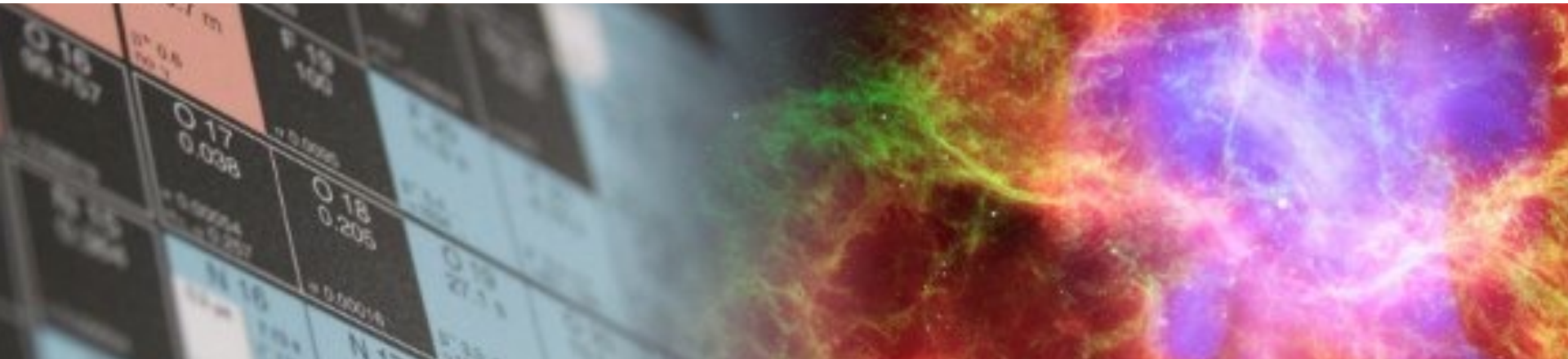


New equation of state developments for neutron star matter and for finite temperature

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TECHNISCHE
UNIVERSITÄT
DARMSTADT



INT Workshop “R-process and EOS after LIGO/Virgo”, May 24, 2022



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und Forschung

Outline

Chiral effective field theory for nuclear forces

Ab initio calculations of nuclear matter




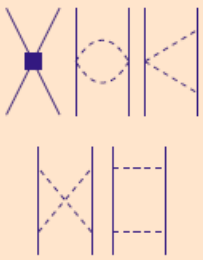


EOS constraints from chiral EFT and astrophysics

Constraints from heavy-ion collisions

EOS for arbitrary proton fraction and finite T

Chiral effective field theory for nuclear forces

Systematic expansion (power counting) in low momenta $(Q/\Lambda_b)^n$

		NN	3N	4N	
LO	$\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$				based on symmetries of strong interaction (QCD)
NLO	$\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$				long-range interactions governed by pion exchanges



Weinberg (1990,91)

Chiral effective field theory for nuclear forces

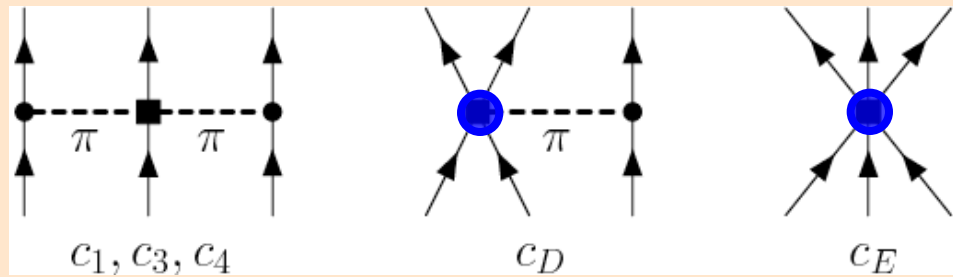
Systematic expansion (power counting) in low momenta $(Q/\Lambda_b)^n$

	NN	3N	4N
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N ² LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N ³ LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

derived in (1994/2002)

+ ... (2011) ... (2006) ...

powerful approach for many-body interactions



only 2 new couplings at N²LO
all 3- and 4-neutron forces predicted to N³LO

Chiral effective field theory for nuclear forces

Systematic expansion (power counting) in low momenta $(Q/\Lambda_b)^n$

IOP Publishing

Journal of Physics G: Nuclear and Particle Physics

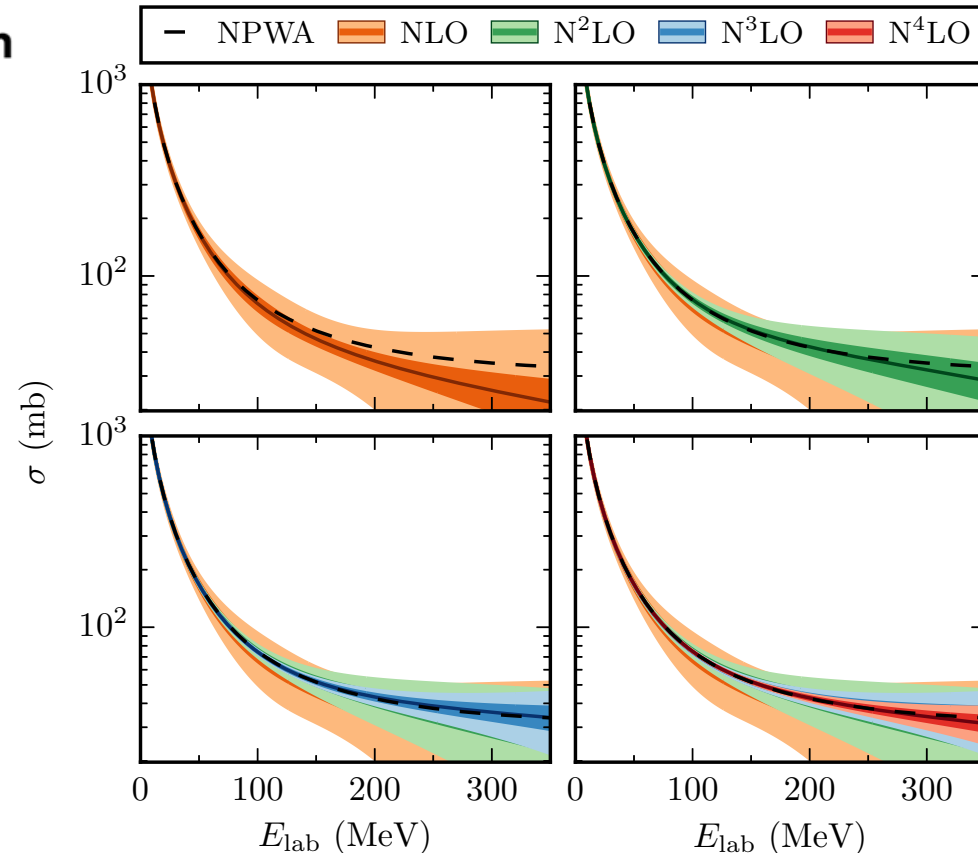
J. Phys. G: Nucl. Part. Phys. 42 (2015) 034028 (20pp)

doi:10.1088/0954-3899/42/3/034028

A recipe for EFT uncertainty quantification in nuclear physics

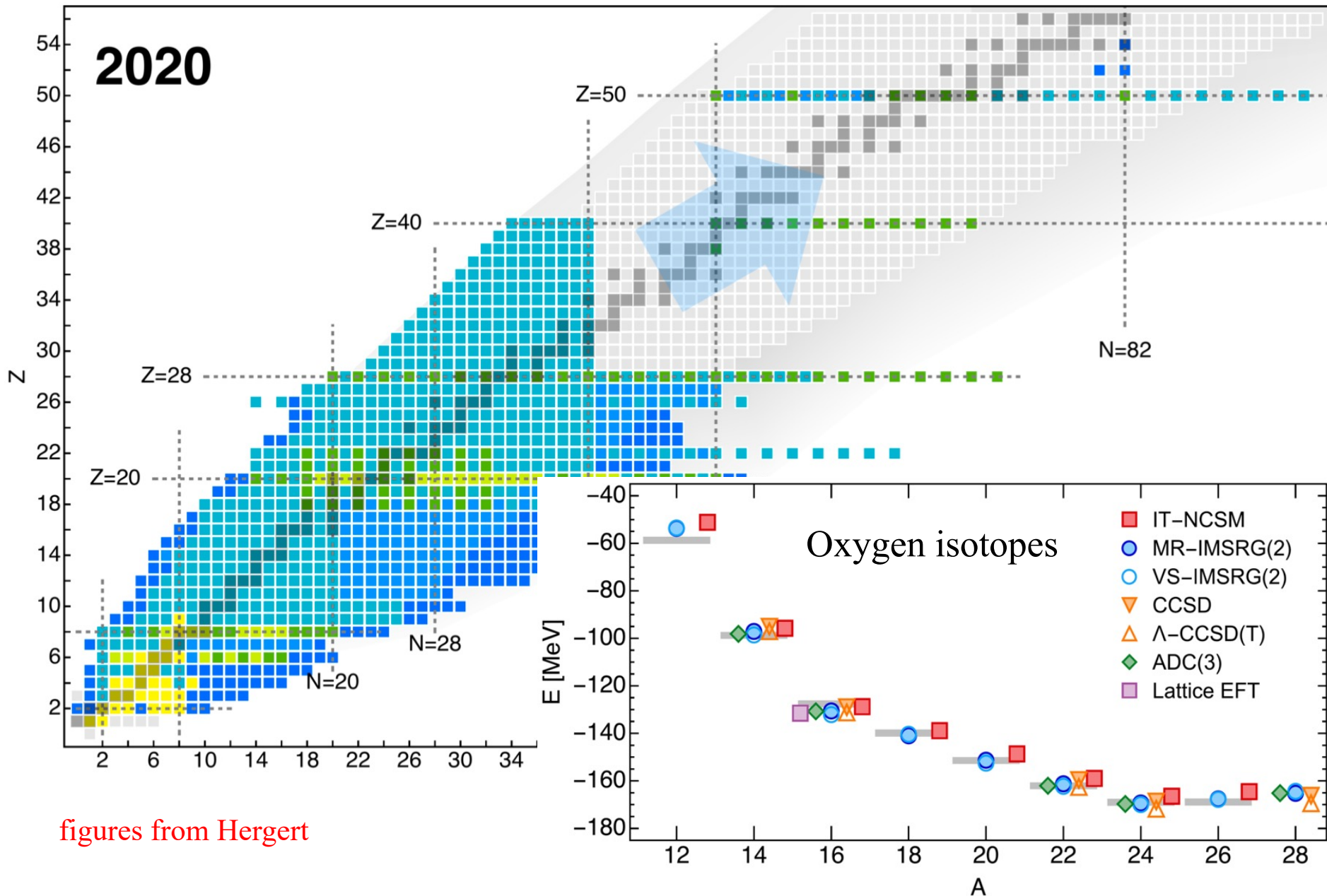
R J Furnstahl¹, D R Phillips² and S Wesolowski¹

Bayesian uncertainty estimates and model checking



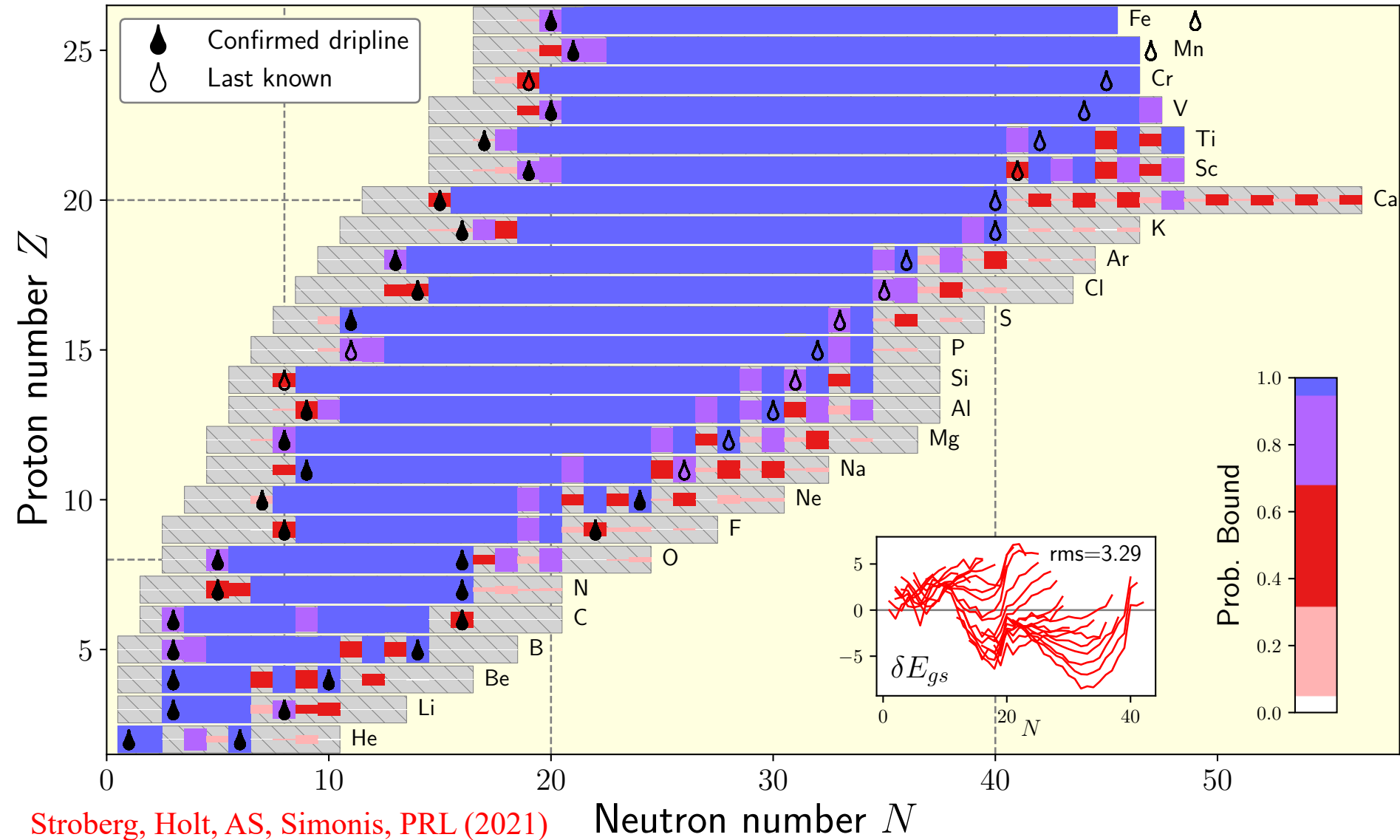
Furnstahl, Phillips, Klos, Wesolowski, Melendez (2015-)

Great progress in ab initio calculations of nuclei



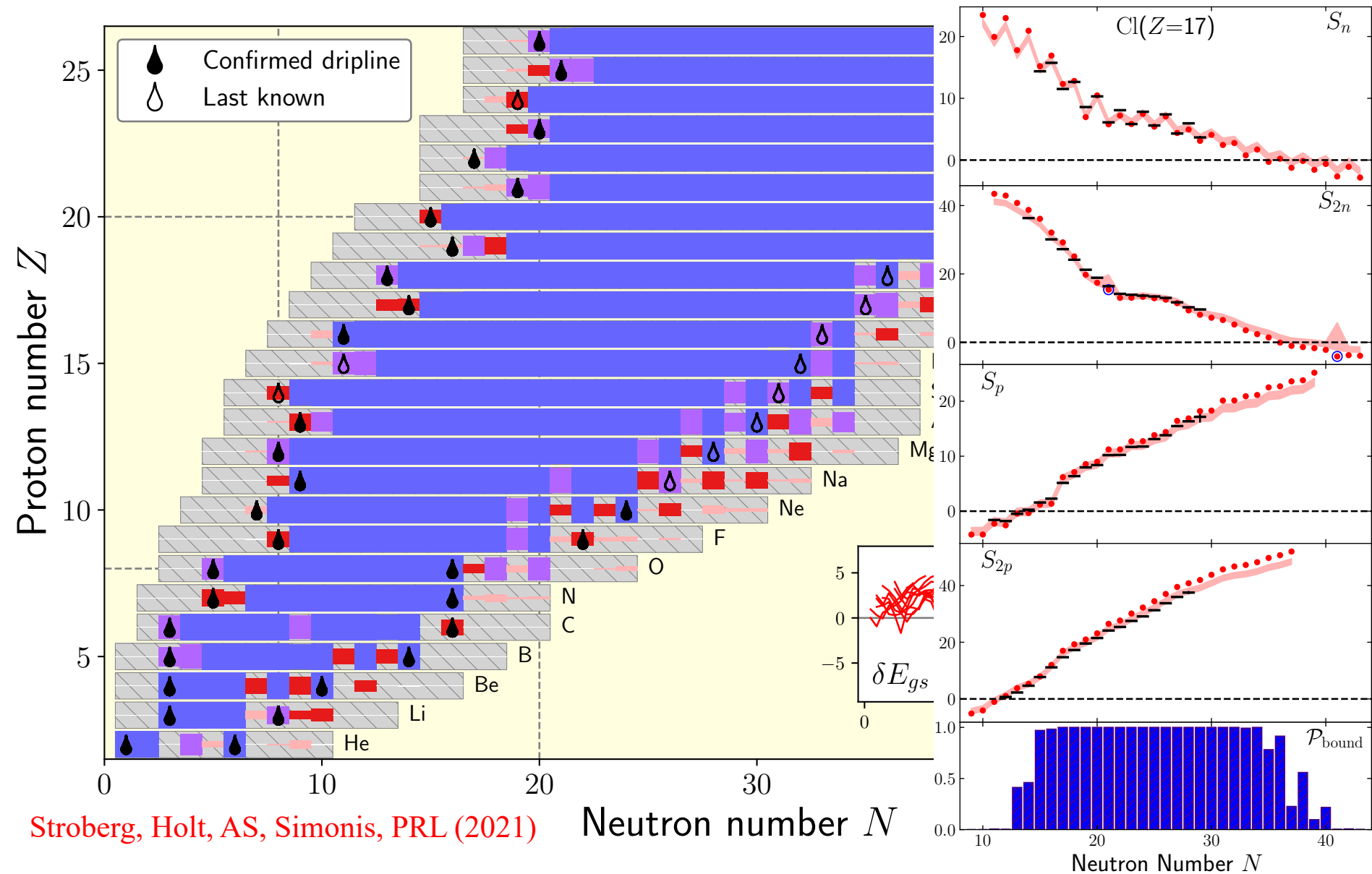
figures from Hergert

Nuclear landscape based on a chiral NN+3N interaction



ab initio is advancing to global theories, limitations due to input NN+3N

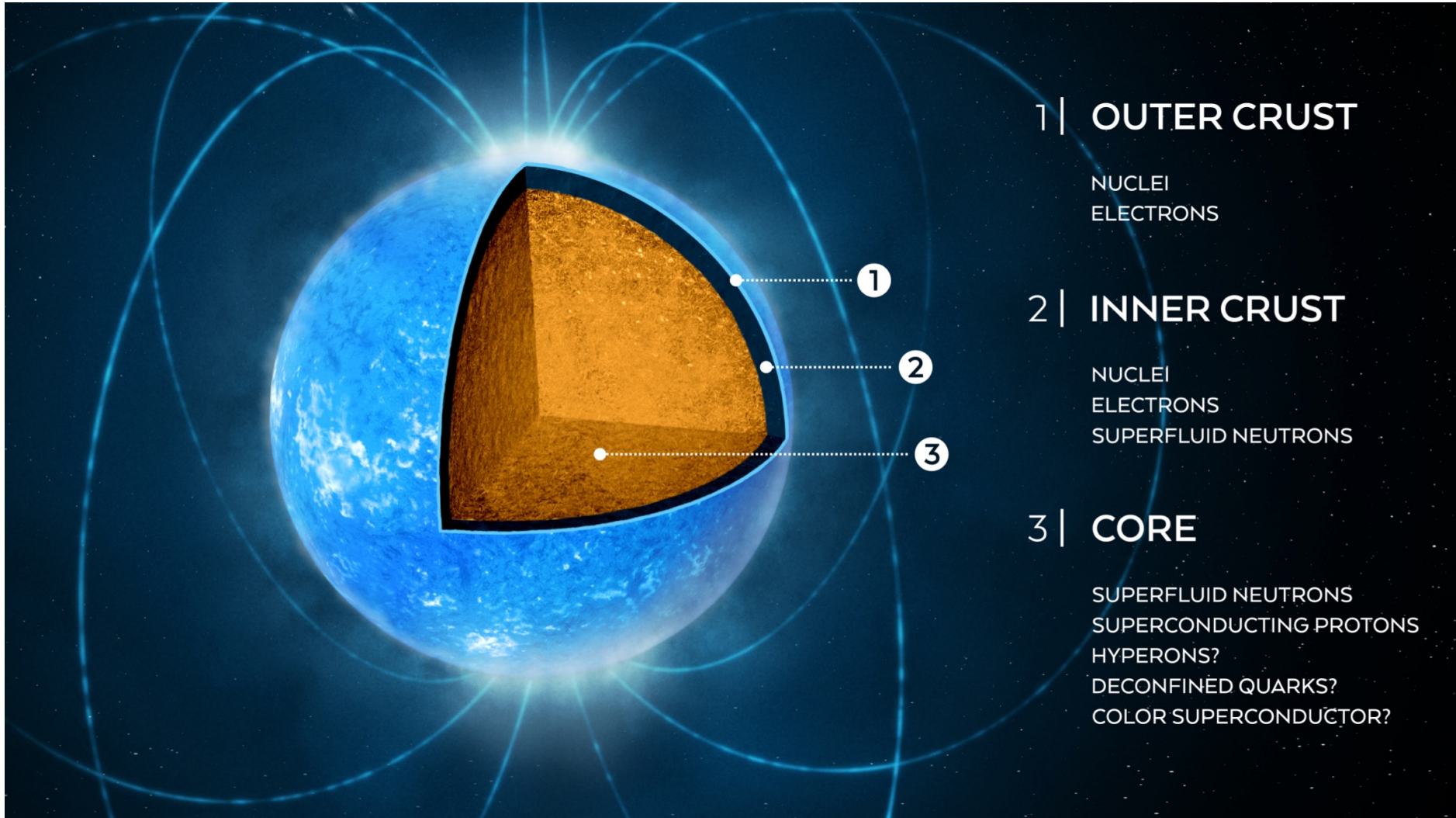
Nuclear landscape based on a chiral NN+3N interaction



ab initio is advancing to global theories, limitations due to input NN+3N

Extreme matter in neutron stars

governed by the same strong interactions



N³LO calculation of neutron matter and symmetric matter

Monte-Carlo evaluation
of energy diagrams
up to 4th order in MBPT

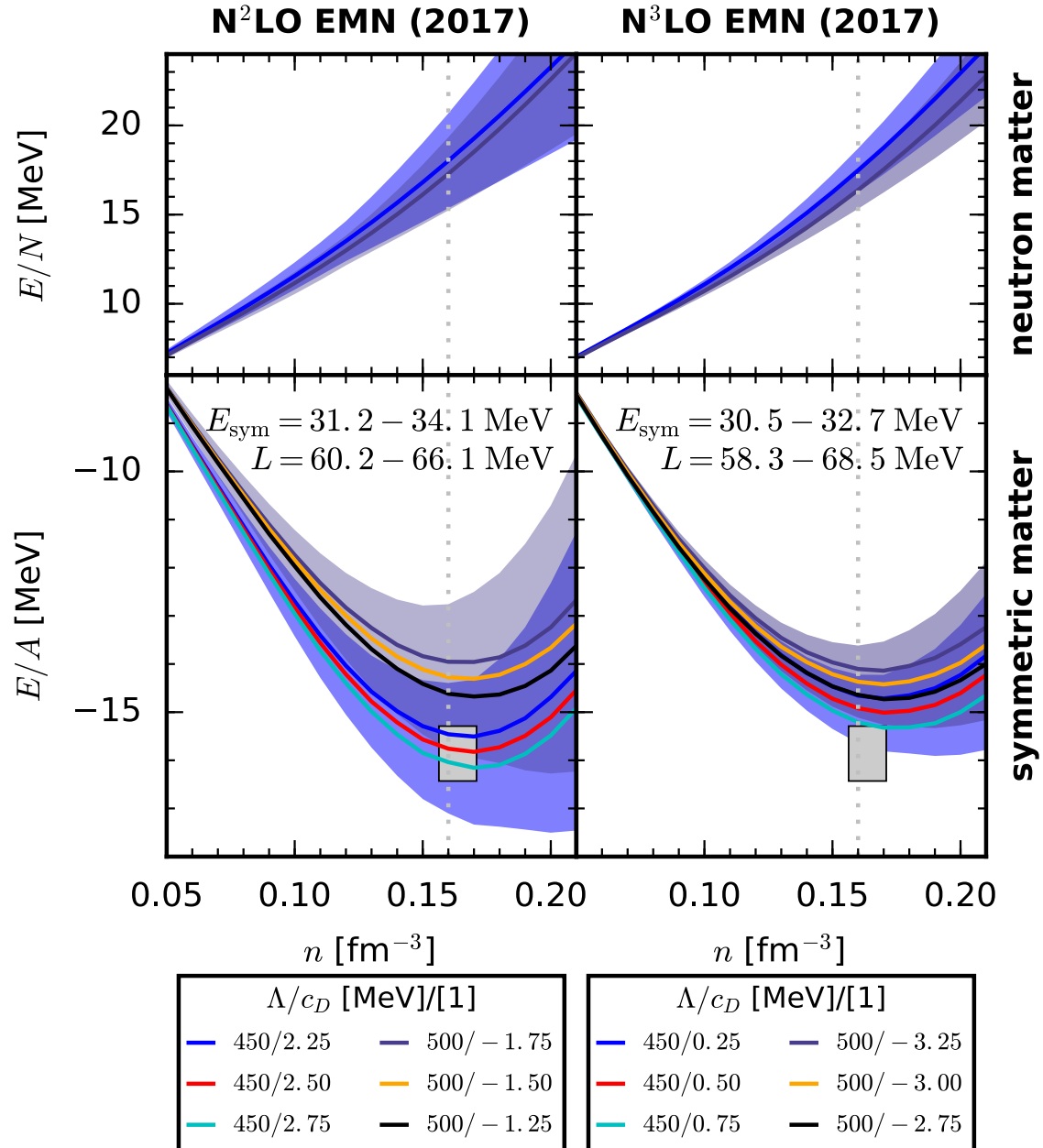
Drischler, Hebeler, AS, PRL (2019)

including NN, 3N, 4N
3N fit to saturation region

all many-body forces
to N³LO predicted for
neutron matter

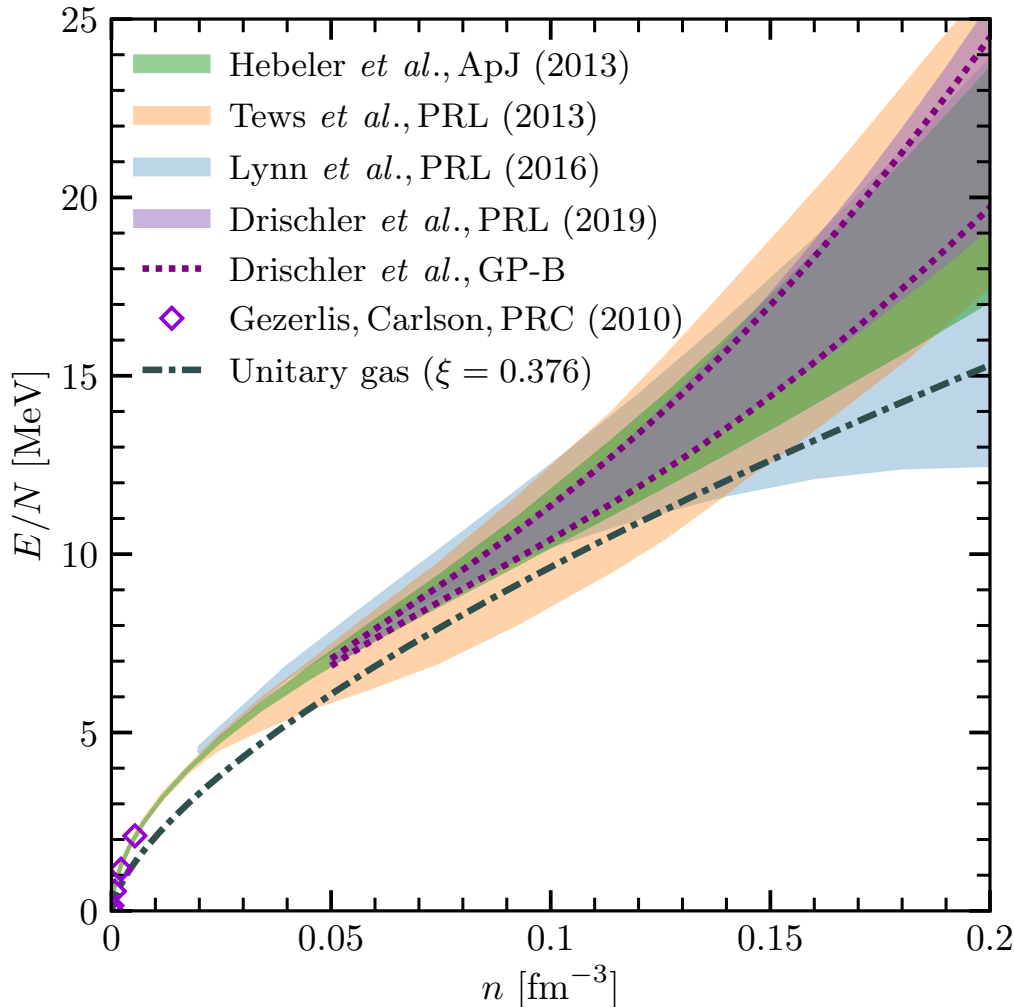
Tews, Krüger, Hebeler, AS, PRL (2013)

systematic improvement
from N²LO to N³LO



Chiral EFT calculations of neutron matter

good agreement up to saturation density for neutron matter
nonlocal/local int. and different calcs. (MBPT, QMC, SCGF, CC)



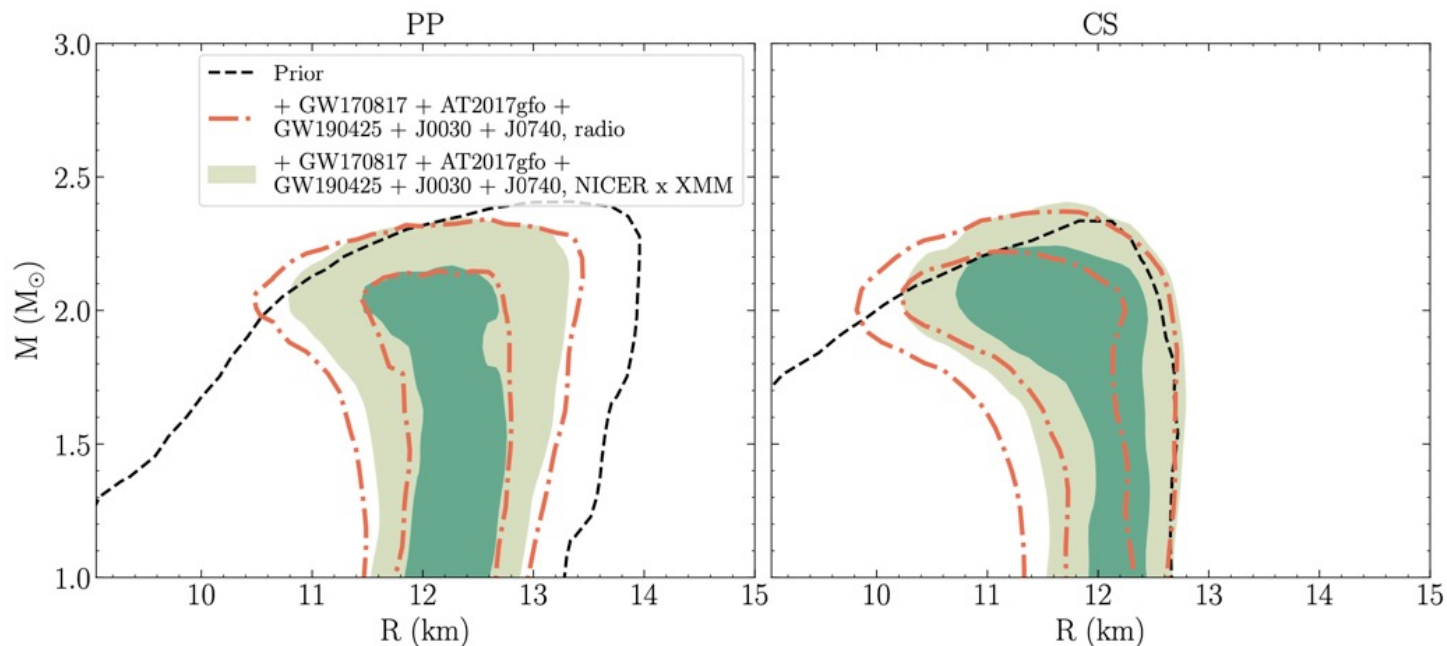
slope determines
pressure of
neutron matter

GP-B (68%) gives
similar band as simple
EFT uncertainties

from Huth, Wellenhofer, AS, PRC (2021)

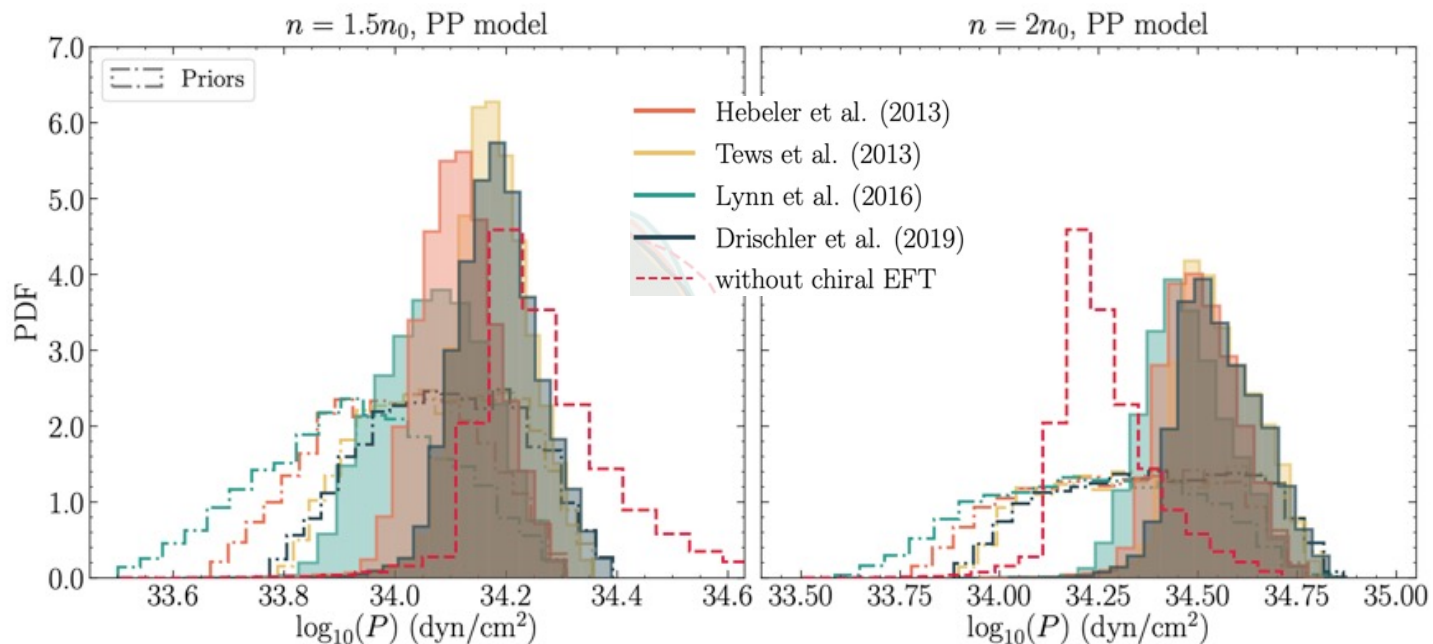
Combined merger and NICER constraints

Raaijmakers et al.,
ApJL (2020), (2021)
for mass-radius



equation of state
at 1.5 and $2 n_0$

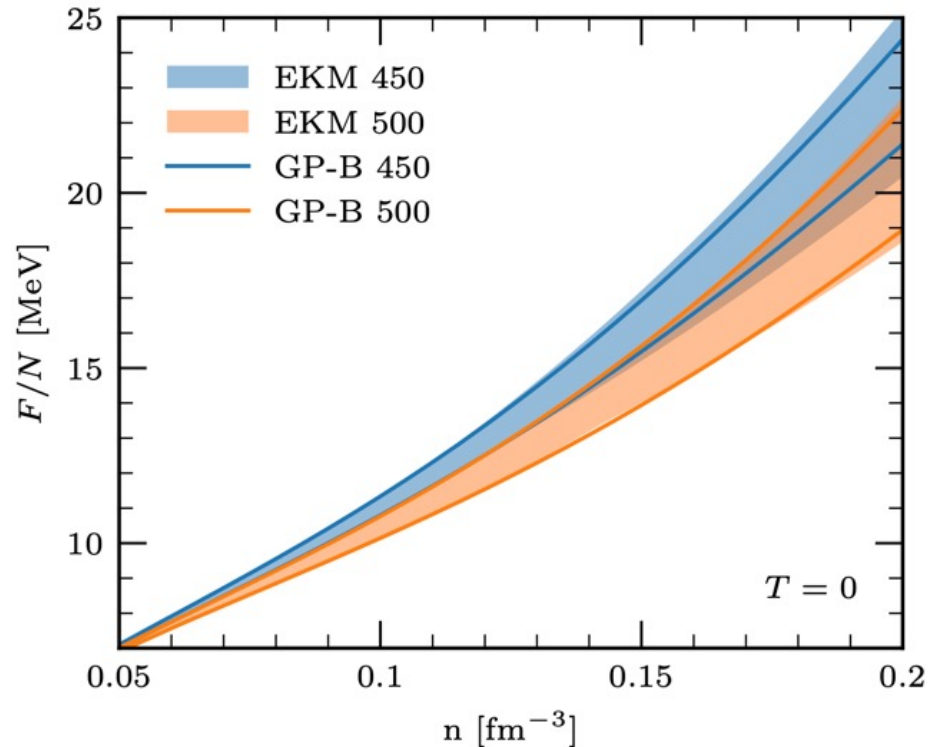
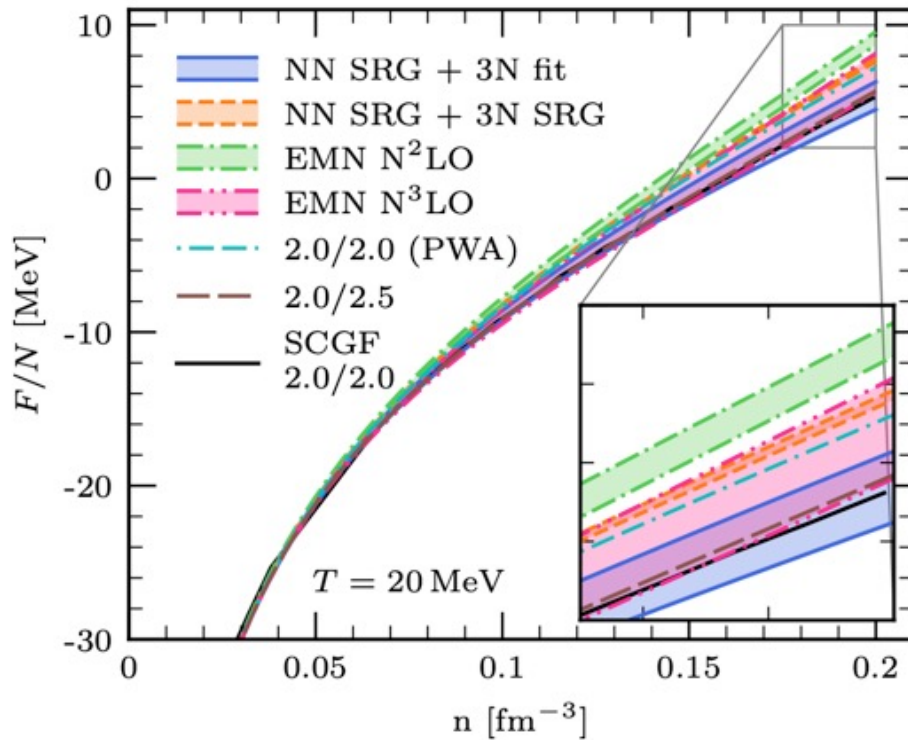
astro prefers
higher pressures



Neutron matter at finite temperature

similar thermal effects for different NN+3N interactions

Keller, Wellenhofer, Hebeler, AS, PRC (2021)



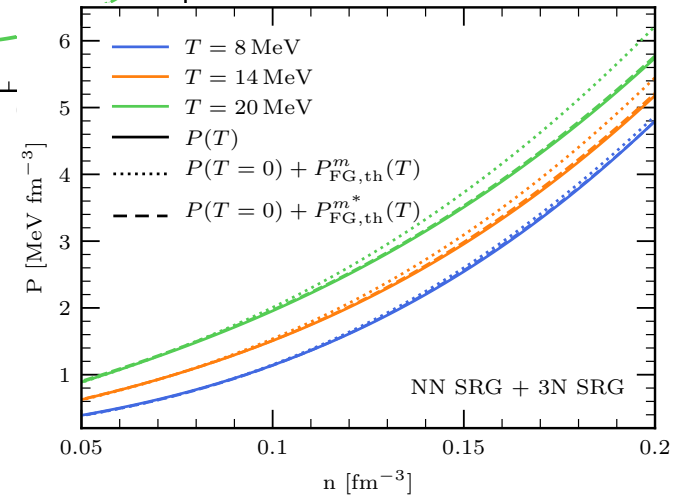
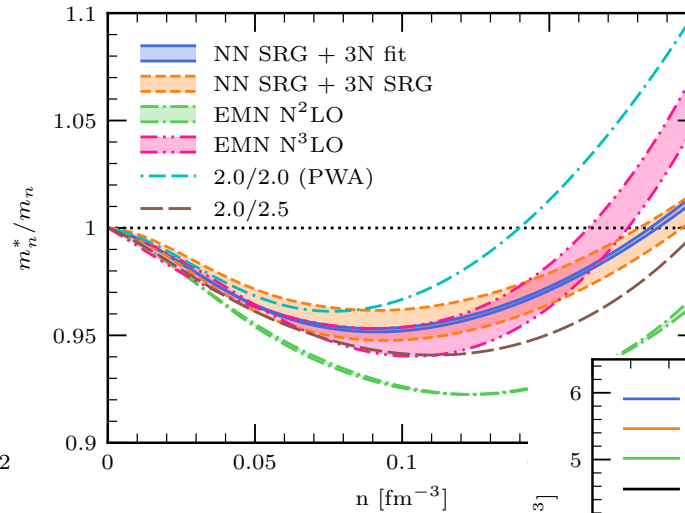
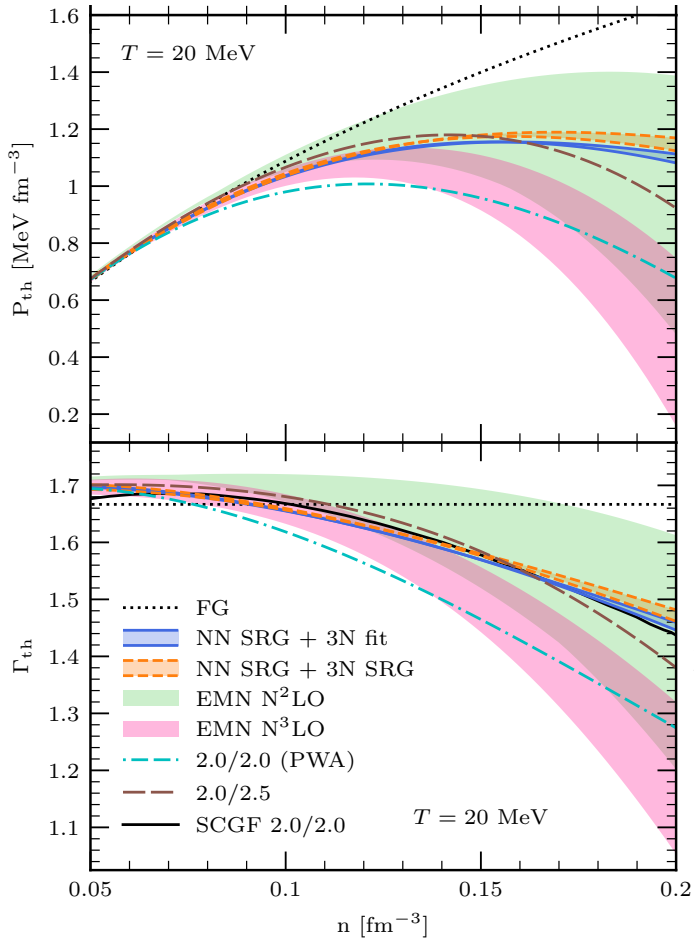
EFT uncertainties (EKM) similar to GP-B (68%) Drischler et al. (2020)

Thermal effects governed by effective mass

decreasing thermal pressure due to repulsive 3N contributions

increasing effective mass m^* beyond n_{sat}

$$\Gamma_{\text{th}}^*(n) = \frac{5}{3} - \frac{n}{m_n^*} \frac{\partial m_n^*}{\partial n}$$

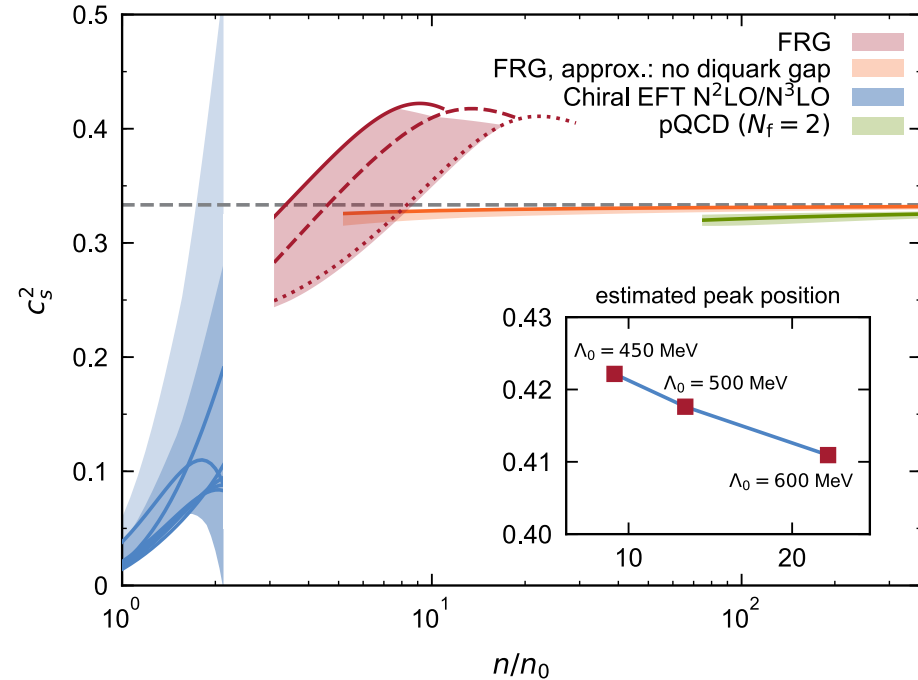
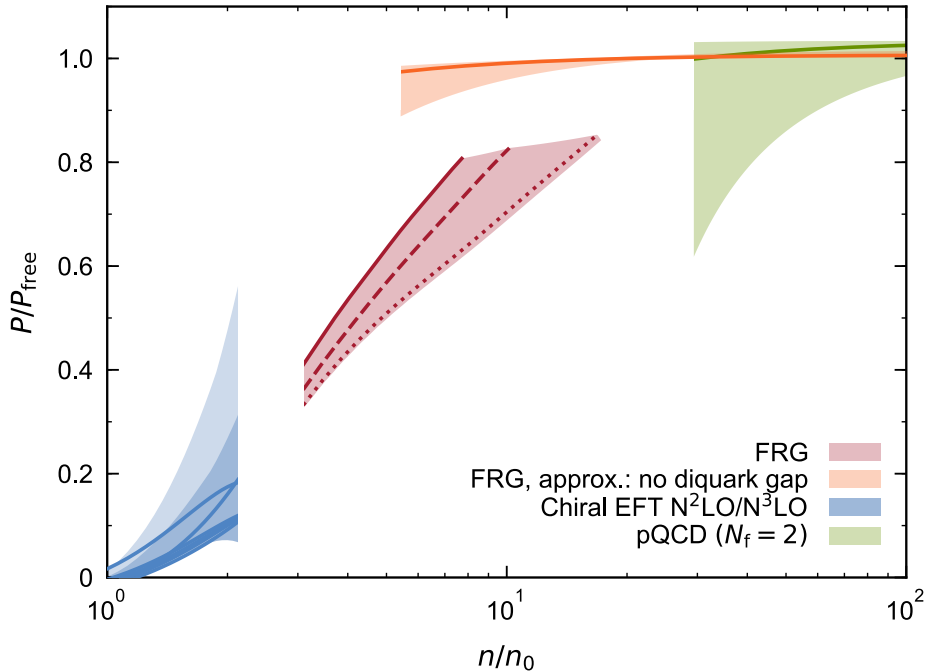


Functional RG: From QCD to intermediate densities

based on QCD at high densities

symmetric matter ($m_u = m_d$, no s quark, no electroweak interactions)

Leonhardt, Pospiech, Schallmo, Braun et al., PRL (2020)



promising consistency between chiral EFT and FRG and pQCD

diquark correlations crucial for intermediate densities and high speed of sound

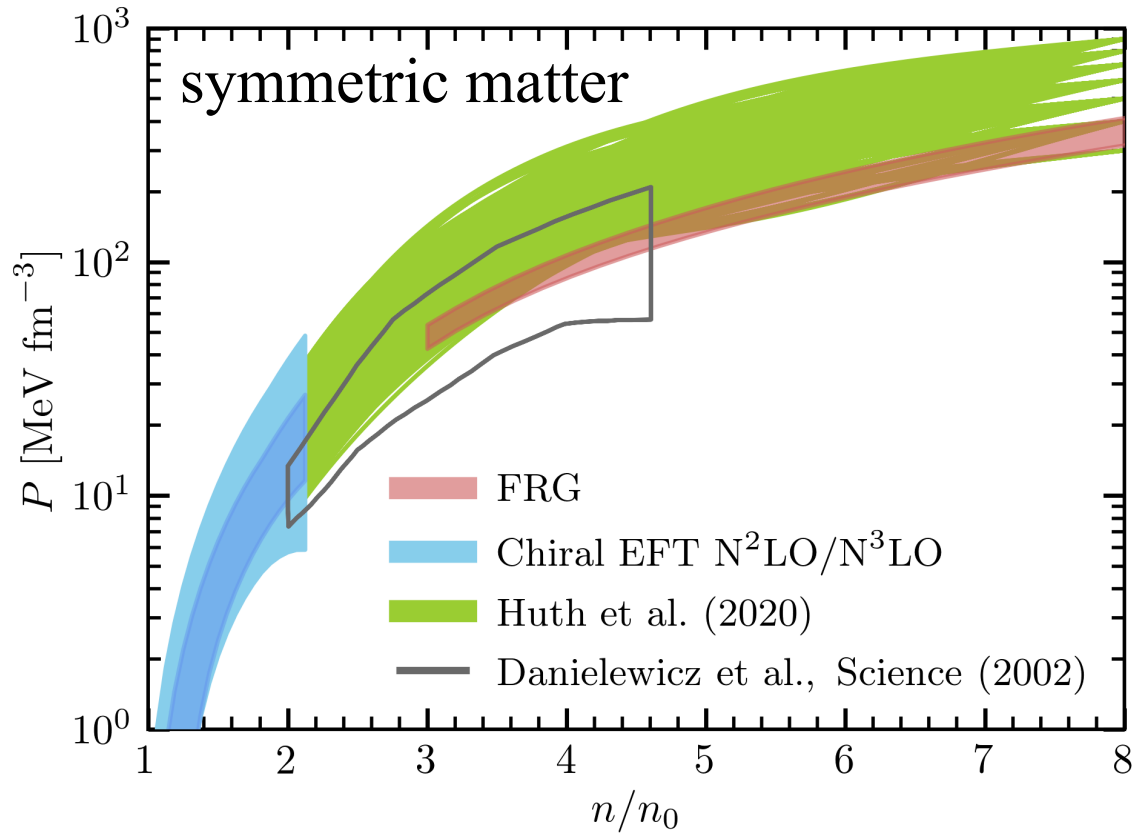
Symmetric matter: From chiral EFT to functional RG

comparison to **new EOS functionals** with $2 M_{\text{sun}} + \text{LIGO/Virgo, NICER}$

Huth, Wellenhofer, AS, PRC (2021)

comparison to
heavy-ion constraint

Danielewicz et al., Science (2002)



Symmetric matter: From chiral EFT to functional RG

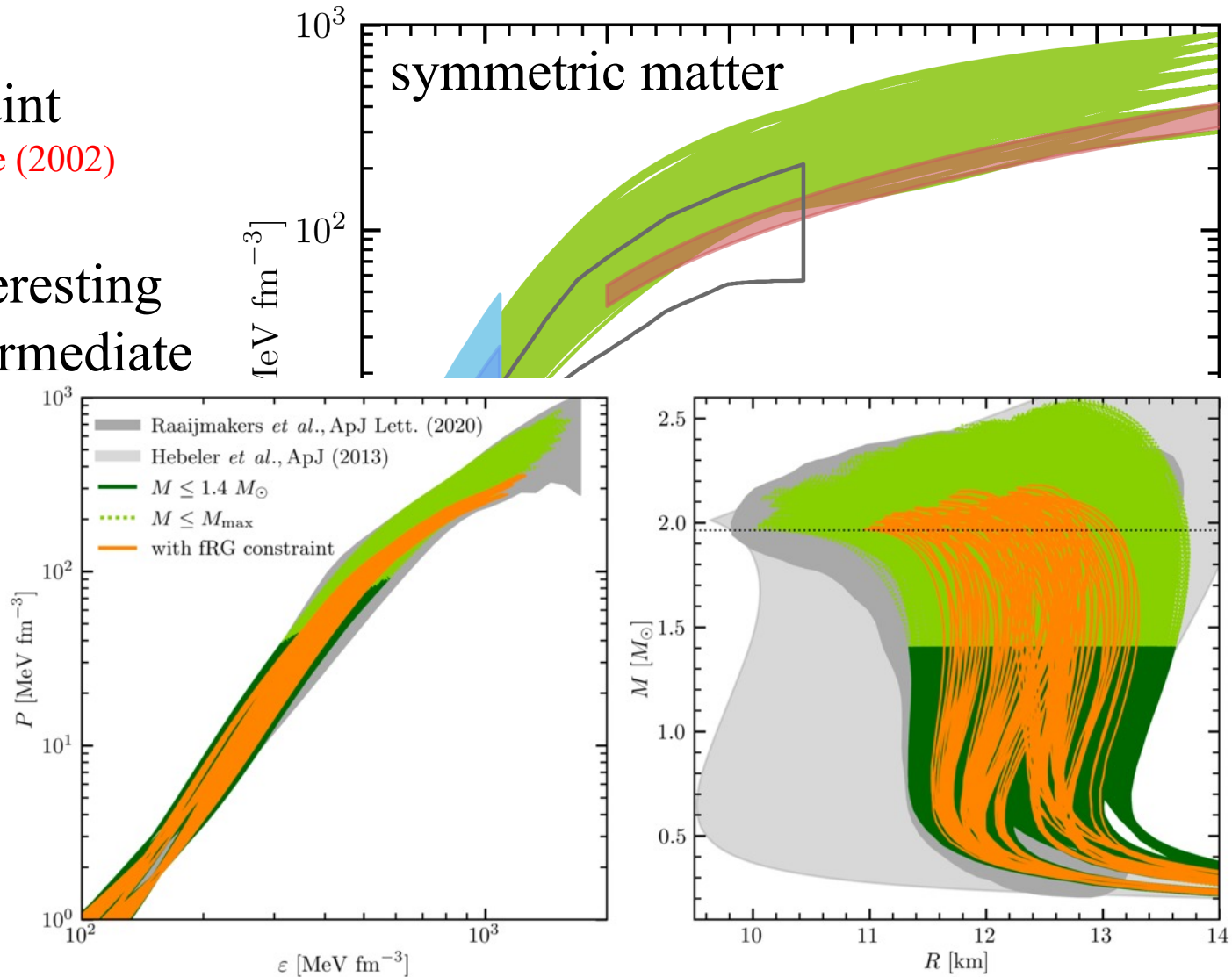
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Huth, Wellenhofer, AS, PRC (2021)

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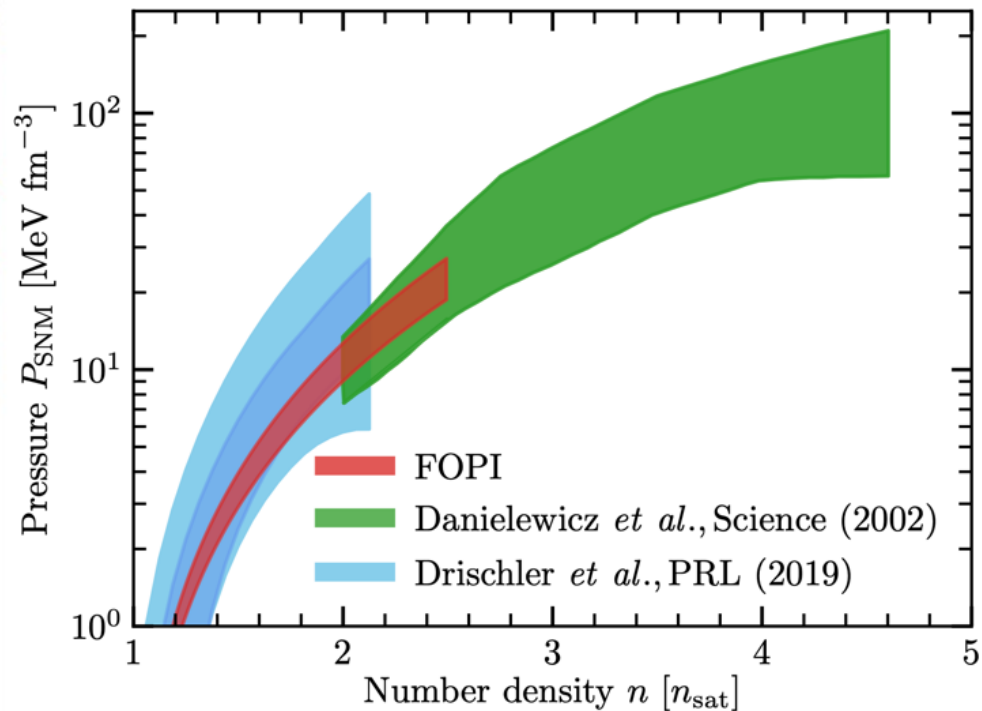
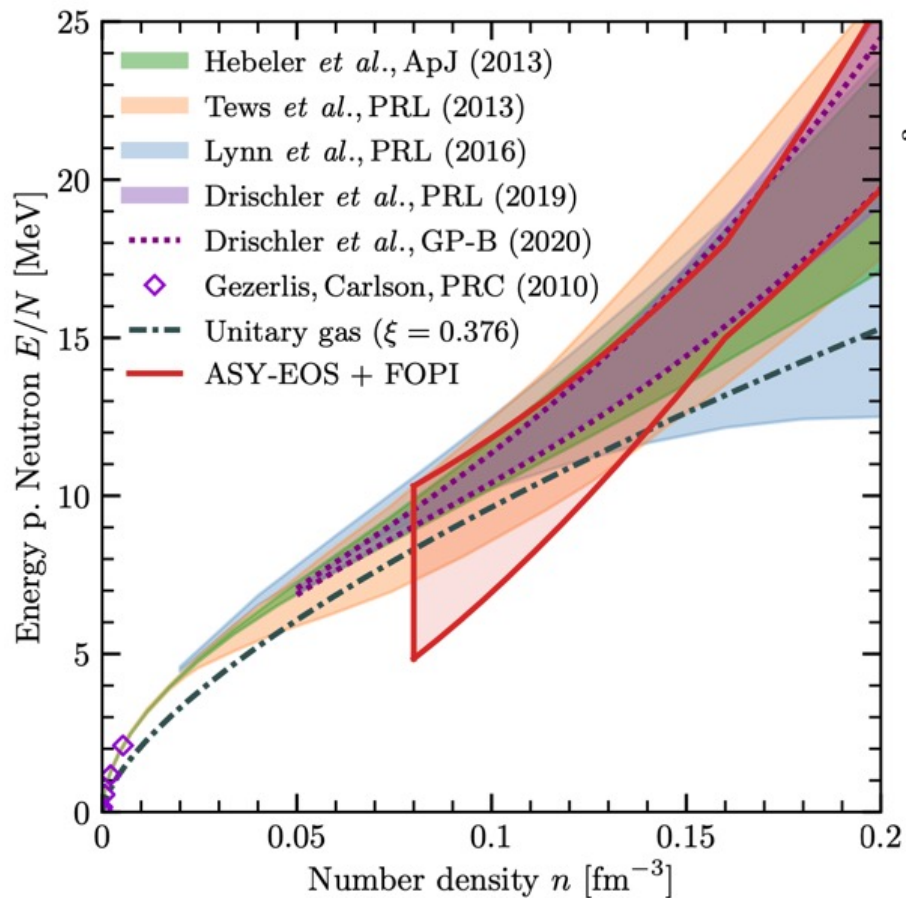
Danielewicz et al., Science (2002)

fRG provides interesting
constraints at intermediate
densities



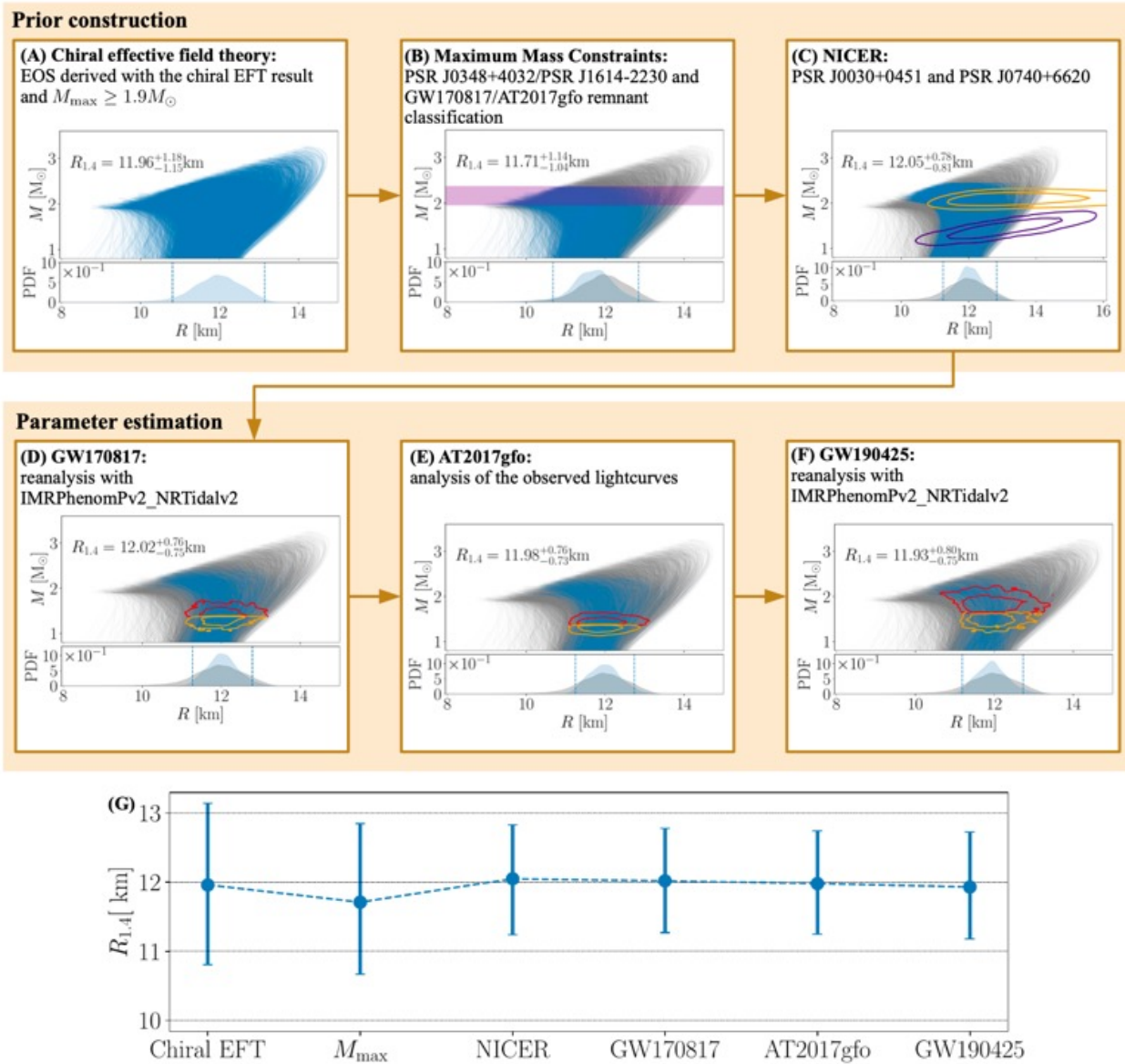
Constraints from heavy-ion collisions Huth, Pang et al., arXiv:2107.06229

include in addition to chiral EFT: constraints from ASY-EOS and FOPI for neutron and symmetric matter with different functionals



Constraints from heavy-ion collisions Huth, Pang et al., arXiv:2107.06229

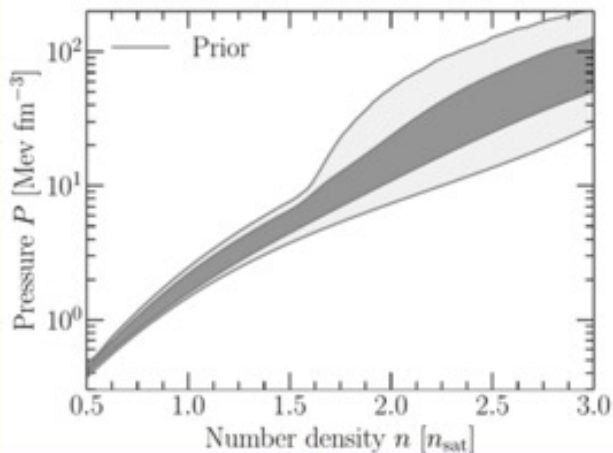
Bayesian multi-messenger framework using EOS draws based on chiral EFT (QMC results) with c_s extension



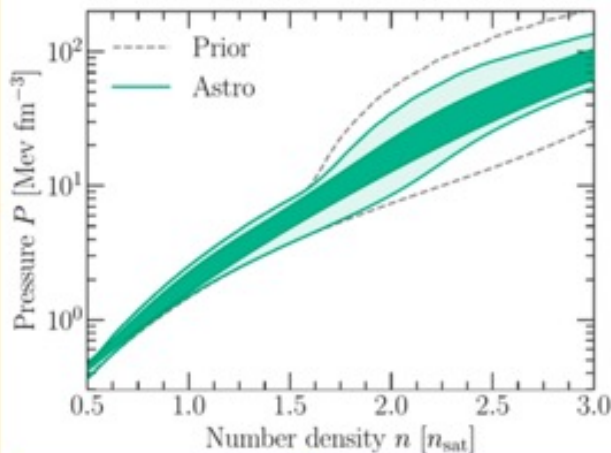
Constraints from heavy-ion collisions Huth, Pang et al., arXiv:2107.06229

inclusion of HIC constraints prefers higher pressures, similar to NICER, overall remarkable consistency with chiral EFT and astro constraints

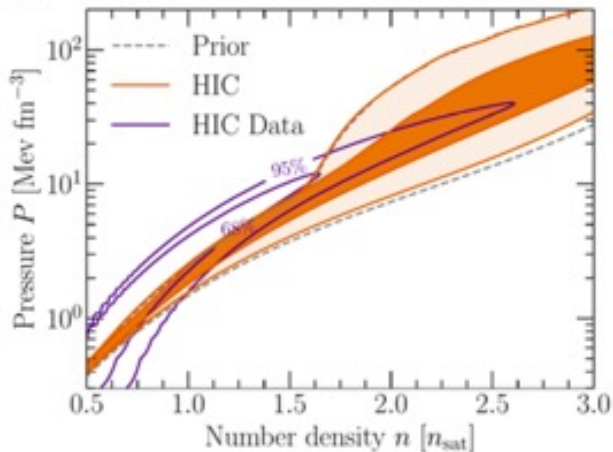
(A) Chiral effective field theory:



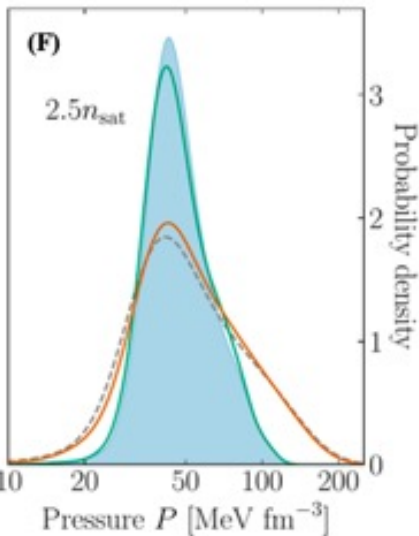
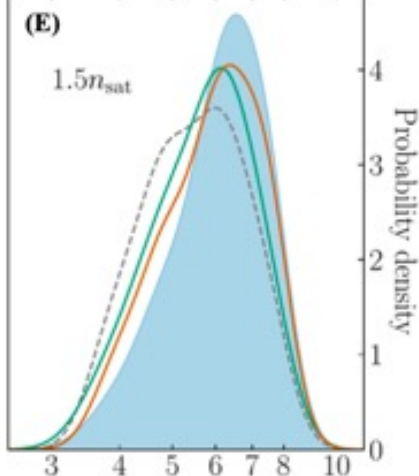
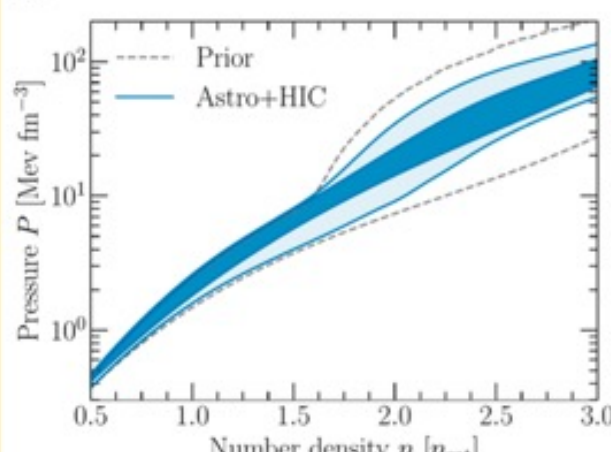
(B) Multi-messenger astrophysics:



(C) HIC experiments:

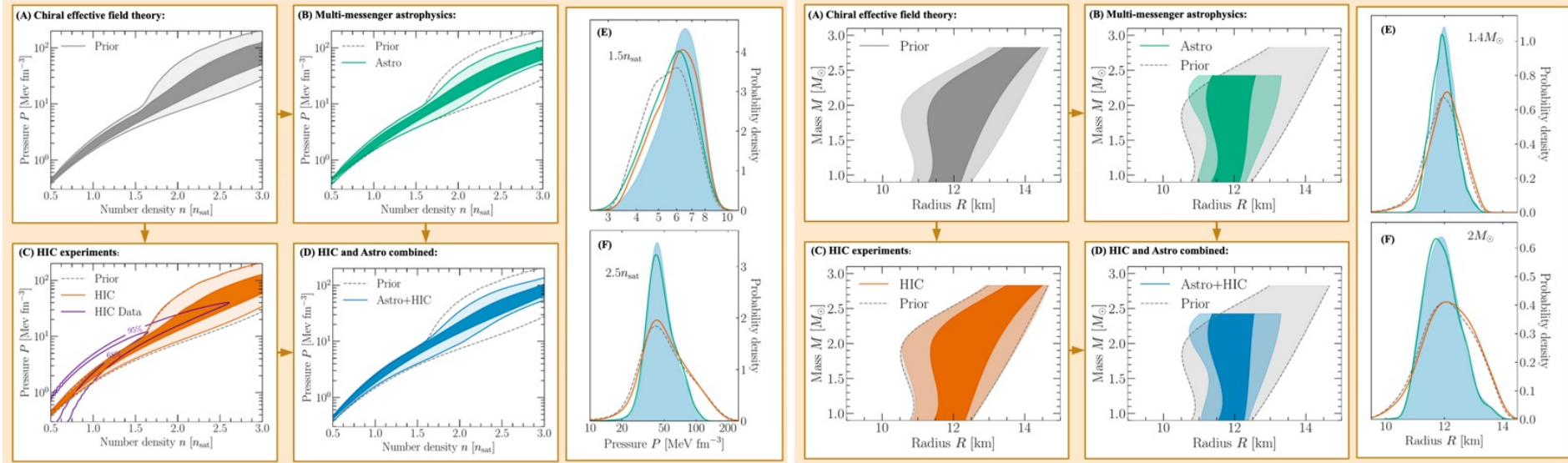


(D) HIC and Astro combined:



Constraints from heavy-ion collisions Huth, Pang et al., arXiv:2107.06229

inclusion of HIC constraints prefers higher pressures, similar to NICER, overall remarkable consistency with chiral EFT and astro constraints



	Prior	Astro only	HIC only	Astro + HIC
$P_{1.5n_{\text{sat}}}$	$5.59^{+2.04}_{-1.97}$	$5.84^{+1.95}_{-2.26}$	$6.06^{+1.85}_{-2.04}$	$6.25^{+1.90}_{-2.26}$
$R_{1.4}$	$11.96^{+1.18}_{-1.15}$	$11.93^{+0.80}_{-0.75}$	$12.06^{+1.13}_{-1.18}$	$12.01^{+0.78}_{-0.77}$

more HIC information for intermediate densities very interesting

EOS for arbitrary proton fraction and temperature

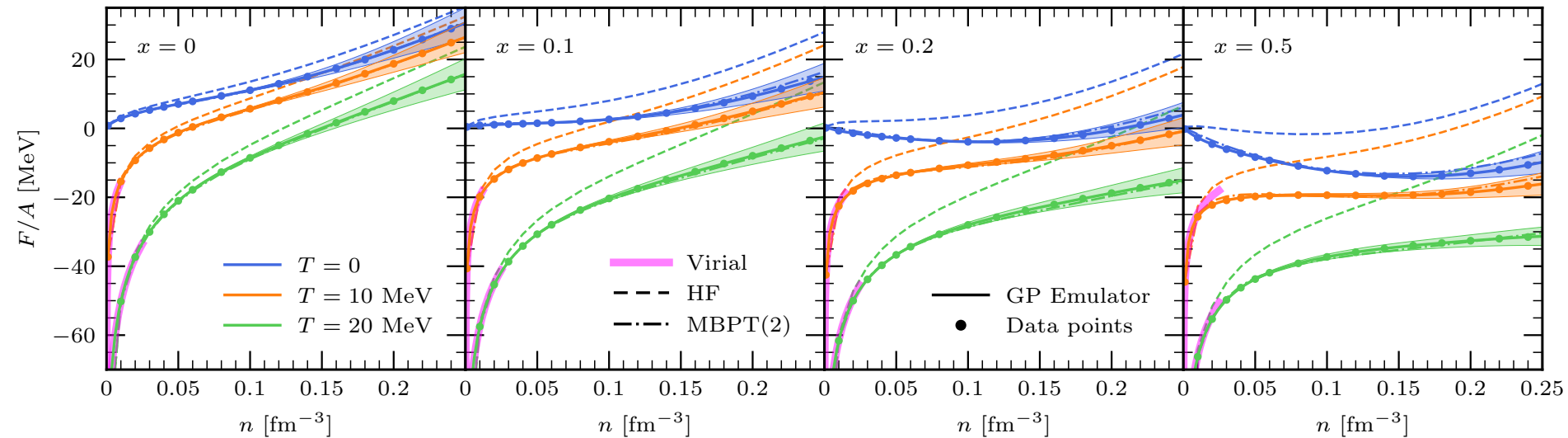
Keller, Hebeler, AS, arXiv:2204.14016

based on chiral EFT NN+3N interactions (EMN 450) to N³LO

order-by-order EFT uncertainties $\Delta X^{(j)} = Q \cdot \max(|X^{(j)} - X^{(j-1)}|, \Delta X^{(j-1)})$
(small) many-body uncertainties at MBPT(3)

excellent reproduction of free energy data by Gaussian process

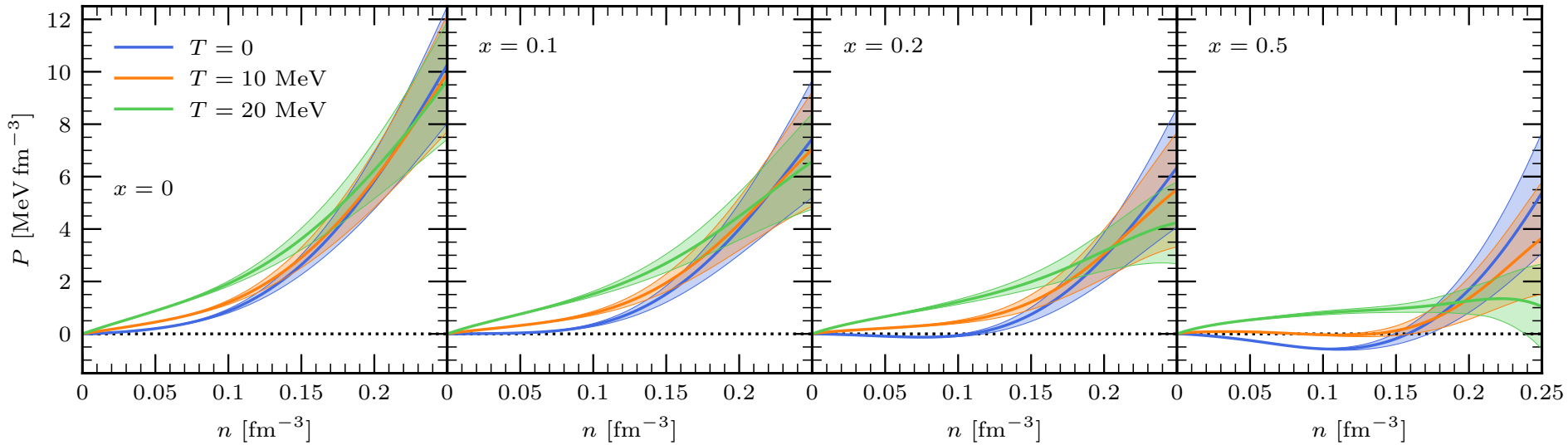
agreement with model-independent virial EOS at low densities



EOS for arbitrary proton fraction and temperature

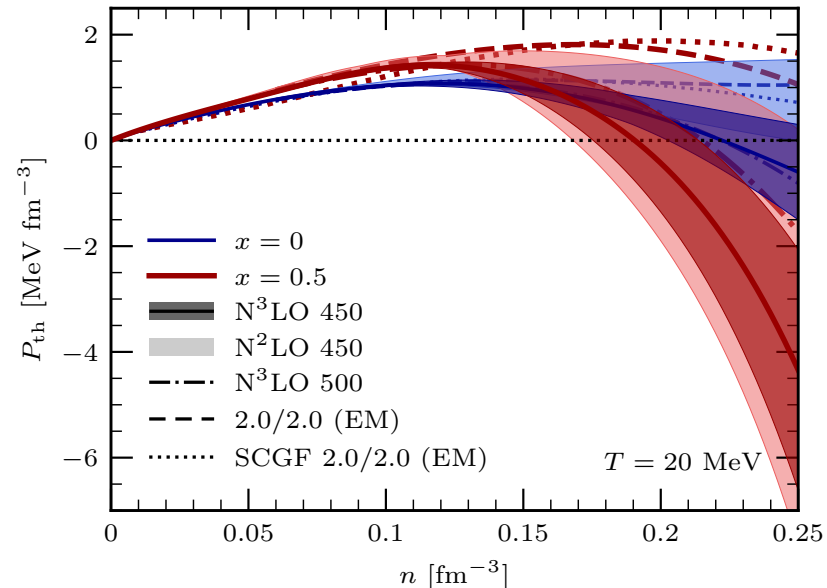
Keller, Hebeler, AS, arXiv:2204.14016

GP emulator to calculate pressure (thermodyn. consistent derivatives)



pressure isothermals cross at higher densities \rightarrow negative thermal expansion

thermal part of pressure decreases with increasing density, observed for different chiral orders, cutoffs and interactions



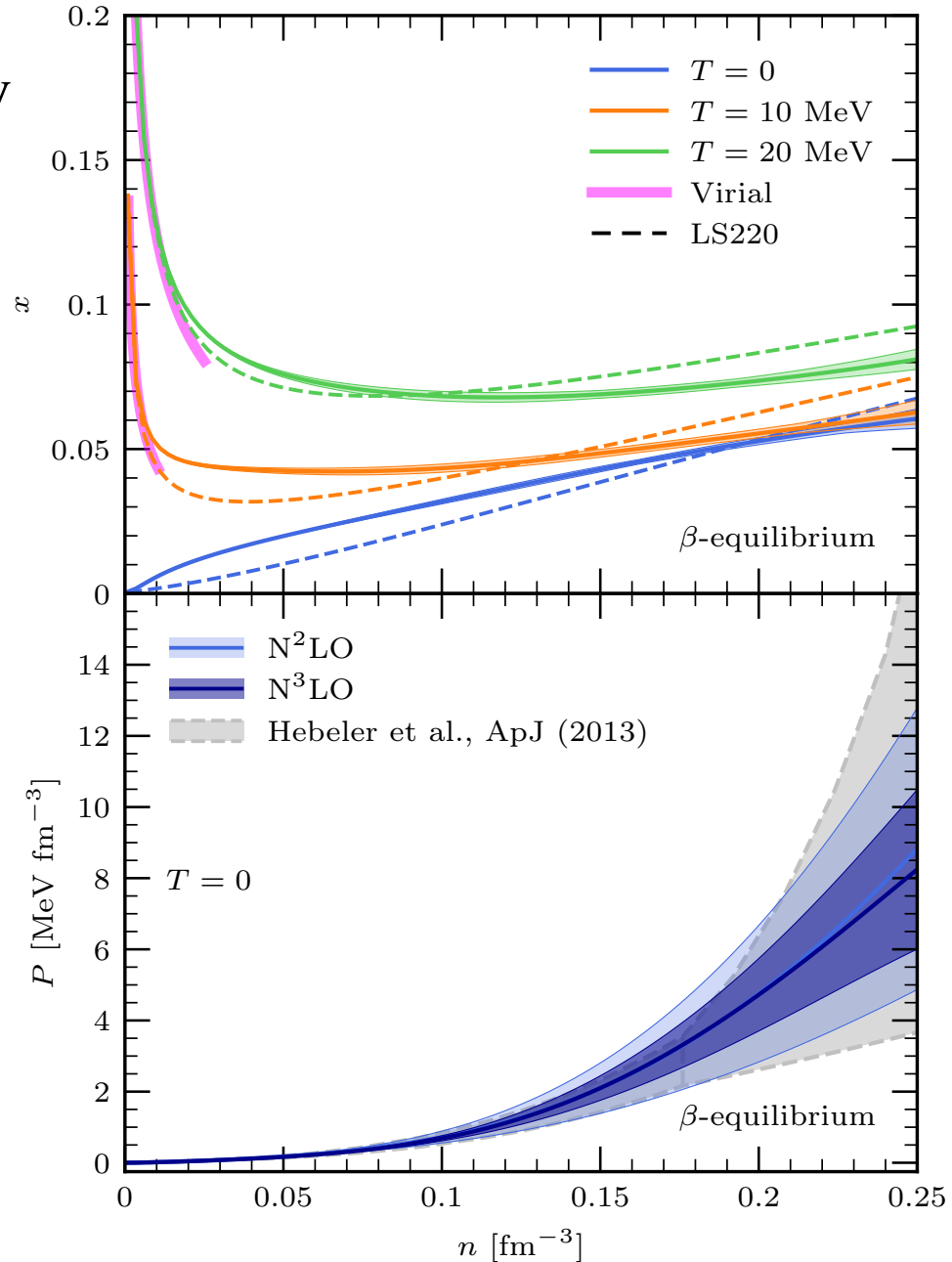
EOS for neutron star matter in beta equilibrium

Keller, Hebeler, AS, arXiv:2204.14016

use GP emulator to access arbitrary
proton fraction,
solve for beta equilibrium

EOS of neutron star matter
at $N^2\text{LO}$ and $N^3\text{LO}$,
no indication of EFT breakdown

$N^3\text{LO}$ band prefers higher
pressures, improvement over
older calculations



Applications to speed of sound and symmetry free energy

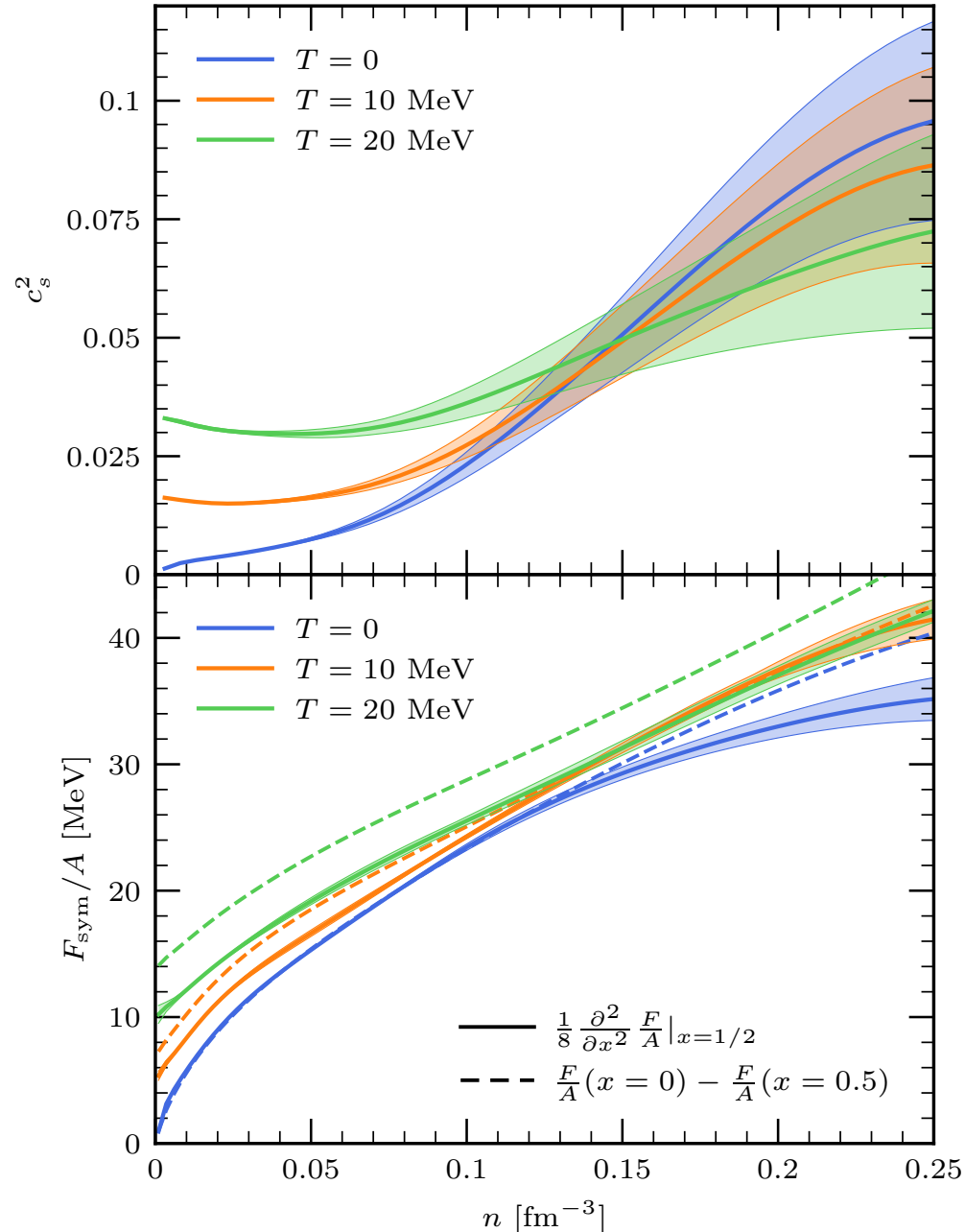
Keller, Hebeler, AS, arXiv:2204.14016

speed of sound for neutron matter
at constant entropy

high-density behavior with
increasing T similar to pressure

symmetry energy tightly
constrained at fixed density

difference in definition mainly
due to kinetic energy (m^*)



Summary

Thanks to: J. Braun, T. Dietrich, C. Drischler, S. Greif, K. Hebeler, **S. Huth**, J. Lattimer, A. Le Fèvre, **J. Keller**, **P. Pang**, C. Pethick, **G. Raaijmakers**, I. Tews, W. Trautmann, A. Watts, C. Wellenhofer

Chiral effective field theory for nuclear forces

Ab initio calculations of nuclear matter

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