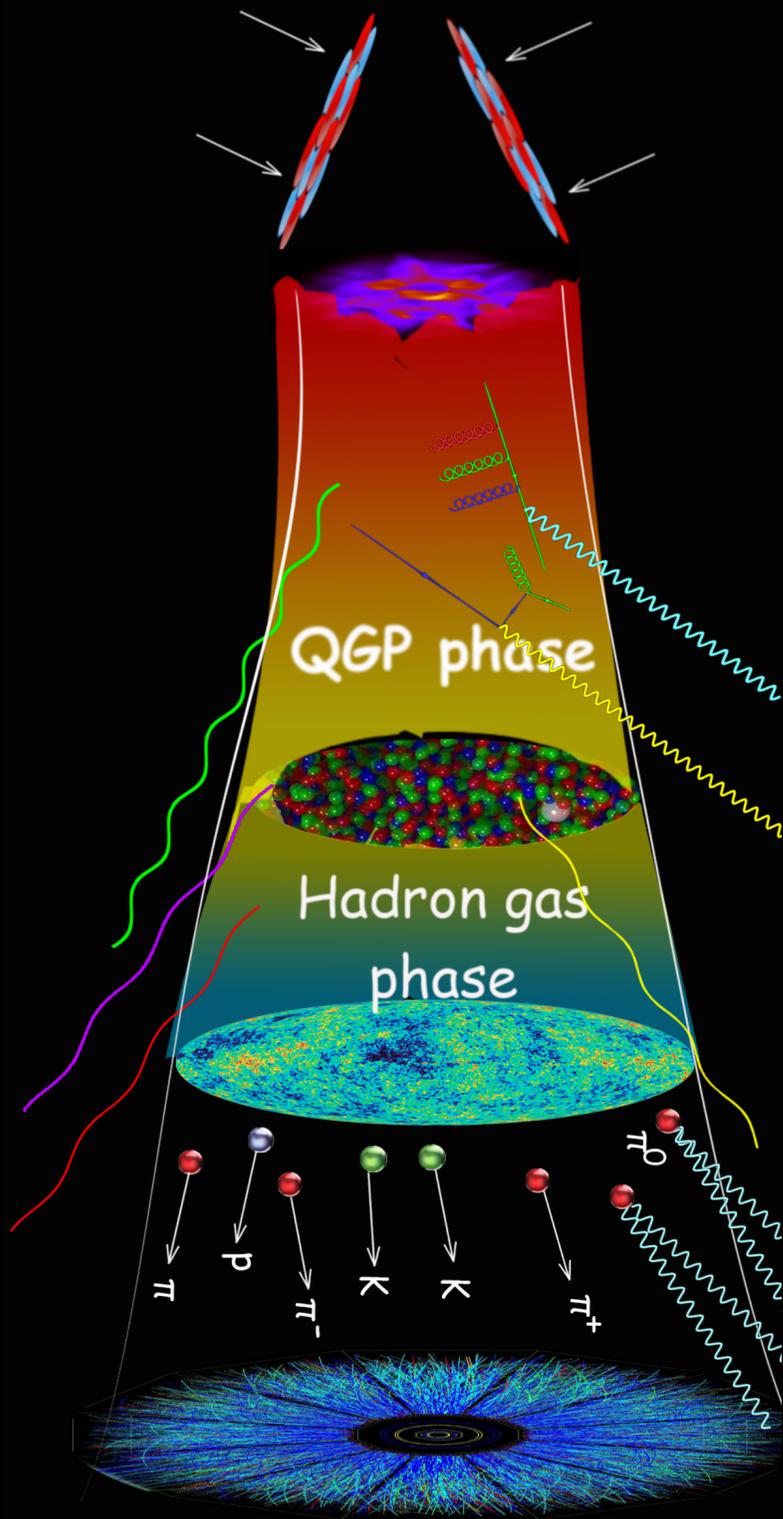
A variety of particles are emitted from the collisions



Multi-messenger nature of heavy-ion physics

# DEFINING THE QUARK-GLUON PLASMA

Which **properties of hot QCD matter** can we determine from relativistic heavy ion data (LHC, RHIC, and future FAIR/NICA/JPAC)?



Equation of State  $T^{\mu\nu} \iff e, P, s$   
 $c_s^2 = \partial P / \partial e|_{s/n}$

Shear and bulk viscosities  
 $\eta/s(T, \mu_B), \zeta/s(T, \mu_B)$

Charge diffusion  $D_B, D_Q, D_S$

Electromagnetic emissivity

Energy-momentum transport  
 $\hat{q}, \hat{e}, \hat{e}_2, \dots$

Spectra, collective flow, femtoscopy

Anisotropic flow  $v_n$   
Flow correlations

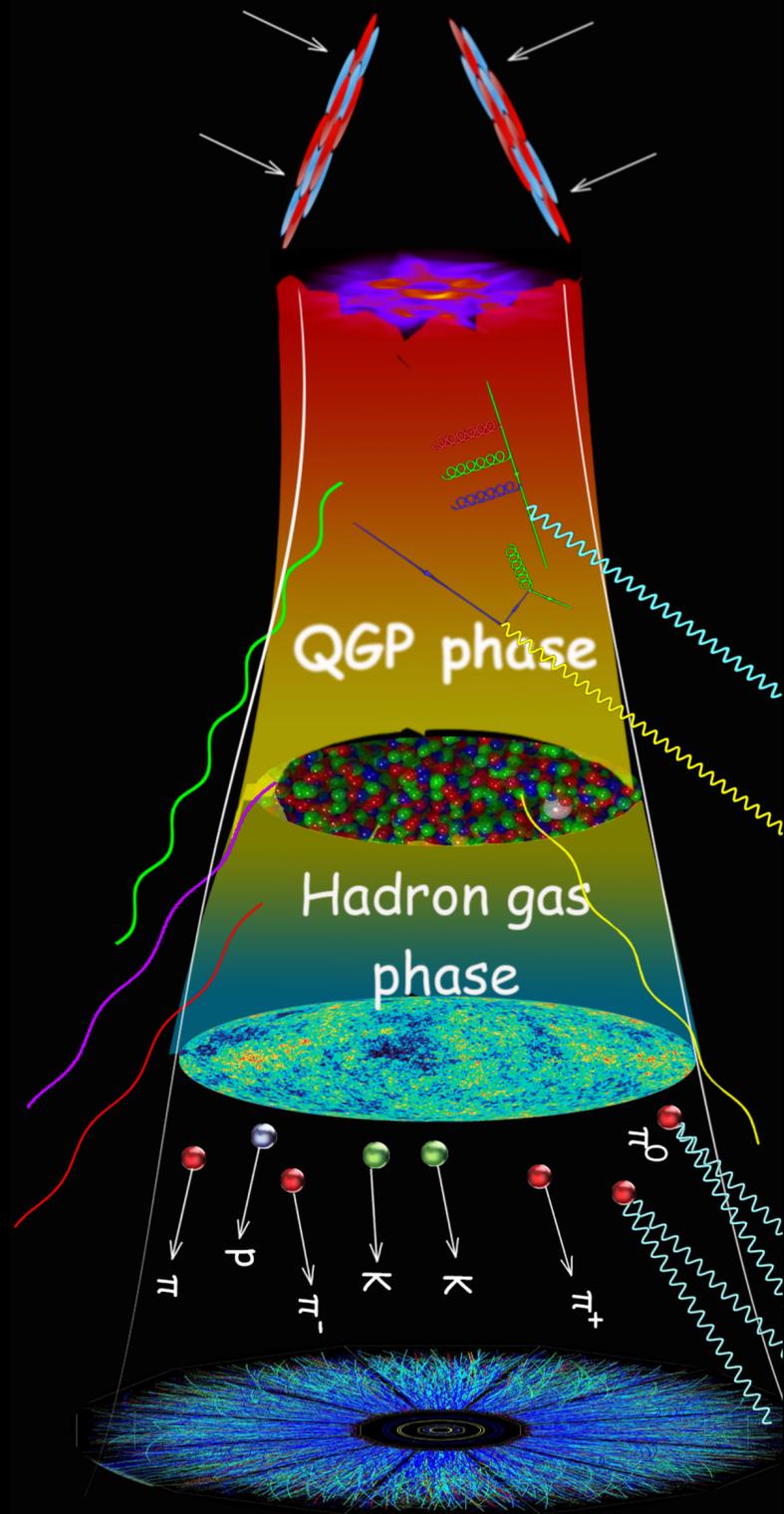
Balance functions

Photons and dileptons

Jets and heavy-quarks

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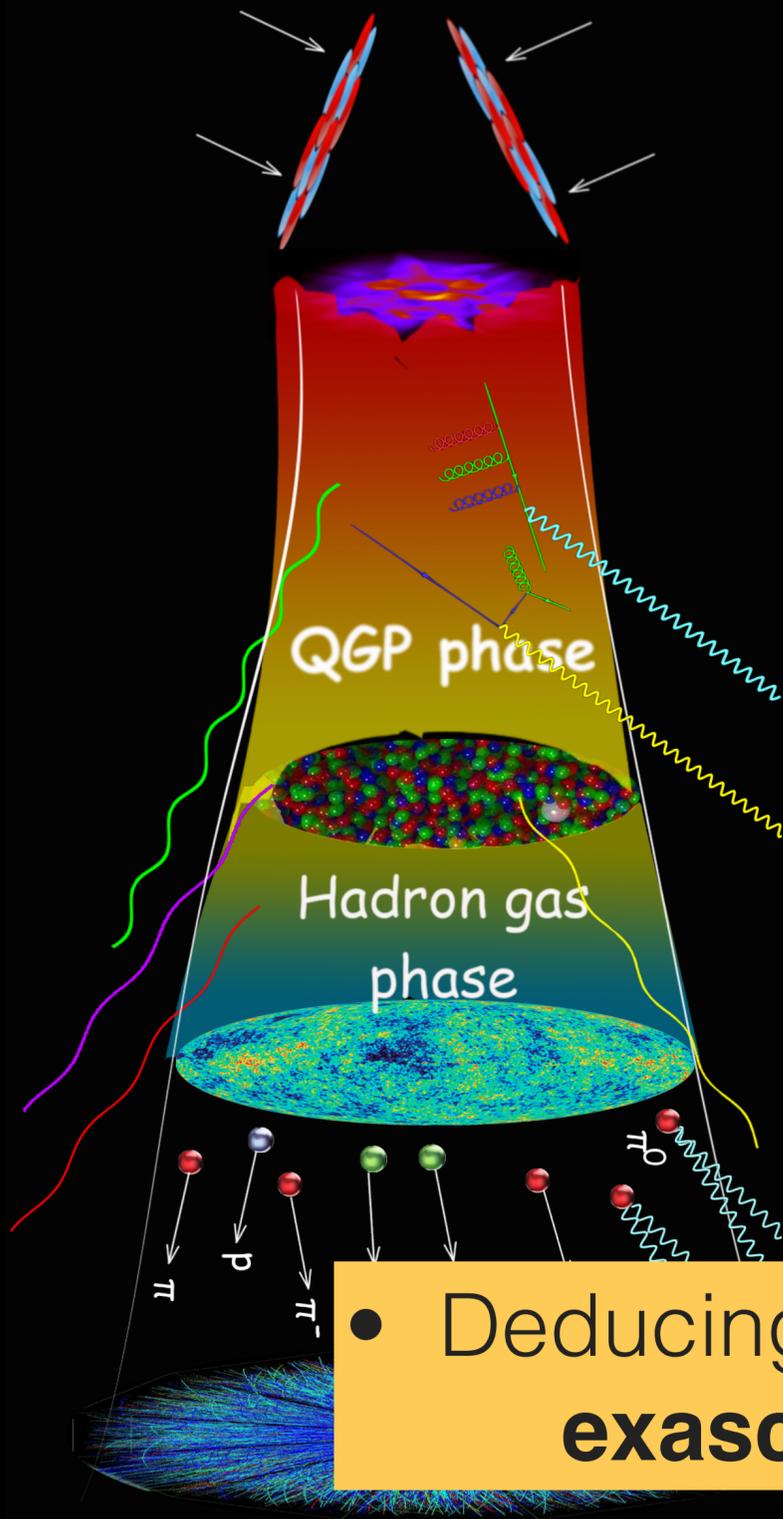
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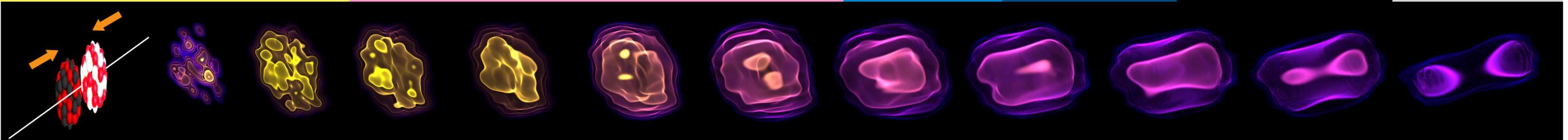
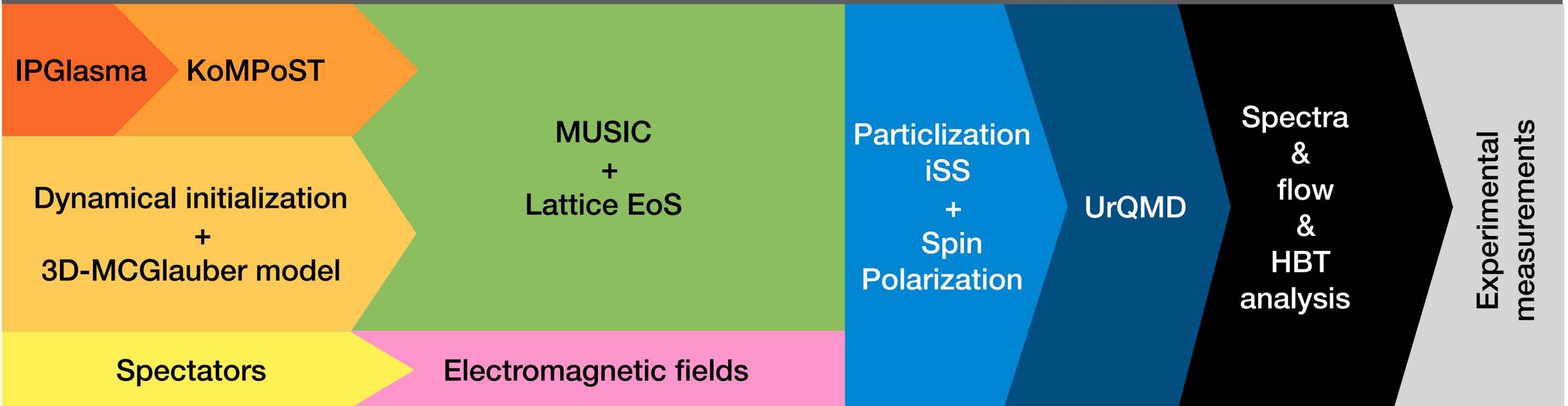
- Deducing the QGP properties from experimental data requires **exascale computing** with advanced statistical methods

quarks

# AN OPEN SOURCE HYBRID FRAMEWORK—IEBE-MUSIC

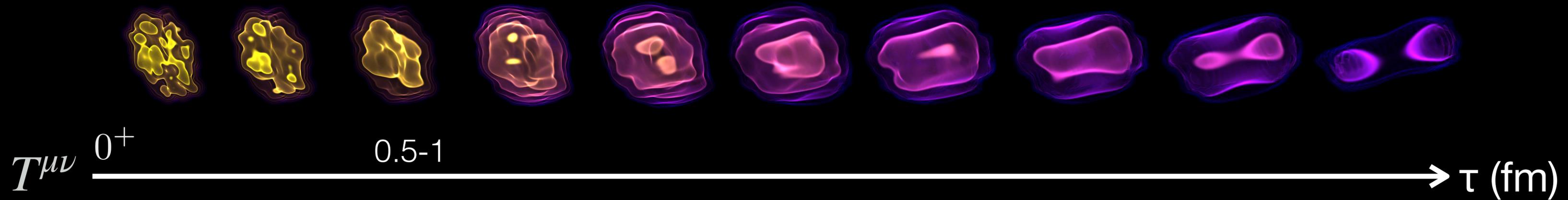
 <https://github.com/chunshen1987/iEBE-MUSIC>

## The iEBE-MUSIC Framework



The **state-of-the-art** event-by-event simulations for relativistic heavy-ion collisions

# THE MULTI-STAGE THEORETICAL FRAMEWORK



Initial State +  
Pre-equilibrium dynamics

Hydrodynamics

Hadronic Transport

$$T^{\mu\nu}_{\text{pre. eq}} = T^{\mu\nu}_{\text{hydro}}$$

+ Landau Matching  
with lattice EoS

Cooper-Frye  
particlization

- Continuously connect the system's energy-momentum tensor  $T^{\mu\nu}$  between different stages

# WHERE WE ARE AND WHERE WE ARE GOING

- Quark-Gluon Plasma is the **hottest**, **smallest**, and the **most perfect** fluid ever created in the laboratory
- A fluid has “close” to the fundamental degrees of freedom

How does the strongly coupled liquid emerge from fundamental QCD interactions?

- Probes the inner working of QGP at multi-resolution scales with jets and heavy-quarks
- What is the smallest possible droplet of QGP?
- What is the structure of QCD phase diagram?

# WHERE WE ARE AND WHERE WE ARE GOING

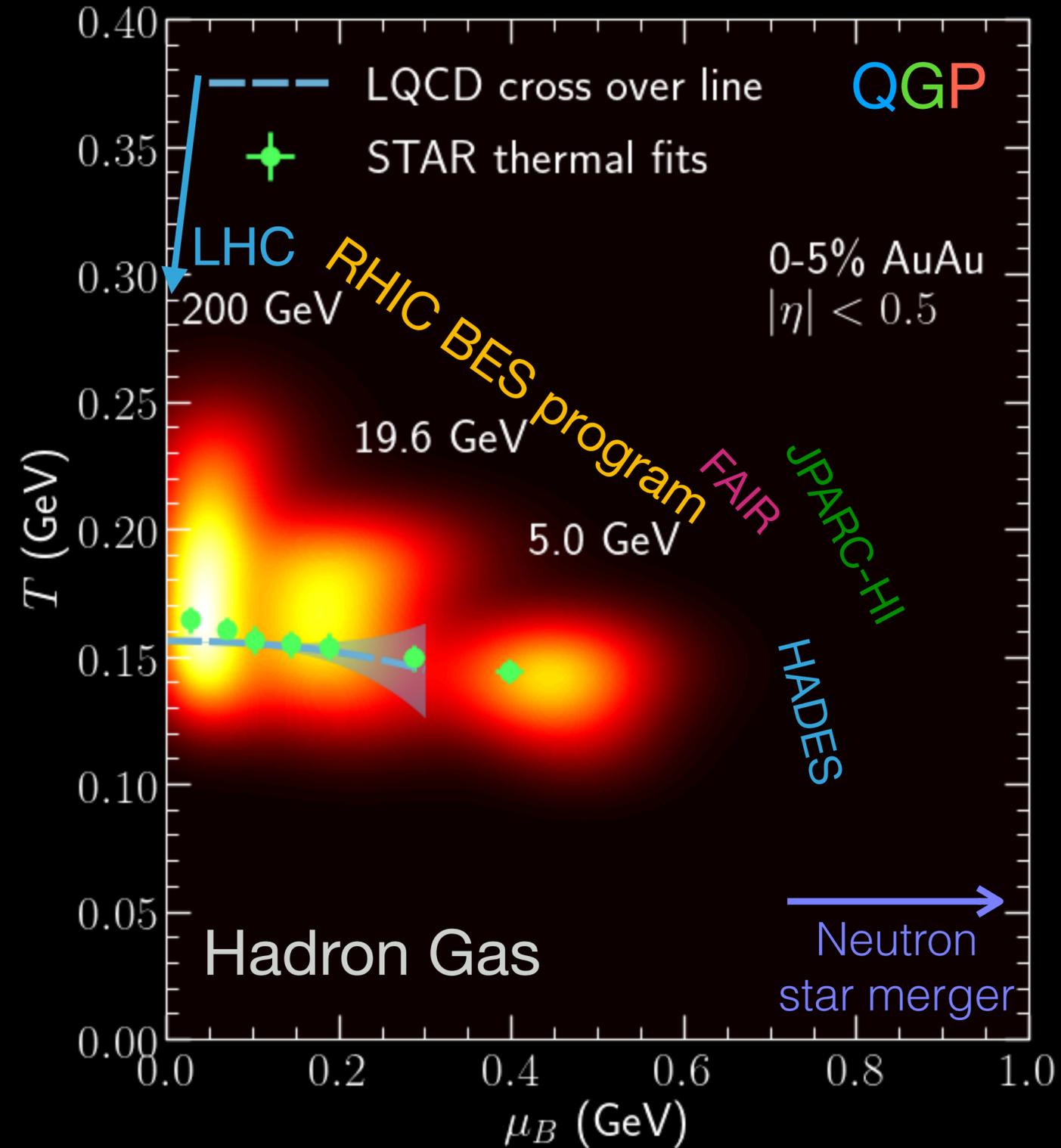
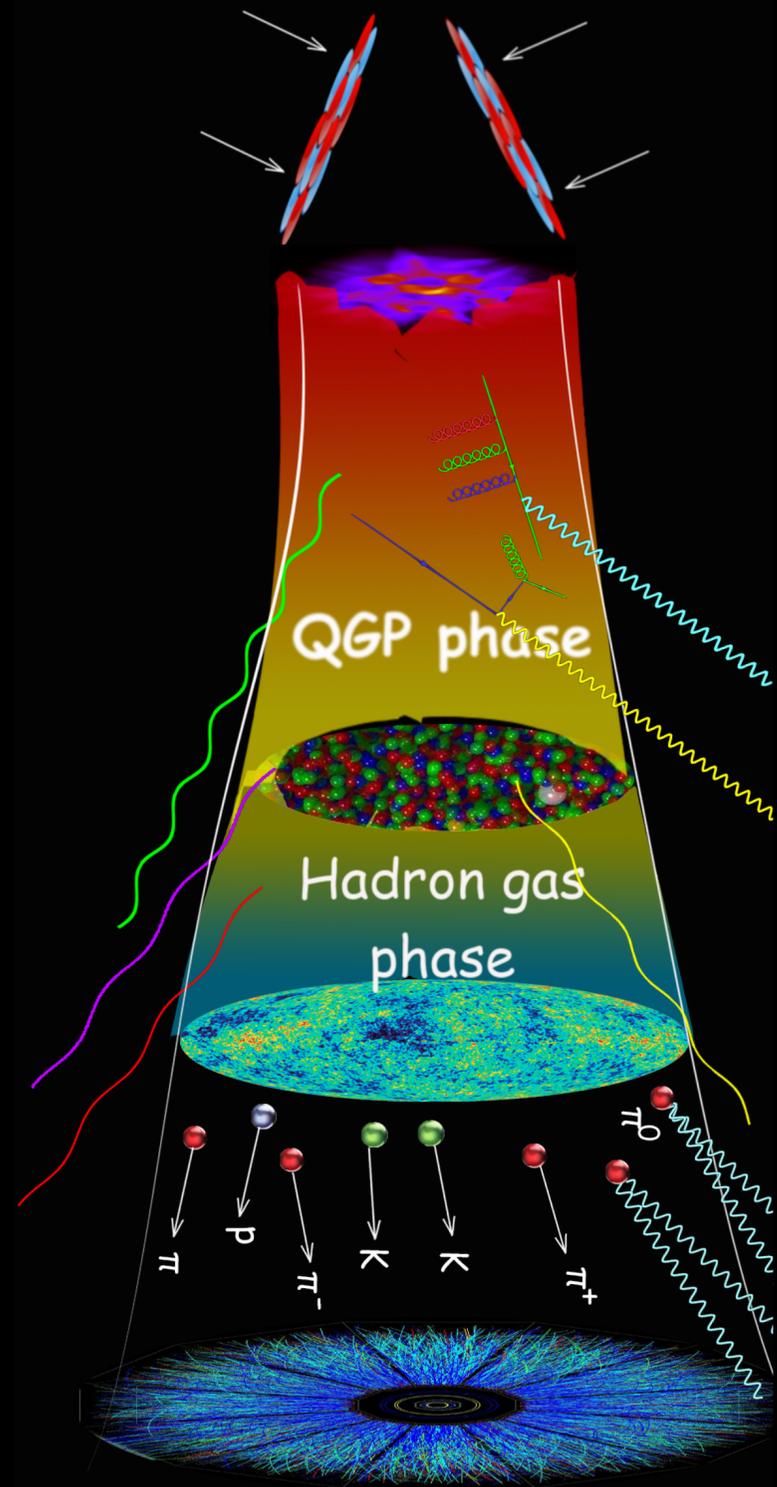
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*3D simulations are essential!*

# PROBING THE NUCLEAR MATTER PHASE DIAGRAM



- Search for a critical point & 1st order phase transition

$$c_s^2(T, \{\mu_q\})$$

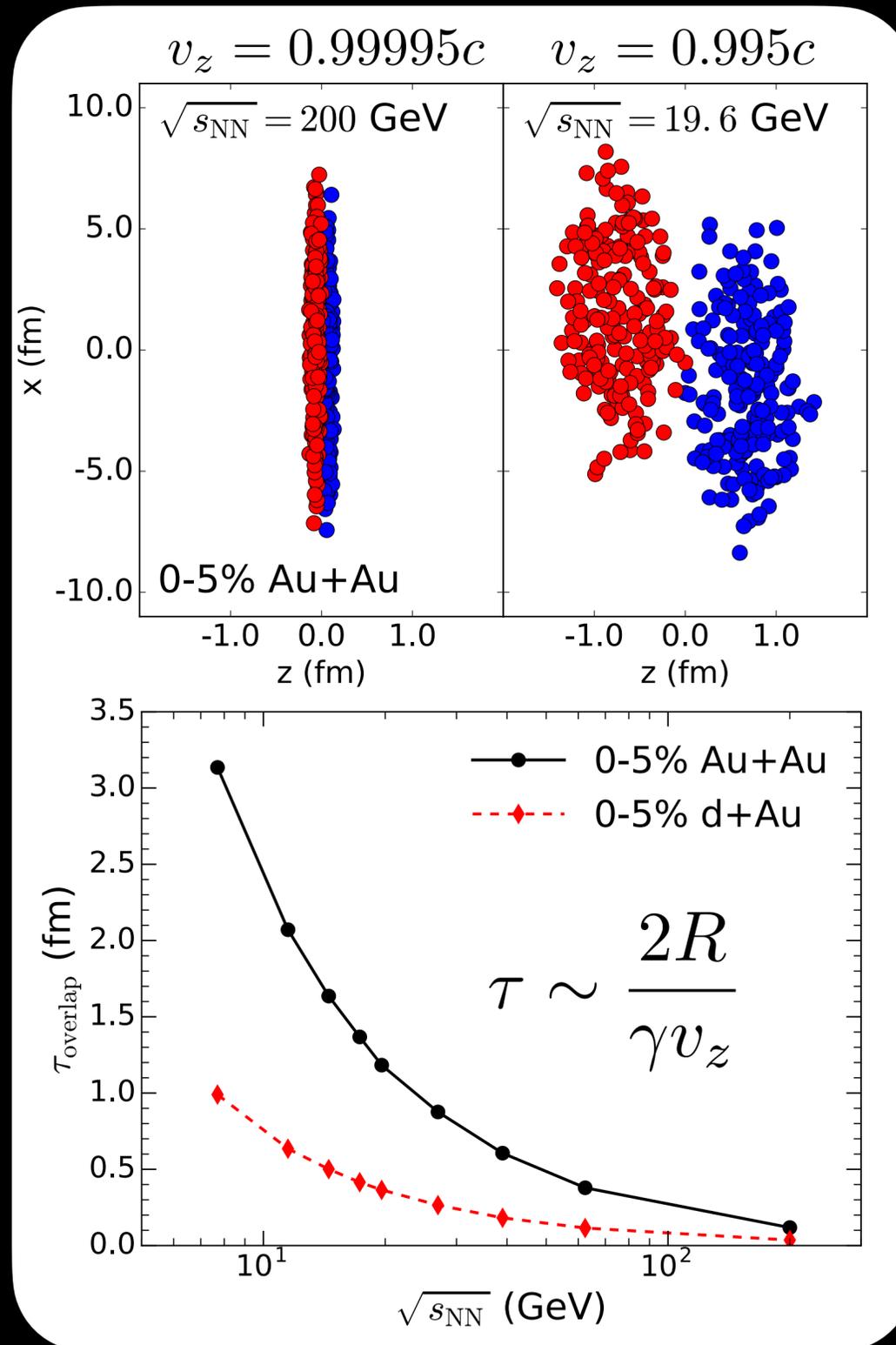
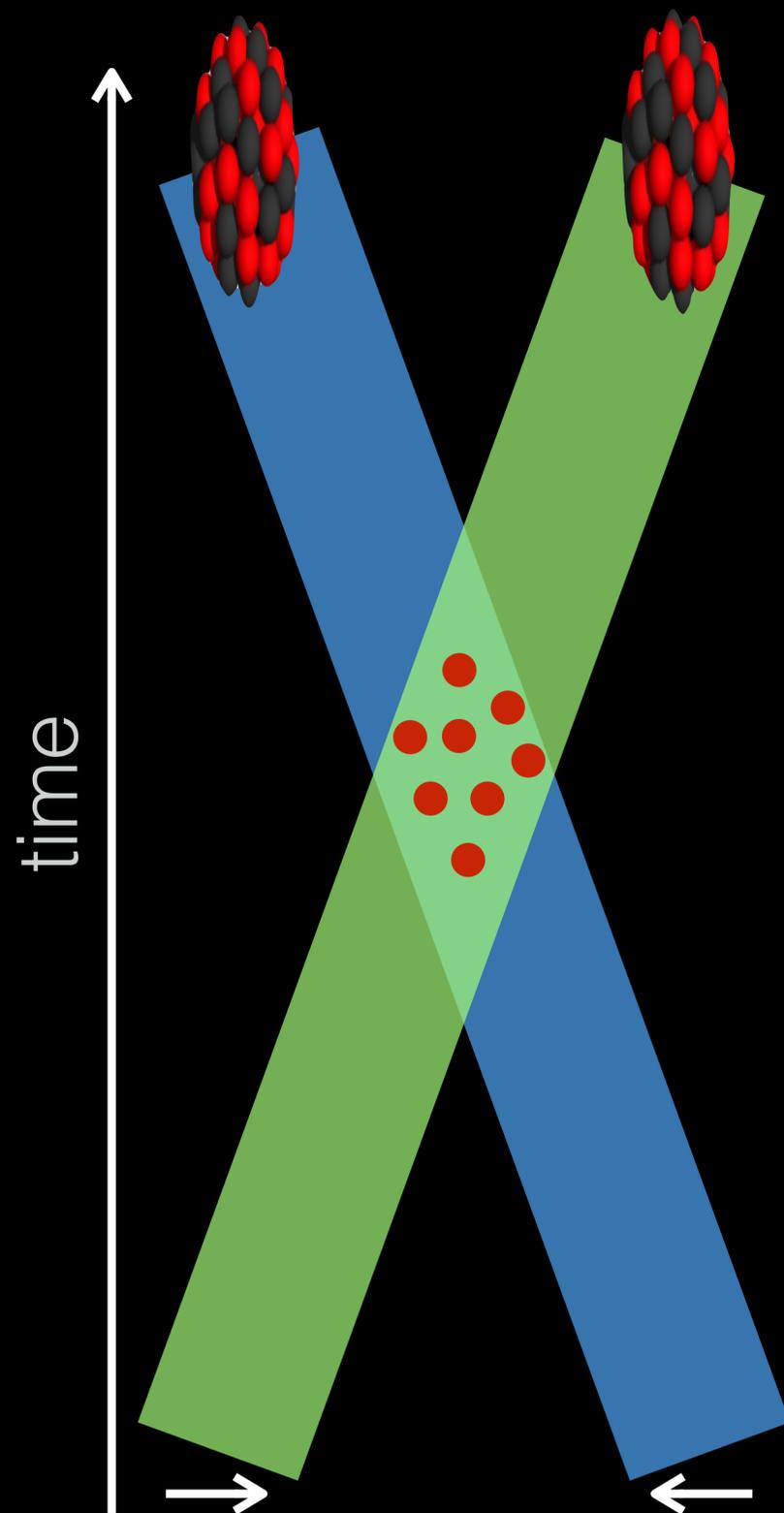
- How do the QGP transport properties change with baryon doping?

$$(\eta/s)(T, \{\mu_q\}), (\zeta/s)(T, \{\mu_q\})$$

- Access to new transport phenomena

*Charge diffusion*

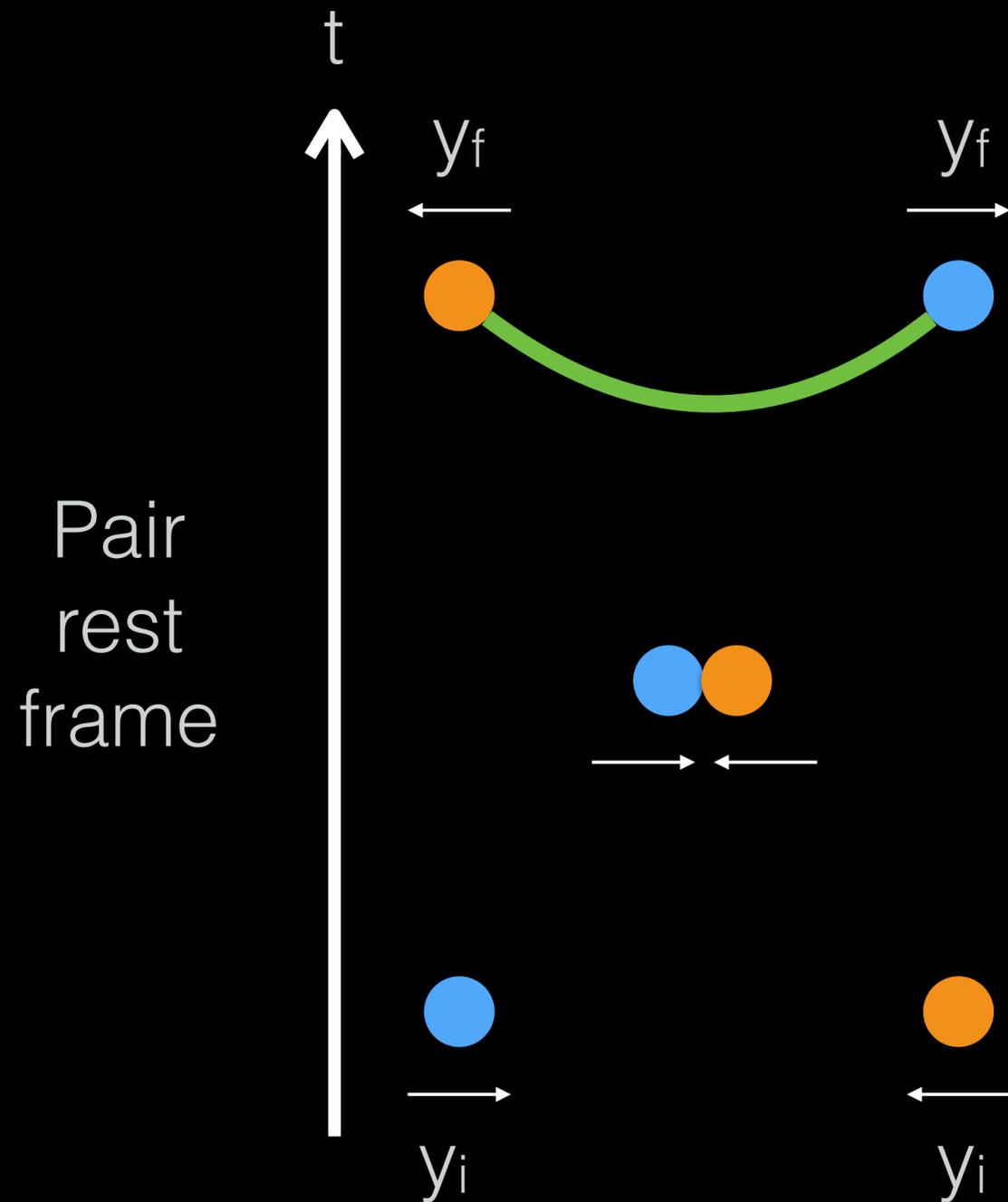
# 3D DYNAMICS BEYOND THE BJORKEN PARADIGM



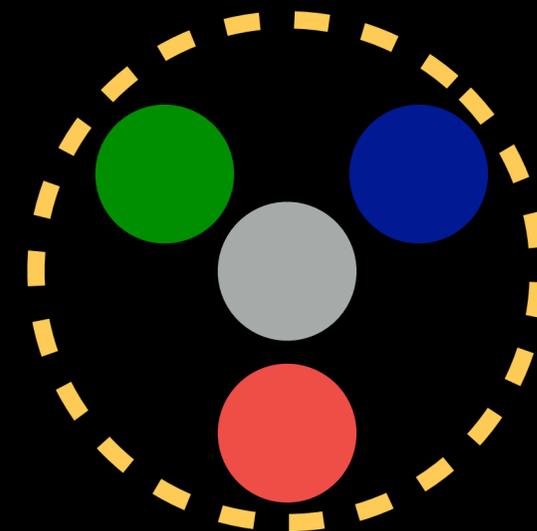
- Geometry-Based initial conditions  
[C. Shen and S. Alzhirani, Phys. Rev. C 102, 014909 \(2020\)](#)
- Classical string-based initial conditions  
[A. Bialas, A. Bzdak and V. Koch, Acta Phys. Polon. B49 \(2018\)](#)  
[C. Shen and B. Schenke, Phys.Rev. C97 \(2018\) 024907](#)
- Transport model based initial conditions  
[Phys. Rev. C91 \(2015\) 064901](#)  
[Nucl. Phys. A982 \(2019\) 407-410](#)  
[Eur. Phys. J. A 58, no.11, 230 \(2022\)](#)  
[arXiv:2301.11894 \[nucl-th\]](#)
- Color Glass Condensate based models  
[M. Li and J. Kapusta, Phys. Rev. C 99, 014906 \(2019\)](#)  
[L. D. McLerran, S. Schlichting and S. Sen, Phys. Rev. D 99, 074009 \(2019\)](#)  
[M. Martinez, M. D. Sievert, D. E. Wertepny and J. Noronha-Hostler, Phys. Rev. C105, 034908 \(2022\)](#)
- Holographic approach at intermediate coupling  
[M. Attems, et al., Phys.Rev.Lett. 121 \(2018\), 261601](#)

# THE 3D MC-GLAUBER + STRING MODEL

C. Shen and B. Schenke, Phys.Rev. C97 024907 (2018)  
C. Shen and B. Schenke, Phys. Rev. C 105, 064905 (2022)



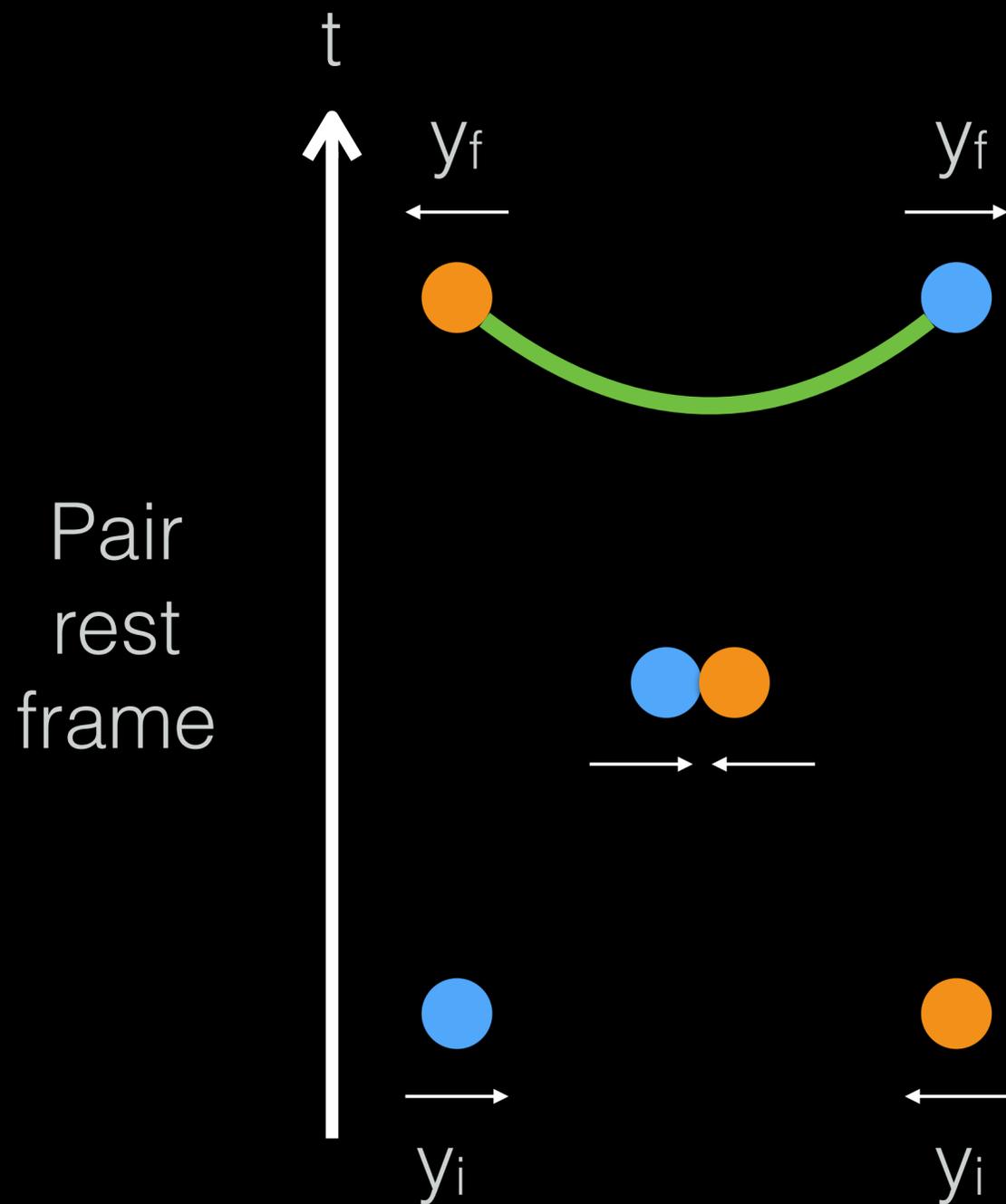
- Collision geometry is determined by MC-Glauber model
- Hot spots associated with valence quarks are sampled from PDF + a soft partonic cloud carrying the rest small  $x$  partons
- Hot spots are randomly picked to lose energy during a collision



# THE 3D MC-GLAUBER + STRING MODEL

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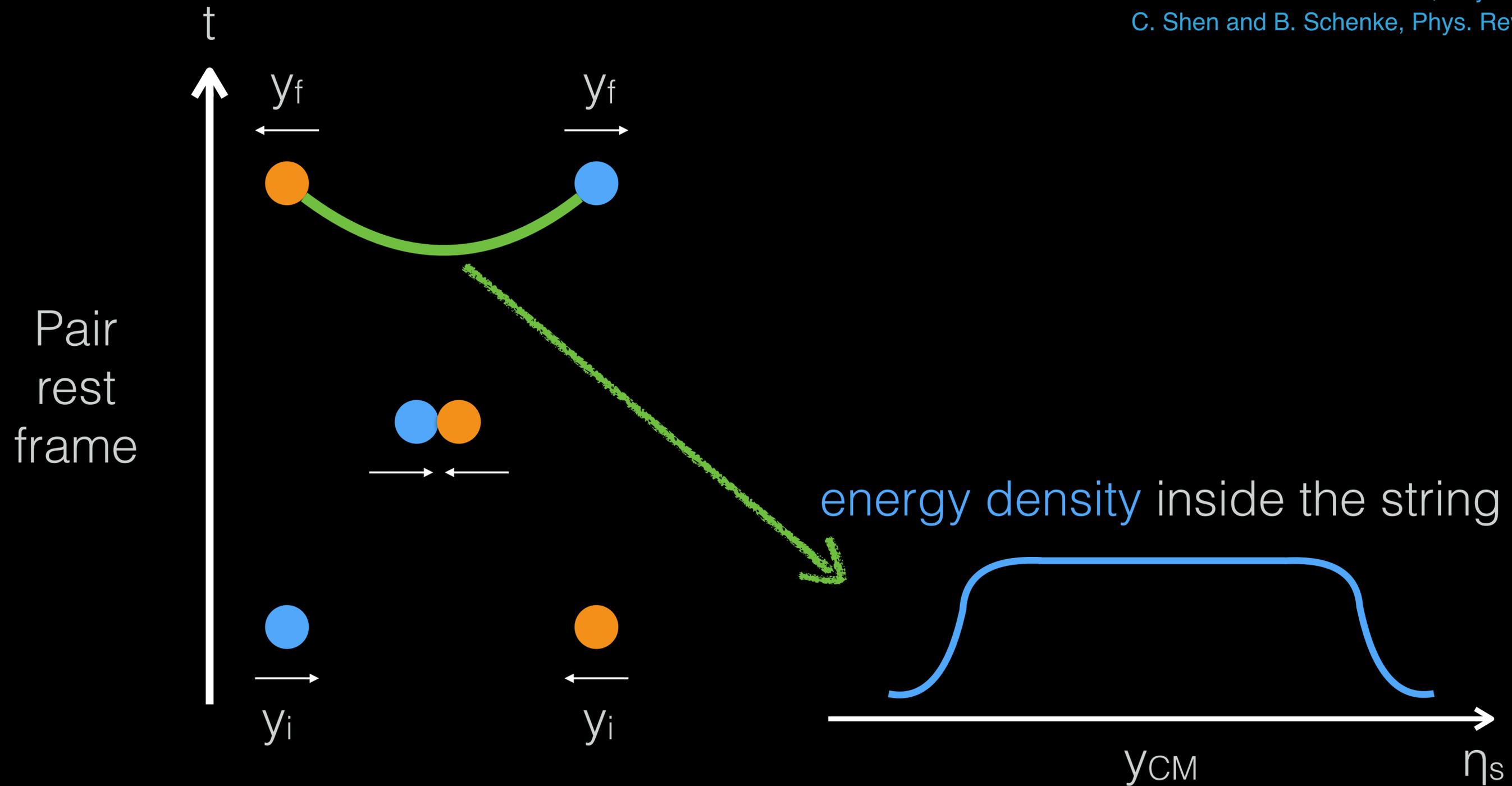
- Collision geometry is determined by MC-Glauber model
- Hot spots are sampled and randomly picked to lose energy during a collision
- Incoming quarks are decelerated with a classical string tension,

$$dp^\mu = -T^{\mu\nu}d\Sigma_\nu$$

$$T^{\mu\nu} = \begin{pmatrix} \sigma & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\sigma \end{pmatrix} \quad d\Sigma_\nu = (dz, 0, 0, -dt)$$

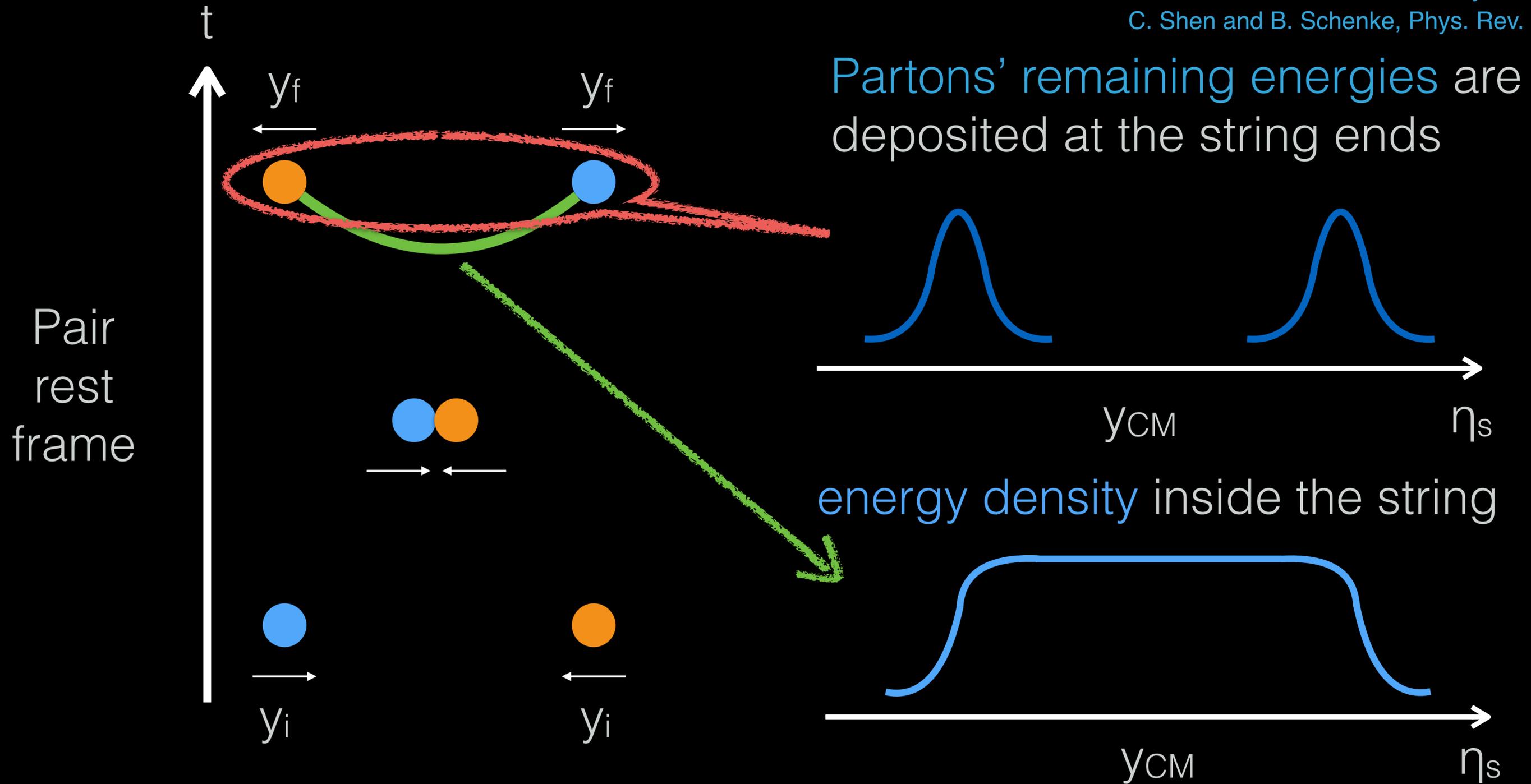
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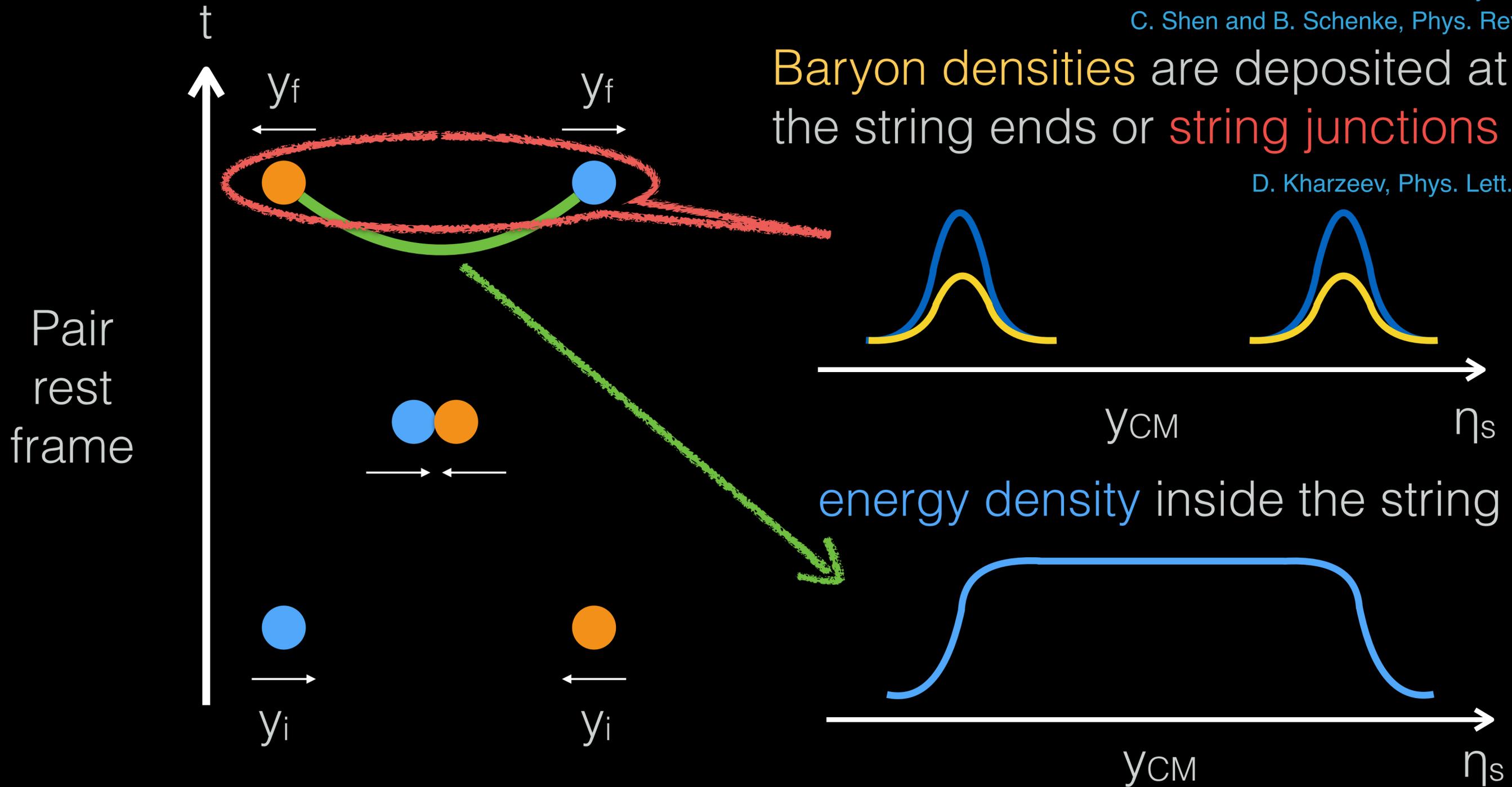


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C. Shen and B. Schenke, Phys.Rev. C97 024907 (2018)  
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Baryon densities are deposited at the string ends or **string junctions**

D. Kharzeev, Phys. Lett. B 378, 238 (1996)

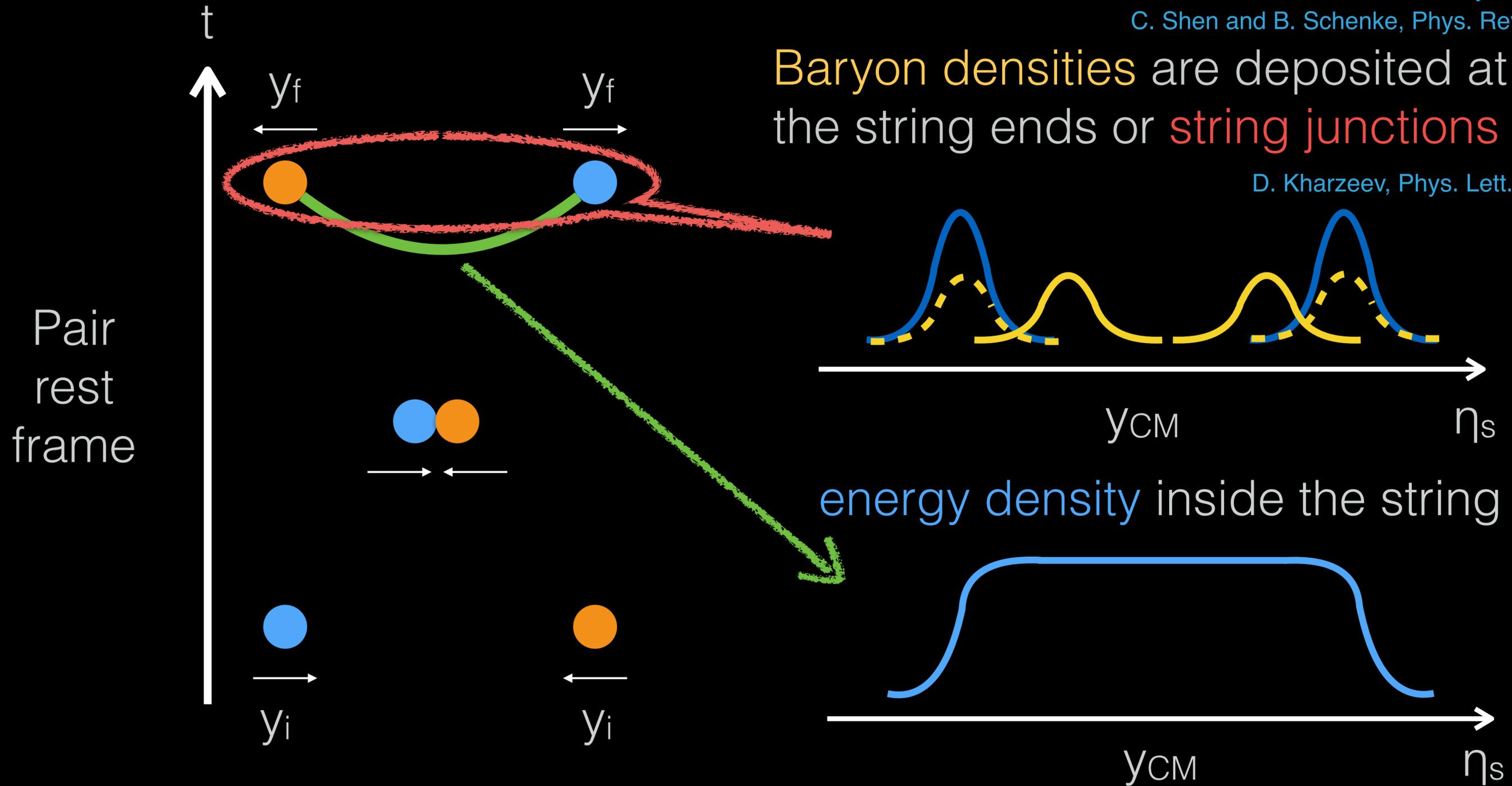


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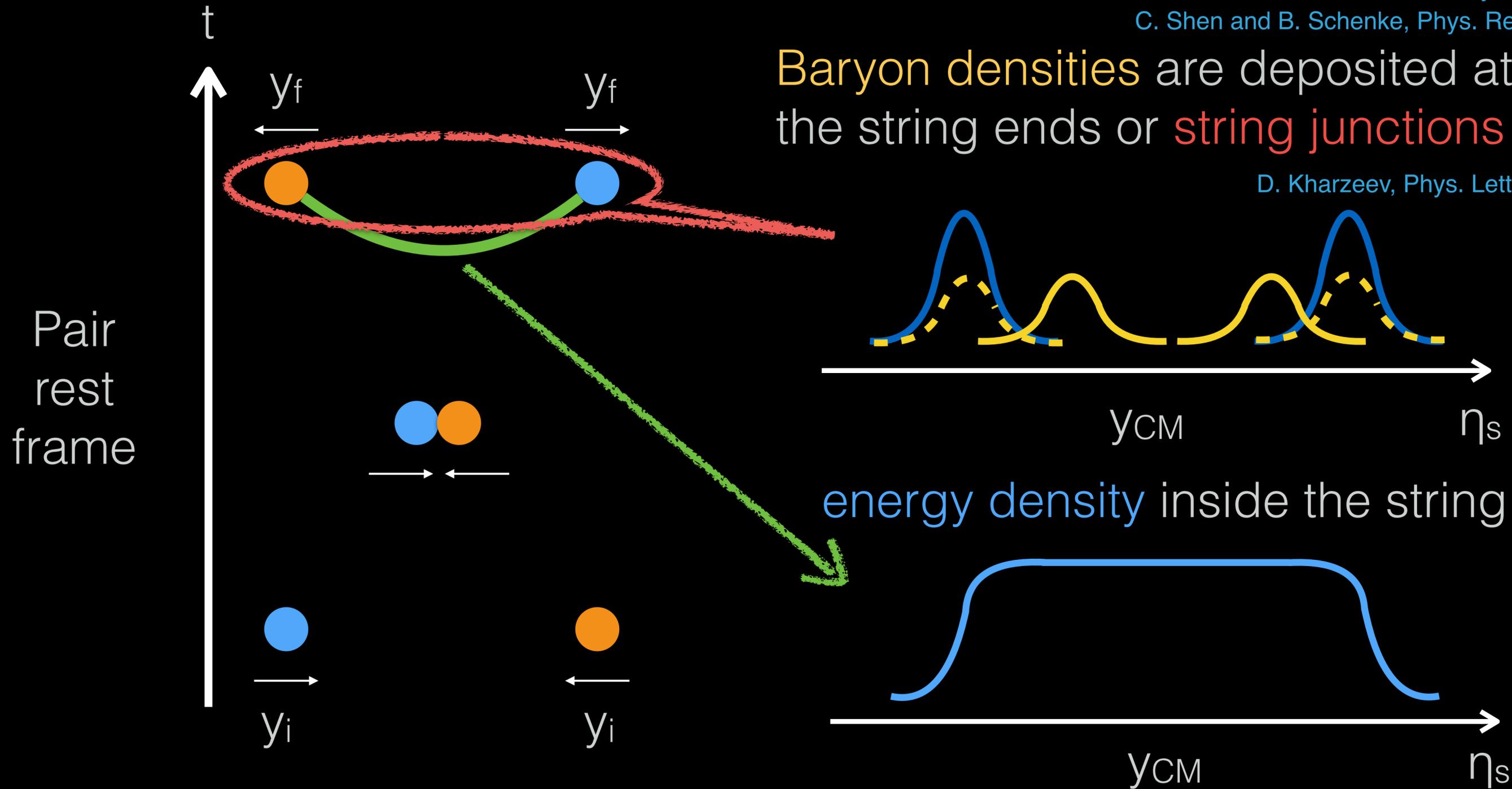


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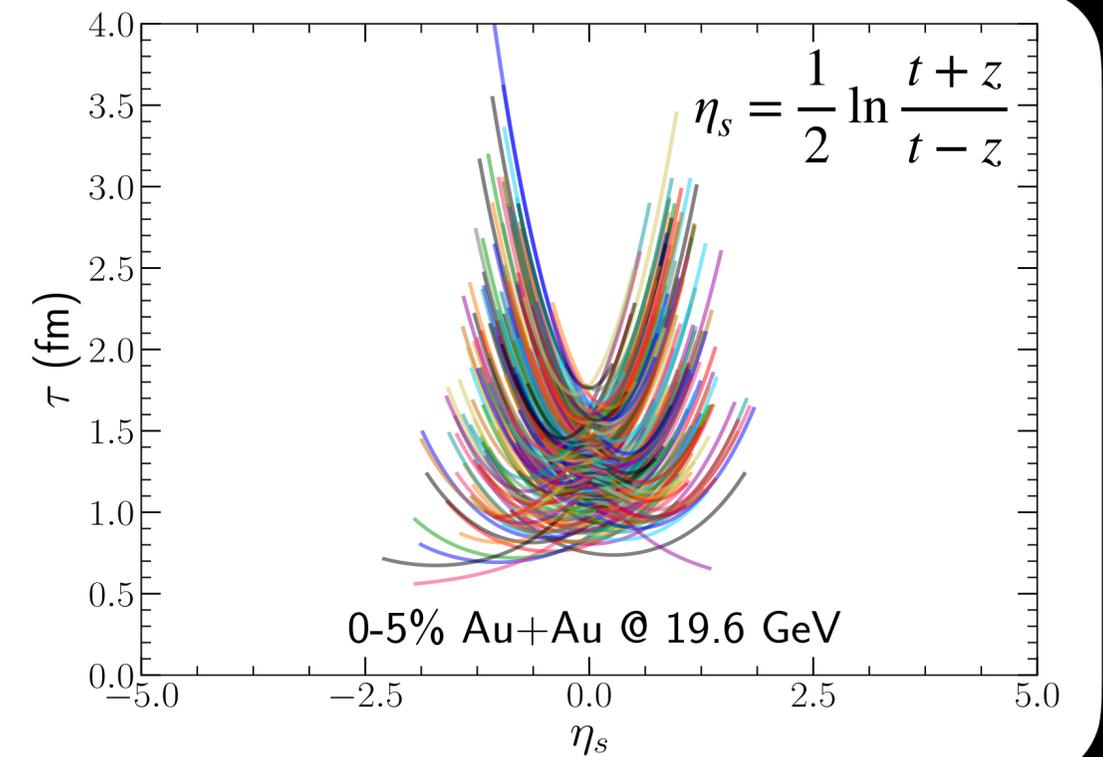
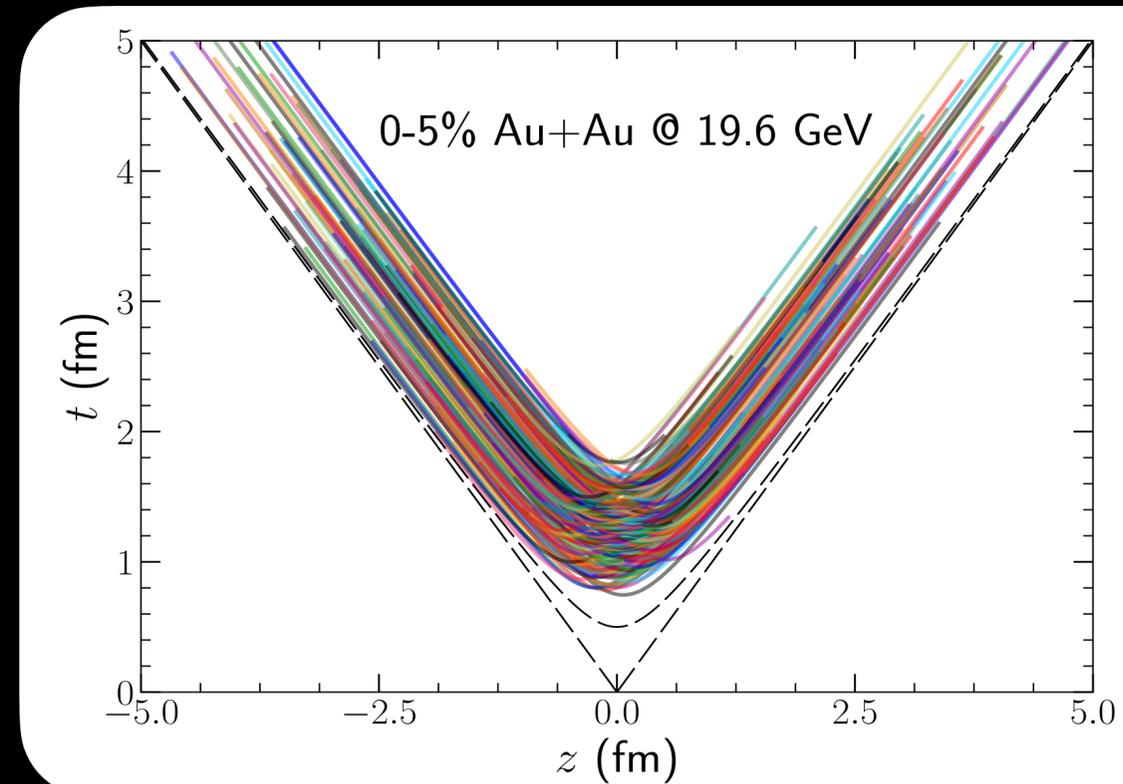
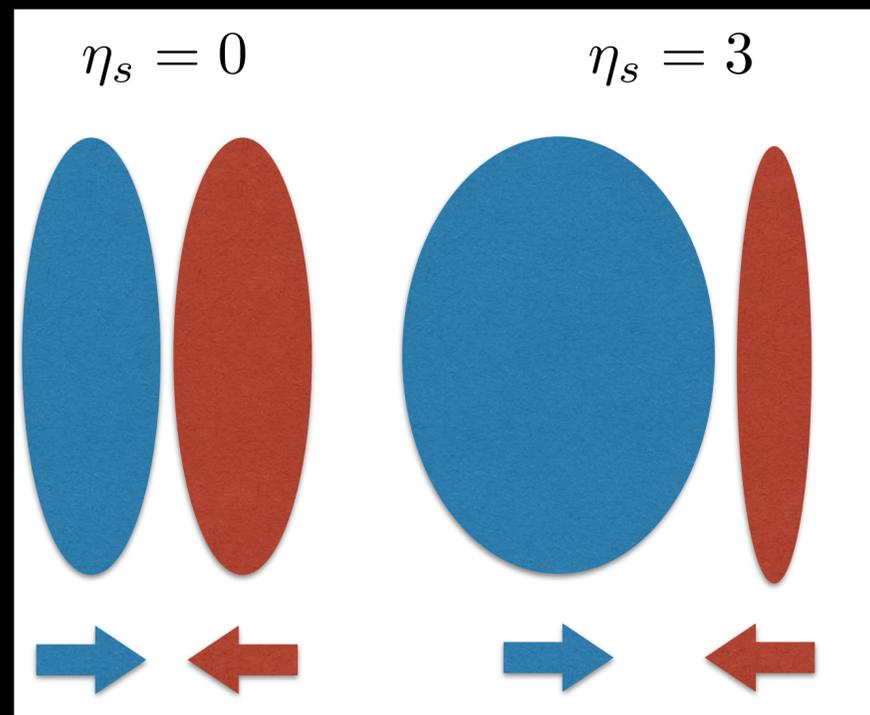
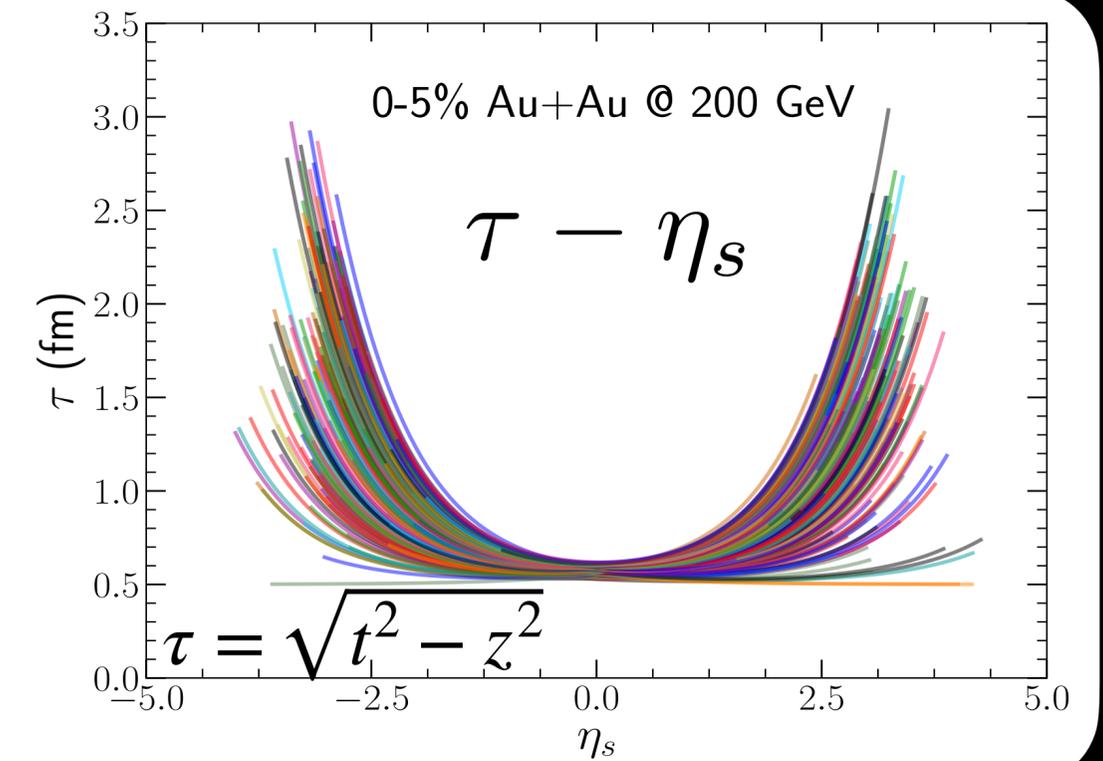
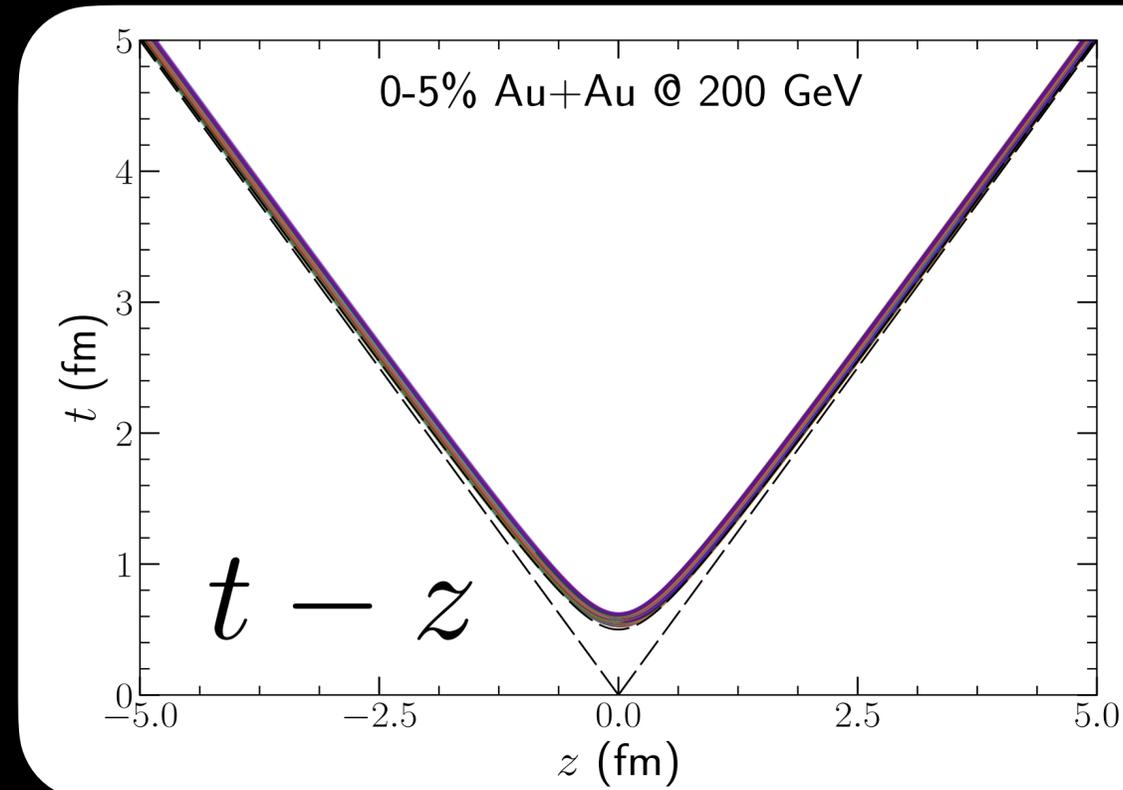
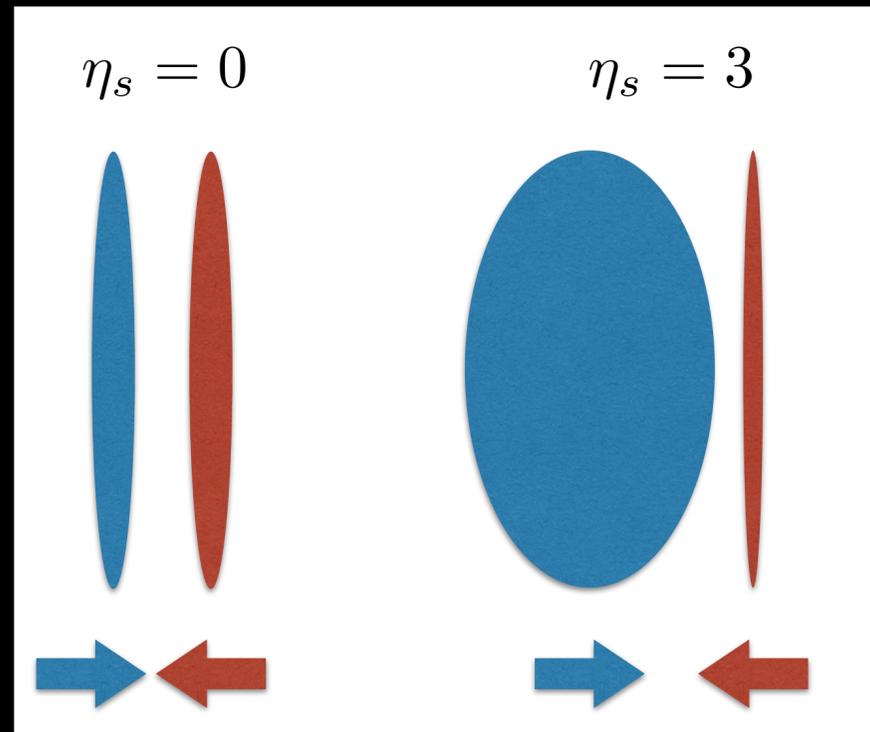
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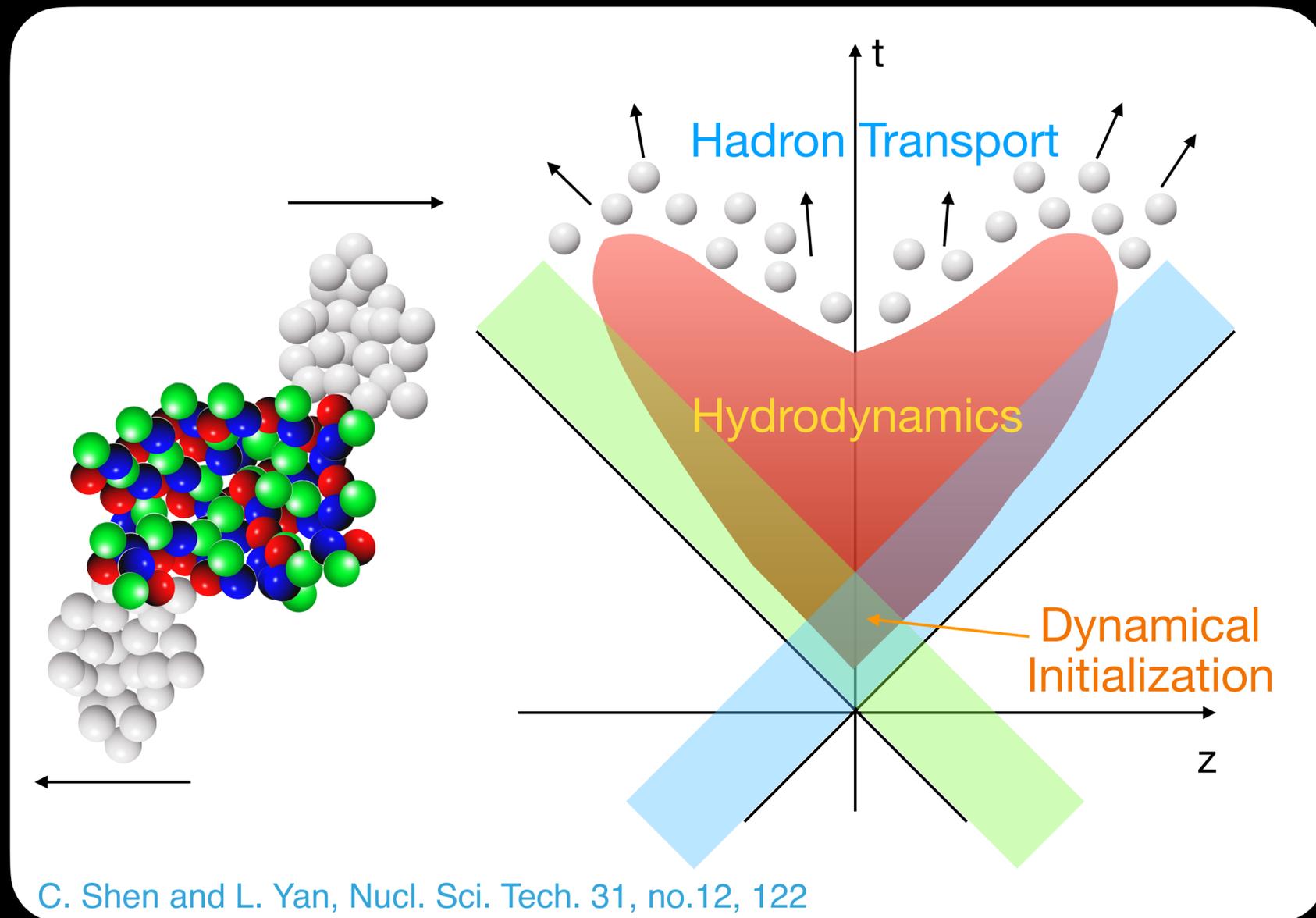
**Imposed conservation for energy, momentum, and net baryon density**

# STRINGS' SPACE-TIME DISTRIBUTION



# HYDRODYNAMICS WITH SOURCES

Energy-momentum current and net baryon density are fed into hydrodynamic simulations as source terms



$$\partial_{\mu} T^{\mu\nu} = J_{\text{source}}^{\nu}$$

$$\partial_{\mu} J^{\mu} = \rho_{\text{source}}$$

M. Okai, K. Kawaguchi, Y. Tachibana, and T. Hirano, Phys. Rev. C95, 054914 (2017)

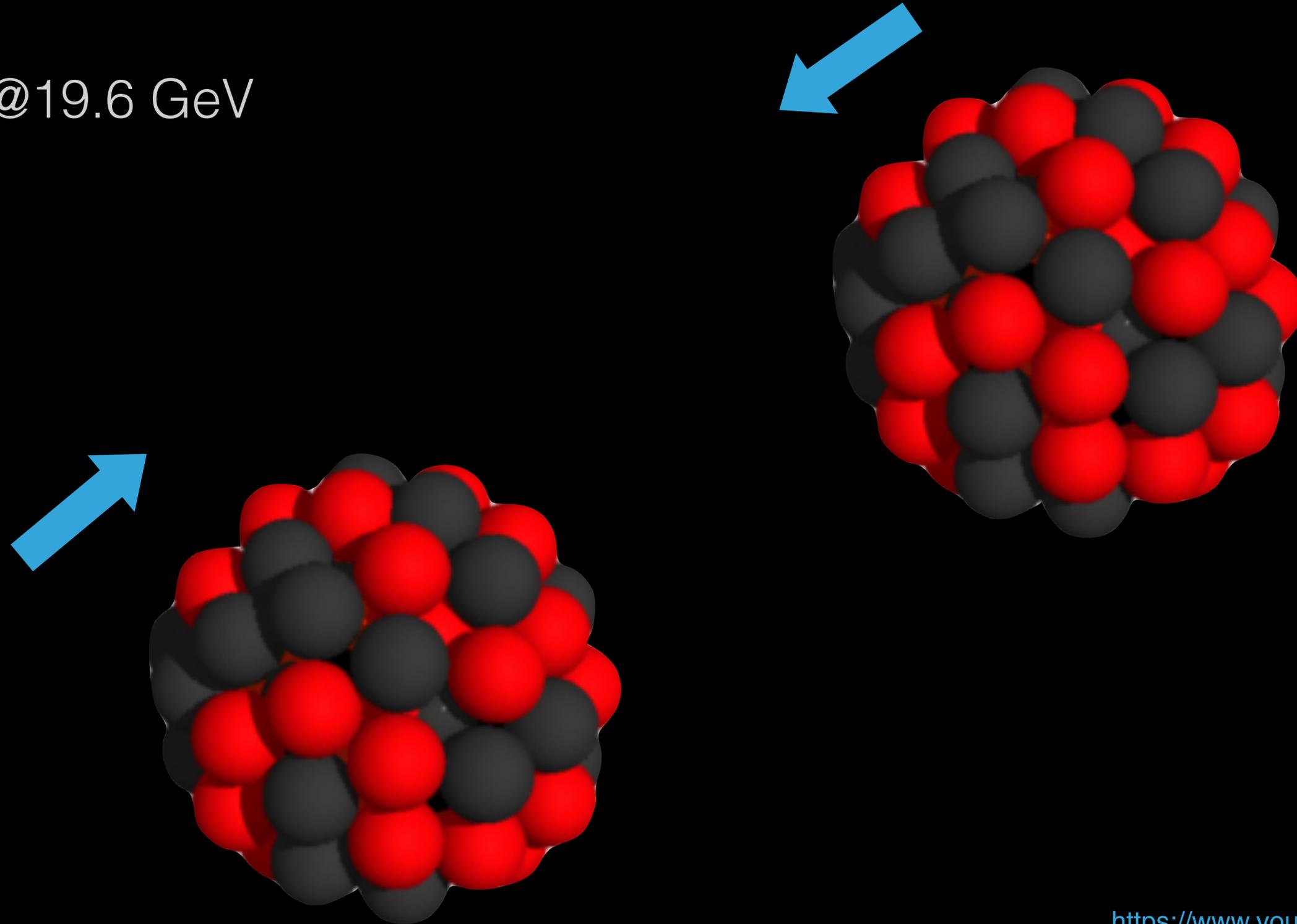
C. Shen and B. Schenke, Phys. Rev. C97 (2018) 024907

L. Du, U. Heinz and G. Vujanovic, Nucl. Phys. A982 (2019) 407-410

Y. Akamatsu, M. Asakawa, T. Hirano, M. Kitazawa, K. Morita, K. Murase, Y. Nara, C. Nonaka and A. Ohnishi, Phys. Rev. C98, 024909 (2018)

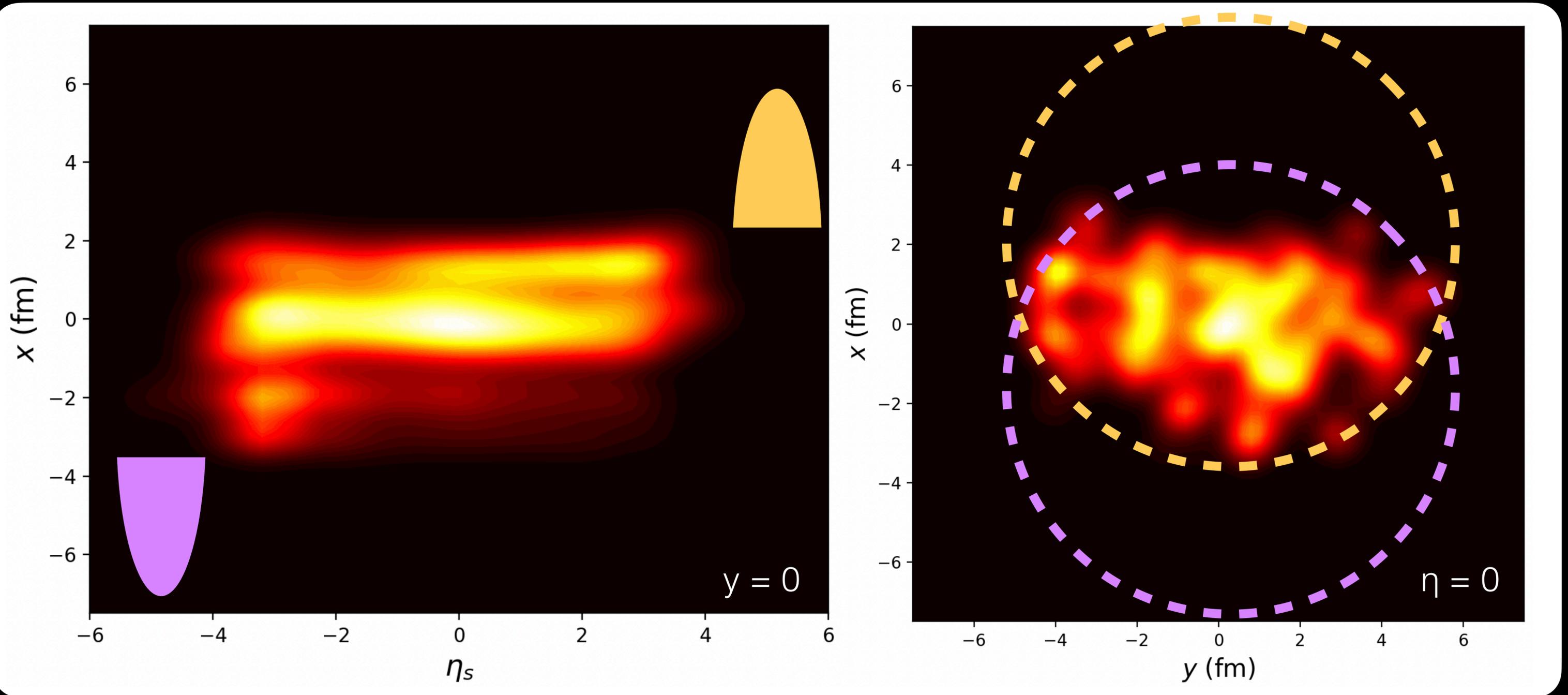
# RELATIVISTIC HEAVY-ION COLLISIONS

0-5% AuAu@19.6 GeV



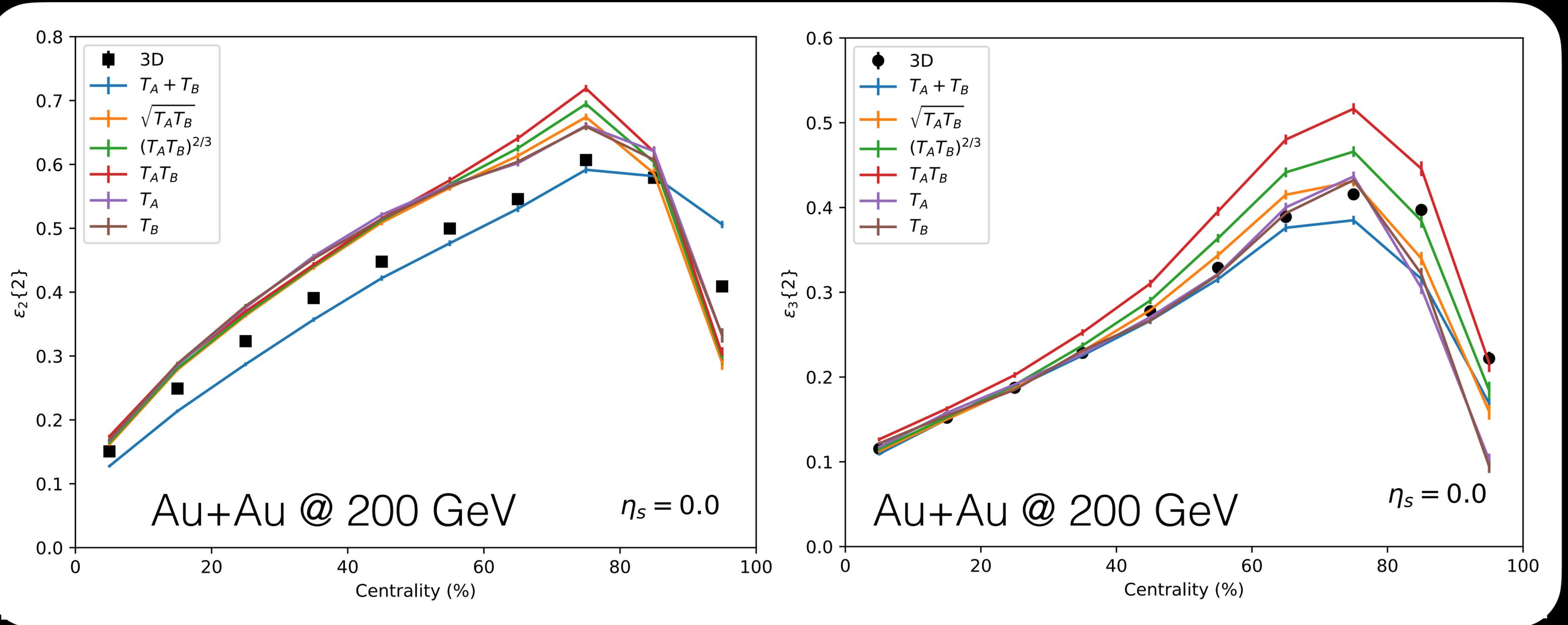
<https://www.youtube.com/watch?v=gFV-9VeqzKE>

# UNDERSTAND THE 3D ENERGY DENSITY PROFILE



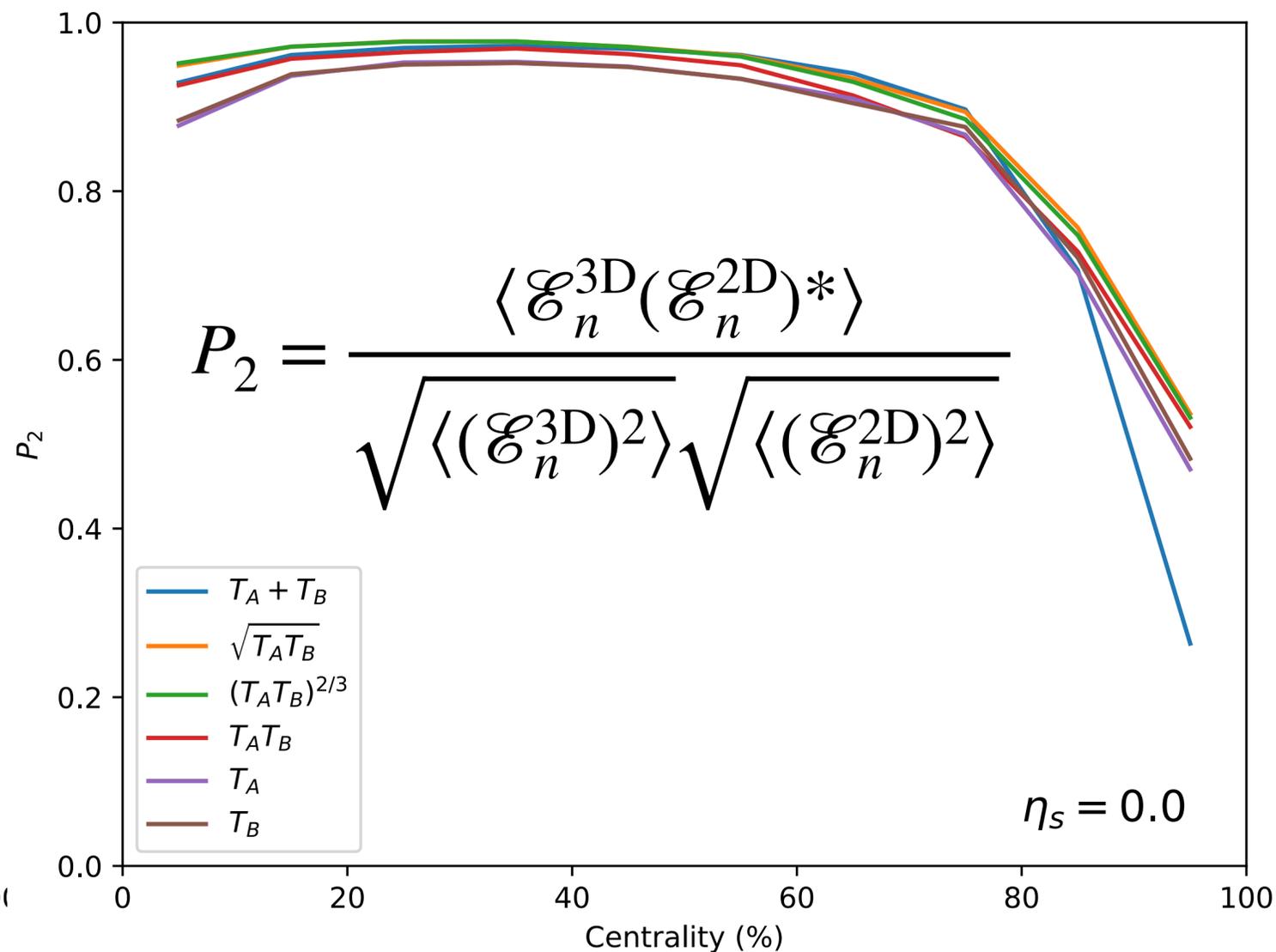
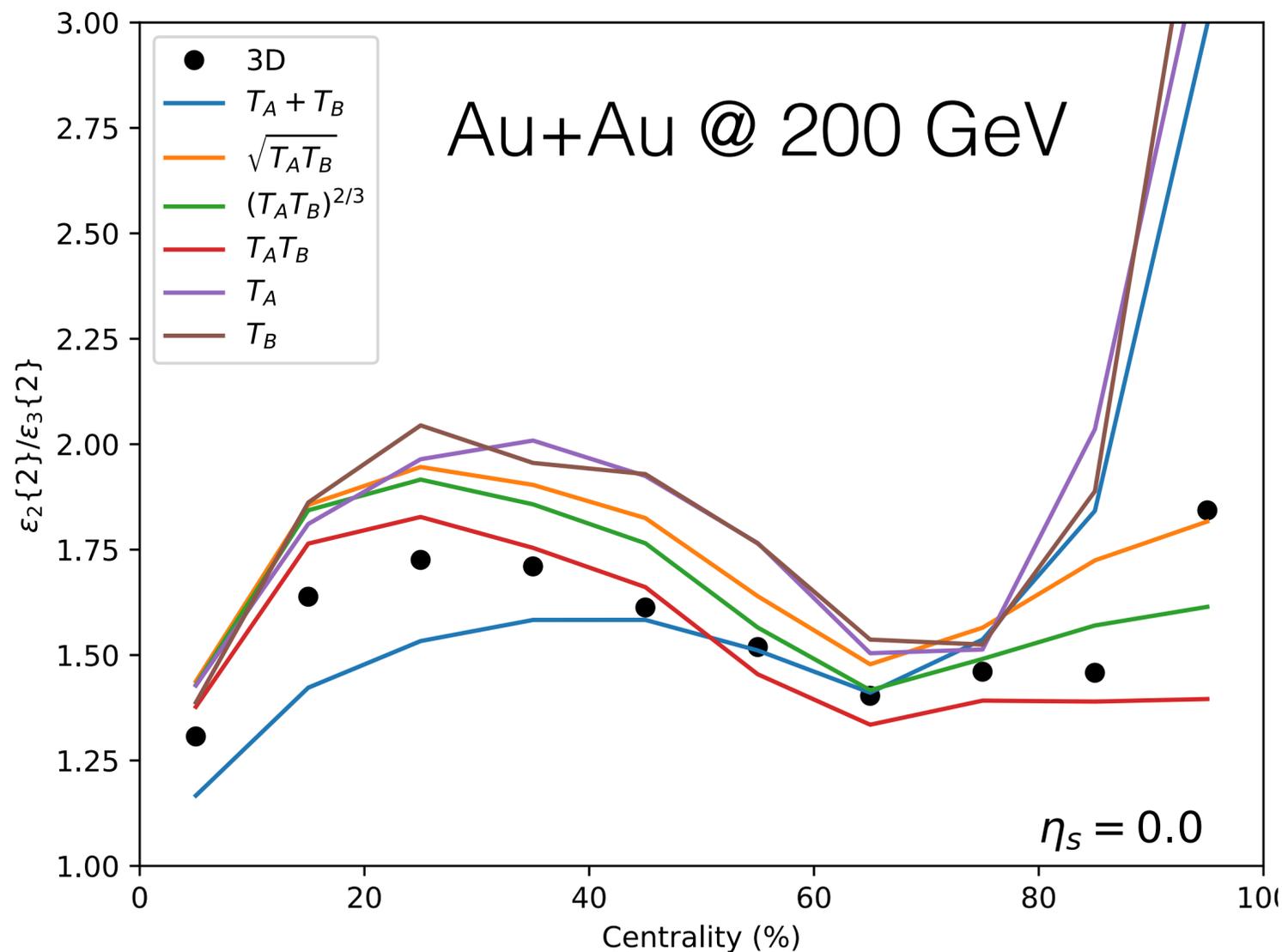
Au+Au@200 GeV  $b = 7$  fm

# MID-RAPIDITY SPATIAL ECCENTRICITY



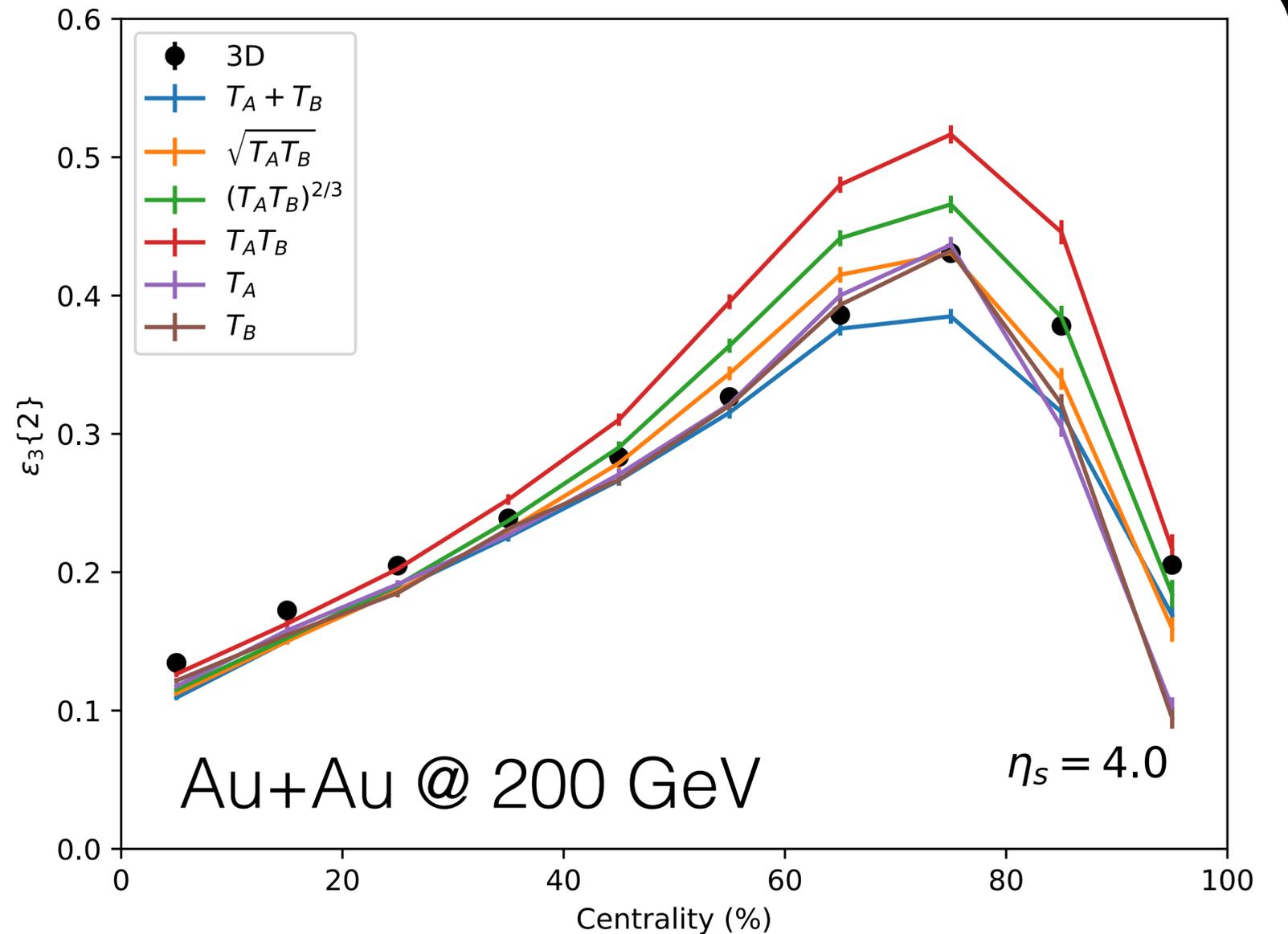
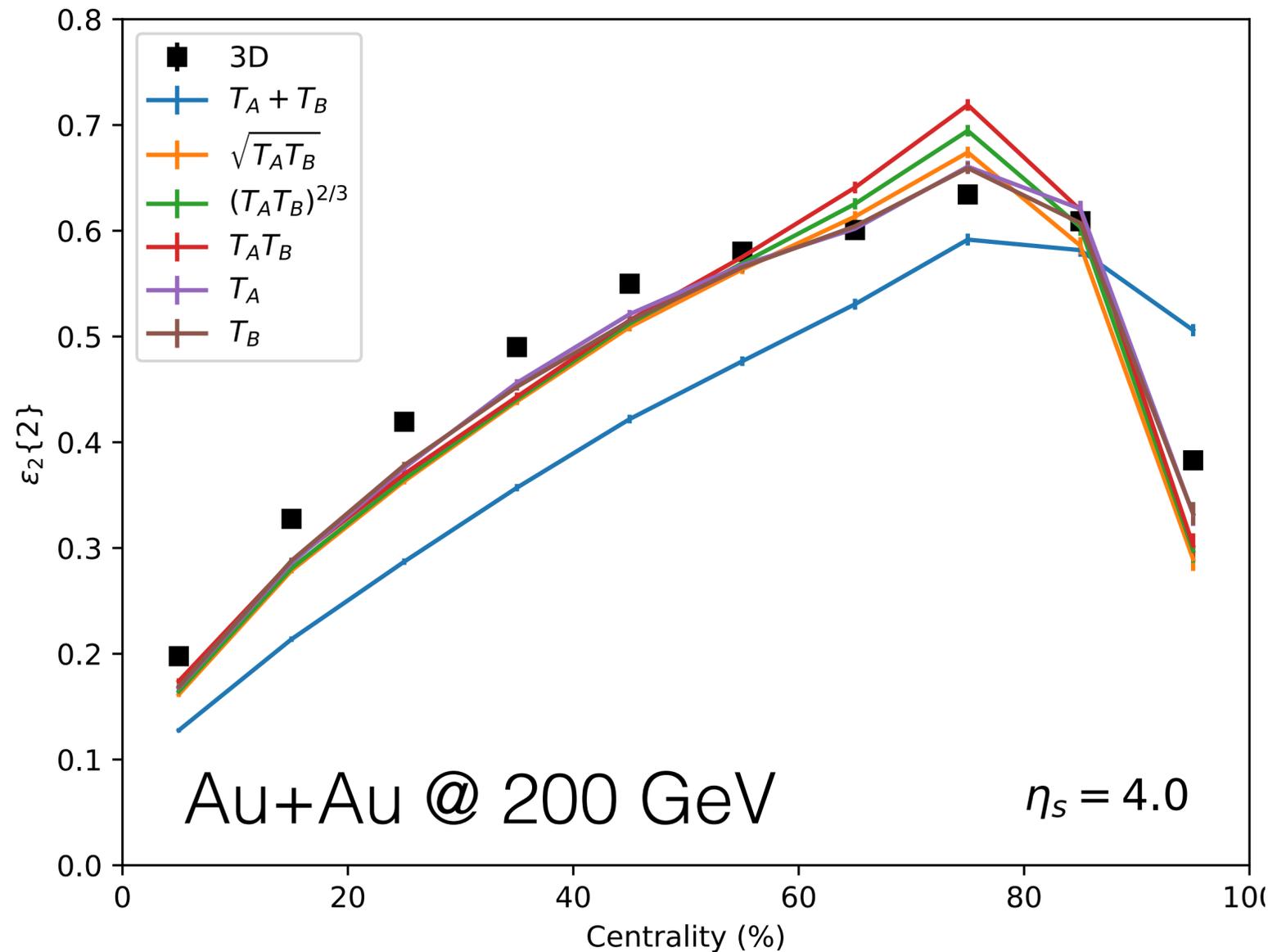
- No clear 2D estimators with nuclear thickness functions for the eccentricities of the 3D MC-Glauber model

# UNDERSTAND SPATIAL ECCENTRICITY



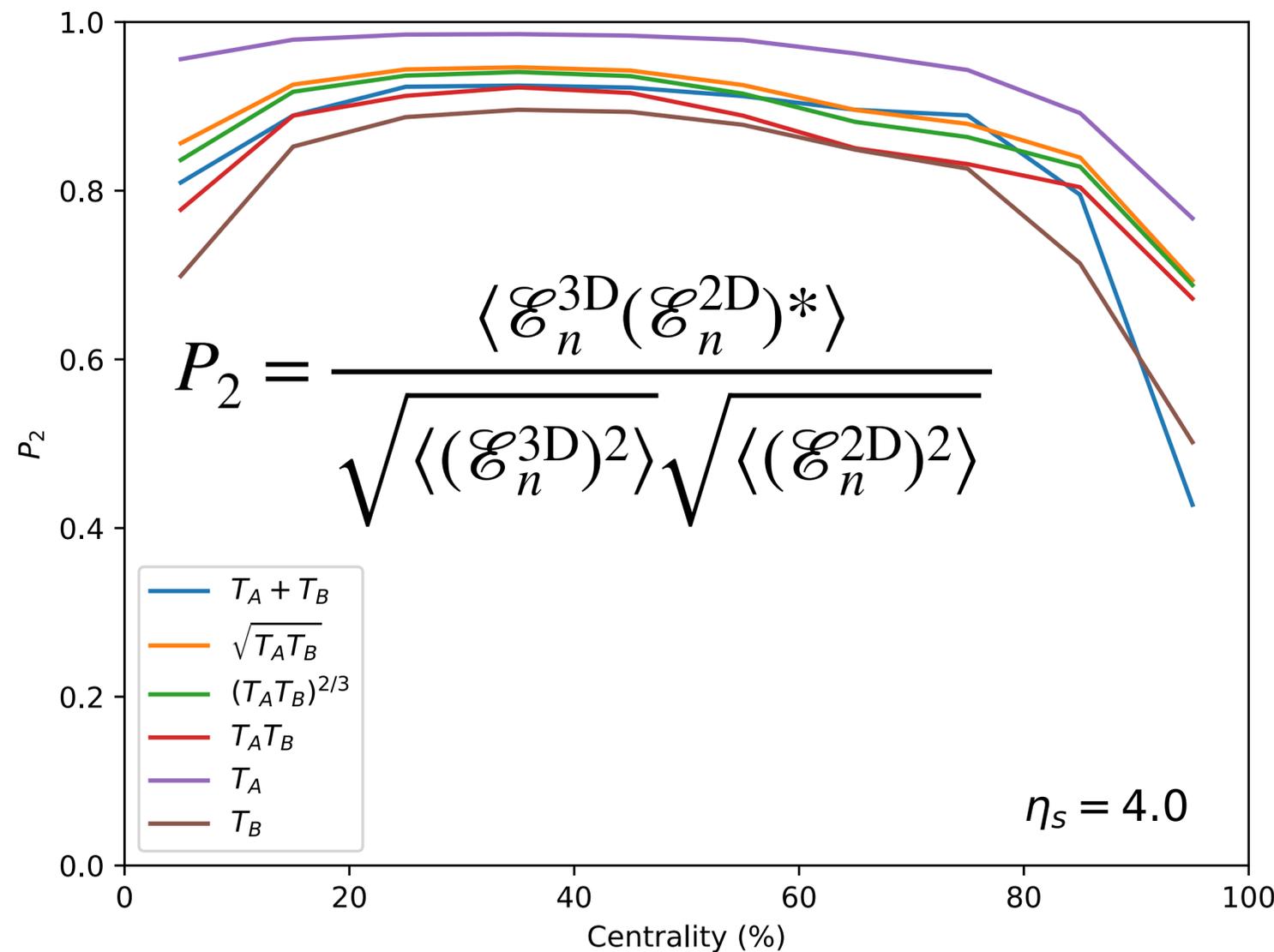
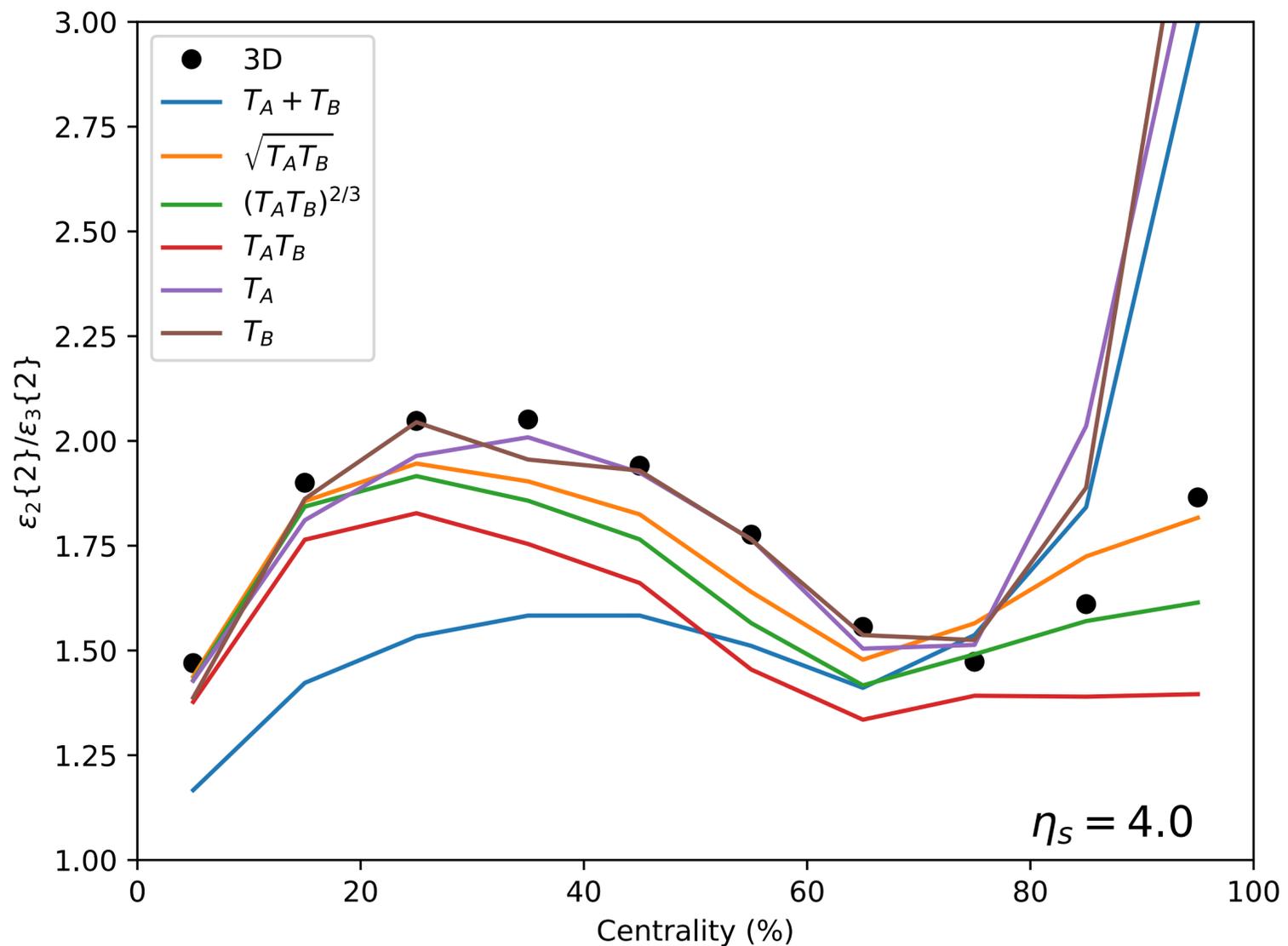
- At mid-rapidity, the ratio of  $\epsilon_2/\epsilon_3$  is close to the  $T_A T_B$  scaling;
- The Pearson correlation slightly favors  $(T_A T_B)^{1/2}$  and  $(T_A T_B)^{2/3}$

# FORWARD SPATIAL ECCENTRICITY



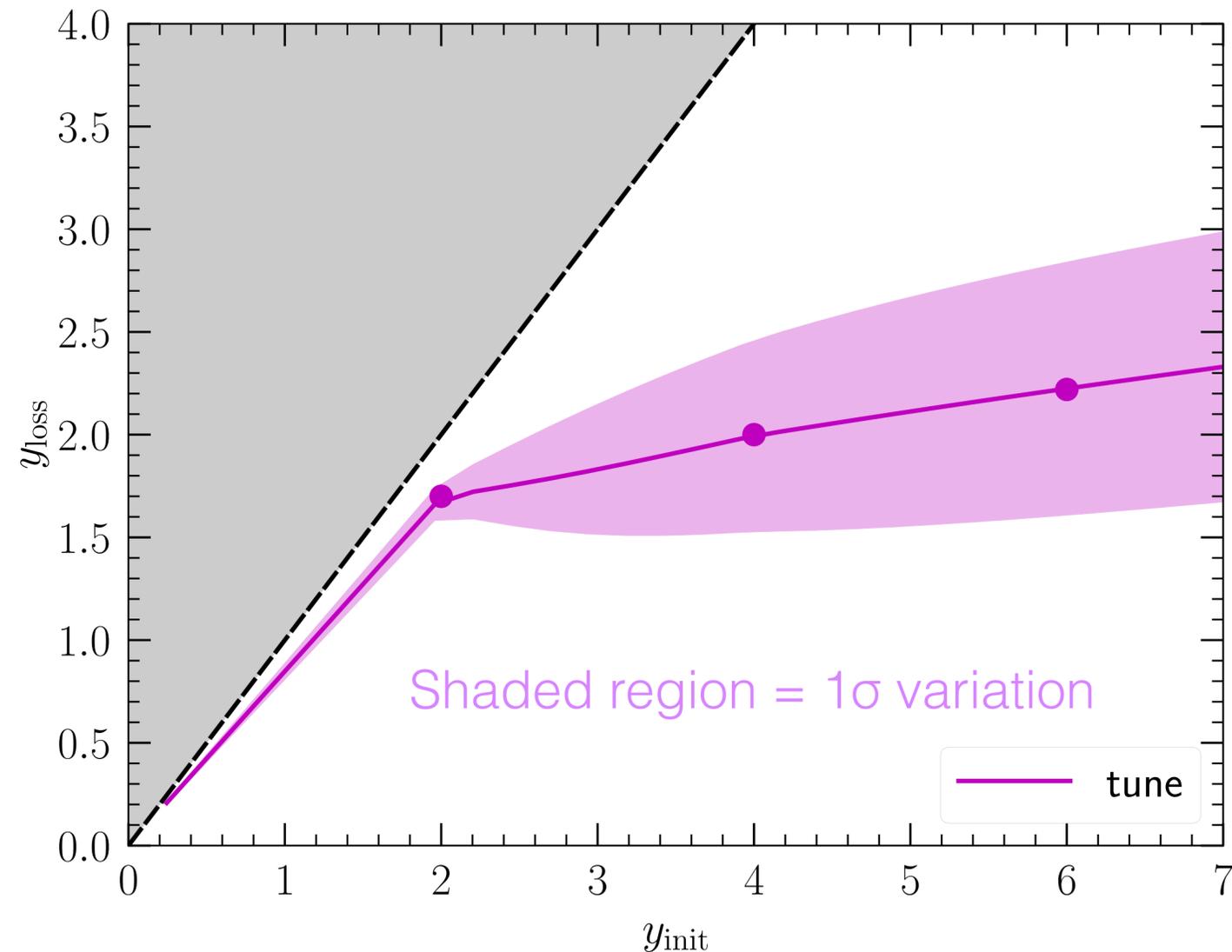
- Ellipticity increases in the forward rapidity compared to those at mid-rapidity

# UNDERSTAND SPATIAL ECCENTRICITY



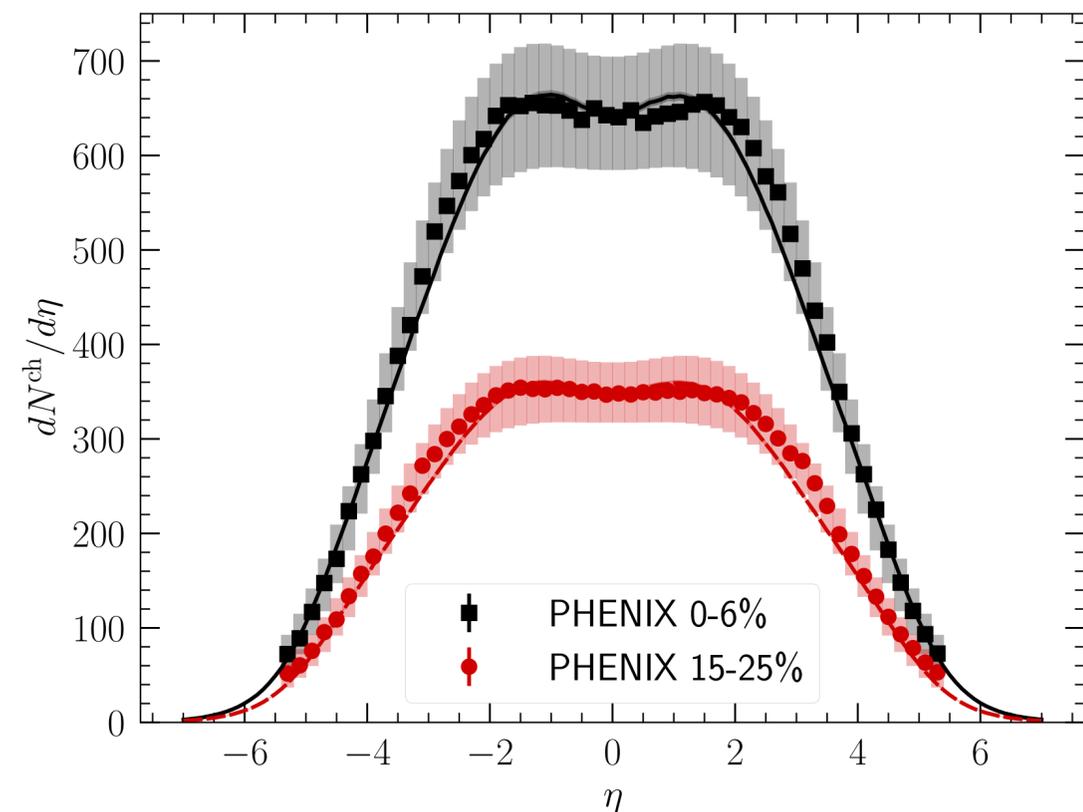
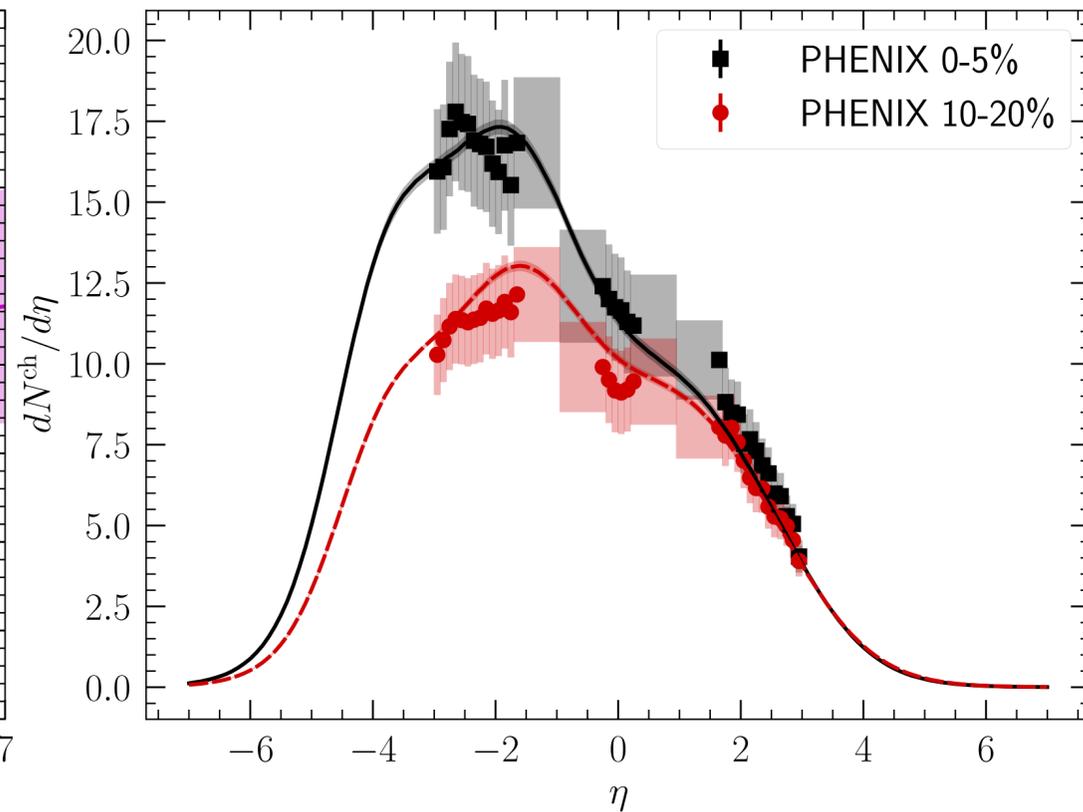
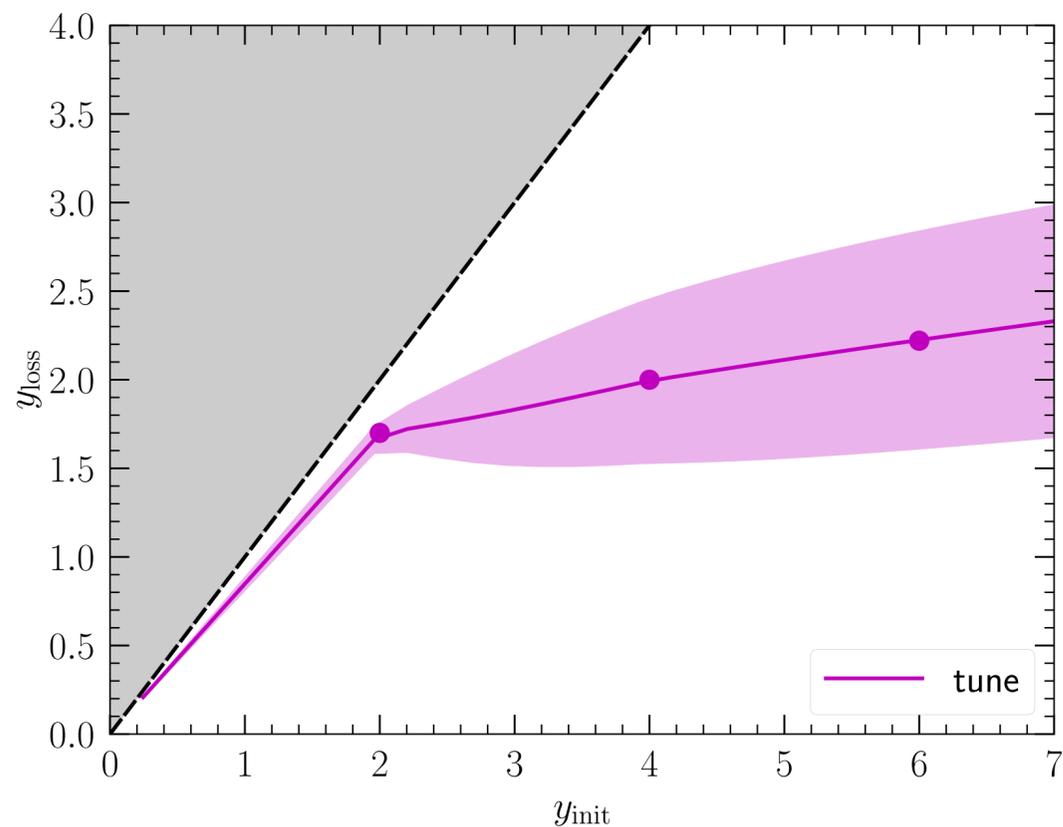
- At forward rapidity, the spatial eccentricity is correlated with  $T_A$
- Similarly, the spatial eccentricity in the backward rapidity is correlated with  $T_B$

# PARAMETERIZE THE CONSTITUENTS ENERGY LOSS



- Piece-wise parameterization of the averaged rapidity loss
- Std of  $y_{loss}$  fluctuations:  $\sigma_y$  bounded between ( $y_{loss} \in [0, y_{init}]$ )

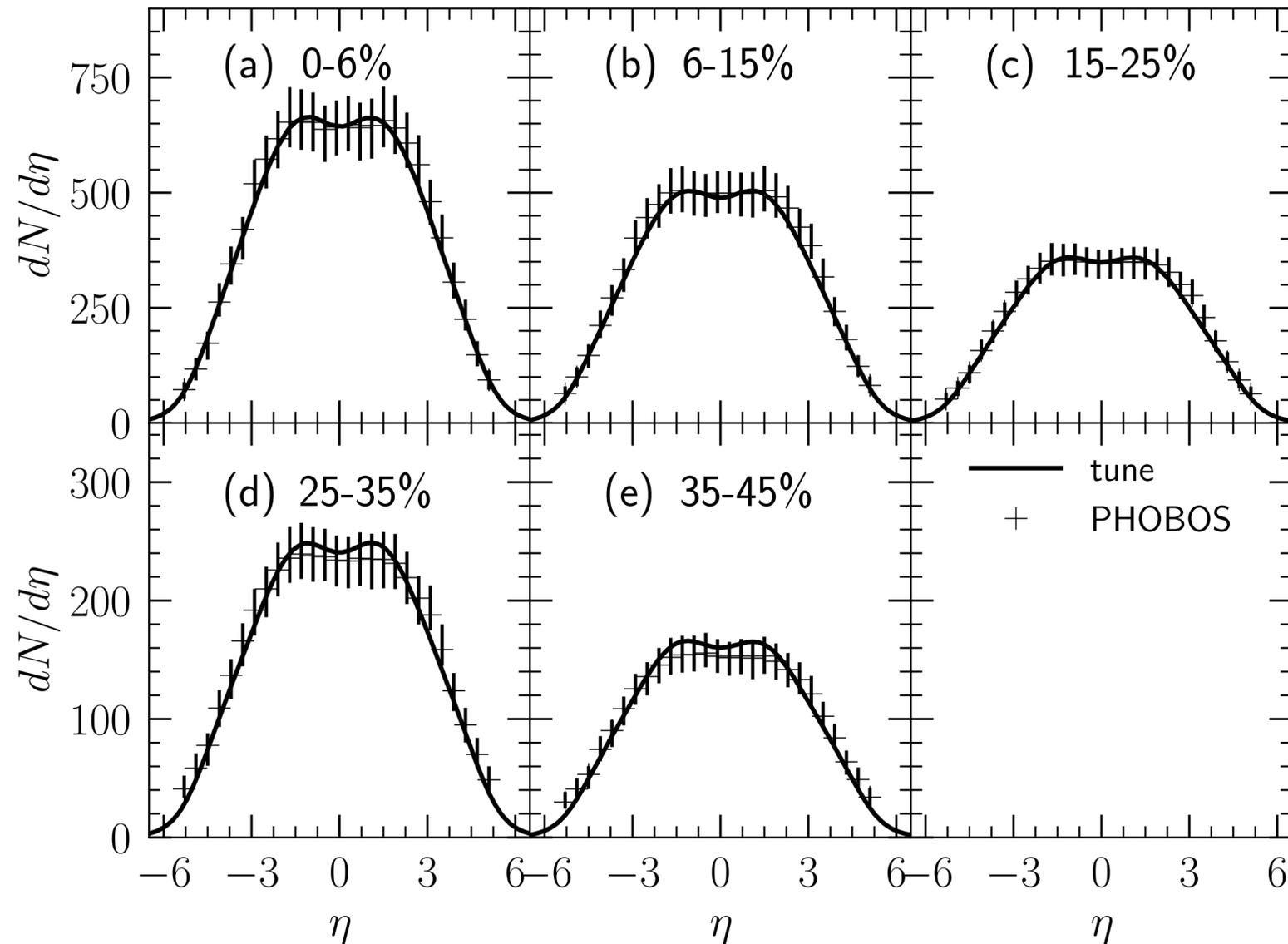
# CALIBRATION OF RAPIDITY LOSS



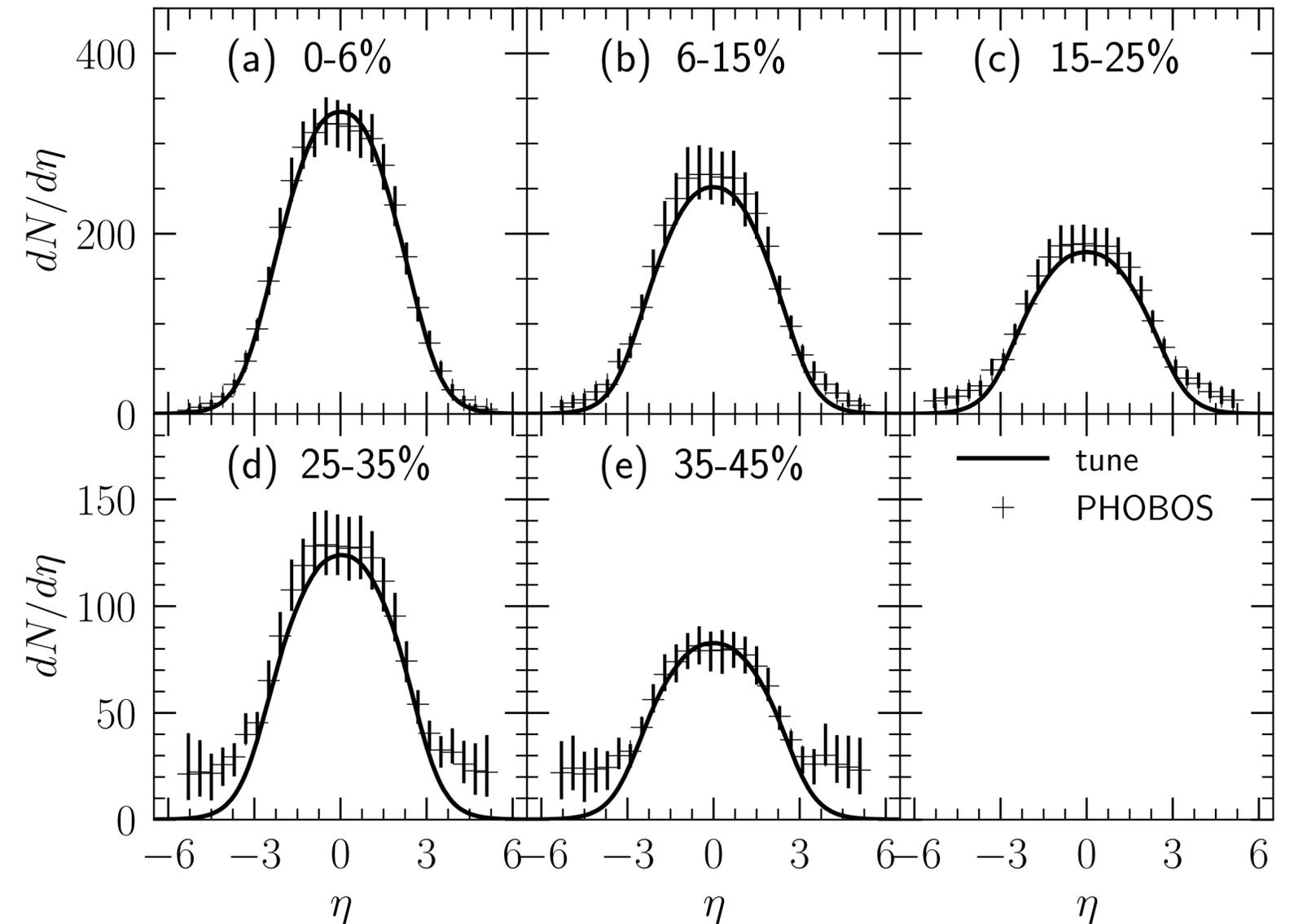
- Calibrated with charged particle pseudo-rapidity distribution in p+Au and Au+Au collisions at 200 GeV

# PARTICLE PRODUCTION IN AA COLLISIONS

Au+Au @ 200 GeV



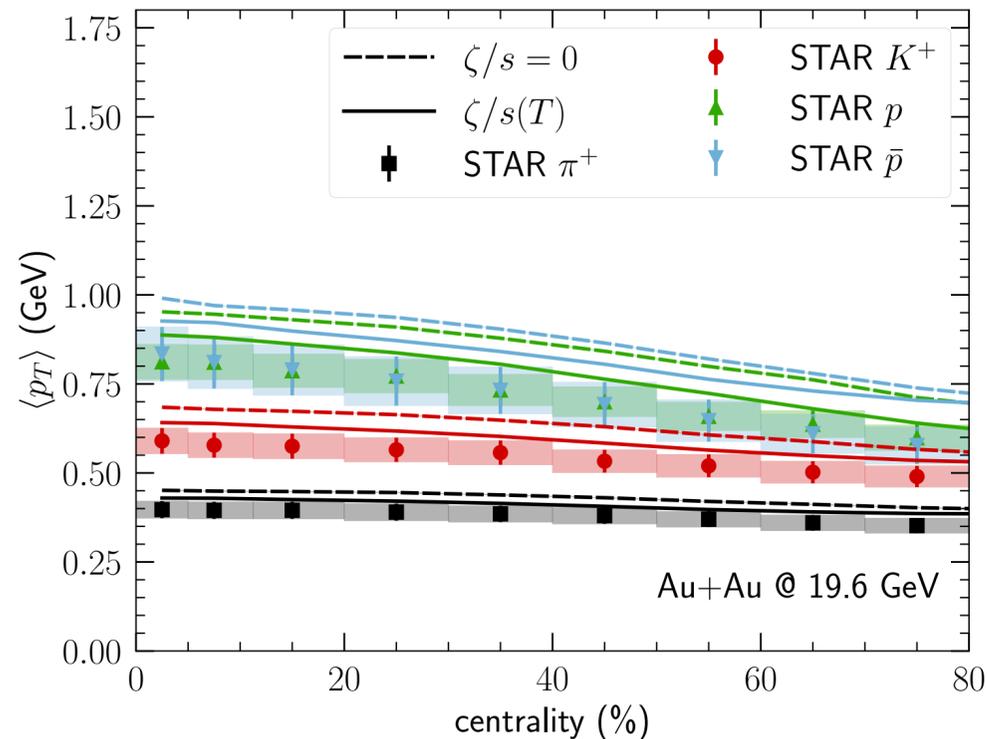
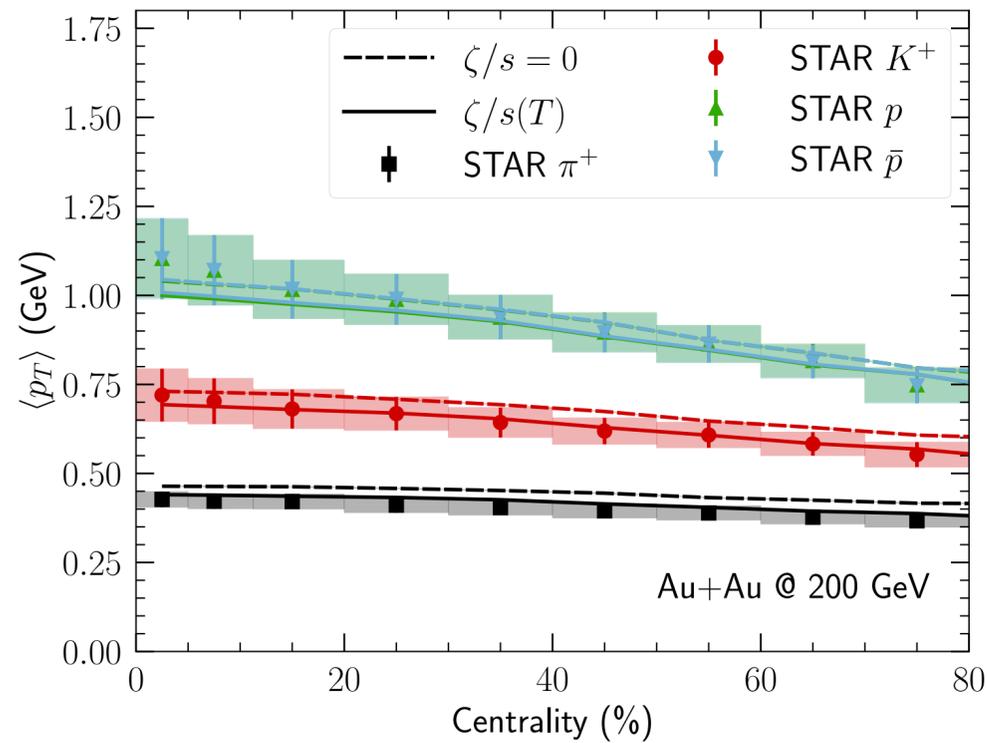
Au+Au @ 19.6 GeV



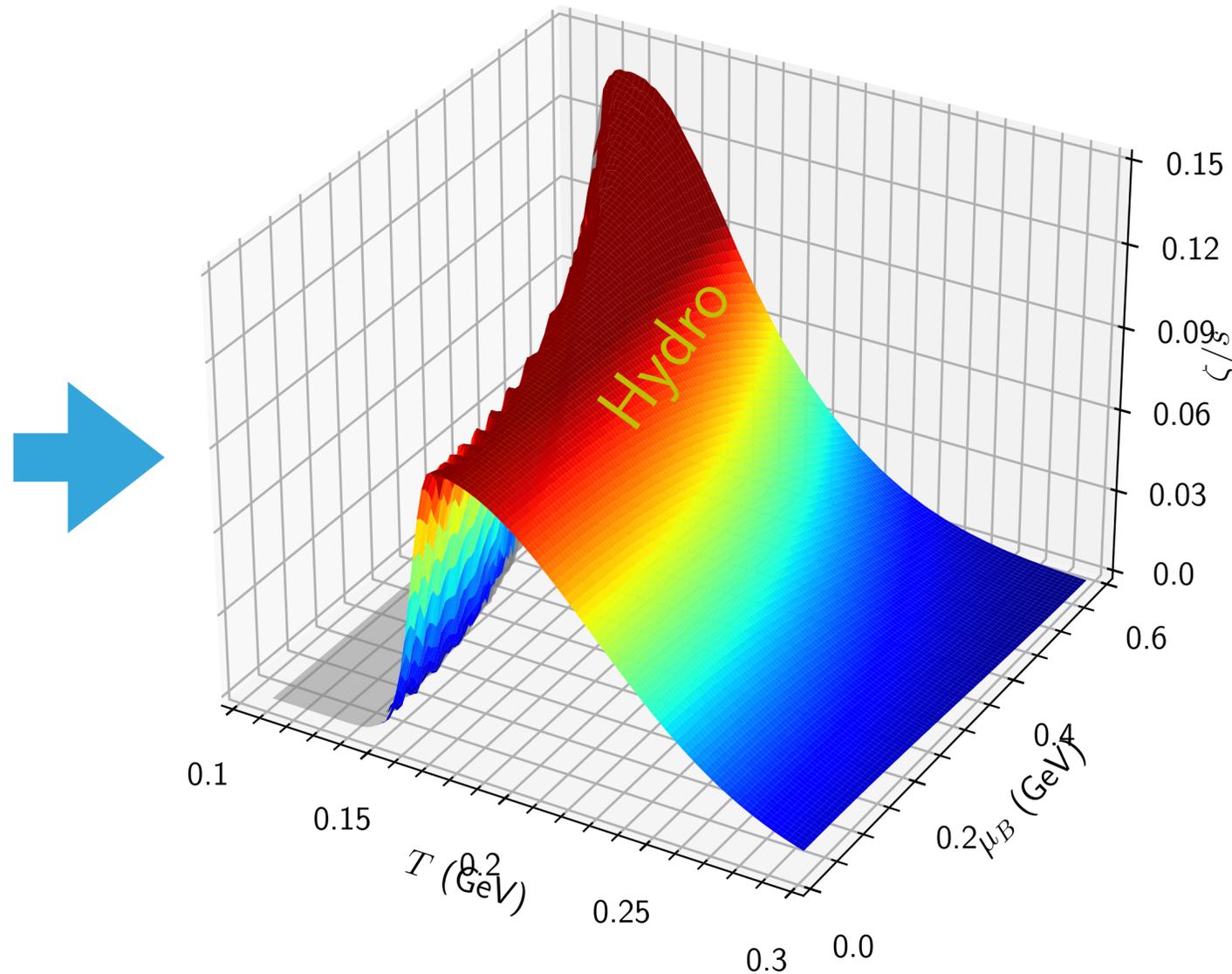
- Extension to AA collisions gives a reasonable description of the PHOBOS data

# CONSTRAINING QGP VISCOSITY AT FINITE $\mu_B$

Sangwook Ryu et al., in preparation



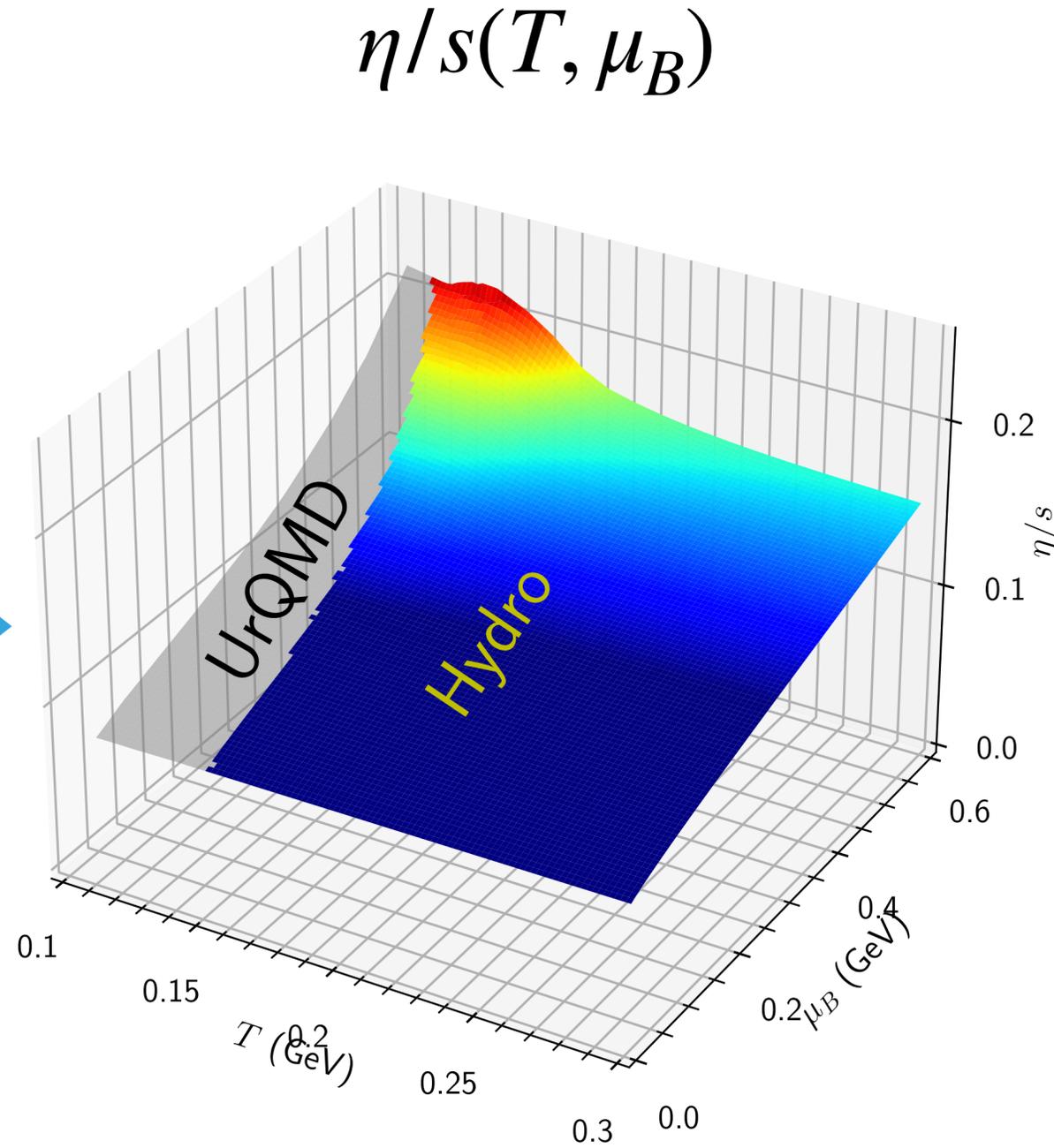
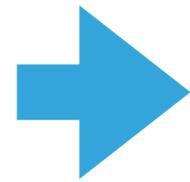
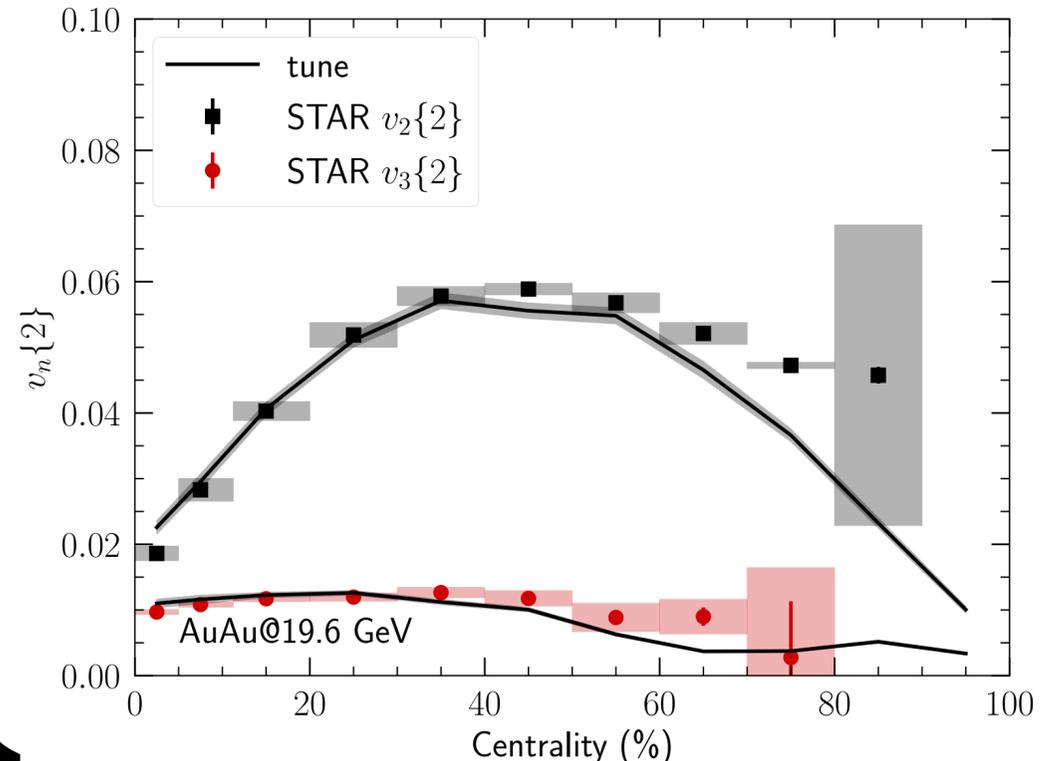
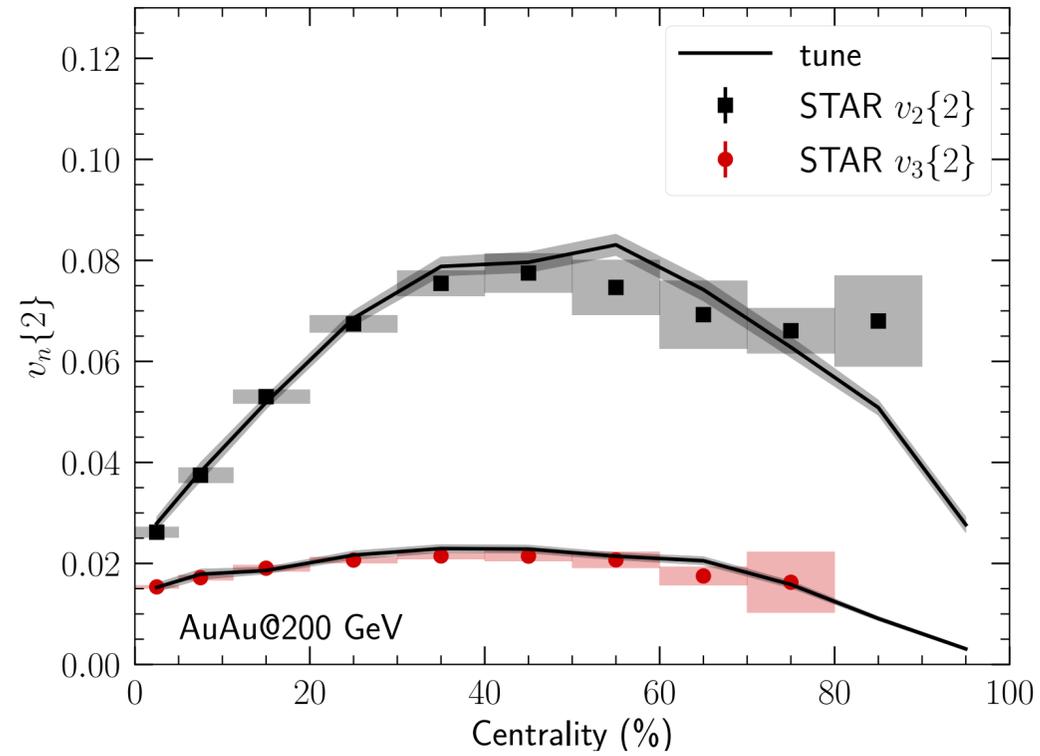
$$\zeta/s(T, \mu_B)$$



By implementing the viscous effects at finite baryon density, we are progressing to constrain the QGP's viscosity with the STAR measurements at Beam Energy Scan program

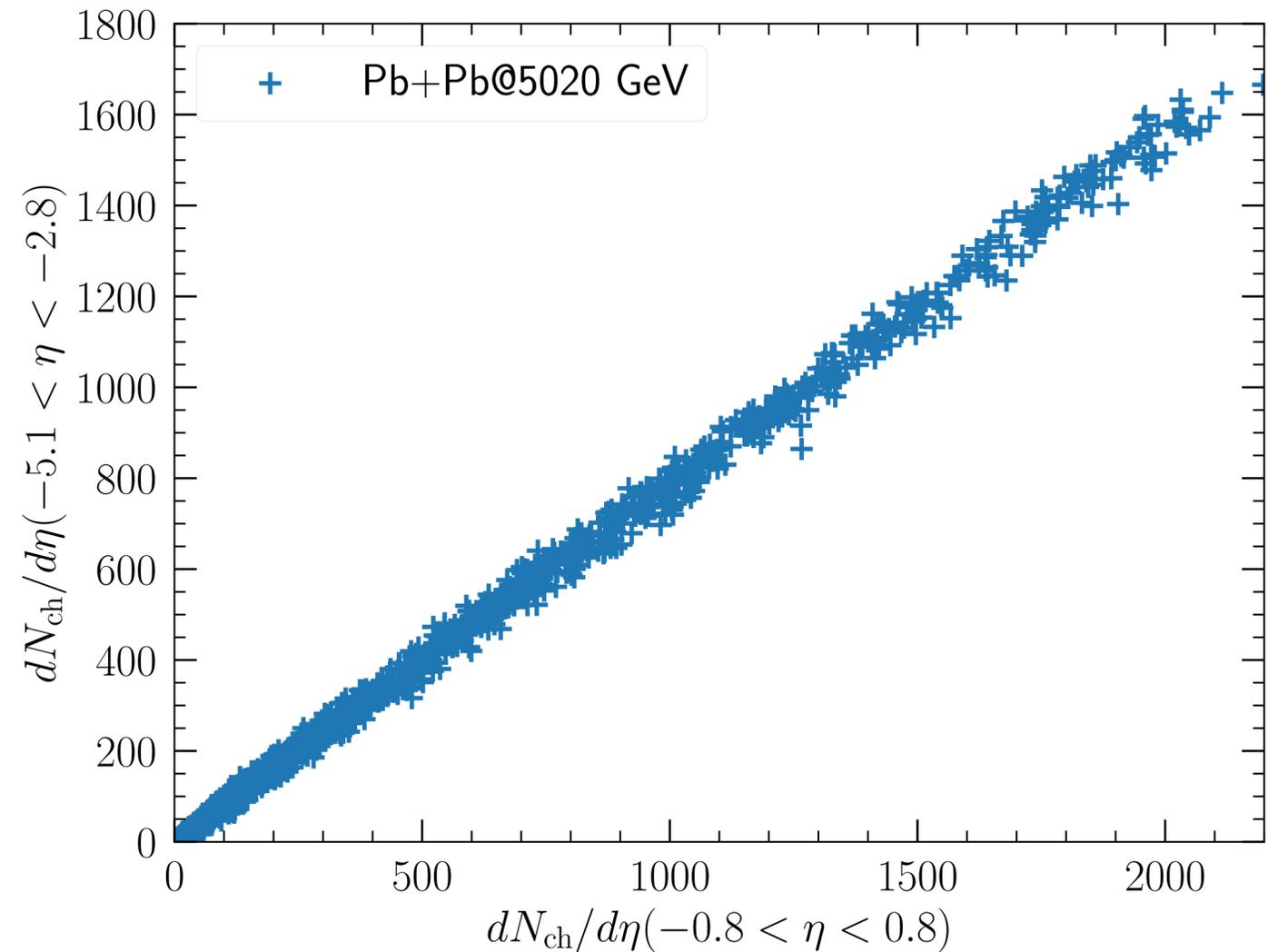
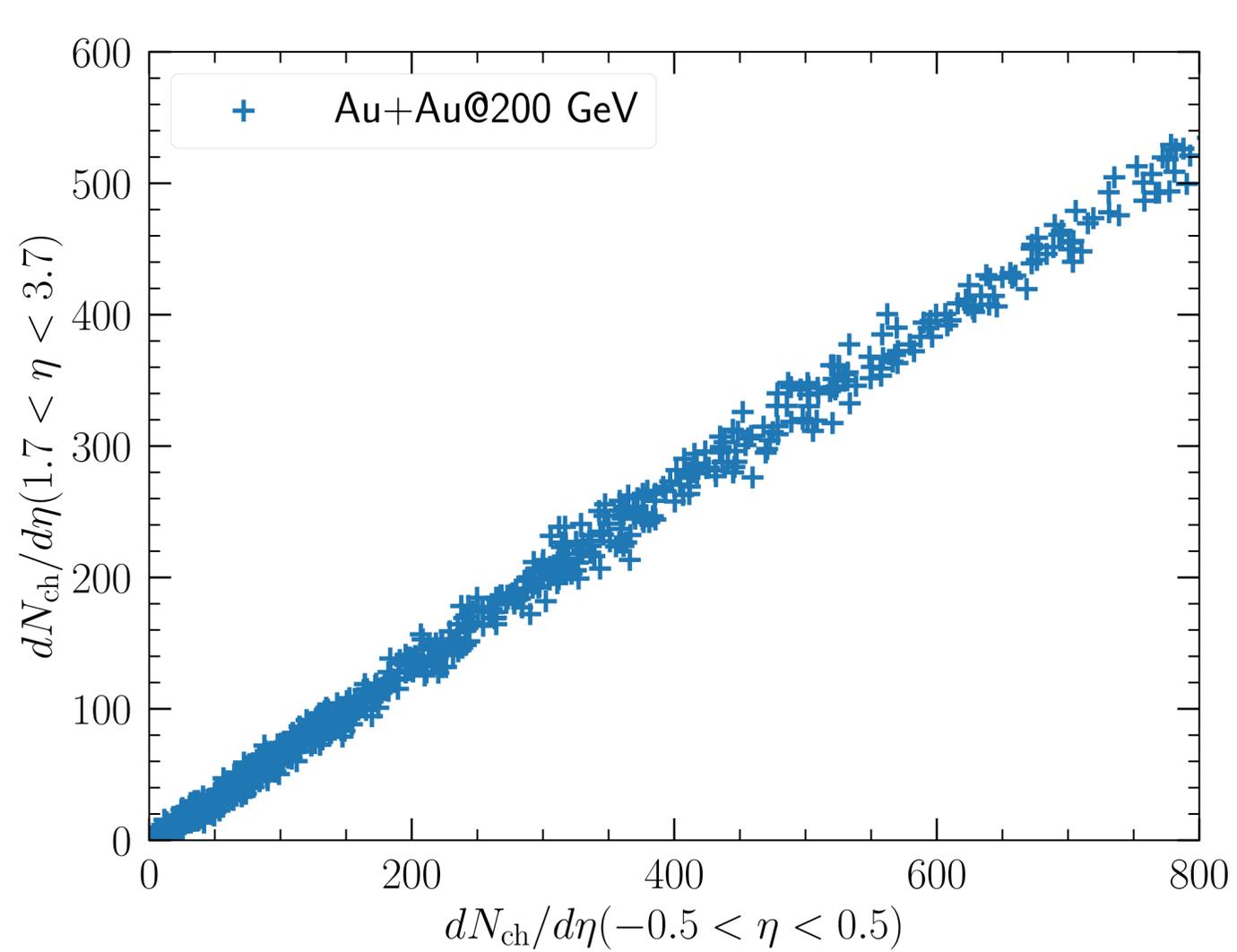
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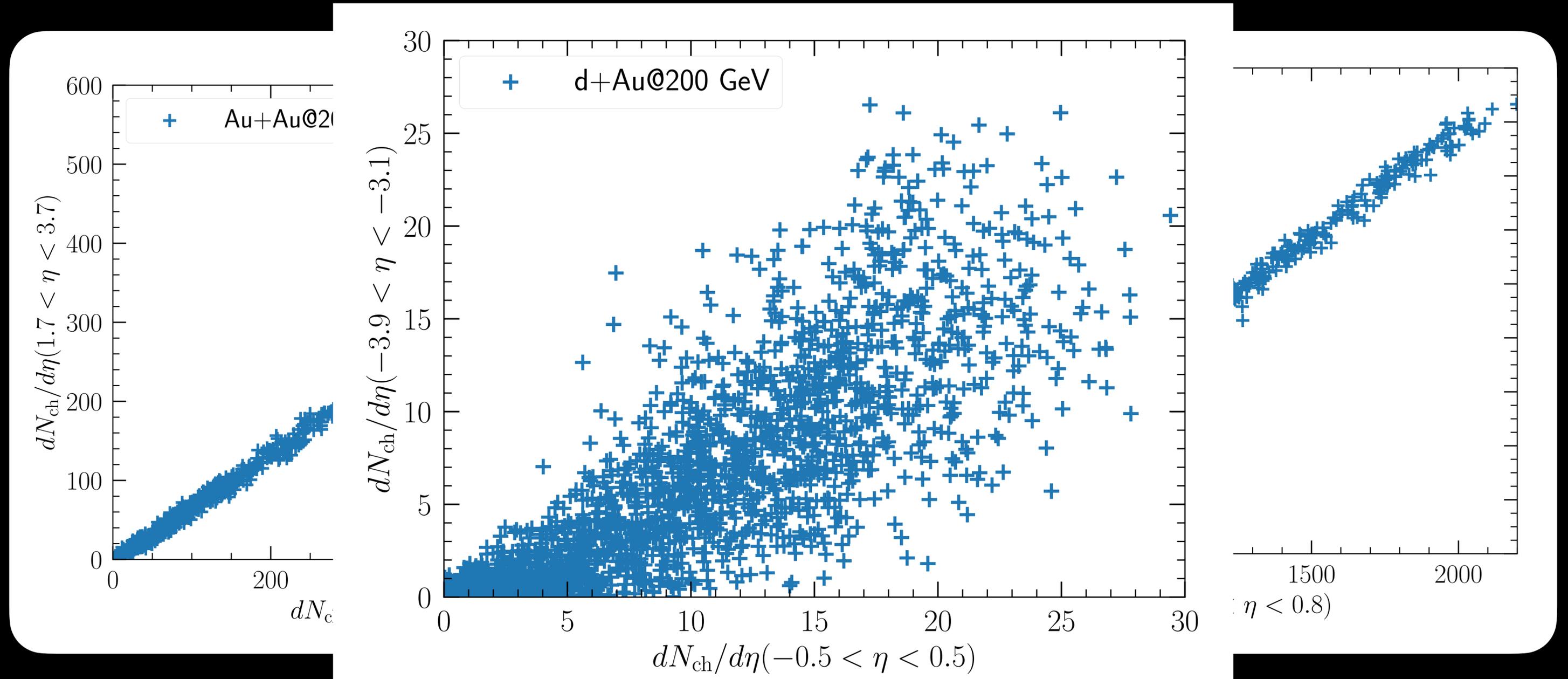
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# PARTICLE YIELD CORRELATION



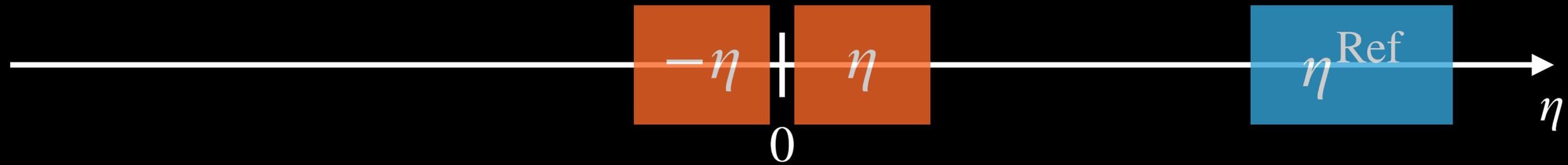
- In symmetric heavy-ion collisions, particle production in the forward rapidity is strongly correlated with those at mid-rapidity

# PARTICLE YIELD CORRELATION



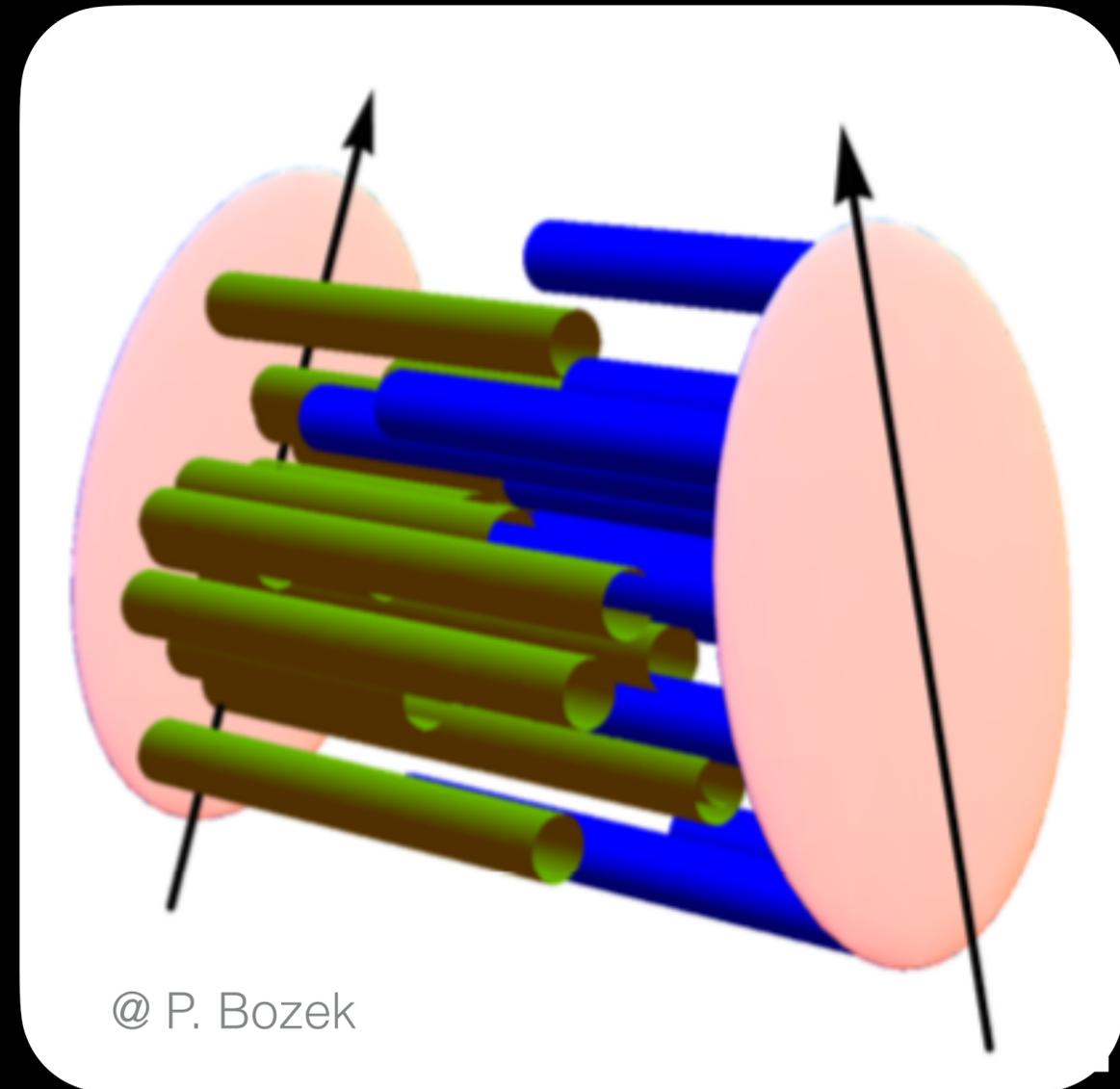
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# LONGITUDINAL FLOW DECORRELATION



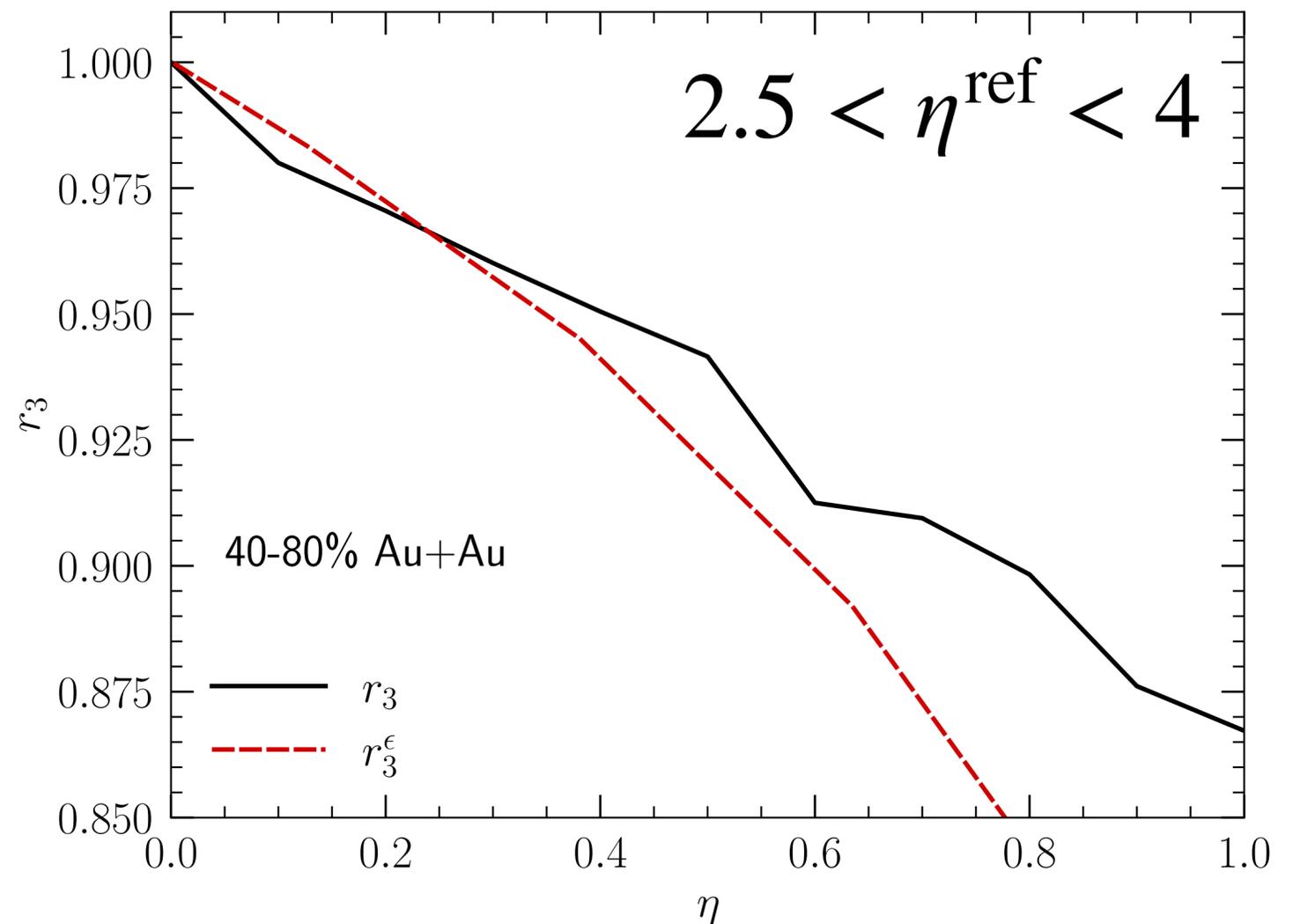
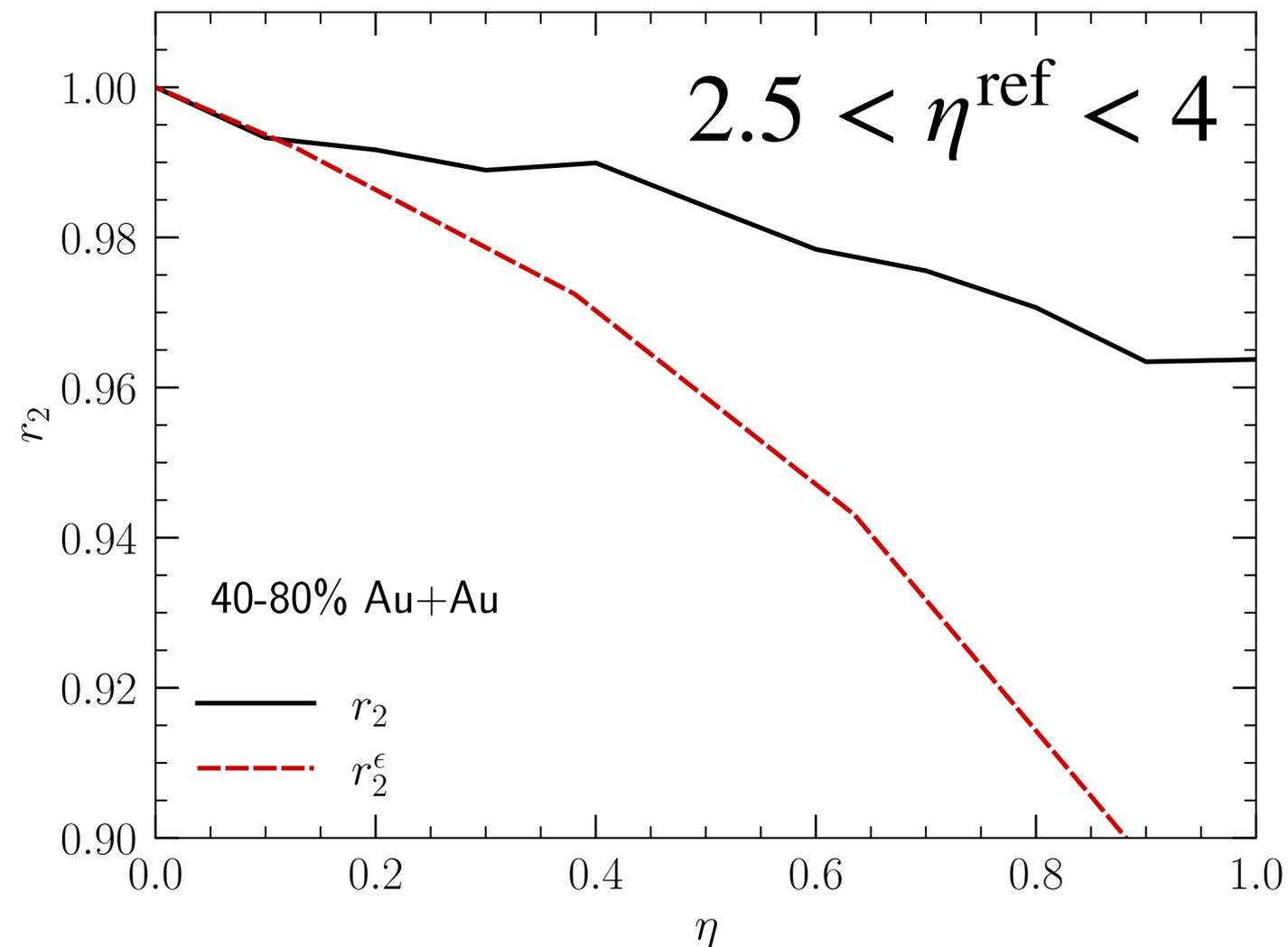
$$r_n = \frac{\langle Q_n(-\eta) Q_n(\eta^{\text{ref}})^* \rangle}{\langle Q_n(\eta) Q_n(\eta^{\text{ref}})^* \rangle}$$

$$r_n^{\mathcal{E}} = \frac{\langle \mathcal{E}_n(-\eta_s) \mathcal{E}_n(\eta_s^{\text{ref}})^* \rangle}{\langle \mathcal{E}_n(\eta_s) \mathcal{E}_n(\eta_s^{\text{ref}})^* \rangle}$$



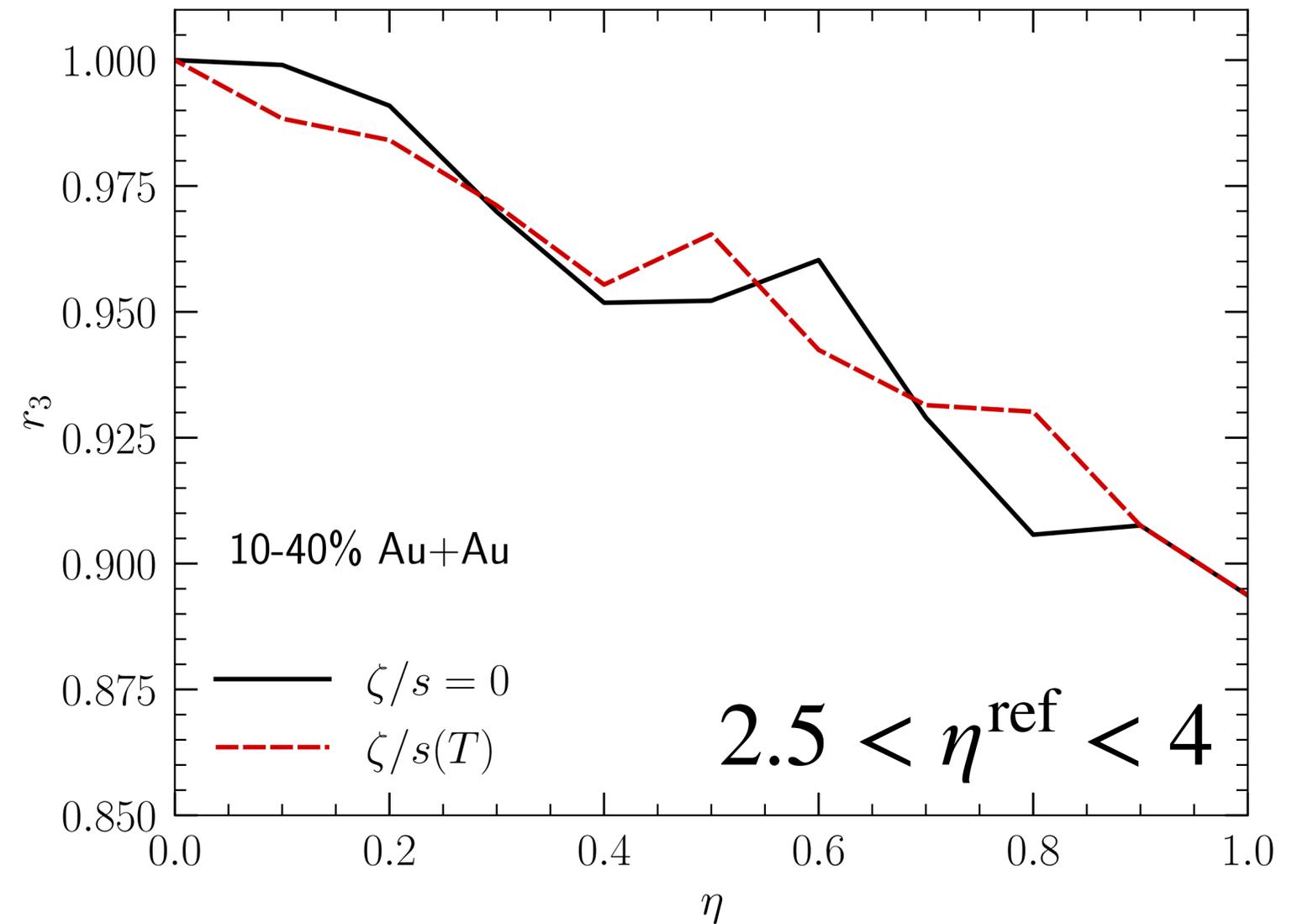
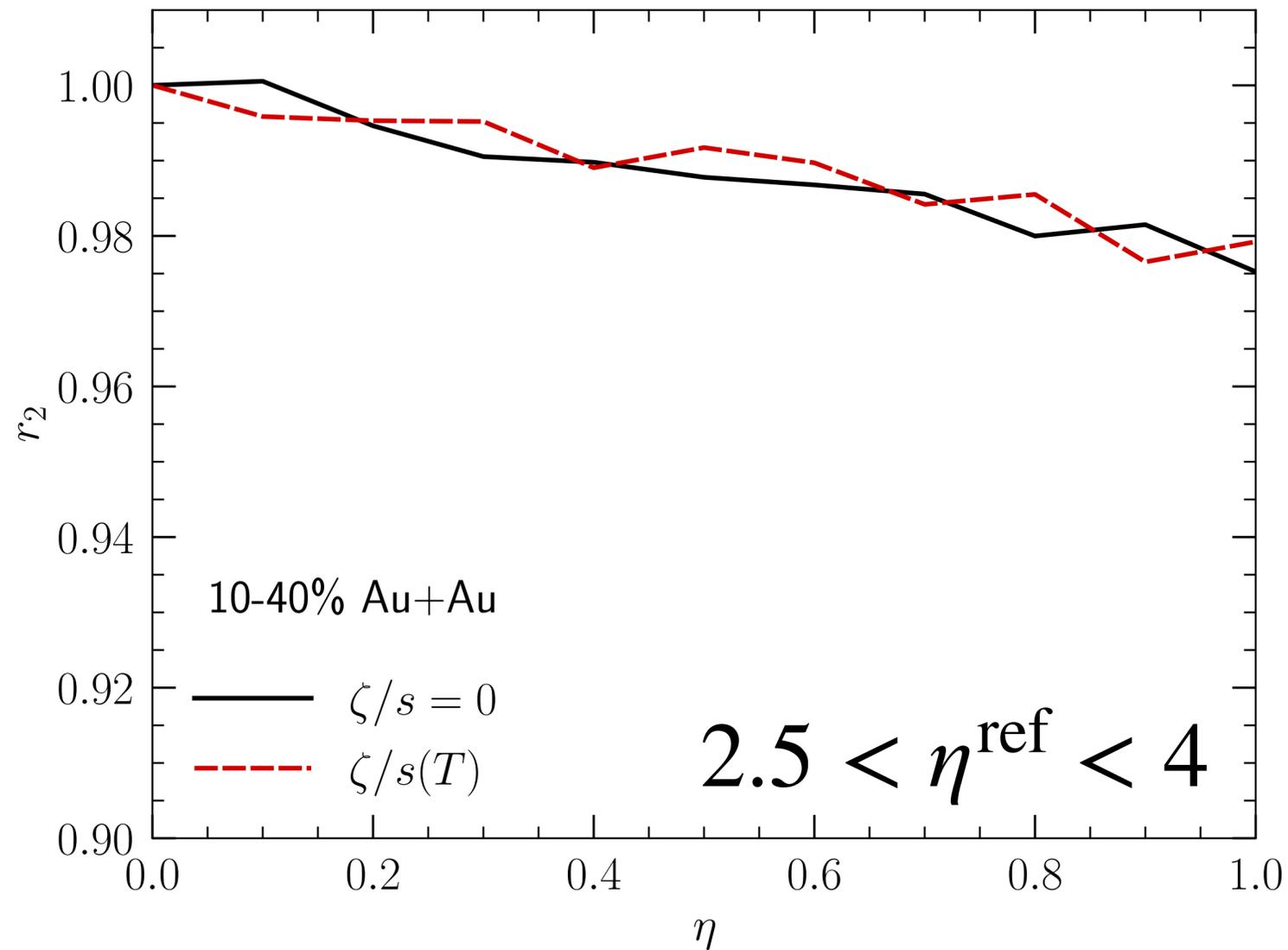
@ P. Bozek

# INITIAL STATE $r_n^\epsilon$ VS. FINAL STATE $r_n$



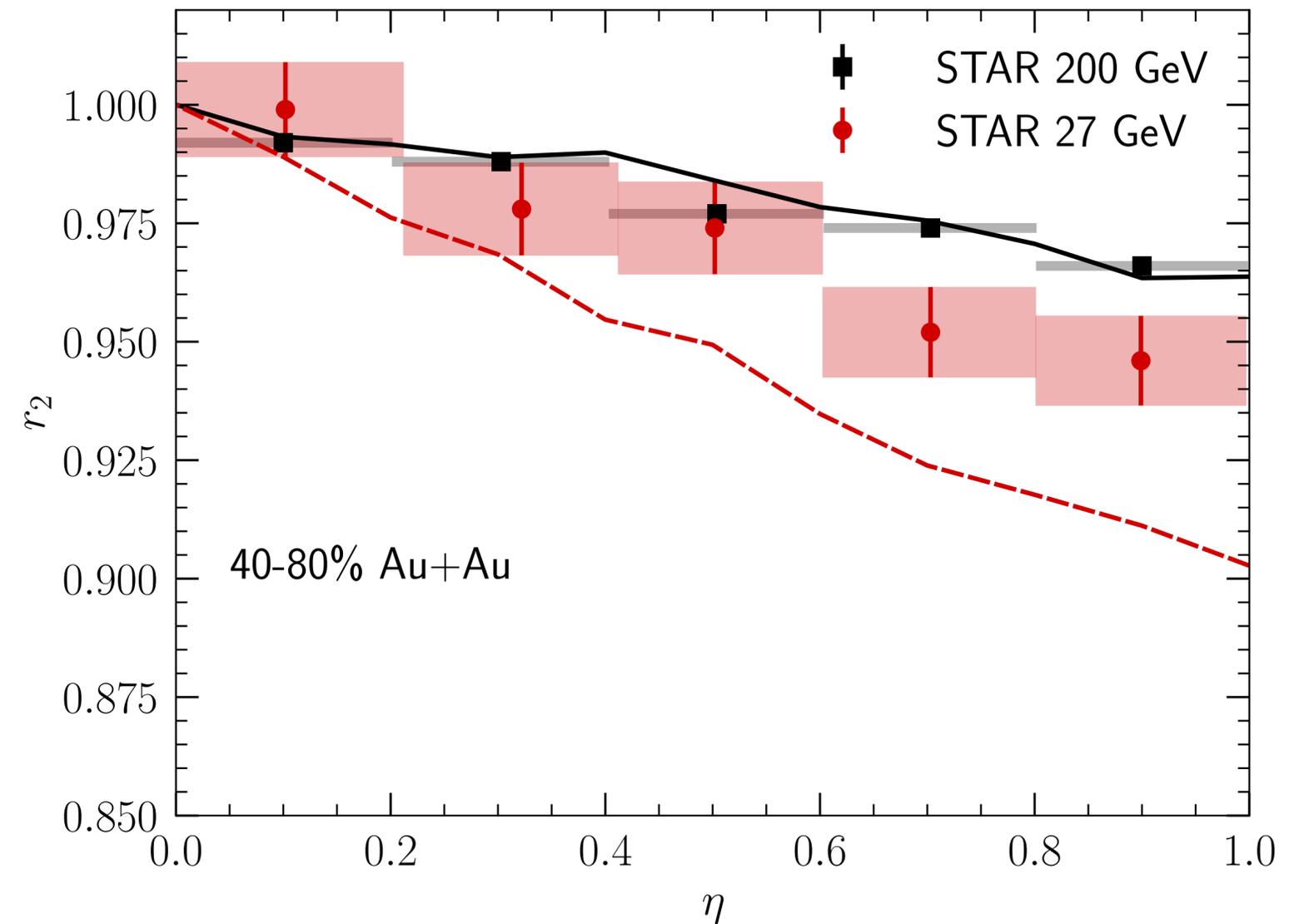
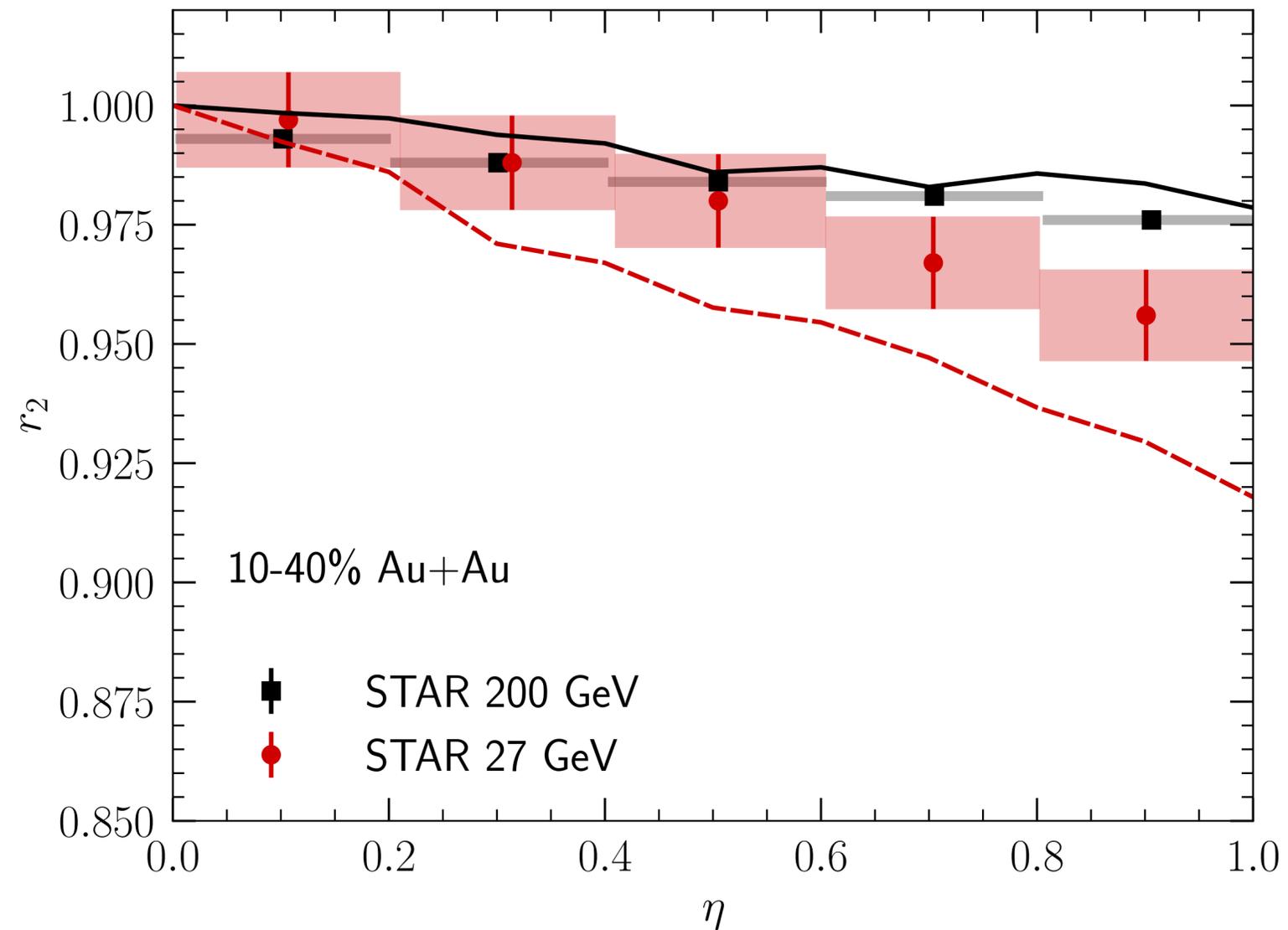
- The initial-state estimator overestimates the rapidity decorrelation

# BULK VISCOUS EFFECTS ON $r_n$



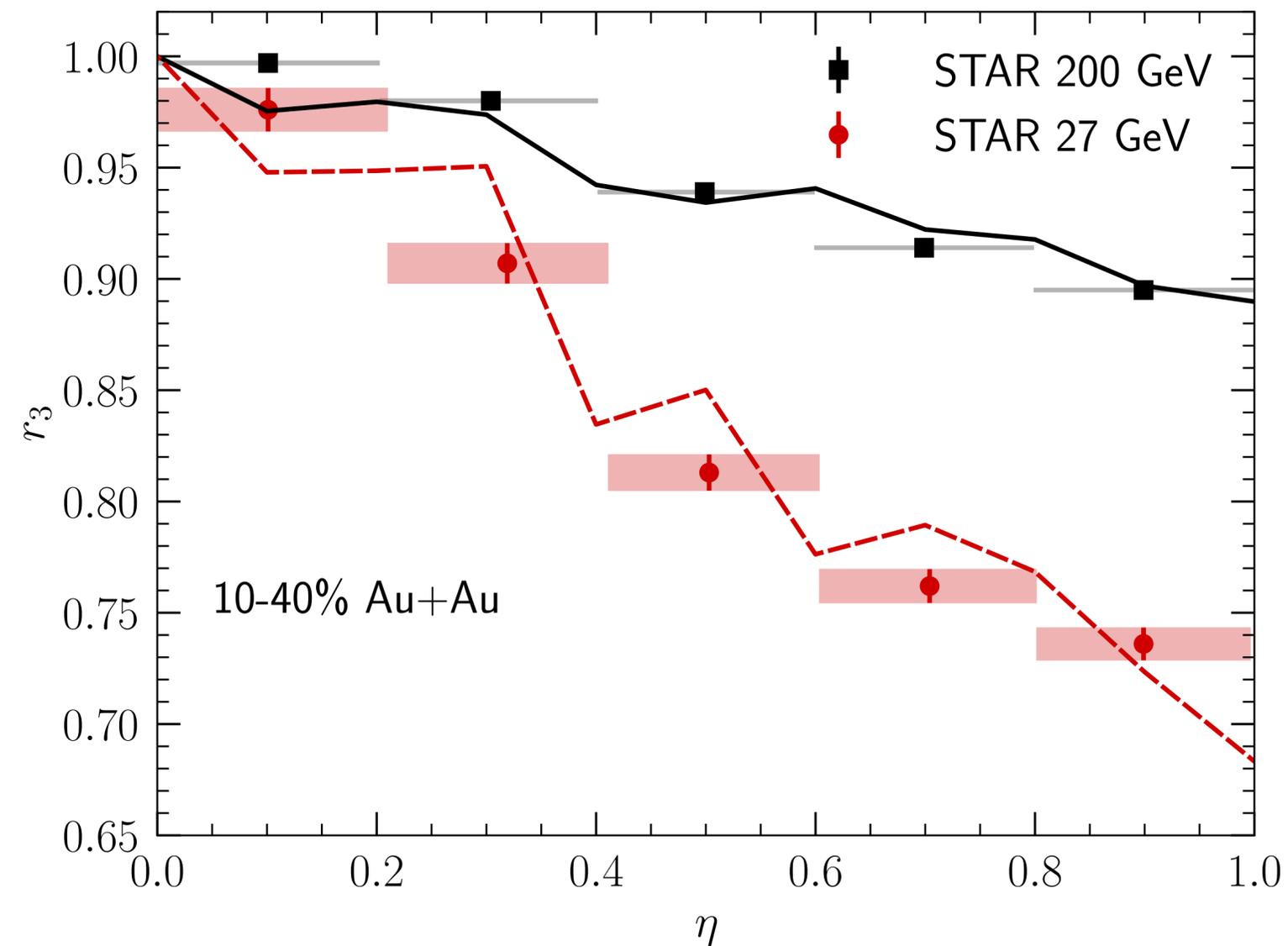
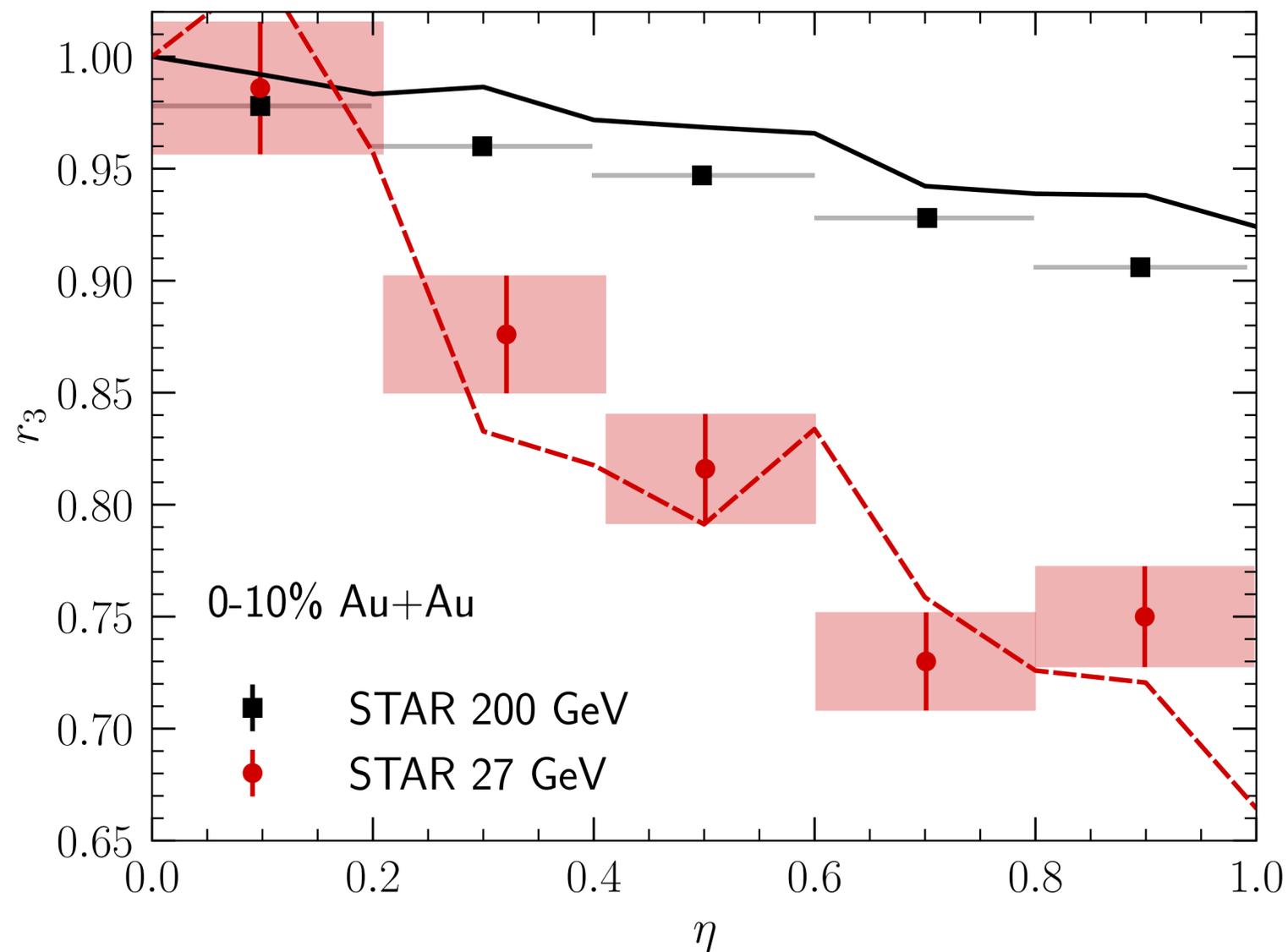
- Bulk viscosity does not have sizable effects on  $r_n$

# COLLISION ENERGY DEPENDENCE OF $r_n$



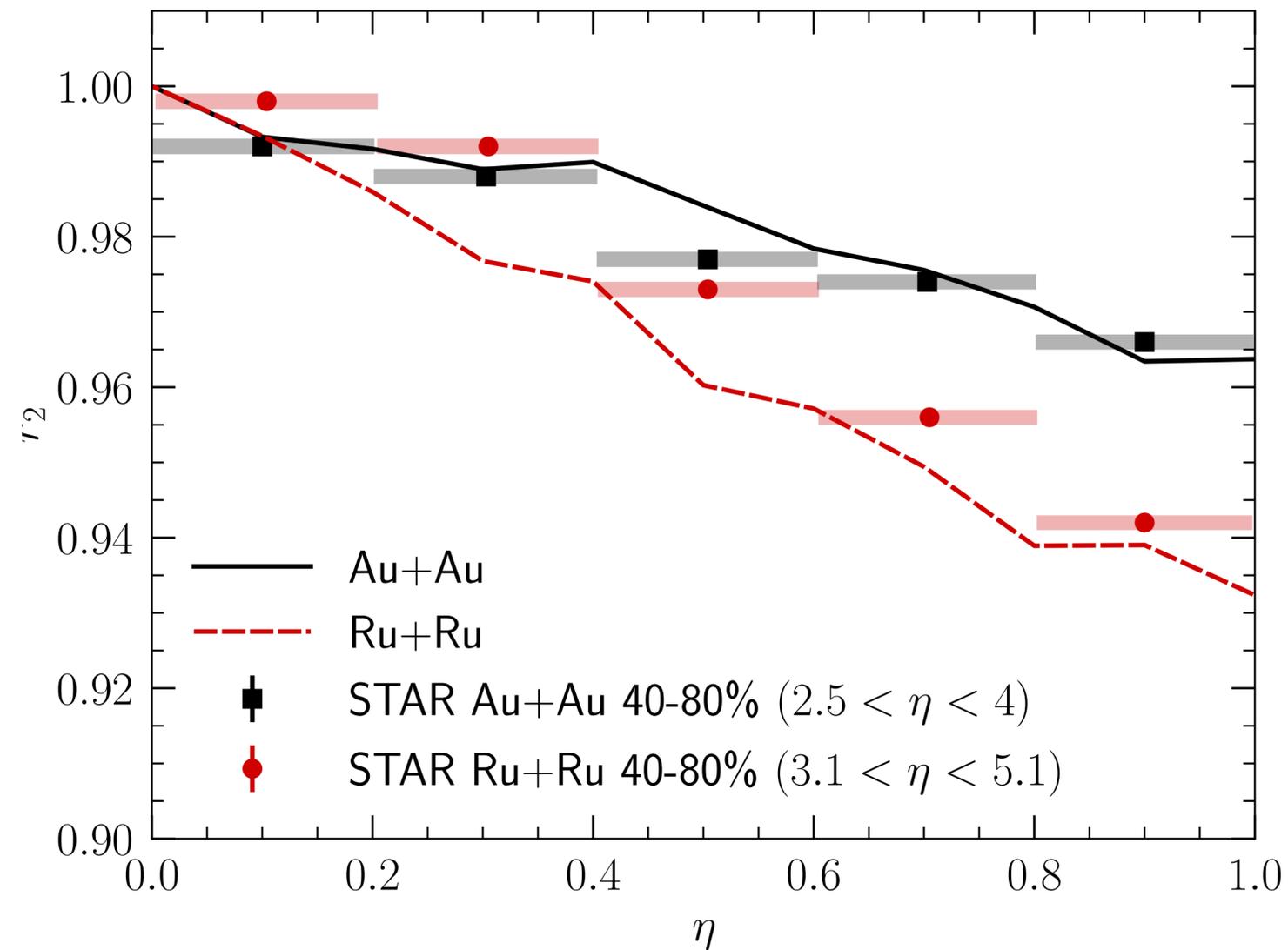
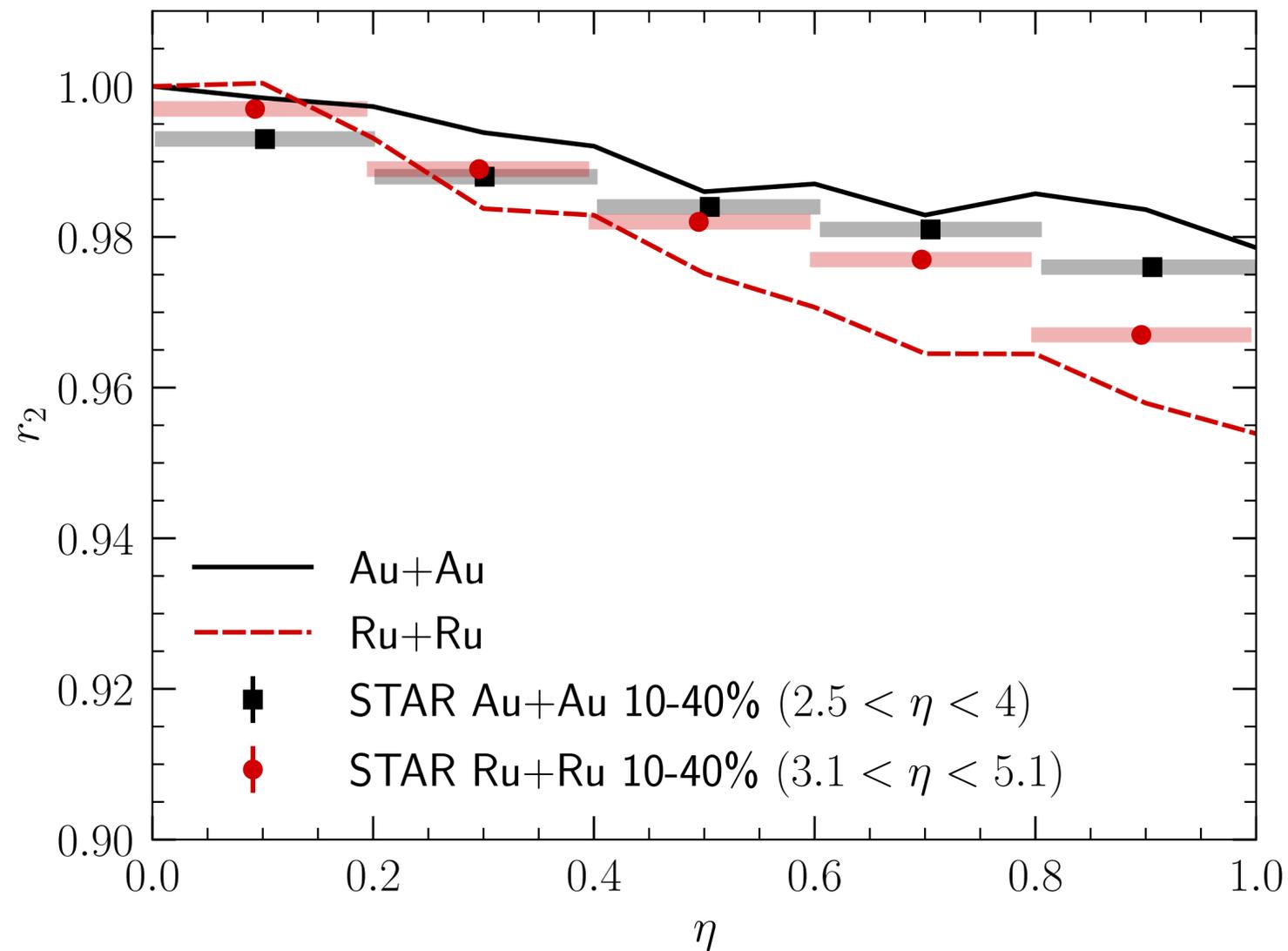
- Our model overestimated the elliptic flow decorrelation at 27 GeV

# COLLISION ENERGY DEPENDENCE OF $r_n$



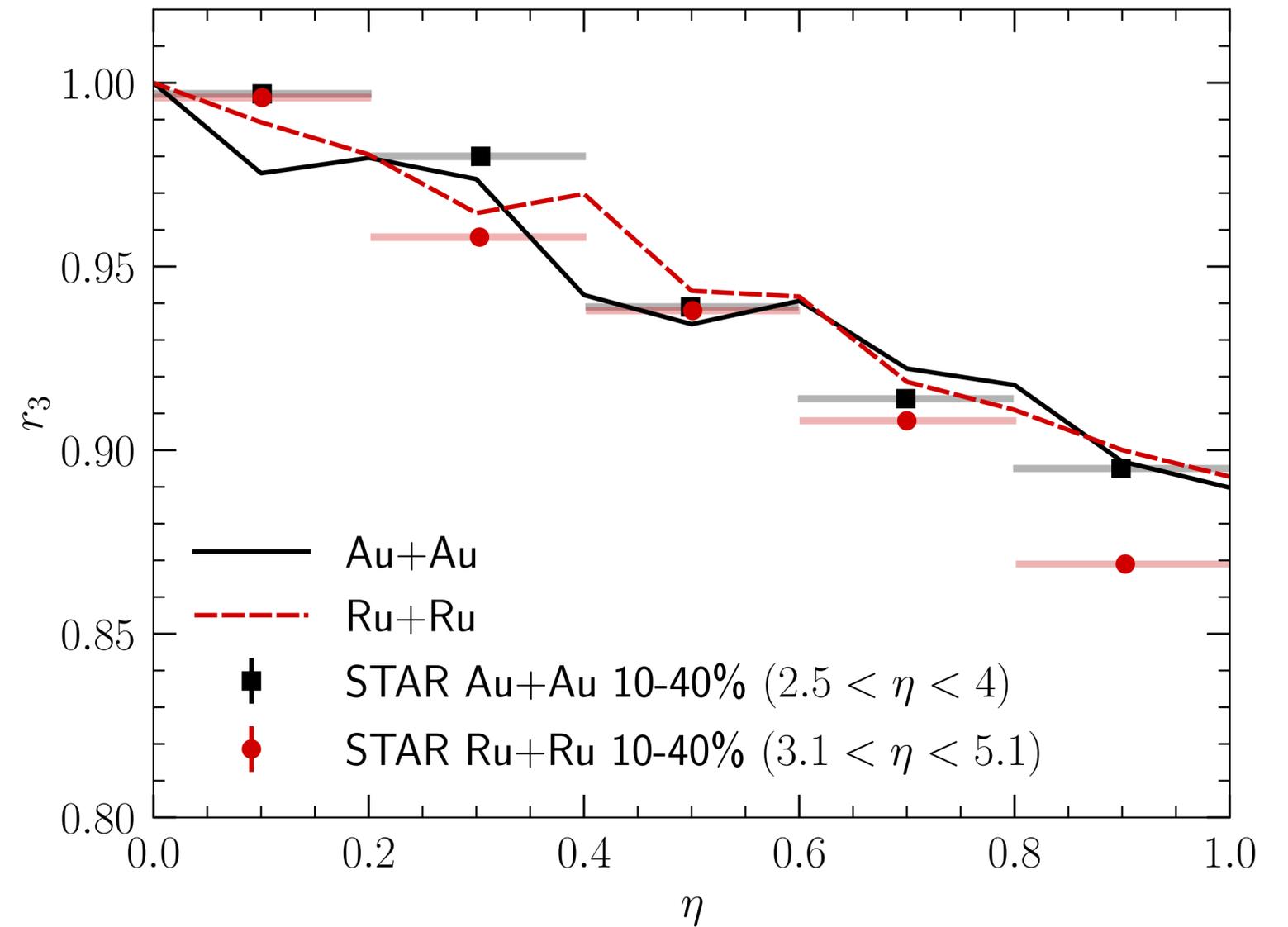
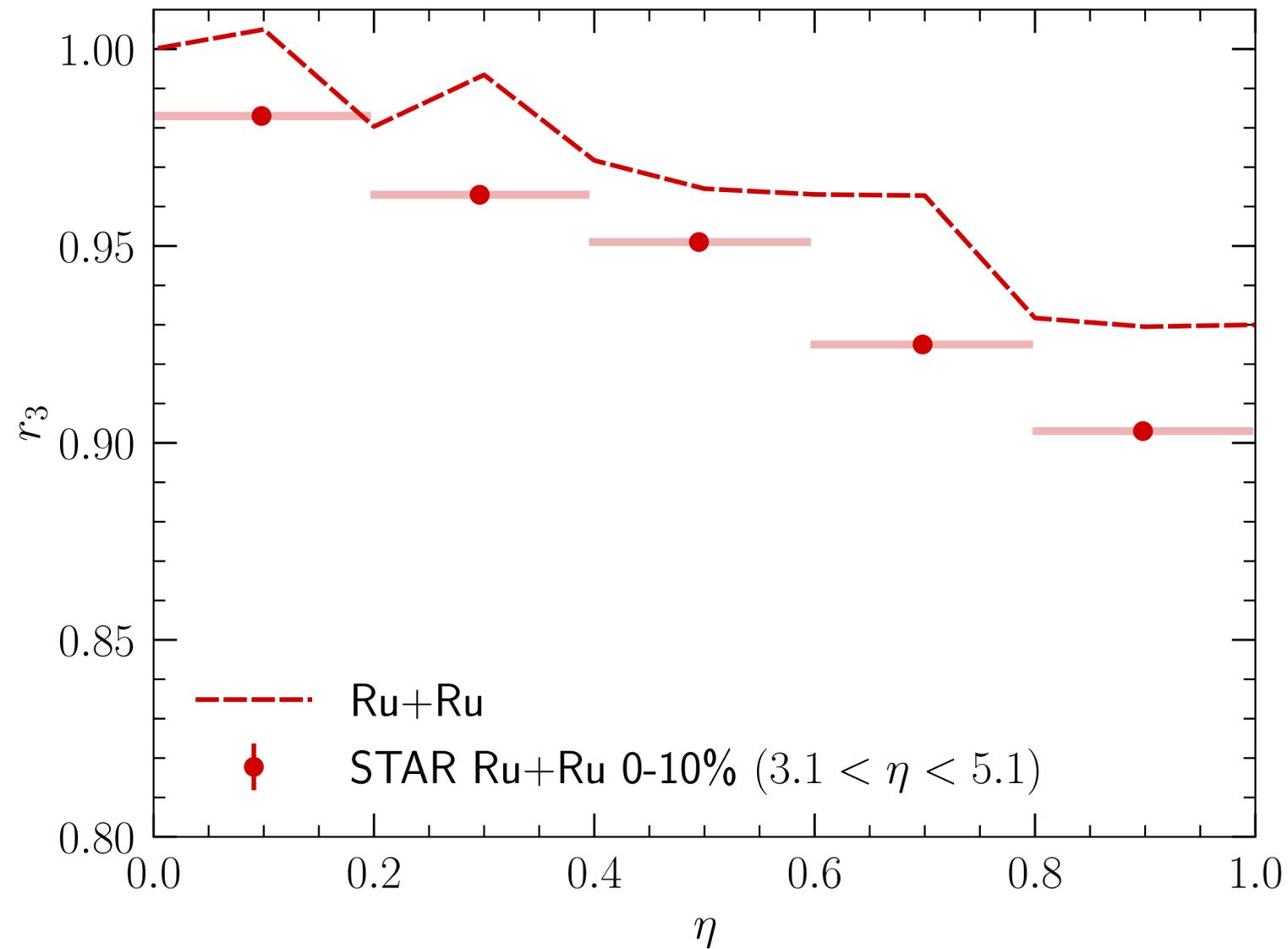
- Our model reproduces the triangular flow decorrelation at 200 and 27 GeV

# SYSTEM SIZE DEPENDENCE OF $r_n$



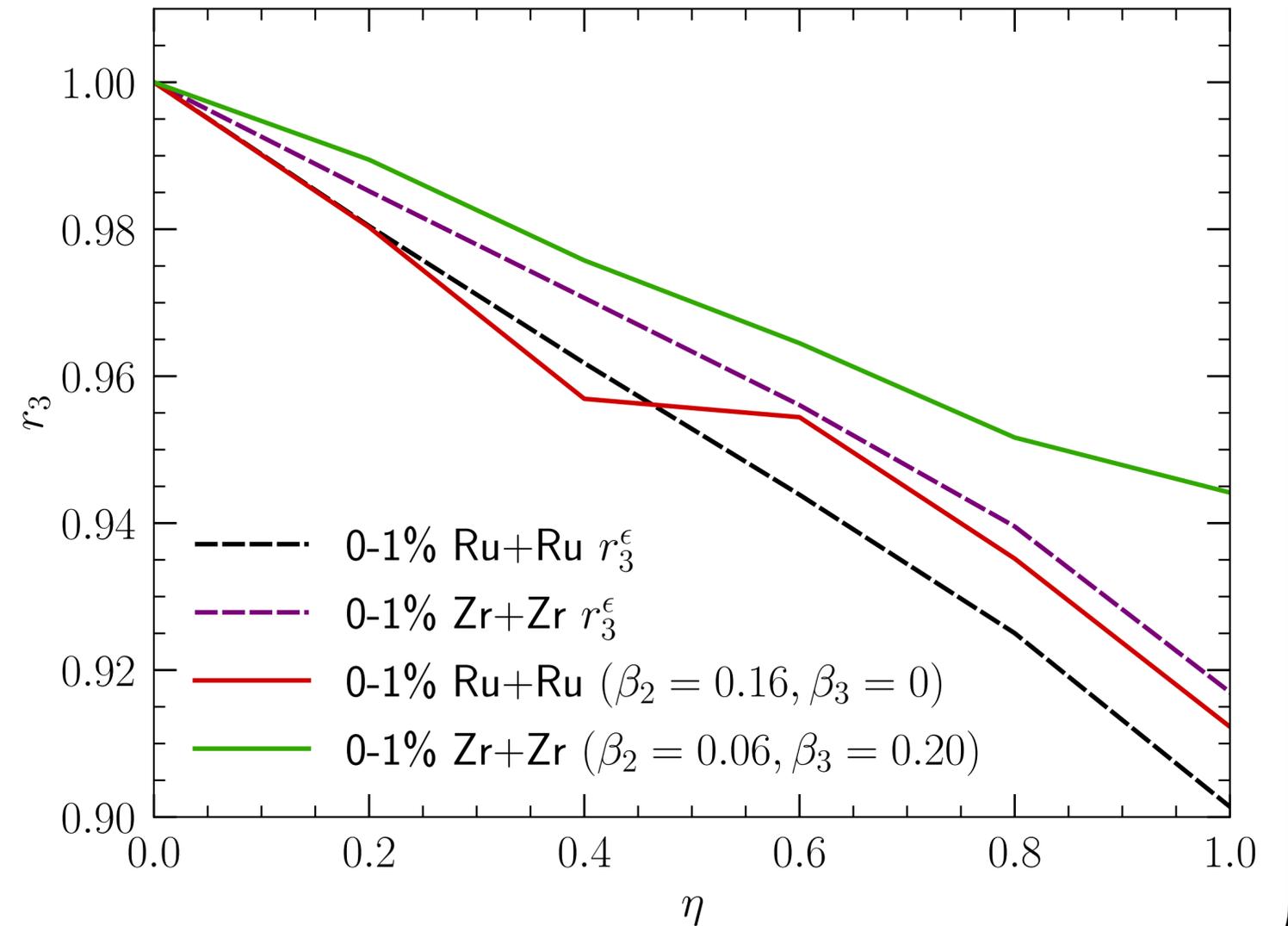
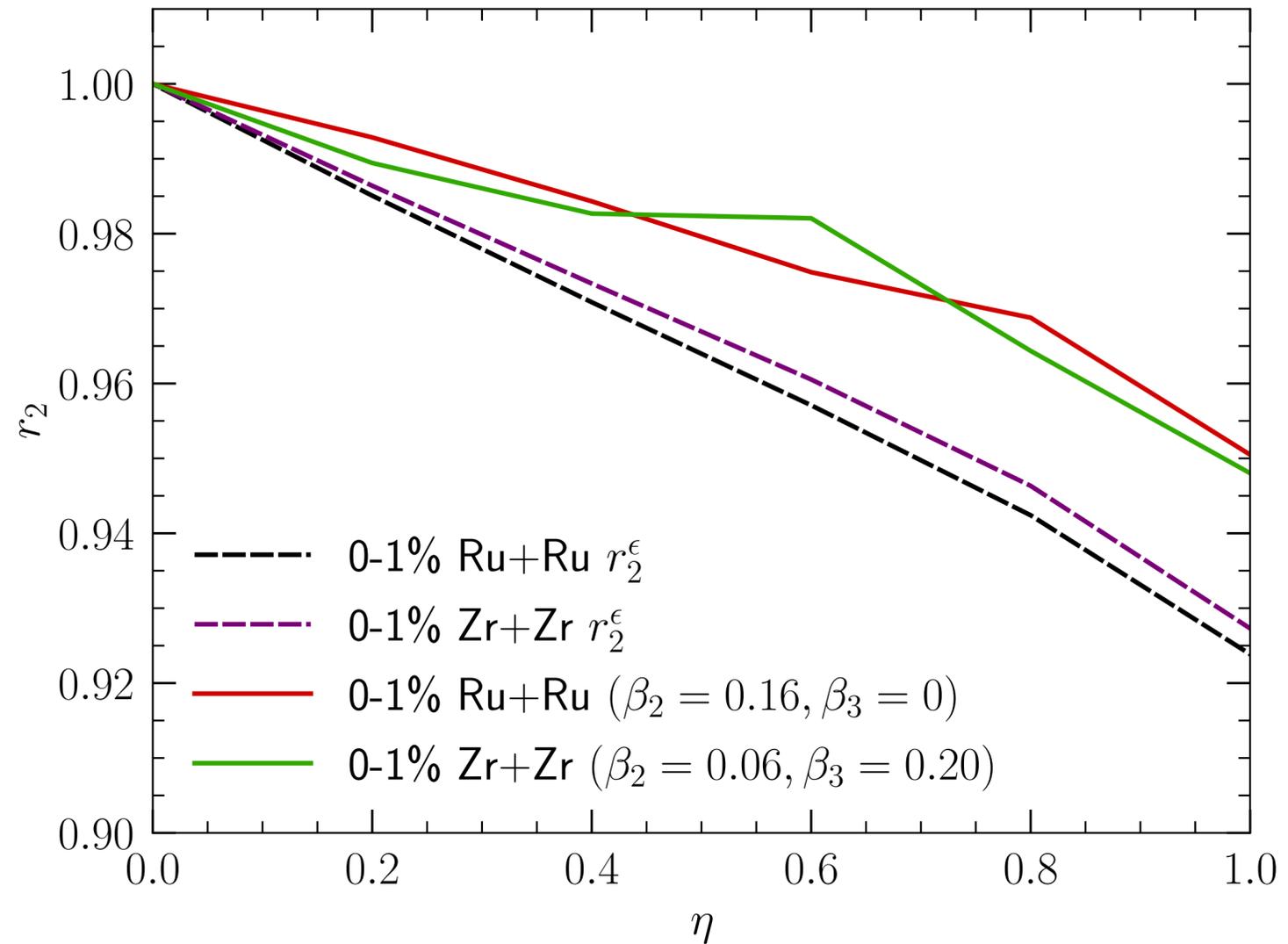
- The smaller Ru+Ru collisions have larger flow decorrelation with those in Au+Au collisions

# SYSTEM SIZE DEPENDENCE OF $r_n$



- Our model underestimated the  $r_3$  compared to the STAR measurements

# NUCLEAR STRUCTURE EFFECTS ON $r_n$ AT RHIC ISOBAR



- The non-zero  $\beta_3$  in Zr+Zr collisions results in a larger  $r_3$  than those in Ru+Ru collisions in central isobar collisions

# SUMMARY

- We developed an effective (3+1)D dynamical framework to understand particle production and flow in relativistic heavy-ion collisions for the RHIC beam energy scan program
  - First principle inputs from **lattice QCD** for EoS
  - Systematically study the **phase structure** (critical point) of hot QCD matter
  - Elucidating the **initial baryon stopping**, **charge diffusion**, and **transport properties** of QGP in a baryon rich environment
- The 3D MC-Glauber model qualitatively captures the system size and collision energy dependence of **flow rapidity decorrelation** in Au+Au and Isobar collisions at RHIC
- **We predict a smaller  $r_3$  in central Zr+Zr than Ru+Ru collisions as a consequence of the non-zero  $\beta_3$  deformation in Zr**