

INT 2025 DISCUSSIONS

Higher order fluctuations

OBSERVABLES:

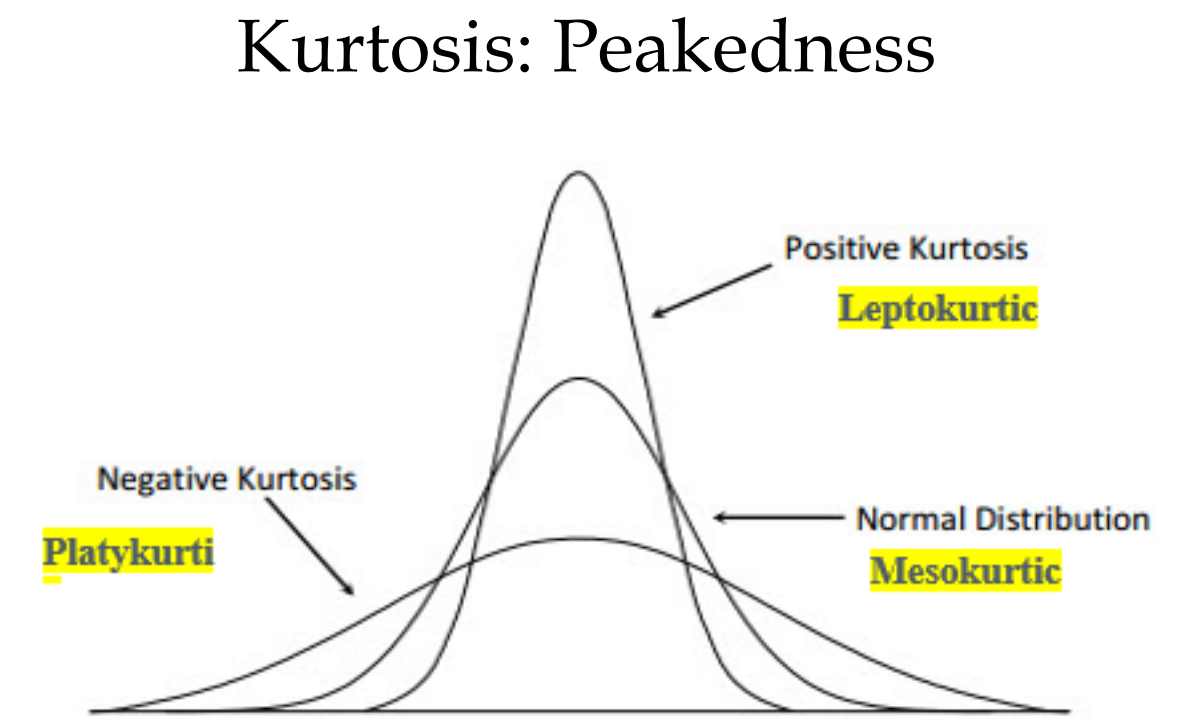
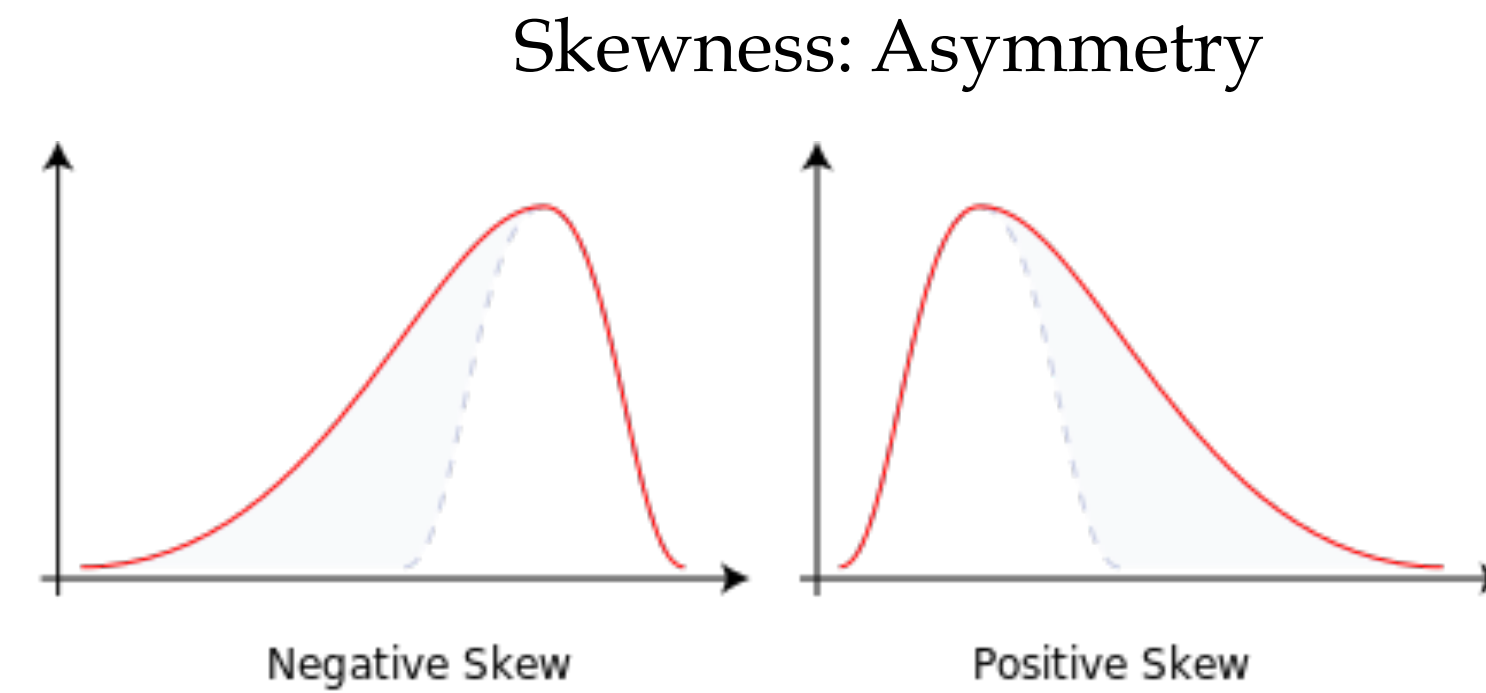
●Cumulants: $n = \text{net-proton/proton multiplicity in an event}$

$$C_1 = \langle n \rangle \quad * \delta n = n - \langle n \rangle$$

$$C_2 = \langle \delta n^2 \rangle$$

$$C_3 = \langle \delta n^3 \rangle$$

$$C_4 = \langle \delta n^4 \rangle - 3 \langle \delta n^2 \rangle$$



●Factorial cumulants (irreducible correlation function):

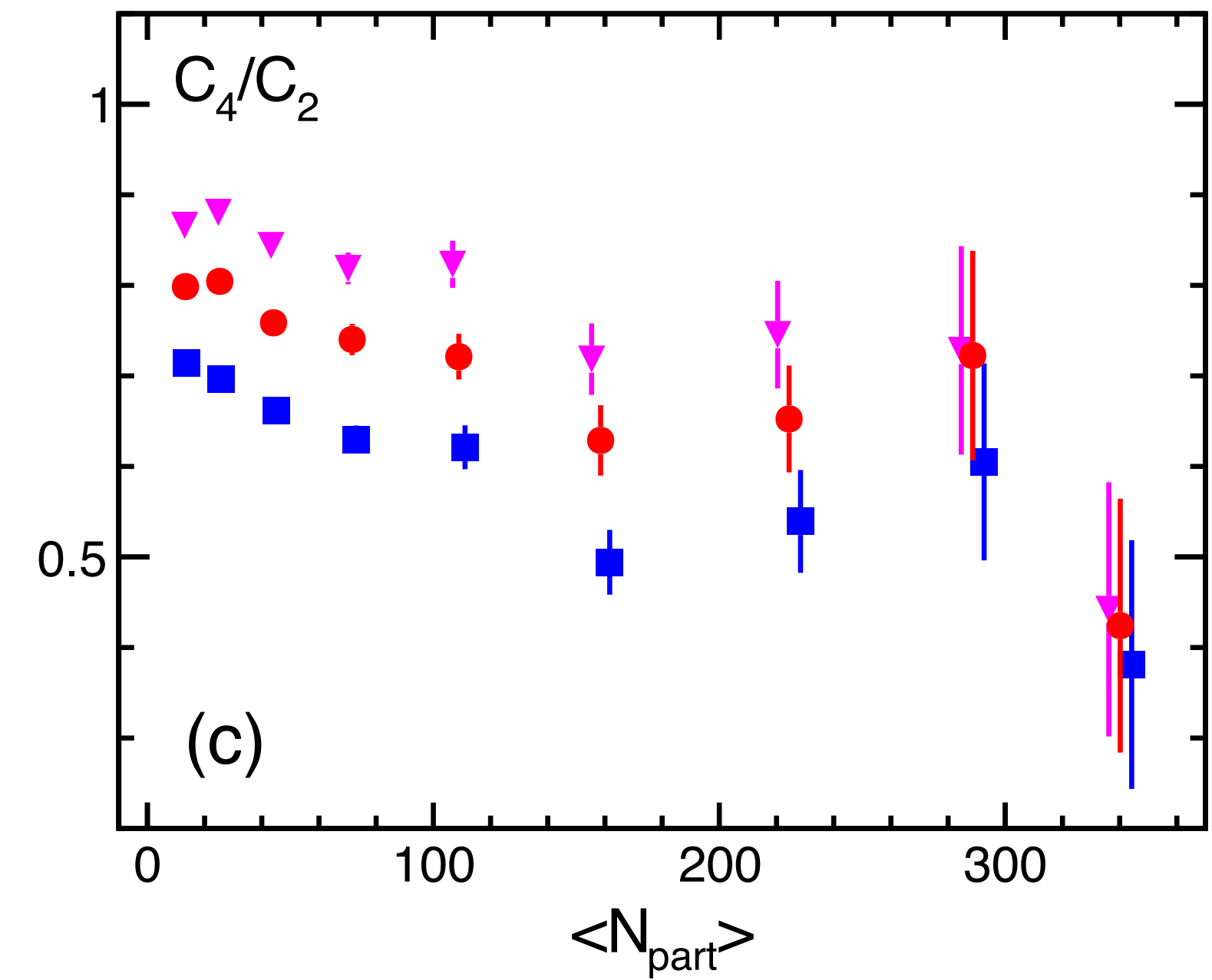
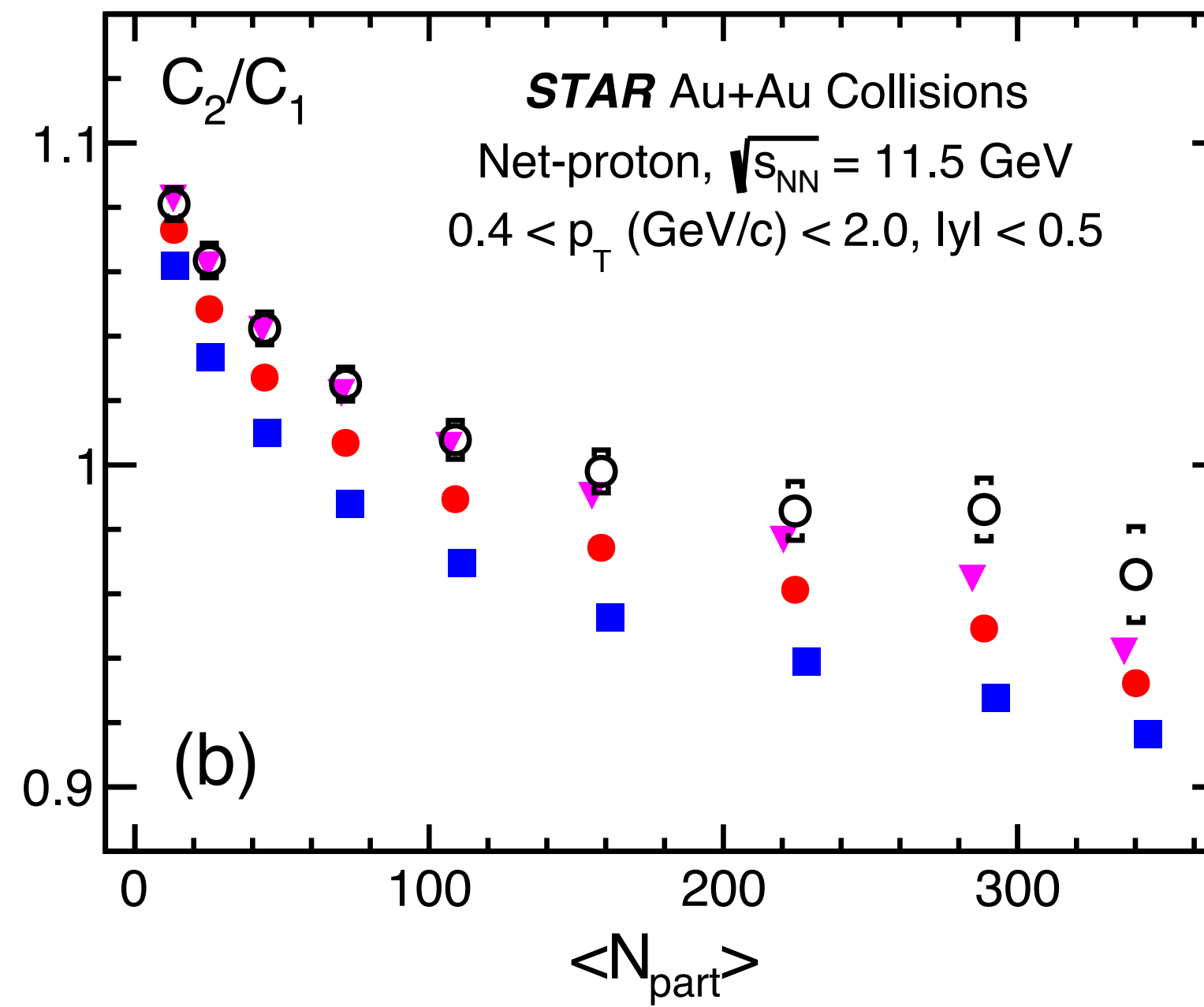
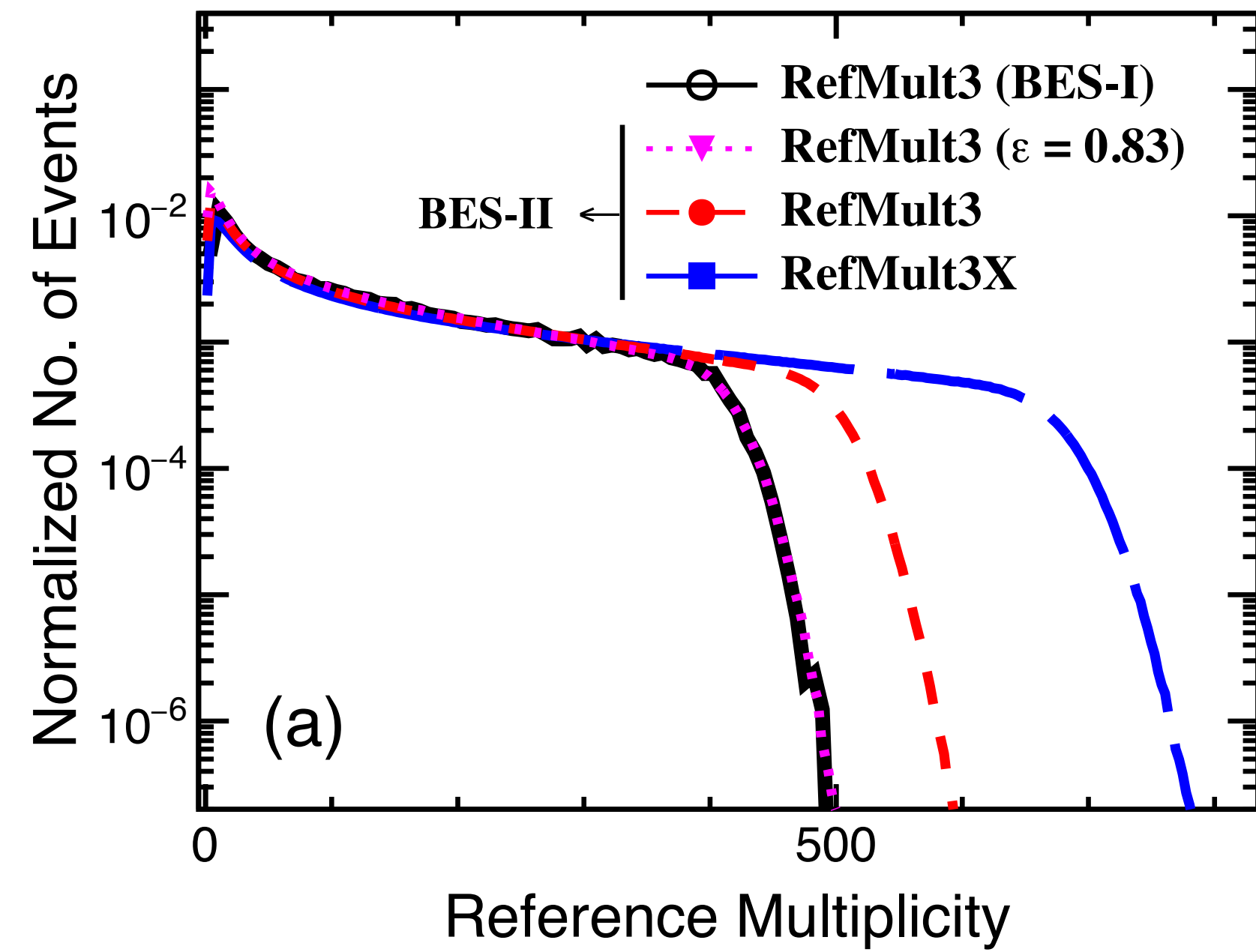
$$\kappa_1 = C_1$$

$$\kappa_2 = -C_1 + C_2$$

$$\kappa_3 = 2C_1 - 3C_2 + C_3$$

$$\kappa_4 = -6C_1 + 11C_2 - 6C_3 + C_4$$

EFFECT OF CENTRALITY RESOLUTION:



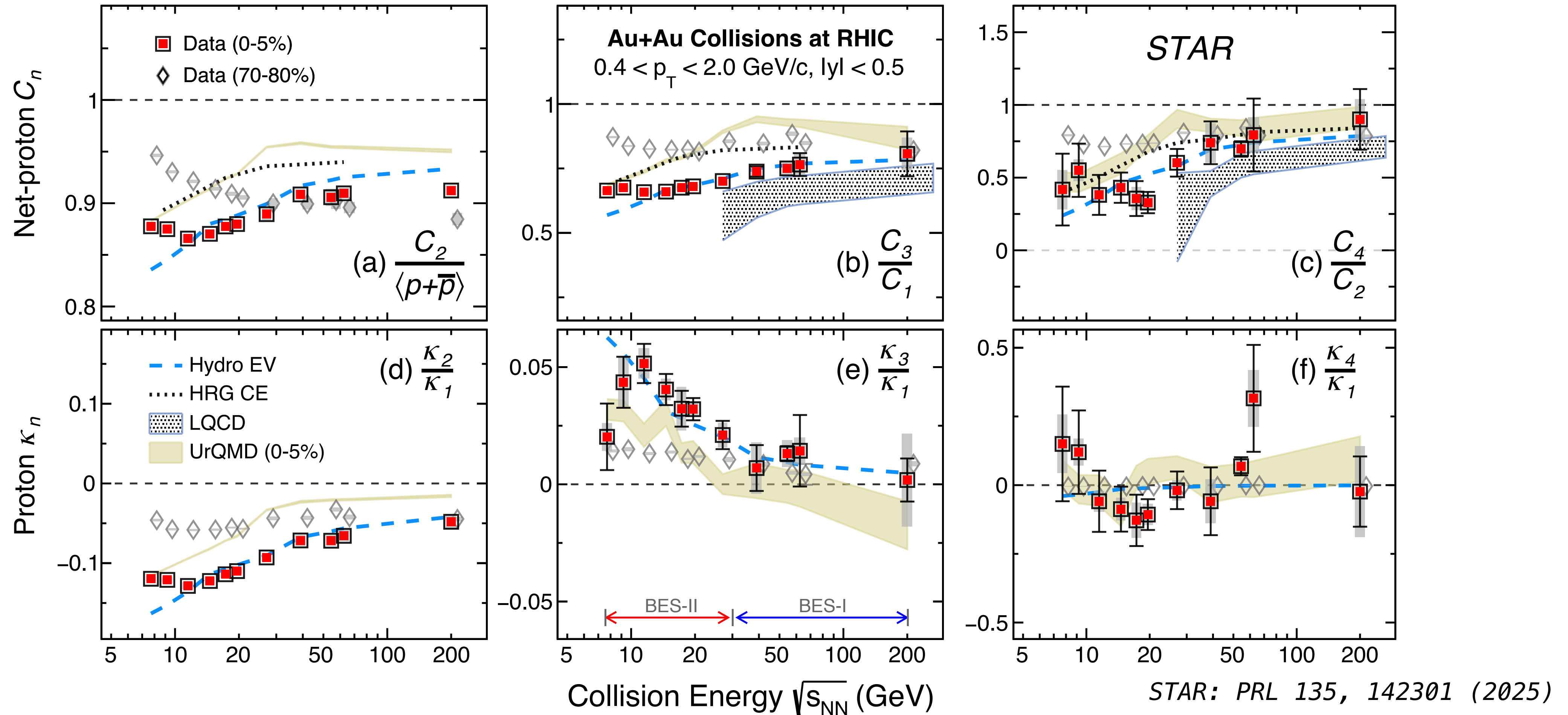
Higher centrality resolution lead to lowering of cumulant ratios:
 Cumulant ratios: RefMult3X (BES-II) < RefMult3 (BES-II) < RefMult3 (BES-I)
 Effect saturates with improved centrality resolution.

STAR: PRL 135, 142301 (2025)

Constraining BES-II centrality to have same resolution as BES-I (using an efficiency factor $\epsilon = 0.83$), the BES-II results are in agreement with BES-I.

C_4/C_2 0-5% are consistent irrespective of different centrality resolution: least affected by resolution.

ENERGY DEPENDENCE OF PROTON FLUCTUATIONS



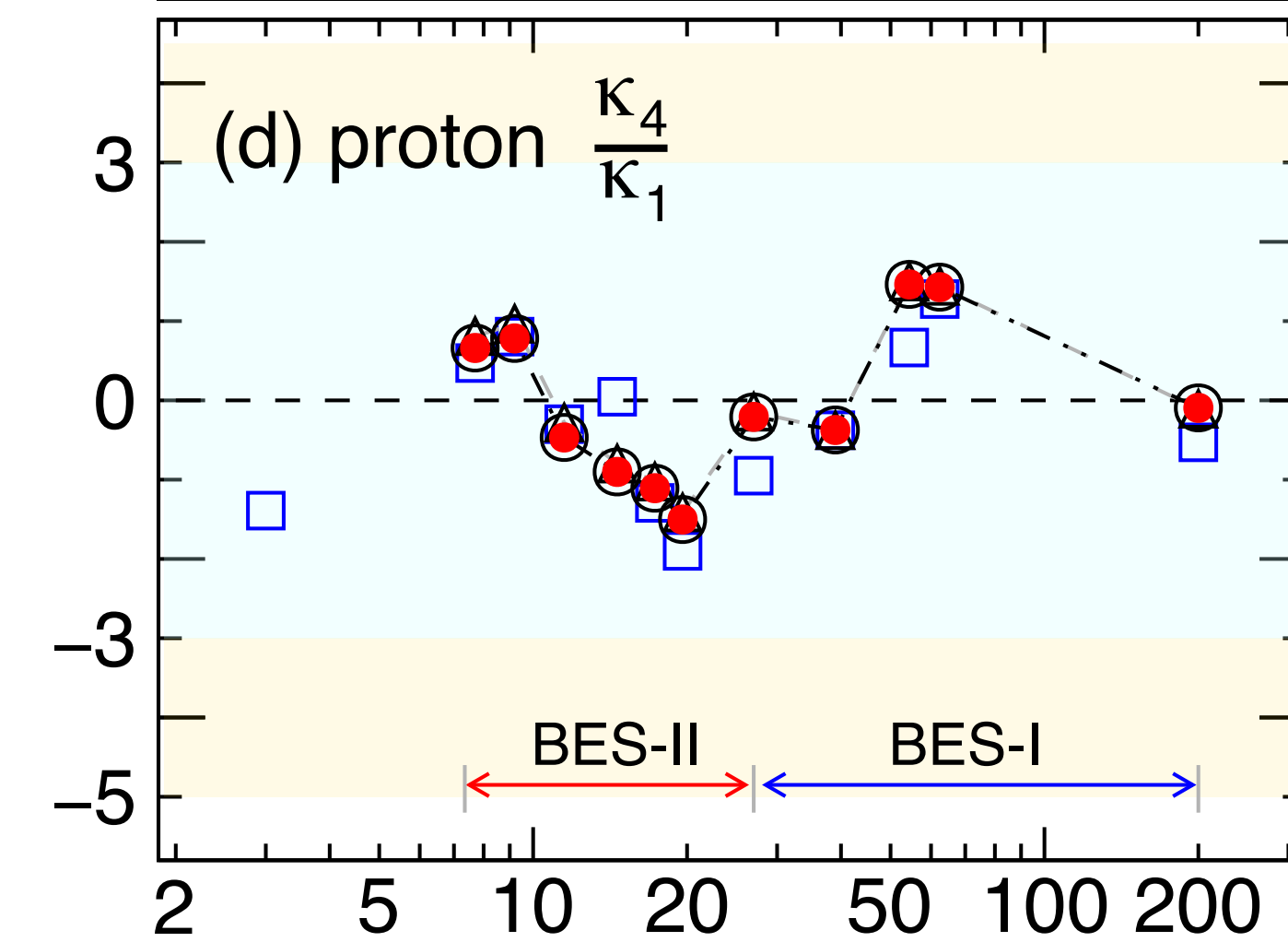
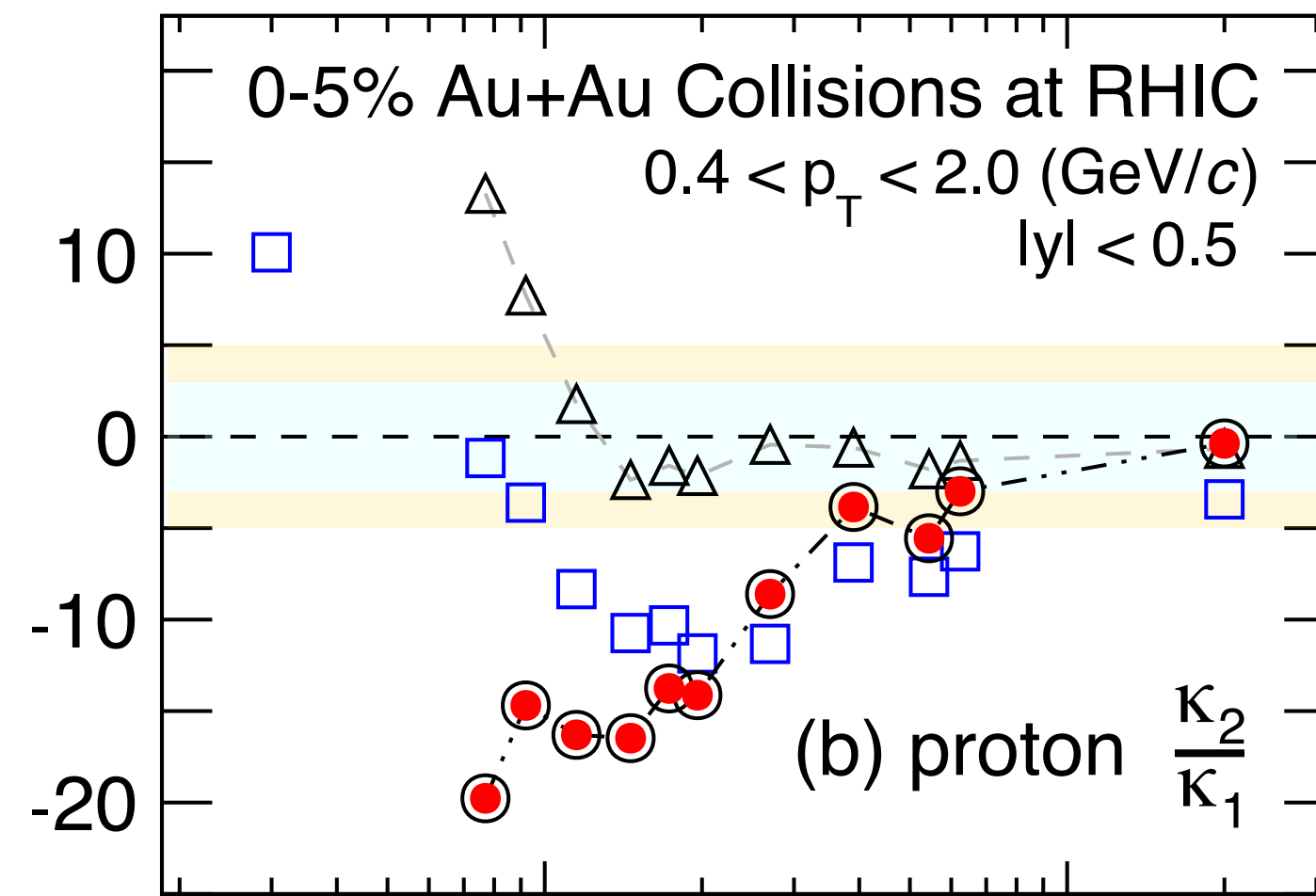
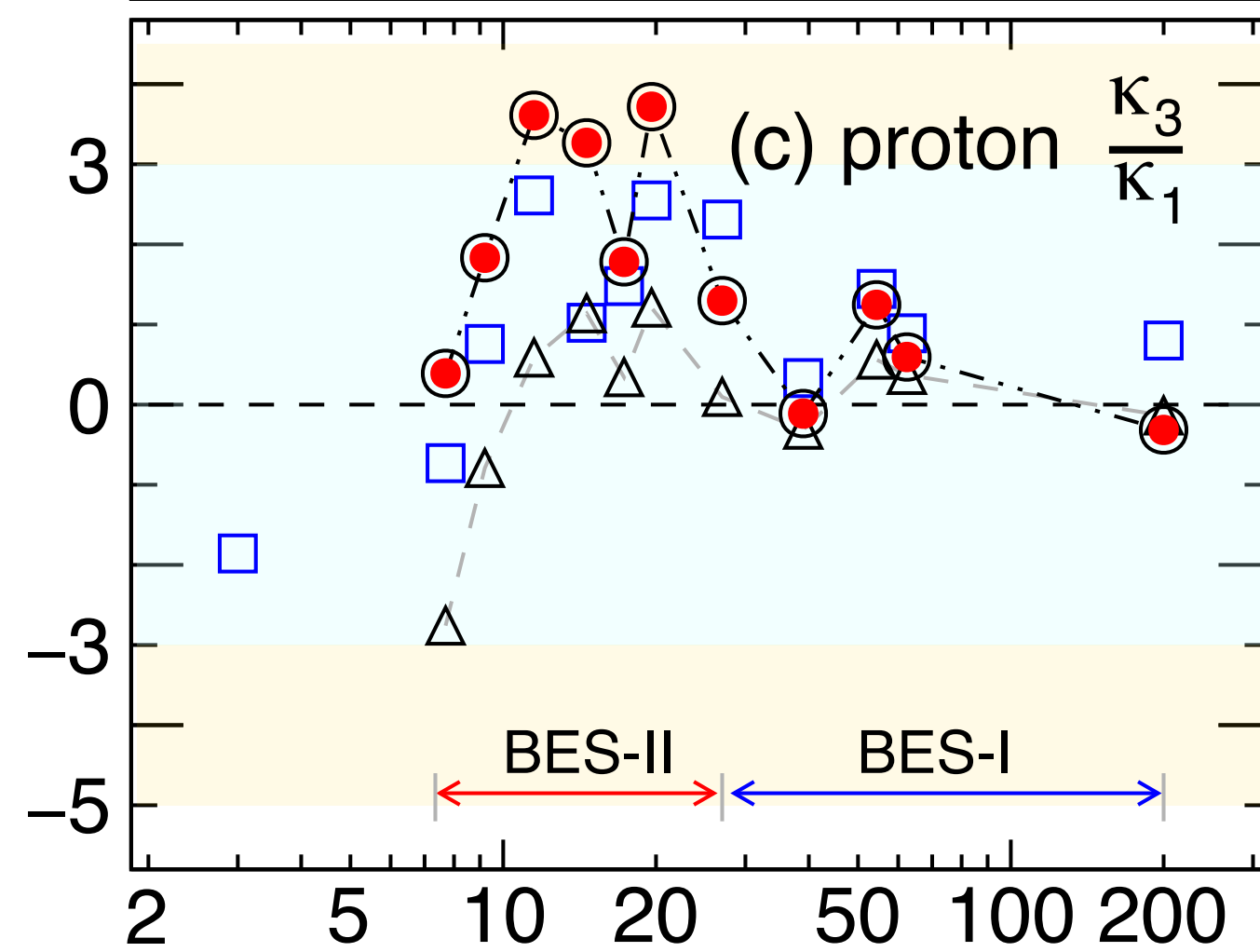
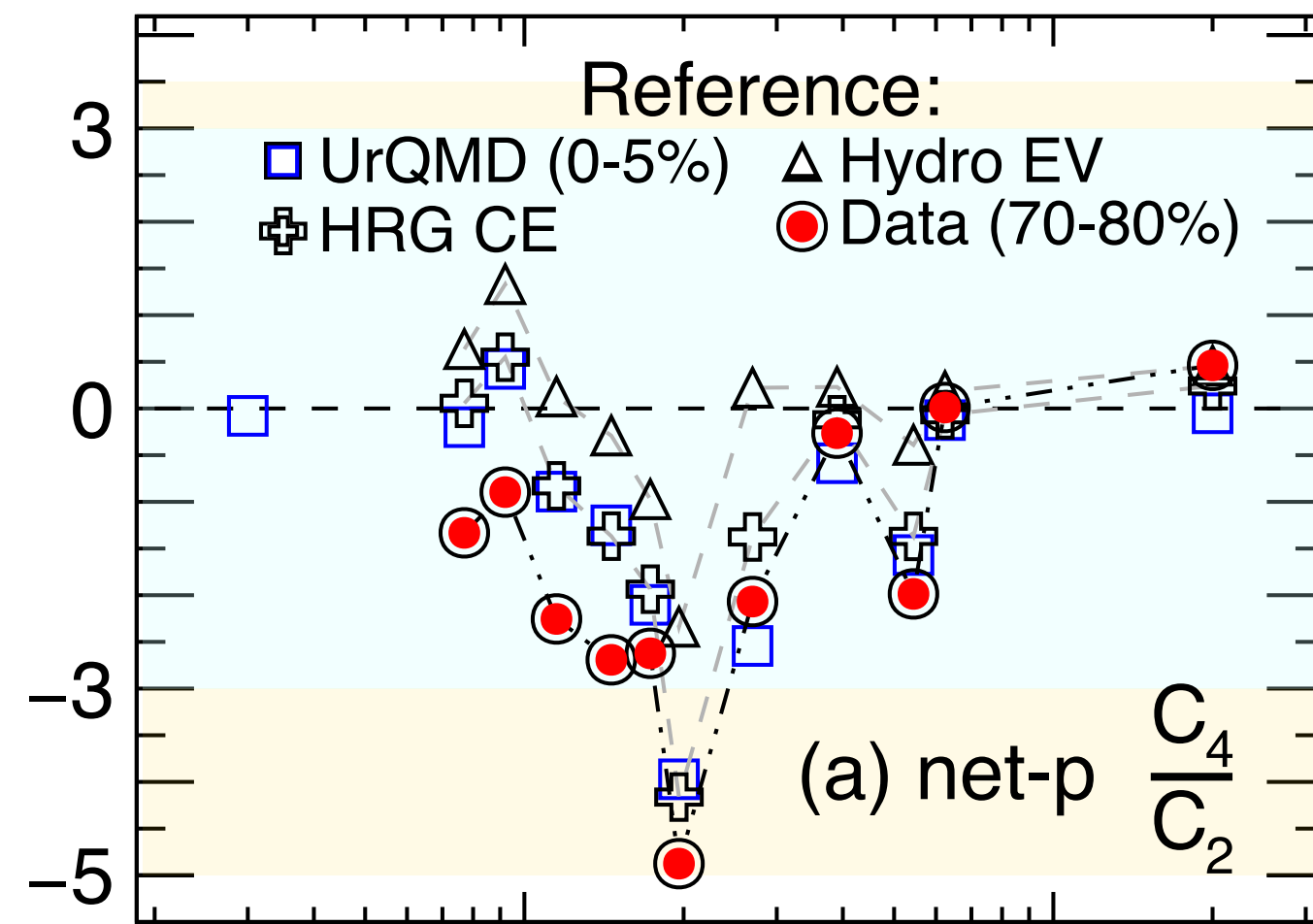
Deviation between data and non-CP models seen in low collisions energies.

- Change of trends in $C_2/\langle p + \bar{p} \rangle$ and κ_2/κ_1 around $\sqrt{s_{NN}} \sim 10$ GeV. An opposite trend seen for κ_3/κ_1 .
- A dip in C_4/C_2 (0-5%) at ~ 20 GeV compared to models.

All non-CP models (HRG, UrQMD, Hydro) are monotonic, do not capture the full energy dependence trends.

DEVIATIONS FROM NON-CP BASELINES

Significance of Deviations



Collision Energy $\sqrt{s_{NN}}$ (GeV)

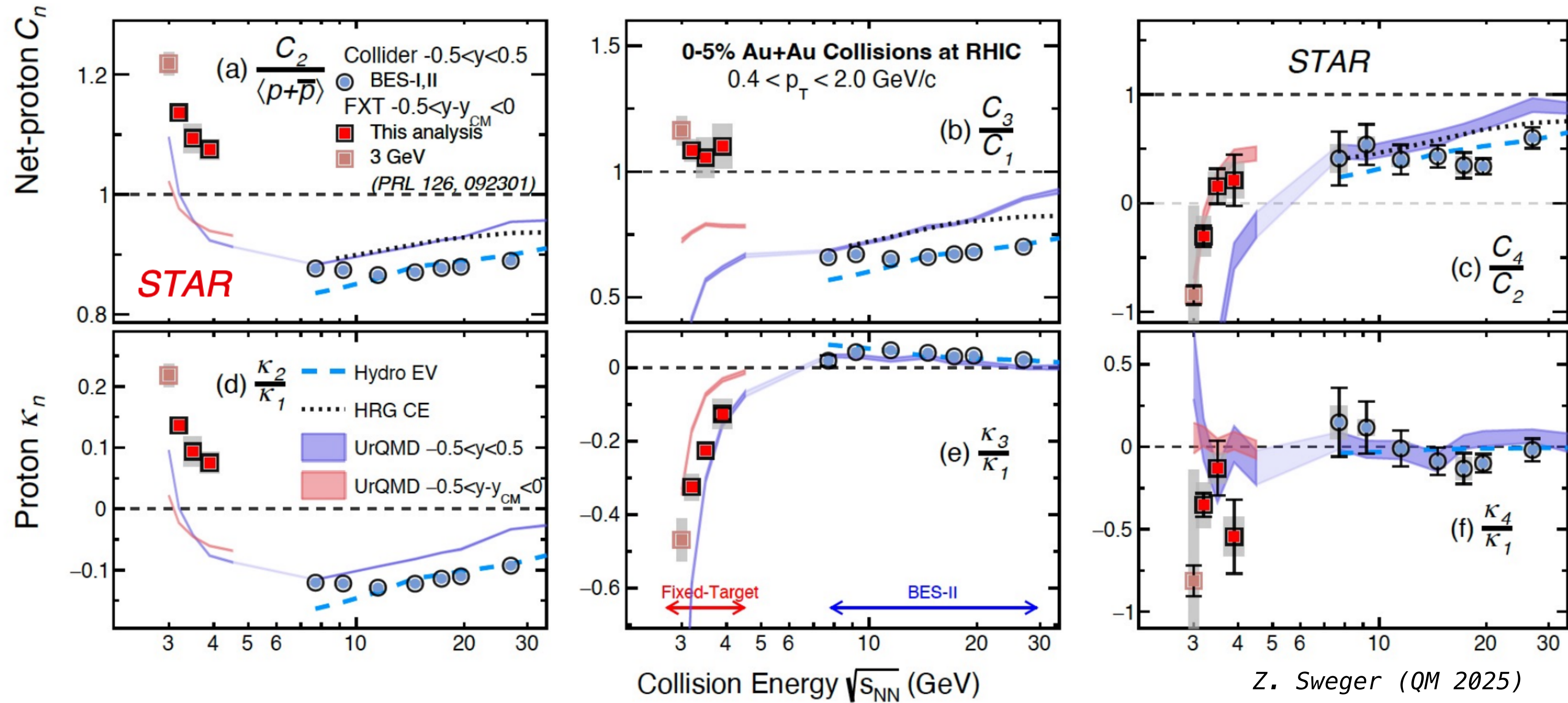
Minimum in C_4/C_2 w.r.t. non-CP models at $2-5\sigma$ level ~ 20 GeV - aligns with the feature of the proposed CP signal.

Similar trend seen in κ_4/κ_1 , albeit within uncertainties.

Deviation also seen for other lower order ratios around similar collision energy range.

Dynamic models with a CP necessary for quantitative assessment of data.

ENERGY DEPENDENCE OF PROTON FLUCTUATIONS: FXT



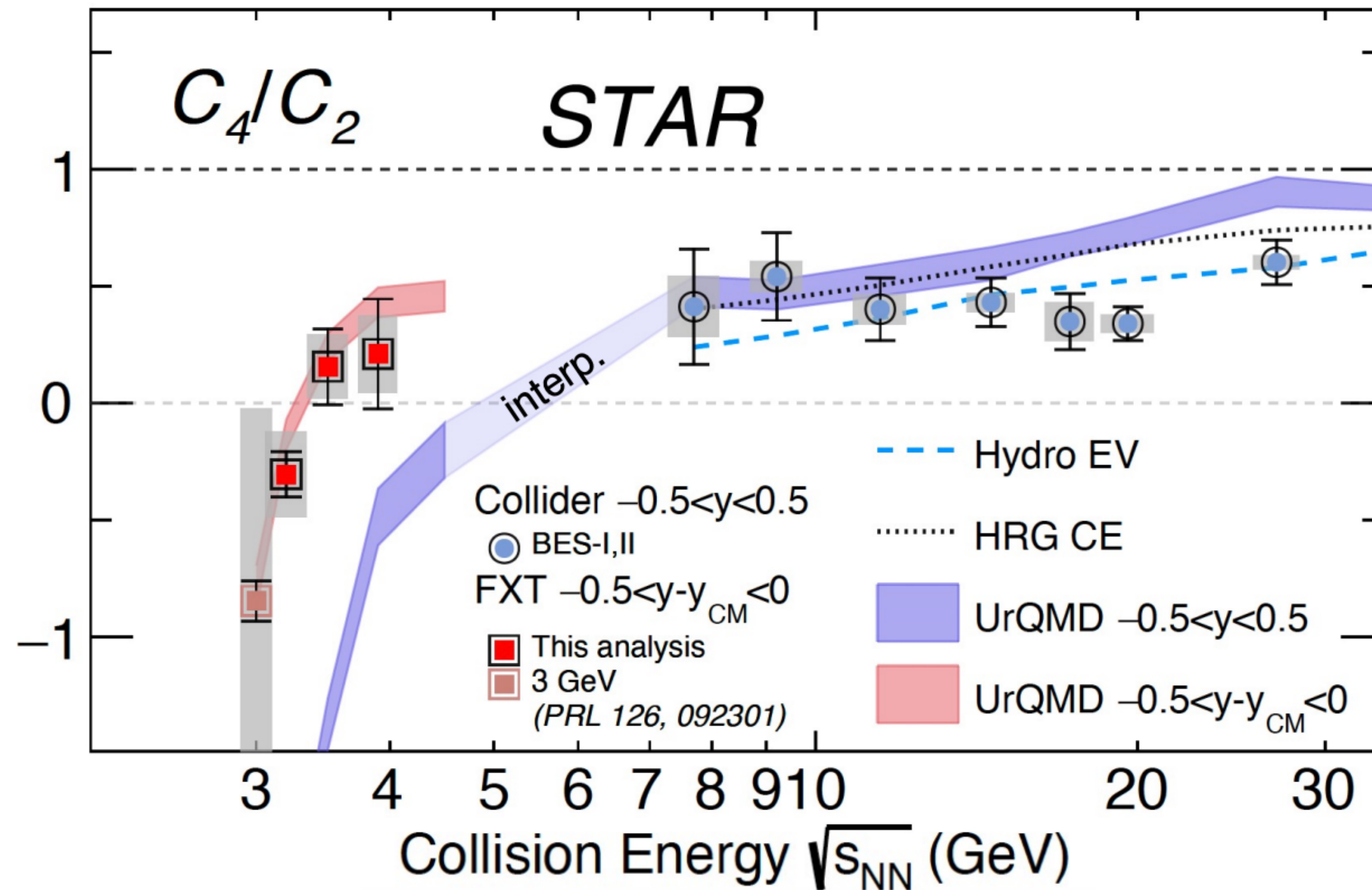
Energy dependence: STAR FXT results at $\sqrt{s_{NN}} = 3.2, 3.5, 3.9$ GeV

Change in trends in lower order ratios

Kurtosis consistent with hadronic baseline UrQMD

DATA FROM STAR FXT COLLISIONS: C4/C2

0-5% Au+Au Collisions at RHIC



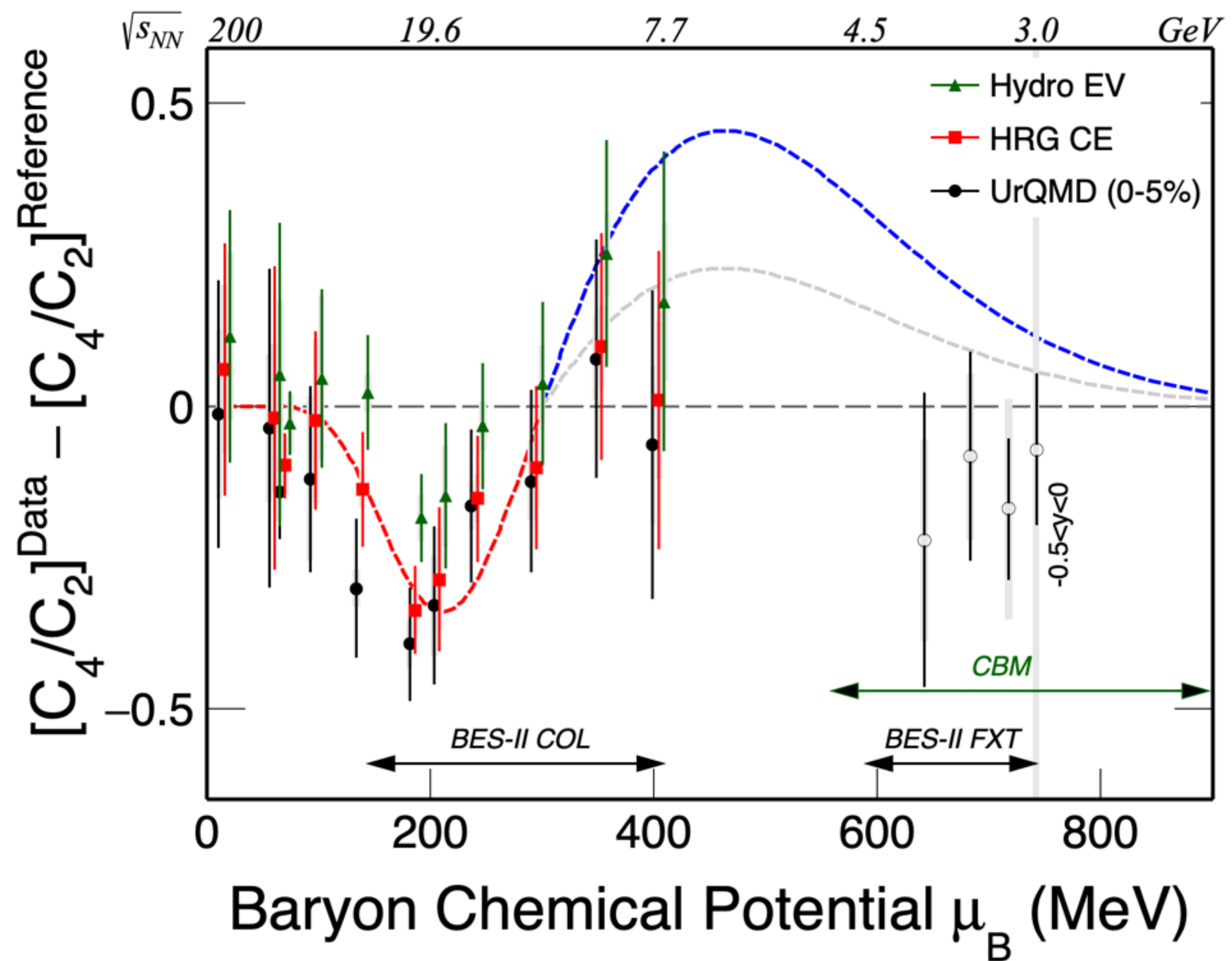
Search for a maximum in data relative to non-CP baseline at $\sqrt{s_{NN}} < 7$ GeV.

STAR FXT results at $\sqrt{s_{NN}} = 3.2, 3.5, 3.9$ GeV consistent with hadronic baseline UrQMD

Analysis at $\sqrt{s_{NN}} = 4.5$ ongoing.

Z. Sweger (STAR): QM25 talk

DEVIATIONS FROM NON-CP BASELINES: C4/C2

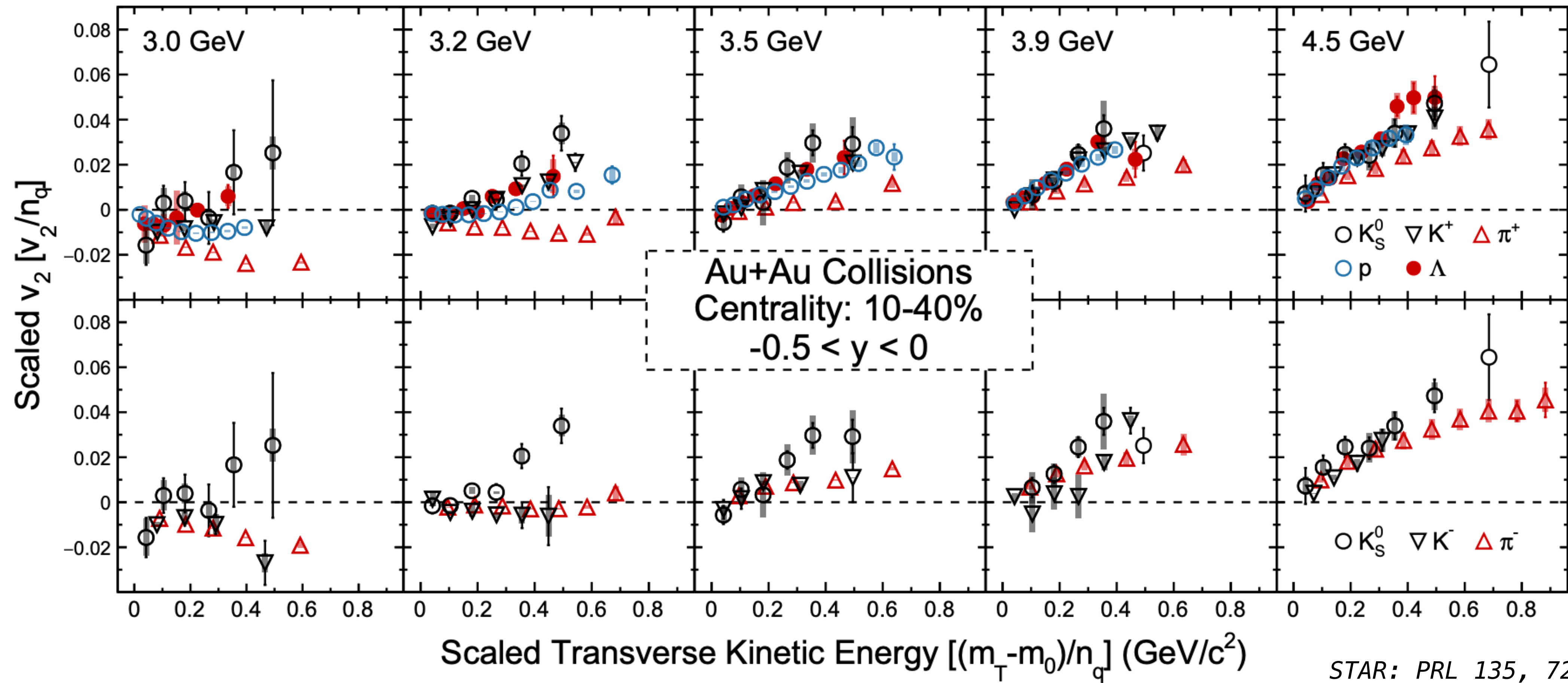


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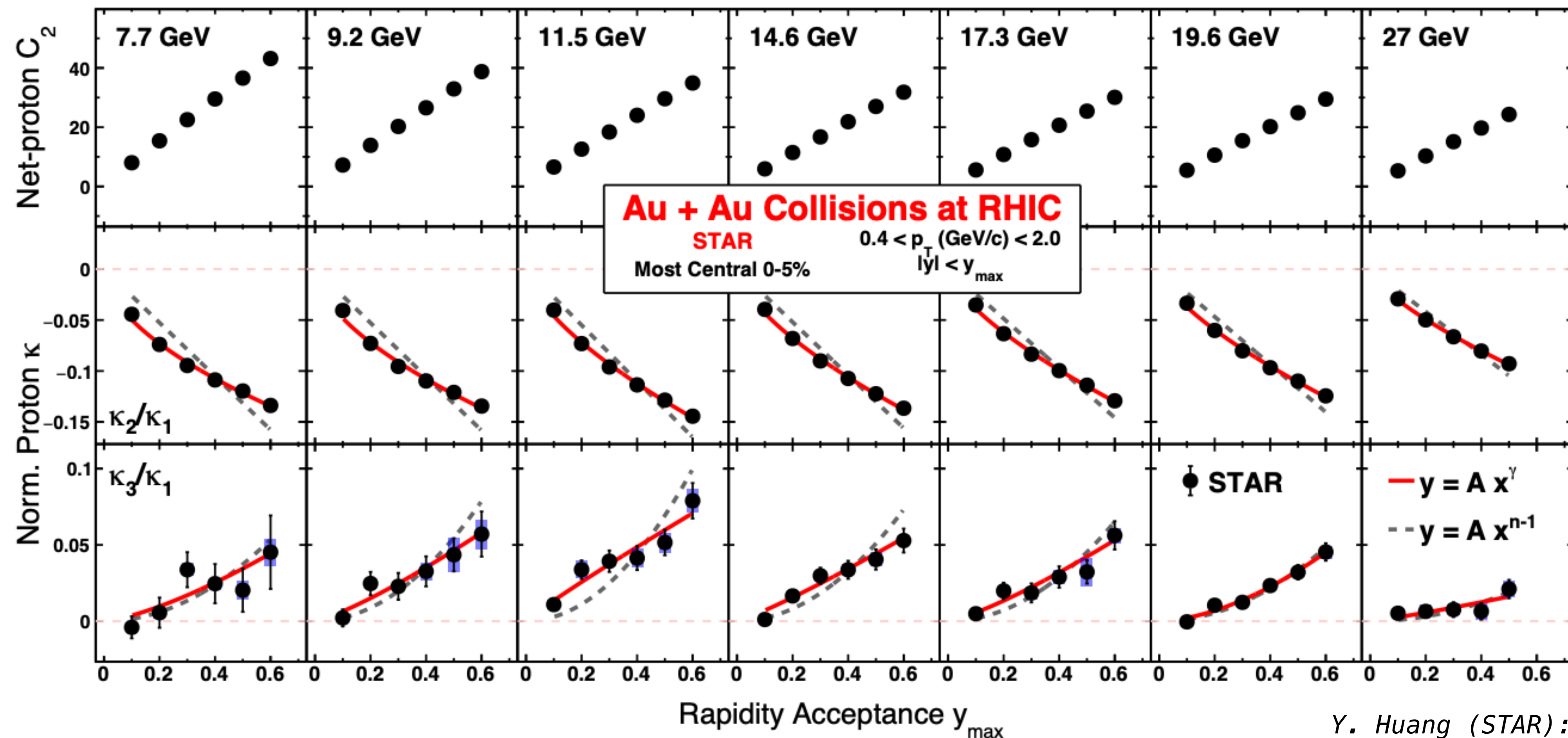
Analysis at $\sqrt{s_{NN}} = 4.5$ ongoing.

ONSET OF DECONFINEMENT:



v_2 measurements at FXT energies indicates restoration of ncq scaling at $\sqrt{s_{NN}} \sim 4.5$ GeV - possible formation of QGP.

RAPIDITY DEPENDENCE:



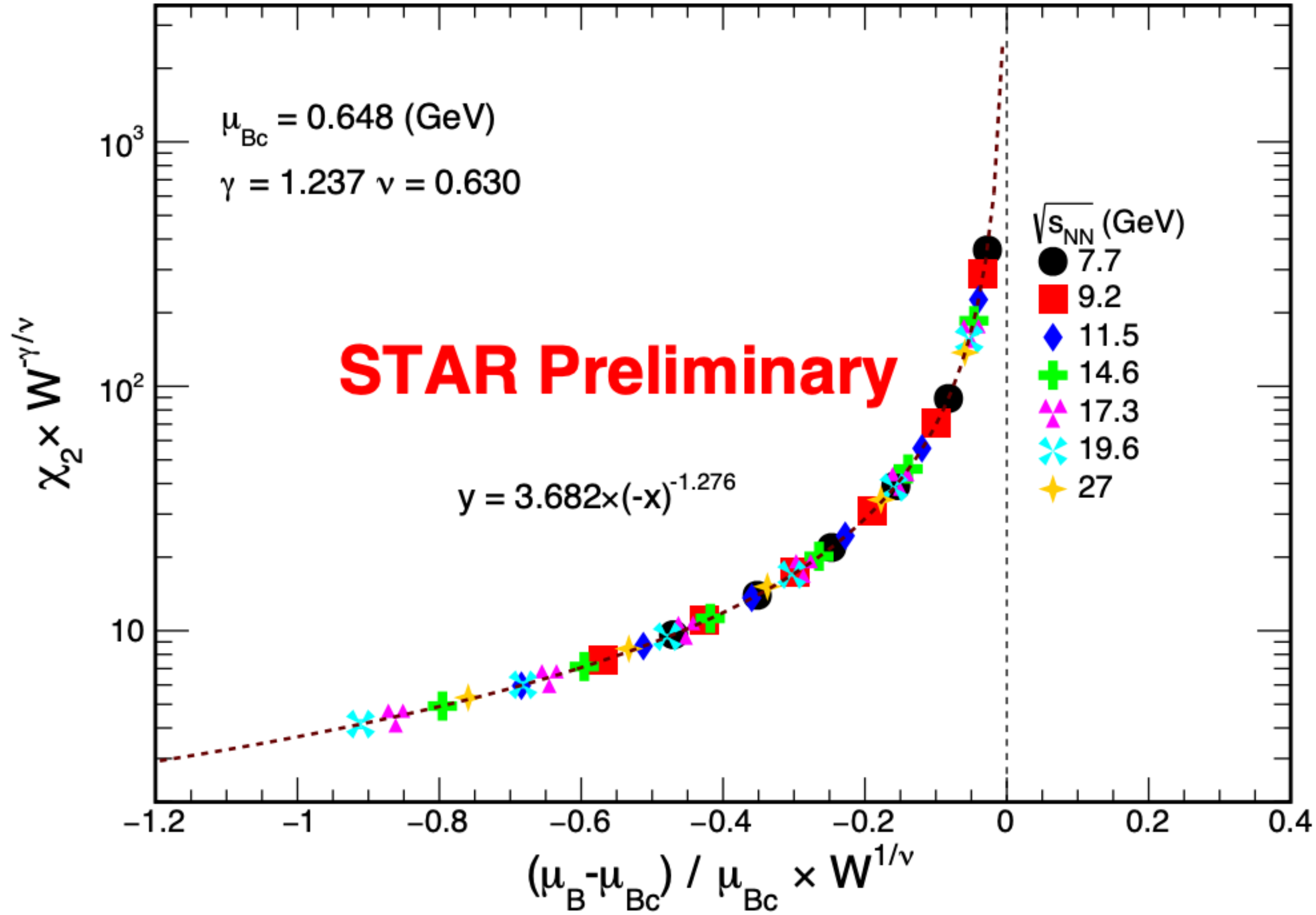
Rapidity dependence studies at collider energies yield smaller exponents than power law trend $\kappa_n/\kappa_1 \sim (\Delta y)^{n-1}$ expected for long-range correlation, such as a CP. *B. Ling, M. Stephanov Phys. Rev. C 93, 034915*

Finite size scaling studies done with 2nd-order cumulant data (as done by Sorensens), yield a critical region of $\mu_B \sim 550\text{-}650 \text{ MeV}$ ($\sim \sqrt{s_{NN}} = 4.5 \text{ GeV}$). *A.Sorensen and P.Sorensen: arXiv:2405.10278*

SUMMARY:

- Precision measurements of proton and net-proton fluctuations from $\sqrt{s_{NN}} = 3 - 27$ GeV (BES-II). Large improvements seen in centrality resolution; PID; rapidity coverage; higher statistics.
- C4/C2 data shows show a minimum in energy dependence at 19.6 GeV compared to all considered non-CP references, especially with the peripheral data and UrQMD calculations.
- FXT data is being analyzed with a new method to suppress volume fluctuations.
- STAR has made a request to PAC for new data taking at $\sqrt{s_{NN}} = 4.2$ and 4.5 GeV, as it is necessary to realize the full potential of STAR FXT program.

BACKUP:



- 1) Susceptibility: $\chi_2(W, \mu_{fo}) = \frac{C_2(W, \mu_{fo})}{T_{fo}^3 W dV_{fo}/dy}$
- 2) Binder cumulant: $U_4 = -3C_4/C_2^2$
- 3) Rapidity window size: W
- 4) Freeze out parameters^{[1][2]}: $T, \mu, dV/dy$
- 5) Critical exponents^[3]: γ, ν
- 6) Uncertainty: $\sigma = \sqrt{\sigma_{\text{stat.}}^2 + \sigma_{\text{sys.}}^2}$

A.Sorensen and P.Sorensen: arXiv:2405.10278