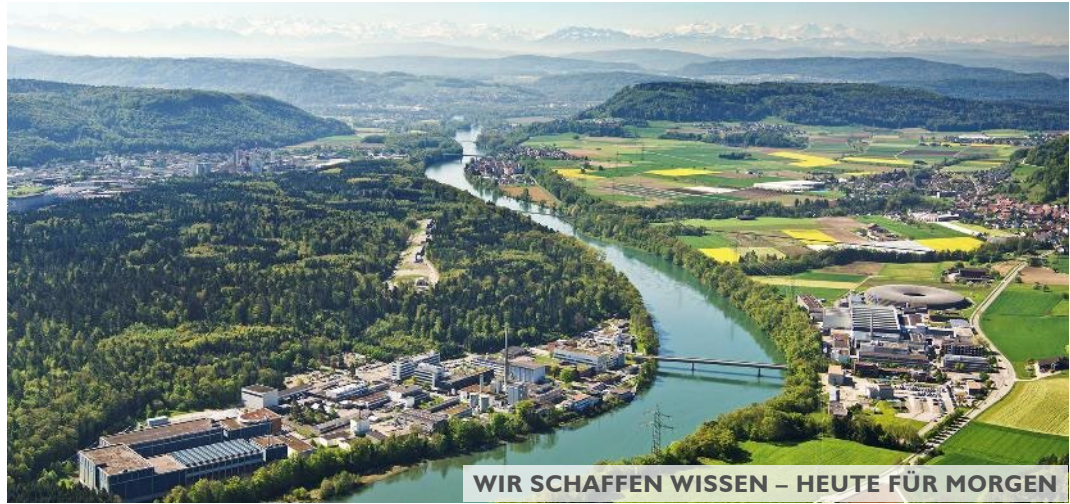


PAUL SCHERRER INSTITUT



Philipp Schmidt-Wellenburg :: Scientist :: Paul Scherrer Institute

## Search for a muon EDM

New physics searches at the precision frontier, Seattle, 05/10/23



Project funded by



Schweizerische Eidgenossenschaft  
Confédération suisse  
Confederazione Svizzera  
Confederaziun svizra

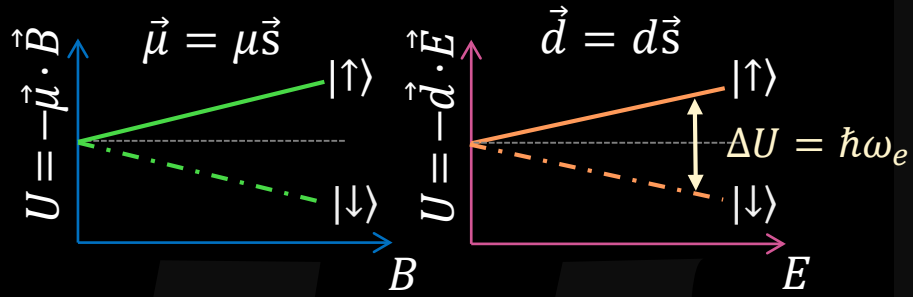
Swiss Confederation

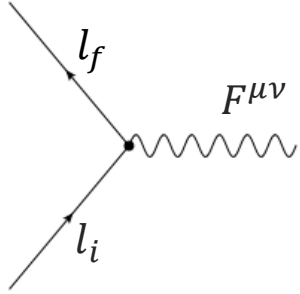
Federal Department of Economic Affairs,  
Education and Research EAER  
State Secretariat for Education,  
Research and Innovation SERI



SWISS NATIONAL SCIENCE FOUNDATION

# CP violation & edm





Effective Hamiltonian:  $\mathcal{H}_{\text{eff}} = c_R^{l_f l_i} \bar{l}_f \sigma_{\mu\nu} P_R l_i F^{\mu\nu} + \text{h. c.}$

$$\langle p' | J_\mu^{\text{EM}} | p \rangle = \bar{\Psi}(p') \left[ F_1 \gamma_\mu + \underbrace{\frac{iF_2}{2M} \sigma_{\mu\nu} q^\nu}_{\text{magnetic-dipole}} + \underbrace{\frac{iF_3}{2M} \sigma_{\mu\nu} \gamma_5 q^\nu}_{\text{electric-dipole}} + \frac{F_4}{M^2} (q^2 \gamma_\mu - \gamma^\mu q_\mu q_\mu) \right] \Psi(p)$$

charge
Anapole - moment

$$\delta F_2 = a_{l_i} = -\frac{2m_{l_i}}{e} \left( c_R^{l_i l_i} + c_R^{l_i l_i^*} \right) = -\frac{4m_{l_i}}{e} \text{Re } c_R^{l_i l_i}$$

$$F_3 = d_{l_i} = i \left( c_R^{l_i l_i} - c_R^{l_i l_i^*} \right) = -2 \text{Im } c_R^{l_i l_i}$$



Non relativistic Hamiltonian:  $\mathcal{H} = -\mu\vec{s}\cdot\vec{B} - d\vec{s}\cdot\vec{E}$   $|\vec{s}| = 1$

The magnetic  $\mu$  and electric  $d$  dipole moment of a lepton are defined by

$$\mu = \frac{gq}{2m} \frac{\hbar}{2}$$

$$d = \frac{\eta q}{2mc} \frac{\hbar}{2}$$

For leptons:

$$g = 2 + 2a$$

$$d = 0 + 10^{-36} ecm$$



$$\vec{\omega}_L = \frac{gq}{2m} \vec{B}$$

$$\vec{\omega}_E = \frac{\eta q}{2mc} \vec{E}$$



Relativistic lepton spin precession in a perpendicular magnetic field

$$\vec{\omega}_L = \frac{gq\vec{B}}{2m} + (1 - \gamma) \frac{q\vec{B}}{\gamma m} = \frac{aq\vec{B}}{m} + \frac{q\vec{B}}{\gamma m}$$

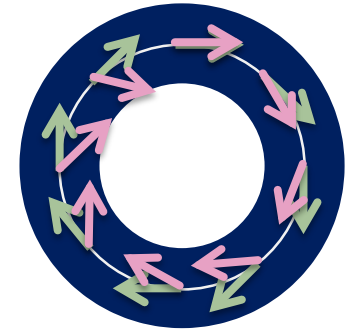
Cyclotron frequency of a lepton in a perpendicular magnetic field

$$\vec{\omega}_C = \frac{q\vec{B}}{\gamma m}$$

Measurement of the anomalous magnetic moment by observing relative precession

$$\vec{\omega}_a = \vec{\omega}_C - \vec{\omega}_L = -\frac{q}{m} a\vec{B}$$

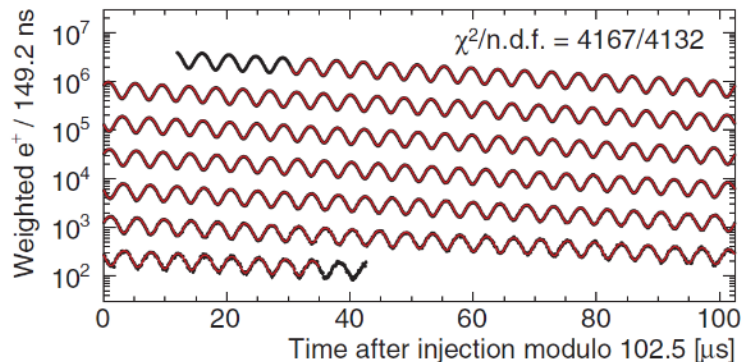
→ Momentum  
→ Spin



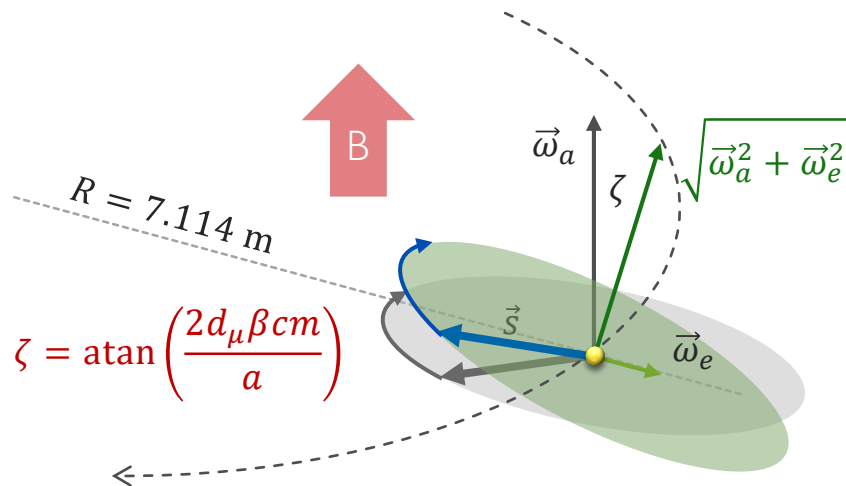
# Muon dipole moments and frequencies



$$\vec{\omega} = \vec{\omega}_L - \vec{\omega}_c = -\frac{q}{m} \left[ a\vec{B} + \underbrace{\left( \frac{1}{\gamma^2 - 1} - a \right) \frac{\vec{\beta} \times \vec{E}}{c}}_{\text{g-2 term } \omega_a} \right]$$



FNAL\* & JPARC\*\*:  $\sigma(d_\mu) \approx 10^{-21} ecm$



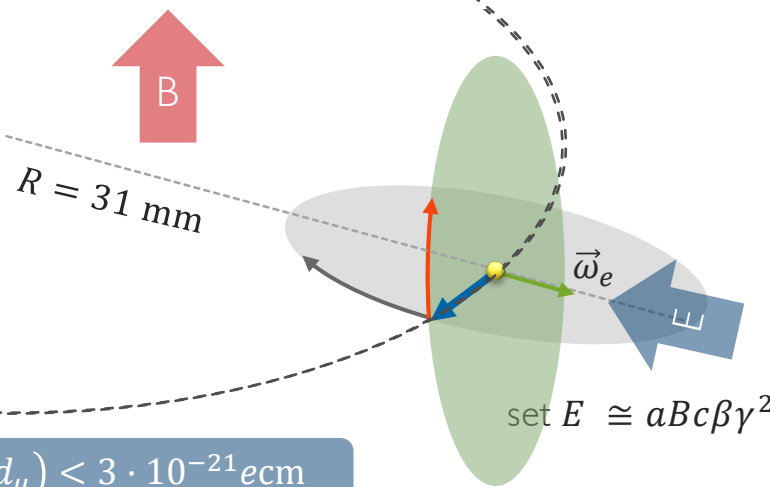
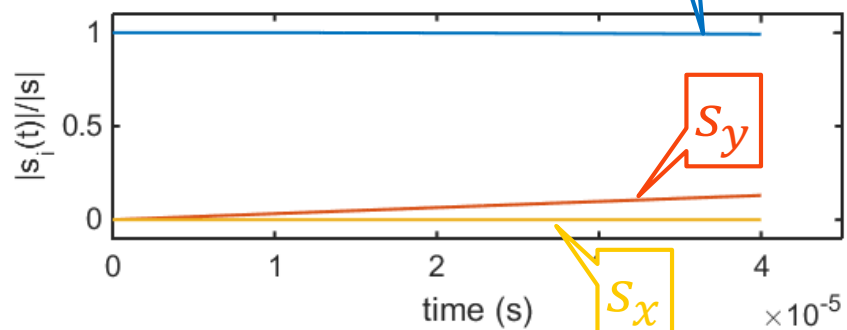
$$\zeta = \text{atan} \left( \frac{2d_\mu \beta c m}{a} \right)$$

# Muon dipole moments –freezing the spin at PSI



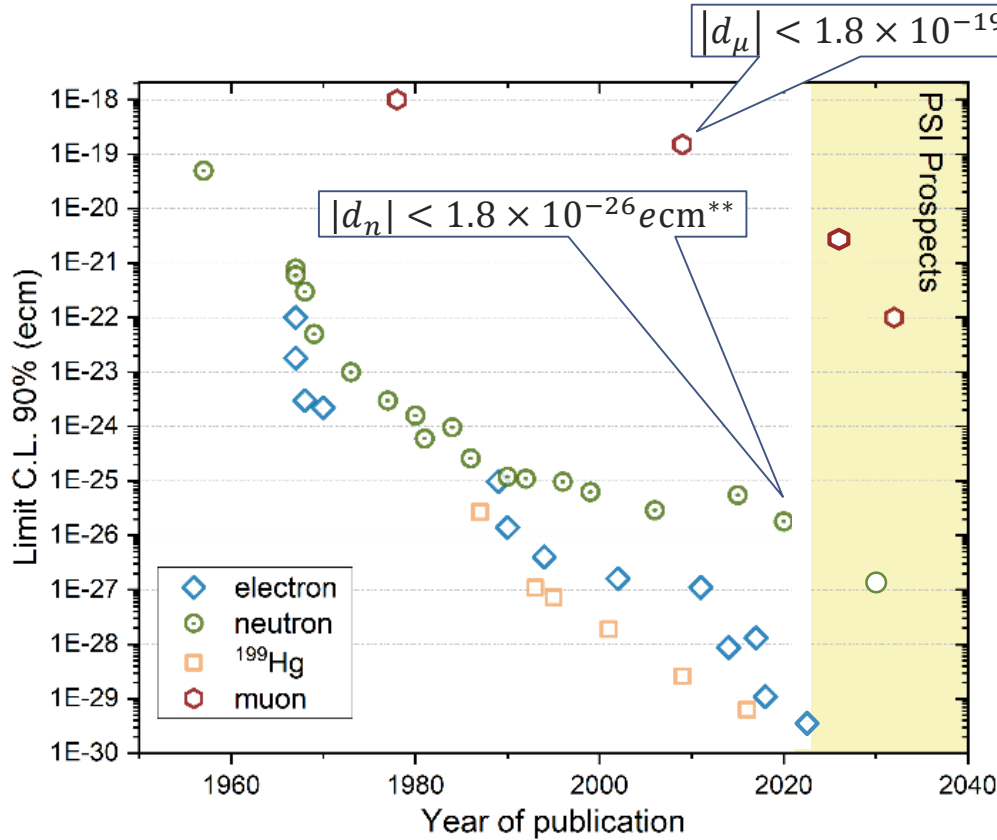
$$\vec{\omega} = -\frac{q}{m} \left[ \underbrace{a\vec{B} + \left( \frac{1}{1-\gamma^2} - a \right) \frac{\vec{\beta} \times \vec{E}}{c}}_{\text{g-2 term } \omega_a} + \underbrace{\frac{2d_\mu mc}{q\hbar} \left( \frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right)}_{\text{EDM term } \omega_e} \right]$$

Frozen-spin potential at PSI:  $\sigma(d_\mu) < 6 \cdot 10^{-23} \text{ ecm}$

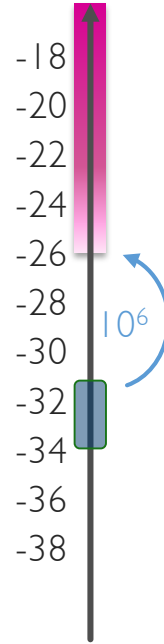


[\*Farley et al., PRL93 042001 (2004)] ,

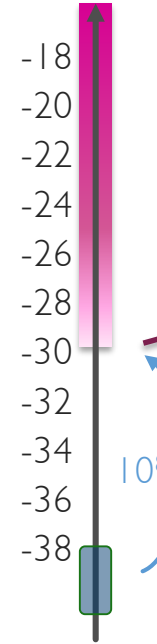
# A not so brief history of EDM searches



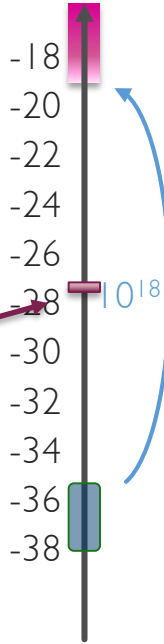
Neutron  
log(d) /ecm



Electron  
log(d) /ecm



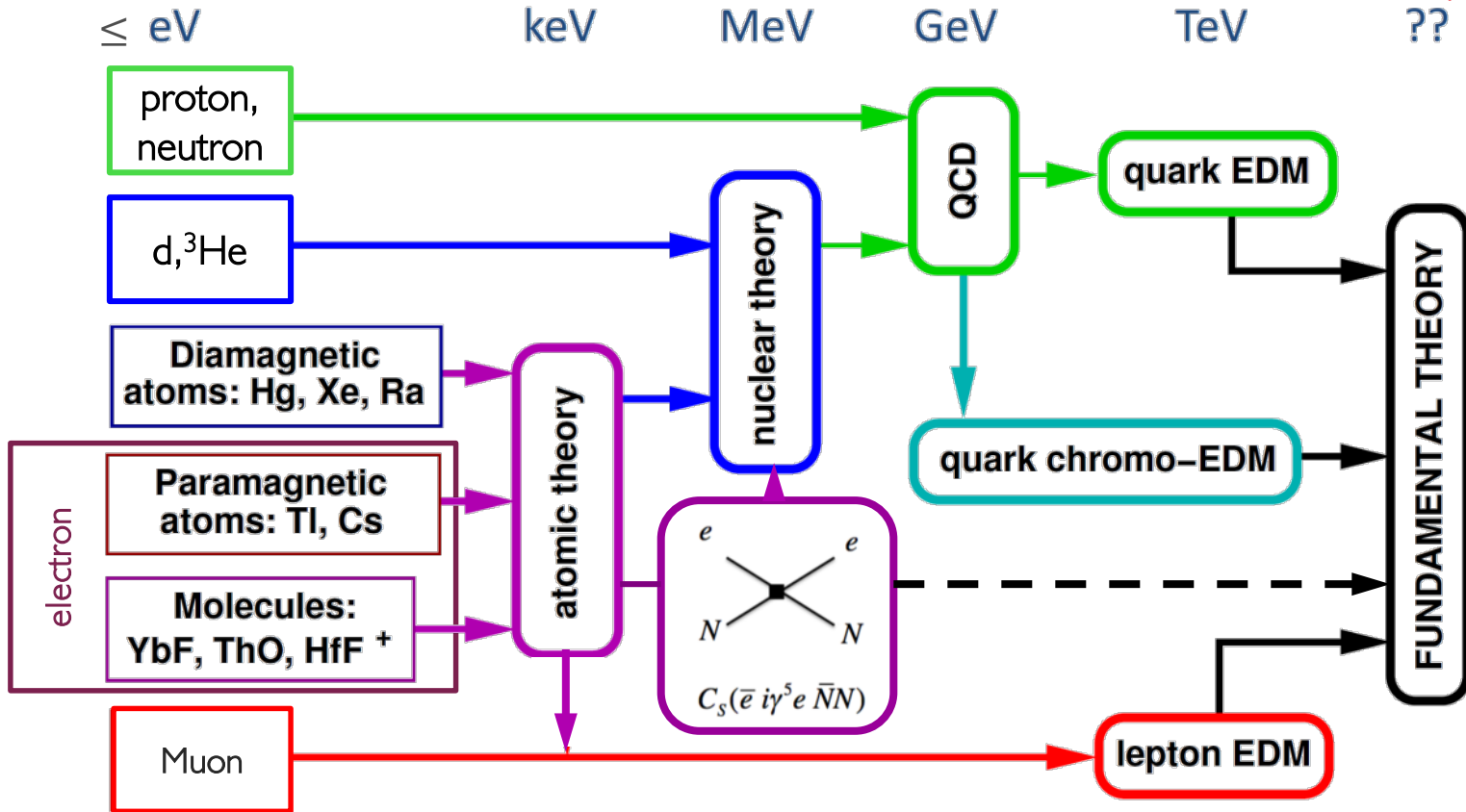
Muon  
log(d) /ecm

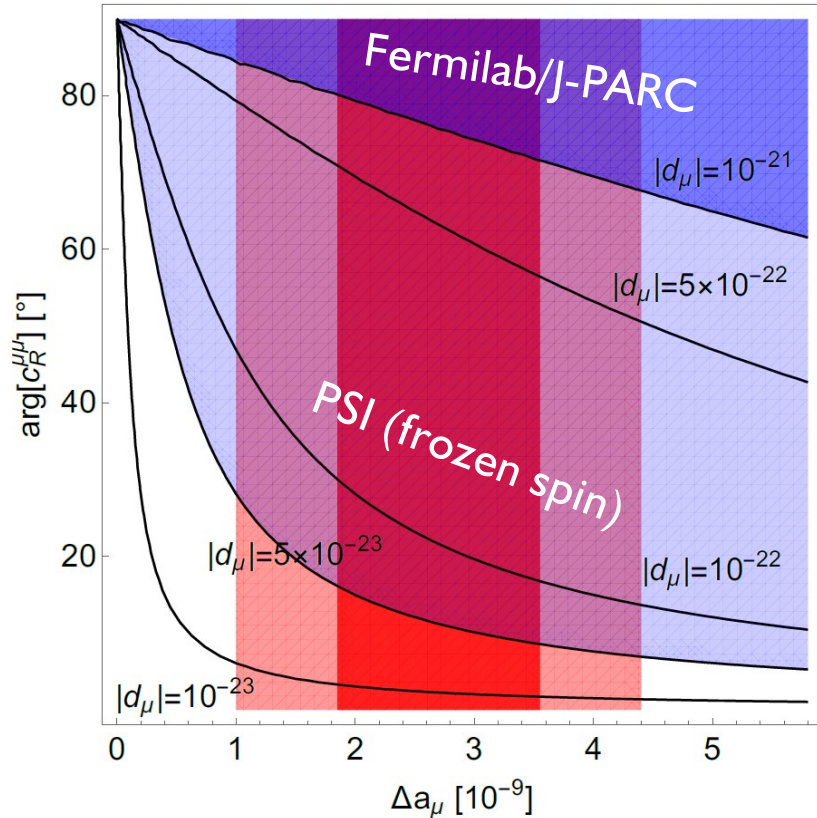


\* Bennett et al., PRD80(2009)052008  
\*\* Abel et al., PRL124(2020)081803

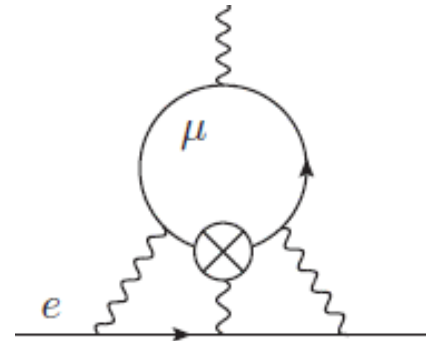


# Complementarity of EDM searches





- MFV:  $|d_{\mu \leftarrow e}^{\text{MFV}}| < 8.5 \times 10^{-28} \text{ ecm}$
- Contribution only starts at the 3-loop level\*  
 $|d_{\mu \leftarrow e}| < 4 \times 10^{-20} \text{ ecm}$
- Y. Ema et al., PRL **128**, 131801 (2022)  
 $|d_\mu(^{199}\text{Hg})| < 6 \times 10^{-20} \text{ ecm}$   
 $|d_\mu(\text{ThO})| < 2 \times 10^{-20} \text{ ecm}$
- Bennett et al., PRD **80**, 052008 (2009)  
 $|d_\mu| < 1.5 \times 10^{-19} \text{ ecm}$

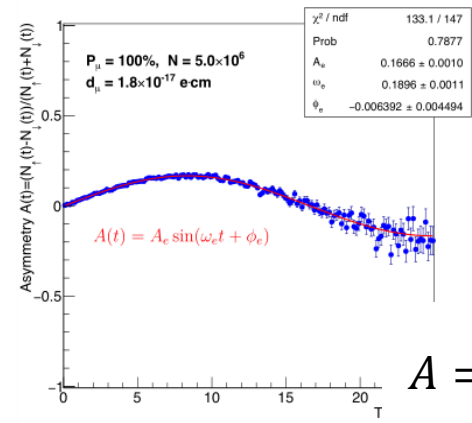
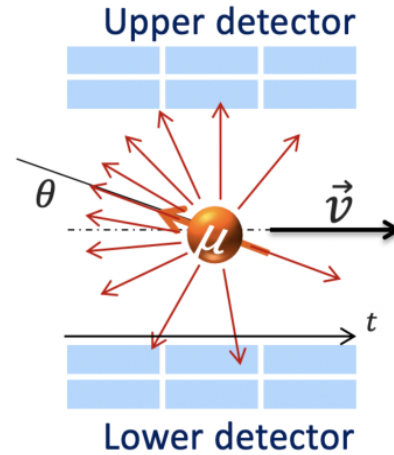
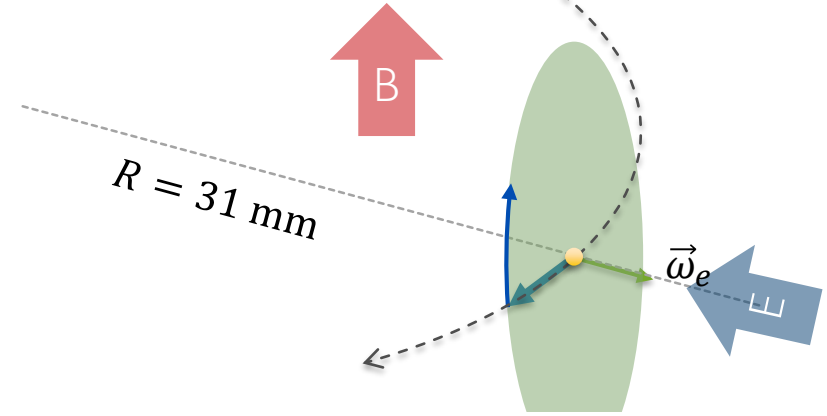


\*A.Crivellin, M. Hoferichter, PSW PRD 98, 113002 (2018)

# The general experimental idea



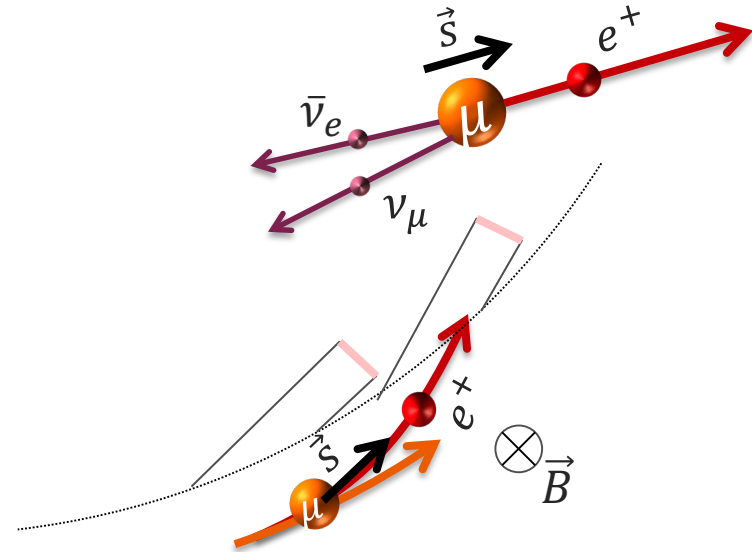
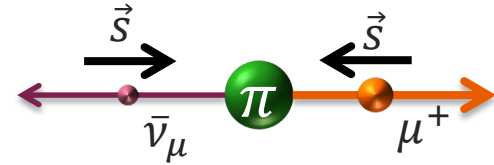
- If the EDM  $\neq 0$ , then there will be a vertical precession out of the plane of the orbit
- An asymmetry increasing with time will be observed recording decay positrons
- If the EDM = 0, then the spin should always be parallel to the momentum asymmetry should be zero
- Some asymmetry could still be observed due to systematic effects



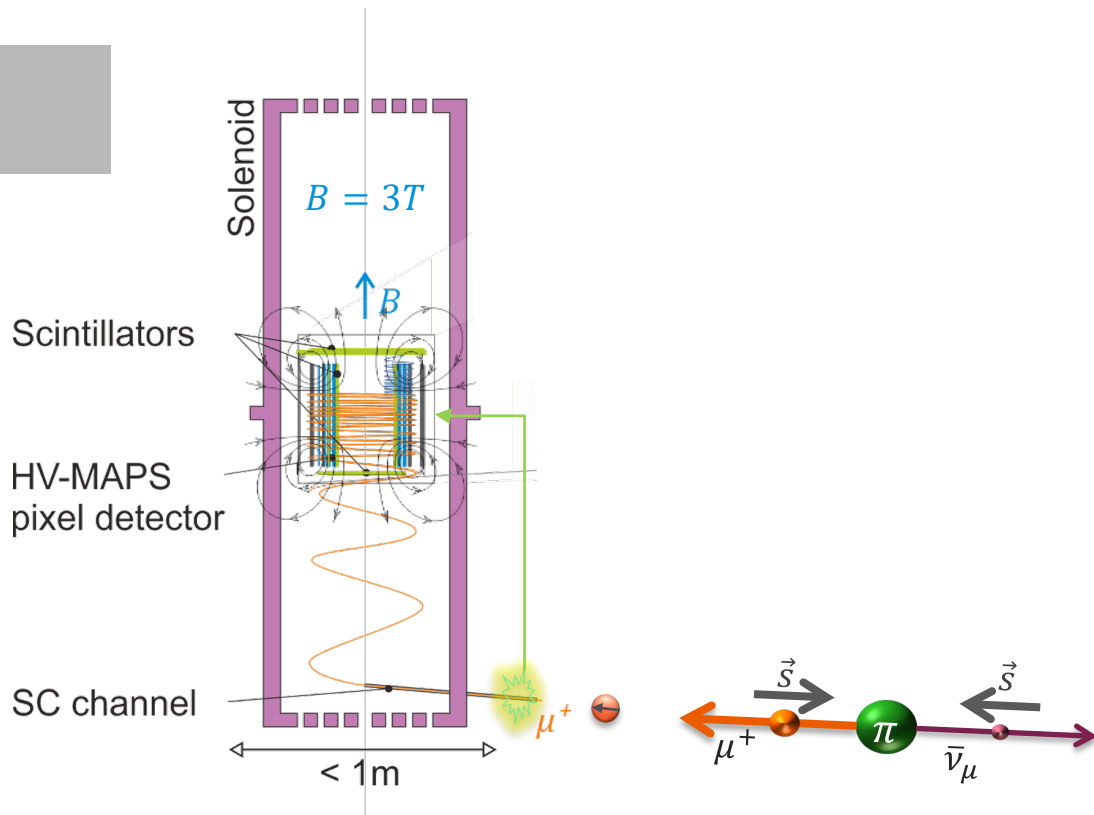
$$A = \frac{N_u - N_d}{N_u + N_d}$$



- Weak decay  $\pi^+ \rightarrow \mu^+ + \bar{\nu}_\mu$   
result in  $P_\mu \approx 95\%$  for  $p_\pi \sim 220 \text{ MeV}/c^2$  backward decay in  $P_\mu \approx 95\%$
- Weak decay  $\mu^+ \rightarrow e^+ + \bar{\nu}_e + \nu_\mu$   
results in decay asymmetry  
 $\bar{\alpha} \approx 0.3$
- Detection of  $e^+$  of decay  
(for EDM vertical resolution)

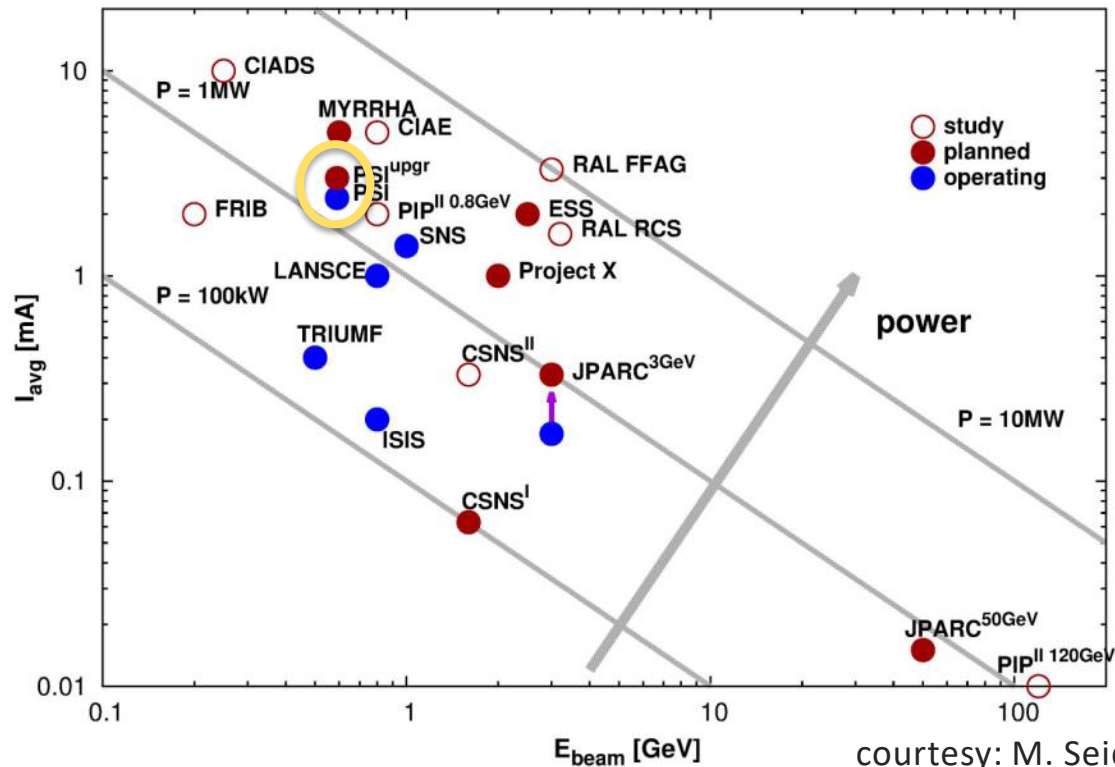
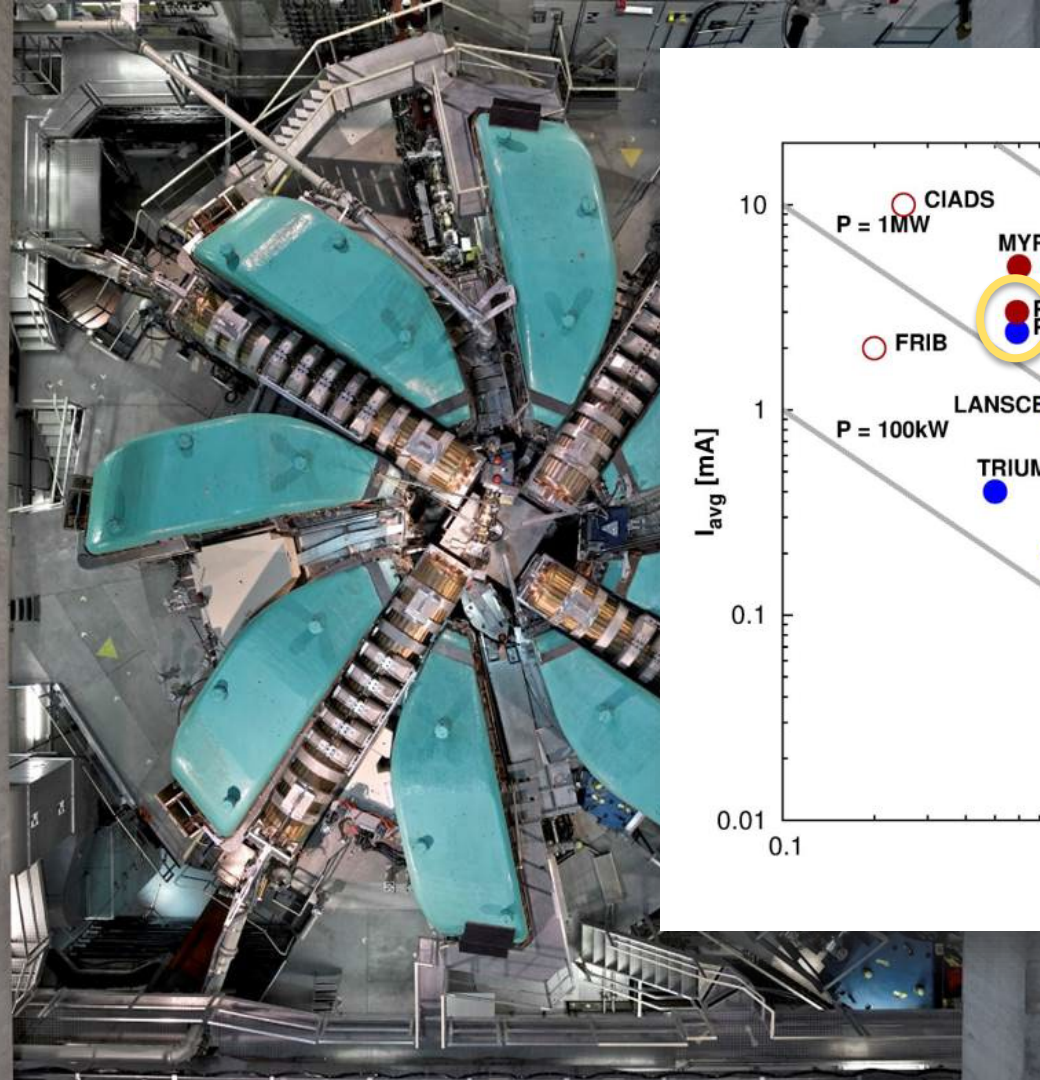


# Search for a muon EDM using the frozen-spin technique with longitudinal injection

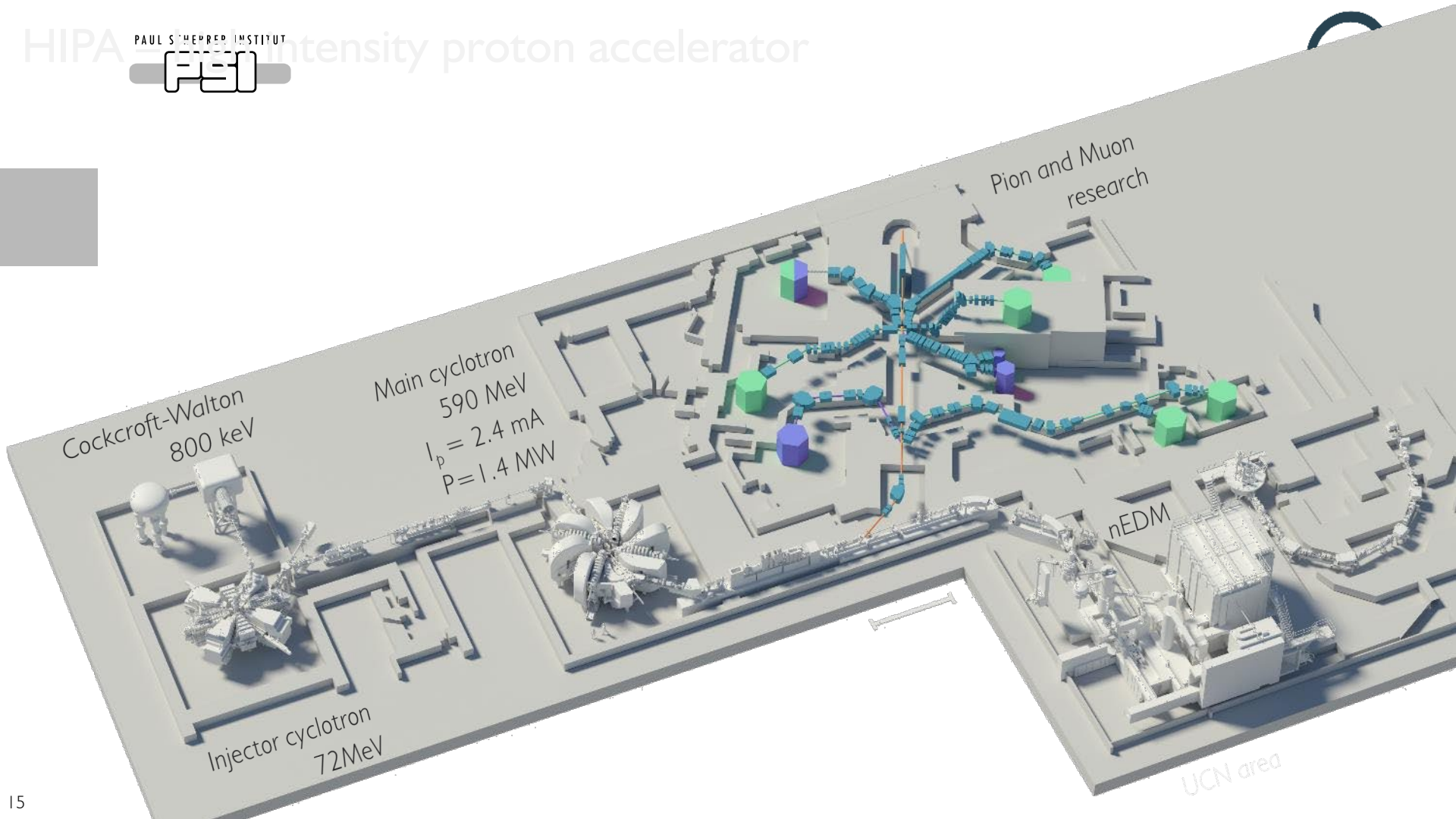


$\mu^+$  @ 125MeV/c or 28MeV/c

- $\mu^+$  from **Pion-decay**  $\rightarrow$  high polarization  $p \approx 95\%$
- Injection through **superconducting channel**
- **Fast** scintillator **triggers** pulse
- Magnetic **pulse stops** longitudinal motion of  $\mu^+$
- Weakly focusing field for **storage**
- **Thin electrodes** provide electric field for **frozen spin**
- Pixelated detectors for  **$e^+$  - tracking**



courtesy: M. Seidel



Cockcroft-Walton  
800 keV

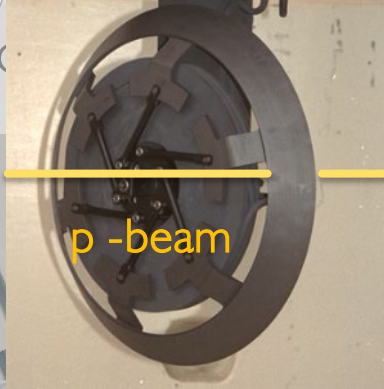
Main cyclotron  
590 MeV  
 $I_p = 2.4 \text{ mA}$   
 $P = 1.4 \text{ MW}$

Pion and Muon  
research

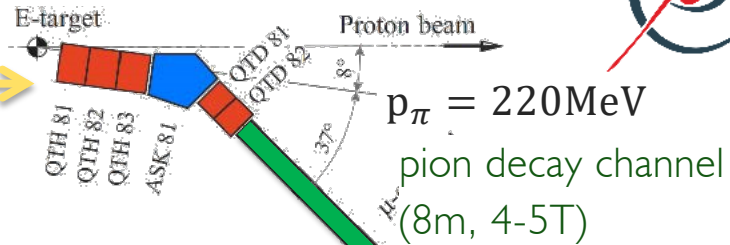
nEDM

Injector cyclotron  
72 MeV

UCN area



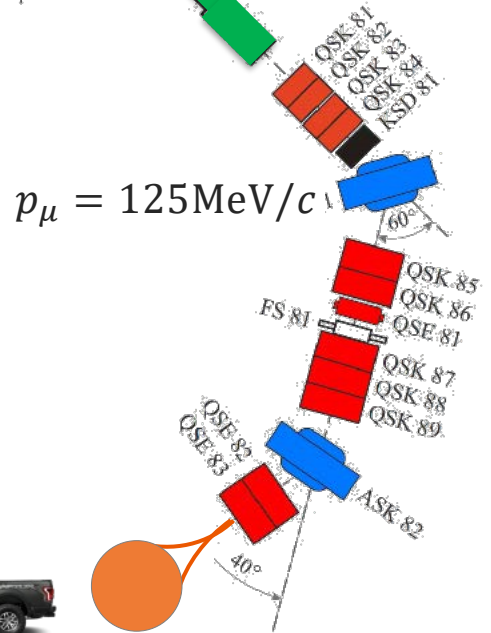
p-beam



1 m

$\mu$ -beam:

- $10^8 \mu^+ / \text{s}$
- Bunch width 3.9 ns





# A phased approach



## Phase I (small solenoid, surface muons)



- Existing solenoid at PSI, max 5T
- Bore diameters 200mm
- Field was measured in 2022 (found suitable for injection)

## Phase 2 (dedicated magnet muon momentum $\geq 125\text{MeV}/c$ )



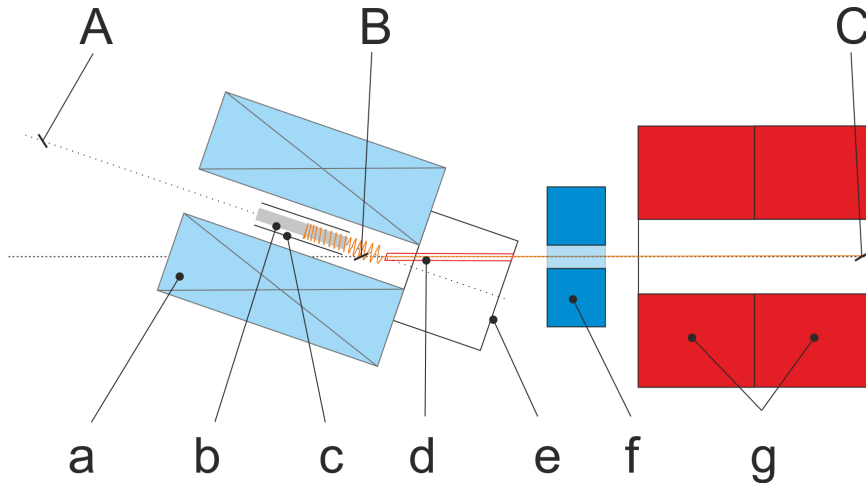
Argonne 4T solenoid

- Large bore (up to 900 mm diameter)
- High Temporal field stability (10ppb/h)
- Excellent spatial field uniformity ( $< 1$  ppb/mm)





- Large phase space at exit of beam collimated by passage through a collimation channel (d)
- Due to adiabatic magnetic collimation large part of transmitted  $\mu^+$  are reflected.
- Simulations show, only about  $0.5 \times 10^{-3}$  muons can be stored

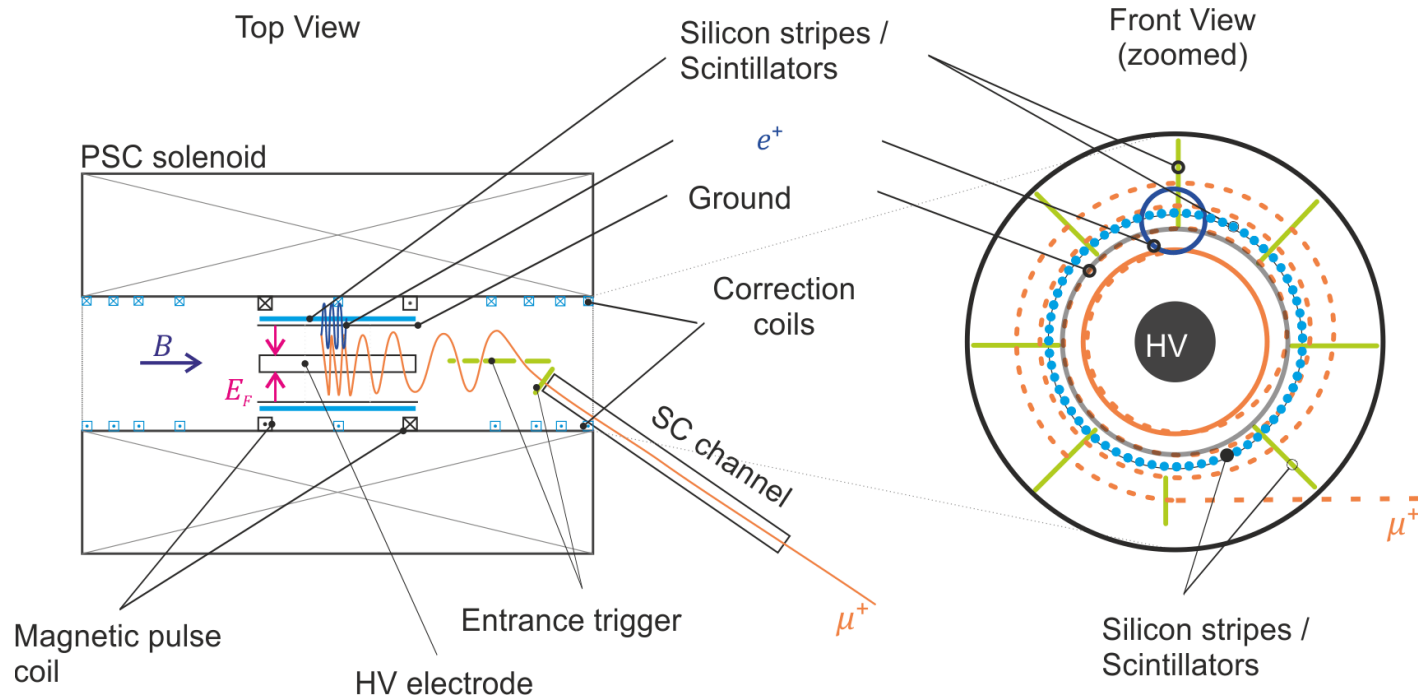
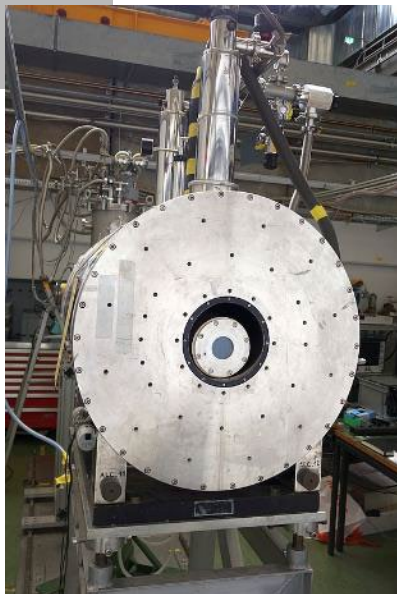


$$\sigma(d_\mu) = \frac{\hbar \gamma a_\mu}{2pE_f \sqrt{N} \tau_\mu \alpha}$$

	$\pi E1$	$\mu E1$
Muon flux ( $\mu^+/s$ )	$4 \times 10^6$	$1.2 \times 10^8$
Channel transmission	0.03	0.005
Injection efficiency	0.017	0.60
Muon storage rate (1/s)	$2 \times 10^3$	$360 \times 10^3$
Gamma factor $\gamma$	1.04	1.56
$e^+$ detection rate (1/s)	500	$90 \times 10^3$
<b>Detections per 200 days</b>	$8.64 \times 10^9$	$1.5 \times 10^{12}$
Mean decay asymmetry $A$	0.3	0.3
Initial polarization $P_0$	0.95	0.95
<b>Sensitivity in one year (<math>e\text{-cm}</math>)</b>	$< 3 \times 10^{-21}$	$< 6 \times 10^{-23}$

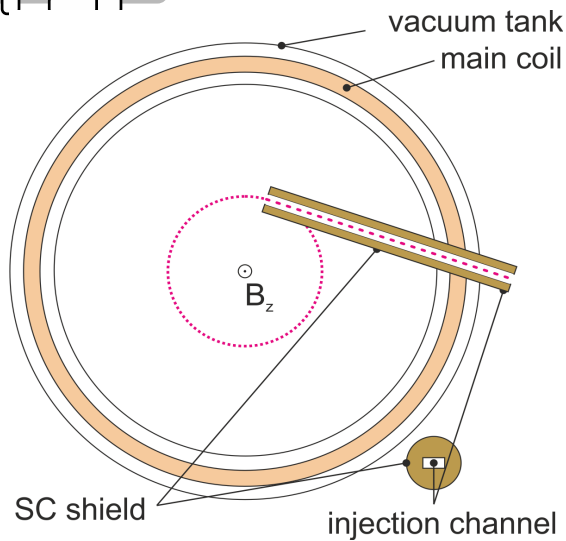
# The muEDM phase I on piE1

## Test bed and frozen spin demonstrator

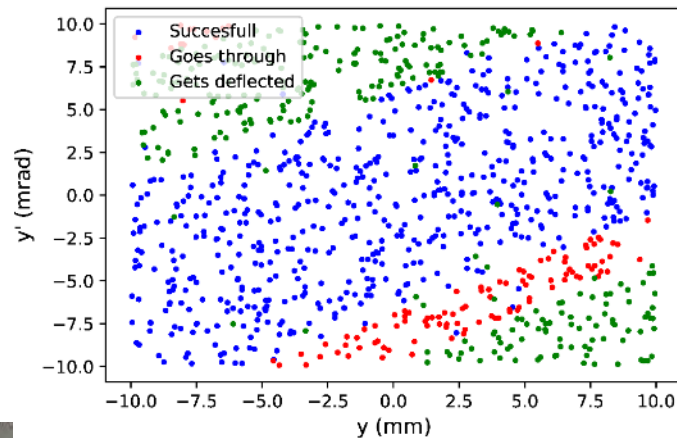


$$\text{muEDM measurement} < 3 \cdot 10^{-21} \text{ ecm}$$

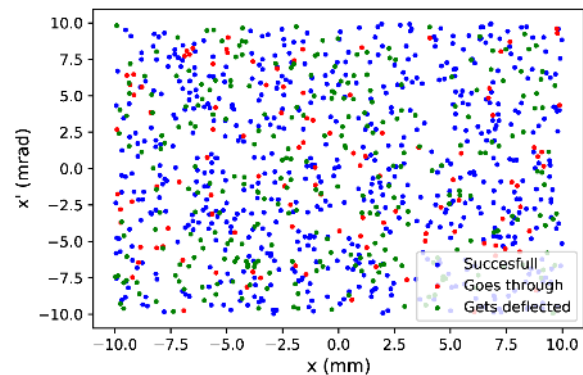
# Injection channel



- Injection channel with SC magnetic shield
- Defines vertical and horizontal divergence

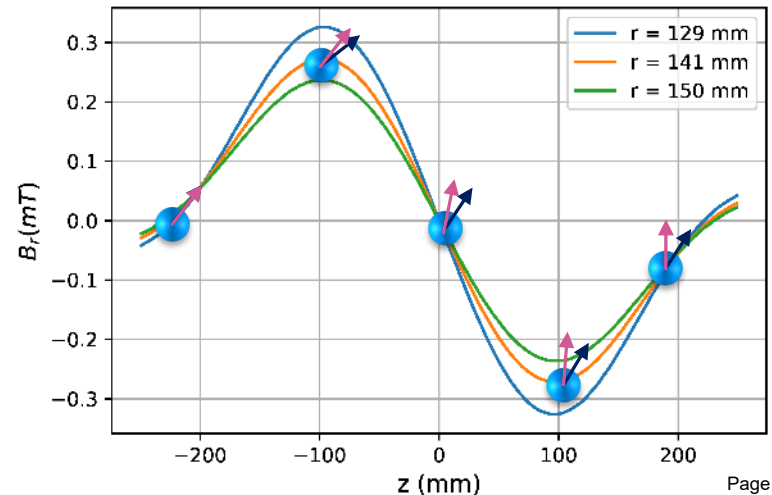
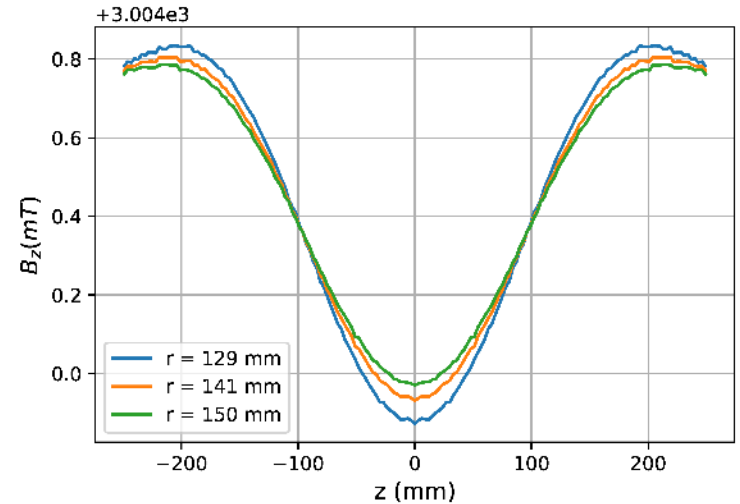
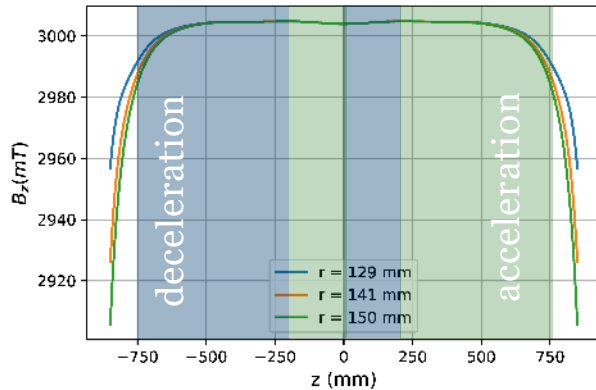


horizontal

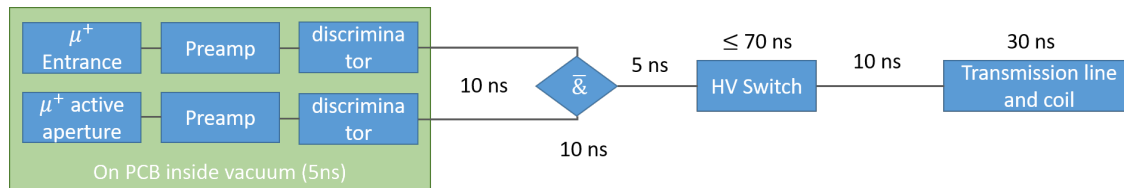
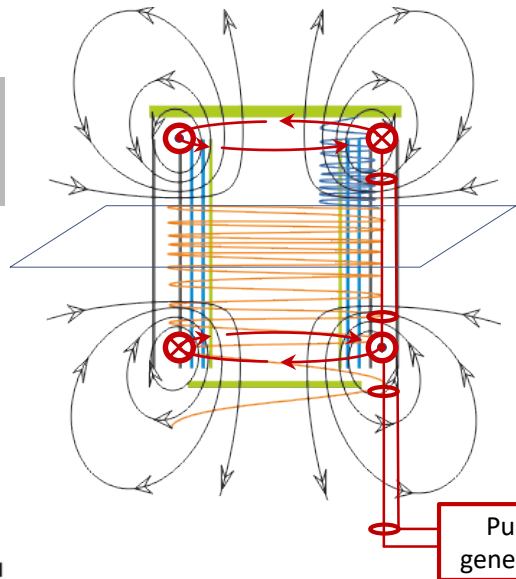


# Storage and injection

- Strength of weakly focusing field in the center region defines “depth” of storage
- The deeper / stronger the weakly focusing field the stronger needs to be the pulse



# Radial magnetic field pulse to kick muons



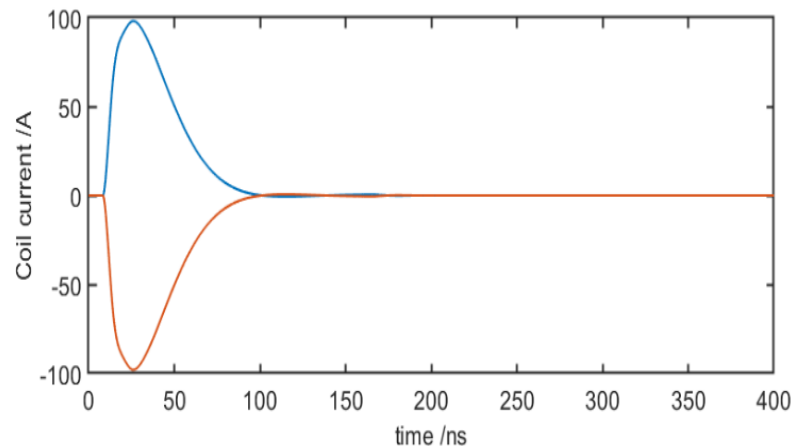
1. Inject beam at vertical angle in solenoid storage magnet.
2. Radial fringe field reduce injection angle.

Solenoid Axis  
Y

Y = 0  
Mid Plane

3. Vertical magnetic kick will reduce the remaining angle to about zero.

4. The beam will be stored at the midplane under the remaining angle to about zero.



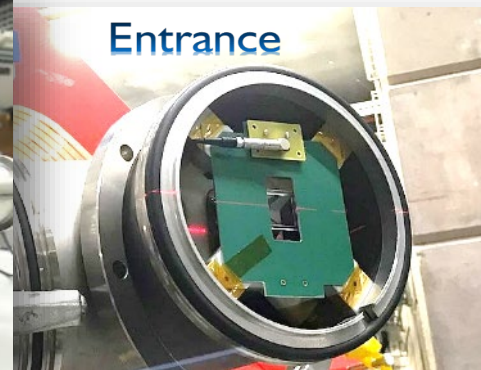
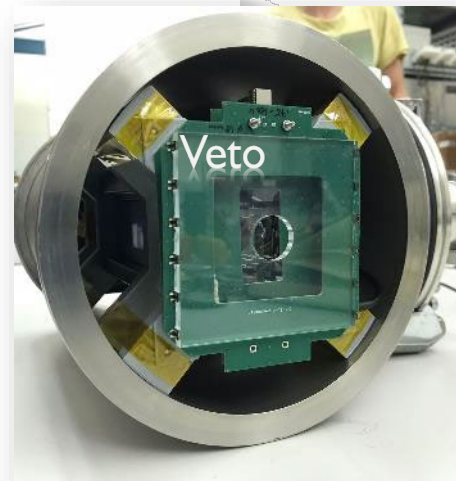
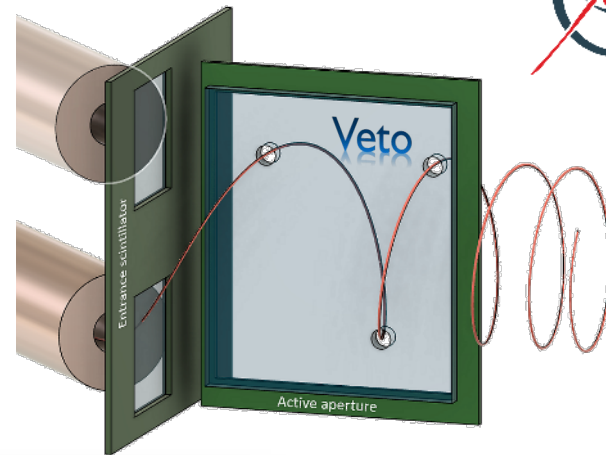
# Muon entrance trigger

- Magnetic pulse needs to be triggered by incident muon
- Only about 2% of muons passing through the collimation channel are within the acceptance phase space
- Scattering in scintillators increase beam divergence



- Combine thin ( $\leq 100\mu\text{m}$ ) entrance scintillator with
- Active aperture as veto

Entrance







## Detection of g-2 precession $\omega_a$

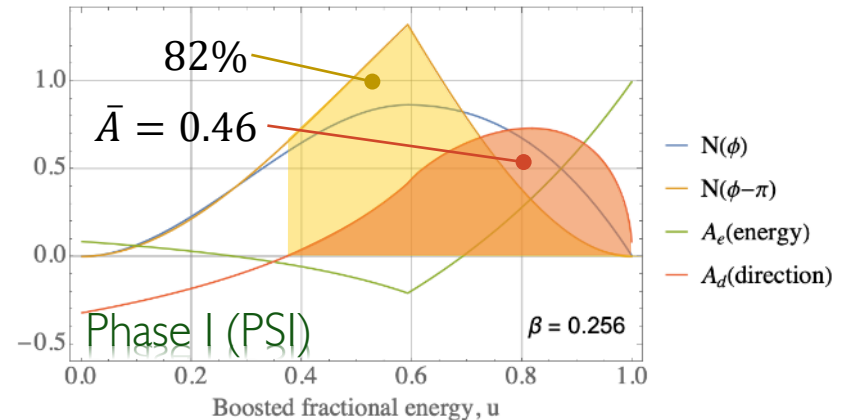
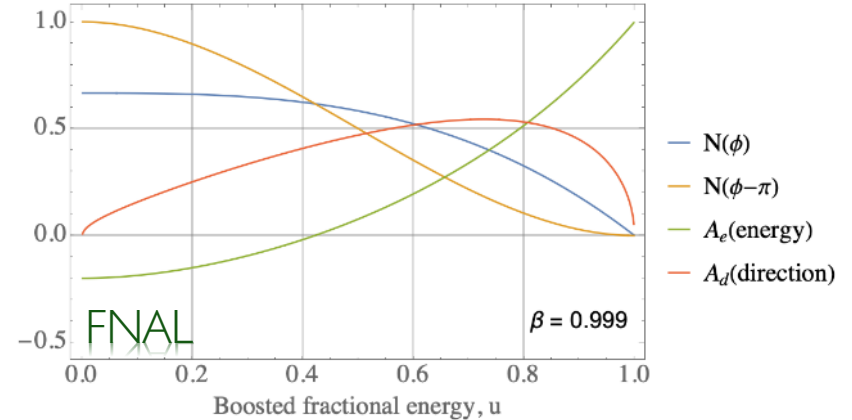
- Measurement of mean magnetic field  $\langle B \rangle$
- Measure  $\omega_a(E)$  to tune electric field to frozen-spin condition

Requires momentum resolution

## Detection of EDM polarization

- Measurement of Asymmetry as function of time  $A(t)$

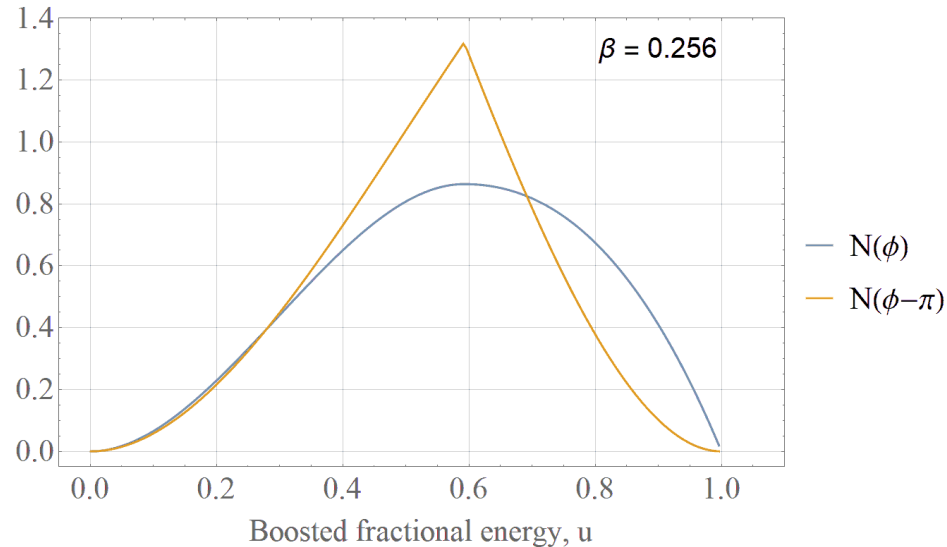
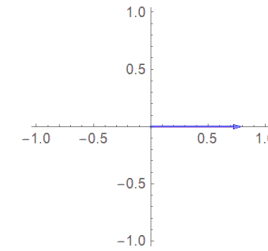
Requires spatial resolution along cylinder



# Tuning the electric field to the frozen-spin condition



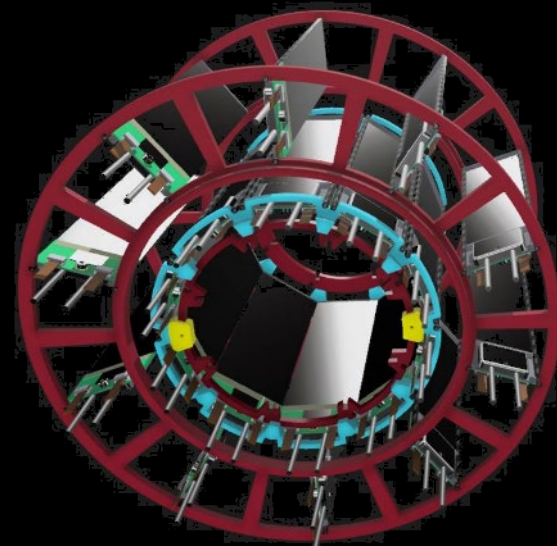
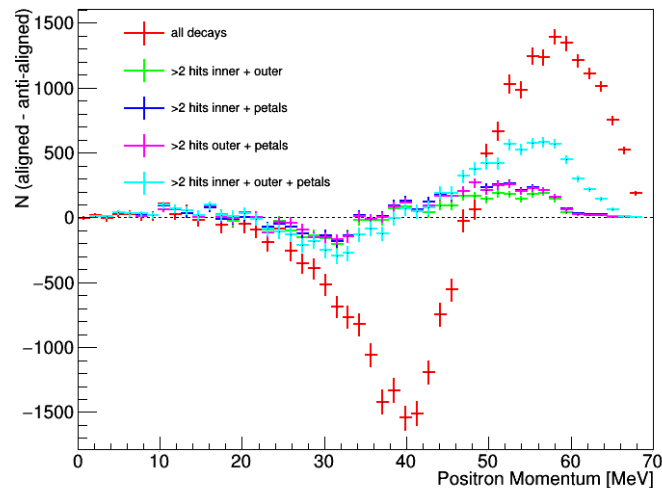
- Measure the g-2 frequency  $\omega_a$
- Two momentum bins  
 $28 \text{ MeV}/c < p_1 < 50 \text{ MeV}/c$   
 $50 \text{ MeV}/c < p_2$
- Change E field in the range  
 $\pm E_{\text{frozen}} \approx \pm 3 \text{ kV}/\text{cm}$
- Extrapolate to  $E_{\text{frozen}}$  where  $\omega_a = 0$





## Silicon strip detector for g-2 detection

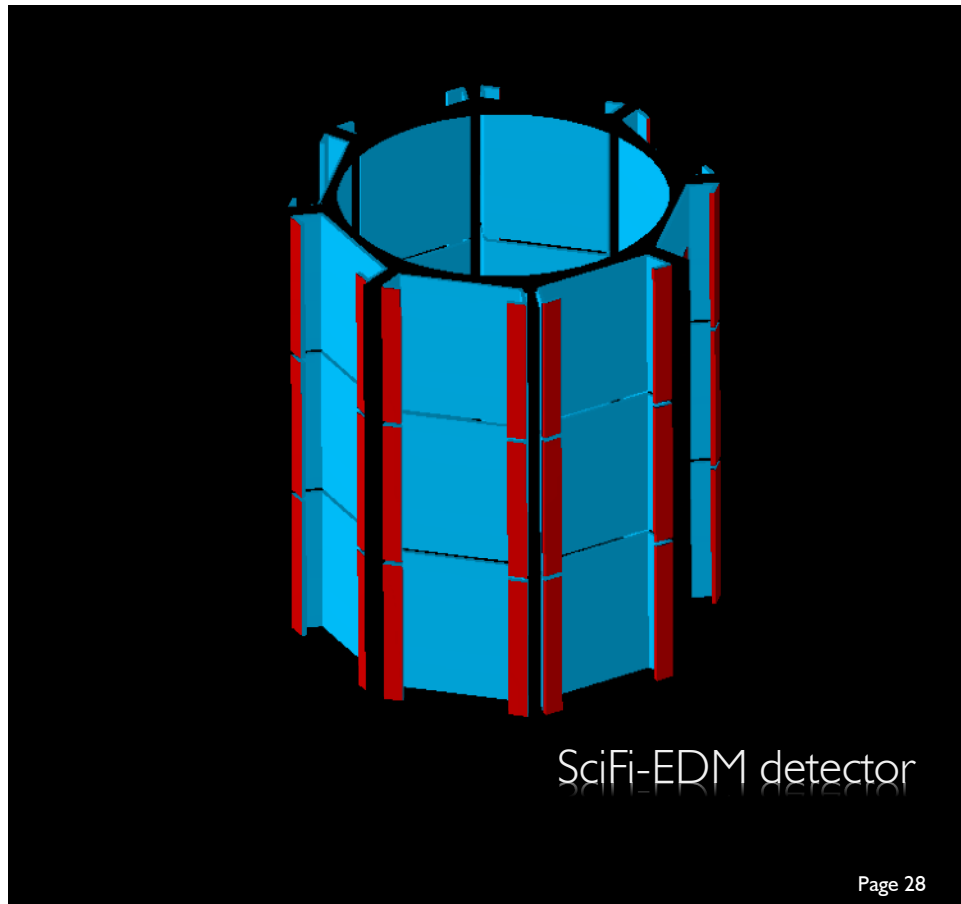
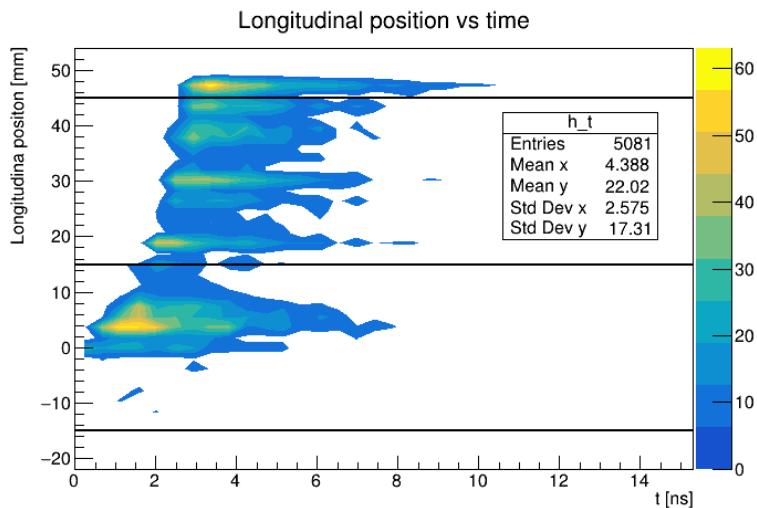
- Reconstruction of transverse positron momentum ( $\Delta p \approx 5 \text{ MeV}/c$ )
- Timing  $\Delta t \approx 2 \text{ ns}$
- Spatial resolution  $\approx 0.1 \text{ mm}$  (lateral)



Si-Petal detector

Scintillating fiber detector for EDM  
asymmetry measurement and timing

- Horizontal fiber ribbons with **250 $\mu\text{m}$**  pitch and **100 $\mu\text{m}$**  resolution
- Timing resolution **< 2ns**
- Reconstruction of longitudinal momentum

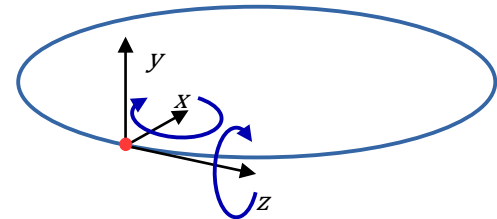




- Systematic effects: all effects that lead to a *real* or *apparent* precession of the spin around the radial axis that are not related to the EDM
- Major sources of systematic effects in the frozen spin technique:
  - Coupling of the magnetic moment with the EM fields of the experimental setup (*real*)
  - Early to late variation of detection efficiency of the EDM detectors (*apparent*)

- Rotations that could mimic the EDM:
  - Radial around x
  - Azimutal around z

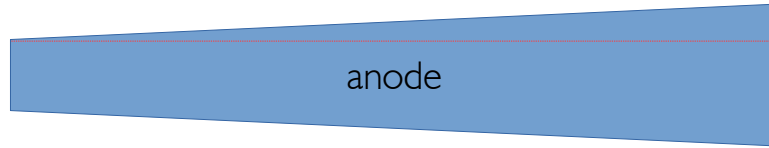
$$\vec{\Omega}_{\text{MDM}} = -\frac{e}{m_0} \left[ a\vec{B} - a\frac{\gamma-1}{\gamma} \frac{(\vec{\beta} \cdot \vec{B})\vec{\beta}}{\beta^2} + \left( \frac{1}{\gamma^2-1} - a \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$



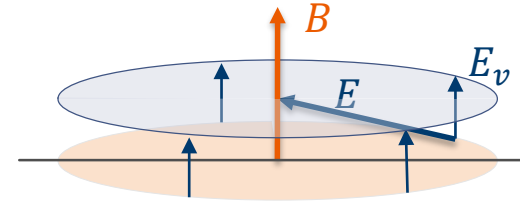


- None constant radius of cylindrical anode (cone)

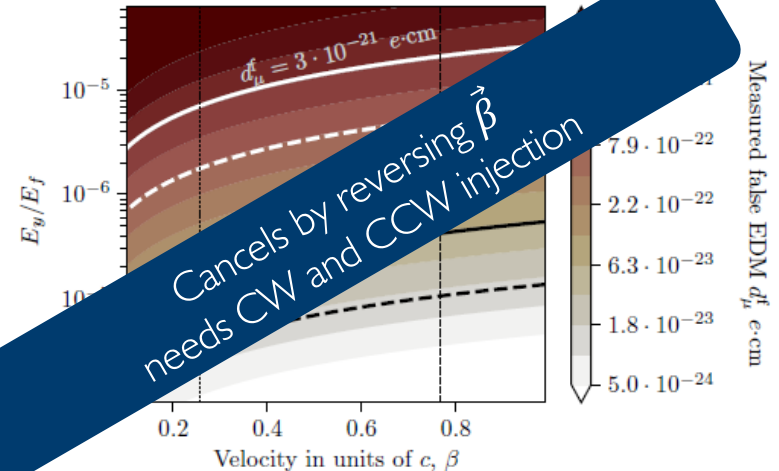
$$E_y \approx E_f \frac{\Delta R}{L} \approx E_f \alpha$$

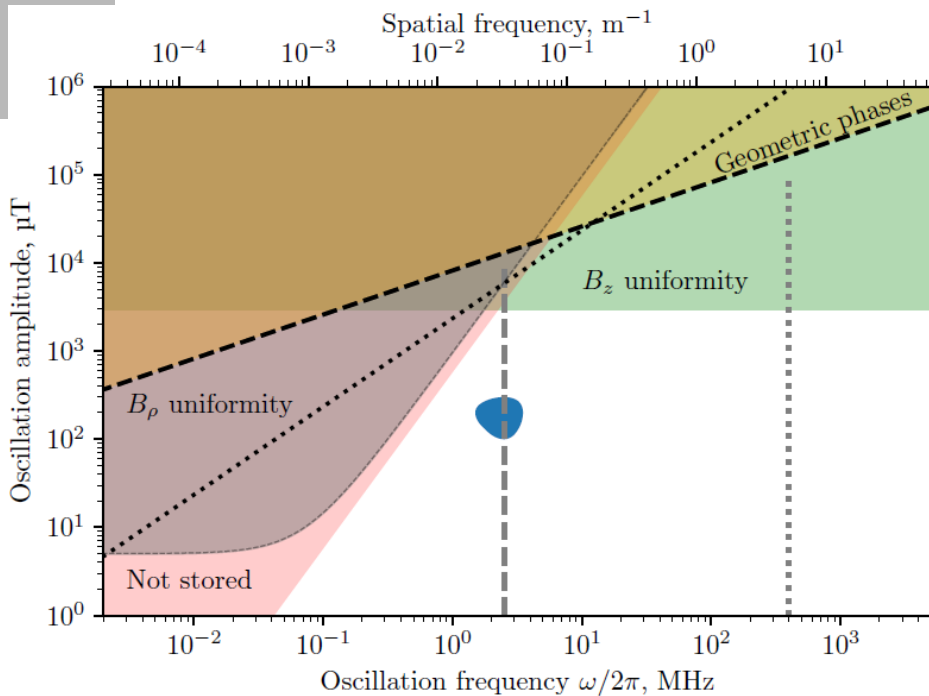


- Cylindricity on the order of 50 nm is measurable even on large samples and possible to machine
- Ground electrode made of thin foil more difficult to keep deviations from cylindricity below  $30\mu\text{m}$

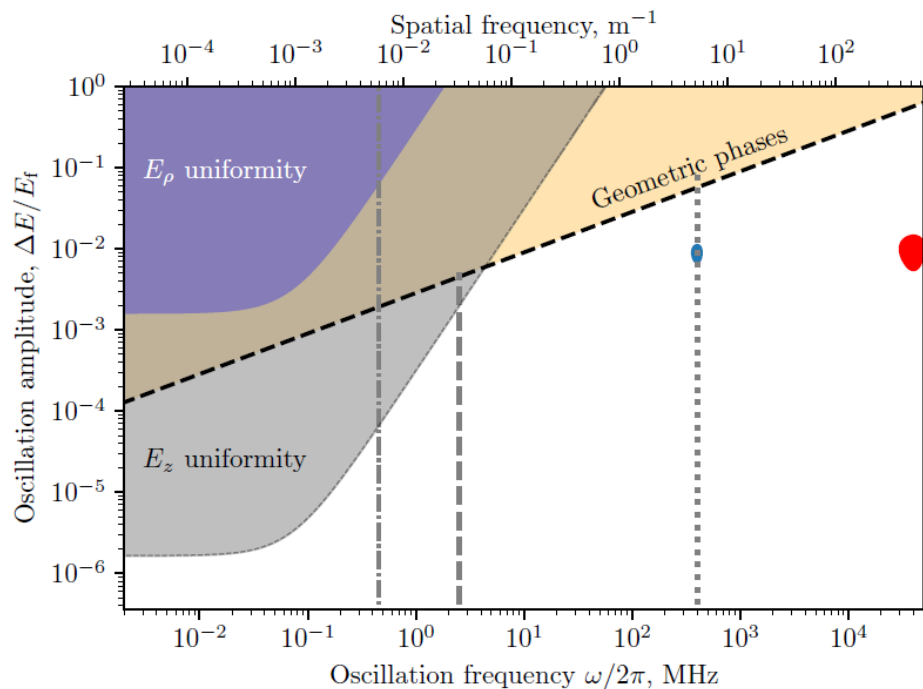


Will move orbit out of central plane until:  
 $\langle B_r^* \rangle = -\langle E_v / \beta \gamma \rangle$





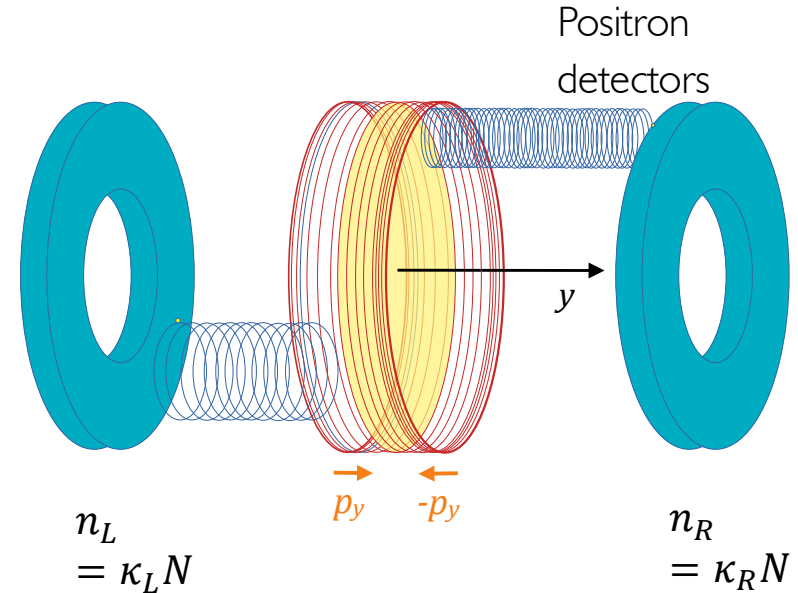
Magnetic field



Electric field



- The EDM will be deduced from the accumulation of asymmetry between the upstream and downstream detectors that increases with time
- Static differences in the detection efficiency of one detector compared to the other is not a problem
- Change of the detection efficiency with time is a problem as it will introduce time dependent asymmetry







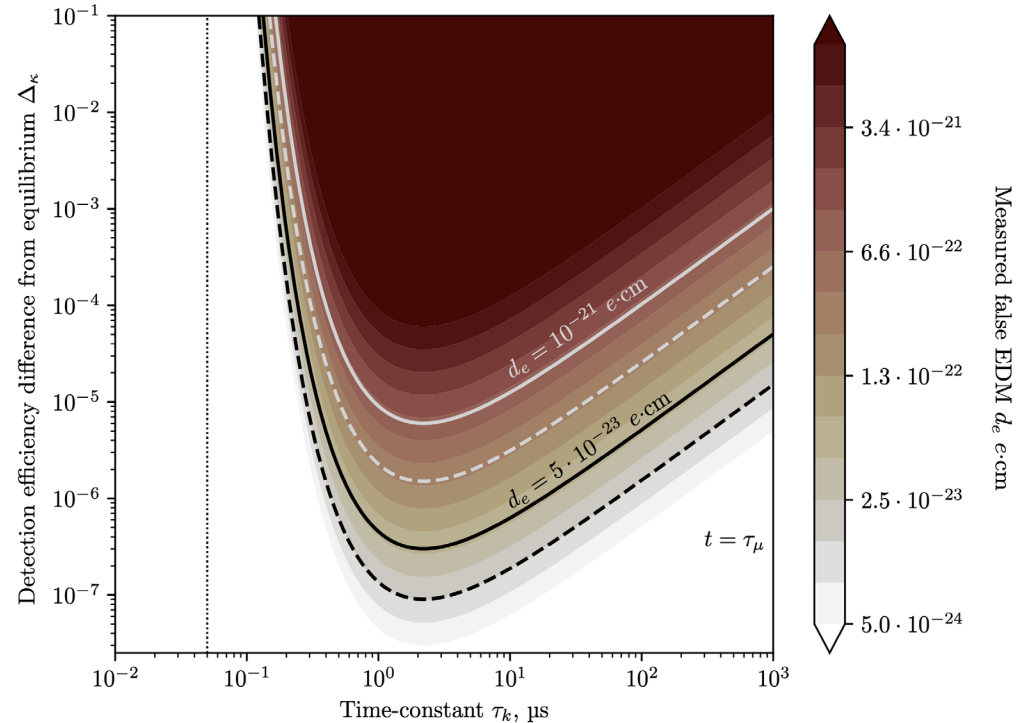
- Assumption: Change of detection efficiency triggered by pulse, exponential decay
- Detection efficiency of up and downstream detectors:

$$\kappa_u = \kappa_{u0} - \Delta_\kappa e^{-t/\tau_k},$$

$$\kappa_d = \kappa_{d0} + \Delta_\kappa e^{-t/\tau_k},$$

- Change in measured asymmetry with time:

$$\dot{A}_m = \frac{2}{\tau_k} \Delta_\kappa e^{-t/\tau_k}$$





- Systematic effects are studied using analytic expressions
- Comparison with GEANT4 spin tracking Monte Carlo for verification
- Deduce specifications for experiment

Next steps:

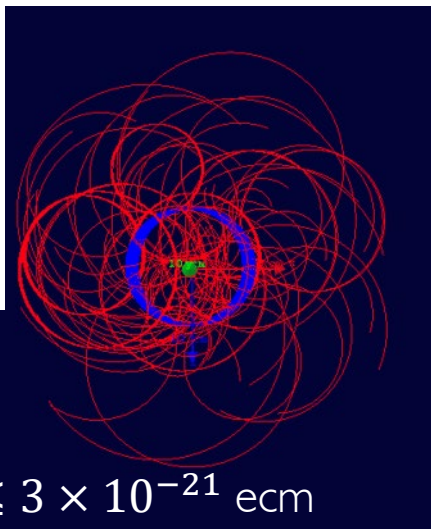
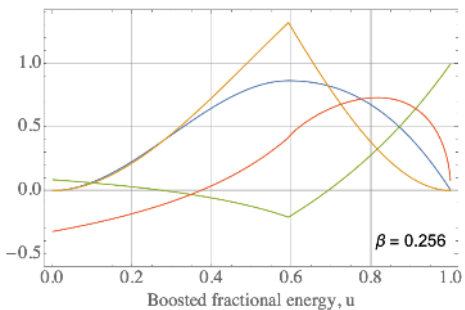
- Parametrization of magnetic-field non-uniformity
- Deduce magnetic-field requirements

Systematic effect	Constraints	Phase I	
		Expected value	Syst. ( $\times 10^{-21}$ e·cm)
Cone shaped electrodes (longitudinal E-field)	Up-down asymmetry in the electrode shape	$\Delta_R < 30 \mu\text{m}$	0.75
Residual B-field from kick	Decay time of kicker field	$< 50 \text{ ns}$	$< 10^{-2}$
Net current flowing muon orbit area	Wiring of electronics inside the orbit	$< 10 \text{ mA}$	$< 10^{-2}$
Longitudinal B-field uniformity	Solenoid alignment	$< 3 \text{ mT}$	-
Resonant geometrical phase accumulation	Misalignment of central axes	Pitch $< 1 \text{ mrad}$ Offset $< 2 \text{ mm}$	$2 \times 10^{-2}$
<b>TOTAL</b>			<b>1.1</b>



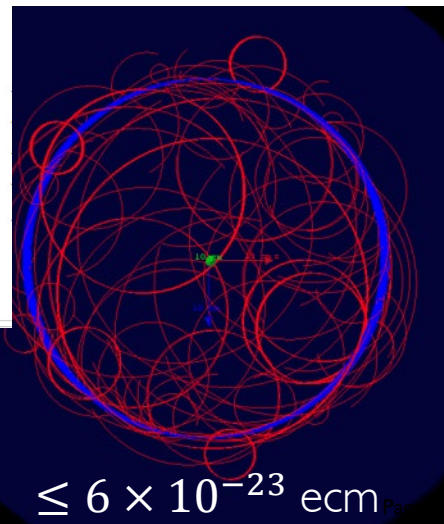
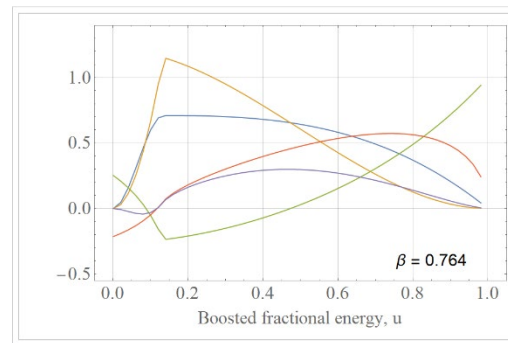
## Phase I

- B-Field 3T
- Momentum 28 MeV/c
- Muon radius 31 mm
- Most positrons outside



## Phase II

- B-Field 3T
- Momentum 125 MeV/c
- Muon radius 141 mm
- Most positrons inside



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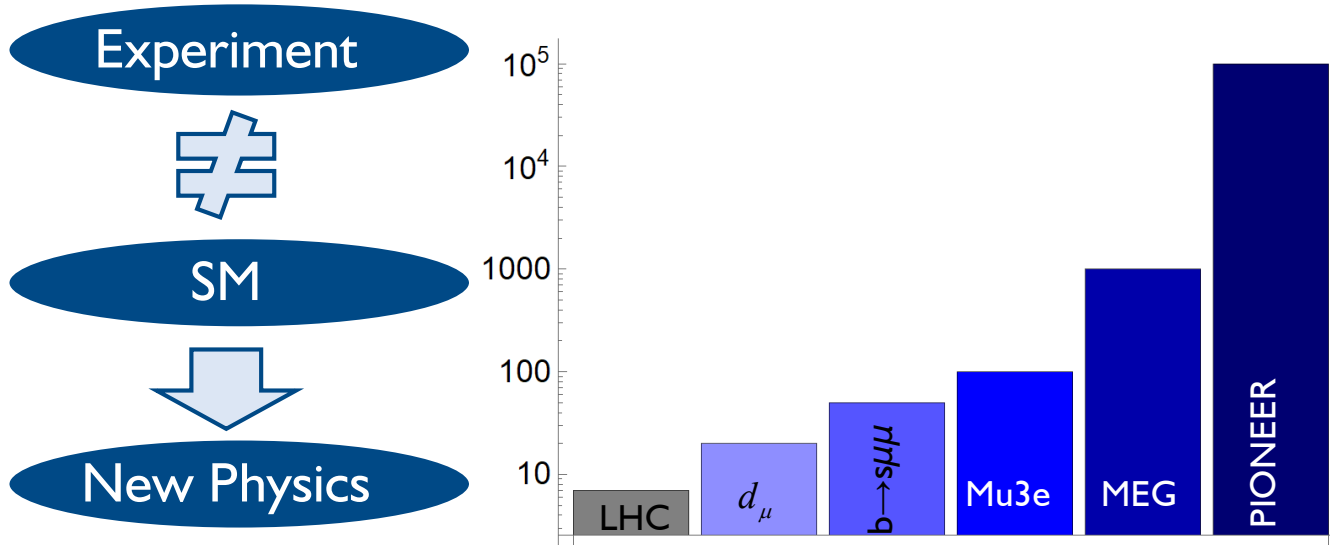
January 24, 2023



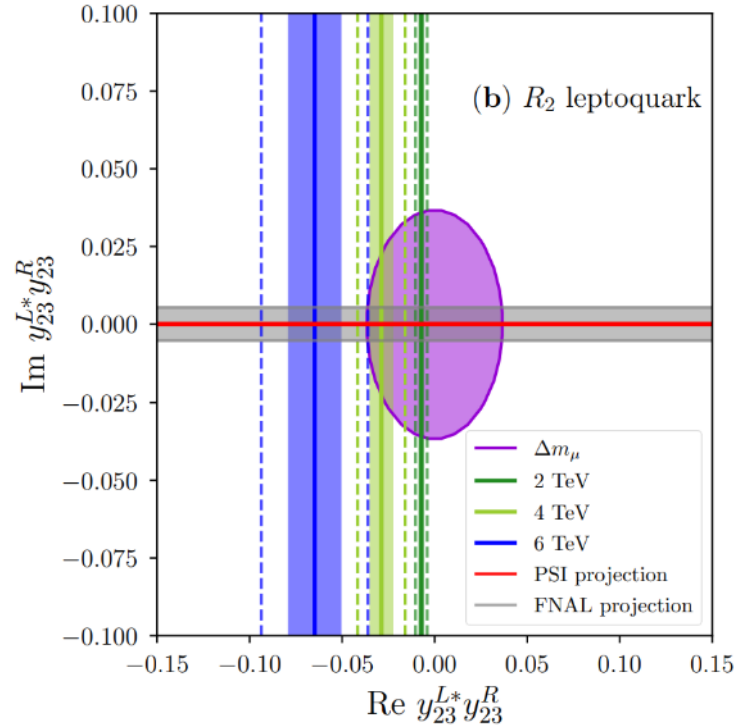
Backup



- At colliders one produces many (up to  $10^{14}$ ) heavy quarks or leptons and measures their decays into light flavors

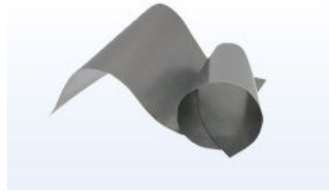


Flavor observables are sensitive to higher energy scales than collider searches

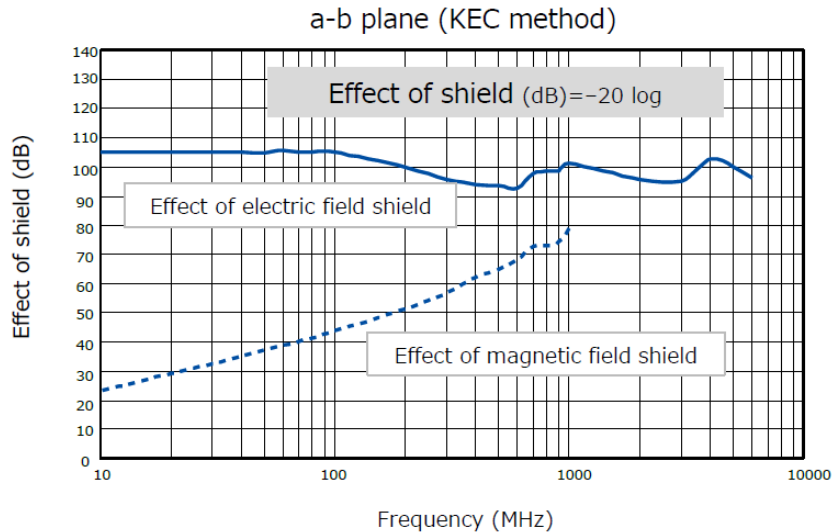


Bigaran, Volkas, 2110.03707

No significant tuning necessary



- Exist off the shelf without substrate down to  $17\mu\text{m}$
- Still considerable damping of magnetic pulse possible
- Tests requires
- Alternative one dimensional wires (carbon fibers / tungsten)







- Characterization of potential electrode material with positrons and muons

$$50 \text{ MeV}/c < p < 145 \text{ MeV}/c$$

$\mu^+, e^+$

