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Mass-radius constraints on the EOS using phase-resolved X-ray observations of neutron stars including prospects for X-ray polarimetry

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- Prospects of X-ray polarimetry to improve EOS constraints

Introduction

- Neutron stars (NS)
 - Properties of the inner core unknown.
 - Aim to constrain the equation of state (EOS).
- (Millisecond) Pulsars
 - X-ray pulses encode information of mass M and radius R.
 - Polarization measurements can be used to get tighter constraints for both NS geometry and EOS



M&R and EoS



Greif+2019

Modeling phase-resolved pulses

PULSE PROFILE MODELING (PPM):PAST



Pechenick et al. 1983, Poutanen & Gierlinski 2003, Viironen & Poutanen 2004, Poutanen & Beloborodov 2006, Morsink et al. 2007, Bogdanov et al.2007, Baubock et al. 2012, 2013, Lo et al. 2013, AlGendy & Morsink 2014, Psaltis et al. 2014, Miller & Lamb 2015

General and special relativistic effects modify the pulse shape

M/R affects the light bending and gravitational redshift.

Effects of relativistic rotation at NS surface depend on R.

Credit: A. Watts

Pulse profile modeling (PPM)

- Oblate-Schwarschild approxmation
- General and special relativistic effects taken separately into account.
 - Spherical non-rotating space time for light bending, time delays...
 - Relativistic Doppler corrections done, assuming no gravity.
- Only small deviation from exact spacetime metric, but fast enough for statistical inference.
- Shape of the star more important (Morsink+2007, AlGendy+2014).



Morsink+2007

PPM: Equation

- Flux depends on:
 - Gravitational redshift $R_{
 m S}/R$
 - Doppler factor $\delta(\phi)$
 - Emitted intensity I'
 - Light bending $\ \alpha(\psi)$
 - Oblate shape $\sigma(\alpha)$
 - Surface area $\,S^\prime\,$
 - Distance D
 - Time delays

$$dF(E) = (1 - R_S/R)^{1/2} \delta^3 I'(E', \sigma')$$
$$\times \cos \sigma' \left| \frac{\partial \cos \alpha}{\partial \cos \psi} \right|_R \frac{dS'}{D^2},$$





Salmi+2018

PPM: Uncertainties



- Possible uncertainties:
 - Hot region shape geometry
 - Atmosphere model $I'(E', \sigma')$
 - Interstellar medium
 - Instrumental properties
 - Background photons (both astrophysical and instrumental)
- X-PSI code (Riley 2021)



Riley+2019

Millisecond pulsars (MP)

- Fast rotation of MPs: Pulse shape sensitive to R and not only M/R.
- Emission powered in 3 ways:
 - Rotation (RMP)
 - Accretion (AMP)
 - Thermo-nuclear (TMP)



Rotation-powered millisecond pulsars (RMPs)



- Primary NICER targets.
- Recycled pulsars with no accretion
- Magnetospheric return-current heats the polar caps.
- Well established atmosphere models (still composition, deep-heating, etc assumptions).
- Faint but stable: Very long exposure time possible.



RMPs: J0030 results



Miller+2019

Riley+2019

RMPs: J0030 results



RMPs: J0030 caveats

- J0030 assumptions:
 - Fully ionized non-magnetic deep-heated Hydrogen atmosphere.
 - Unconstrained background.
- Coming J0030 updates (Vinciguerra+, in prep.):
 - Updated instrument calibration.
 - Background constraints.
 - New data.



Miller+2019

RMPs: Background

- Pulsed component:
 - Only hot spots
- Unpulsed component:
 - Hot spots (for high compactness or certain geometries)
 - Anything else: Background
- Background sources: Instrumental particles, cosmic X-ray background, other sources in the field of view.



Wolff+2021

RMPs: J0740 results

Background constrained using XMM



RMPs: New J0740 analysis

- J0740 with NICER background estimates instead of XMM.
- New NICER background estimates directly used to limit background.
- More cleaned 3C50 data set (Remillard+2022) used to quantify the uncertainty in background.



Salmi+2022, submitted

RMPs: New J0740 analysis

- J0740 Radius intervals for different background prior choices.
- XX = No lower limit, no upper limit
- 33 = 3 σ lower limit, 3 σ upper limit
- Riley+2021 NICER-only: $R = 11.29^{+1.20}_{-0.81}$ km
- Riley+2021 NICER+XMM ("compressed scaling"): $R = 12.70^{+1.25}_{-0.96}$ km
- Salmi+2022 NICER-3C50-3X:

 $R = 12.97^{+1.56}_{-1.39} \text{ km}$

• Setting upper limit for background non-trivial since the AGN in the FoV not accounted in the estimate.



RMPs: New J0740 analysis

Conclusions:

- Inferred compactness affected by constraining background.
- Consistent results with NICER+XMM.
- No EOS re-analysis needed for J0740.
- New data for J0740 being analyzed.



Salmi+2022, submitted

Accretion-powered millisecond pulsars (AMPs)

- Gas from a companion forms an accretion disk and channels to the magnetic poles.
- AMPs are bright and rotate very rapidly.
- Downside:
 - Detected only during outbursts (duration ~weeks).
- Radiation polarized due to Compton scattering in the accretion column
 - \rightarrow Observed in harder X-rays.



Gierliński+2002

AMPs: Additional effects

- Other complications compared to RMPs:
 - Accretion shock?
 - Accretion column?
 - Accretion disc?
 - Atmosphere model?
 - Time variability?



AMPs: Efforts so far

- Simplified emission models (Salmi+2018, Leahy+2008 Poutanen & Gierlinski 2003)
- RXTE, Nicer, eXTP, Strobe-X





Thermo-nuclear powered millisecond pulsars (TMPs)

- Thermonuclear burning of accreted matter (X-ray bursts).
- Seen burst oscillations some times: Origin not sure.
- Very bright but short (seconds).
- Burst atmosphere models exist, but not sure if they are consistent with burst pulsations (Suleimanov+2012, Suleimanov+2018).
- Likely variable of spot properties (temperature, spot size, location).



Spitkovsky, Levin & Ushomirsky

TMPs: Future

 Prospects for current and future instruments with TMPs.



Watts 2019

Prospects for polarimetry

- Polarimetry can be used to constrain hot spot geometry, linked to M and R.
- Polarization angle (PA) dependence on geometry helpful to break degeneracy.
- Detectable polarization expected from AMPs.
 - RMPs too weakly polarized?
 - TMPs too short duration?



Viironen & Poutanen 2004

Polarimetry: Radiation transport

- Polarized Oblate-Schwarschild approxmation (Loktev+2020)
- PA transport from spot to observer accounting for relativistic and oblateness effects.

•
$$\chi_{\text{obl}} = \chi_0 + \chi_1 + \chi'$$

• Stokes parameters integrated over surface area

•
$$\begin{pmatrix} dF_{I} \\ dF_{Q} \\ dF_{U} \end{pmatrix} = dF_{I} \begin{pmatrix} 1 \\ P\cos 2\chi \\ P\sin 2\chi \end{pmatrix}$$



$$\cos 2\chi^{\text{tot}} = \frac{F_{\text{Q}}^{\text{tot}}}{F_{\text{I}}^{\text{tot}}}, \quad \sin 2\chi^{\text{tot}} = \frac{F_{\text{U}}^{\text{tot}}}{F_{\text{I}}^{\text{tot}}}.$$

Polarimetry: Simple PA fitting



Oblate fit to oblate PA profile with 2 deg PA uncertainty

Spherical fit to oblate PA profile with 2 deg PA uncertainty

Polarimetry: Emission models

 Model for escaping radiation in the hot spot frame:

 $I(E,\mu)$ and $Q(E,\mu), \ \mu = \cos \sigma$

- Thomson slab model (Salmi+2021, Viironen & Poutanen 2004, Sunyaev & Titarchuk 1985)
- Compton slab model (Bobrikova et al., In prep., Poutanen & Svensson 1996)
- Thermal seed photons get polarized, change energies (for Compton case) and emission angles, due to scatterings with electrons.
- Scattering layer close to the surface for AMP luminosity.



Trippe 2014

Polarimetry: Compton slab model

- Isothermal hot slab on top of thermal seed photons.
- Polarized radiative transfer with exact Compton redistribution matrix.
- Faster than full self-consistent accretion-heated atmosphere model (Suleimanov+2018).
- Produces AMP spectra consistent with observations.





Polarimetry: Compton slab model

- A pre-computed grid produced to be used for upcoming analyses (Bobrikova+, in prep.)
- T_bb [0.5 1.5 keV]
- T_e [30 100 keV]
- τ [0.5 3.5]
- μ = 0.0, 0.2, 0.4, 0.6, 0.8, 1.0



Polarimetry: Instruments

IXPE

- Launched in 2021 Dec.
- No AMPs observed yet.
- ~10 sources waiting for starting an ouburst.
- eXTP
 - Launch in 2027?
 - Larger effective area.
 - More possible candidates and shorter exposure times required.





Polarimetry: Simulations

 Predictions for the inferred credible intervals for geometry model parameters* based on simulated IXPE data and Stokes parameter fitting.

* Spot colatitude and observer inclination.



Salmi+2021

Polarimetry: Simulations

- Magnetic field configuration can be constrained as well when the other spot not hidden behind the accretion disk.
- Constraining the shapes of the spots to be studied.

Salmi+2021



Polarimetry: Effect on M&R



Salmi+2018 detected a few % improvement even when geometry already limited due to radio observations.

Conclusions and Future

- More new and old M&R constraints coming from modeling RMPs with NICER.
 - Nicer+XMM J0740 results consistent with Nicer-only, if using new Nicer background estimates.
- Fast rotating AMPs and TMPs are promising targets to further constrain M&R, especially with future instruments.
 - New models for emission developed.
- Polarimetry helps to constrain parameter degeneracies in PPM, and enables tighter constraints on M&R.