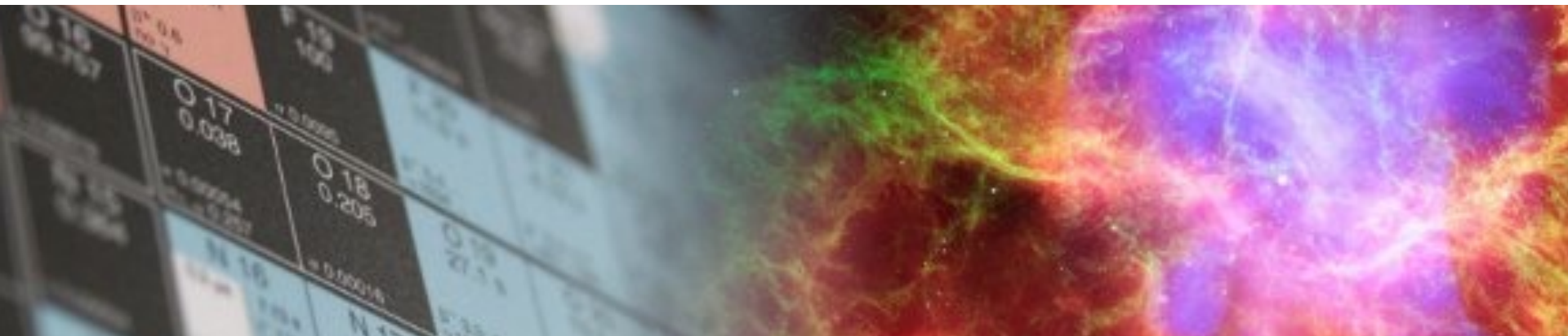


Challenges for Nuclear Hamiltonians

Achim Schwenk



TECHNISCHE
UNIVERSITÄT
DARMSTADT



INT Program “Nuclear Hamiltonians
for Advancing Nuclear Physics and Beyond”, May 7, 2026

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Exzellente Forschung für
Hessens Zukunft

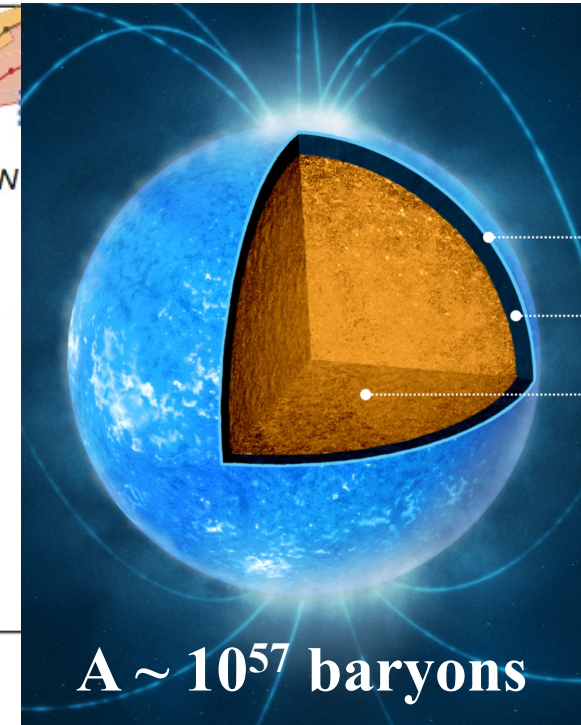
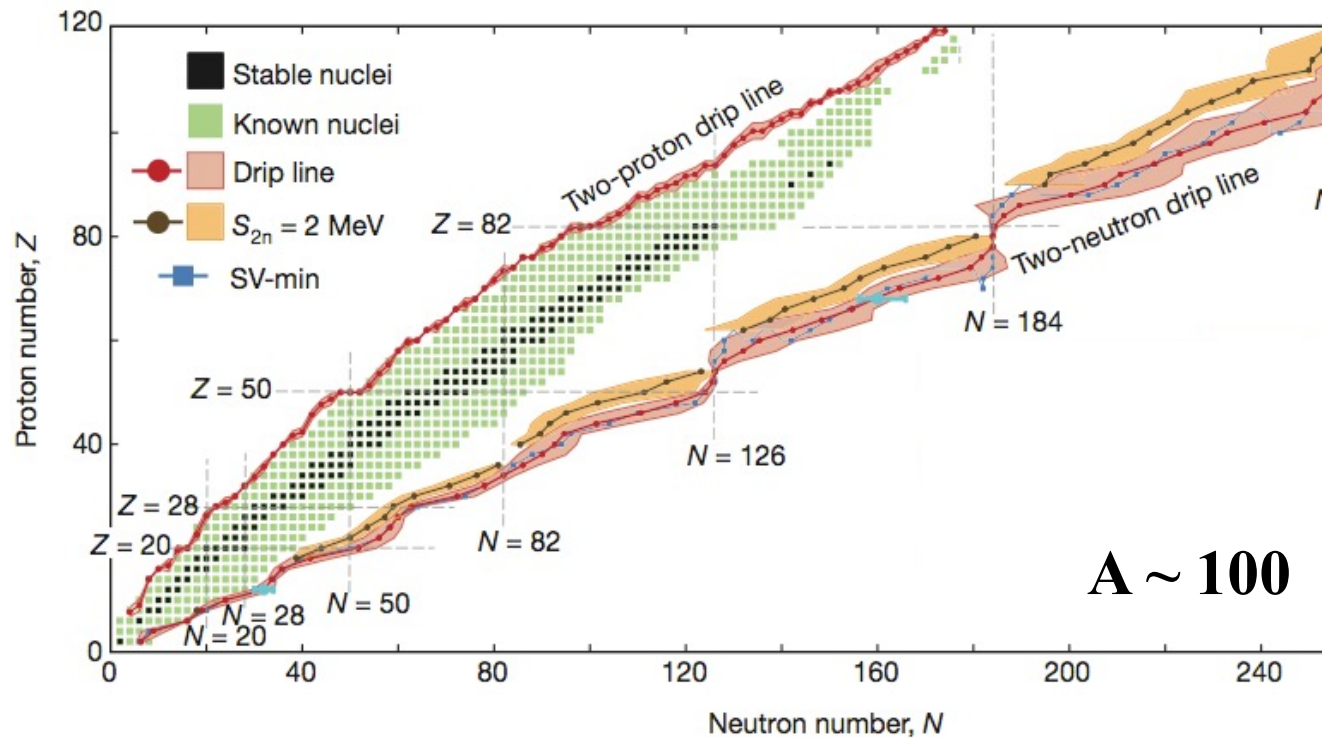
Structure of nuclei and dense matter in neutron stars

doi:10.1038/nature11188

The limits of the nuclear landscape

Jochen Erler^{1,2}, Noah Birge¹, Markus Kortelainen^{1,2,3}, Witold Nazarewicz^{1,2,4}, Erik Olsen^{1,2}, Alexander M. Perhac¹ & Mario Stoitsov^{1,2,†}

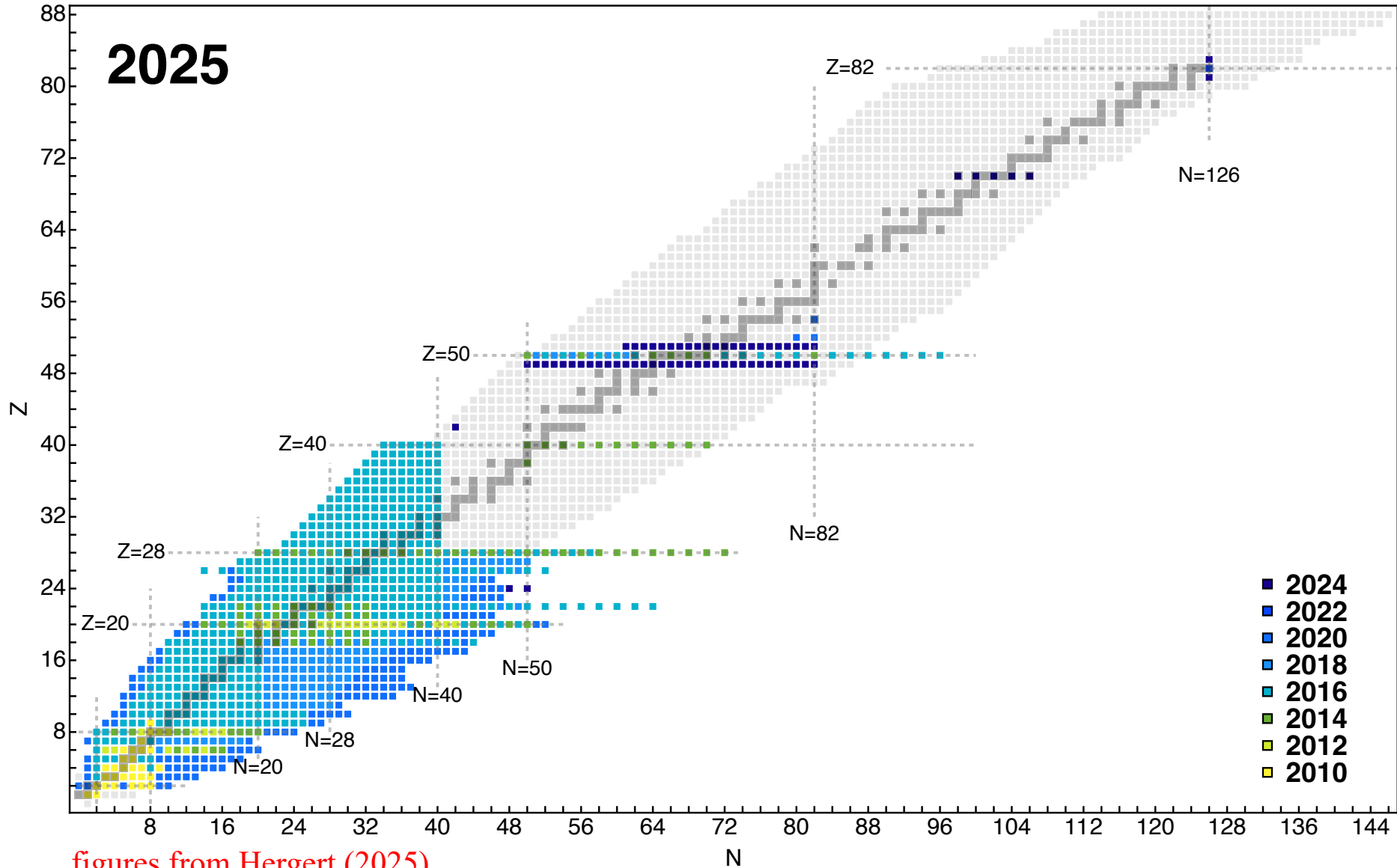
~ 4000 ± 500 nuclei unknown, **extreme neutron-rich**



Extreme neutron-rich matter in neutron stars

Great progress in ab initio calculations of nuclei

systematic interaction expansion + systematic many-body expansion



figures from Hergert (2025)

Great progress in ab initio calculations of nuclei

systematic interaction expansion + systematic many-body expansion

ARTICLES

<https://doi.org/10.1038/s41567-022-01715-8>

nature
physics

Check for updates

OPEN

Ab initio predictions link the neutron skin of ^{208}Pb to nuclear forces

Baishan Hu^{1,11}, Weiguang Jiang^{2,11}, Takayuki Miyagi^{1,3,4,11}, Zhonghao Sun^{5,6,11}, Andreas Ekström², Christian Forssén², Gaute Hagen^{1,5,6}, Jason D. Holt^{1,7}, Thomas Papenbrock^{1,5,6}, S. Ragnar Stroberg^{8,9} and Ian Vernon¹⁰

Heavy atomic nuclei have an excess of neutrons over protons, which leads to the formation of a neutron skin whose thickness is sensitive to details of the nuclear force. This links atomic nuclei to properties of neutron stars, thereby relating objects that differ in size by orders of magnitude. The nucleus ^{208}Pb is of particular interest because it exhibits a simple structure and is experimentally accessible. However, computing such a heavy nucleus has been out of reach for ab initio theory. By combining advances in quantum many-body methods, statistical tools and emulator technology, we make quantitative predictions for the properties of ^{208}Pb starting from nuclear forces that are consistent with symmetries of low-energy quantum chromodynamics. We explore 10^9 different nuclear force parameterizations via history matching, confront them with data in select light nuclei and arrive at an importance-weighted ensemble of interactions. We accurately reproduce bulk properties of ^{208}Pb and determine the neutron skin thickness, which is smaller and more precise than a recent extraction from parity-violating electron scattering

PHYSICAL REVIEW C **105**, 014302 (2022)

Converged *ab initio* calculations of heavy nuclei

T. Miyagi^{1,*}, S. R. Stroberg^{2,†}, P. Navrátil^{1,‡}, K. Hebeler^{3,4,5,§} and J. D. Holt^{1,6,||}

¹TRIUMF, 4004 Wesbrook Mall, Vancouver, BC V6T 2A3, Canada

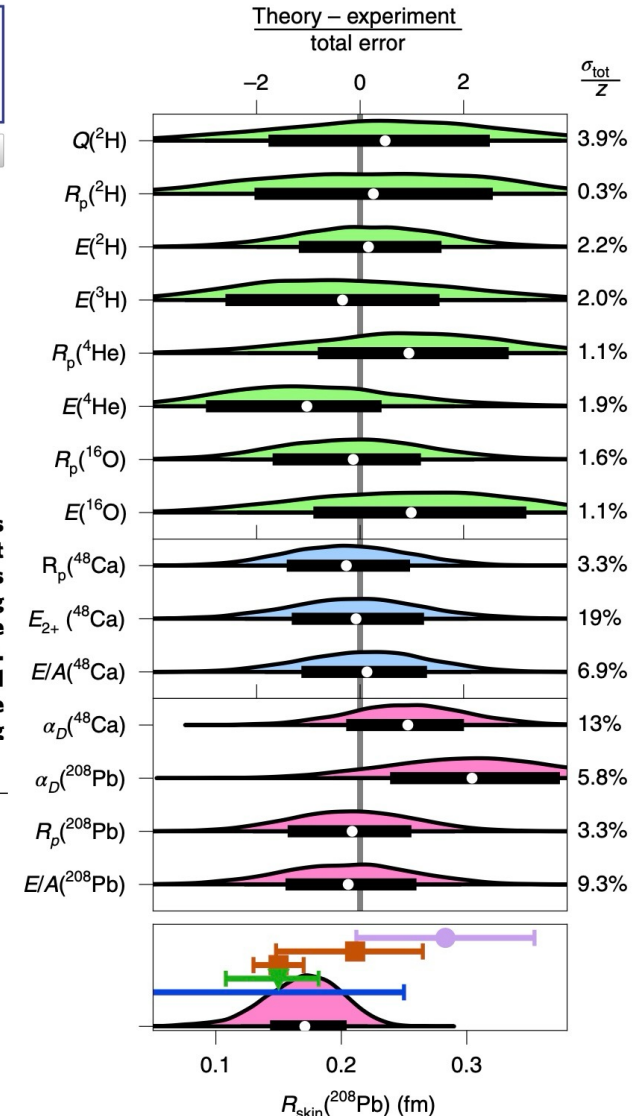
²Department of Physics, University of Washington, Seattle, Washington 98195, USA

³Technische Universität Darmstadt, 64289 Darmstadt, Germany

⁴Extreme Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany

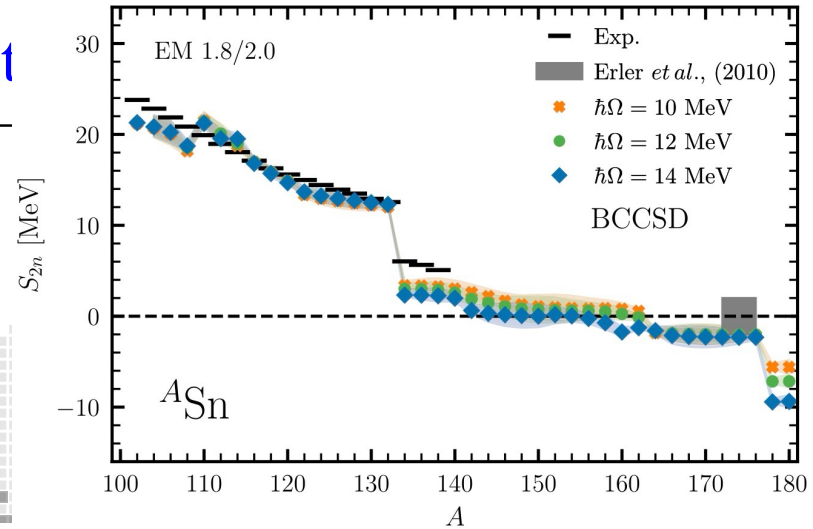
⁵Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany

⁶Department of Physics, McGill University, 3600 Rue University, Montréal, QC H3A 2T8, Canada



Great progress in ab initio calculations of nuclei

systematic interaction expansion + syst



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Physics Letters B

journal homepage: www.elsevier.com/locate/physletb



Letter

Towards heavy-mass *ab initio* nuclear structure: Open-shell Ca, Ni and Sn isotopes from Bogoliubov coupled-cluster theory

A. Tichai ^{a,b,c,*}, P. Demol ^d, T. Duguet ^{e,d}

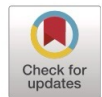
^a Technische Universität Darmstadt, Department of Physics, 64289 Darmstadt, Germany

^b ExtreMe Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany

^c Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany

^d KU Leuven, Instituut voor Kern- en Stralingsfysica, 3001 Leuven, Belgium

^e IRFU, CEA, Université Paris-Saclay, 91191 Gif-sur-Yvette, France



Great progress in ab initio calculations of nuclei

systematic interaction expansion + systematic many-body expansion

88
80

2025

Z=82

PHYSICAL REVIEW LETTERS 132, 232503 (2024)

Impact of Two-Body Currents on Magnetic Dipole Moments of Nuclei

T. Miyagi^{1,2,3,*}, X. Cao^{4,†}, R. Seutin^{3,1,2,‡}, S. Bacca^{5,6,§}, R. F. Garcia Ruiz^{7,||},
K. Hebeler^{1,2,3,¶}, J. D. Holt^{8,9,**} and A. Schwenk^{1,2,3,††}

¹Technische Universität Darmstadt, Department of Physics, 64289 Darmstadt, Germany

²ExtreMe Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung GmbH,
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³Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany

⁴Department of Physics and Institute for Condensed Matter Theory, University of Illinois at Urbana-Champaign,
1110 West Green Street, Urbana, Illinois 61801-3080, USA

⁵Institute of Nuclear Physics, Johannes Gutenberg-Universität Mainz, 55099 Mainz, Germany

⁶PRISMA+ Cluster of Excellence, Johannes Gutenberg-Universität Mainz, 55099 Mainz, Germany

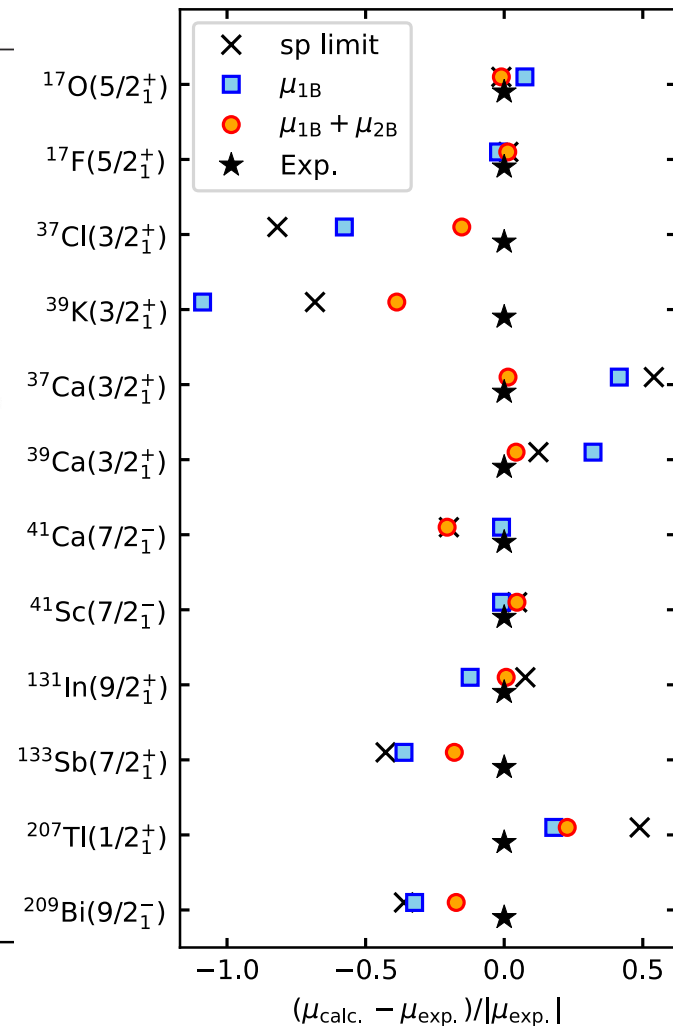
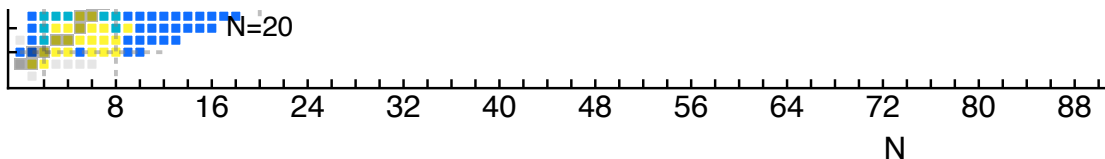
⁷Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA

⁸TRIUMF, 4004 Wesbrook Mall, Vancouver British Columbia V6T 2A3, Canada

⁹Department of Physics, McGill University, Montréal, Quebec City H3A 2T8, Canada

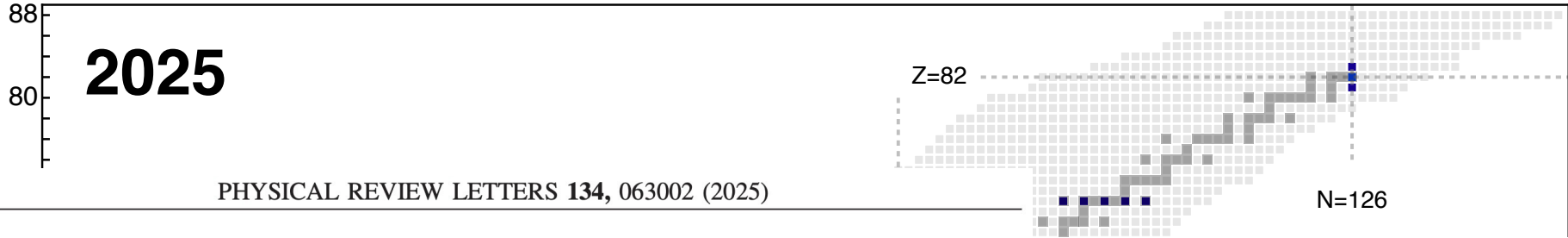
(Received 28 November 2023; revised 23 March 2024; accepted 25 April 2024; published 7 June 2024)

We investigate the effects of two-body currents on magnetic dipole moments of medium-mass and heavy nuclei using the valence-space in-medium similarity renormalization group with chiral effective field theory interactions and currents. Focusing on near doubly magic nuclei from oxygen to bismuth, we have found that the leading two-body currents globally improve the agreement with experimental magnetic moments. Moreover, our results show the importance of multishell effects for ⁴¹Ca, which suggest that the $Z = N = 20$ gap in ⁴⁰Ca is not as robust as in ⁴⁸Ca. The increasing contribution of two-body currents in heavier systems is explained by the operator structure of the center-of-mass dependent Sachs term.



Great progress in ab initio calculations of nuclei

systematic interaction expansion + systematic many-body expansion



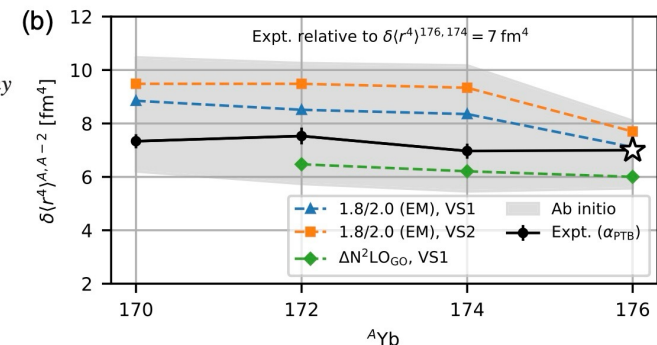
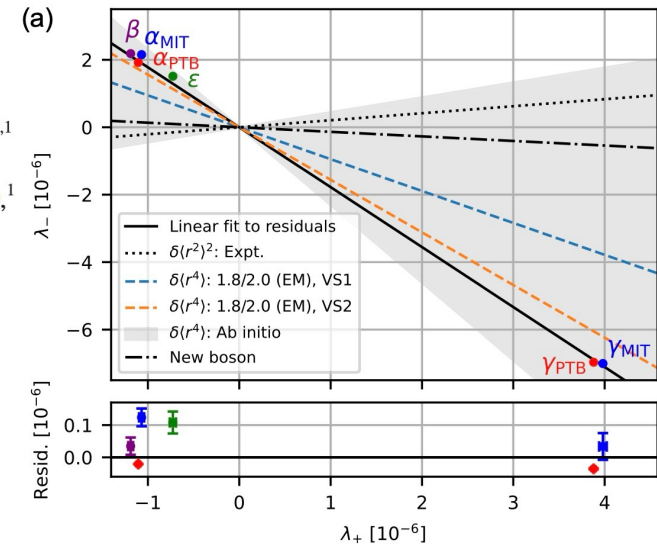
Probing New Bosons and Nuclear Structure with Ytterbium Isotope Shifts

Menno Door^{1,2,*}, Chih-Han Yeh^{3,*}, Matthias Heinz^{4,5,1,§}, Fiona Kirk^{3,6}, Chunhai Lyu¹, Takayuki Miyagi^{4,5,1}, Julian C. Berengut⁷, Jacek Bieroń⁸, Klaus Blaum¹, Laura S. Dreissen^{3,9}, Sergey Eliseev¹, Pavel Filianin¹, Melina Filzinger³, Elina Fuchs^{3,6}, Henning A. Füst^{3,10}, Gediminas Gaigalas¹¹, Zoltán Harman¹, Jost Herkenhoff¹, Nils Huntemann³, Christoph H. Keitel¹, Kathrin Kromer¹, Daniel Lange^{1,2}, Alexander Rischka¹, Christoph Schweiger¹, Achim Schwenk^{4,5,1}, Noritaka Shimizu¹² and Tanja E. Mehlstäubler^{3,10,13}

¹Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany
²Heidelberg University, Grabengasse 1, 69117 Heidelberg, Germany
³Physikalisch-Technische Bundesanstalt, Bundesallee 100, 38116 Braunschweig, Germany
⁴Department of Physics, Technische Universität Darmstadt, Darmstadt, 64289, Germany
⁵ExtreMe Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung GmbH, Darmstadt, 64291, Germany
⁶Institut für Theoretische Physik, Leibniz Universität Hannover, Appelstraße 2, 30167 Hannover, Germany
⁷School of Physics, University of New South Wales, Sydney, New South Wales 2052, Australia
⁸Institute of Theoretical Physics, Jagiellonian University, Kraków, 30-348, Poland
⁹Department of Physics and Astronomy, LaserLab, Vrije Universiteit Amsterdam, De Boelelaan 1081, Amsterdam, 1081 HV, The Netherlands
¹⁰Institut für Quantenoptik, Leibniz Universität Hannover, Welfengarten 1, 30167 Hannover, Germany
¹¹Institute of Theoretical Physics and Astronomy, Vilnius University, Vilnius, 10222, Lithuania
¹²Center for Computational Sciences, University of Tsukuba, Ibaraki, 305-8577, Japan
¹³Laboratorium für Nano- und Quantenengineering, Leibniz Universität Hannover, Schneiderberg 39, 30167 Hannover, Germany

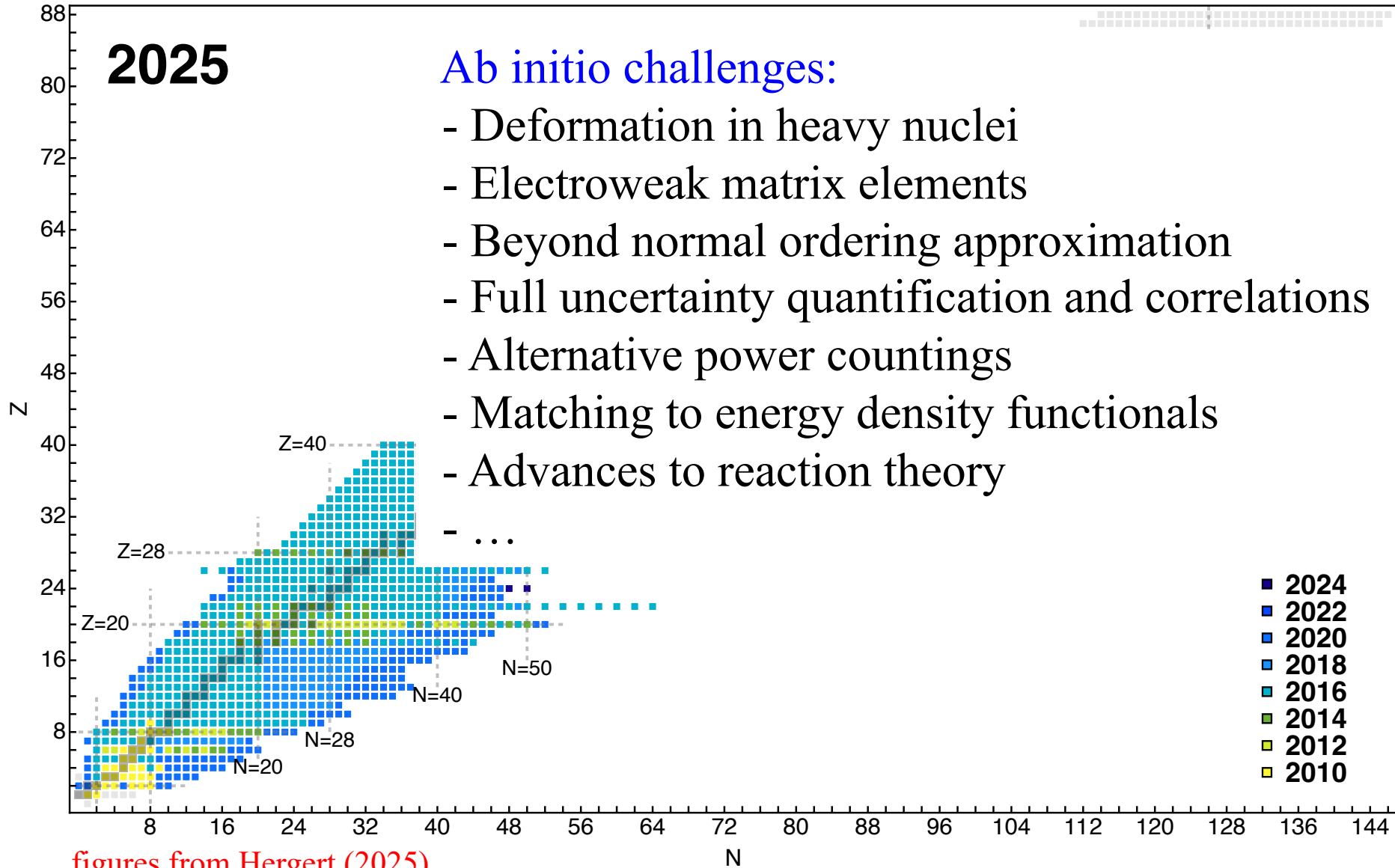
(Received 23 June 2024; revised 6 November 2024; accepted 23 December 2024; published 11 February 2025)

In this Letter, we present mass-ratio measurements on highly charged Yb^{42+} ions with a precision of 4×10^{-12} and isotope-shift measurements on Yb^+ on the $^2\text{S}_{1/2} \rightarrow ^2\text{D}_{5/2}$ and $^2\text{S}_{1/2} \rightarrow ^2\text{F}_{7/2}$ transitions with a precision of 4×10^{-9} for the isotopes $^{168,170,172,174,176}\text{Yb}$. We present a new method that allows us to extract higher-order changes in the nuclear charge distribution along the Yb isotope chain, benchmarking *ab initio* nuclear structure calculations. Additionally, we perform a King plot analysis to set bounds on a fifth force in the keV/ c^2 to MeV/ c^2 range coupling to electrons and neutrons.



Great progress in ab initio calculations of nuclei

systematic interaction expansion + systematic many-body expansion



Outline

Chiral EFT interaction uncertainties and challenges

with P. Arthuis, M. Companys, K. Hebeler, A. Tichai, U. Vernik

Next generation NN+3N interactions: Wish list

with F. Alp, Y. Dietz, K. Hebeler

Ab initio nuclear masses for r-process nucleosynthesis

with J. Kuske, T. Miyagi, A. Arcones

Uncertainty quantification and correlated mass model for calcium isotopes

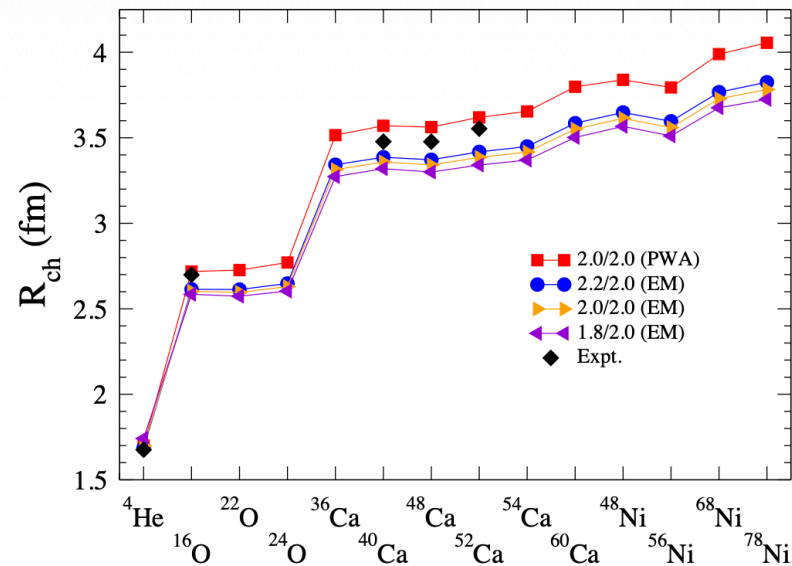
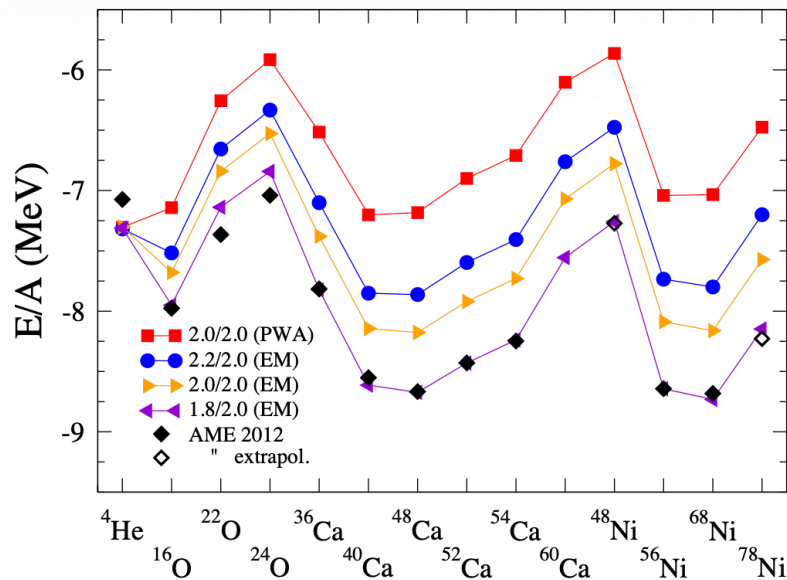
with M. Cincar, Z. Li, T. Plies, U. Vernik, M. Heinz, T. Miyagi,
I. Svensson, A. Tichai, K. Hebeler

Chiral NN+3N interactions up to ^{208}Pb

Optimization strategies for NN+3N interactions

1.8/2.0 (EM) interaction [Hebeler et al., PRC \(2011\)](#), [Simonis et al., PRC \(2017\)](#)

NN N^3LO (SRG evolved) + 3N N^2LO fit to ^3H energy and ^4He radius



+ SRG preserves high-quality NN scattering

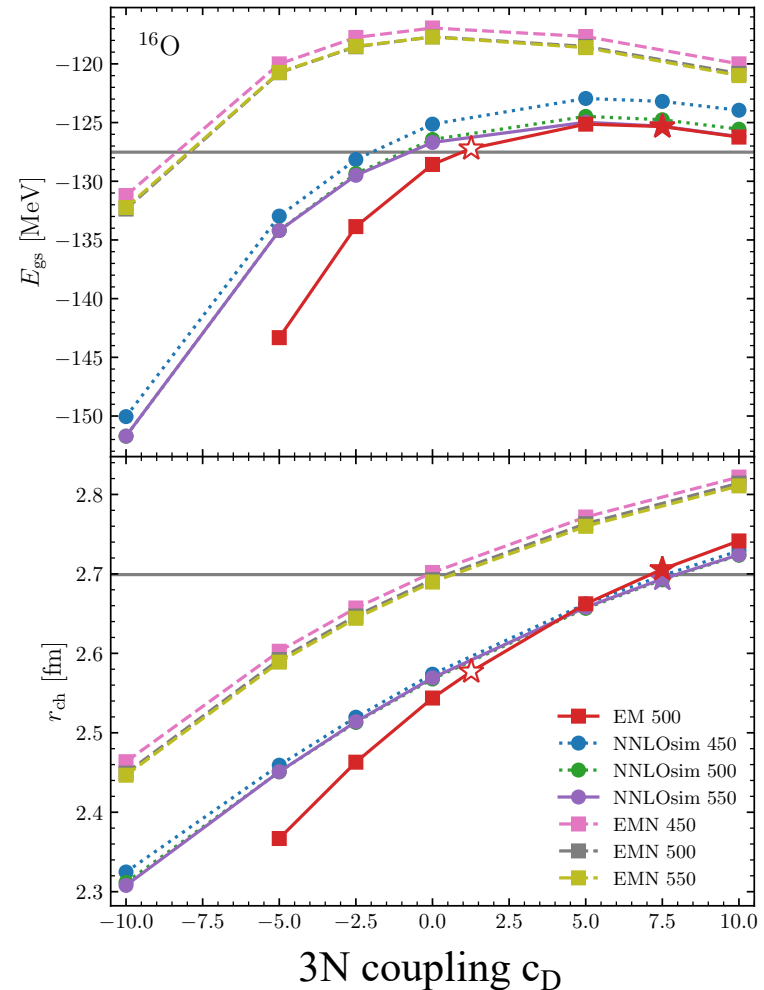
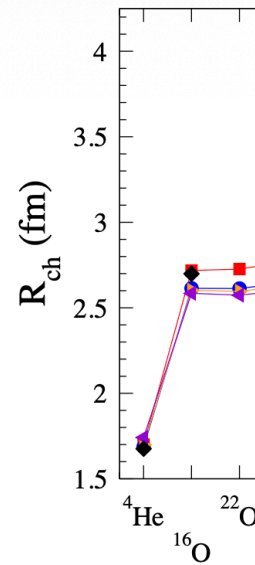
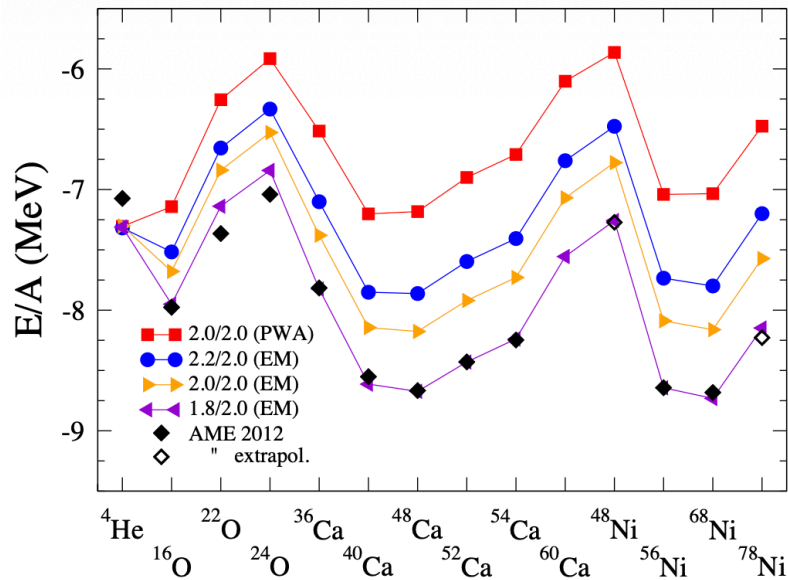
- mixed N^3LO + N^2LO , SRG evolution not consistent,...

Chiral NN+3N interactions up to ^{208}Pb

Optimization strategies for NN+3N interactions

1.8/2.0 (EM) interaction [Hebeler et al., PRC \(2011\)](#), [Simonis et al., PRC \(2017\)](#)

NN N³LO (SRG evolved) + 3N N²LO fit to ^3H energy and ^4He radius



3N fit to ^3H energy and ^{16}O energy/radius

[Arthuis, Hebeler, AS, arXiv:2401.06675](#)

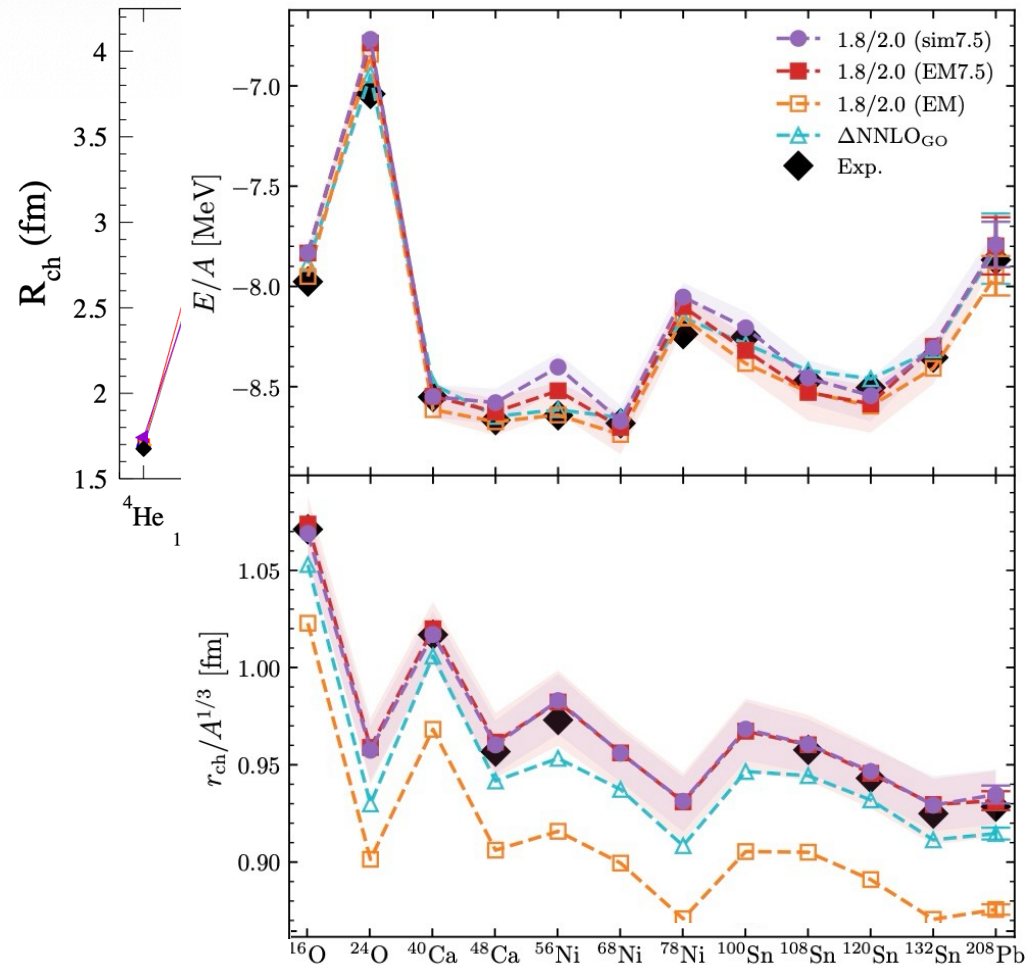
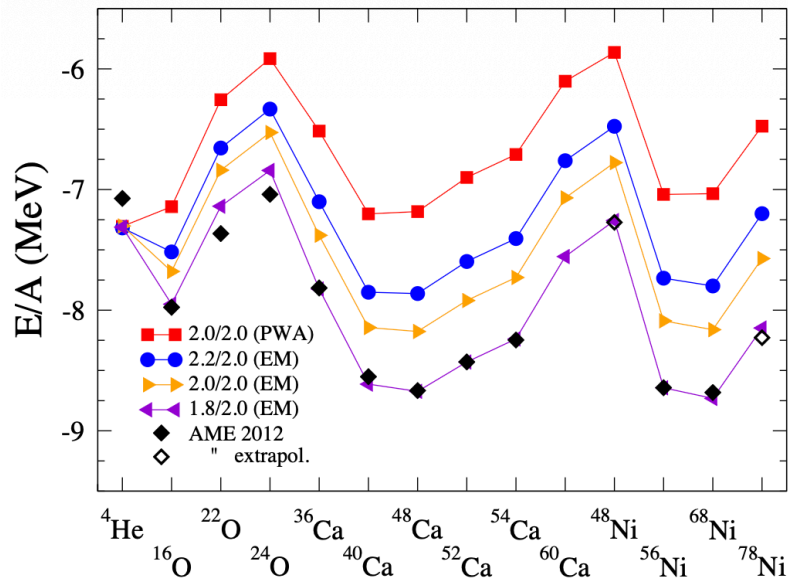
with large $c_D = 7.5$

Chiral NN+3N interactions up to ^{208}Pb

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[Arthuis, Hebeler, AS, arXiv:2401.06675](#)

with large $c_D = 7.5$

Chiral NN+3N interactions up to ^{208}Pb

other NN+3N interactions for global ab initio calcs [see Gaute's talk](#)

- Δ -full interactions $\Delta\text{N}^2\text{LO}_{\text{GO}}$ [Jiang et al., PRC \(2020\)](#)
fit to very low-energy NN scattering and $A=3,4$,
optimized to nuclear matter/medium-mass nuclei
- nonimplausible $\Delta\text{N}^2\text{LO}$ interactions [Hu et al., Nat. Phys. \(2024\)](#)
similar strategy plus conservative uncertainty quantification
- $\text{N}^3\text{LO}_{\text{Texas}}$ mixed NN $\text{N}^3\text{LO} + 3\text{N } \text{N}^2\text{LO}$ [Hu et al., arXiv:2512.11723](#)
similar fitting strategy, including also higher energy NN scattering
- Lattice EFT: NN $\text{N}^3\text{LO} + 3\text{N } \text{N}^2\text{LO}$ [Elhatisari et al., Nature \(2024\)](#)
+ 6 additional 3N parameters adjusted to selected nuclei
- order-by-order $\text{LO} \dots \text{N}^3\text{LO}$ [Hüther et al., PLB \(2020\)](#)
based on EMN NN with consistent 3N SRG evolved,
but for unevolved interactions 3N fits to ^{16}O not possible with EMN

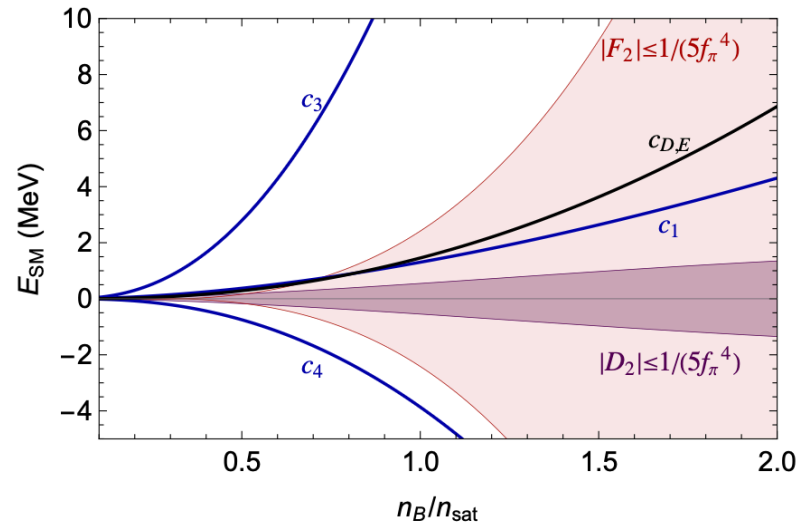
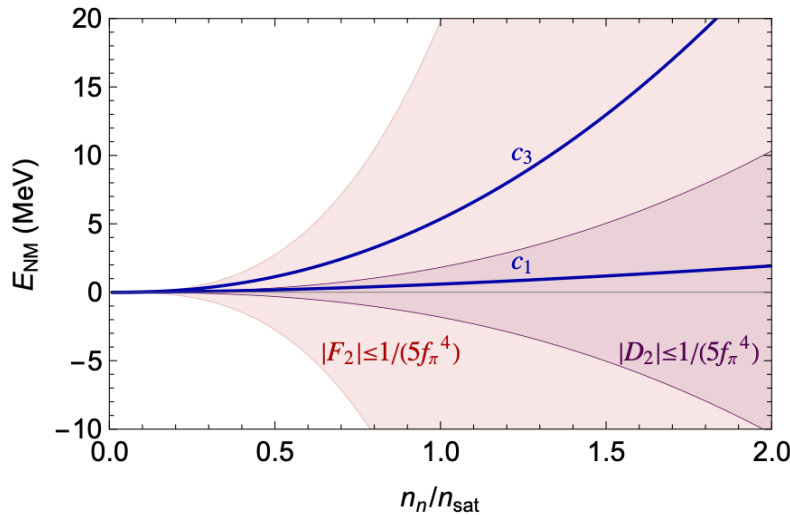
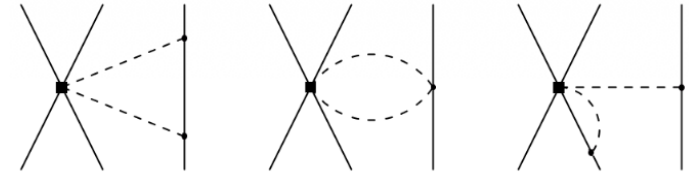
Quark mass dependent 3N forces

Cirigliano, Dawid, Dekens, Reddy, PRL (2025)

suggested class of $N^4\text{LO}$ 3N forces

may be as large as N^2 or 3LO

see Hartree-Fock calcs for nuclear matter



explore dominant F_2 interaction in medium-mass nuclei

Vernik, Hebeler, AS, arXiv:2512.20454

define F_2 in units F_π^{-4} , so range above is ± 0.2

3N fits to ${}^3\text{H}$ energy and ${}^{16}\text{O}$ energy/radius

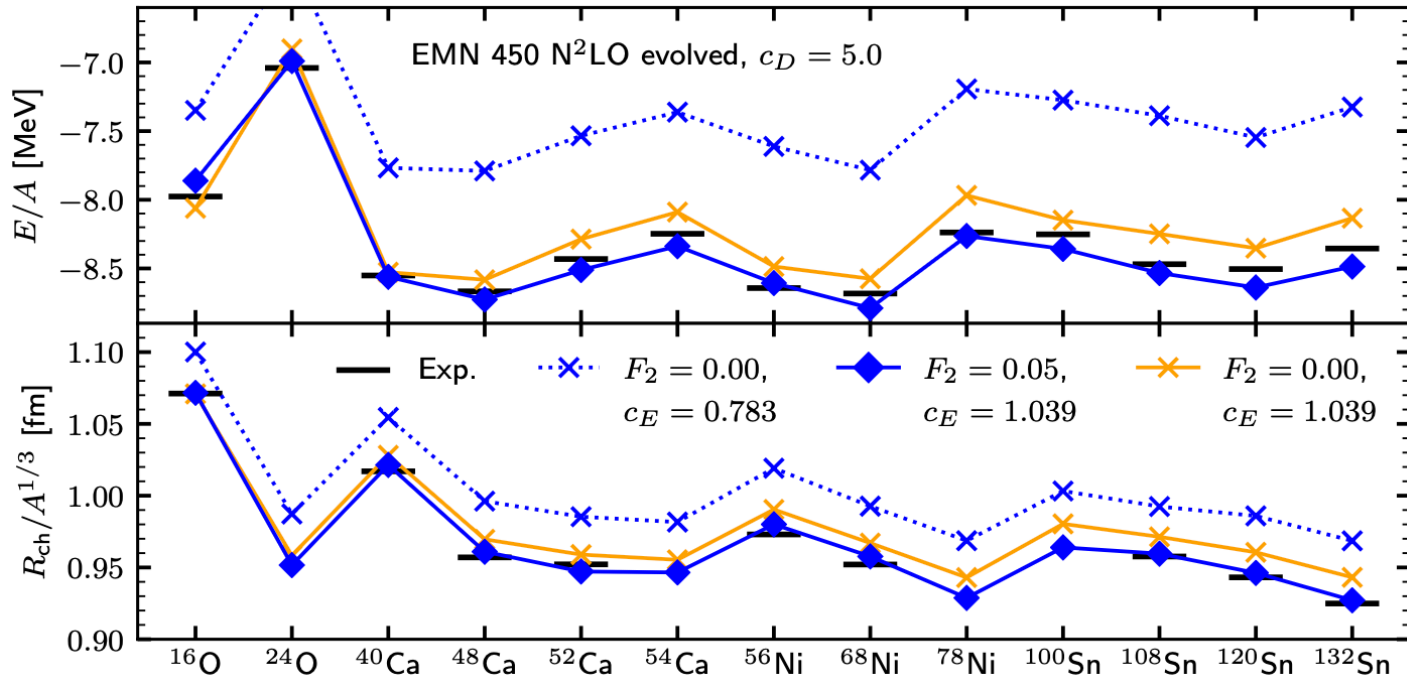
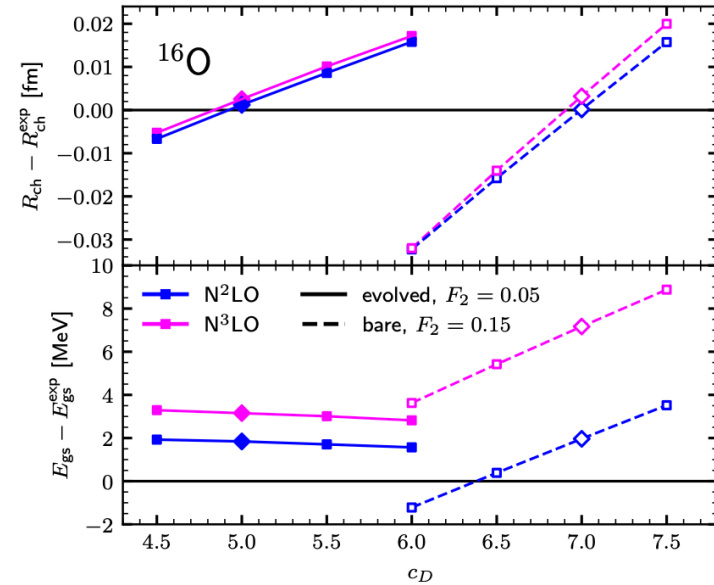
(also studied fits to ${}^3\text{H}$ energy and half-life, not as promising for nuclei)

Quark mass dependent 3N forces

Vernik, Hebeler, AS, arXiv:2512.20454

3N fits to ${}^3\text{H}$ energy and ${}^{16}\text{O}$ energy/radius possible for unevolved and evolved NN

good reproduction of energies/radii up to ${}^{132}\text{Sn}$ at NN+3N N^2LO and N^3LO both large $c_D = 5$

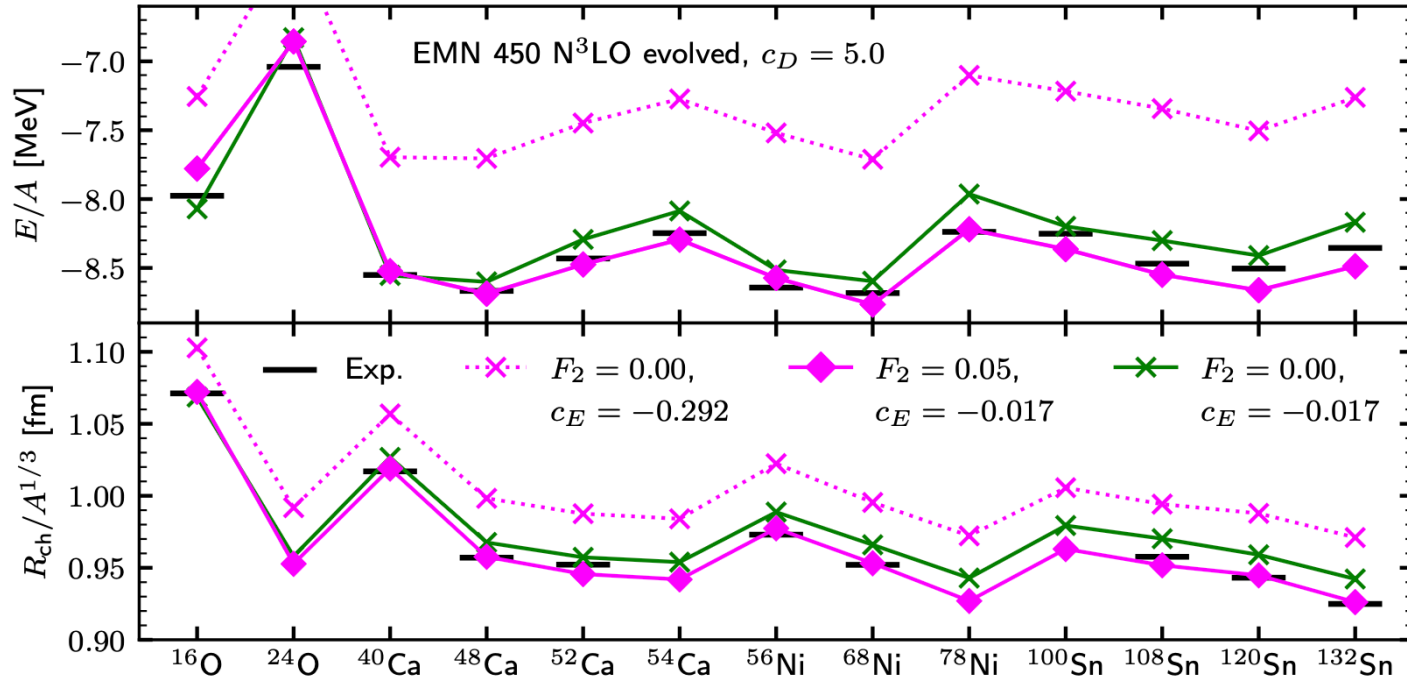
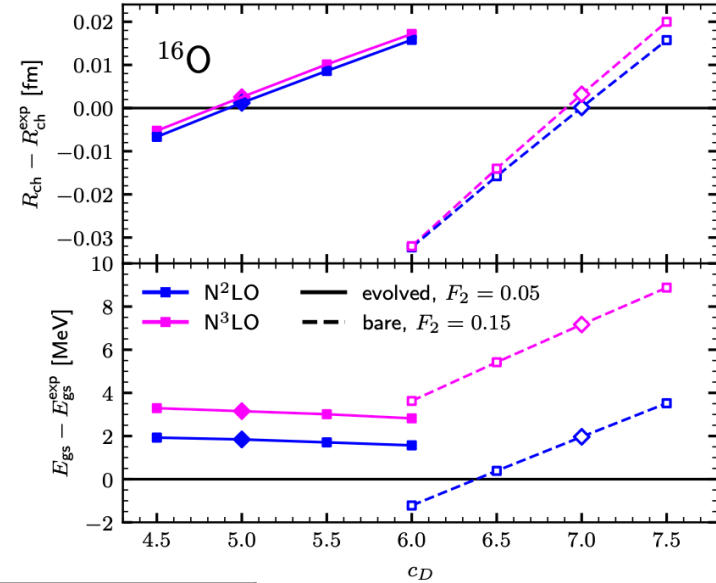


Quark mass dependent 3N forces

Vernik, Hebeler, AS, arXiv:2512.20454

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Quark mass dependent 3N forces

Vernik, Hebeler, AS, arXiv:2512.20454

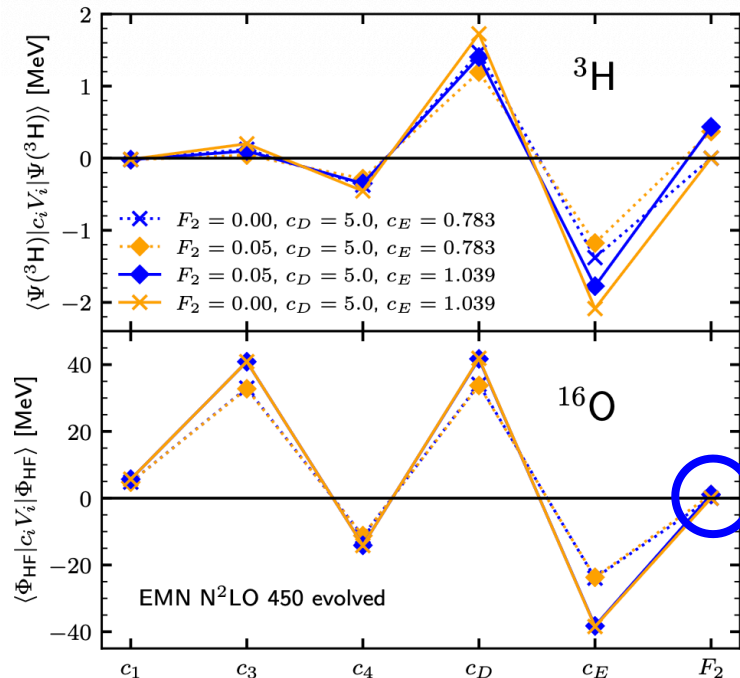
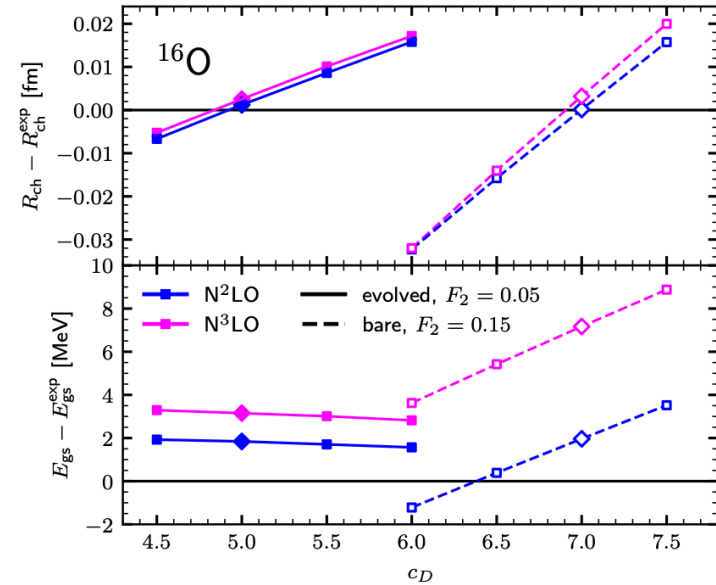
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good reproduction of energies/radii up to ${}^{132}\text{Sn}$ at NN+3N N^2LO and N^3LO both large $c_D = 5$

however: main effect of F_2 is to shift short-range 3N c_E

F_2 itself has very small impact on energies of nuclei

seems more natural to include F_2 with other small short-range 3N terms at N^4LO



Next generation NN+3N interactions: Wish list

- Low resolution enough for converged calculations up to ^{208}Pb
- Order-by-order interactions amenable to UQ, at least two orders with 3N
- Interactions for different cutoffs/schemes
- Good description of NN scattering and $A=3,4$ systems
- Pion-full: leading two-body currents are parameter-free, 3-neutron interactions parameter-free up to N^3LO

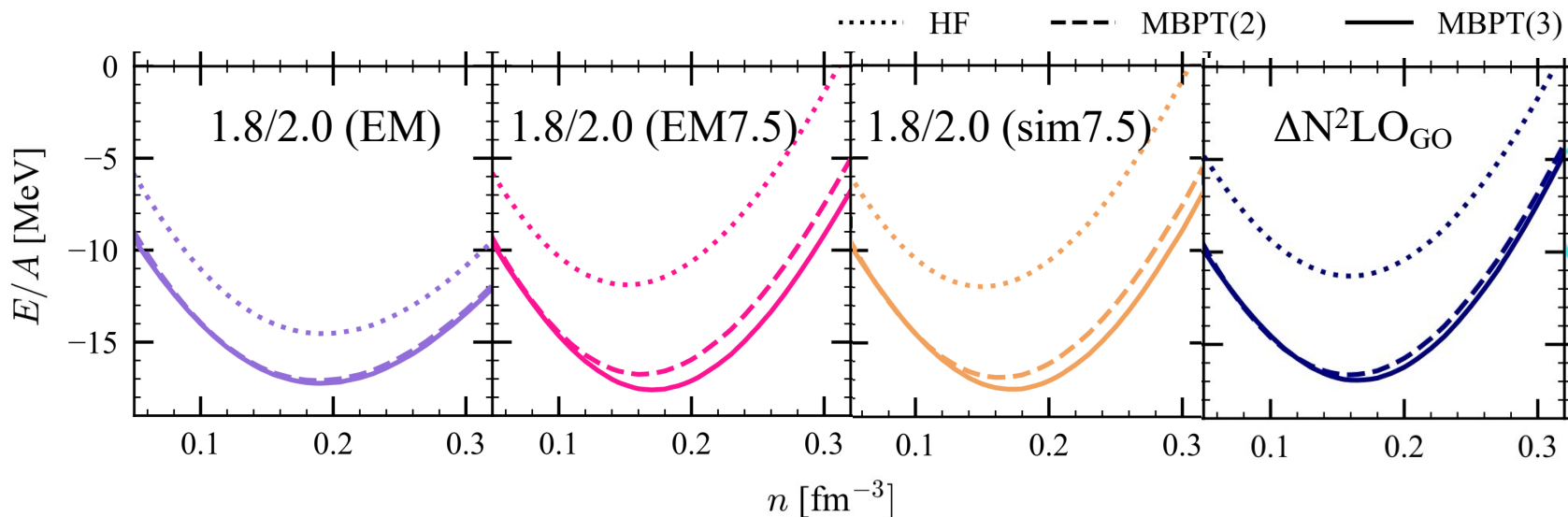
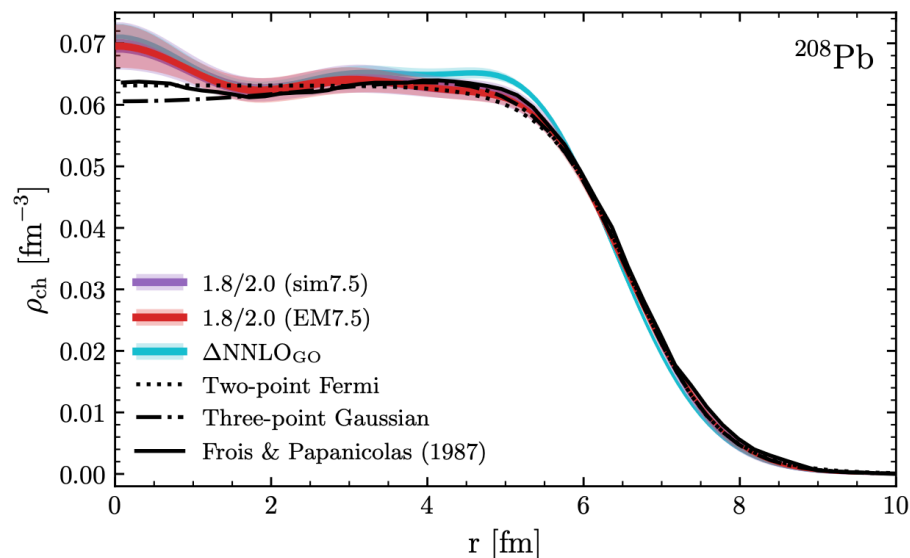
Density distributions in nuclei

Arthuis, Hebeler, AS, arXiv:2401.06675, see also Matthias' talk

good agreement for density distributions up to ^{208}Pb

for these interactions
reasonable radii and densities
at Hartree-Fock level
compare with nuclear matter results

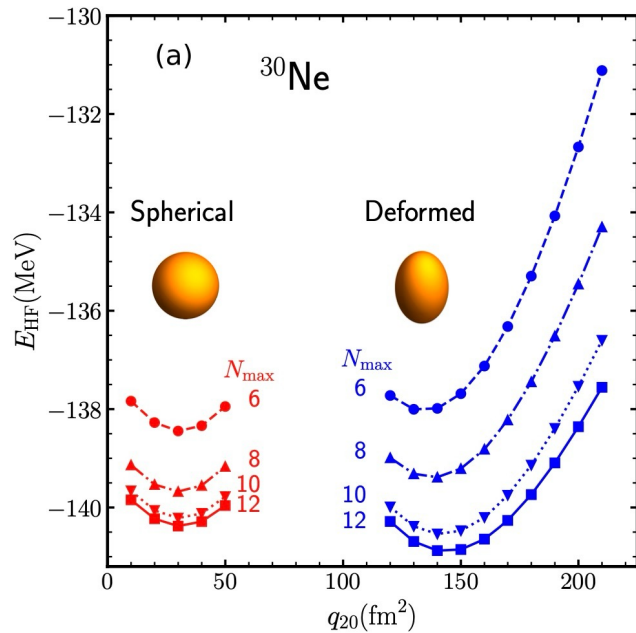
Alp, Dietz, Hebeler, AS, PRC (2025)



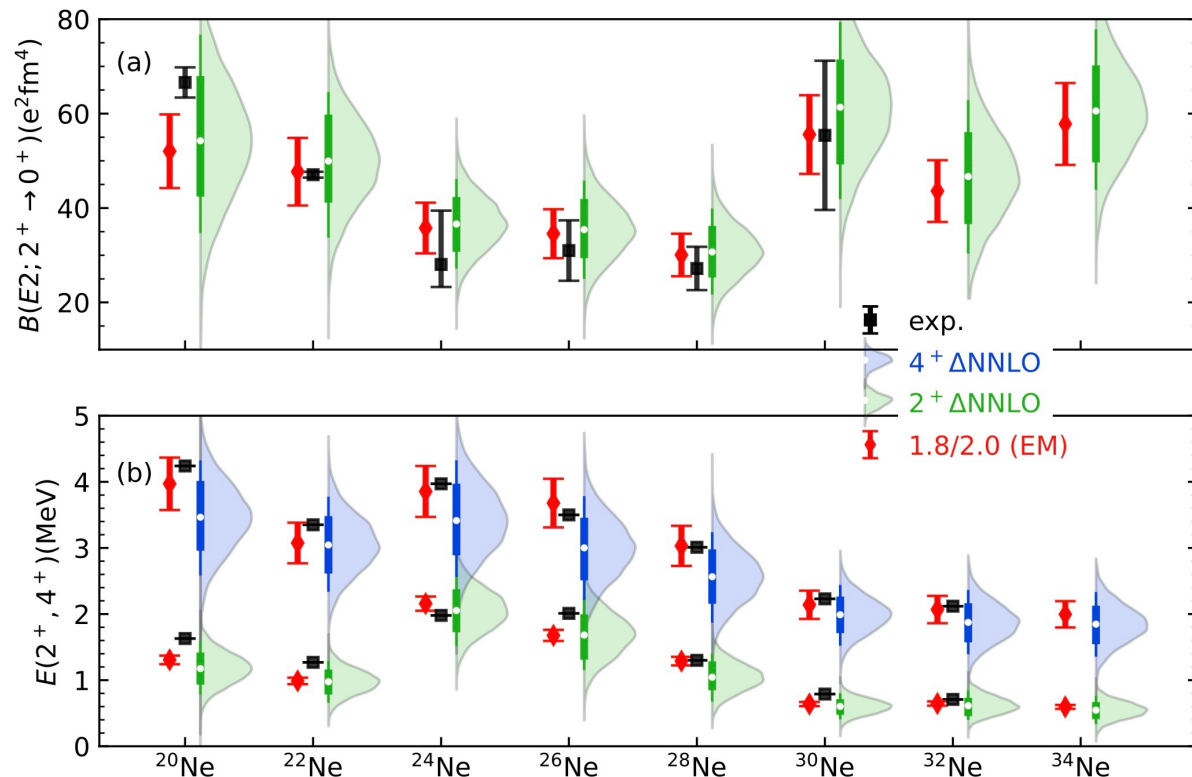
Ab initio calculations of deformed nuclei

Sun et al., PRX (2025)

can explore shapes at the Hartree-Fock level



deformed coupled-cluster theory to include correlations on top of Hartree-Fock shape

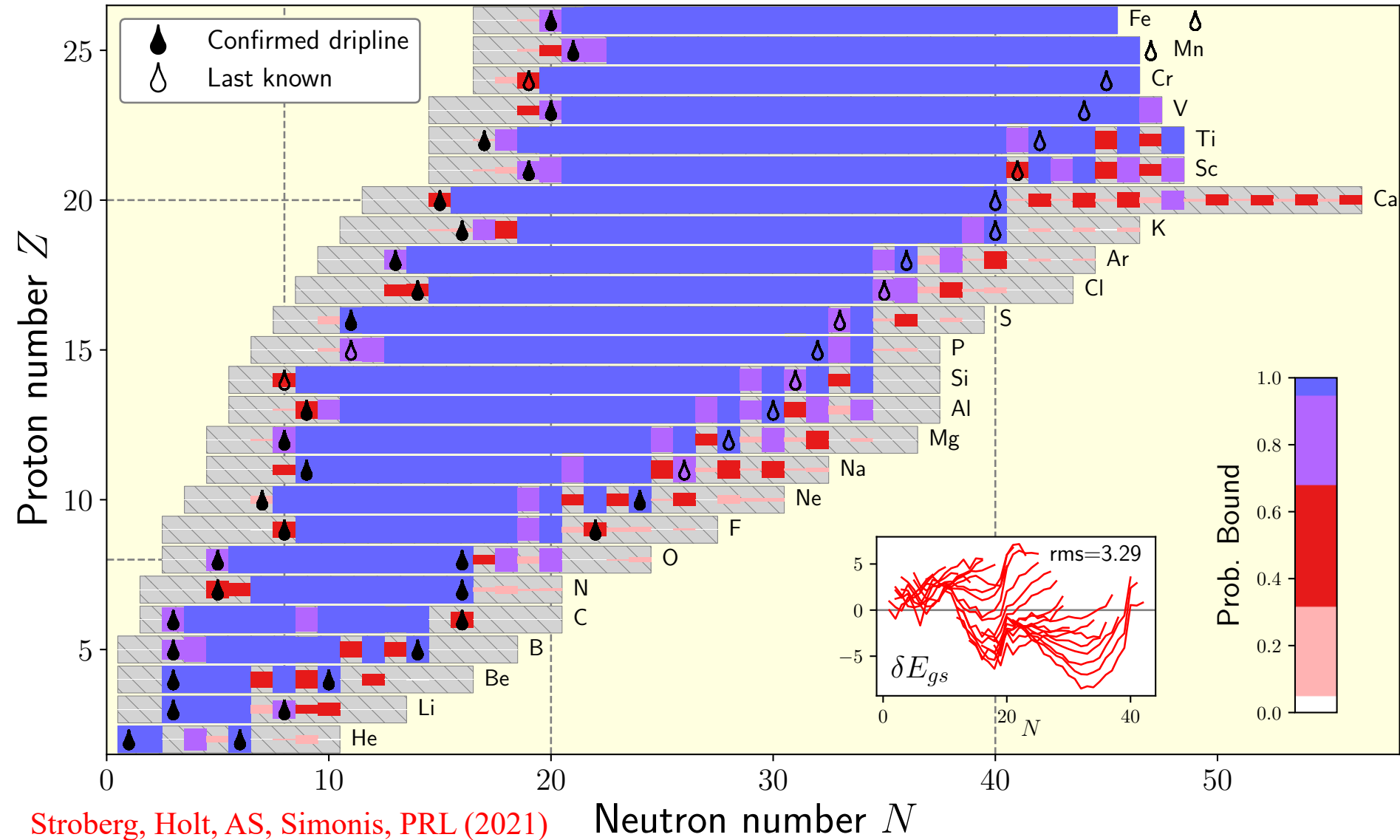


Need to overcome 3N normal ordering challenges to go beyond $A \sim 100$

Next generation NN+3N interactions: Wish list

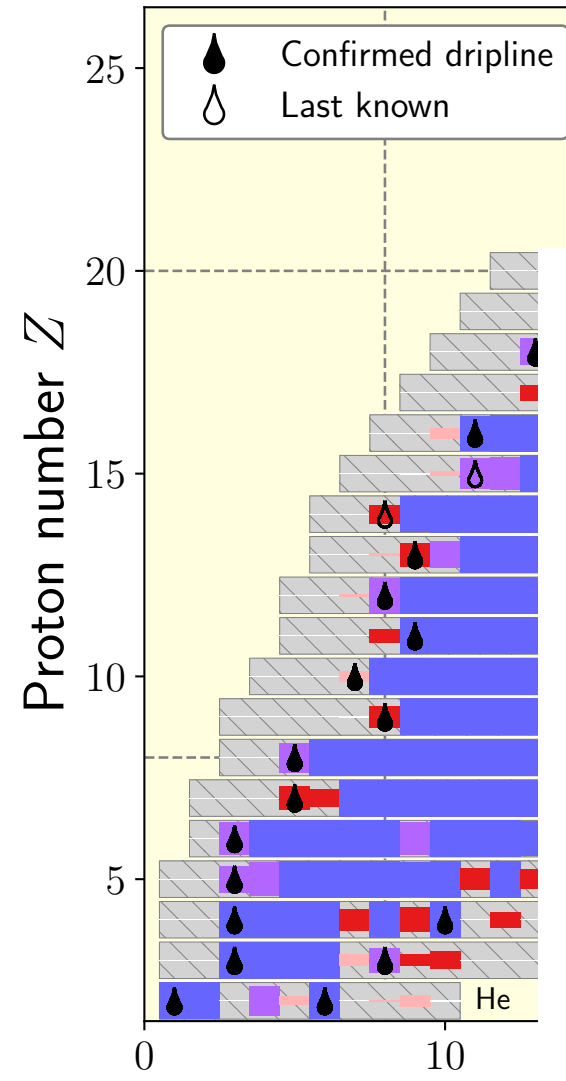
- Low resolution enough for converged calculations up to ^{208}Pb
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- Interactions for different cutoffs/schemes
- Good description of NN and $A=3,4$ systems
- Pion-full: leading two-body currents are parameter-free, 3-neutron interactions parameter-free up to $N^3\text{LO}$
- Reasonable saturation properties (informed by matter/nuclei), reasonable saturation density at HF level?

Nuclear landscape based on a chiral NN+3N interaction

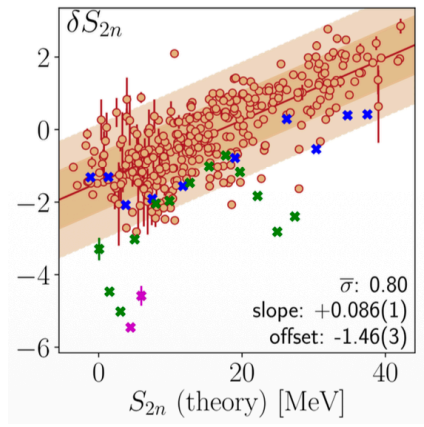


global ab initio calculations, but limited uncertainty estimate for NN+3N

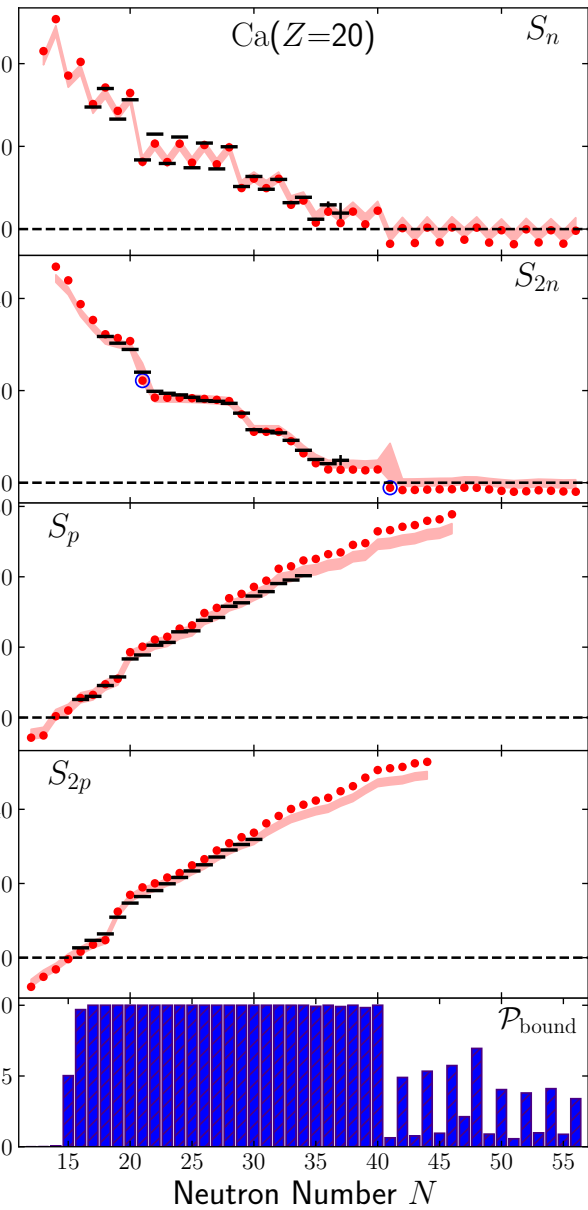
Nuclear landscape based on a chiral NN+3N interaction



Final predictions include systematic uncertainty from residuals to known masses



incl. syst. uncertainties:
dripline at ^{61}Ca or beyond



Stroberg, Holt, AS, Simonis,

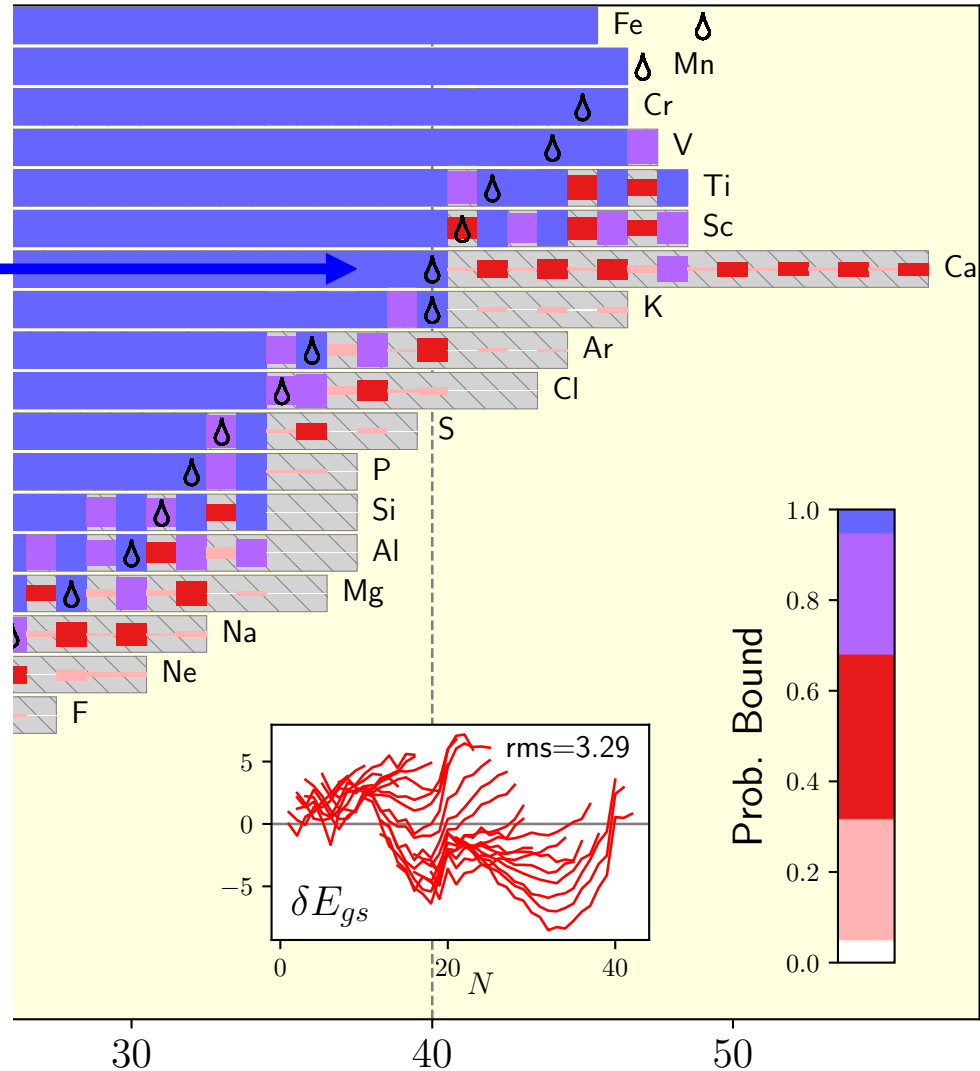
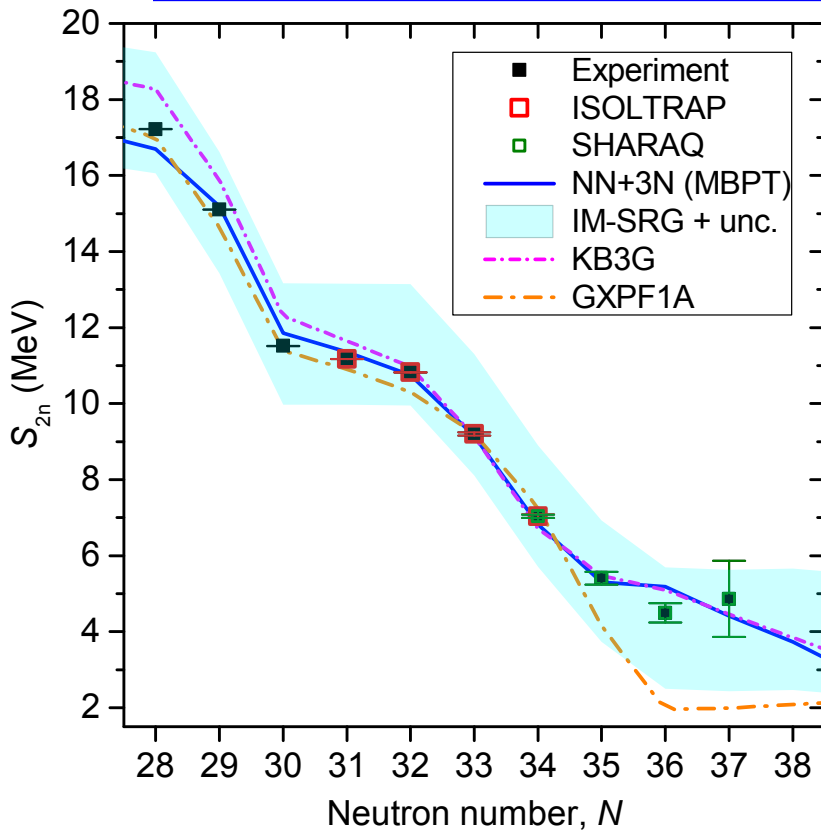
global ab initio calculations, but limited uncertainty estimate for NN+3N

Neutron-rich calcium masses

active exp-theory collaborations for rare isotopes

pioneering $^{51-57}\text{Ca}$ masses

Gallant et al., PRL (2012), Wienholtz et al.,
Nature (2013), Michimasa et al., PRL (2019)



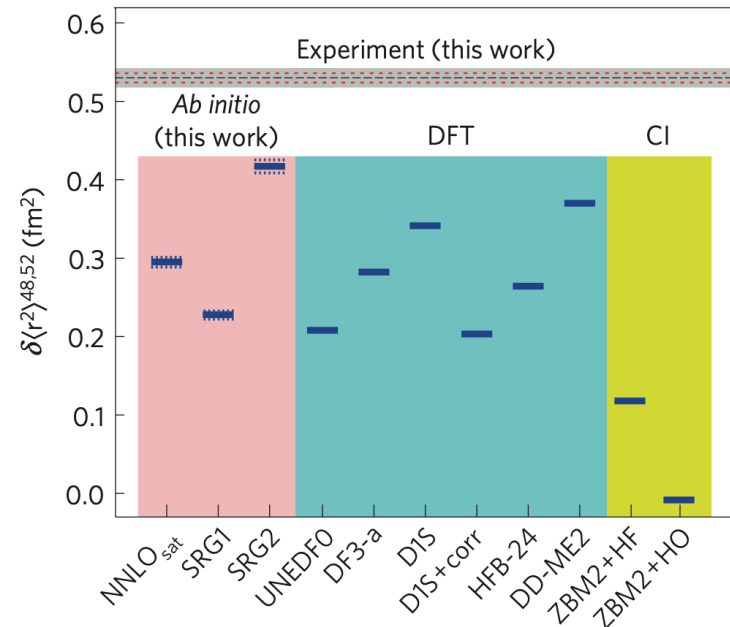
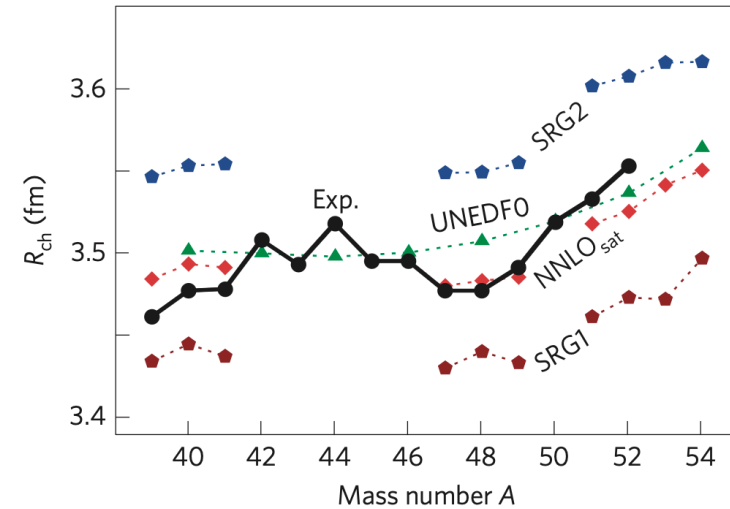
^{52}Ca - ^{48}Ca radius puzzle

Unexpectedly large charge radii of neutron-rich calcium isotopes

R. F. Garcia Ruiz^{1*}, M. L. Bissell^{1,2}, K. Blaum³, A. Ekström^{4,5}, N. Frömmgen⁶, G. Hagen⁴, M. Hammen⁶, K. Hebeler^{7,8}, J. D. Holt⁹, G. R. Jansen^{4,5}, M. Kowalska¹⁰, K. Kreim³, W. Nazarewicz^{4,11,12}, R. Neugart^{3,6}, G. Neyens¹, W. Nörtershäuser^{6,7}, T. Papenbrock^{4,5}, J. Papuga¹, A. Schwenk^{3,7,8}, J. Simonis^{7,8}, K. A. Wendt^{4,5} and D. T. Yordanov^{3,13}

Challenging to reproduce large charge radius increase from ^{48}Ca to ^{52}Ca with ab initio calculations

Challenge: Uncertainties greatly reduced in differential, correlated quantities



Possible solutions to the ^{52}Ca - ^{48}Ca radius puzzle?

Due to 3N variations?

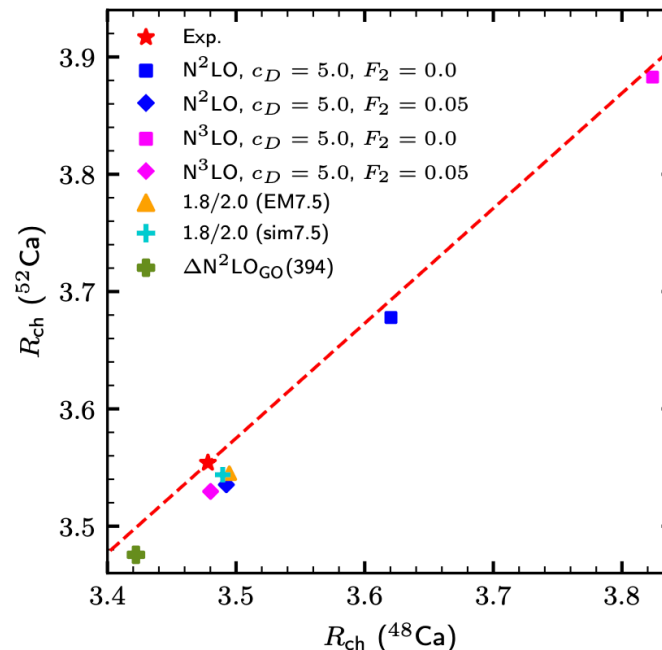
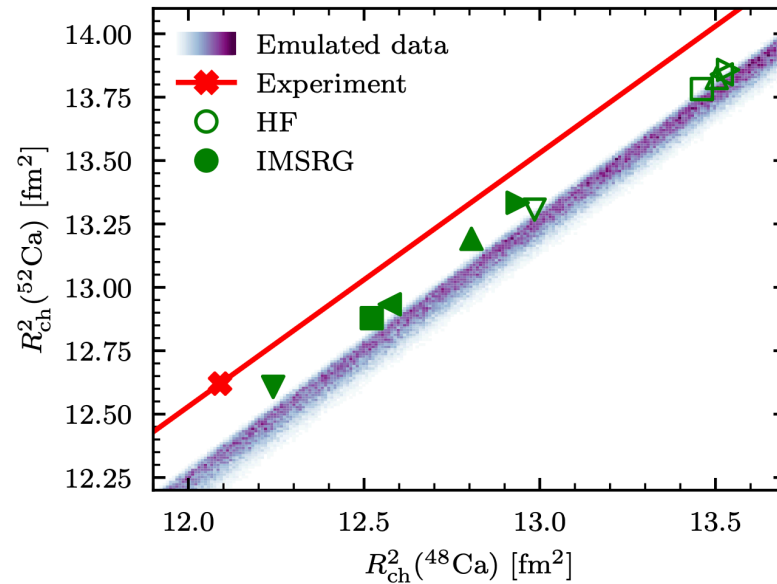
Comanys Franzke, Tichai, Hebeler, AS,
arXiv:2510.08362

broad variations of
 c_3 , c_4 , c_D , c_E also
highly correlated,
do not solve puzzle

Due to quark mass dependent
3N forces?

Vernik, Hebeler, AS, arXiv:2512.20454

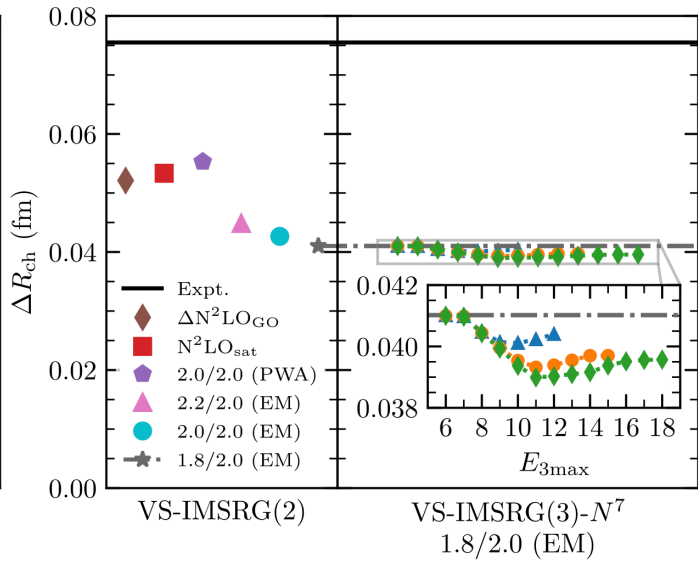
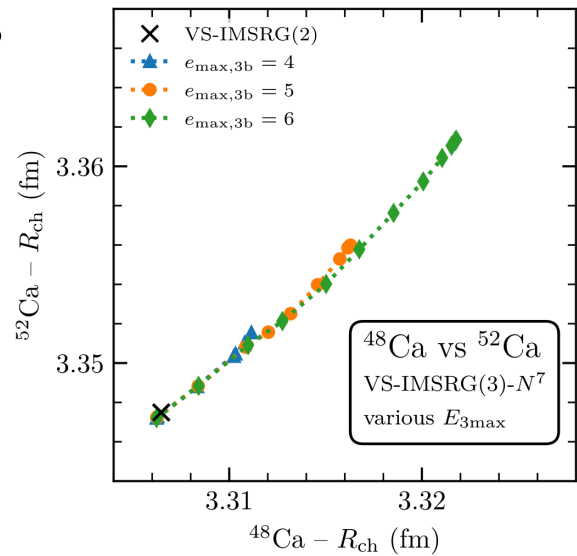
Other NN interactions
have so far not solved
puzzle either...



Possible solutions to the ^{52}Ca - ^{48}Ca radius puzzle?

Due to many-body uncertainties? [Heinz et al., PRC \(2025\)](#)

many-body truncations
highly correlated, so
change IMSRG(2 \rightarrow 3)
is very small for
radius increase



Remaining many-body possibilities:

- collective many-body correlations beyond IMSRG(3)
- approximations related to reference state
- normal ordering approximation
- ...

Outline

Chiral EFT interaction uncertainties and challenges

with P. Arthuis, M. Companys, K. Hebeler, A. Tichai, U. Vernik

Next generation NN+3N interactions: Wish list

with F. Alp, Y. Dietz, K. Hebeler

Ab initio nuclear masses for r-process nucleosynthesis

with J. Kuske, T. Miyagi, A. Arcones

Uncertainty quantification and correlated mass model for calcium isotopes

with M. Cincar, Z. Li, T. Plies, U. Vernik, M. Heinz, T. Miyagi,
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Nuclear masses around N=82 and r-process nucleosynthesis

Kuske, Miyagi, Arcones, AS, arXiv:2509.19131

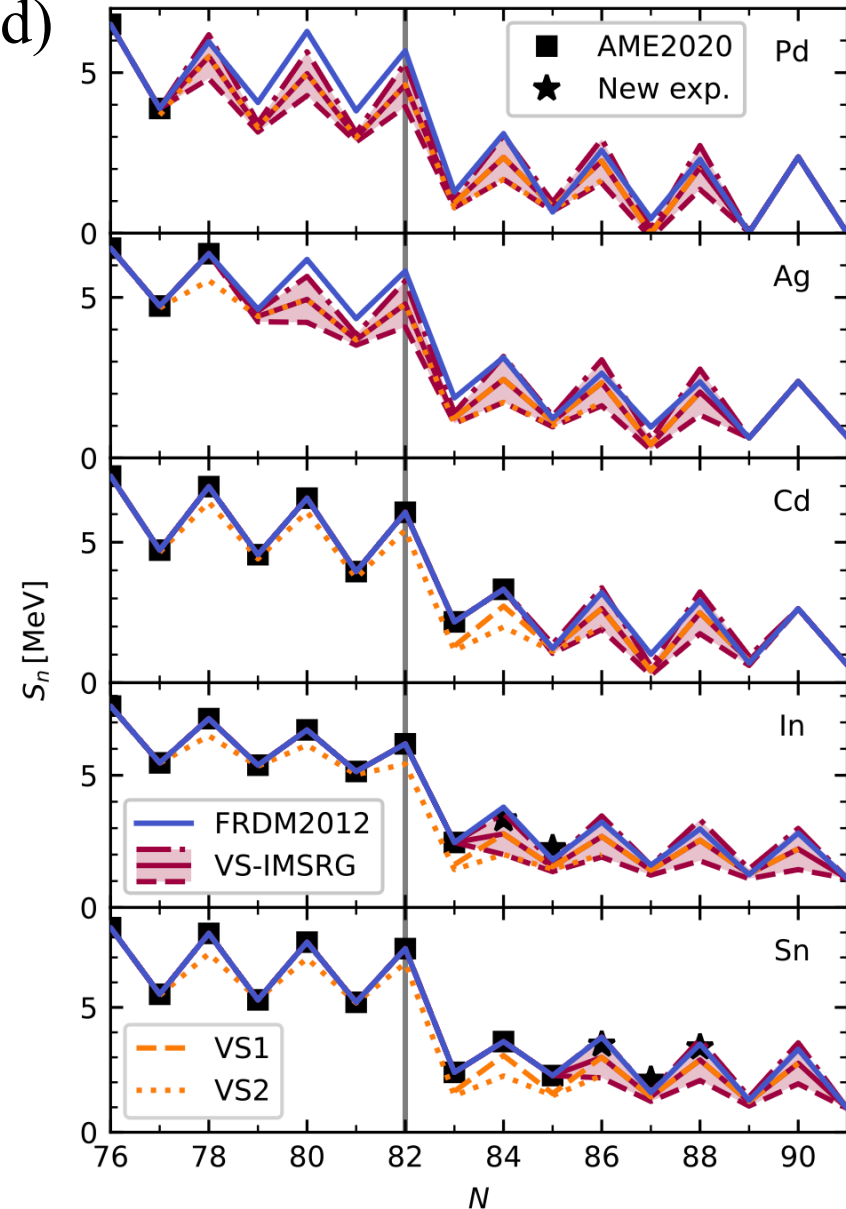
masses around N=82 (Sn, In, Cd, Ag, Pd)

→ interesting region at exp frontier

VS-IMSRG results with valence space
+ interaction uncertainties

separation energies have smaller
uncertainties due to correlations;
IMSRG(3f2) is within VS1, VS2

incorporate VS-IMSRG masses
with uncertainties (min/central/max)
in baseline AME2020 + FRDM2012



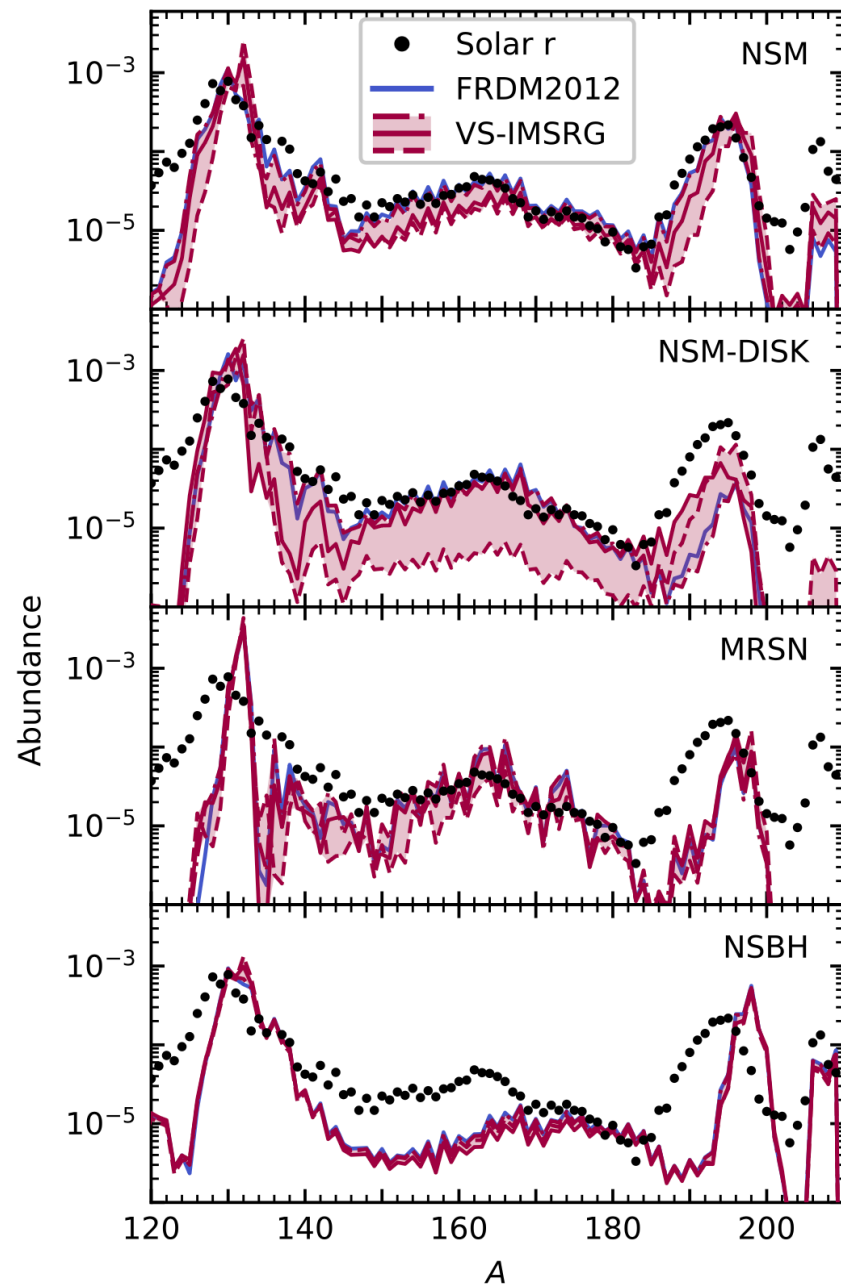
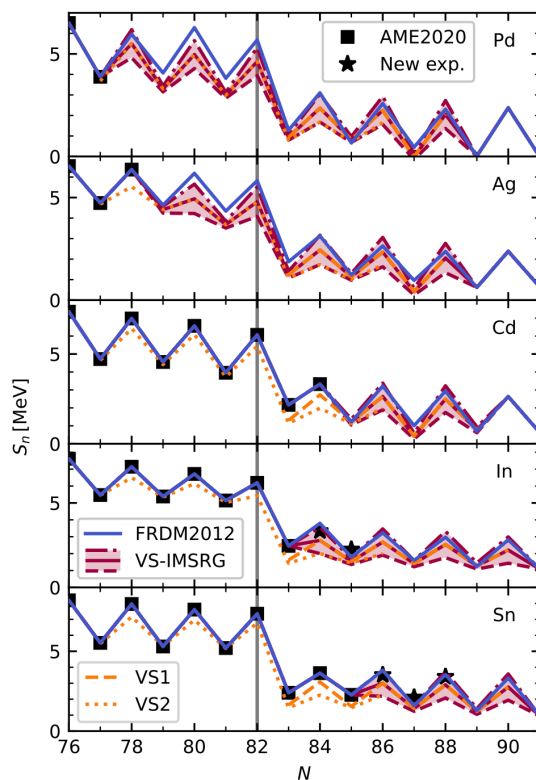
Nuclear masses around N=82 and r-process nucleosynthesis

Kuske, Miyagi, Arcones, AS, arXiv:2509.19131

VS-IMSRG masses (min/central/max)

in baseline AME2020 + FRDM2012

explore r-process predictions for
different astrophysics scenarios



Nuclear masses around N=82 and r-process nucleosynthesis

Kuske, Miyagi, Arcones, AS, arXiv:2509.19131

VS-IMSRG masses (min/central/max)

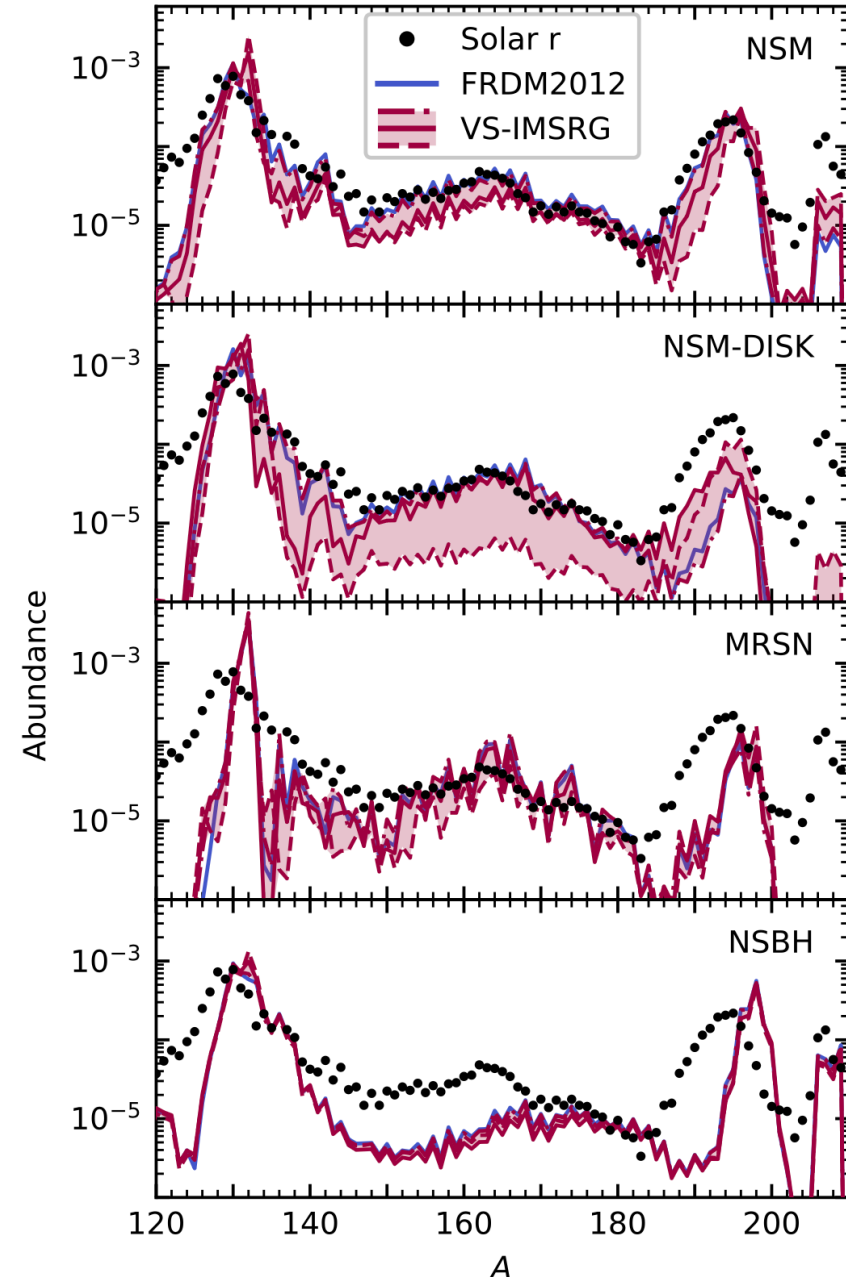
in baseline AME2020 + FRDM2012

explore r-process predictions for
different astrophysics scenarios

largest effects for n-star mergers
(NSM and NSM-DISK)

ab initio masses strengthen waiting
point of 2nd peak, leading to slower
nucleosynthesis flow, and important
impact on 3rd peak

future: use correlated ab-initio-based
mass model conditioned on data



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Uncertainty estimates for SRG-evolved interactions

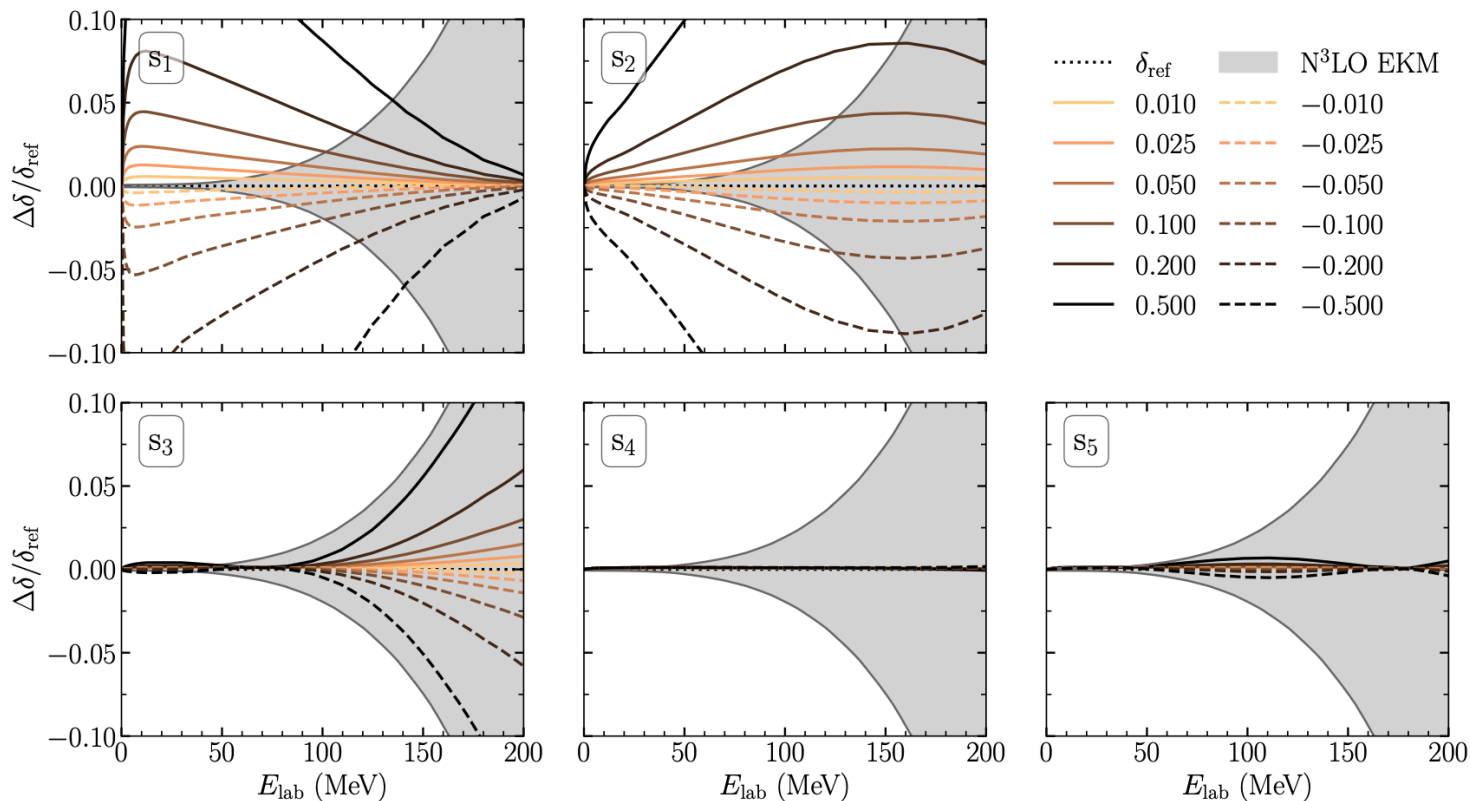
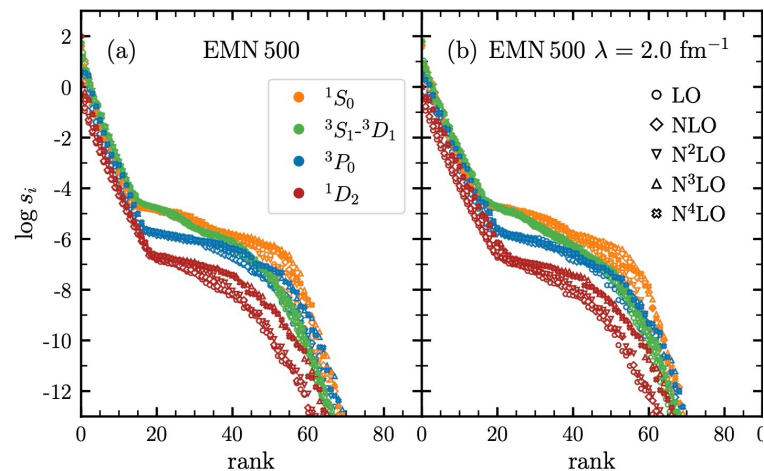
Plies, Heinz, AS, arXiv:2509.24671, see Matthias' talk

use singular value decomposition (SVD)

as operator basis see Tichai et al., PLB (2021)

consider largest 5 singular values/operators

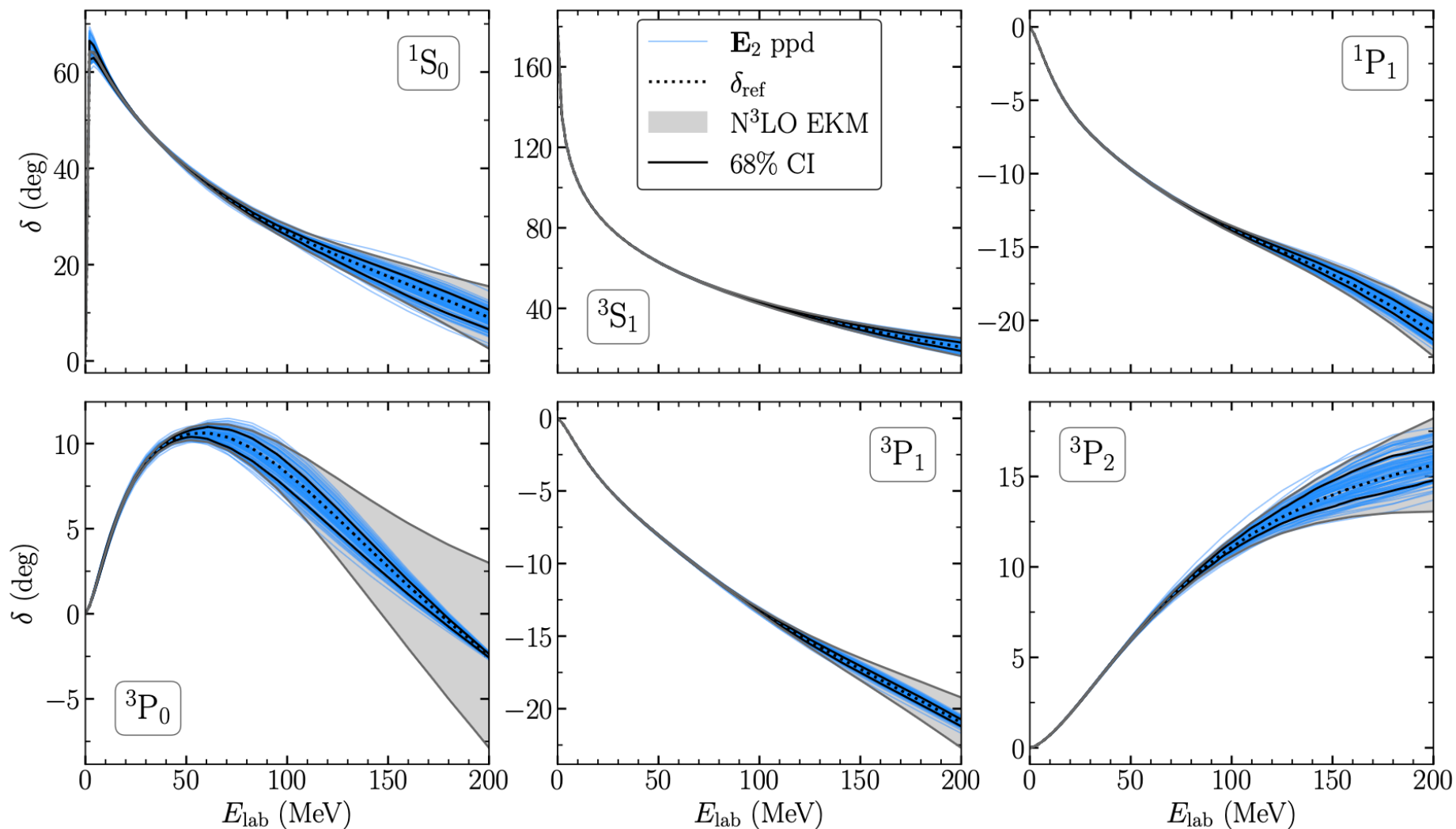
effectively 3 generate phase shift variation



Uncertainty estimates for SRG-evolved interactions

Plies, Heinz, AS, arXiv:2509.24671, see Matthias' talk

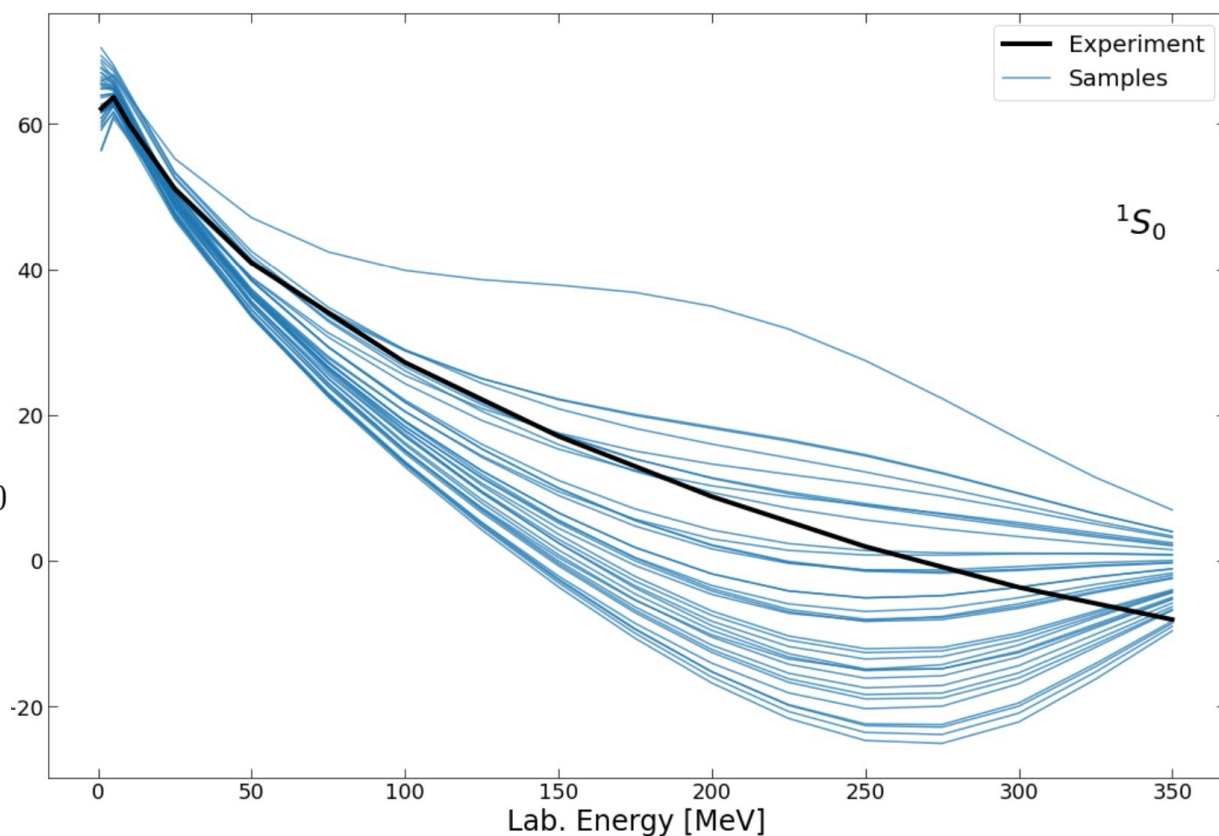
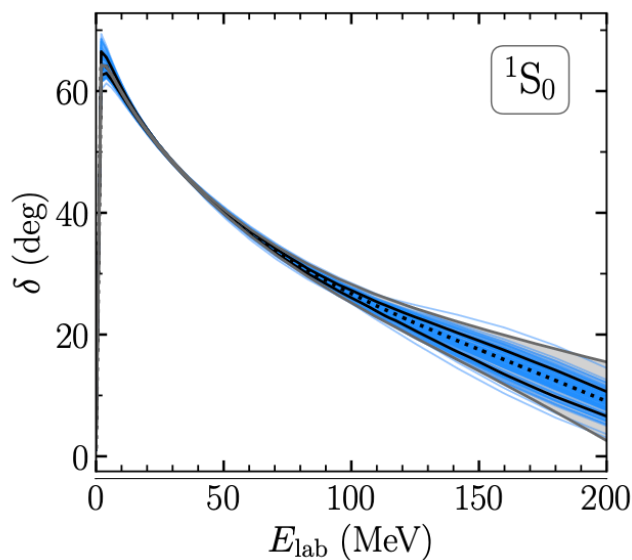
generate range of low-resolution NN interactions from random draws among 3 singular values with likelihood given by EFT uncertainties



Uncertainty estimates for SRG-evolved interactions

Plies, Heinz, AS, arXiv:2509.24671, see Matthias' talk

generate range of low-resolution NN interactions from random draws among 3 singular values with likelihood given by EFT uncertainties



comparison to nonimplausible $\Delta N^2\text{LO}$ interactions Ekström, Forssen et al.

Uncertainty estimates for SRG-evolved interactions

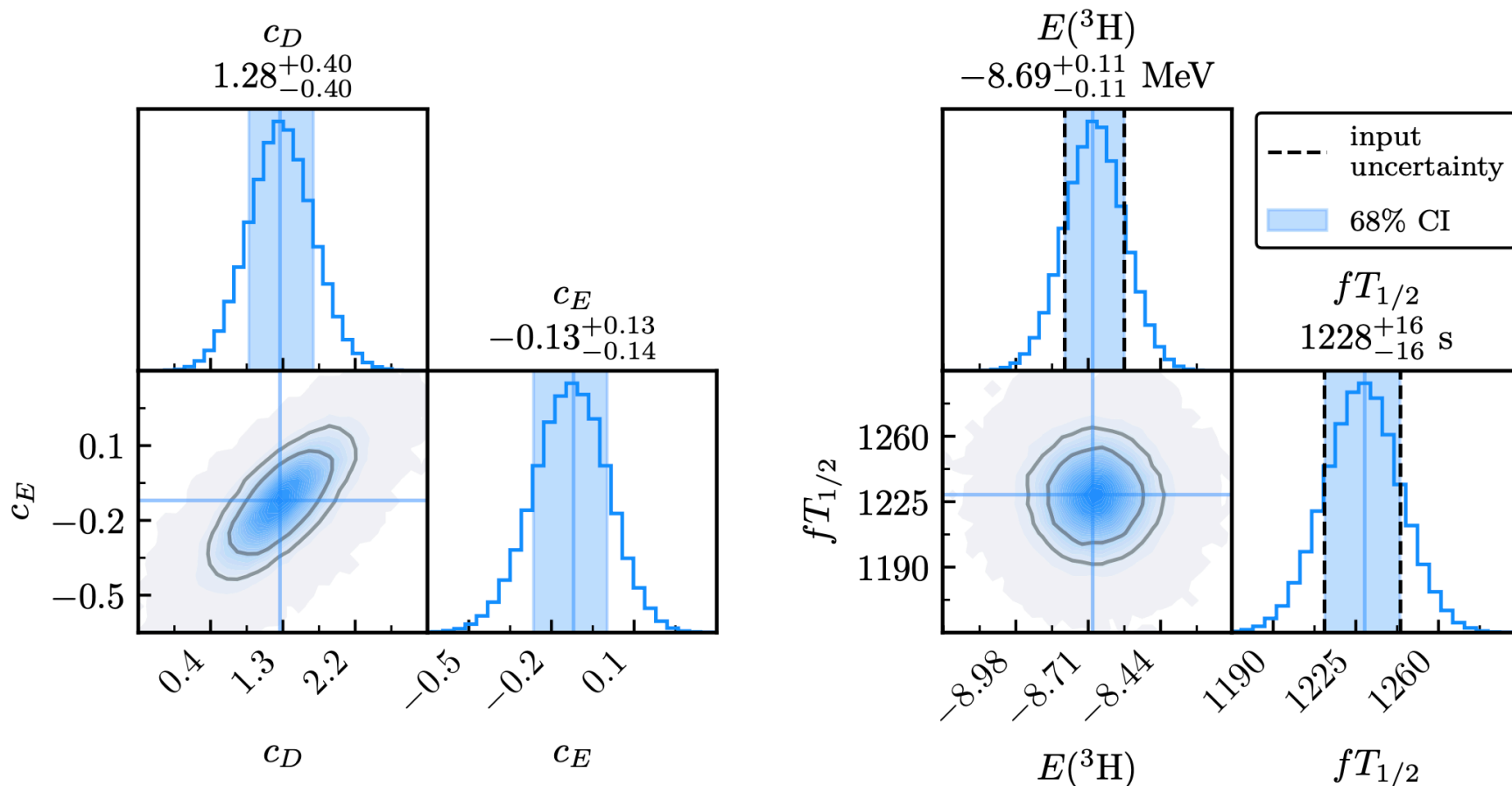
Plies, Heinz, AS, arXiv:2509.24671, see Matthias' talk

generate range of low-resolution NN+3N interactions

NN: S and P waves, higher partial waves unvaried

3N uncertainties from ${}^3\text{H}$ energy and half-life

following Wesolowski, Svensson et al., PRC (2021)



Uncertainty estimates for SRG-evolved interactions

Plies, Heinz, AS, arXiv:2509.24671, see Matthias' talk

generate range of low-resolution NN+3N interactions

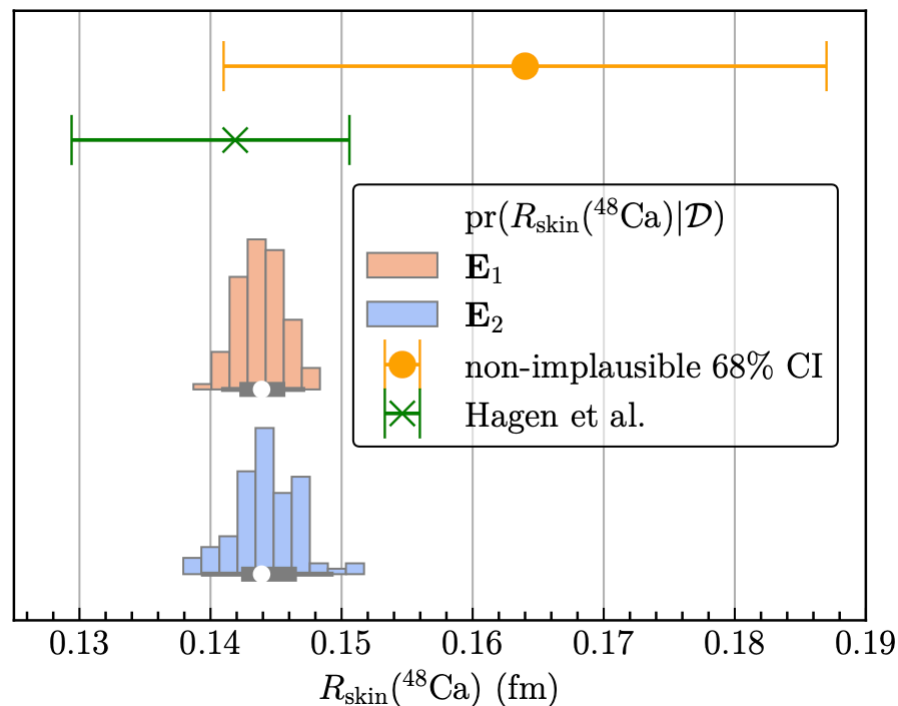
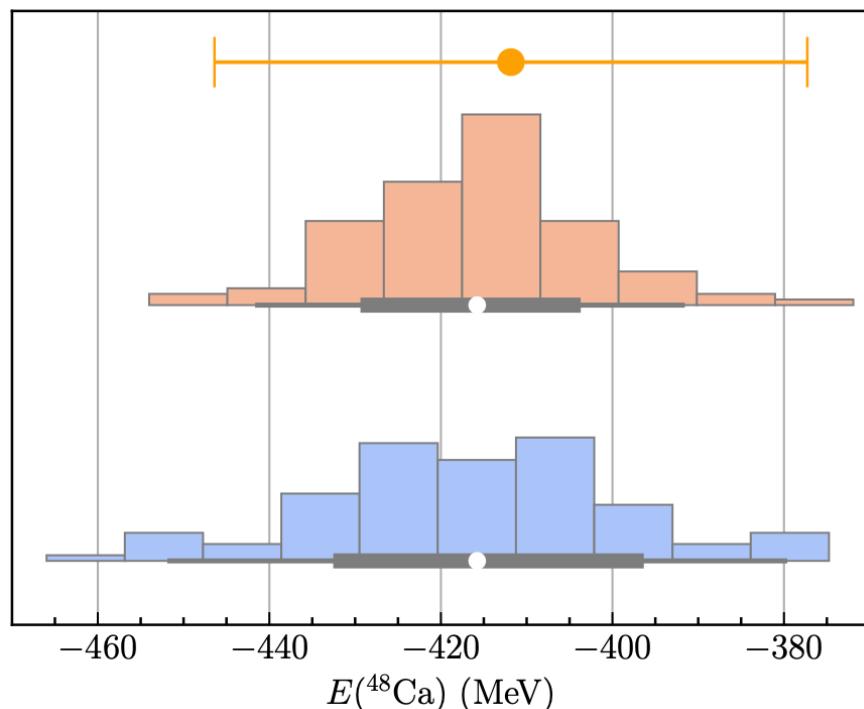
NN: S and P waves, higher partial waves unvaried

3N uncertainties from ${}^3\text{H}$ energy and half-life

following Wesolowski, Svensson et al., PRC (2021)

resulting posterior distributions for ${}^{48}\text{Ca}$ energy and neutron skin

Note: no explicit statistical model for truncation uncertainties included



Correlated mass model for calcium isotopes

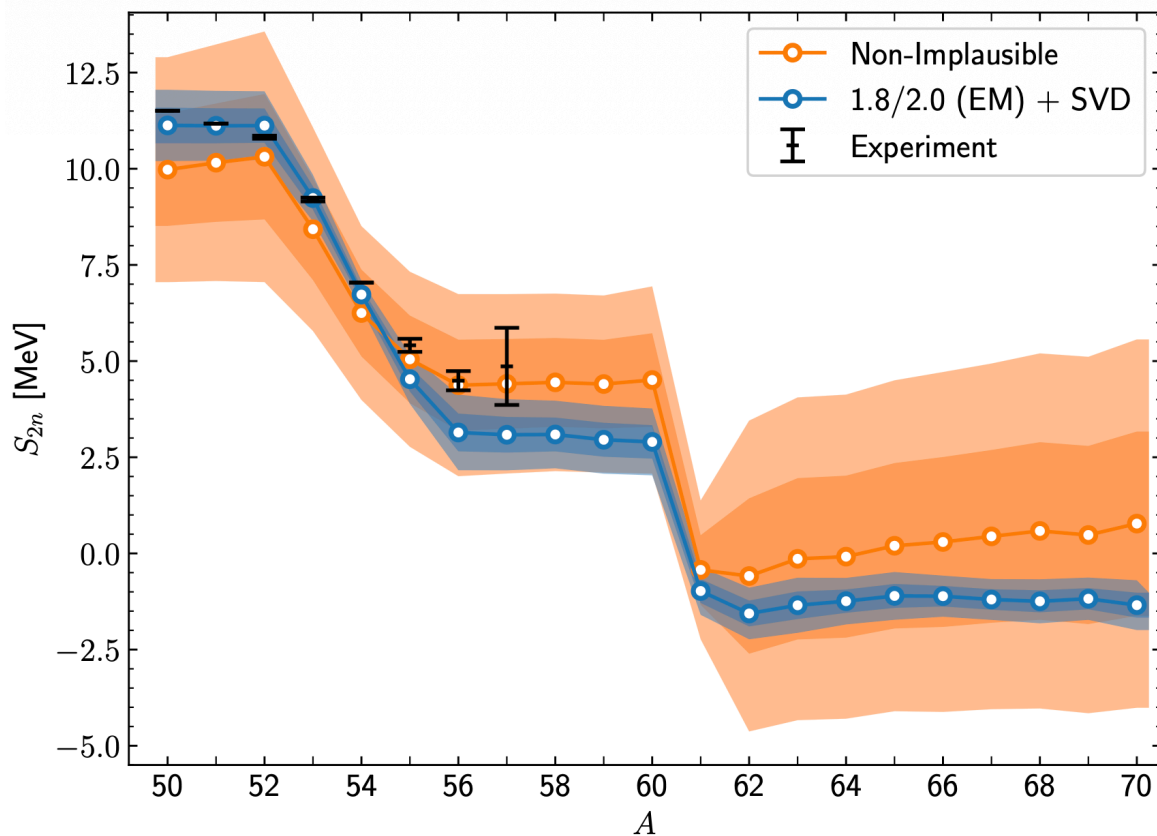
Cincar, Li, Plies, Vernik, Heinz, Miyagi, AS, in prep.

Goal: Build correlated ab-initio-based mass model for S_{2n} of Ca isotopes

Start from interaction distributions:

34 non-implausible interactions [Hu et al., Nature Phys. \(2022\)](#)

101 SVD variations for 1.8/2.0 (EM) [Plies, Heinz, AS, arXiv:2509.24671](#)



Correlated mass model for calcium isotopes

Cincar, Li, Plies, Vernik, Heinz, Miyagi, AS, in prep.

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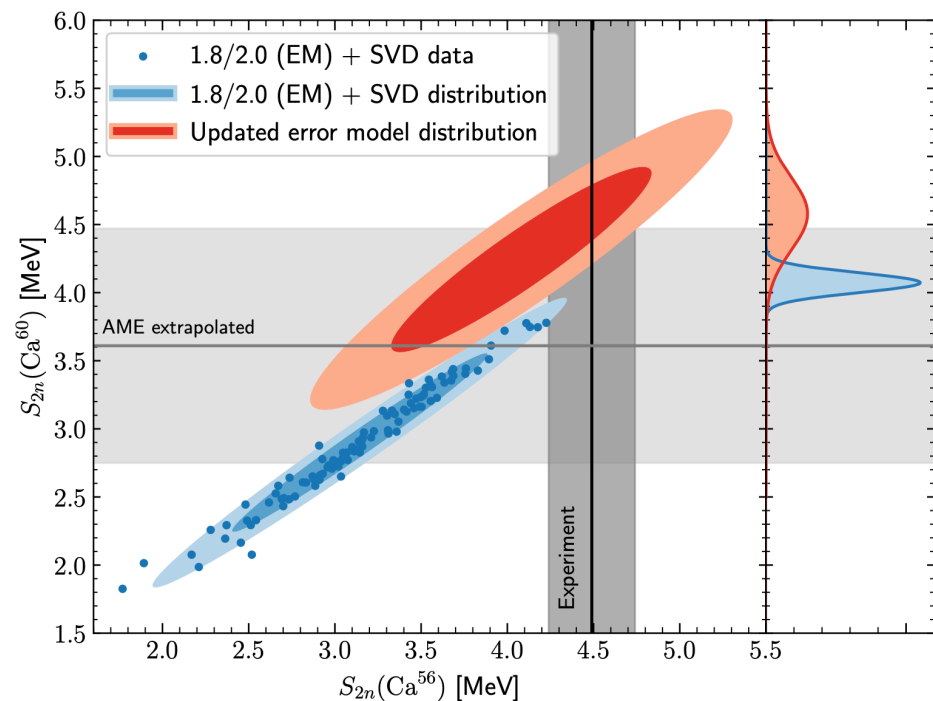
Start from interaction distributions: 34 NI, 101 SVD interactions

Include other uncertainties from:

- Many-body IMSRG(2, 3f2)
- Model space
- Systematic uncertainties

(assume ind. normally distr.)

Condition on exp. $S_{2n}({}^{50-56}\text{Ca})$
uses correlations among S_{2n}



Correlated mass model for calcium isotopes

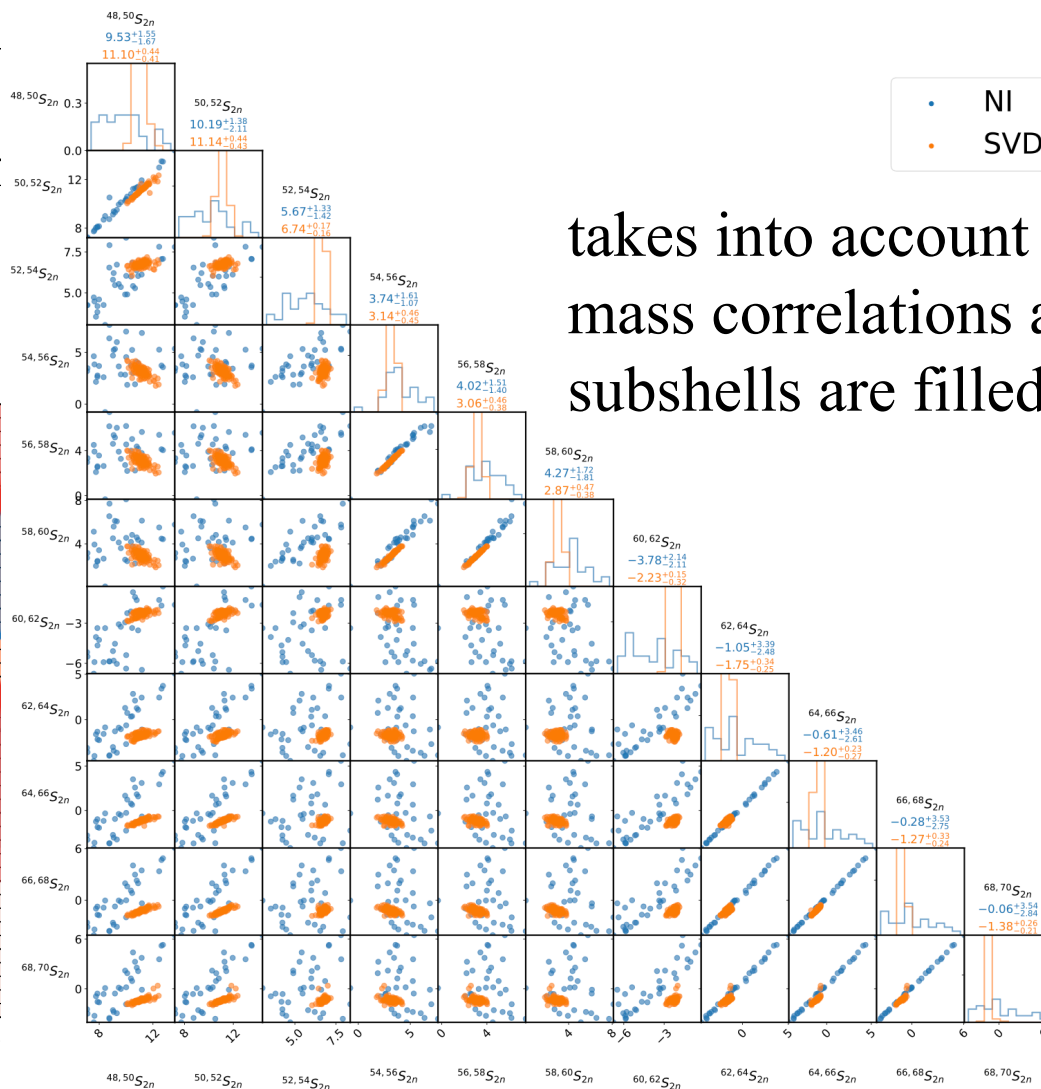
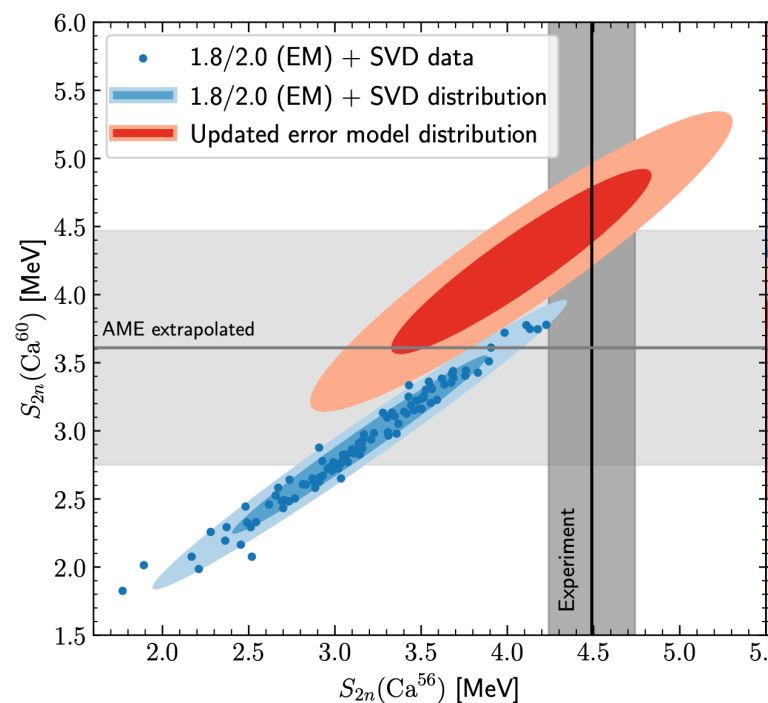
Cincar, Li, Plies, Vernik, Heinz, Miyagi, AS, in prep.

Goal: Build correlated ab-initio-based mass model for S_{2n} of Ca isotopes

Start from interaction distrib

Include other uncertainties fi
(assume ind. normally distr.)

takes into account
mass correlations as
subshells are filled



Correlated mass model for calcium isotopes

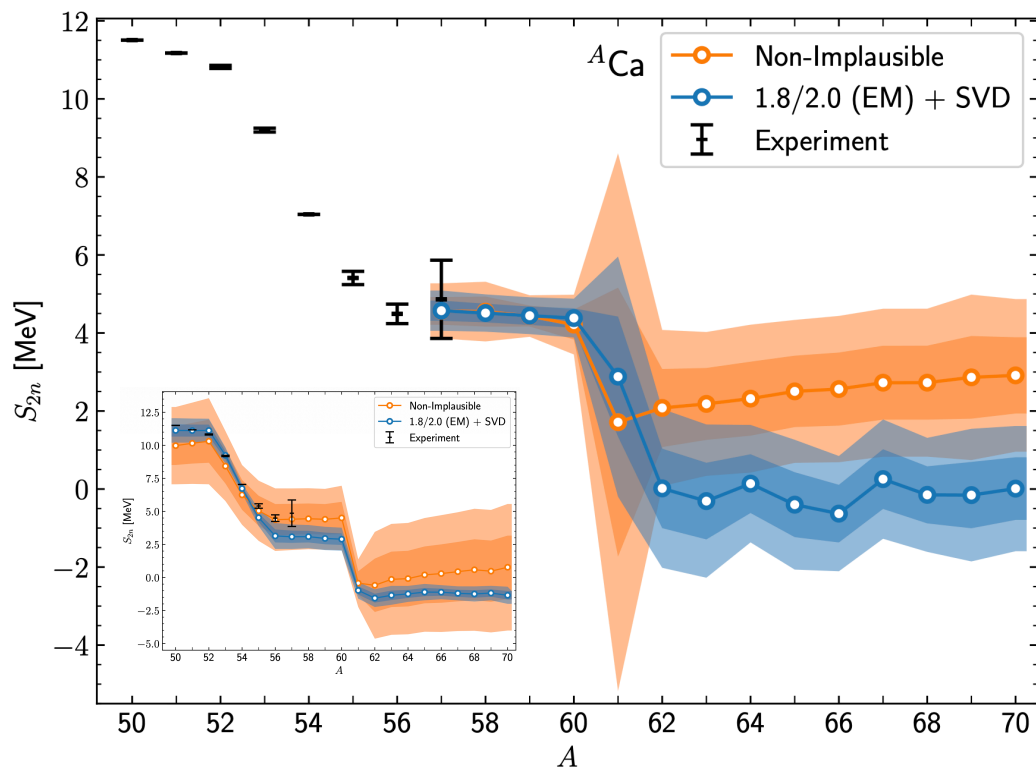
Cincar, Li, Plies, Vernik, Heinz, Miyagi, AS, in prep.

Goal: Build correlated ab-initio-based mass model for S_{2n} of Ca isotopes

Start from interaction distributions: 34 NI, 101 SVD interactions

Include other uncertainties: Many-body, model space, systematic

Leads to mass model with correlated uncertainties conditioned on data



large uncertainties for ^{61}Ca
due to $s_{1/2}$ or $g_{9/2}$ uncertainty

difficult to predict dripline
in Ca given theo. uncertainties

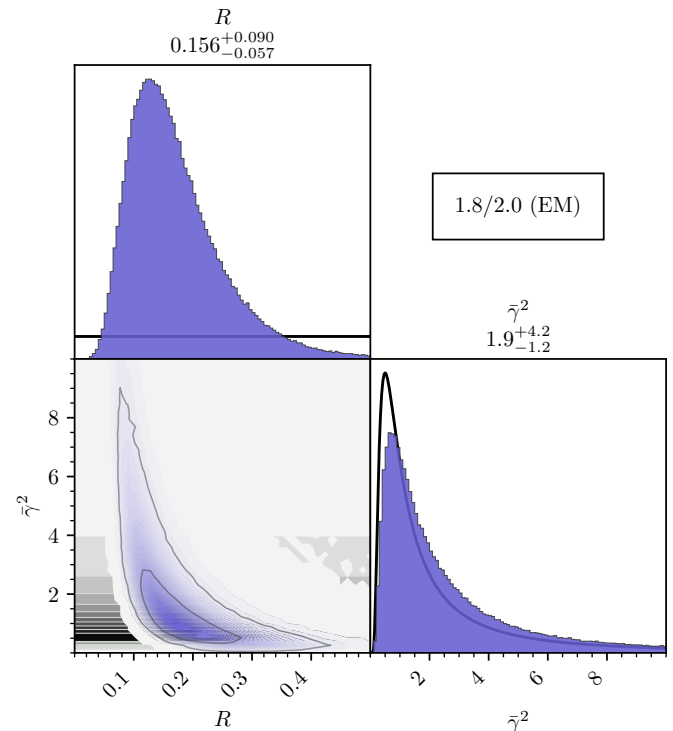
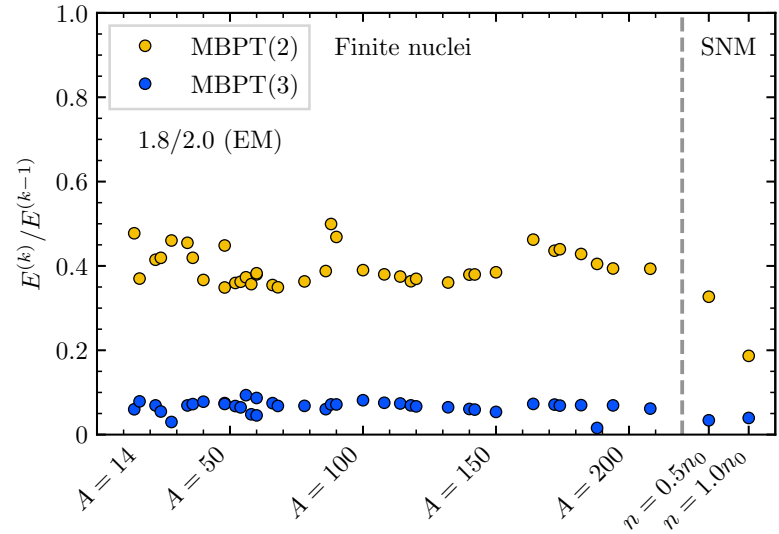
Many-body truncation uncertainties

Svensson, Tichai, Hebeler, AS, PRC (2025)

idea: use BUQEYE error model
for MBPT expansion

$$E_0 = \underbrace{E_{\text{ref}}\gamma_0}_{E_{\text{HF}}} + \underbrace{E_{\text{ref}}\gamma_1 R^1}_{\text{MBPT(2)}} + \underbrace{E_{\text{ref}}\gamma_2 R^2}_{\text{MBPT(3)}} + \dots$$

Bayesian inference of ratio R
and variance of γ_i from 3 nuclei



Many-body truncation uncertainties

Svensson, Tichai, Hebeler, AS, PRC (2025)

idea: use BUQEYE error model
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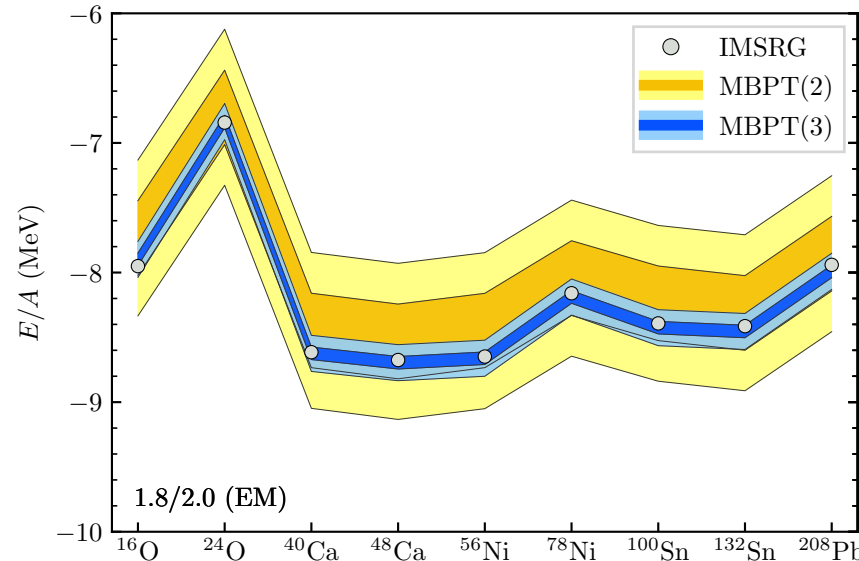
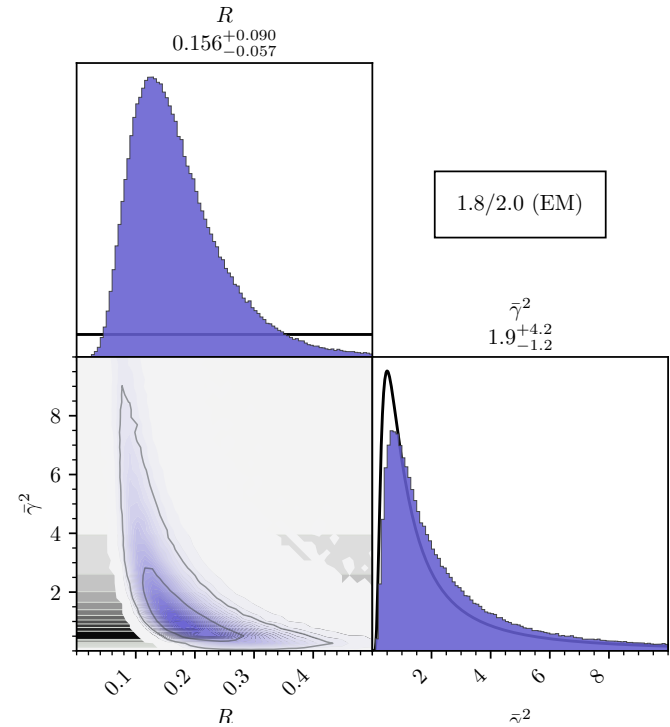
$$E_0 = \underbrace{E_{\text{ref}}\gamma_0}_{E_{\text{HF}}} + \underbrace{E_{\text{ref}}\gamma_1 R^1}_{\text{MBPT(2)}} + \underbrace{E_{\text{ref}}\gamma_2 R^2}_{\text{MBPT(3)}} + \dots$$

Bayesian inference of ratio R
and variance of γ_i from 3 nuclei

posterior distributions at different orders

good agreement with IMSRG(2)

enables many-body uncertainty
estimates beyond expert assessment



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Next generation NN+3N interactions: Wish list

- Low resolution enough for converged calculations up to ^{208}Pb
- Order-by-order interactions amenable to UQ, at least two orders with 3N
- Interactions for different cutoffs/schemes
- Good description of NN and $A=3,4$ systems
- Pion-full: leading two-body currents are parameter-free, 3-neutron interactions parameter-free up to $N^3\text{LO}$
- Reasonable saturation properties (informed by matter/nuclei), reasonable saturation density at HF level?