

Testing CKM Unitarity with the NA62 Experiment

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Testing the Standard Model in Charged-Weak Decays (INT-26-95W)

Seattle, WA, January 15, 2026

1st-row CKM Unitarity

Unitarity condition for 1st-row of CKM Matrix:

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \rightarrow |V_{ud}|^2 + |V_{us}|^2 + \cancel{|V_{ub}|^2} = 1$$

$\sim 0.949 \quad \sim 0.05 \quad \sim 2 \times 10^{-5}$

$$\Delta_{\text{CKM}} \cong |V_{ud}|^2 + |V_{us}|^2 - 1$$

- V_{ub} : measured from B meson decays ($B \rightarrow X_u \ell \bar{\nu}$, $B \rightarrow \pi \ell \bar{\nu}$), can ignore
- V_{ud} : most precise determination from super-allowed nuclear β decays

$$|V_{ud}| = 0.97367(11)_{\text{exp}}(13)_{\text{Rad.Cor.}}(27)_{\text{Nucl.}}$$

- **Focus on determination of V_{us} and V_{us} / V_{ud} from kaon decays**

V_{us} from $K_{\ell 3}$ decays

$$\Gamma(K_{\ell 3}) = |V_{us}|^2 \frac{C_K^2 G_f^2 m_K^5}{192\pi^3} S_{EW} |f_+^{K^0\pi^-}|^2 I_{K\ell}(\lambda_{K\ell}) \left(1 + 2\Delta_K^{SU(2)} + 2\Delta_{K\ell}^{EM}\right)$$

where $K \in [K^+, K^0]$, $\ell \in [e, \mu]$, $C_K^2 = \begin{cases} \frac{1}{2} & \text{for } K^+ \\ 1 & \text{for } K^0 \end{cases}$

$S_{EW} = 1.0232$: universal Short-Distance EW Correction

Experiment:

- $\Gamma(K_{\ell 3})$: branching ratios for K_S , K_L , K^\pm , and kaon lifetimes
- $I_{K\ell}(\lambda_{K\ell})$: integral of form factor over phase space
 - K_{e3} : Only λ_+ (or λ_+' , λ_+'')
 - $K_{\mu 3}$: need λ_+ and λ_0

Theory:

- $f_+^{K^0\pi^-}$: hadronic matrix element (form factor) at zero momentum transfer ($t=0$)
- $\Delta_K^{SU(2)}$: Form factor correction for SU(2) breaking
- $\Delta_{K\ell}^{EM}$: Form factor correction for Long-Distance EM effects

V_{us} / V_{ud} from $K_{\mu 2}$ and $K_{\pi 2}$ decays

$$\frac{|V_{us}|}{|V_{ud}|} \frac{f_K}{f_\pi} = \left(\frac{\Gamma_{K\mu 2(\gamma)} m_{\pi^\pm}}{\Gamma_{\pi 2(\gamma)} m_{K^\pm}} \right)^{1/2} \frac{1 - m_\mu^2/m_{\pi^\pm}^2}{1 - m_\mu^2/m_{K^\pm}^2} \left(1 - \frac{1}{2} \delta_{\text{EM}} - \frac{1}{2} \delta_{SU(2)} \right)$$

Experiment:

- $\Gamma_{K\mu 2(\gamma)}$: branching ratio $\text{Br}(K_{\mu 2})$ and lifetime τ_{K^\pm} from fit to K^\pm decays
- $\Gamma_{\pi 2(\gamma)}$: branching ratio $\text{Br}(\pi_{\mu 2})$ and lifetime τ_{π^\pm} from PDG

Theory:

- f_K/f_π : ratio of decay constants
- δ_{EM} : long-distance EM corrections
- $\delta_{SU(2)}$: strong isospin breaking
 $f_K/f_\pi \rightarrow f_{K^\pm}/f_{\pi^\pm}$

$$\frac{|V_{us}|}{|V_{ud}|} \frac{f_K}{f_\pi} = 0.27679(28)_{\text{Br}}(20)_{\text{corr}}$$

See: [Boyle et al. \(JHEP 2023\)](#)

Status of 1st-row CKM Unitarity

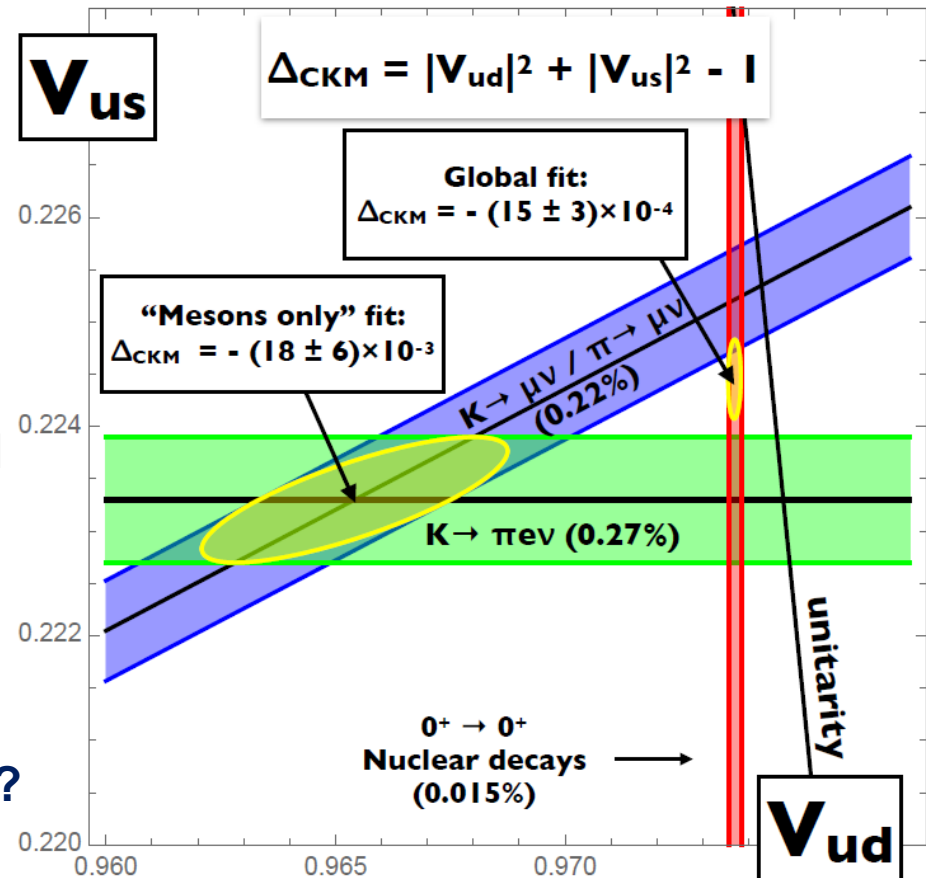
$$\Delta_{\text{CKM}} \cong |V_{ud}|^2 + |V_{us}|^2 - 1$$

	Value	% Error
V_{ud}	0.97373 ± 0.00031	0.032
$V_{us}(K_{\ell 3})$	0.2231 ± 0.0007	0.31
$V_{us}(K_{\mu 2})$	0.2252 ± 0.0005	0.22

Existing tensions:

- 3 σ deficit in global fit for 1st row CKM unitarity: **Cabibbo angle anomaly**
- 2.6 σ discrepancy in $|V_{us}|$ from average of $K_{\ell 3}$ ($\ell = e, \mu$) modes vs $K_{\mu 2}$ mode

Need for additional experimental data?



Impact of New Measurements

[Cirigliano, Crivellin, Hoferichter, Moulson \(Phys.Lett.B 2023\)](#)

	current fit	$K_{\mu 3} / K_{\mu 2}$ BR at 0.5%		
		central	+2 σ	-2 σ
$\Delta_{\text{CKM}}^{(1)}$	-0.00176(56) -3.1 σ	-0.00173(55) -3.1 σ	-0.00162(56) -2.9 σ	-0.00185(56) -3.3 σ
$\Delta_{\text{CKM}}^{(2)}$	-0.00098(58) -1.7 σ	-0.00098(58) -1.7 σ	-0.00108(58) -1.9 σ	-0.00087(58) -1.5 σ
$\Delta_{\text{CKM}}^{(3)}$	-0.0164(63) -2.6 σ	-0.0157(60) -2.6 σ	-0.0118(62) -1.9 σ	-0.0202(63) -3.2 σ

- Measurement of $\text{Br}(K_{\mu 3}) / \text{Br}(K_{\mu 2})$ could help resolve or confirm discrepancy in $K_{\ell 3}$ vs $K_{\mu 2}$ modes
- Additional measurement of V_{us} / V_{ud} and V_{us} by NA62 could impact 1st-row CKM unitarity test

$$\Delta_{\text{CKM}}^{(1)} = |V_{ud}^{\beta}|^2 + |V_{us}^{K_{\ell 3}}|^2 - 1,$$

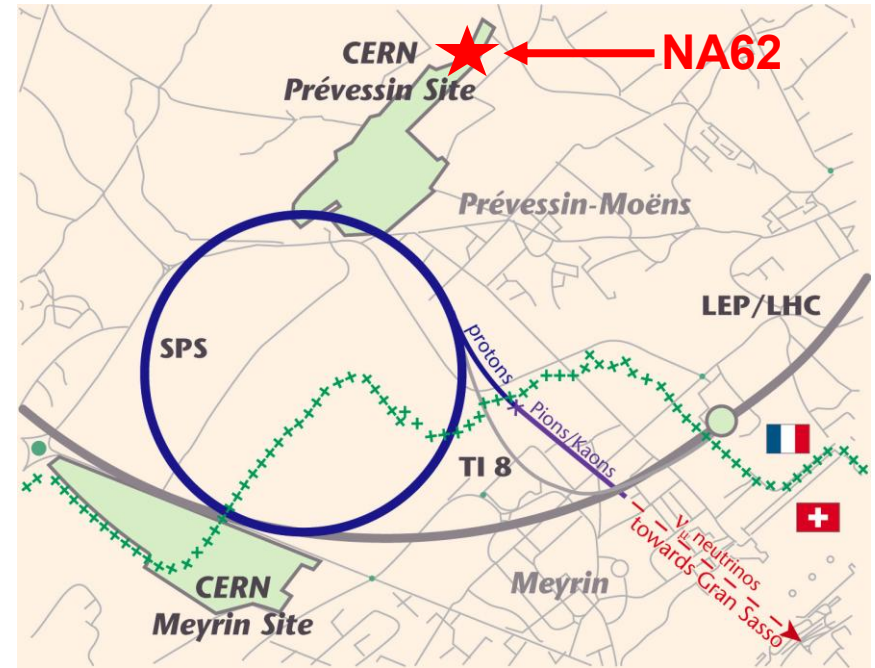
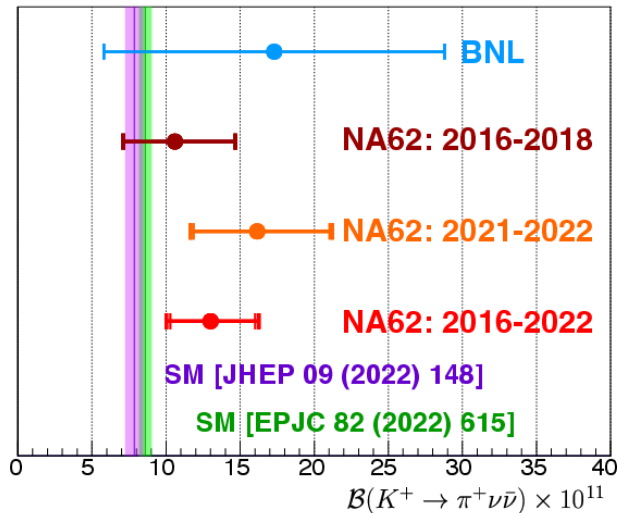
$$\Delta_{\text{CKM}}^{(2)} = |V_{ud}^{\beta}|^2 + |V_{us}^{K_{\ell 2}/\pi_{\ell 2}, \beta}|^2 - 1,$$

$$\Delta_{\text{CKM}}^{(3)} = |V_{ud}^{K_{\ell 2}/\pi_{\ell 2}, K_{\ell 3}}|^2 + |V_{us}^{K_{\ell 3}}|^2 - 1,$$

The NA62 Experiment

Fixed target kaon decay experiment located at the CERN Prévessin site

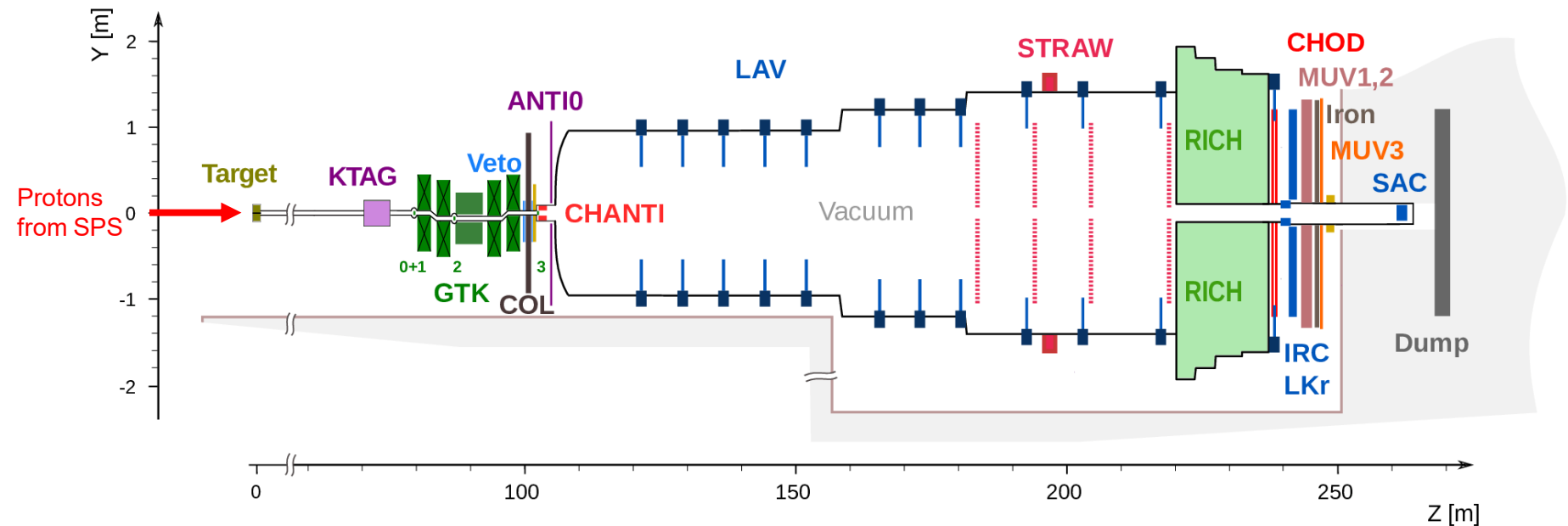
- 400 GeV/c proton beam from Super Proton Synchrotron (SPS) directed at beryllium target
- Produces secondary 75 GeV/c kaon beam (70% π^+ , 23% p, **6% K^+**)
- Primary goal: to measure rare decay
 $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (13.0^{+3.3}_{-3.0}) \times 10^{-11}$
[*JHEP 02 \(2025\) 191](#)



Broader physics program:

- Rare and forbidden K^+ decays, hidden sectors, exotics
- **Precision Measurements**
 $(K^+ \rightarrow \mu^+ \nu, K^+ \rightarrow \pi^0 \mu^+ \nu, K^+ \rightarrow \pi^+ \pi^0)$

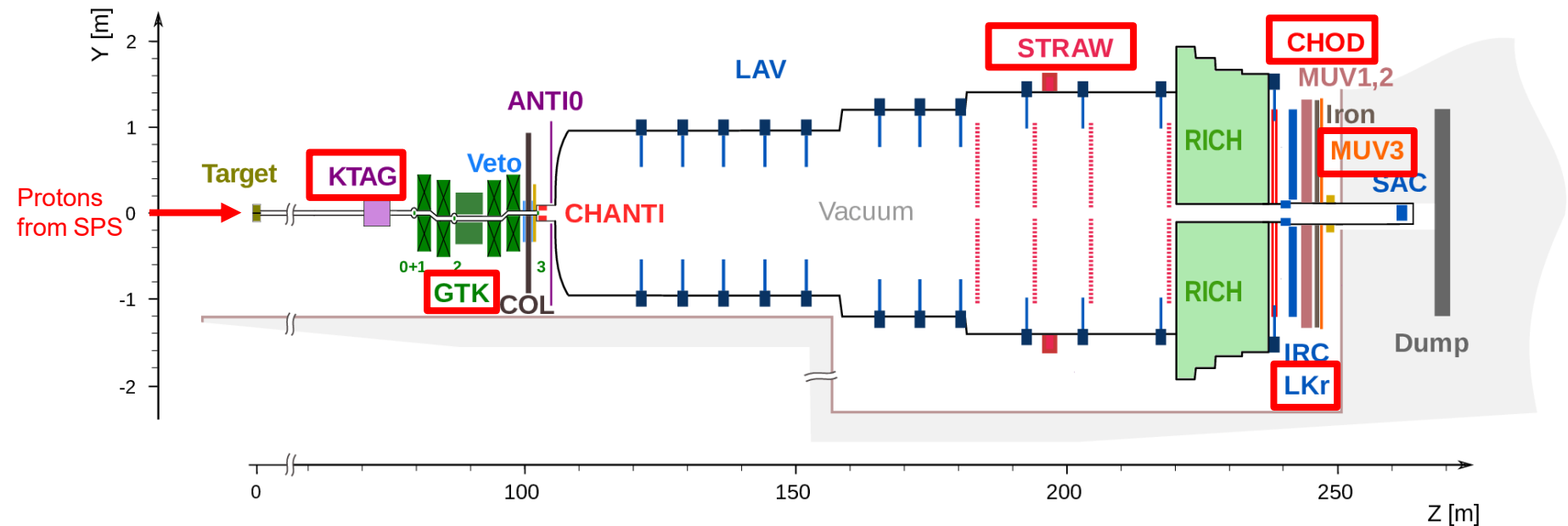
The NA62 Detector



Comprehensive system for measuring kaon decays:

- Particle tracking: GTK, STRAW
- Calorimeters: LKr, MUV1, MUV2
- Particle identification: KTAG, MUV3, RICH
- Trigger and Veto systems: CHOD, CHANTI, ANTI-0, SAC, IRC, LAV

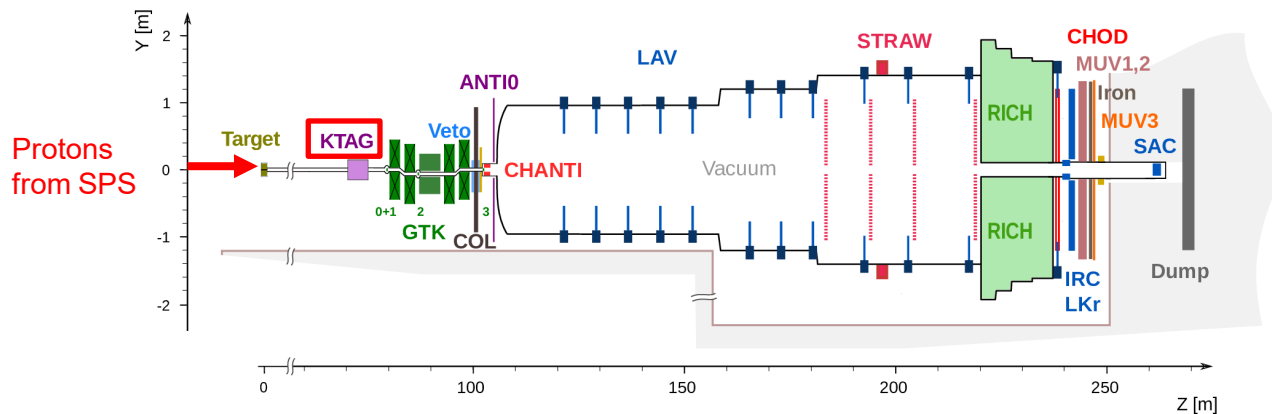
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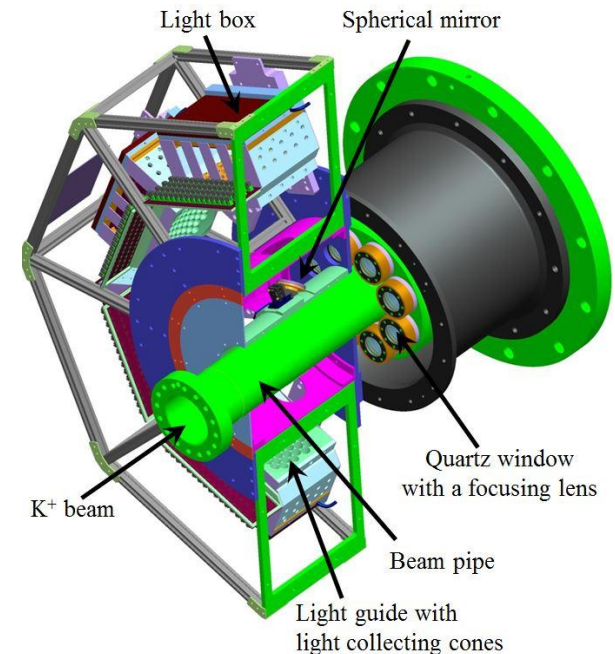
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The NA62 Detector

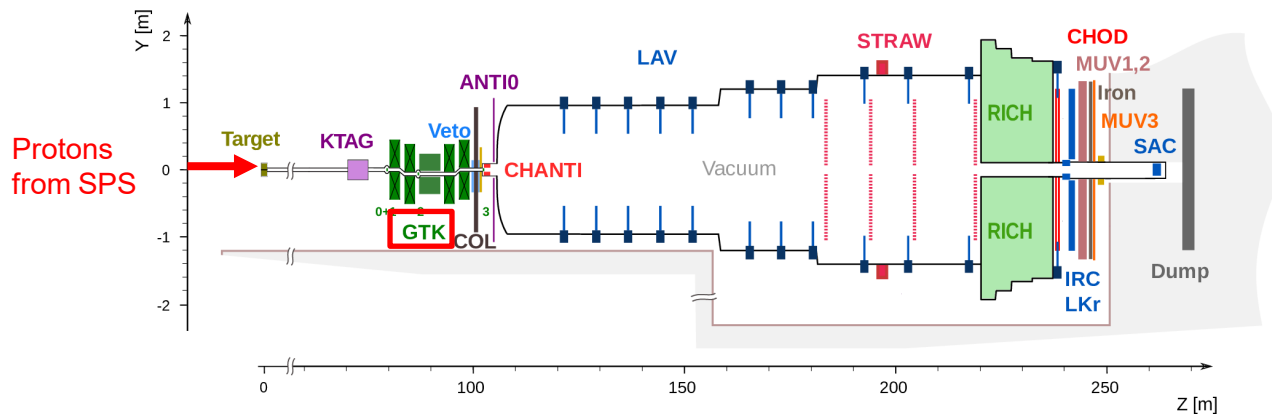


Kaon tagger (KTAG):

- Differential Cherenkov counter for tagging beam kaons
- 70 ps timing resolution
- >95% kaon tagging efficiency, pion misidentification rate $O(10^{-4})$

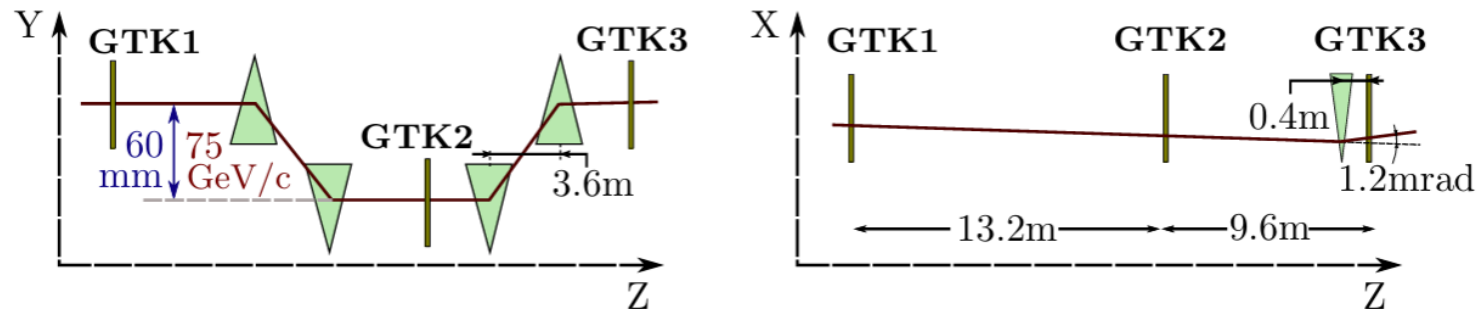


The NA62 Detector

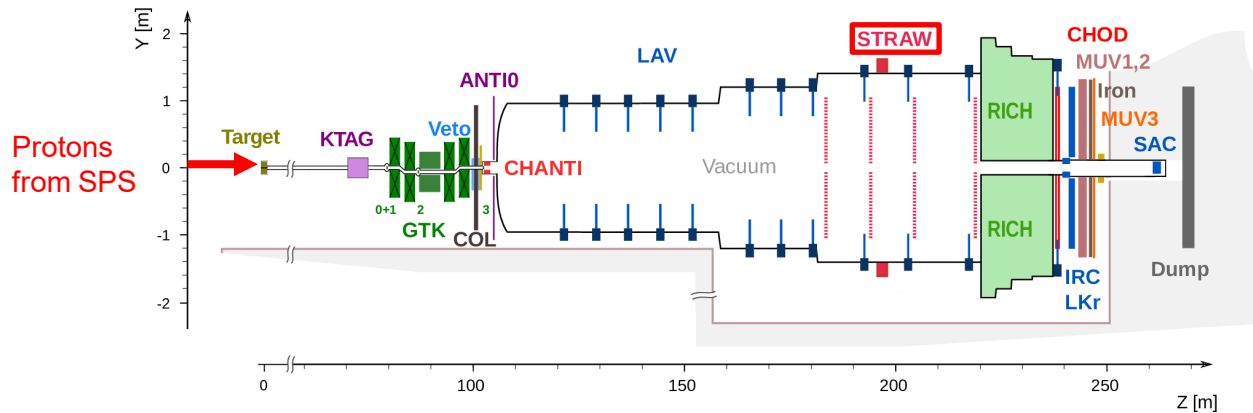


Gigatracker (GTK):

- Silicon hybrid pixel beam spectrometer for measuring beam momentum
- Needed for computing missing mass squared $m_{\text{miss}}^2 = (p_{K^+} - p_{\text{track}})^2$
- 100 ps time resolution, 0.15 GeV/c momentum resolution

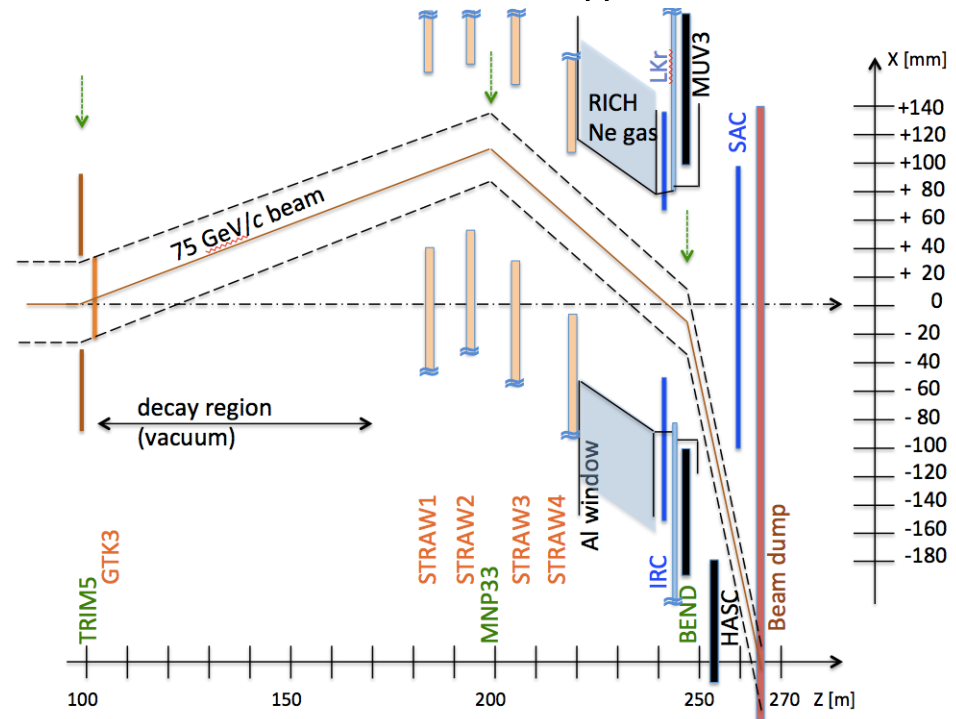


The NA62 Detector

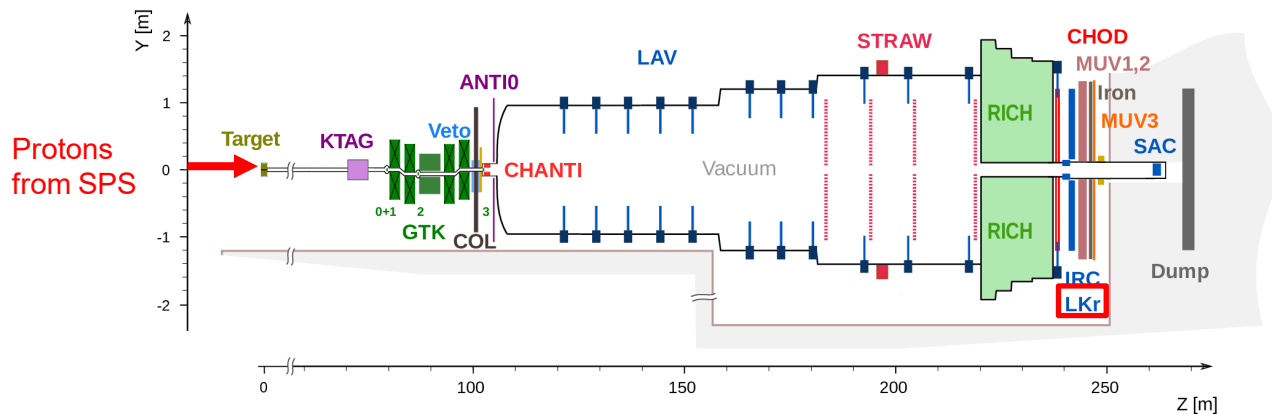


Straw Tracker:

- Four chambers in $\{x, y, u, v\}$ planes, two both upstream and downstream of dipole magnet (MNP33)
- Measures momentum of charged particles (K^+ , π^+ , μ^+)
- 130 μm spatial resolution
- $\sigma_p/p = (0.30 \oplus 0.005 \cdot p)\%$

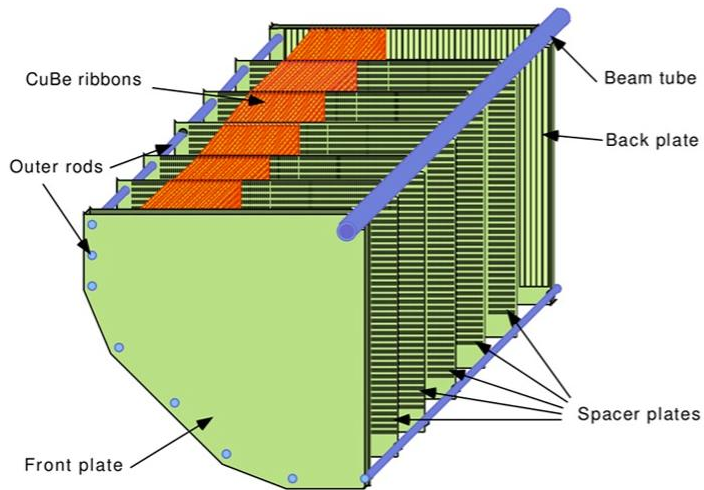


The NA62 Detector

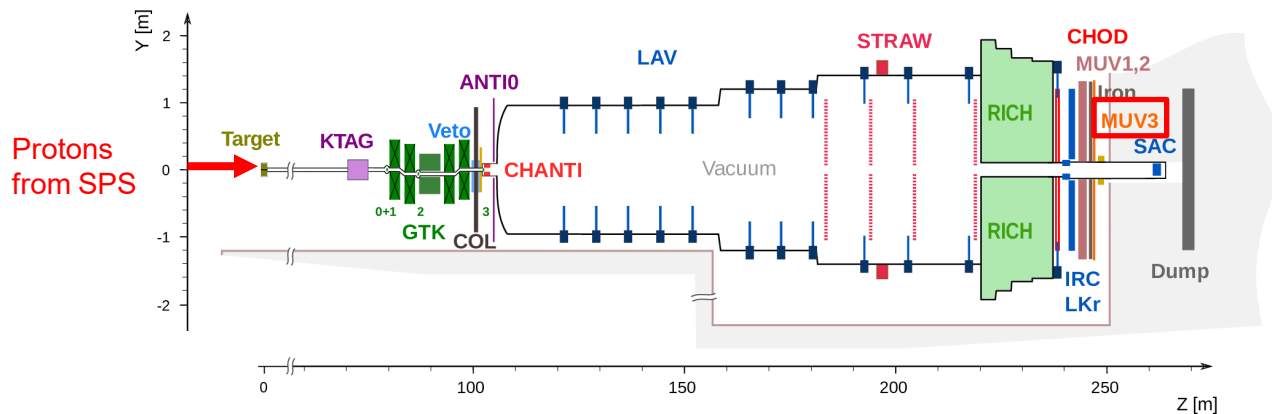


Liquid Krypton Calorimeter (LKr):

- Measures energy, position and timing of photons → infer presence of π^0
- 1 mm spatial resolution, 0.5 – 1 ns time resolution
- $\sigma_E/E = (4.8/\sqrt{E} \oplus 11/E \oplus 0.9)\%$

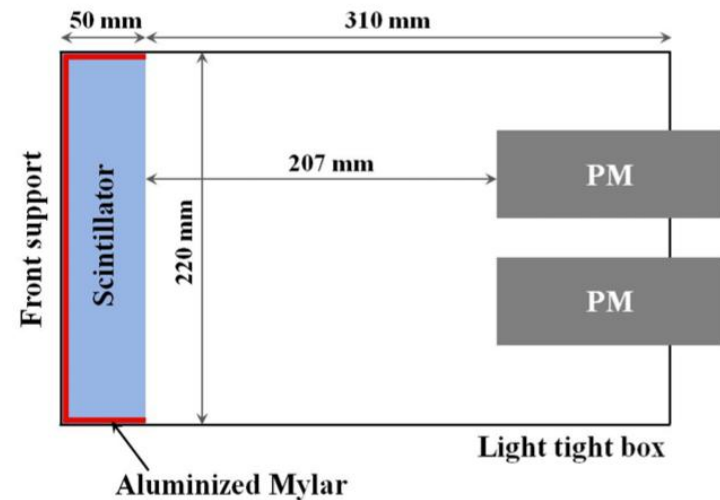


The NA62 Detector

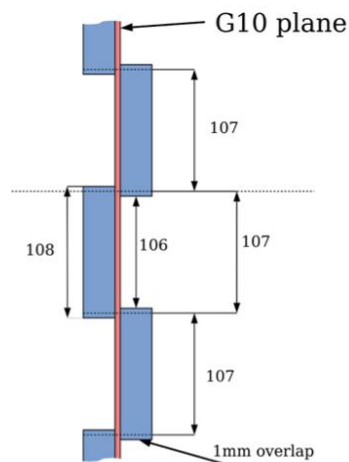
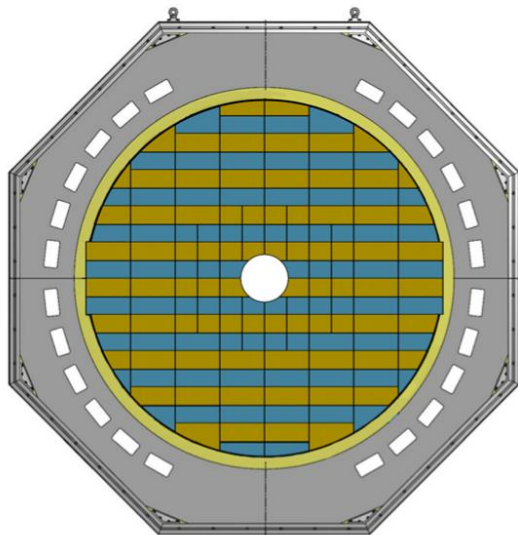
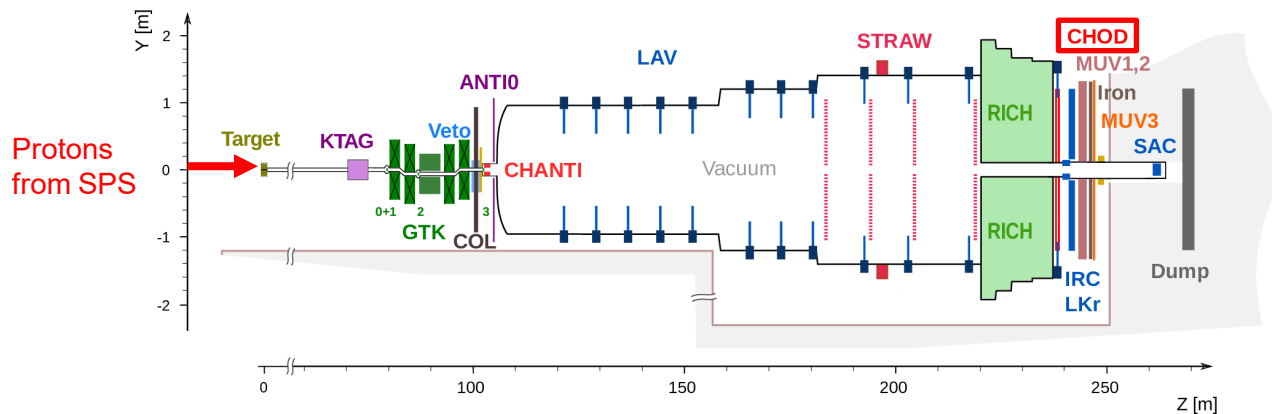


Muon Veto Station (MUV3):

- muon tagger (hit in-time with STRAW track)
- >99% muon detection efficiency
- Misidentification rate $O(<10^{-5})$
- ~500 ps time resolution



The NA62 Detector



Charged hodoscopes (CHOD):

- Two scintillator hodoscopes: matrix of tiles (CHOD) and two planes of slabs (NA48-CHOD)
- 1 ns (CHOD) and 200 ps (NA48-CHOD) time resolution
- Acts as L0 trigger

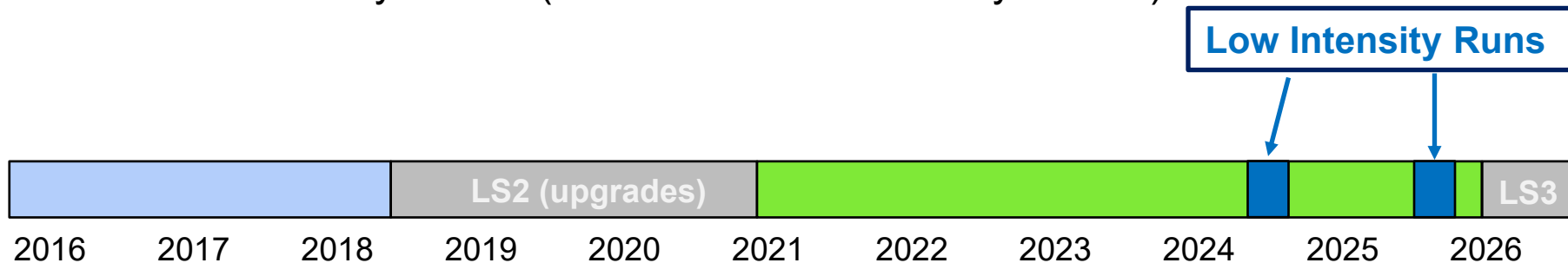
Data Set

Normal data taking conditions at ~ 750 MHz hadron beam, ~ 4.5 MHz of kaon decays in fiducial region

- Required for reaching $O(10^{13})$ total kaon decays for $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$
- Large amount of overlapping events (pileup) \rightarrow more difficult to properly simulate detector effects (i.e. worse Data/MC agreement)

Take dedicated low intensity runs at $\sim 1\%$ nominal intensity instead:

- Use **minimum bias trigger** (CHOD + STRAW) for measurement, **control trigger** (NA48-CHOD + STRAW) for systematic + efficiency studies
- Stable conditions, low overlap \rightarrow better handle on systematic uncertainties (i.e. better Data/MC agreement)
- One week of data taking in 2024 and 2025 sufficient to ensure uncertainties are not statistically limited ($< 0.1\%$ for main K^+ decay modes)



Measuring V_{us} / V_{ud}

Use NA62 to measure ratio of $\Gamma(K^+ \rightarrow \mu^+ \nu)$ to $\Gamma(\pi^+ \rightarrow \mu^+ \nu)$:

- $\Gamma(\pi^+ \rightarrow \mu^+ \nu)$ determined from $K^+ \rightarrow \pi^+ \pi^0$ muon DIF decays
- Determine relative yields from maximum likelihood fit of shape templates from Monte Carlo (MC) simulation to **missing mass squared distributions** ($m_{K^+ - \mu^+}^2$)
- Multi-bin shape template fit for $K^+ \rightarrow \pi^+ \pi^0$ to separate from $K^+ \rightarrow \pi^0 \mu^+ \nu$ background, single bin fit (i.e. counting experiment) for $K^+ \rightarrow \mu^+ \nu$
- Use this ratio to extract $|V_{us}| / |V_{ud}|$:

$$\frac{|V_{us}|}{|V_{ud}|} \frac{f_K}{f_\pi} = \left(\frac{\Gamma_{K\mu 2(\gamma)} m_{\pi^\pm}}{\Gamma_{\pi 2(\gamma)} m_{K^\pm}} \right)^{1/2} \frac{1 - m_\mu^2 / m_{\pi^\pm}^2}{1 - m_\mu^2 / m_{K^\pm}^2} \left(1 - \frac{1}{2} \delta_{\text{EM}} - \frac{1}{2} \delta_{SU(2)} \right)$$

- Big advantage: first-order cancellation of shared systematic effects
- Aim is $\leq 0.5\%$ precision (limited by $\sim 0.4\%$ uncertainty on $\text{Br}(K_{\pi 2})$)

Measuring V_{us} / V_{ud}

$$1) \Gamma(K^+ \rightarrow \mu^+ \nu) = \frac{Br(K^+ \rightarrow \mu^+ \nu)}{\tau_{K^+}} = \frac{1}{\tau_{K^+}} \frac{N_{\mu}^{K\mu 2}}{N_K a_{\mu}^{K\mu 2}}$$

$$2) \Gamma(\pi^+ \rightarrow \mu^+ \nu) = \frac{Br(\pi^+ \rightarrow \mu^+ \nu)}{\tau_{\pi^+}} = \frac{1}{\tau_{\pi^+}} \frac{N_{\mu-\pi^0}^{\pi\mu 2}}{N_K Br(K^+ \rightarrow \pi^+ \pi^0) a_{\pi^+ \rightarrow X}^{K\pi 2} a_{\mu-\pi^0}^{\pi\mu 2}}$$

$$R_A^{K\mu 2} = \frac{\Gamma(K^+ \rightarrow \mu^+ \nu)}{\Gamma(\pi^+ \rightarrow \mu^+ \nu)} = \frac{Br(\pi^+ \rightarrow \mu^+ \nu) \tau_{\pi^+}}{\tau_{K^+}} \frac{N_{\mu}^{K\mu 2}}{N_{\mu-\pi^0}^{\pi\mu 2}} \frac{a_{\pi^+ \rightarrow X}^{K\pi 2} a_{\mu-\pi^0}^{\pi\mu 2}}{a_{\mu}^{K\mu 2}}$$

$N_{\mu}^{K\mu 2}$ = number of tagged muons from $K^+ \rightarrow \mu^+ \nu$

$N_{\mu-\pi^0}^{\pi\mu 2}$ = number of tagged muon-pi0 from $K^+ \rightarrow \pi^+ \pi^0 \rightarrow \pi^+ \rightarrow \mu^+ \nu$

$a_{\mu}^{K\mu 2}$ = acceptance for $K_{\mu 2}$ muons

$a_{\mu-\pi^0}^{\pi\mu 2}$ = combined acceptance for muon-pi0 from $K_{\pi 2}$ pi0 and $\pi_{\mu 2}$ DIF muon

$a_{\pi^+ \rightarrow X}^{K\pi 2}$ = acceptance for π^+ decay from $K_{\pi 2}$ decays

Obtain from Data
Obtain from MC

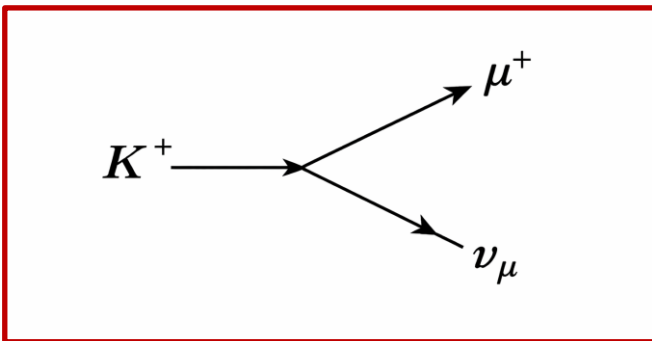
Signal Selections

Two signal regions (SRs) separately defined for both based on n_{π^0} and missing mass squared (MMS) selections ($m_{K^+-\mu^+}^2$, $m_{K^+-\pi^0}^2$):

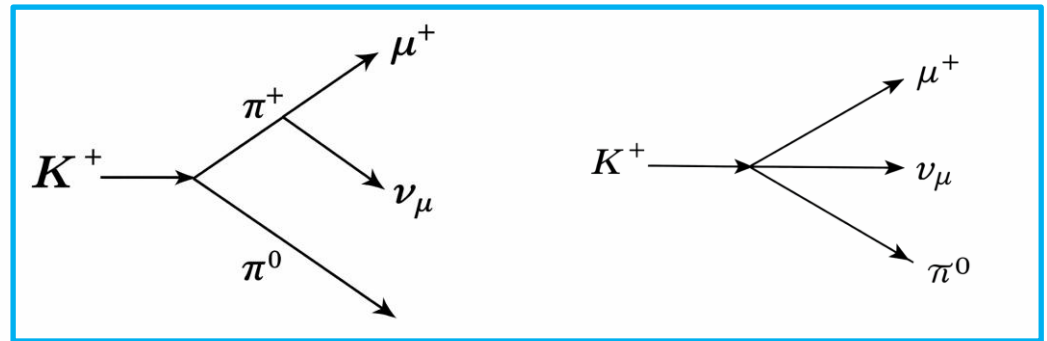
- Presence of π^0 determined from photon candidates in **LKr**
- Muon candidate determined from **STRAW track** matched to hit in **MUV3**
- Kaon decay determined from presence of **KTAG candidate** and kaon candidate in **GTK** matched to **STRAW track**
- Additional selections to reduce remaining background (track momentum, ratio of LKr energy to track momentum)

Goal is to keep selections simple, **minimize systematic effects** from selections

$$n_{\pi^0} = 0$$

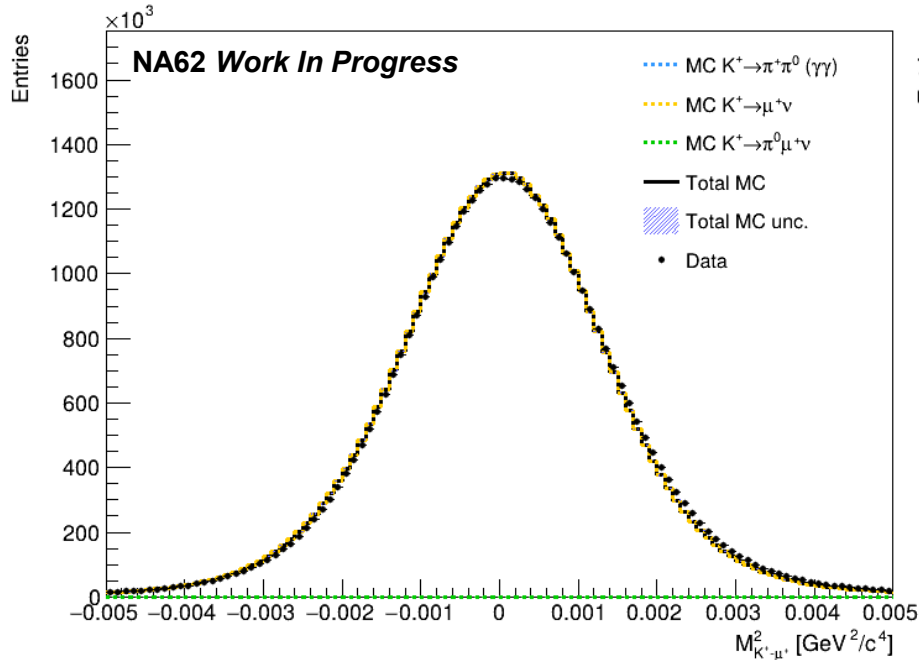


$$n_{\pi^0} = 1$$

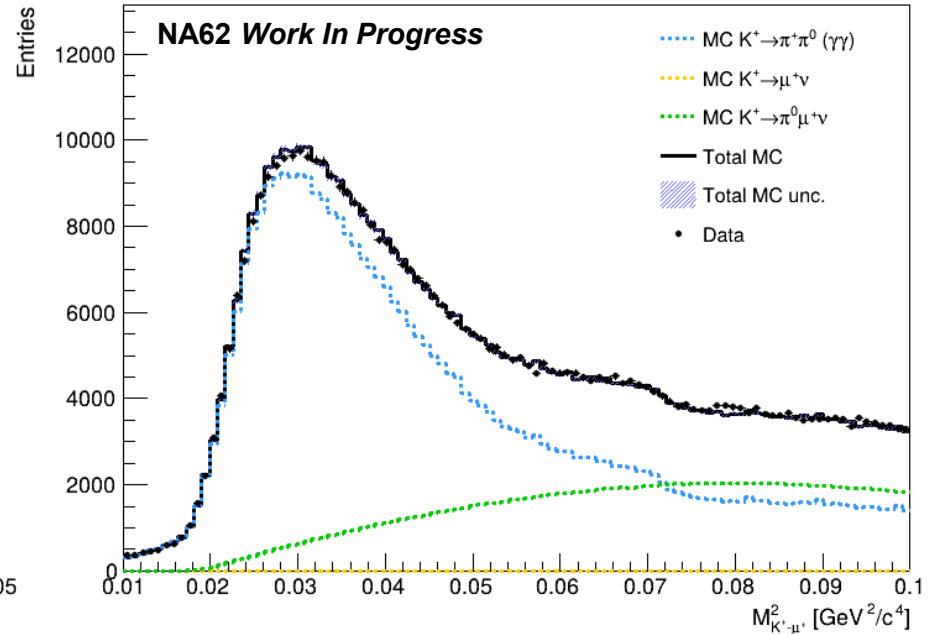


Signal Regions

Km2 SR ($K^+ \rightarrow \mu^+ \nu$)



K2pi SR ($K^+ \rightarrow \pi^+ \pi^0$)



Process	MC Acceptance ($n_{\pi^0} = 0$)	MC Acceptance ($n_{\pi^0} = 1$)
Km2	$0.42 \pm 7.6 \times 10^{-4}$	0.0 ± 0.0
K2pi	$5.7 \times 10^{-5} \pm 1.0 \times 10^{-6}$	$1.1 \times 10^{-2} \pm 1.0 \times 10^{-5}$
Km3	$6.0 \times 10^{-6} \pm 1.0 \times 10^{-7}$	$2.6 \times 10^{-2} \pm 1.7 \times 10^{-5}$

Data shown for **single run** in 2024 (out of 25 total), rest of data set blinded

Systematic Uncertainties

Implement systematic effects on yield through nuisance parameters in fit:

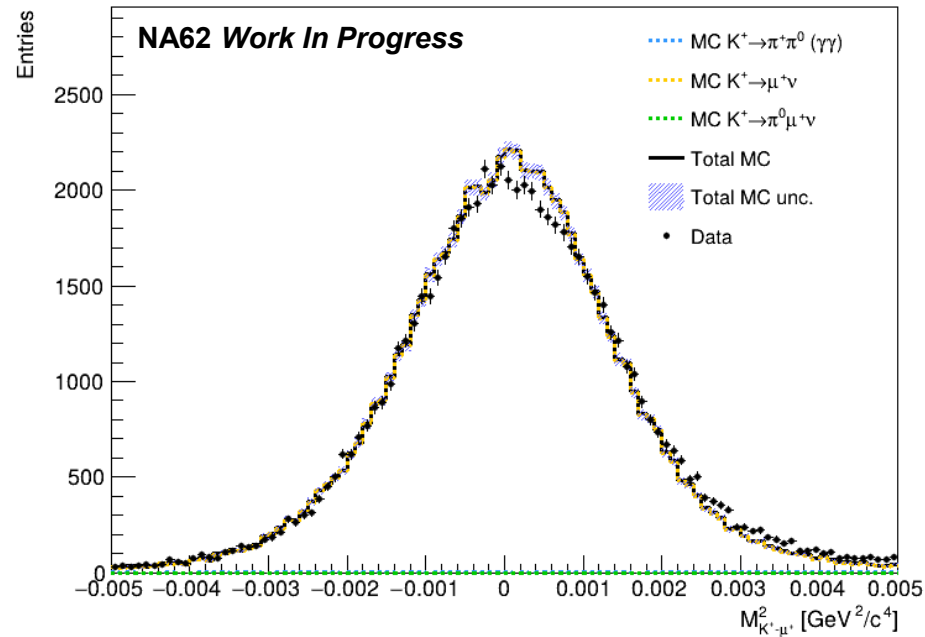
Systematic	Type	Relevant processes	Size
PDG Br	logN	Background	~0.4-2%
Pi0 selection efficiency in Data vs MC	logN	Signal + background (only in K2pi SR)	0.5%
MC Acceptance	Shape	K2pi, Km3 (K2pi SR) Km2 (Km2 SR)	2% (K2pi), 1% (Km3) 5% (Km2)

To determine effect of MC acceptance systematics on extracted yield, define separate control regions (CRs) orthogonal to signal regions to evaluate Data/MC agreement:

- $K^+ \rightarrow \mu^+ \nu$ ($n_{\pi^0} = 0$): SR selection with MUV3 selection inverted (veto)
- $K^+ \rightarrow \pi^+ \pi^0$ ($n_{\pi^0} = 1$): SR selection with MUV3 selection inverted (veto)
- $K^+ \rightarrow \pi^0 \mu^+ \nu$ ($n_{\pi^0} = 1$): SR selection with $m_{K^+ - \pi^0}^2 > 0.035 \text{ GeV}^2/c^4$
- For remaining backgrounds ($\ll 1\%$), rely on MC

Control Regions ($n_{\pi^0} = 0$)

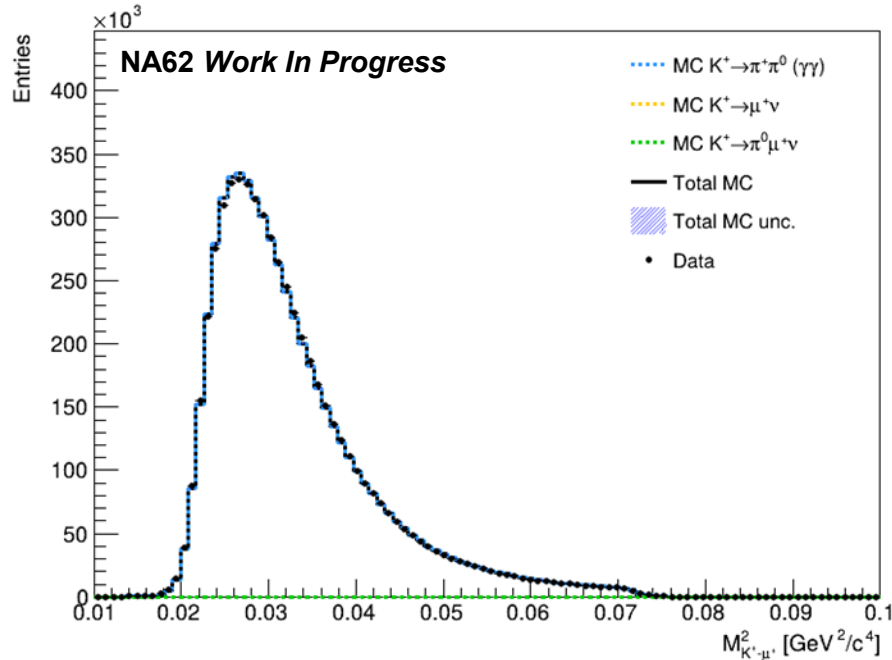
Km2 CR ($K^+ \rightarrow \mu^+ \nu$)



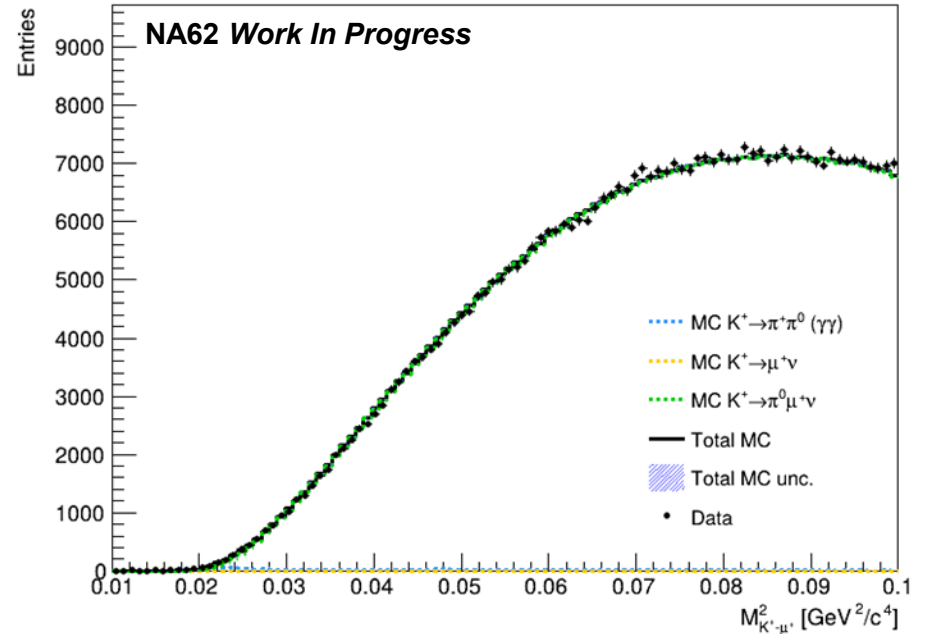
Data shown for **single run** in 2024 (out of 25 total), rest of data set blinded

Control Regions ($n_{\pi^0} = 1$)

K2pi CR ($K^+ \rightarrow \pi^+ \pi^0$)



Km3 SR ($K^+ \rightarrow \pi^0 \mu^+ \nu$)



Data shown for **single run** in 2024 (out of 25 total), rest of data set blinded

Estimated Total Uncertainty on V_{us} / V_{ud}

Rough estimate using statistical uncertainties for MC acceptances and external uncertainty on $\text{Br}(K_{\pi 2})$:

	Relative Uncertainty
$N_{K\pi 2}$	2.9×10^{-3}
$N_{K2\pi}$	2.2×10^{-3}
$a_{K\pi 2}$	9.3×10^{-4}
$a_{K2\pi}$	1.8×10^{-4}
$\text{Br}(K_{\pi 2})$	3.9×10^{-3}
V_{us}/V_{ud}	5.4×10^{-3}

Caveats:

- Systematic studies incomplete (MUV3 efficiency, L0/L1 trigger efficiency, etc.)
- Limited statistics from looking at single run

However, demonstrates that precision of $O(0.5\%)$ can be achieved!

Measuring $\text{Br}(K_{\mu 3}) / \text{Br}(K_{\mu 2})$ and V_{us}

Can also use NA62 to measure ratio $R_{32} = \text{Br}(K_{\mu 3}) / \text{Br}(K_{\mu 2})$:

- Use distributions of MC simulated kinematic variables to perform template fit of six main K^+ decay modes
- Determine branching ratios of main decay modes from fraction of the data for each component

Compute expected fraction:

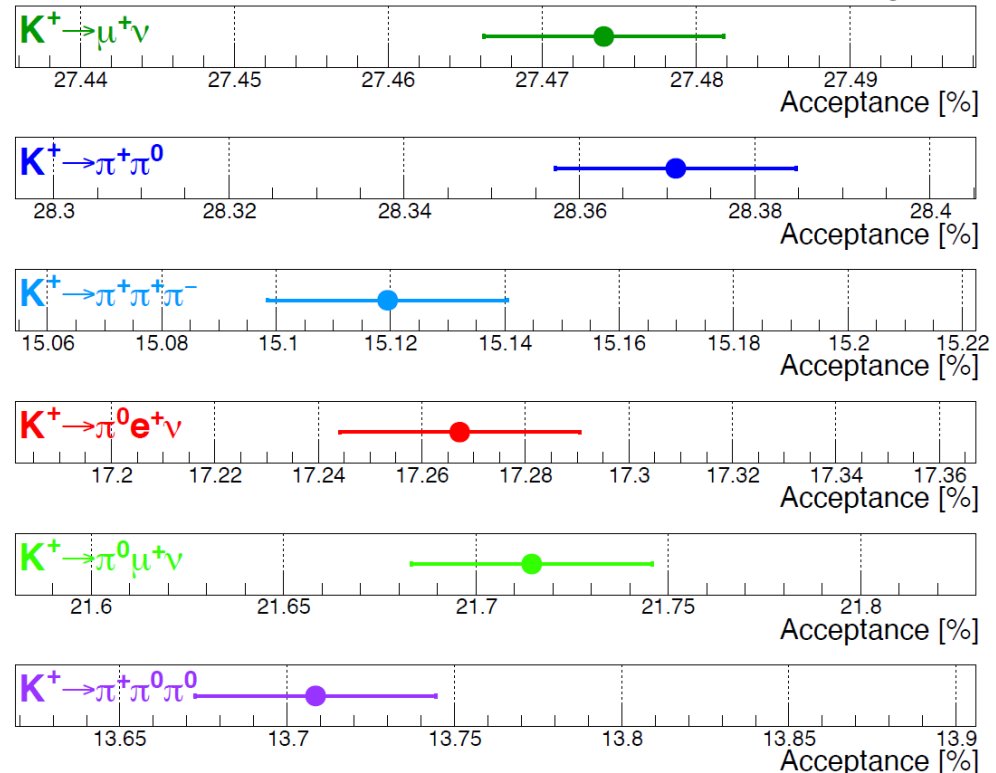
$$f_i = \frac{\mathcal{B}_i A_i}{\sum_{i=1}^6 \mathcal{B}_i A_i}$$

$$f'_i = \frac{N'_{\text{MC},i}}{N_{\text{data}}} = \frac{N'_{\text{MC},i}}{\sum_i N'_{\text{MC},i}}$$

↓

$$\mathcal{B}'_i = \frac{f'_i}{A_i} \cdot \sum_{i=1}^6 \mathcal{B}_i A_i$$

NA62 Work In Progress



Measuring $\text{Br}(K_{\mu 3}) / \text{Br}(K_{\mu 2})$ and V_{us}

Advantage: can extract branching ratios without absolute normalization

- Use PDG value for K^+ lifetime
- Use branching ratios to determine both $\text{Br}(K_{\mu 3}) / \text{Br}(K_{\mu 2})$ and V_{us} :

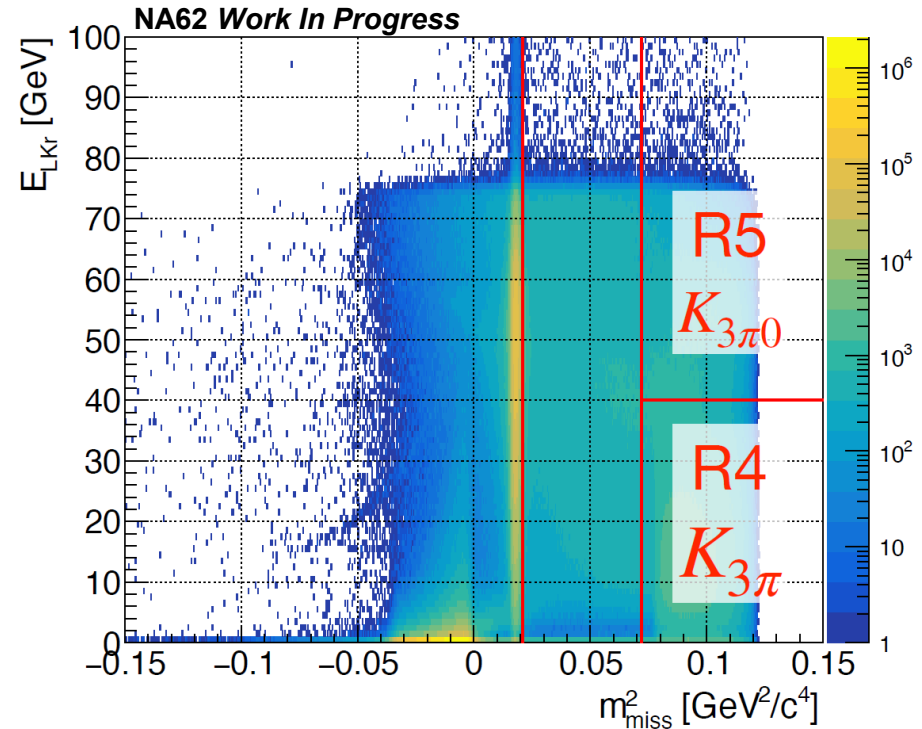
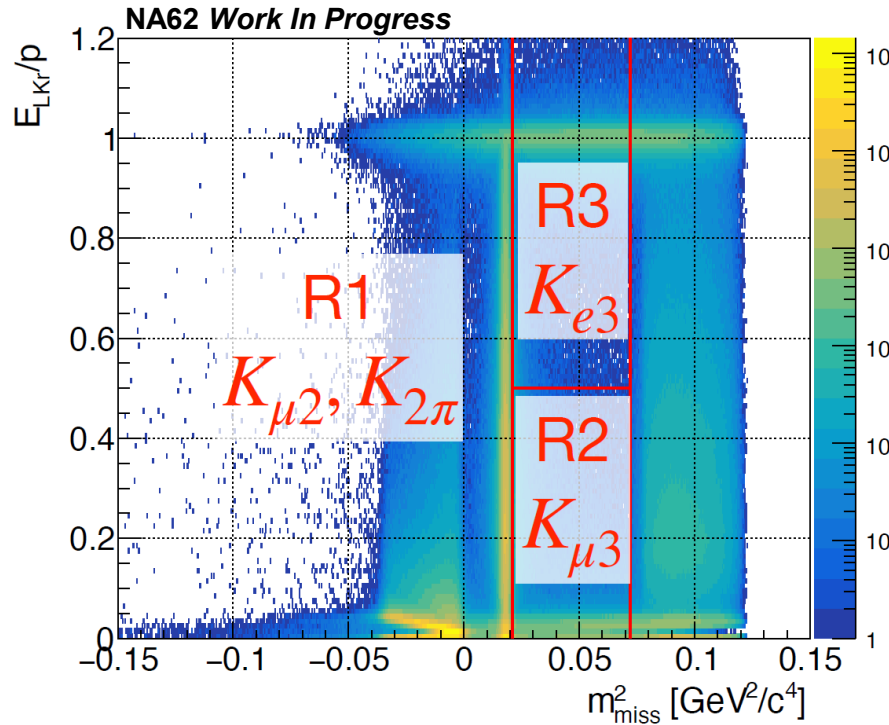
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- **Similar target precision of ~0.5%**

Two approaches to template fit:

- Maximum likelihood fit vs minimizing χ^2
- Use one as a cross-check for the other

Selectons and Fit Bin Definitions

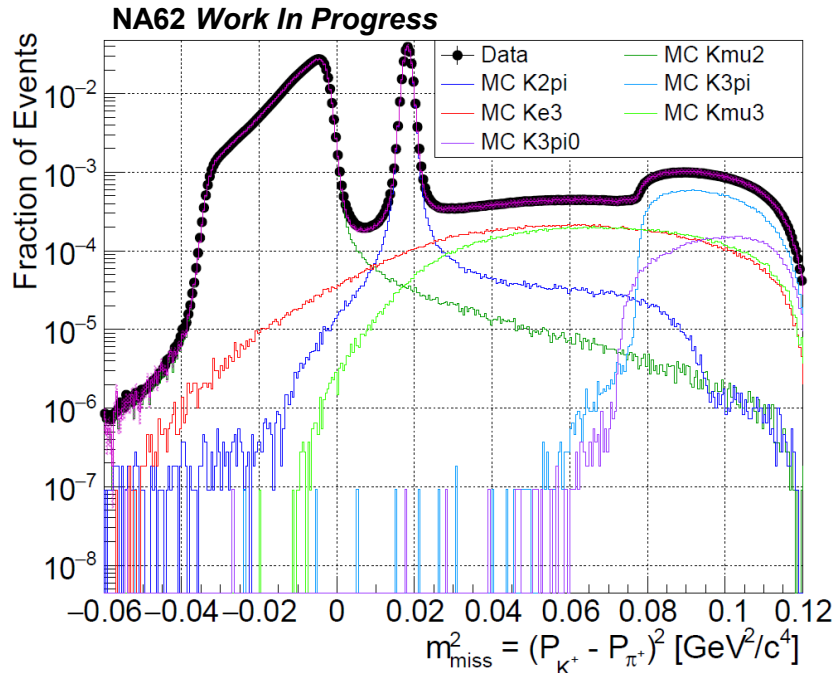


Similar selection criteria to V_{us} / V_{ud} :

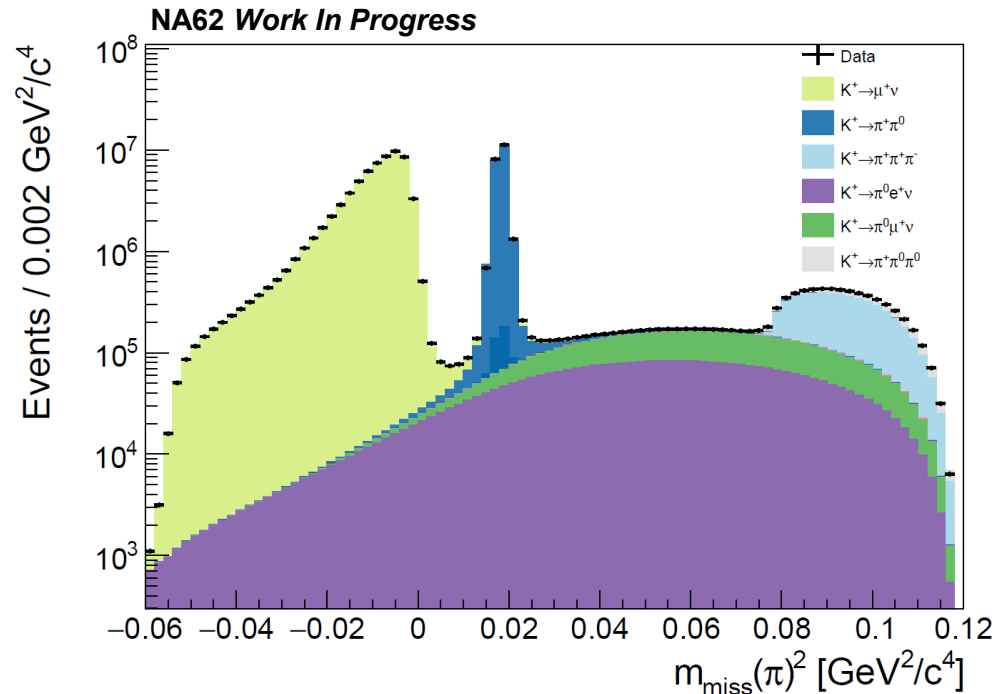
- One positively charged track, KTAG association, STRAW track matched to GTK candidate
- To avoid strong correlations between K_{e3} vs $K_{\mu 3}$ and $K_{3\pi}$ and $K_{3\pi 0}$, define five separate MMS bins

Template Fits to MMS

Maximum Likelihood Fit



χ^2 Fit



Data shown for **single run** in 2024 (out of 25 total), rest of data set blinded

Current Status and Prospects

- Analysis frameworks developed, systematic studies underway
- Only small portion of 2024 low intensity data set analyzed, 2025 available and planned to be included
- Even with limited data set, statistical uncertainties comparable to systematics → **final measurement not expected to be statistical limited**, current data set is sufficient

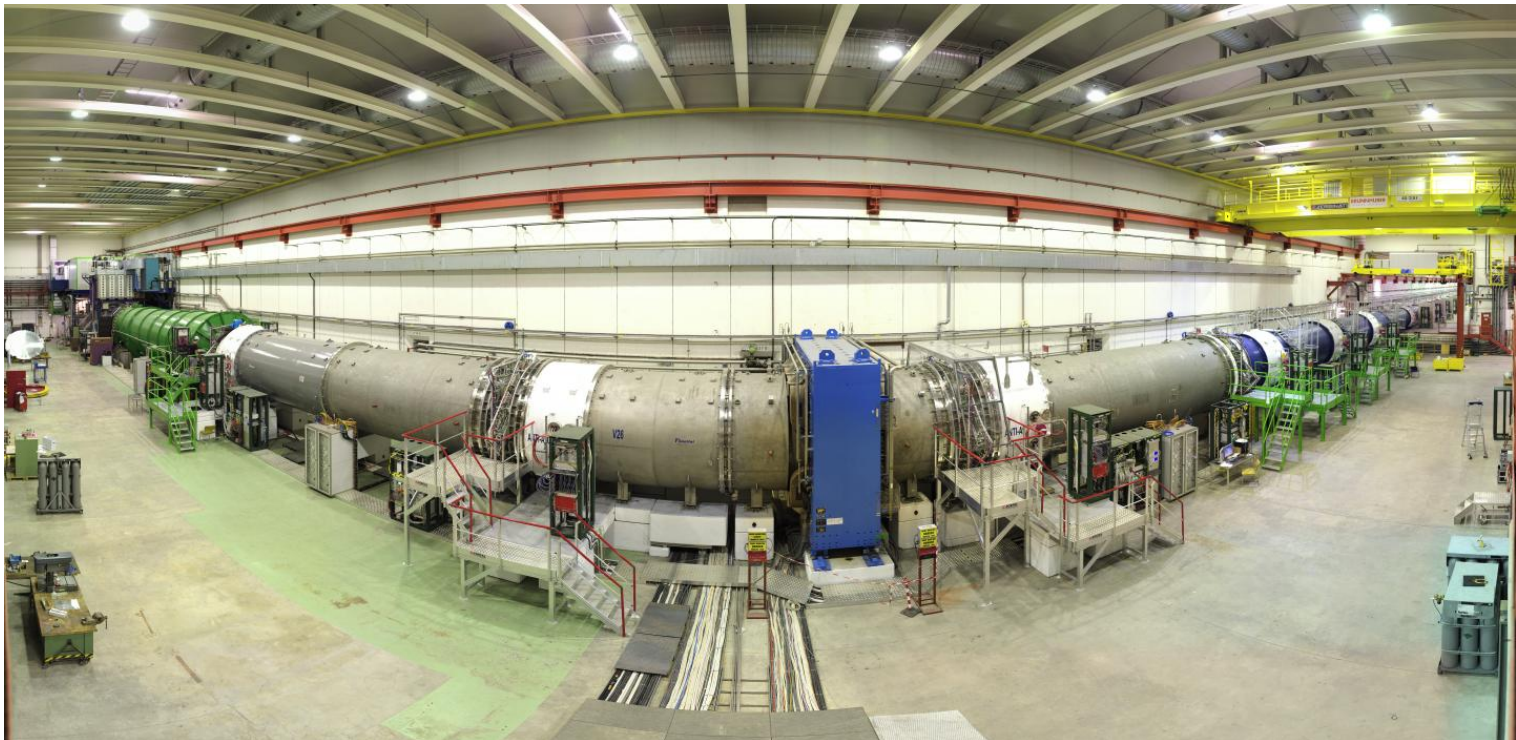
Largest external uncertainties:

- $V_{us} / V_{ud} : \text{Br}(K_{\pi 2})$ ($\sim 0.4\%$)
- $\text{Br}(K_{\mu 3}) / \text{Br}(K_{\mu 2})$ and $V_{us} : \tau(K^+)$ ($\sim 0.16\%$)

Theoretical uncertainties not a limiting factor to achieving $O(0.5\%)$ precision

Summary

- Efforts at NA62 underway to test 1st-row CKM unitarity through measurement of V_{us} / V_{ud} , $\text{Br}(K_{\mu 3}) / \text{Br}(K_{\mu 2})$, and V_{us}
- Target precision of 0.5% is realistic and can have significant impact on status of Cabibbo angle anomalies
- Look forward to new results!



Backup

V_{us} / V_{ud} Analysis Selection Details

- MinBias Trigger (non-overlapping with CTRL trigger events)
- At least one “good” downstream track
- At least 1 good KTAG candidate
- Track-associated and in-time MUV3 hit
- Track energy-to-momentum ratio < 0.8
- Track momentum between 10 and 60 GeV
- GTK matched tracks (SpectrometerGigaTrackerMatching)

Common preselection
(k2pi + km2 SRs)

- 0 good pi0 candidate
- $-0.0025 < m_{K^+ - \mu^+}^2 < 0.0025 \text{ GeV}^2/c^4$

Only $n_{\pi^0} = 0$ selection
(km2 SR)

- 1 good pi0 candidate
- $0.01 < m_{K^+ - \pi^0}^2 < 0.03 \text{ GeV}^2/c^4$
- $0.01 < m_{K^+ - \mu^+}^2 < 0.1 \text{ GeV}^2/c^4$

Only $n_{\pi^0} = 1$ selection
(k2pi SR)

V_{us} / V_{ud} Analysis Systematics

- Evaluate systematic uncertainties as either normalization or shape variations on initial estimated MC yield
- Normalization uncertainties:
 - Implemented as flat logN parameters in fit
 - PDG BRs: Assign flat unc to backgrounds based on PDG uncertainty for background branching ratios
 - π^0 selection: Assign flat unc to account for difference in π^0 efficiency between Data and MC
- Shape uncertainties:
 - Derived from binned template histograms for both up/down variations
 - MC acceptance: Assign conservative flat bin-by-bin variation to signal (K2 π , K μ^2) as well as dominant background in K2 π SR (K μ^2)

Systematic	Type	Relevant processes	Size
PDG Br	logN	Background	~0.4-2%
π^0 selection efficiency in Data vs MC	logN	Signal + background (only in K2 π SR)	0.5%
MC Acceptance	Shape	K2 π , K μ^2 (K2 π SR) K μ^2 (K μ^2 SR)	2% (K2 π), 1% (K μ^2) 5% (K μ^2)

Br(K_{μ3}) / Br(K_{μ2}) and V_{us} Analysis Selection Details

PRE-SELECTION: match and reconstruction of good-quality one positive tracks

1. Track size: [1,20] after Trigger/L0Emulator Check (Mask2 Events);
2. One positive good downstream track:
 - Track-CHOD association and $|t_{\text{trigger}} - t_{\text{track}}| \leq 2 \text{ ns}$;
 - $Q == +1$;
 - Fake Vertex mask;
 - $|P_{\text{beam}} - P_{\text{track}}| < 20 \text{ GeV}$;
 - $P_{\text{track}} : [5, 70] \text{ GeV}$;
 - $Z_{\text{track}} : [105, 180] \text{ m}$;
 - $\text{CDA} < 30 \text{ mm}$ and $\chi^2 < 20$;
 - Hit at each four straw chambers;
 - Acceptance in STRAW, CHODs, RICH, LKr, MUV1-3, no IRC and LAV;
 - CHANTI non-association and RICH association;
 - If more than one good track exists, the track with highest momentum considered;
3. Kaon TAGging:
 - closest in time with at least a hit in five sectors; $|t_{\text{Cedar}} - t_{\text{track}}| \leq 5 \text{ ns}$;
4. Upstream-Downstream matching:
 - Matching quality check
 - $\chi_{\text{GTK}}^2 < 40$ and $\chi_{\text{GTK-event}}^2 < 10$
 - $N_{\text{matched GTK}} == 1$

FINAL-SELECTION: apply kinematic and upstream cuts to evaluate final events for Squared Missing Mass plot

1. $\text{CDA} \leq 3.5 \text{ mm}$; **Kinematic cuts**
 2. $Z_{\text{vertex}} : [115, 175] \text{ m}$;
 3. $P_{\text{beam}} : [73, 77] \text{ GeV}$ & $P_{\text{track}} : [10, 65] \text{ GeV}$;
 4. $P_t : [25, 285]$;
 5. Upstream-matter interactions: **Upstream bkg cuts**
 - $X(Y)_{\text{track@GTK3}} < 30 (15) \text{ cm}$;
 - $|XY_{\text{track@GTK3}} - XY_{\text{GTK3 hit}}| < 24 \text{ cm}$;
 - $|t_{\text{Cedar}} - t_{\text{GTK3 hit}}| > 1.2 \text{ ns}$ && $\text{ToT GTK3 hit} > 23 \text{ ns}$ && $N_{\text{GTK3 hits}} > 50$;
 - $100 \text{ m} < Z_{\text{track@GTK3}} < 105 \text{ m}$;
 6. Upstream decay cuts:
 - $m_{\pi\mu 2}^2 < -0.02 \text{ GeV}^2$ and box cut $|X(Y)_{\text{track@TRIM5}}| < 10 \text{ cm}$;
- Squared missing mass as PID: $m_{\text{miss}}^2 = (P_K^\mu - P_{\text{track}}^\mu)^2$ **PID**