

Current neutron star constraints and non-trivial features in the EoS

to appear soon with J. Noronha-Hostler (ICASU/UIUC), N. Yunes (ICASU/UIUC), M. C. Miller (U. Maryland)

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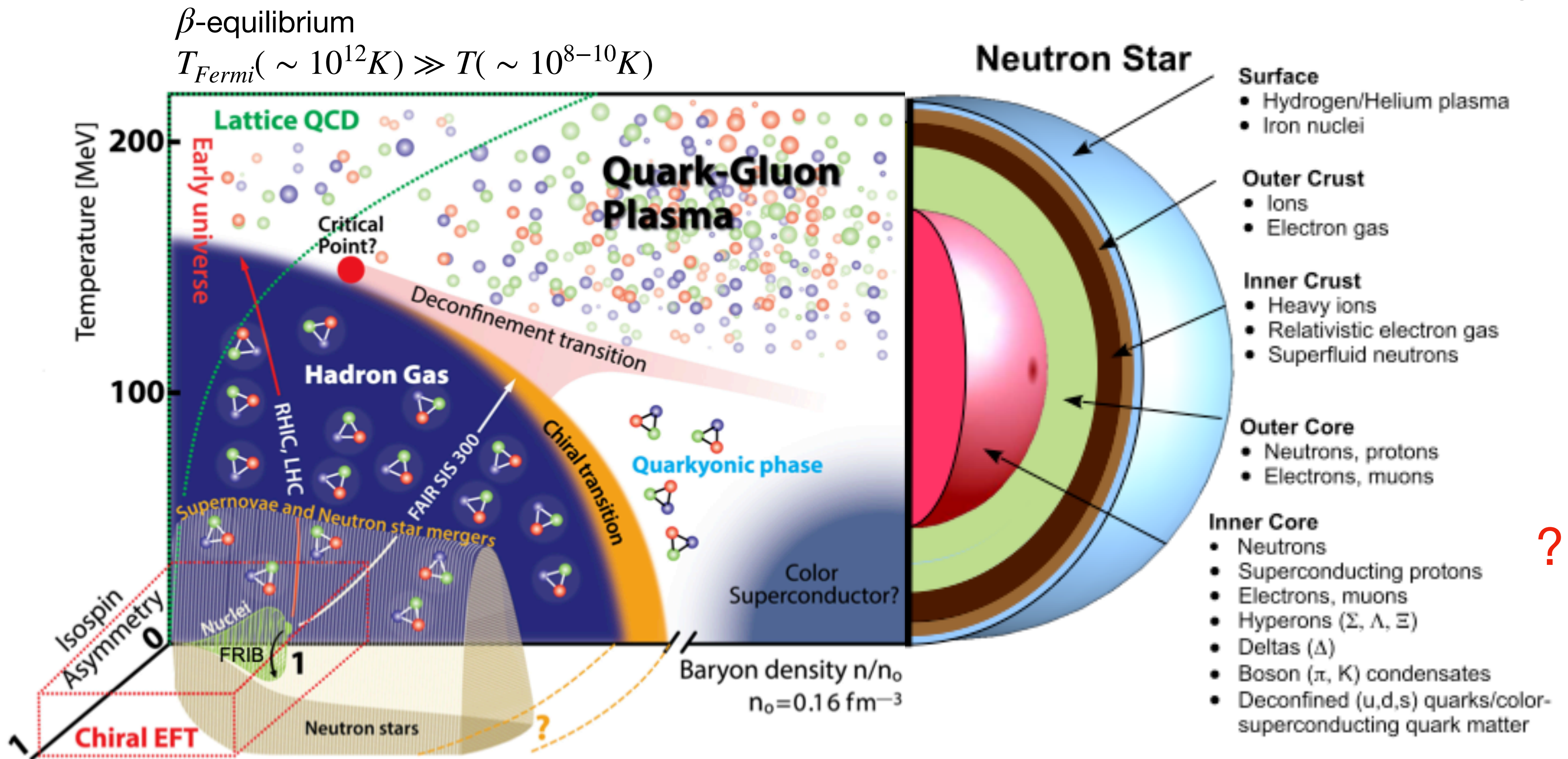
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Neutron Stars as probes for the QCD EoS

“Neutron stars are a remarkable marriage of Einstein’s theory of general relativity with nuclear physics”

Yunes, Miller, Yagi. Nature Rev.Phys (2022)

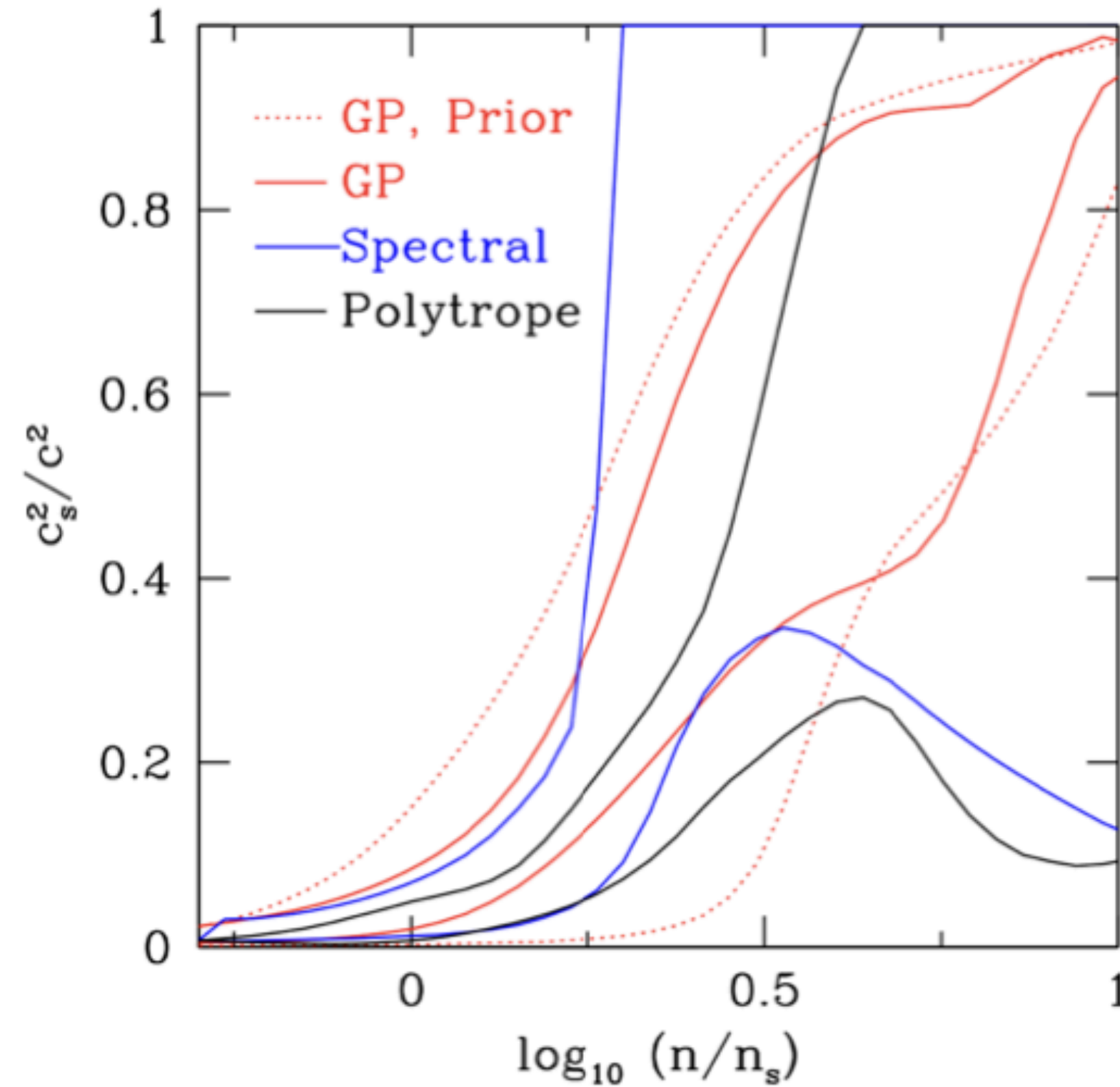
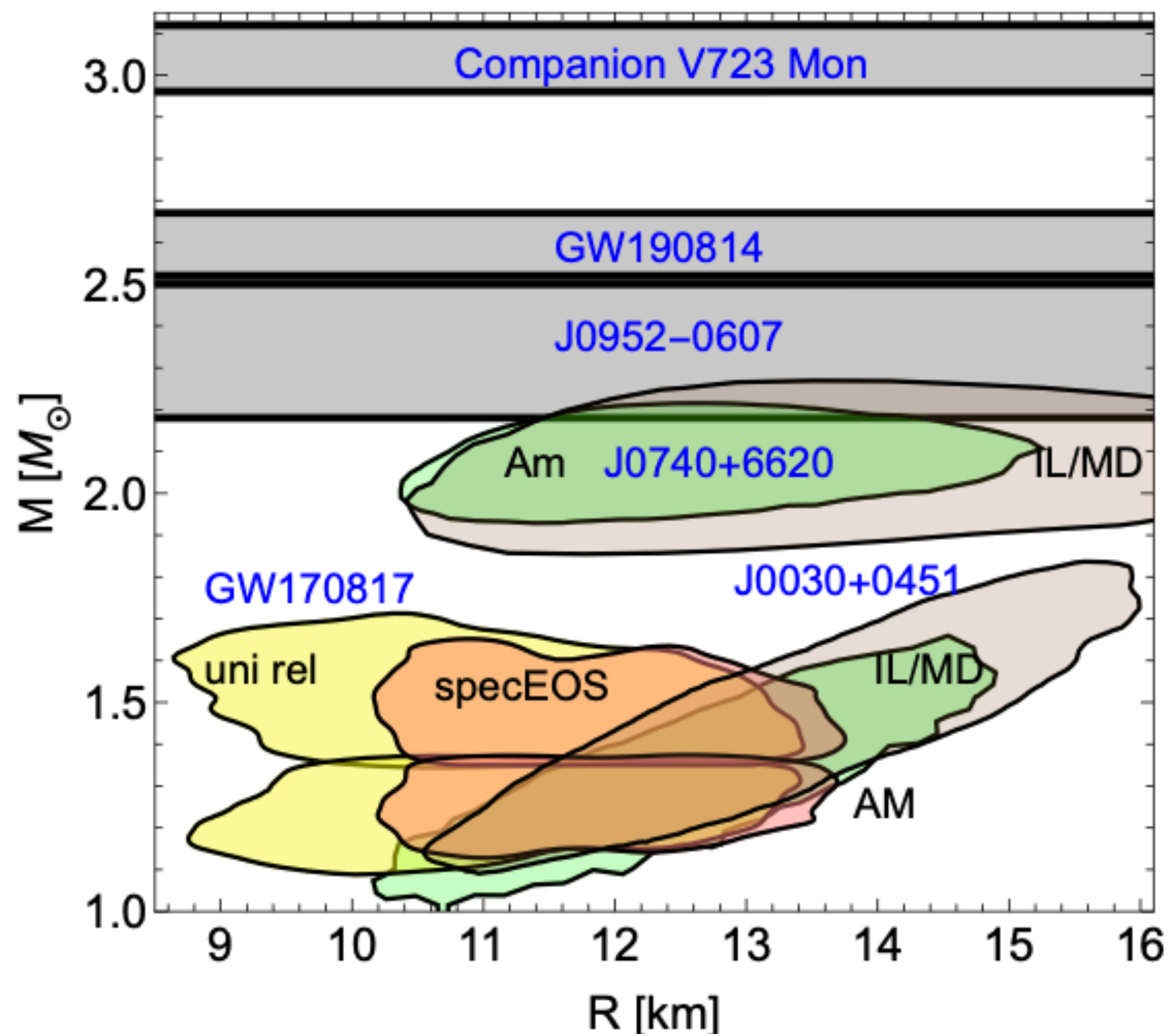


Drischler, Holt, Wellenhofer, Annu. Rev. Nucl. Part. Sci. (2021)

Weber et al. Mod.Phys.Lett.A (2014)

Current observational landscape

Electromagnetic + gravitational wave observations of NS/mergers



Bayesian analysis:
Generate a family of EoS to produce a prior distribution → extract posterior using NS observations.

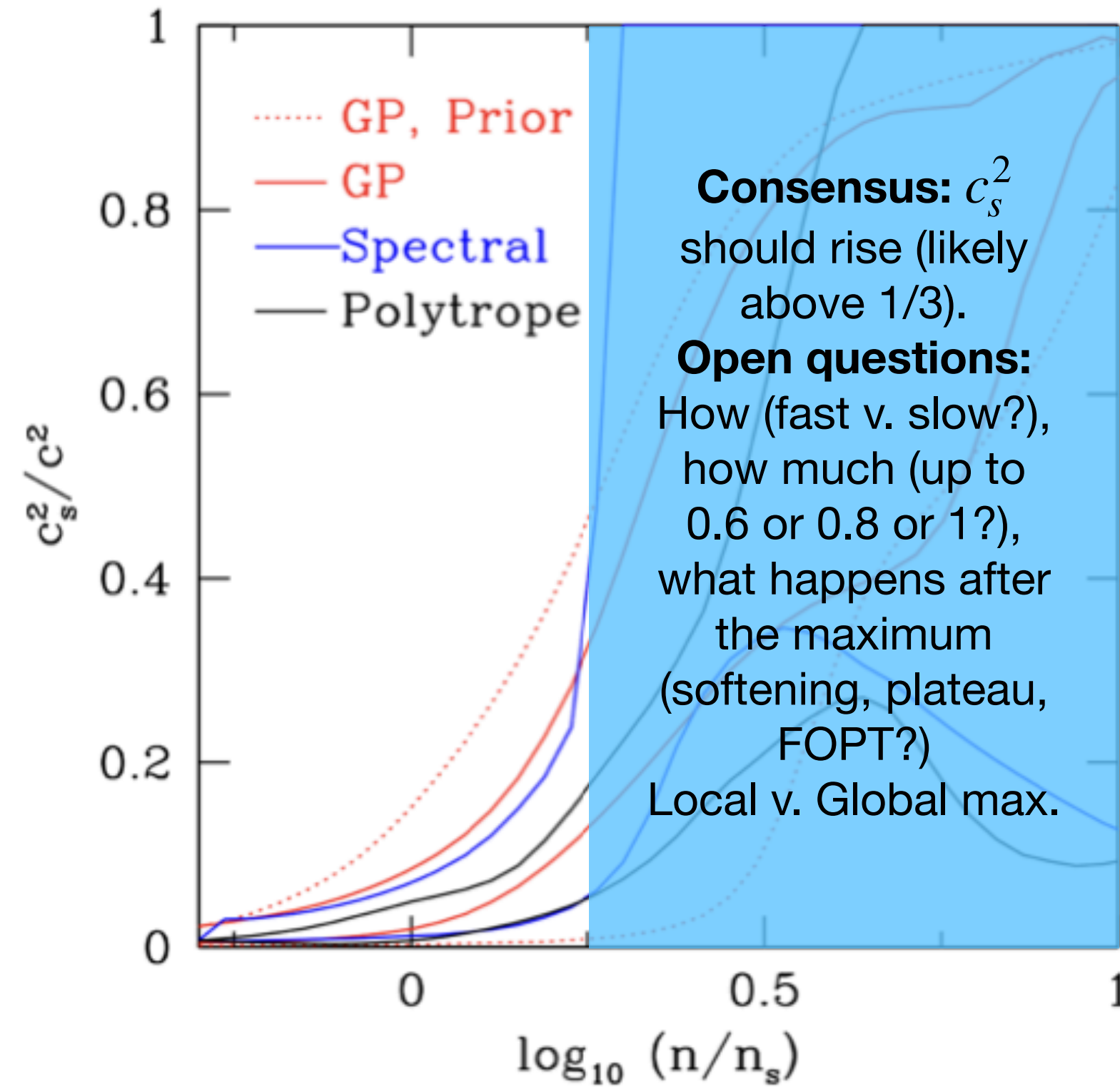
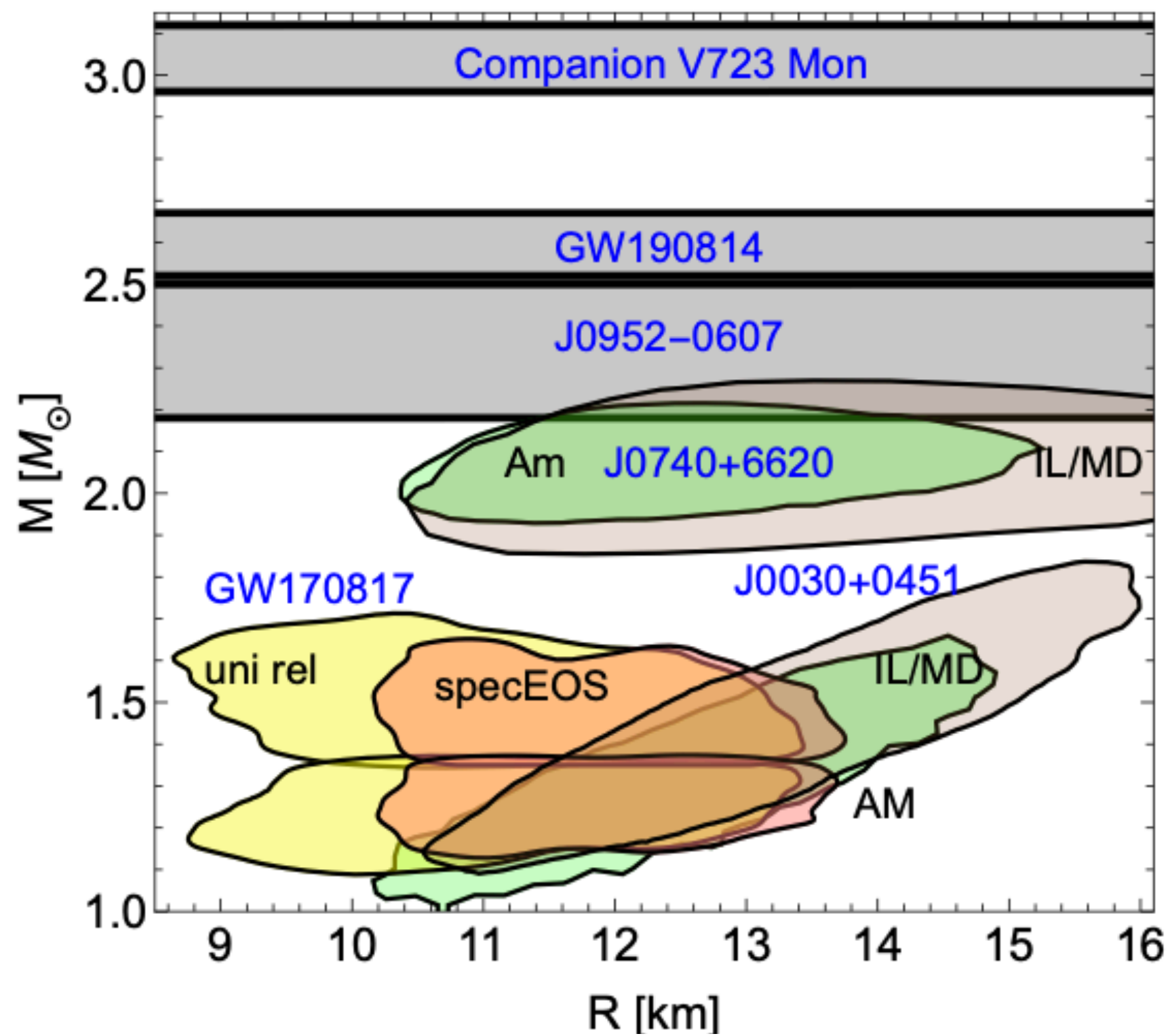
Shown: Constraints at 2σ level from LIGO/Virgo GW170817 and NICER J0030, J0740 used to extract $c_s^2(n_B)$ posterior with 3 different methods for generating the EoS in Miller et al. AJL (2021).

From: "Long Range Plan: Dense matter theory for heavy-ion collisions and neutron stars," arXiv:2211.02224, see for refs.

Note: GW190814, J0952-0607, V723 Mon still under debate.

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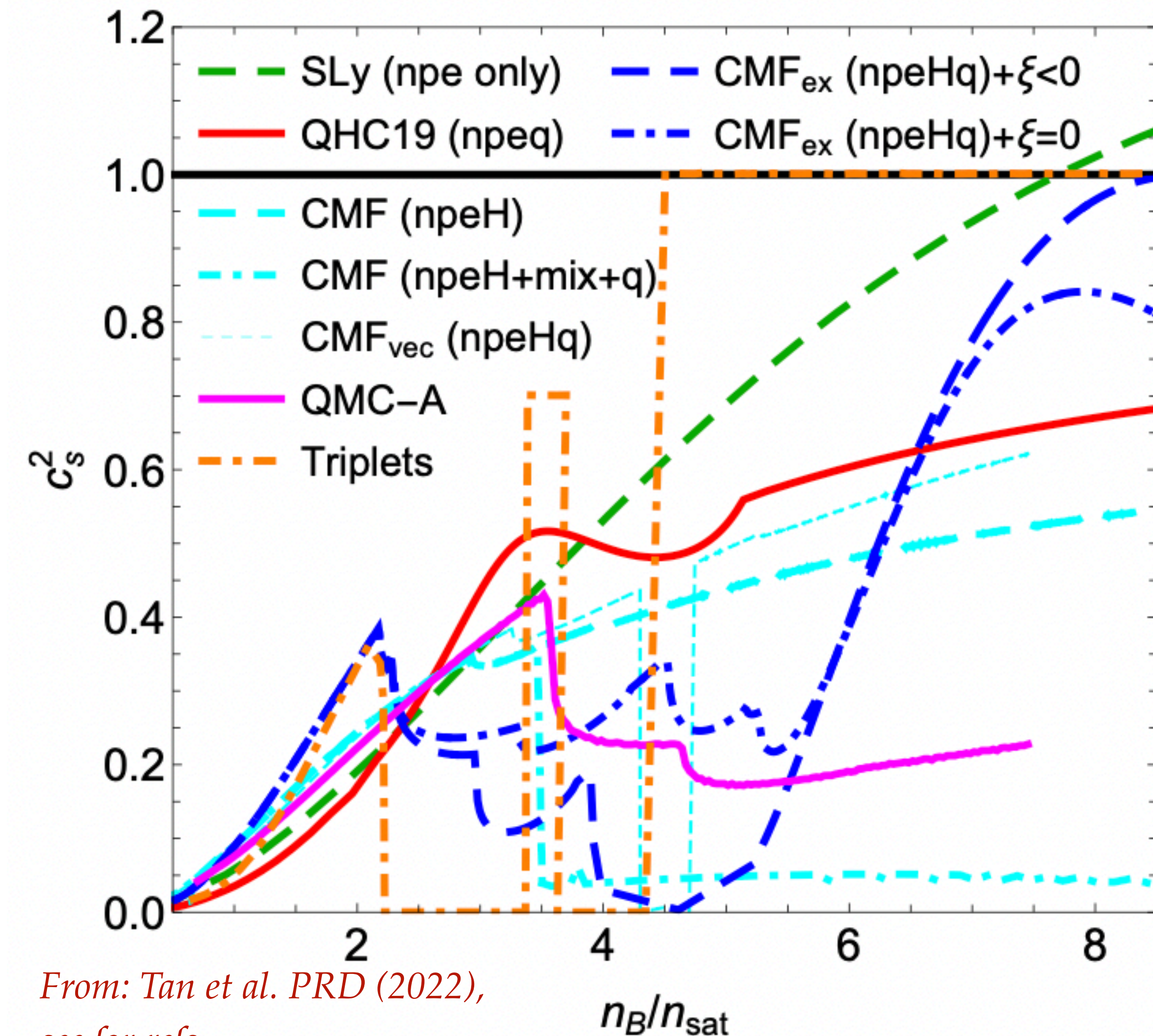
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Nuclear models predict structure

EoS can be modeled with 2 thermodynamic variables e.g. (n_B, P) , (P, c_s^2) , (n_B, c_s^2) ...



Crossover:

- Bump
- Spike
- Plateau
- Oscillations

1st order PT:

$$\text{Gap in } c_s^2(n_B) / c_s^2 \rightarrow 0$$

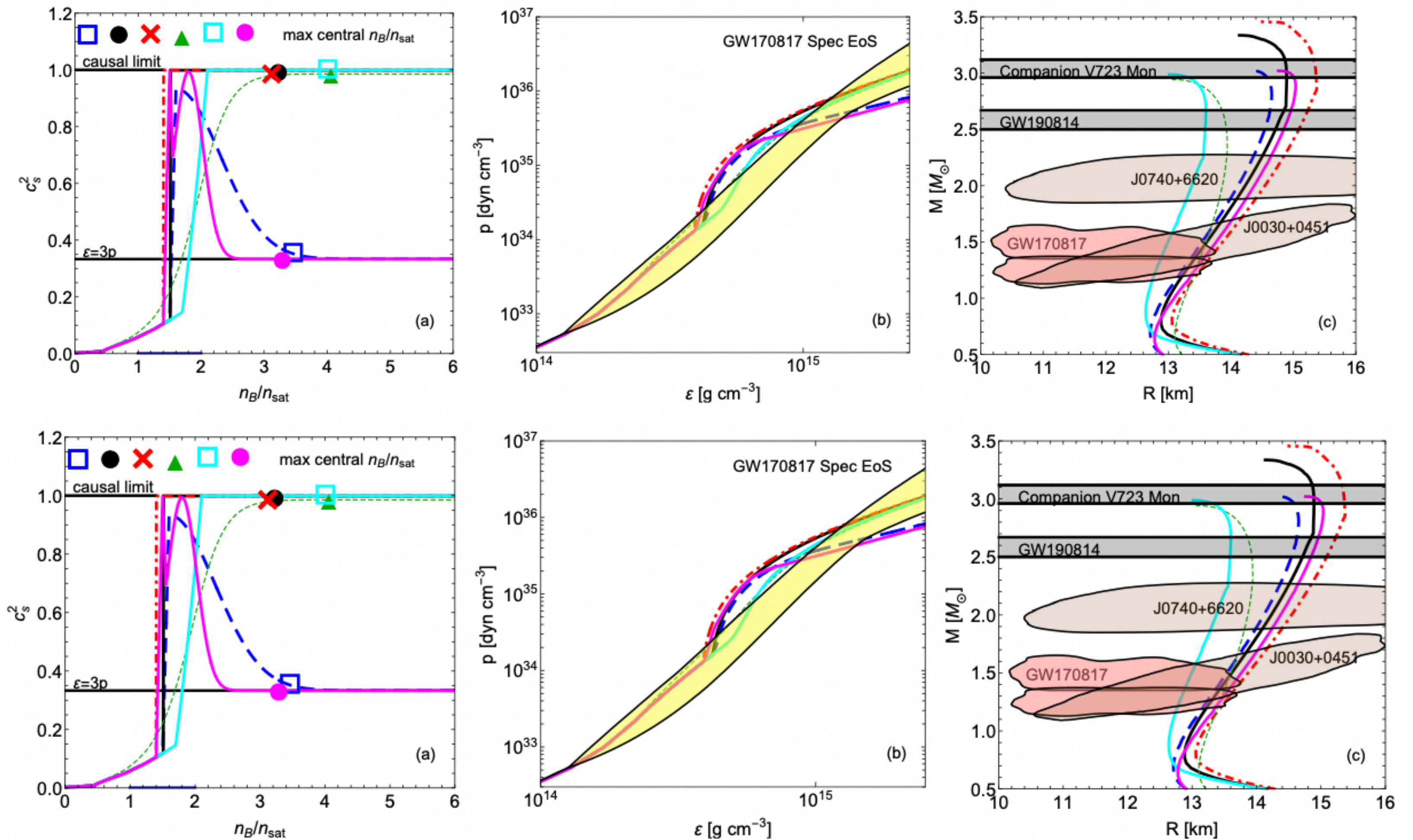
**Nuclear models with quark/
strange degrees of freedom lead
to non-trivial structure in c_s^2**

*From: Tan et al. PRD (2022),
see for refs.*

Effects of sharp/non-trivial features on NS properties

Systematic study: Tan et al. (2022)

- Sharp/non-trivial features important for producing heavy/ultra-heavy NS
- These EoS fit constraints and outside of the regime captured by e.g. spectral EoS



How do we ensure an adequate amount of EoS with non-trivial features is represented in our priors?

Non-parametric(ish) approach to EoS inference

Gaussian processes (GP)

- Stochastic process (collection of random variables)
- **Reproduces continuous functions** between $(-\infty, \infty)$ over a specified domain

In practice, for NS EoS inference:

Auxiliary variable $\phi(x) = \log(1/c_s^2 - 1)$, enforces stability and causality

L. Lindblom PRD (2010)

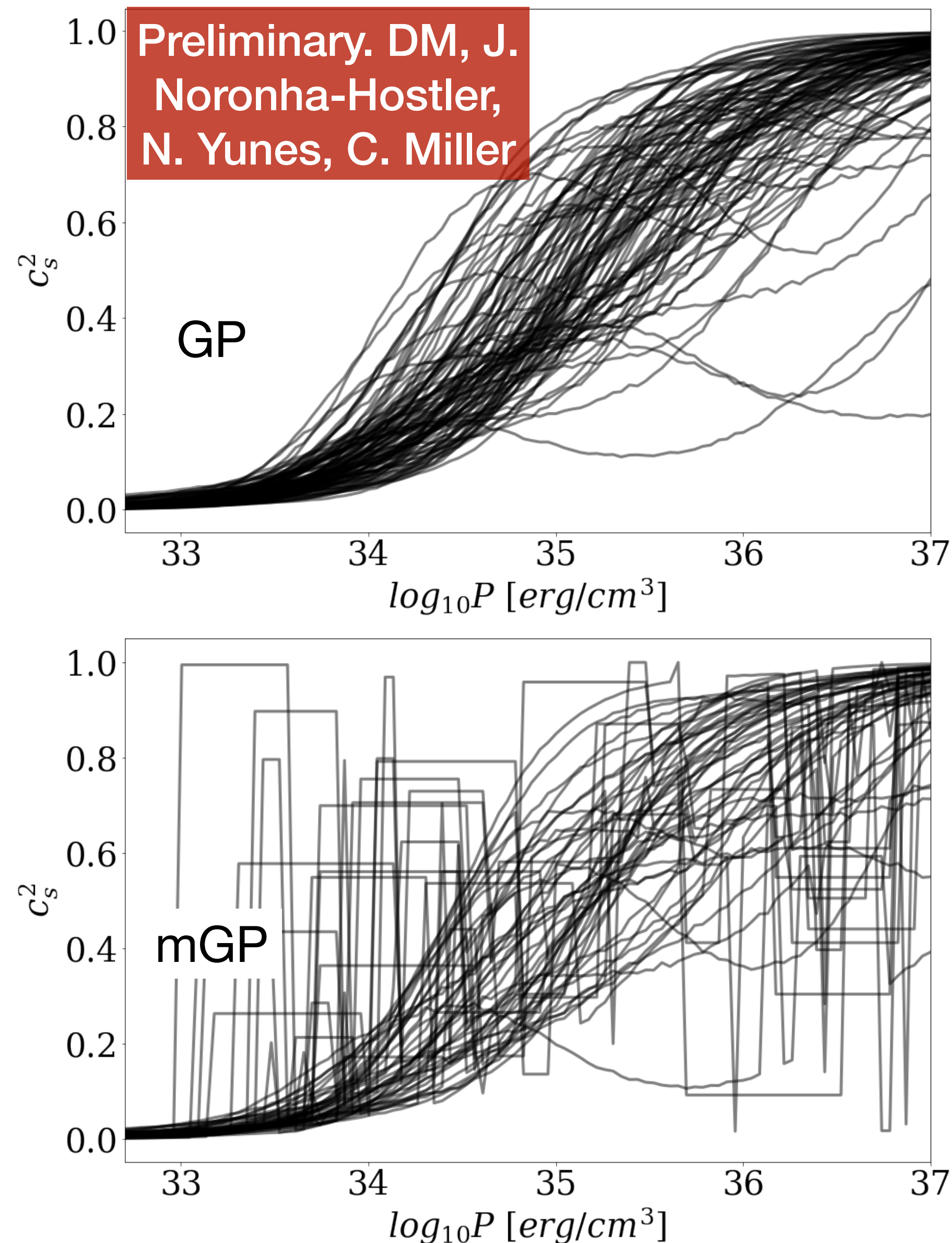
Each x_i specifies a domain point (e.g. in P, n_B)

A GP sample is given by

$$\phi_k(\vec{x}) = \vec{\mu}(\vec{x}) + L\vec{u},$$

where $\vec{u} \sim \mathcal{N}(0, I)$, L : Cholesky decomposition of covariance matrix Σ .

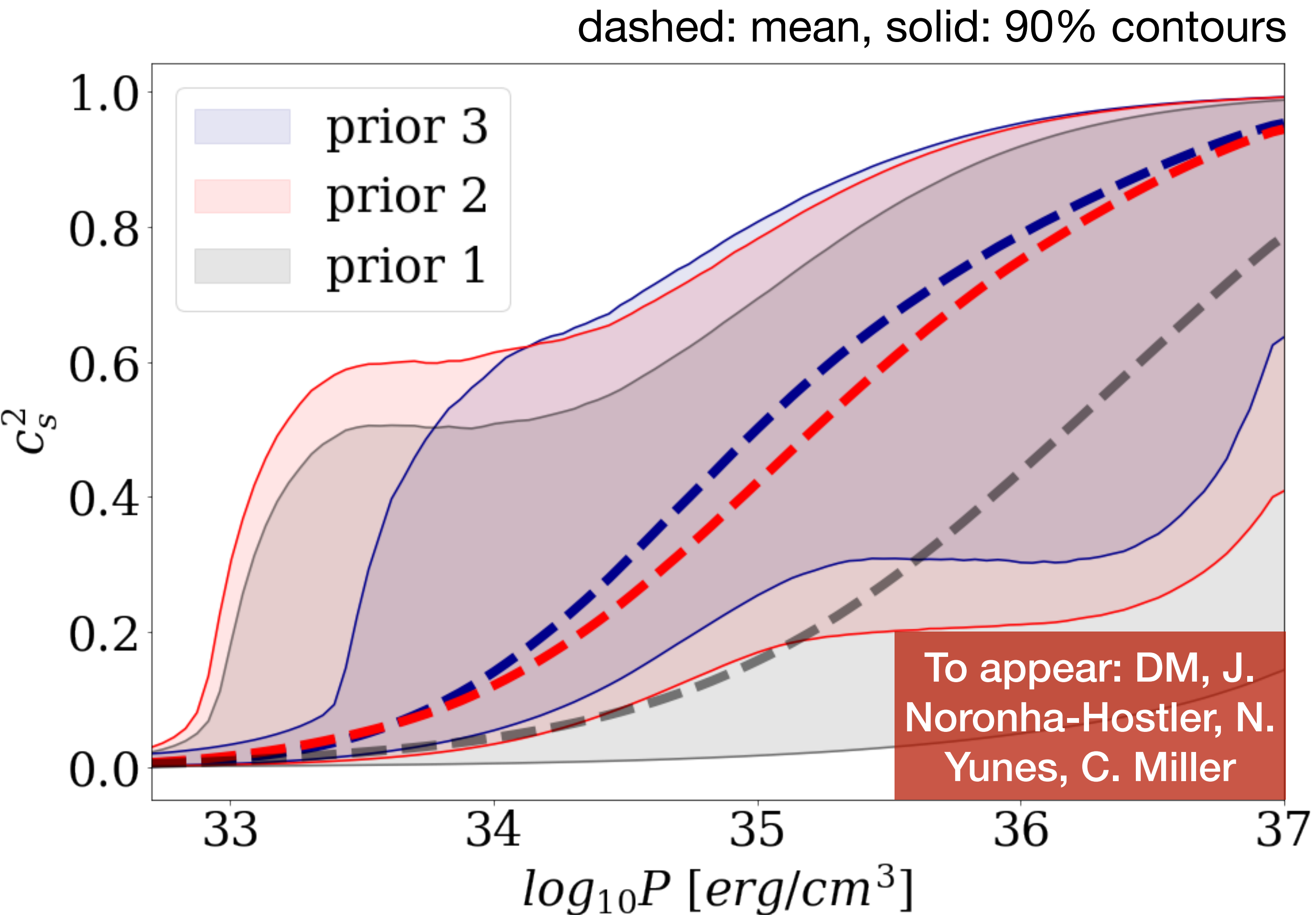
Modified GP (mGP) EoS



Modified: GP background + added features

- **Why:** Motivated by nuclear models and H. Tan et al (2022), current (non-)parametric methods do not capture sharp/non-trivial features well + important for explaining heavy and ultra-heavy stars.
- **What:** spikes, wells, plateaus, bumps, kinks added onto smooth GP background.
- **Method:** 3 modification categories — spike, spike + plateau, 2 plateaus. Final functional form depends on background GP.
- Prior contains both unmodified GP and mGP samples.
- Can be analyzed together or separately.

Sample selection



We perform a pruning of the prior to ensure we have enough EoS that meet **basic constraints**

- 900,000 EoS in prior 1
- of which only 281,139 in prior 2 reach $M_{max} \geq 1.4M_{\odot}$
- Final cut imposes
 - $M_{max} \geq 1.8M_{\odot}$
 - $9.0 \text{ km} \leq R_{1.4} \leq 18.0 \text{ km}$
 - $10 \leq \Lambda_{1.4} \leq 2000$
- **Prior 3: 104,594 total EoS split between modified and unmodified GP**

Use prior 3 with NICER/LIGO + low-density + pQCD to obtain posterior distributions

Low-density and pQCD constraints

All EoS are matched to QHC19 at $0.5 n_{sat}$

+ No features allowed below $1.1 n_{sat}$

+ Likelihood of symm. energy 32 ± 2 MeV

+ Causality/integral constraints from Komoltsev and Kurkela (PRL, 2022)

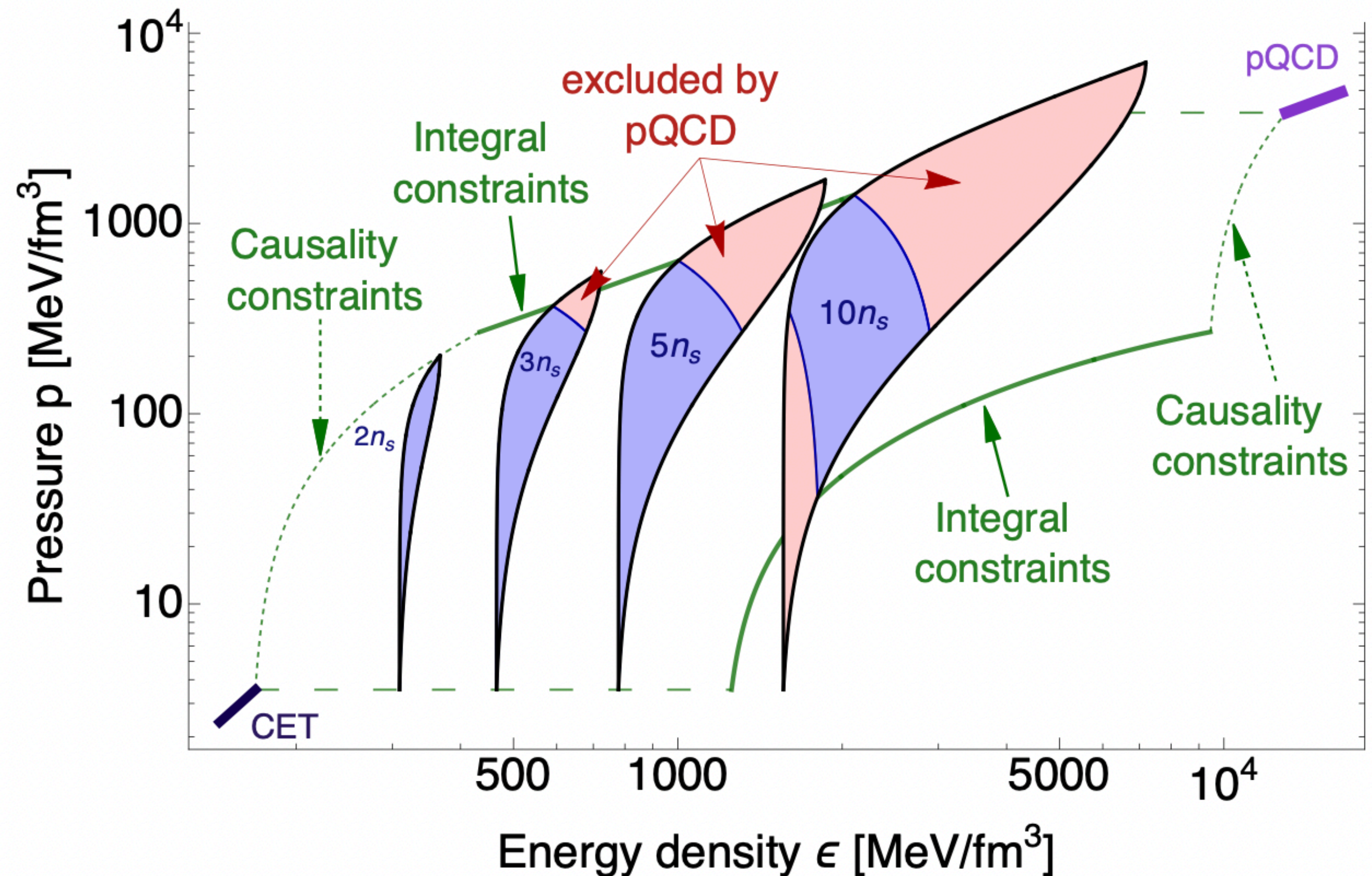
Averaged over pQCD renormalization parameter $X = [1/2, 2]$ (log-linear).

$w_{pQCD} = 1$ when in agreement for all X.

$0 < w_{pQCD} < 1$, in tension.

$w_{pQCD} = 0$ not allowed.

From: Komoltsev, Kurkela, PRL (2022)



Questions addressed in this talk

- Are sharp features in $c_s^2(n_B)$ consistent with NICER/LIGO observations?
- Is there a clear preference for unmodified/modified GP?
- What is the global maximum of c_s^2 ?
- Where is the global maximum of c_s^2 in terms of the density?
- Is there conclusive evidence for a softening of the EoS within the range of n_B^{TOV} (signaling a possible phase transition to an exotic phase)?

Marczenko (arXiv:2207.13059), also Komoltsev & Kurkela PRL (2022)

Evidence for smooth vs. sharp features in the EoS

- Assume equal prior probability for all EoS:

$$P[(m)GP] = \frac{1}{N_{(m)GP}}$$

- The Bayesian evidence is

$$P[(m)GP | D] = \frac{1}{N_{(m)GP}} \sum_i^{N_{(m)GP}} \mathcal{L}_i$$

- Bayes factor: statistical evidence for model 1 (smooth features) against model 2 (sharp features)

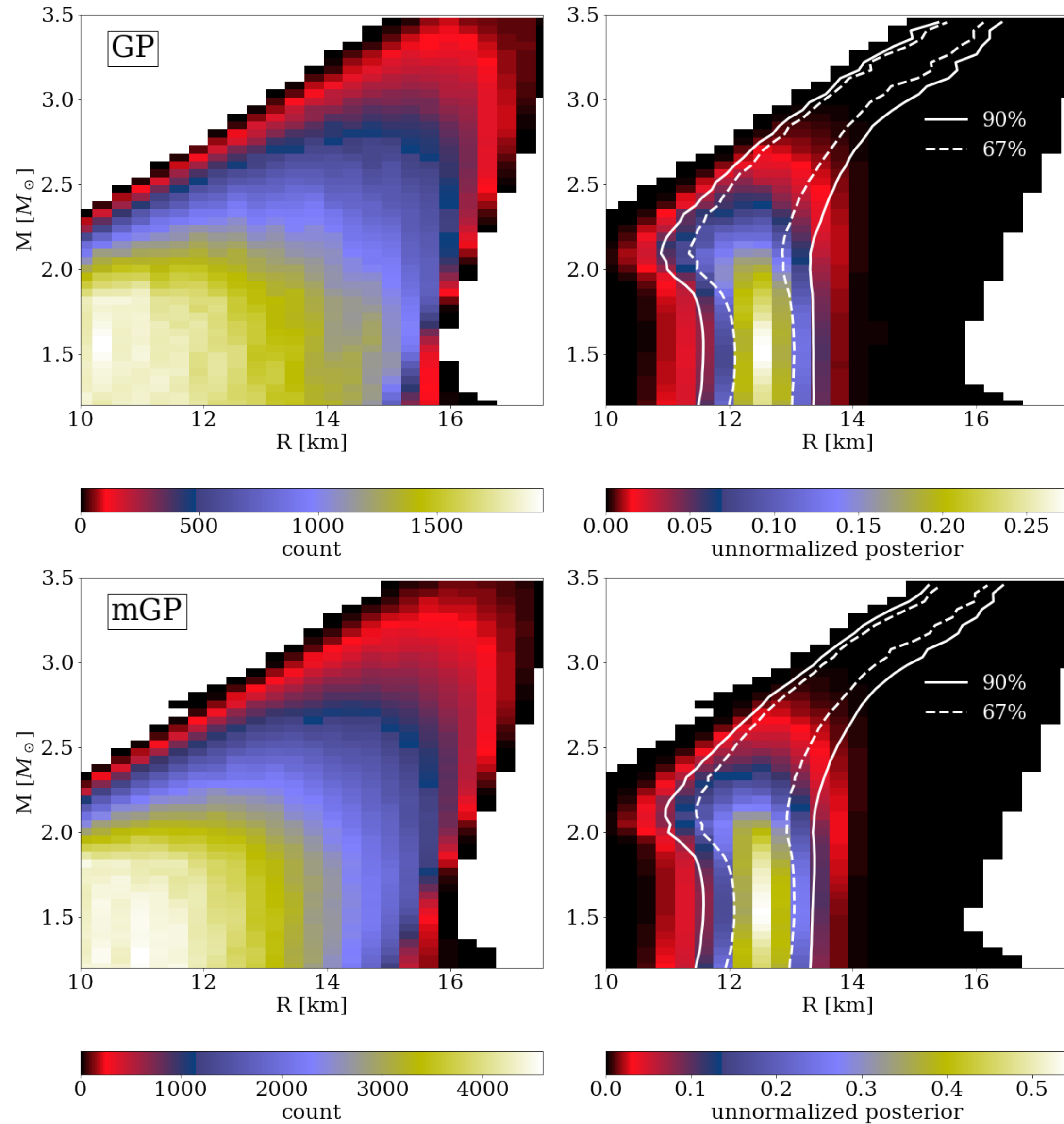
$$K = \frac{P[GP | D]}{P[mGP | D]} = \mathbf{1.126}$$

We find no evidence that GP EoS are preferred over mGP EoS

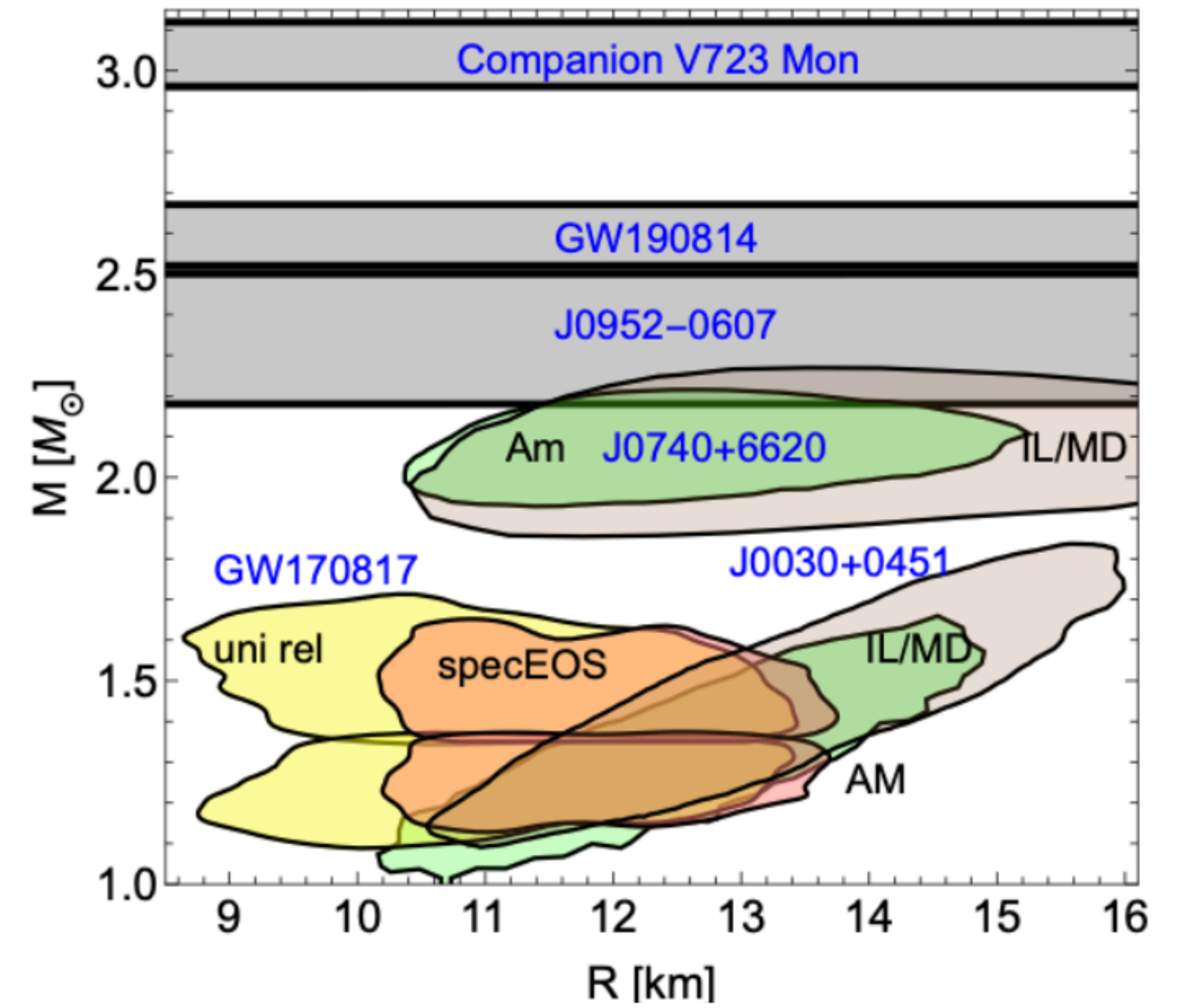
See also: previous inference study on FOPT/crossovers, Somasundaram et al. (2021), 2112.08157, piecewise linear EoS.

Posteriors: mass-radius

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Both frameworks can account for current measurements



Effects of pQCD constraints

- Show EoS only up to n_B^{TOV}
→ pQCD constraints imposed at n_B^{TOV}

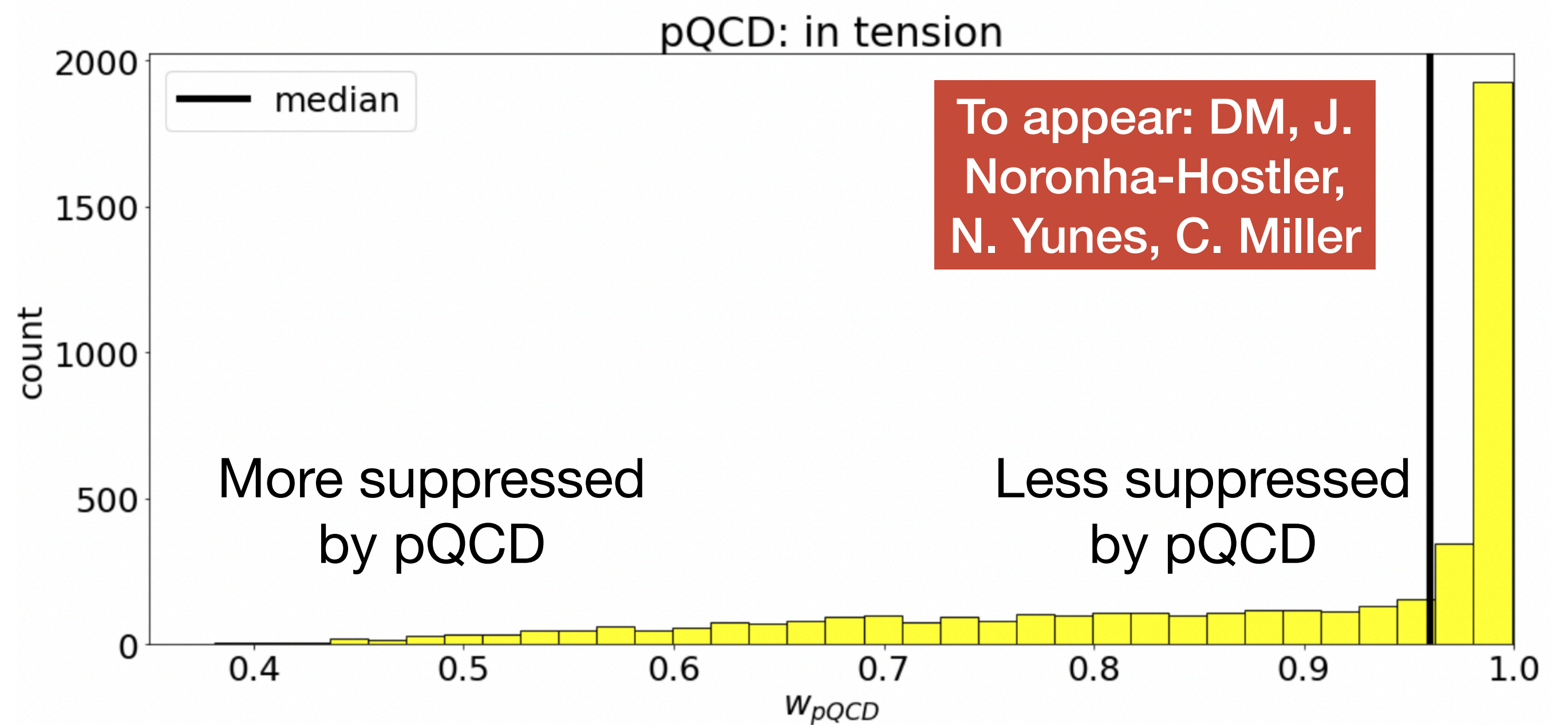
11 EoS ruled out (0.8%)

127,199 EoS in agreement (96.5%)

4,592 EoS in tension (3.5%) →

- Thermodynamic + consistency constraints can't be neglected, but the effect for pQCD renormalization parameter $X = [1/2, 2]$ imposed at max. central densities **does not affect the shape of the posteriors.**

See also: R. Somasundaram, I. Tews, J. Margueron, arXiv: 2204.14039



Posteriors: $c_s^2(n_B)$

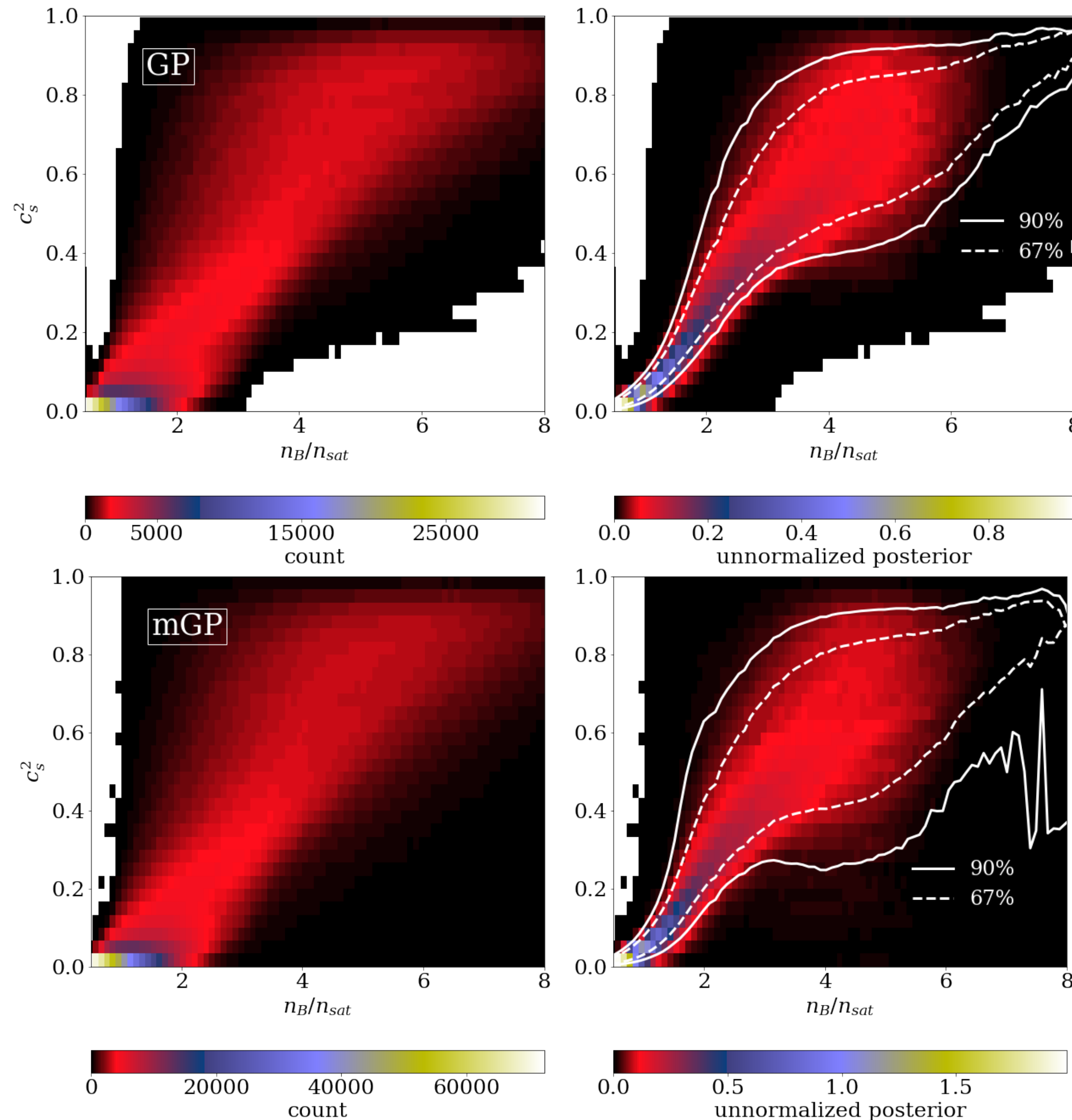
To appear: DM, J. Noronha-Hostler, N. Yunes, C. Miller

More systematic treatment below n_{sat} , see: Raaijmakers et al AJL (2021), 2105.06981

Low density regime sensitive to observations

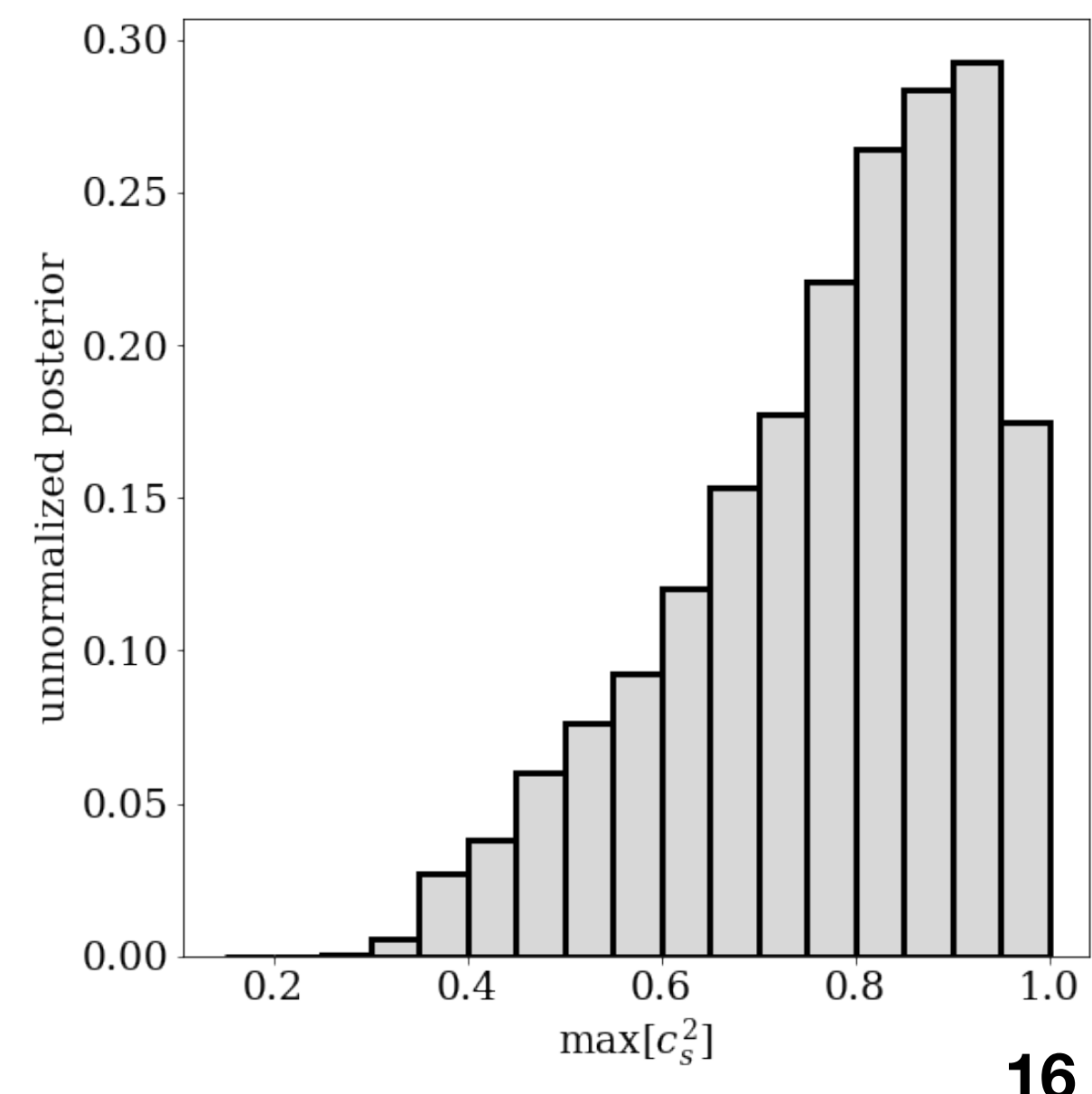
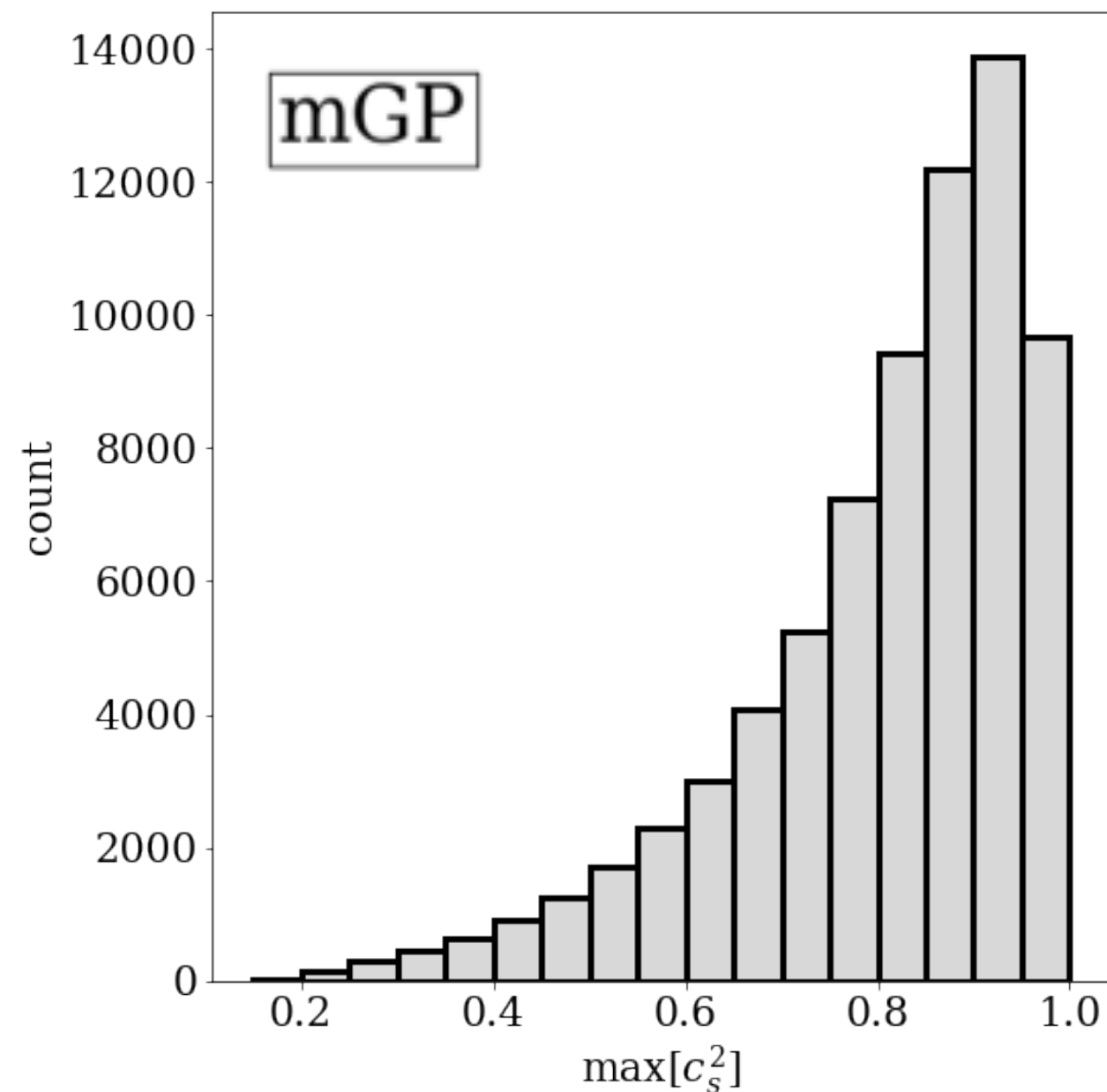
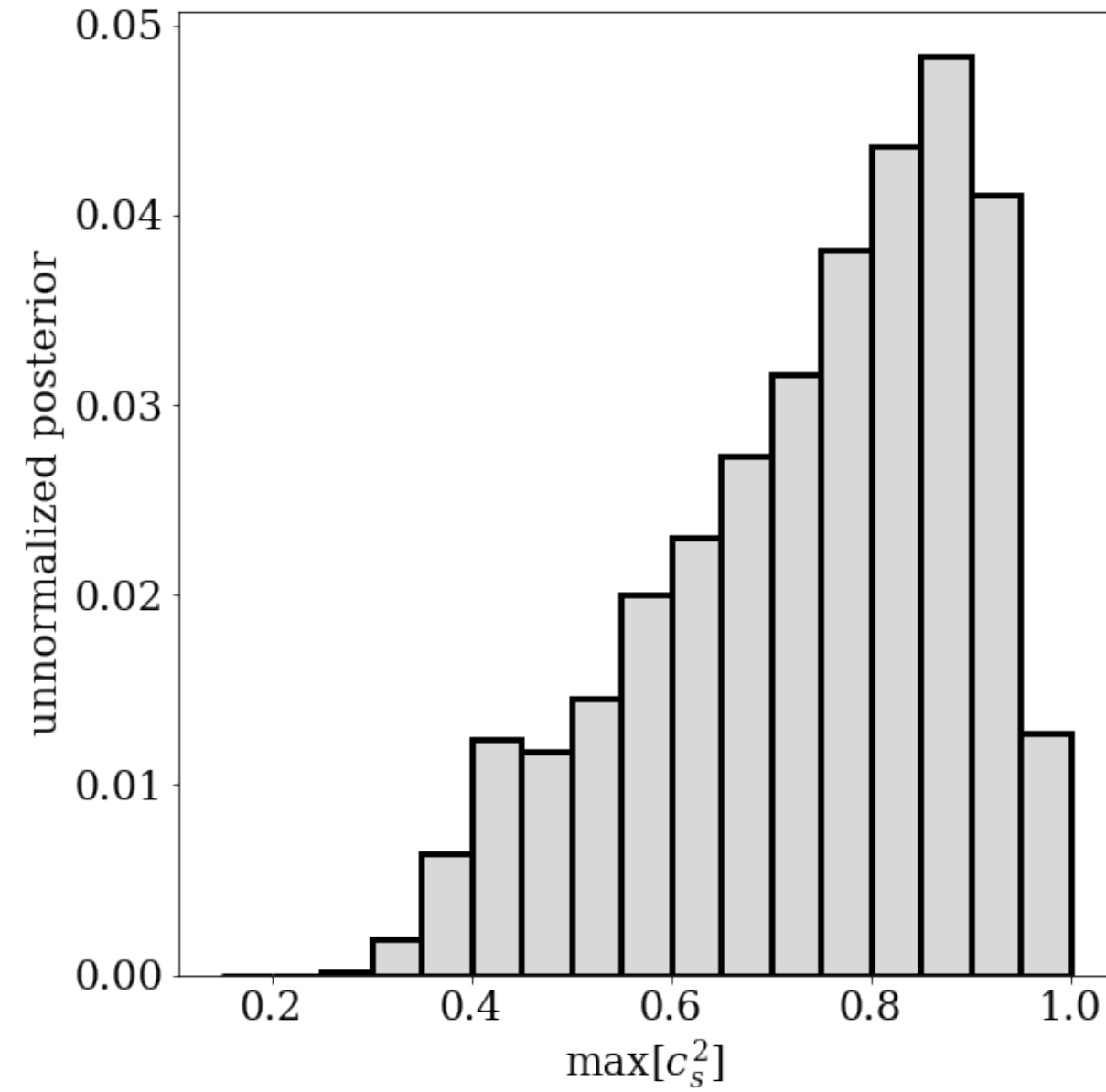
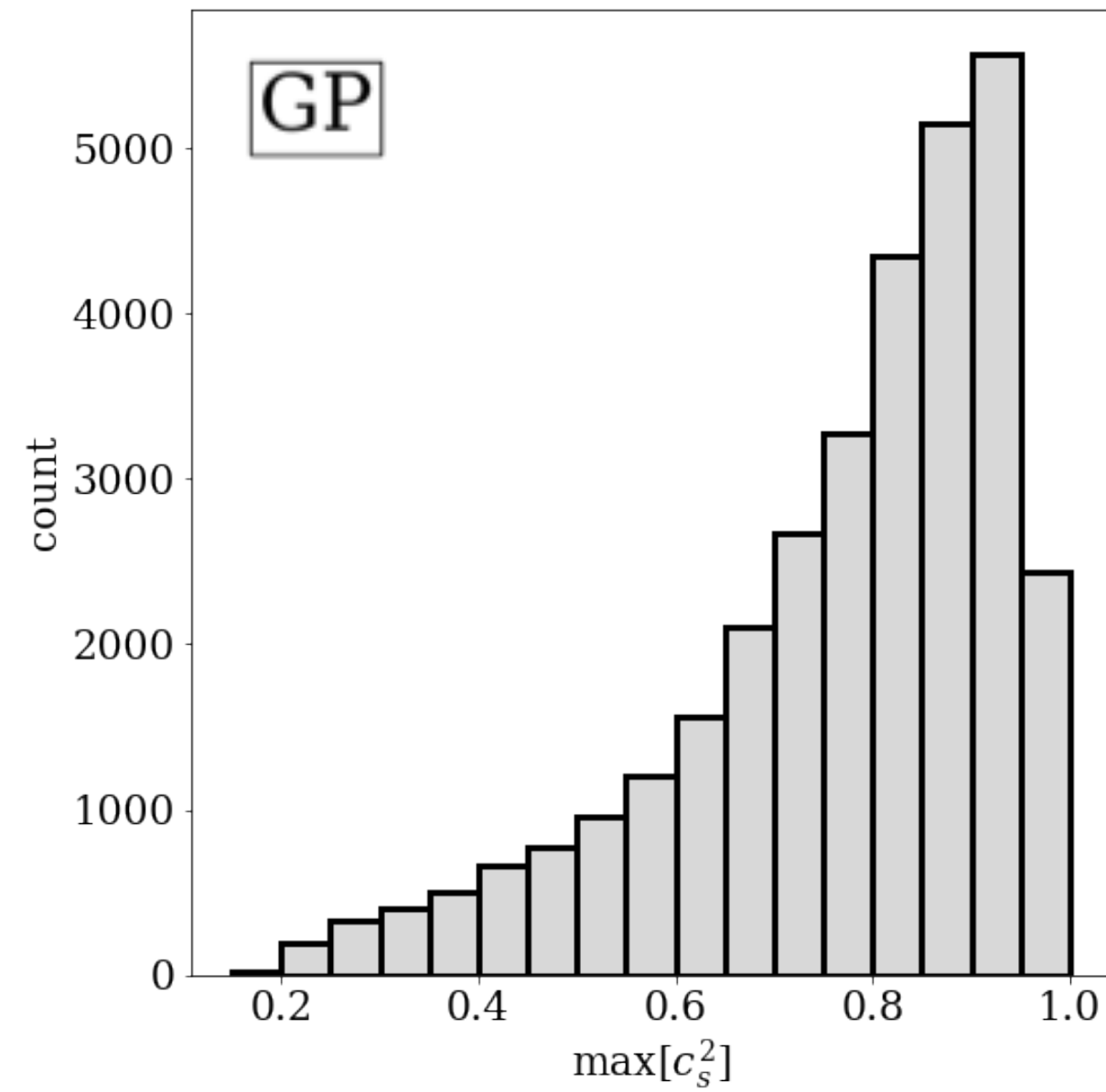
At the 90% level, c_s^2 rises above 1/3 around $\sim 3n_{sat}$

We cannot conclude that there is a softening of the EoS within the range of n_B^{TOV}



What is the global maximum of the speed of sound?

Preliminary. DM, J. Noronha-Hostler, N. Yunes, C. Miller



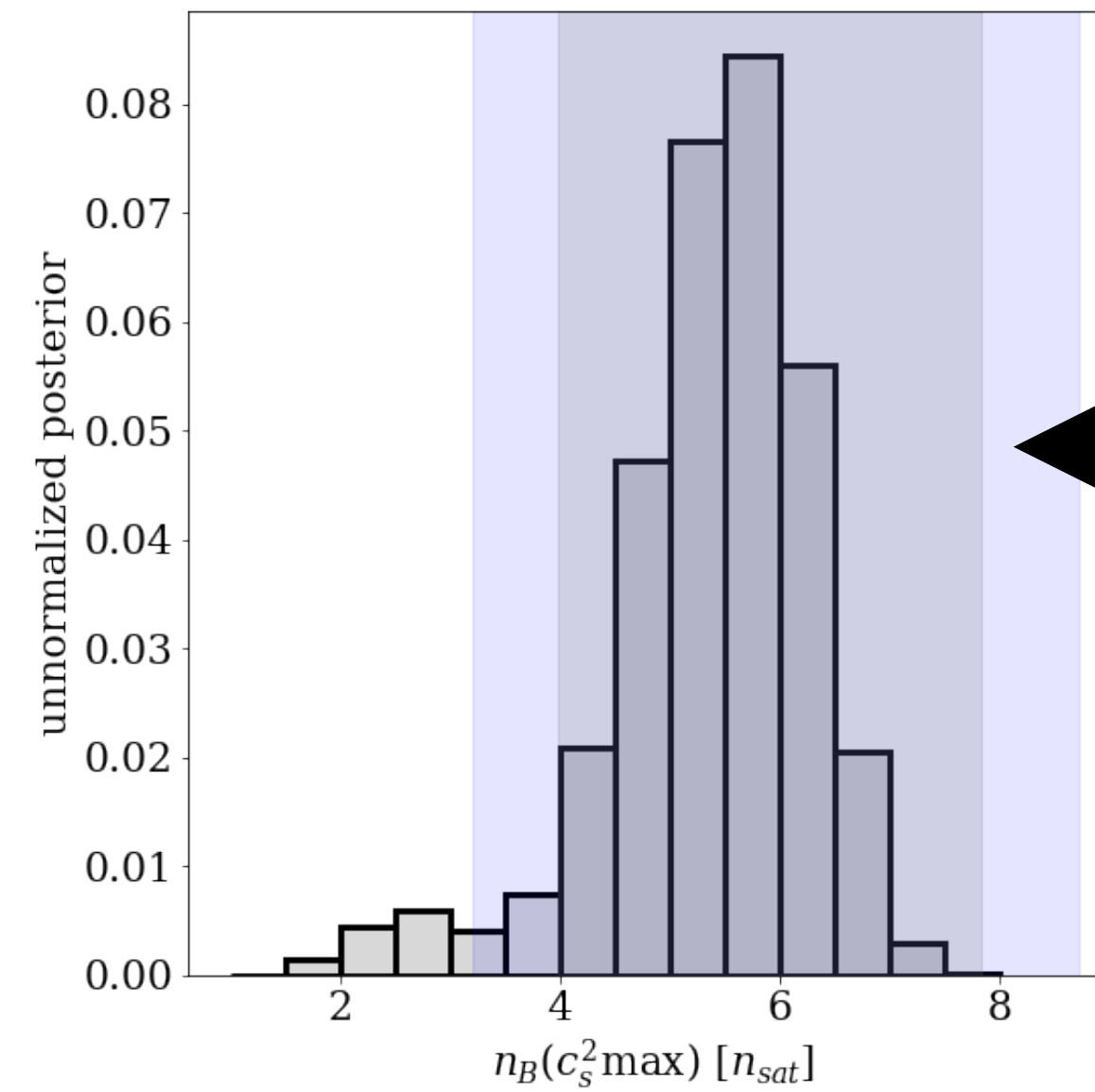
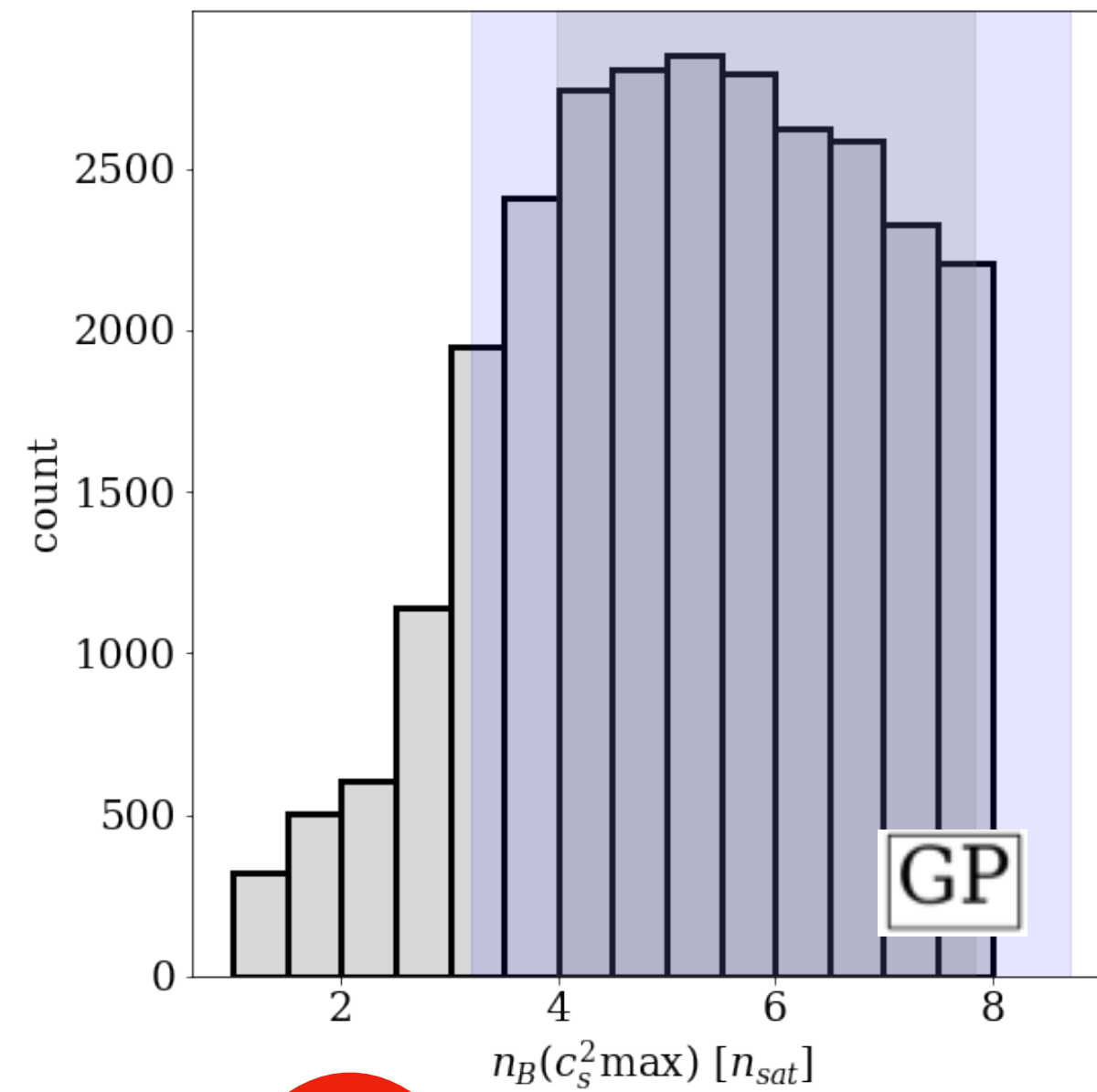
Prior 3 is biased to large values of c_s^2 :

Observations **enhance** the probability of a lower c_s^2 at the global max.

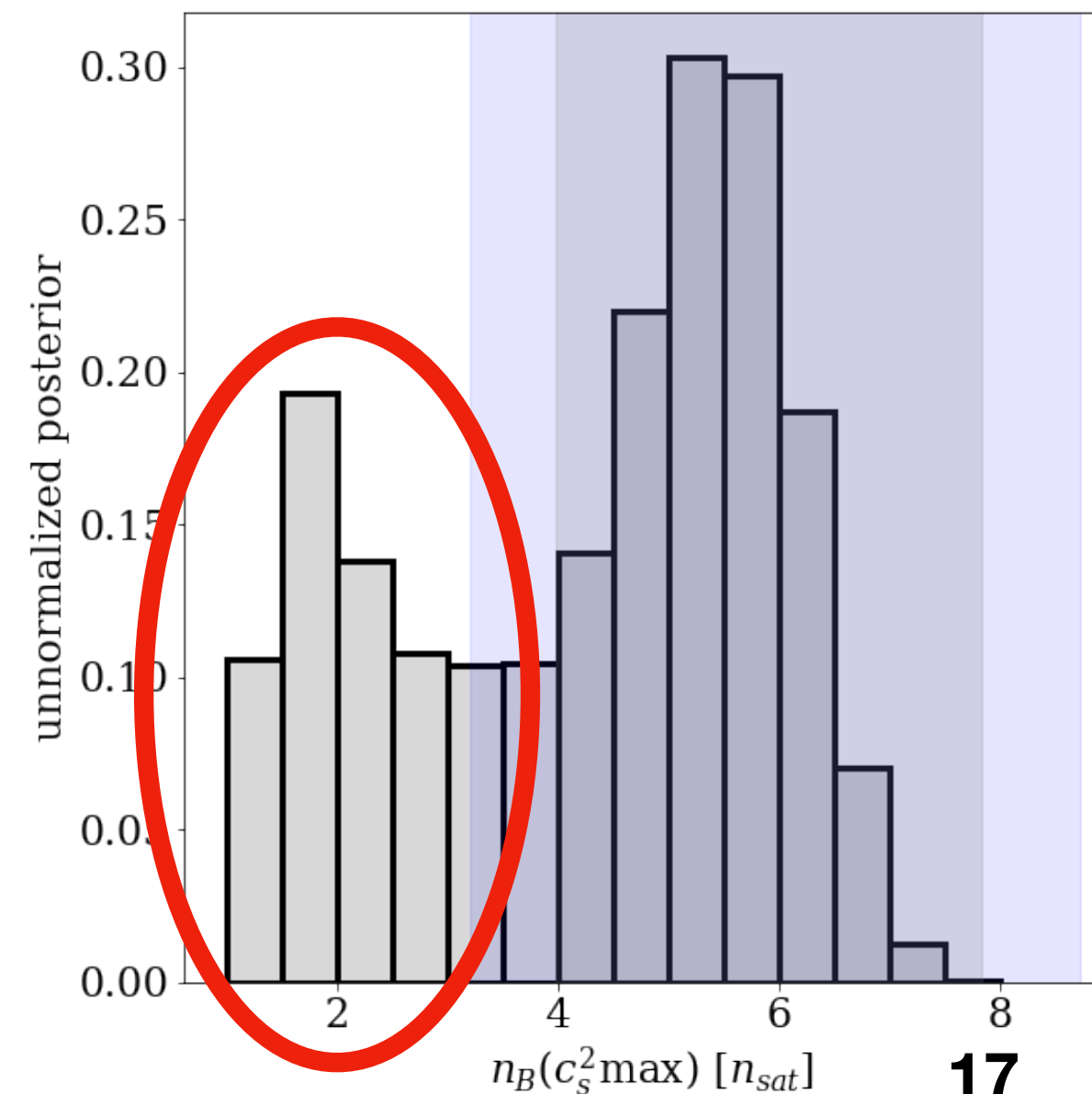
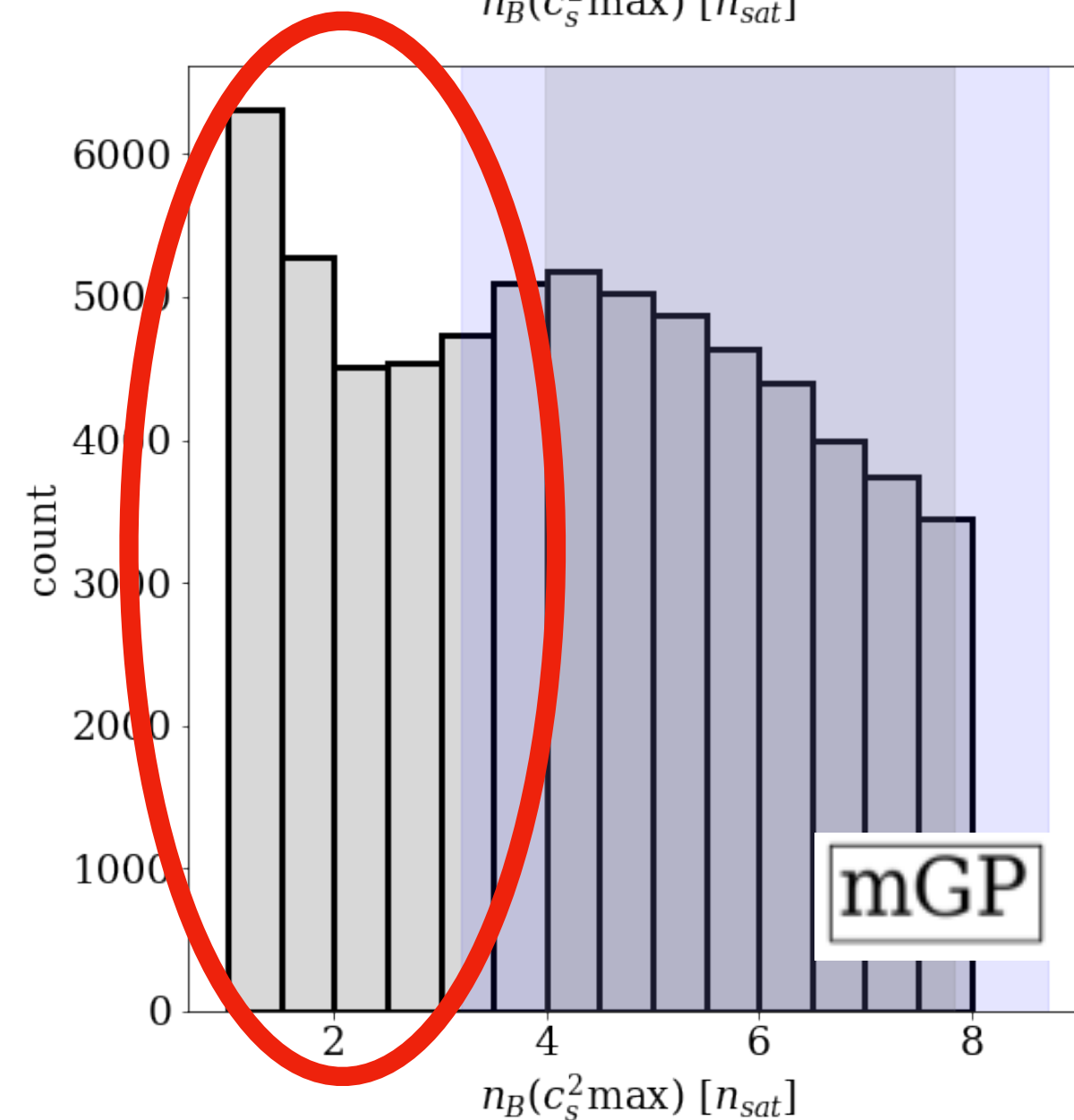
→ Influence of NICER/LIGO-motivated cuts for prior 3 vs. biased GP is currently being investigated and will be improved for future work.

Where is the global maximum of the speed of sound?

Preliminary. DM, J. Noronha-Hostler, N. Yunes, C. Miller

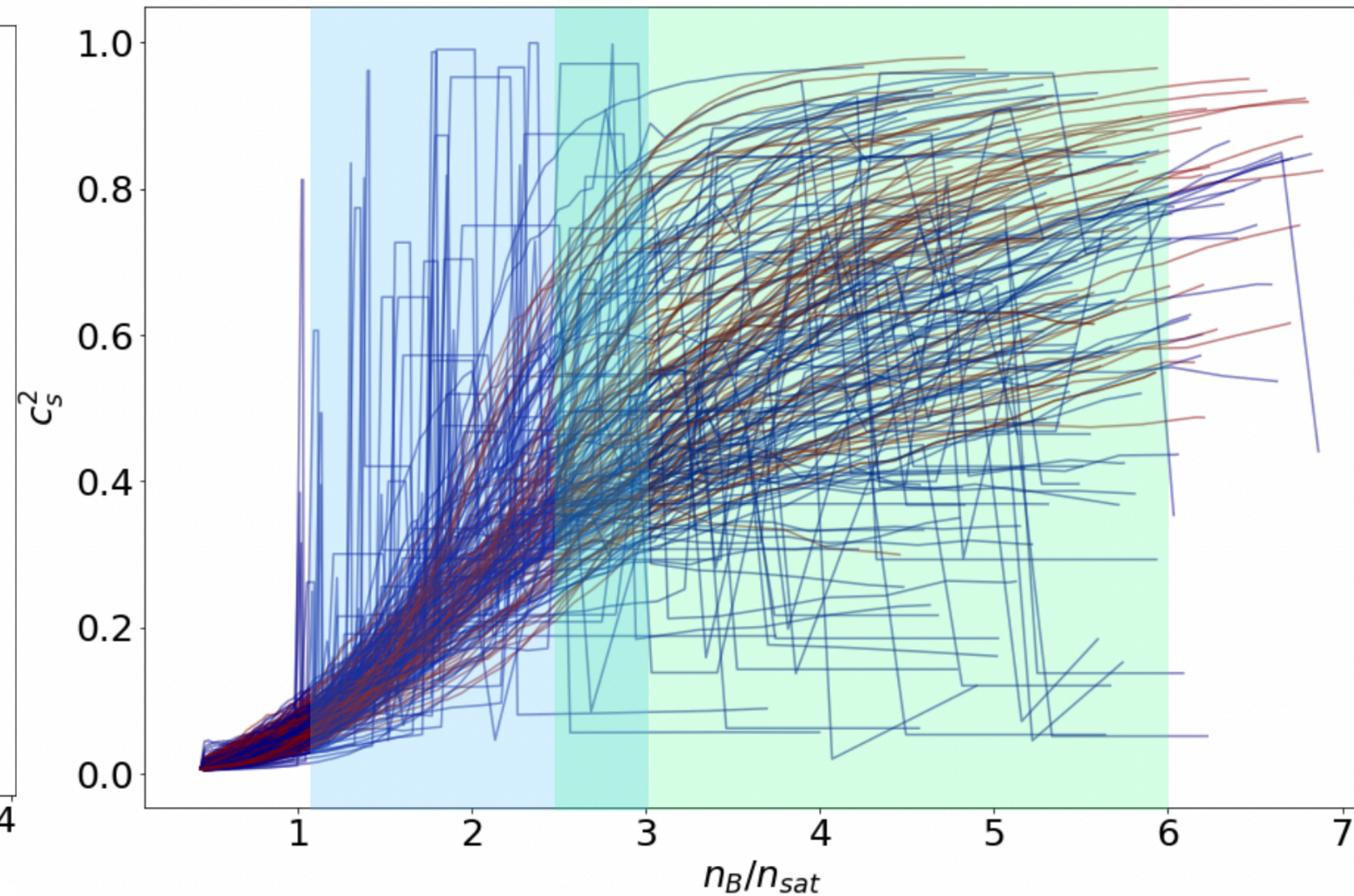
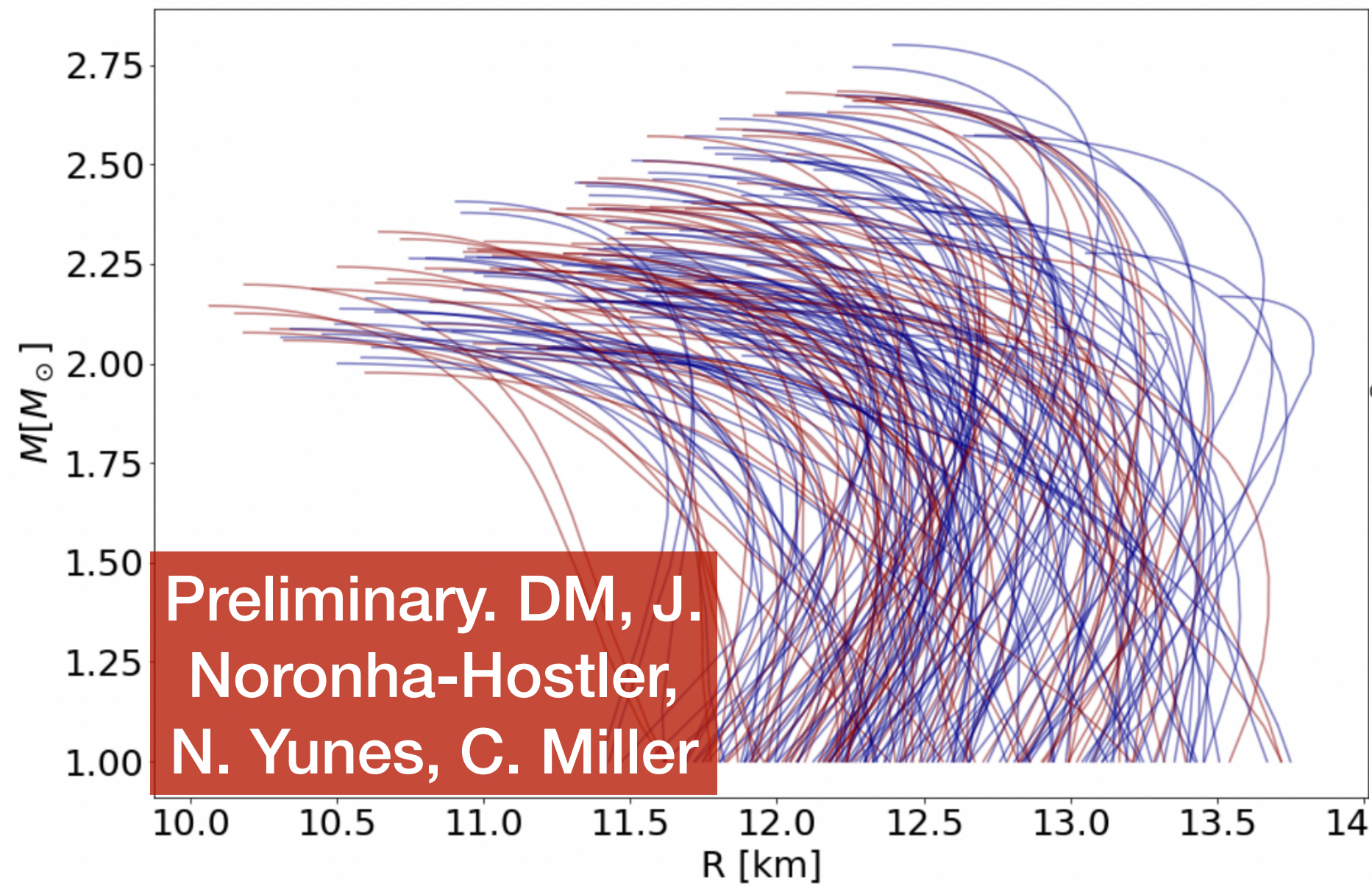


Because of constraints at and below n_{sat} , large values of c_s^2 below $\sim 3 n_{sat}$ can only be achieved with sharp rises (better captured by the mGP).



The posterior distribution for $n_B(c_s^2 \text{max})$ is bimodal

Two possibilities for the behavior of c_s^2



Sample of 200 EoS in the 90th percentile for likelihood

We're currently investigating how these two cases can be distinguished with future data

Both features can produce heavy/ultra-heavy stars

Global maximum between $\sim 1.1-3n_{sat}$ or

Softening: Possible PT/crossover

c_s^2 rises monotonically to higher densities going above $1/3$ between $\sim 1.5-3n_{sat}$

Summary

- Are sharp features in $c_s^2(n_B)$ consistent with NICER/LIGO observations? **Yes**
- Is there a clear preference for smooth/non-trivial features in the EoS? **No**
- What is the global maximum of c_s^2 ? **More work required**

Improve low density treatment: χ EFT

Further relax assumptions about mean behavior of GP

- Where is the global maximum of c_s^2 in terms of the density?
- Is there conclusive evidence for a softening of the EoS within the range of n_B^{TOV} (signaling a possible phase transition to an exotic phase)?
- What can future data tell us about the dense matter speed of sound?

Near i) n_B^{TOV} OR ii) $1.5 - 3n_{sat}$

No

More work required

It depends on whether we have i) or ii)

Seen with mGP



Outlook

EoS inference from astro. observations is a new field.

More astrophysical data is coming. Next 10 years: NICER and LIGO/Virgo O4+O5.

We're learning ways to integrate theoretical constraints with observations and experiments (talk by Ingo Tews) + robust constraints from HIC.

– Can we find a flexible common parametrization of the EOS, applicable to neutron star calculations and different types of heavy-ion collisions simulations?

Effective models (talk by Rajesh Kumar).

At Illinois: combining flexible $T=0$ parameterizations (this talk) with expansions into Y_Q (talk by Nanxi Yao) and finite T (graduate student Katie Zine).

– What other observables could enable the extraction of the EOS?

Breaking of universal relations (talk by Veronica Dexheimer) + GW signals (ongoing work).



Back-up

Non-parametric(-ish) approach to EoS inference

Non-parametric, but...

choice: $\vec{\mu}(\vec{x})$ specifies mean behavior of $\phi_k(x)$

choice: Covariance matrix Σ , could be model-informed or agnostic (still requires hyperparameters)

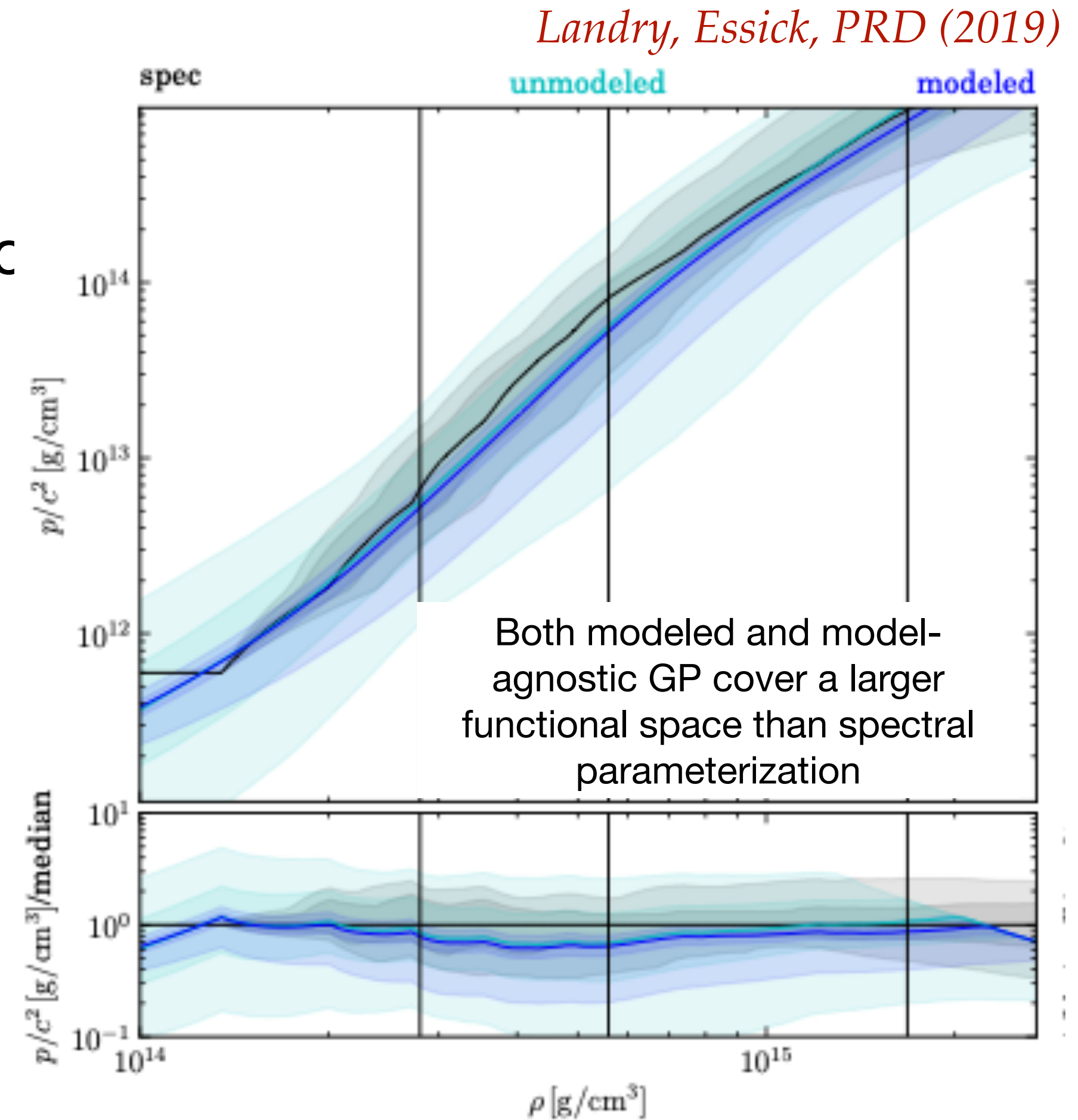
- **This work**: agnostic limit + collection of nuclear physics models lead to parametrization in $\phi(\log P)$:

$$\mu_i(\log p_i) = a - 2(\log p_i - 32.7), \text{ hadronic: } a = 5.5$$

- Covariance matrix

$$\Sigma^{ij} = K_{se}^{ij} + K_{wn}^{ij} = \sigma^2 \exp\left(\frac{x_i - x_j}{2l^2}\right) + \sigma_{wn}^2(x)\delta(x_i - x_j)$$

- Choose $l = \sigma = 1$ following Miller et al. AJP 2021



Constraints on n_B^{TOV}

Preliminary. DM, J. Noronha-Hostler, N. Yunes, C. Miller

Left: total count per bin

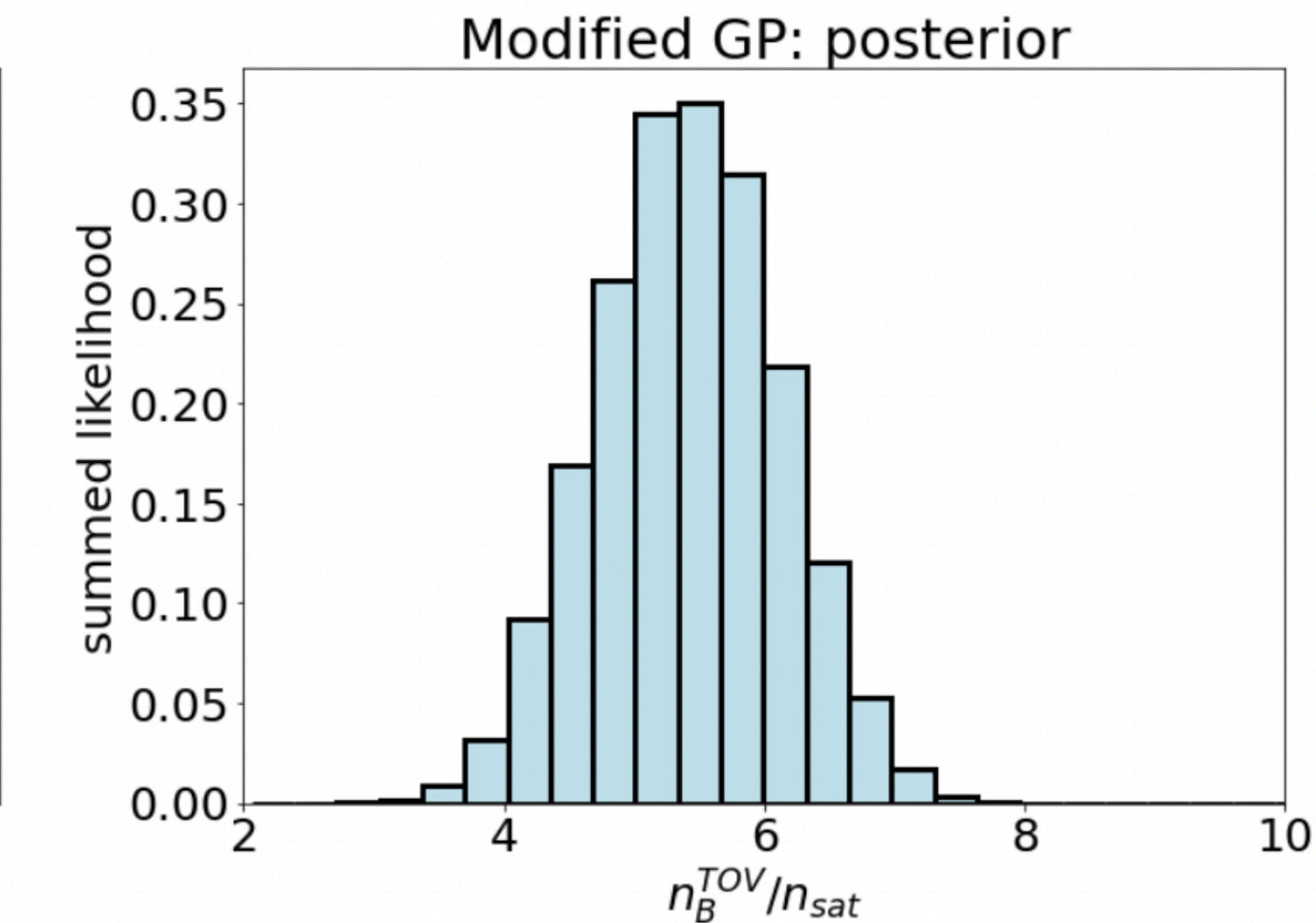
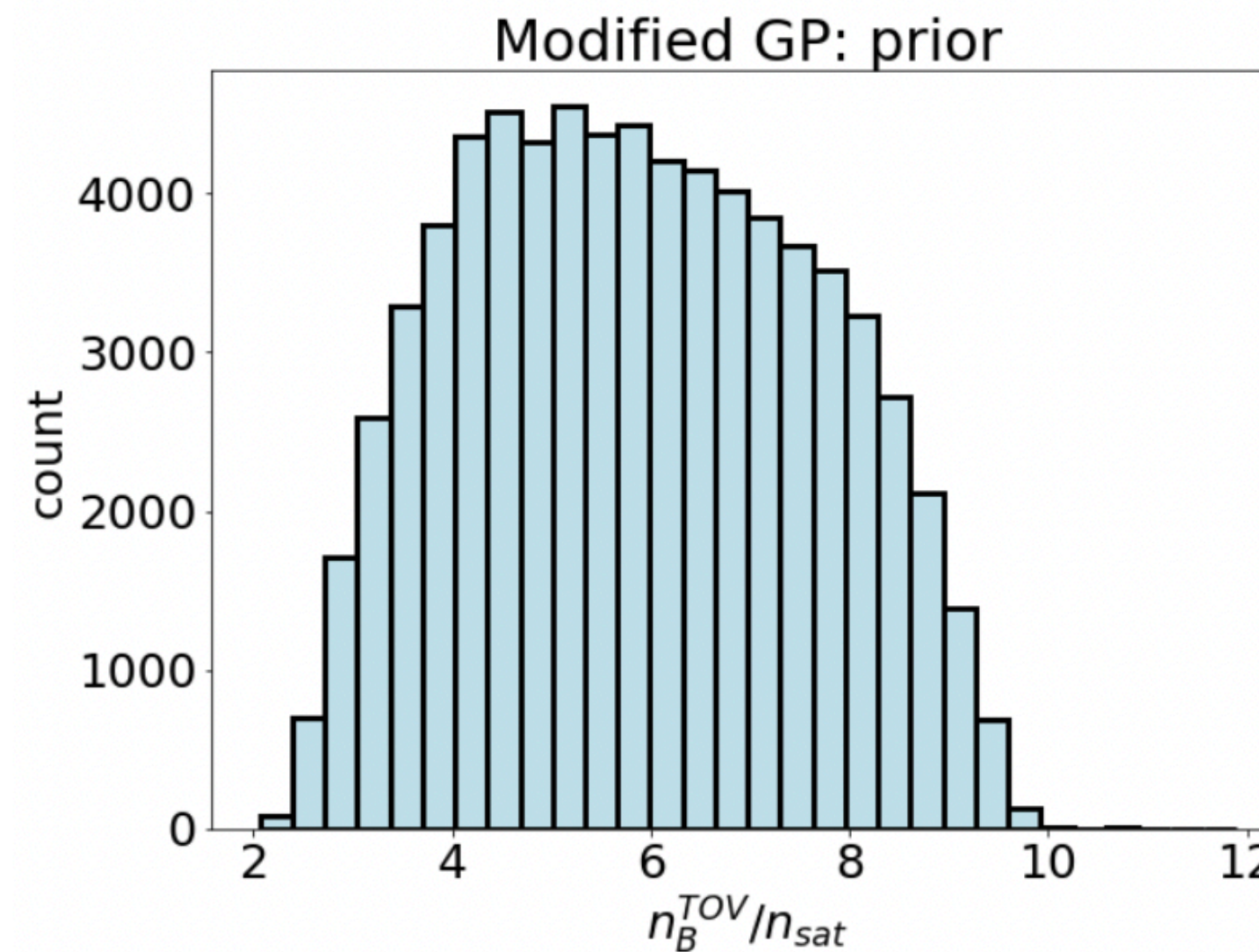
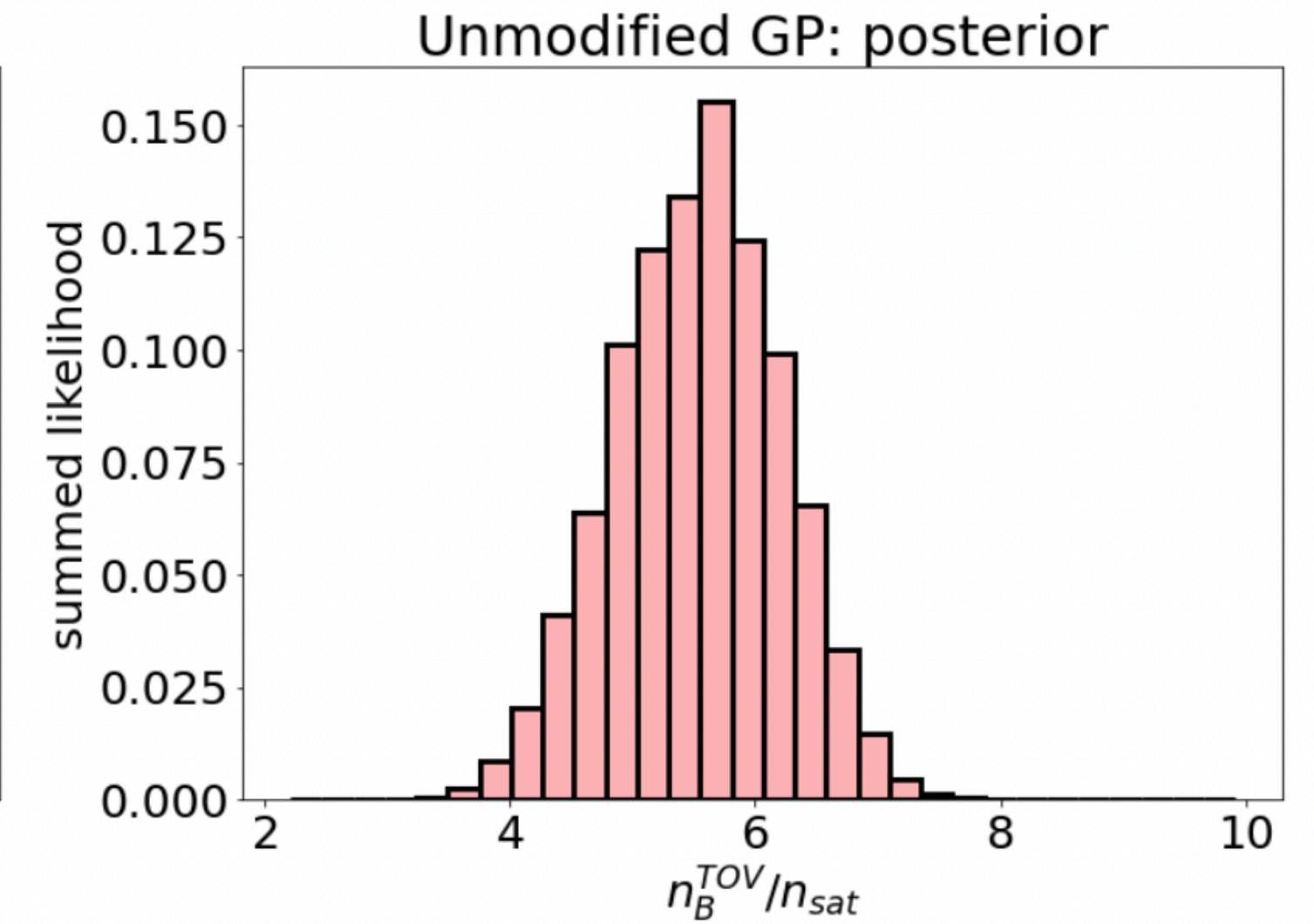
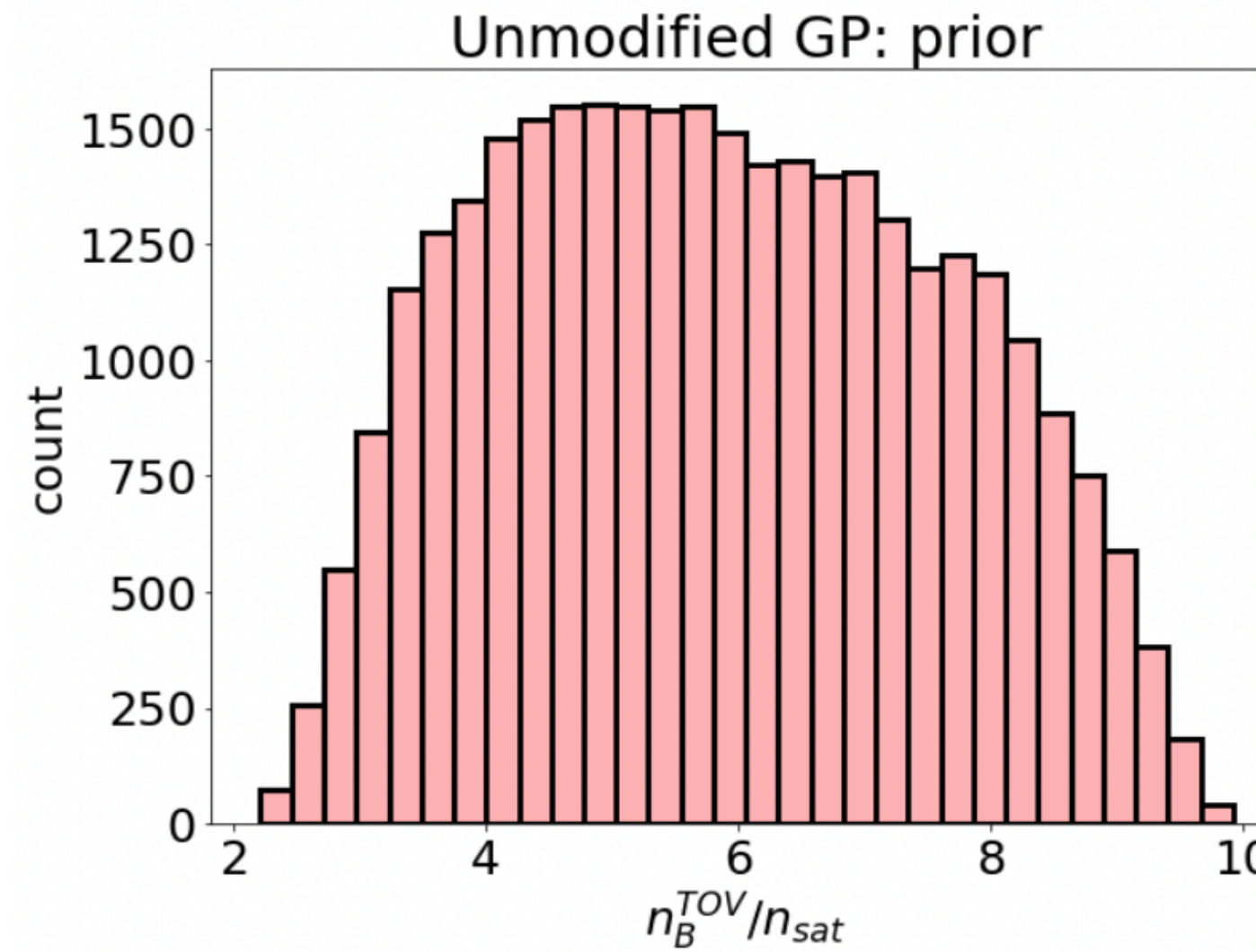
Right: summed likelihood per bin (not normalized)

- **General agreement:**

$$4n_{sat} \lesssim n_B^{TOV} \lesssim 8n_{sat}$$

- **Modified GP: peaks at slightly lower n_B^{TOV}**

- **Likely due to strong phase transitions**



$$n_B^{TOV} - n_B(c_s^2 \max)$$

