



# CLFV at the EIC and LHC vs low-energy

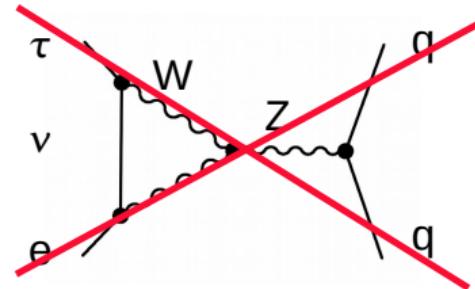
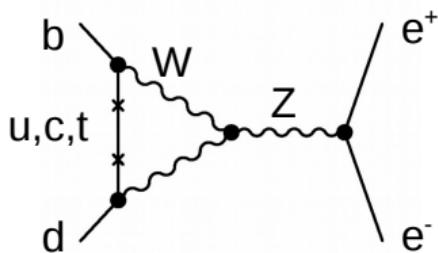
Emanuele Mereghetti

Electroweak and Beyond the Standard Model Physics at the EIC

February 14<sup>th</sup>, 2024, Seattle.

with K. Fuyuto, V. Cirigliano, C. Lee, B. Yan, S. Gonzalez-Solis, F. Delzanno

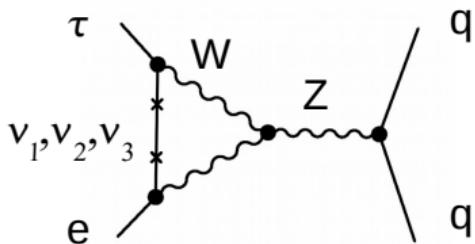
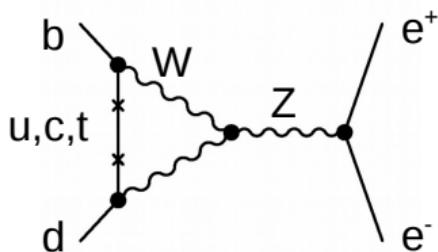
## Charged lepton flavor violation



- mismatch between quark weak and mass eigenstates  $\implies$  quark family number is not conserved  
✓ visible in several rare  $\Delta F = 1$  and  $\Delta F = 2$  processes
- in minimal SM with massless neutrinos, no such mismatch

lepton family (LF) is exactly conserved

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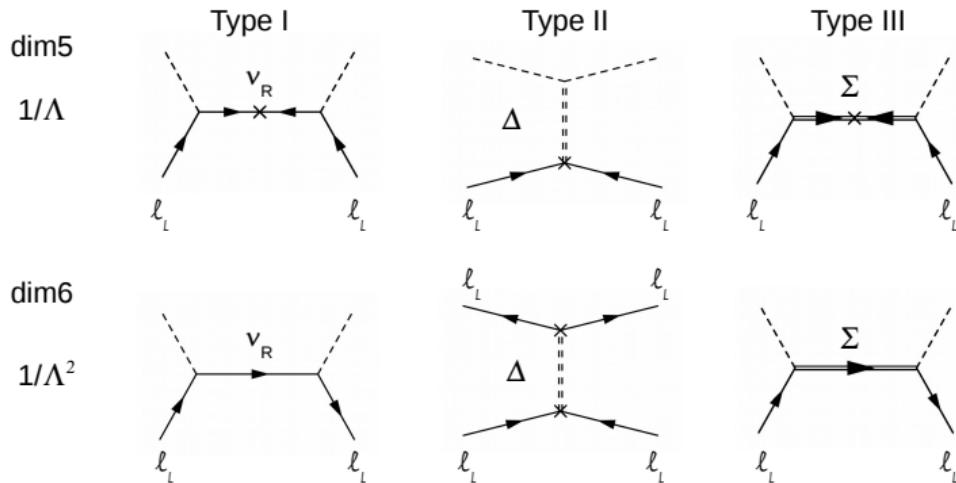
but neutrino have masses!

- LF is broken in neutrino sector
- charged LFV highly suppressed by GIM mechanism

$$\text{BR} \sim \left( \frac{m_\nu}{m_W} \right)^4 \sim 10^{-44}$$

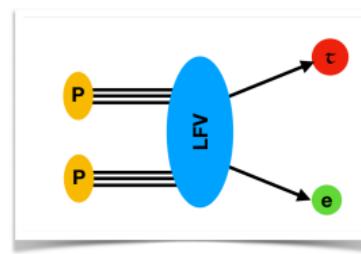
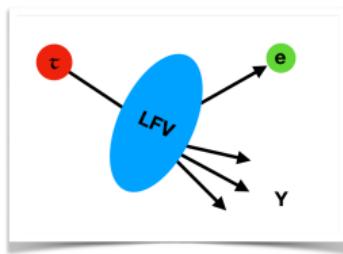
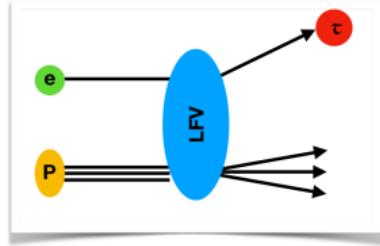
S. Petcov, '77; W. Marciano and A. Sanda, '77

## Charged lepton flavor violation



- ... however, models that explain  $m_\nu$  usually introduce new CLFV at tree or loop level
- e.g. type I, II and III see-saw A. Abada, C. Biggio, F. Bonnet, M. B. Gavela, T. Hambye, '08
- and a variety of models from leptoquarks, to  $Z'$ , to SUSY
- CLFV experiments crucial to falsify TeV origin of  $m_\nu$

## CLFV at low- and high-energy

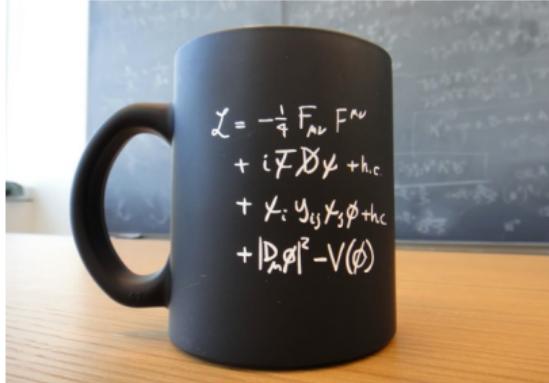


1.  $\mu, \tau$  and meson decays
2.  $p\bar{p}$  collisions
3.  $e p$  collisions

$\mu \rightarrow e\gamma, \mu \rightarrow 3e, \tau \rightarrow \ell\gamma, \tau \rightarrow \ell\pi\pi, \tau \rightarrow \ell K\pi, B \rightarrow \pi\tau\ell, \dots$   
 $p\bar{p} \rightarrow \ell\ell', h \rightarrow \ell\ell', t \rightarrow q\tau e \dots$   
at HERA and the upcoming EIC

M. Gonderinger and M. R. Musolf, '10; HERA collaboration, '11; T. Husek, K. Monsalvez-Pozo, J. Portoles, '20, ...

# The Standard Model Effective Field Theory



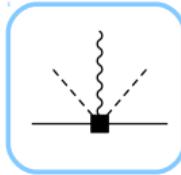
Study CLFV at EIC within EFT framework

- SM fields, no new light degrees of freedom (but easy to add new particles, e.g.  $\nu_R$ )
- local  $SU(3)_c \times SU(2)_L \times U(1)_Y$  invariance
- organize them in a power counting based on canonical dimension

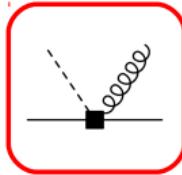
1. no CLFV at dim. 4

2. GIM suppression at dim. 5,  $\text{BR} \sim (m_\nu/m_W)^4$

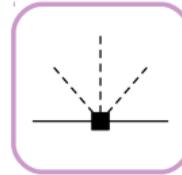
## SMEFT for CLFV



vector/axial currents



dipole



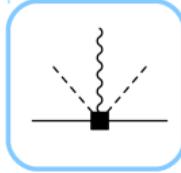
Yukawa

### 1. LFV $Z$ couplings, & $\gamma$ , $Z$ dipole and Yukawa couplings

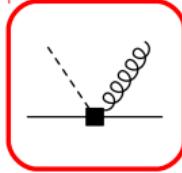
$$\mathcal{L} = -\frac{g}{2c_w} Z_\mu \left[ \left( c_{L\varphi}^{(1)} + c_{R\varphi}^{(1)} \right)_{\tau e} \bar{\tau}_L \gamma^\mu e_L + c_{e\varphi} \bar{\tau}_R \gamma^\mu e_R \right] - \frac{e}{2v} [\Gamma_\gamma^e]_{\tau e} \bar{\tau}_L \sigma^{\mu\nu} e_R F_{\mu\nu} - [Y'_e]_{\tau e} h \bar{\tau}_L e_R + \text{h.c.}$$

$$c = \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right)$$

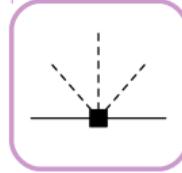
## SMEFT for CLFV



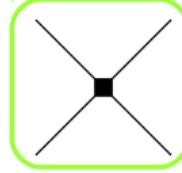
vector/axial currents



dipole



Yukawa



four-fermion

1. LFV  $Z$  couplings, &  $\gamma$ ,  $Z$  dipole and Yukawa couplings
2. leptonic and semileptonic interactions

7 Vector/Axial:  $C_{LQ}^{(1,3)}$ ,  $C_{eu}$ ,  $C_{ed}$ ,  $C_{Lu}$ ,  $C_{Ld}$ ,  $C_{Qe}$

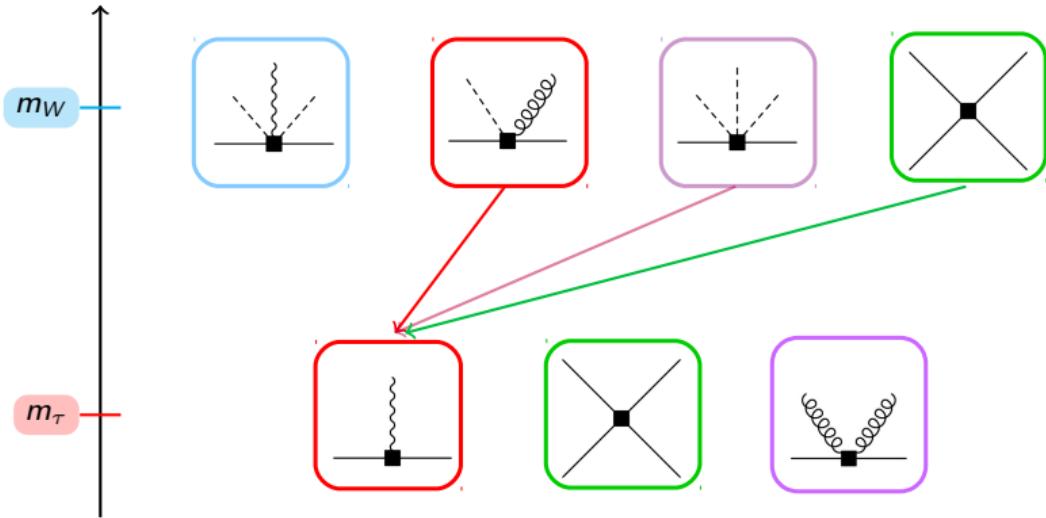
3 Scalar/Tensor:  $C_{LeQu}$ ,  $C_{LeQu}^{(1,3)}$

3 purely leptonic:  $C_{LL}$ ,  $C_{ee}$ ,  $C_{Le}$

- assume generic quark flavor structures ( $> 120$  indep.  $\tau \leftrightarrow e$  couplings)

$$[C_{Ld}]_{\tau e} = \begin{pmatrix} [C_{Ld}]_{dd} & [C_{Ld}]_{ds} & [C_{Ld}]_{db} \\ [C_{Ld}]_{sd} & [C_{Ld}]_{ss} & [C_{Ld}]_{sb} \\ [C_{Ld}]_{bd} & [C_{Ld}]_{bs} & [C_{Ld}]_{bb} \end{pmatrix}$$

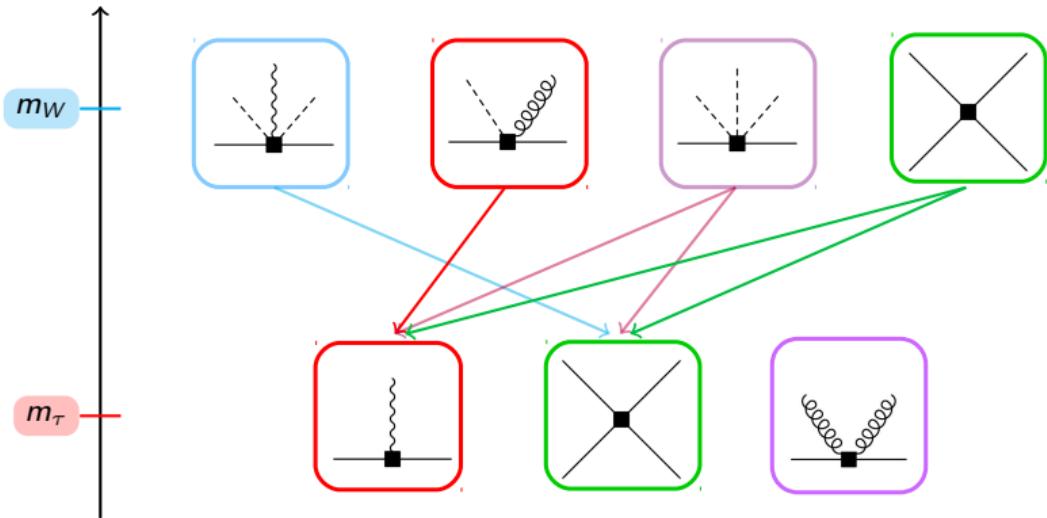
## Connecting observables at different scales



- for  $\mu$  and  $\tau$  decays,  $\mu \rightarrow e$  conversion, integrate heavy particles out
- end up with  $\gamma$  dipole operator

$$\mathcal{L} = -\frac{e}{2\nu} \bar{e}_L^p [\Gamma]_{pr} \sigma^{\mu\nu} e_R^r F_{\mu\nu}$$

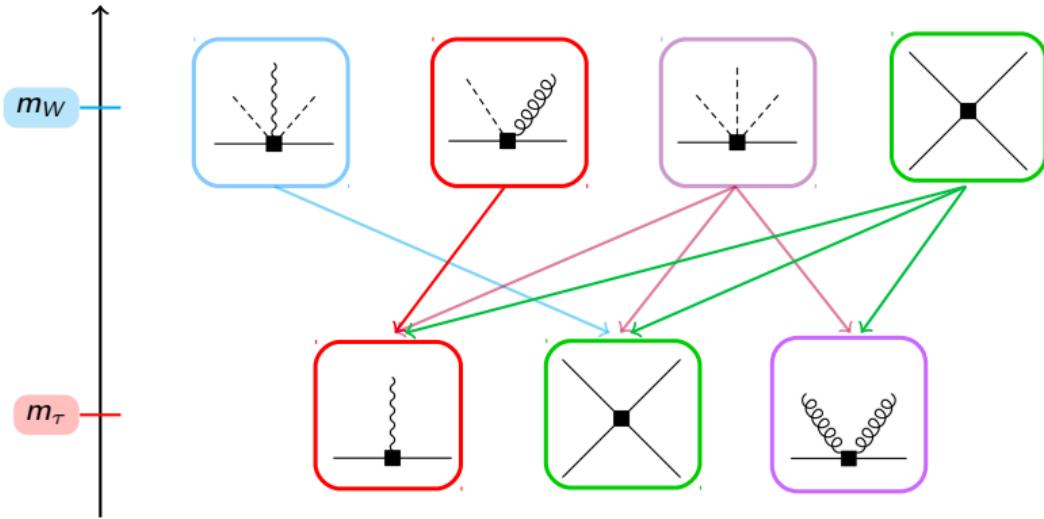
## Connecting observables at different scales



- for  $\mu$  and  $\tau$  decays,  $\mu \rightarrow e$  conversion, integrate heavy particles out
- leptonic and semileptonic ops. with  $u$ ,  $d$  and  $s$  quarks

$$\mathcal{L} = -\frac{4G_F}{\sqrt{2}} L_{prst}^{\Gamma} \bar{e}^p \Gamma e^r \bar{e}^s \Gamma e^t - \frac{4G_F}{\sqrt{2}} C_{prst}^{\Gamma} \bar{e}^p \Gamma e^r \bar{q}^s \Gamma q^t$$

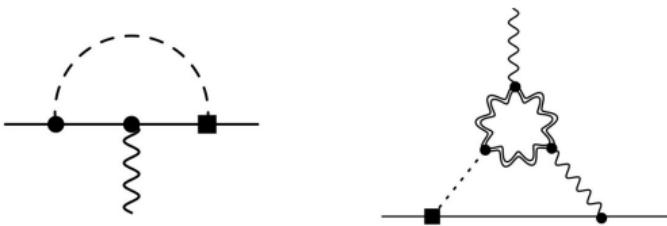
## Connecting observables at different scales



- for  $\mu$  and  $\tau$  decays,  $\mu \rightarrow e$  conversion, integrate heavy particles out
- and gluonic operators

$$\mathcal{L} = \frac{\alpha_s}{4\pi v^3} GG \bar{e}^p [C_{GG}]_{pr} e^r + \dots$$

## Connecting observables at different scales (running is important)

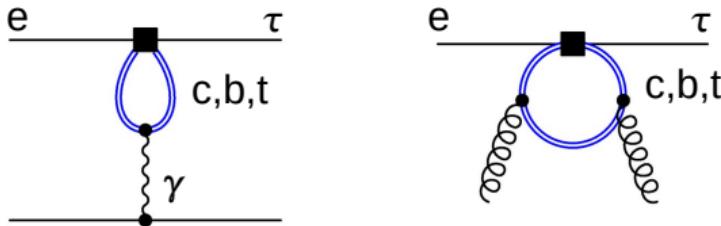


### Lepton bilinears

- $Z$  couplings, photon dipoles  $\implies$  tree level matching ✓
- $Z$  dipole & Higgs coupling run and match onto  $\gamma$  dipole at one or two loops ✓

$$[\Gamma_\gamma^e]_{\tau e}(\mu = 2 \text{ GeV}) = \left( [\Gamma_\gamma^e]_{\tau e} - 2.0 \cdot 10^{-2} [\Gamma_Z^e]_{\tau e} - 6.0 \cdot 10^{-5} (Y')_{\tau e} \right) (\mu = 1 \text{ TeV}).$$

## Connecting observables at different scales (running is important)



### Semileptonic operators

- light-quark 4-fermion operators  $\implies$  tree level matching ✓
- vector/axial  $t$  operators, vector  $b$  and  $c$  operators run into light quark ops. via penguins ✓  
 $C_{\text{VLV}}^{eu}(\mu = 2 \text{ GeV}) = (-10[C_{LQ,U} - C_{Lu}]_{tt} - 2.0[C_{LQ,U} + C_{Lu}]_{tt} + 3.0[C_{LQ,D} + C_{Ld}]_{bb} - 6.8[C_{LQ,U} + C_{Lu}]_{cc}) \cdot 10^{-3}$   
 $C_{\text{VLA}}^{eu}(\mu = 2 \text{ GeV}) = (-27[C_{LQ,U} - C_{Lu}]_{tt}) \cdot 10^{-3}$   
✗ very suppressed contribs. from **axial**  $b$  and  $c$  ops
- scalar/tensor operators run into dipole and match onto dim-7 glue ops.

$$\Gamma_\gamma^e(\mu = 2 \text{ GeV}) = -0.46 \left[ C_{LeQu}^{(3)} \right]_{tt} + 6.5 \cdot 10^{-4} \left[ C_{LeQu}^{(1)} \right]_{tt} - 2.0 \cdot 10^{-3} \left[ C_{LeQu}^{(3)} \right]_{cc} + 2.9 \cdot 10^{-6} \left[ C_{LeQu}^{(1)} \right]_{cc}$$

## Constraints on $\tau \rightarrow e$ transitions

## $\tau$ and $B$ CLFV decays

Decay mode	$V$ $q^{(0)} q^{(1)} s \, c \, b$	$A$ $q^{(0)} q^{(1)} s \, c \, b$	$S$ $q^{(0)} q^{(1)} s \, c \, b$	$P$ $q^{(0)} q^{(1)} s \, c \, b$	$T$ $u \, c$
	$ds \ db \ sb \ cu$	$cu$			
$\tau \rightarrow e\gamma$					✓✓
$\tau \rightarrow e\ell^+\ell^-$	✓✓				
$\tau \rightarrow e\pi^0$		✓	✓		
$\tau \rightarrow e\eta, \eta'$	✓	✓	✓		
$\tau \rightarrow e\pi^+\pi^-$	✓✓	✓✓	✓✓✓✓	✓✓✓✓✓	✓
$\tau \rightarrow eK^+K^-$	✓✓✓✓✓✓	✓✓✓✓✓✓	✓✓✓✓✓✓	✓✓✓✓✓✓	✓✓
$J/\psi \rightarrow \tau e$	✓				✓
$\Upsilon \rightarrow \tau e$	✓				
$\tau \rightarrow eK_S^0$				✓	
$\tau^- \rightarrow e^- K\pi$	✓				
$B^0 \rightarrow e\tau$		✓			
$B^+ \rightarrow \pi^+ e\tau$	✓		✓		
$B^+ \rightarrow K^+ e\tau$	✓		✓	✓	

✓ = tree    ✓ = loop

- $\tau$  branching ratios in the  $\sim 10^{-7}$ - $10^{-8}$  range
- non-perturbative input mostly under control (some model dep. in  $K^+K^-$ )

A. Celis, V. Cirigliano, E. Passemar, '14,    V. Cirigliano, A. Crivellin, M. Hoferichter, '18  
E. Passemar *private comm.*,    K. Beloborodov, V. Druzhinin, S. Serednyakov, '19

- $B$  branching ratios  $\sim 10^{-5}$
- $f_B, f_{+,0}(B \rightarrow \pi, K)$  well determined from LQCD

## $\tau$ and $B$ CLFV decays

Decay mode	$V$ $q^{(0)} q^{(1)}$ $s \ c \ b$	$A$ $q^{(0)} q^{(1)}$ $s \ c \ b$	$S$ $q^{(0)} q^{(1)}$ $s \ c \ b$	$P$ $q^{(0)} q^{(1)}$ $s \ c \ b$	$T$ $u \ c$
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$\tau \rightarrow e\ell^+\ell^-$		✓✓			
$\tau \rightarrow e\pi^0$			✓		
$\tau \rightarrow e\eta, \eta'$			✓		
$\tau \rightarrow e\pi^+\pi^-$	✓	✓✓			
$\tau \rightarrow eK^+K^-$	✓	✓✓✓✓✓			
$J/\psi \rightarrow \tau e$	✓				
$\Upsilon \rightarrow \tau e$	✓				
	$ds \ db \ sb \ cu$	$cu$			
$\tau \rightarrow eK_S^0$			✓		
$\tau^- \rightarrow e^- K\pi$	✓				
$B^0 \rightarrow e\tau$			✓		
$B^+ \rightarrow \pi^+ e\tau$	✓				
$B^+ \rightarrow K^+ e\tau$	✓				

✓ = tree      ✓ = loop

1.  $uu, dd, ss$  components of all Dirac structures well constrained by multiple channels
  - V isoscalar  $uu + dd$  gives small and uncertain contrib. to  $\tau \rightarrow eKK$

## $\tau$ and $B$ CLFV decays

Decay mode	$V$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$A$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$S$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$P$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$T$ $u \; c$
	$ds \; db \; sb \; cu$	$cu$			
$\tau \rightarrow e\gamma$					✓✓
$\tau \rightarrow e\ell^+\ell^-$	✓✓				
$\tau \rightarrow e\pi^0$		✓	✗✗		
$\tau \rightarrow e\eta, \eta'$		✓	✗✗		
$\tau \rightarrow e\pi^+\pi^-$	✓✓✓✓✓✓		✗✗		
$\tau \rightarrow eK^+K^-$	✓✓✓✓✓✓		✗✗		
$J/\psi \rightarrow \tau e$	✓		✗✗		
$\Upsilon \rightarrow \tau e$	✓				
	$ds \; db \; sb \; cu$	$cu$			
$\tau \rightarrow eK_S^0$	✓	✓		✓	
$\tau^- \rightarrow e^- K\pi$					
$B^0 \rightarrow e\tau$		✓			
$B^+ \rightarrow \pi^+ e\tau$	✓		✓		
$B^+ \rightarrow K^+ e\tau$	✓		✓		

✓ = tree    ✓ = loop

2.  $bb, cc$  vectors run into light quark  $V$  via penguins

- $bb, cc$   $S, P$  match onto dim 7 gluonic operators
- no constraints on axial  $cc$  or  $bb$  components

need  $\eta_c \rightarrow e\tau, \eta_b \rightarrow e\tau!$

## $\tau$ and $B$ CLFV decays

Decay mode	$V$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$A$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$S$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$P$ $q^{(0)} q^{(1)}$ $s \; c \; b$	$T$ $u \; c$
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$\tau \rightarrow e\eta, \eta'$		✓	✗✗		
$\tau \rightarrow e\pi^+\pi^-$	✓✓✓✓✓✓		✗✗		
$\tau \rightarrow eK^+K^-$	✓✓✓✓✓✓		✗✗		
$J/\psi \rightarrow \tau e$	✓		✗✗		
$\Upsilon \rightarrow \tau e$	✓				
	$ds \; db \; sb \; cu$	$cu$			
$\tau \rightarrow eK_S^0$	✓	✓		✓	
$\tau^- \rightarrow e^- K\pi$	✓				
$B^0 \rightarrow e\tau$		✓			
$B^+ \rightarrow \pi^+ e\tau$	✓				
$B^+ \rightarrow K^+ e\tau$	✓				

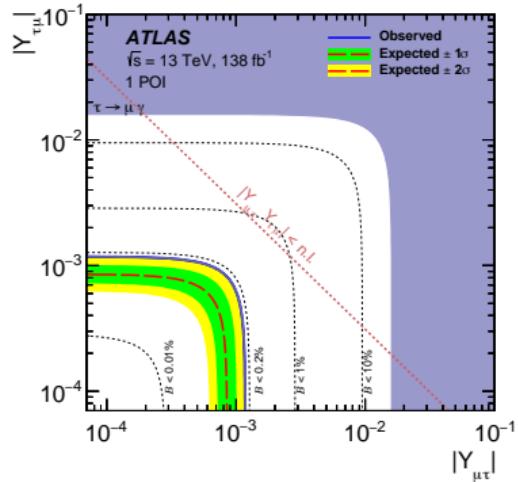
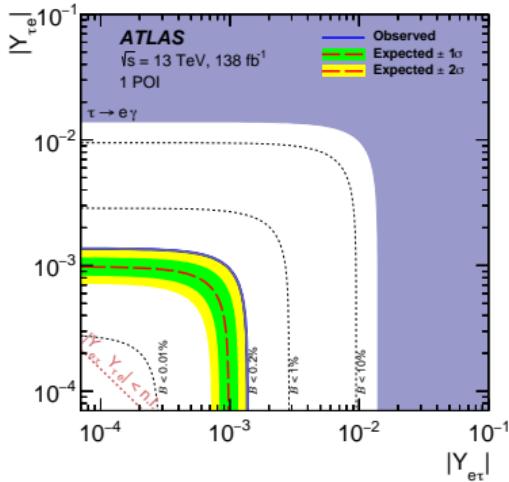
✓ = tree      ✓ = loop

3. strong constraints on  $ds, sd$  from  $\tau \rightarrow eK, \tau \rightarrow eK\pi$

- and on vector/scalar  $bd, bs$  ( $B \rightarrow P\tau e$ ) and axial/pseudoscalar  $bd$  ( $B \rightarrow \tau e$ ) components
- no constraints on  $cu$ , axial and pseudoscalar  $sb, bs$ ,

$B_s \rightarrow e\tau$  at Belle II and LHCb  
 $D \rightarrow e\tau$  at LHCb and BESIII

## Z, Higgs and top decays



ATLAS collaboration, arXiv:2302.05225

- $Z \rightarrow \tau e$  studied at LEP and LHC, LHC giving strongest bounds

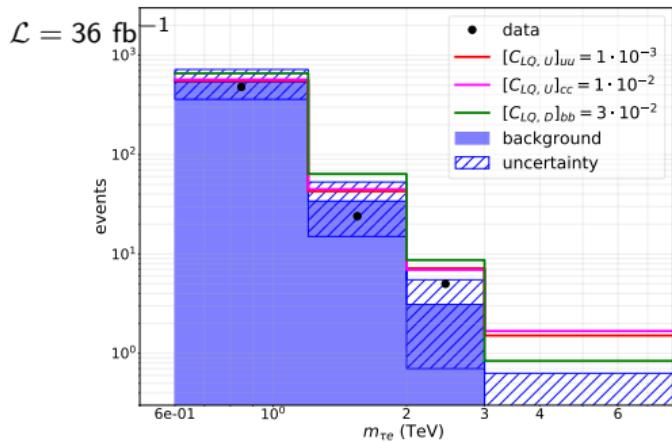
$$\text{BR}(Z \rightarrow e\tau) < 5.0 \cdot 10^{-6} \implies |c_{L\varphi}^{(1)} + c_{L\varphi}^{(3)}| < 7.8 \cdot 10^{-3}$$

- limit on  $H \rightarrow \tau e$  from LHC

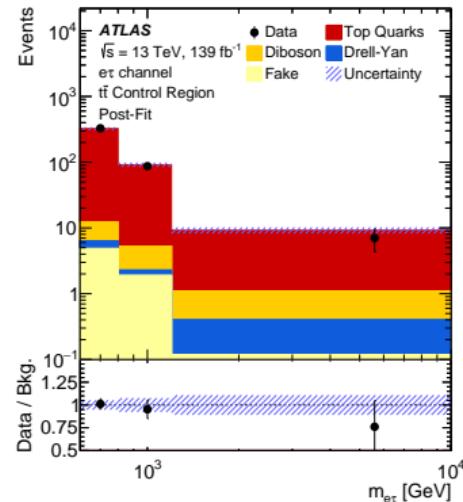
$$\text{BR}(H_0 \rightarrow e\tau) < 2.0 \cdot 10^{-3} \implies |Y'_{e\tau, \tau e}| < 1.3 \cdot 10^{-3}$$

- ATLAS looked for  $t \rightarrow qll'$ ,  $C \sim 0.1$  bounds

## High invariant mass CLFV Drell-Yan



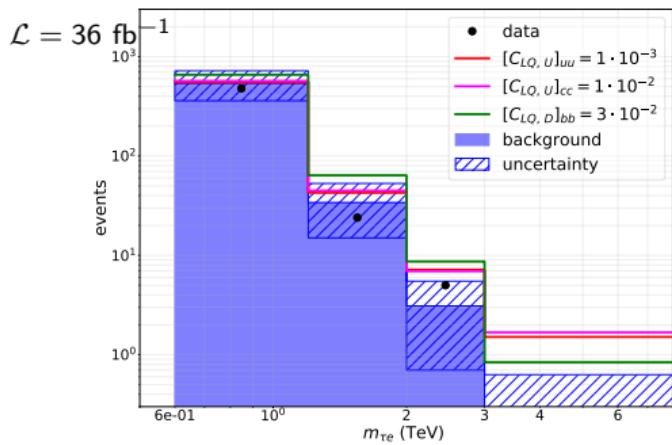
ATLAS arXiv:1807.06573



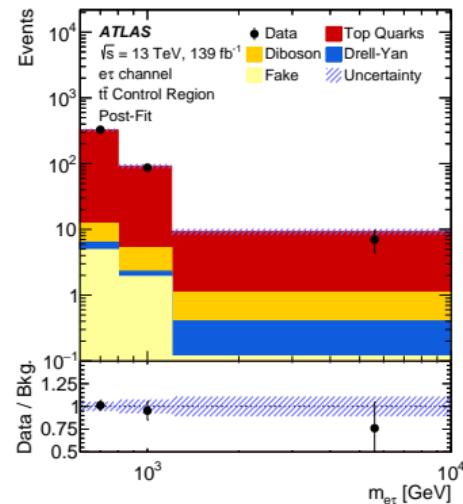
ATLAS arXiv:2307.08567

- ATLAS published  $pp \rightarrow \tau e$  results, with hadronic  $\tau$ , framed as  $Z'$  searches  
6 invariant mass bins from 100 GeV to 3 TeV, compatible with background only
- if  $\Lambda \gtrsim 3 - 4$  TeV, can be reframed as constraints on four-fermion operators as at low-energy
- simulate SMEFT operators at NLO in QCD, with POWHEG + Pythia8 + Delphes

## High invariant mass CLFV Drell-Yan



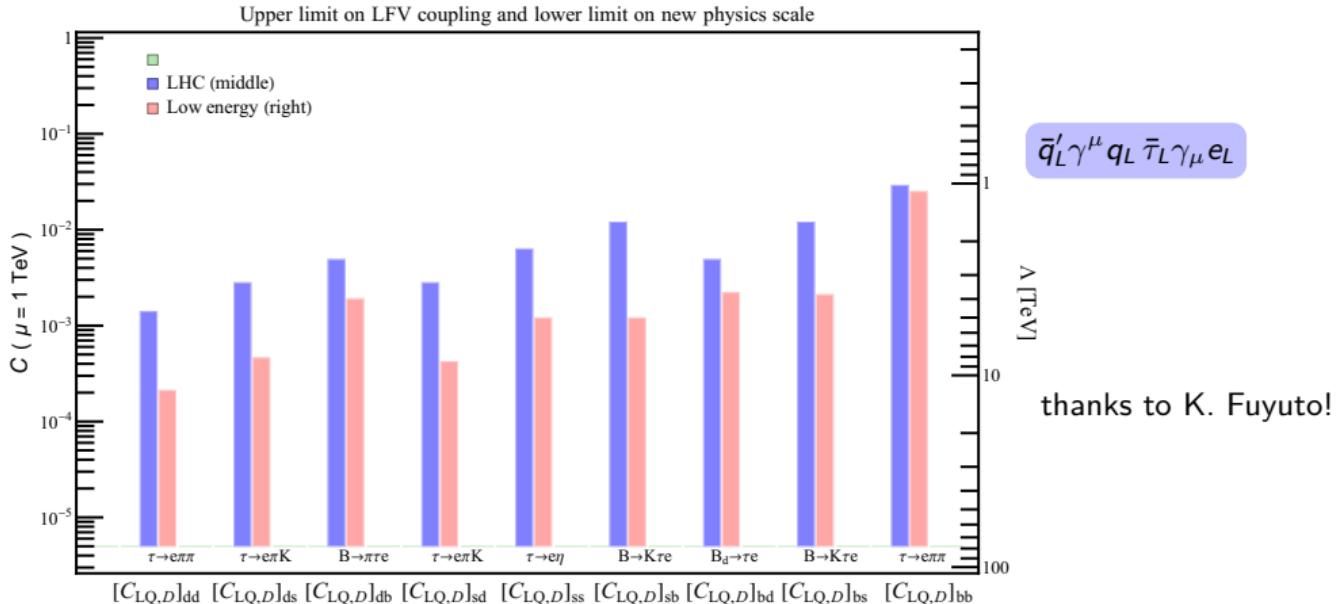
ATLAS arXiv:1807.06573



ATLAS arXiv:2307.08567

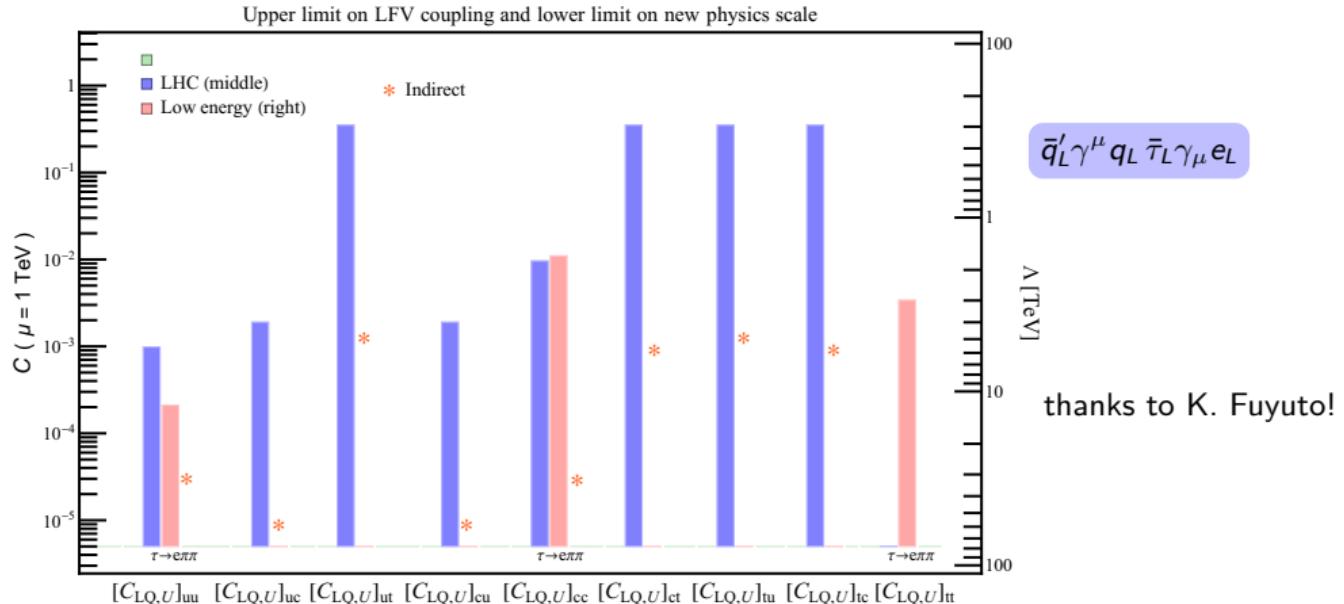
- signal from four-fermion enhanced at large  $m_{\tau e}$ , indep. of Lorentz structure
- $C_{\tau eq; q_j} \lesssim 10^{-3}$  for valence quarks,  $\lesssim 3 \cdot 10^{-2}$  for  $b$  quarks
- new '22 and '23 ATLAS and CMS analysis with full luminosity and better backgrounds

## Summary of existing constraints



- all channels with  $d$ -type quarks sector well constrained by low-energy
- LHC in striking distance in  $db$ ,  $ss$ , and better in  $bb$  channel

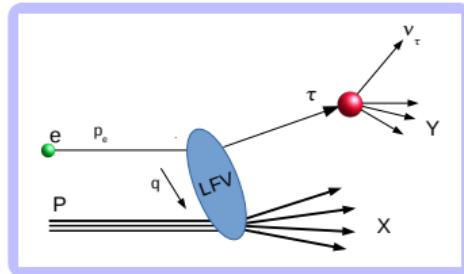
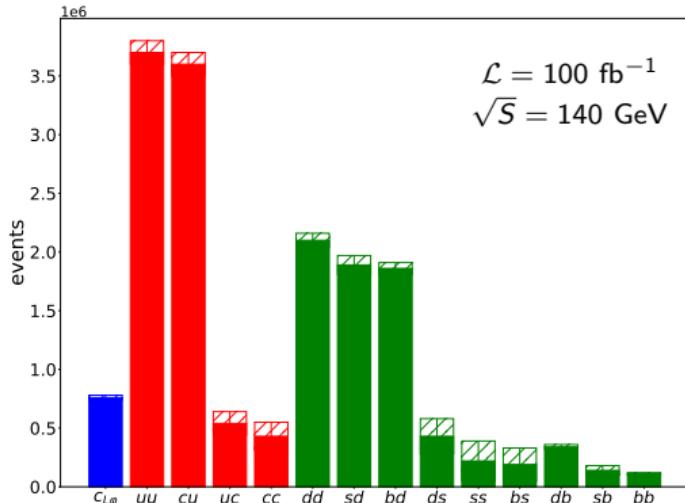
## Summary of existing constraints



- strong constraints on  $t\bar{t}$  couplings from  $\tau \rightarrow e\pi\pi$
- more fragmentary info for  $u$ -type FCNC operators
- similar results for other Lorentz structures

## **CLFV at the EIC**

## CLFV Deep Inelastic Scattering



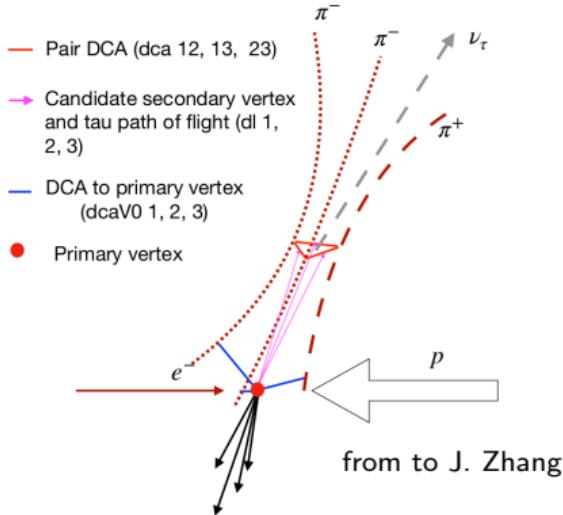
Left handed  $\tau_L, e_L$

Left handed  $u_L, d_L$

NNPDF31\_lo\_as\_0118

- most cross sections in the 1-10 pb range, for  $\Lambda = v$ ,
- heavy flavors  $c, b$  suppressed by factor ten
- large PDF uncertainties for heavy-flavor-initiated processes, need NLO corrections
- is a NLO + parton shower framework needed/available for EIC?

## $\tau$ at the EIC



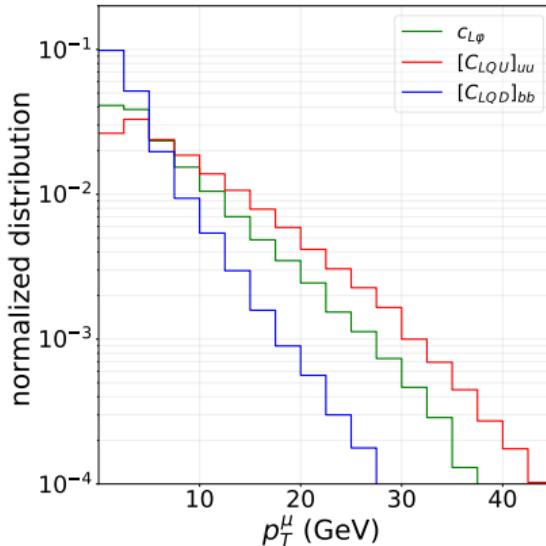
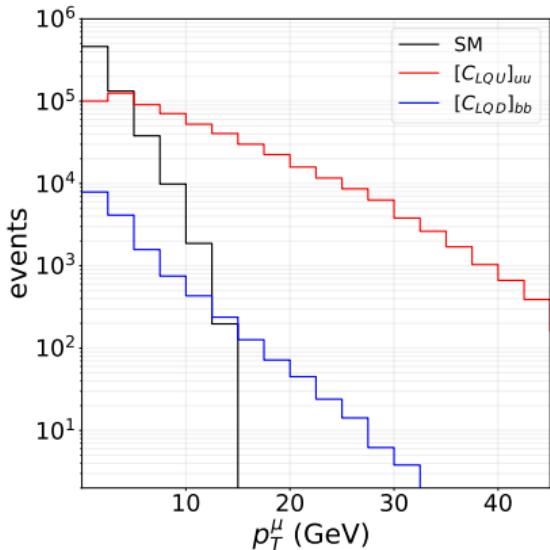
$$1. \text{ } ep \rightarrow \tau X \rightarrow e + \cancel{E} + X$$

$$2. \text{ } ep \rightarrow \tau X \rightarrow \mu + \cancel{E} + X$$

$$3. \text{ } ep \rightarrow \tau X \rightarrow X_h + \cancel{E} + X$$

- (substantial) background from standard NC and CC DIS
- generate  $10^8$  SM &  $10^6$  SMEFT events with Pythia8 + Delphes for EIC  
using Delphes card by M. Arratia and S. Sekula

## Muon channel



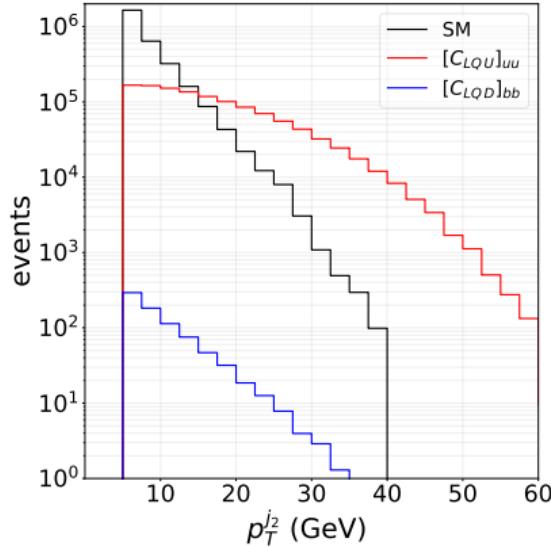
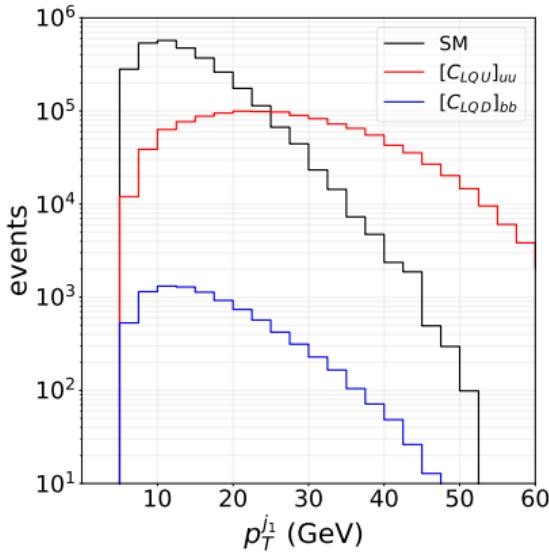
- too much background in  $e$  channel,  $\mu$  channel much more promising!
- in SM,  $\mu$  come from hadron decays, typically at small  $p_T$

$$p_T^\mu > 10 \text{ GeV}, \quad \cancel{E}_T > 15 \text{ GeV}, \quad p_T^{j_1} > 20 \text{ GeV}$$

eliminates all SM background

- smaller signal efficiency for  $Z$  couplings, heavy quarks
- ? assumed same performance for muon and electrons, realistic?

## Hadronic channel



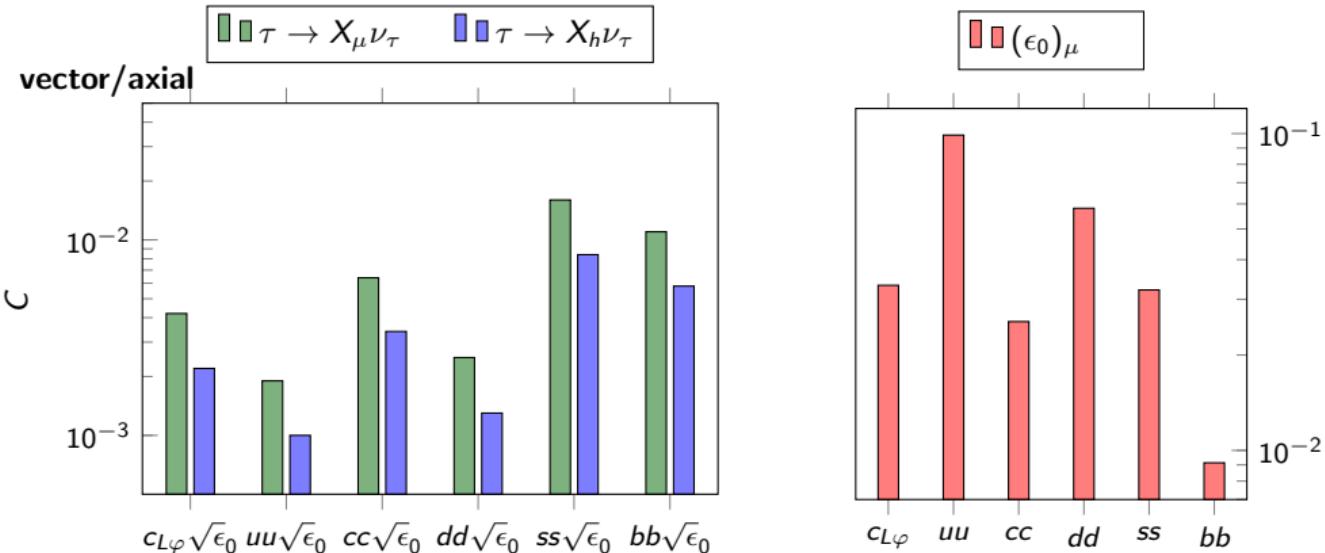
- one “ $\tau$ -tagged” jet, with 1 or 3 charged tracks, and close in  $\phi$  to  $\not{E}_T$
- recoils against a second jet, no charged leptons in final state

$$p_T^{j_1} > 20 \text{ GeV}, \quad p_T^{j_2} > 15 \text{ GeV}, \quad \not{E}_T > 15 \text{ GeV} \implies \epsilon_{SM} = 10^{-5}$$

does not quite kill all SM background

? cuts severely suppress heavy quark signals, can be improved with  $b$ -tagging?

## EIC sensitivity to CLFV



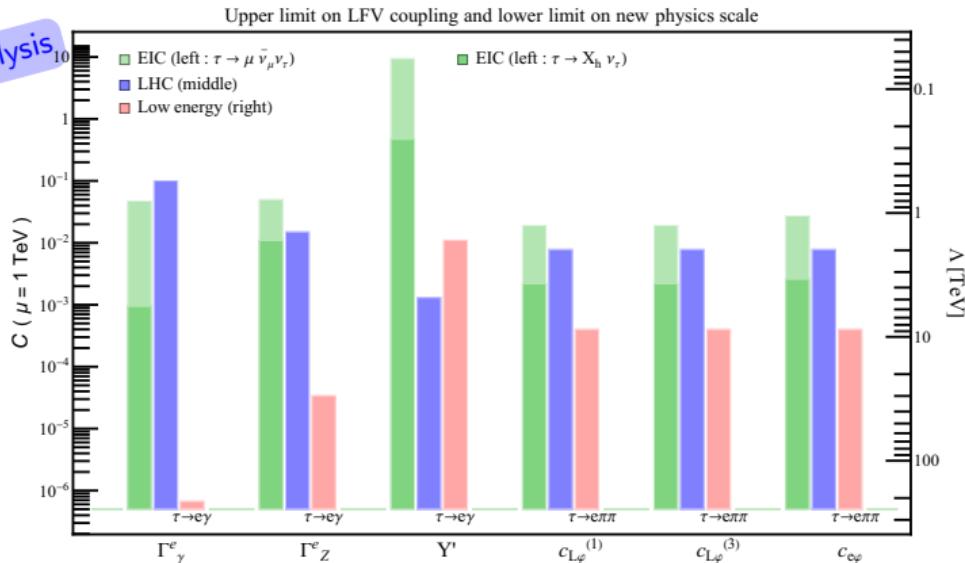
- $\epsilon_{n_b}$ : signal efficiency for the cuts to reduce the SM background to  $n_b$  events

At EIC with  $\mathcal{L} = 100 \text{ fb}^{-1}$ ,  $\sqrt{S} = 140 \text{ GeV}$ ,  $n_{\text{obs}} = n_b$

- EIC can probe couplings at the  $10^{-3} - 10^{-2}$  level in  $\mu$  channel  
can improve with “smarter” hadronic channel analysis
- no suppression for off-diagonal, e.g.  $C_{cu} \sim C_{uu}$

# Constraints on $\tau \leftrightarrow e$ transitions: dipole, Yukawa and $Z$

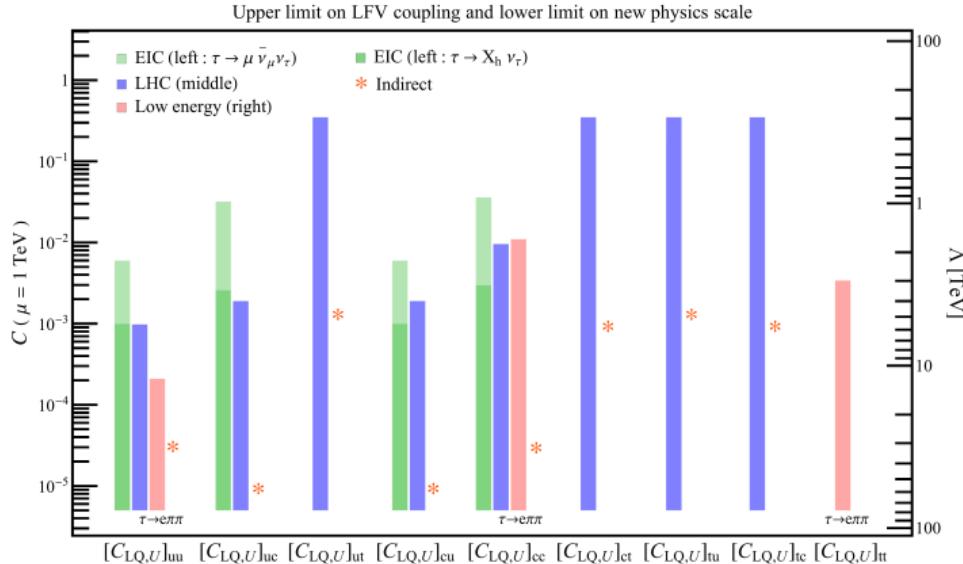
single coupling analysis



V. Cirigliano, K. Fuyuto , C. Lee, EM, B. Yan, '21

- $\gamma$  and  $Z$  overwhelming constrained by  $\tau \rightarrow e\gamma$
- strong direct LHC bound on  $Y'$
- $\tau \rightarrow e\pi\pi$  dominates  $Z$  couplings

## Constraints on $\tau \leftrightarrow e$ transitions: four-fermion operators



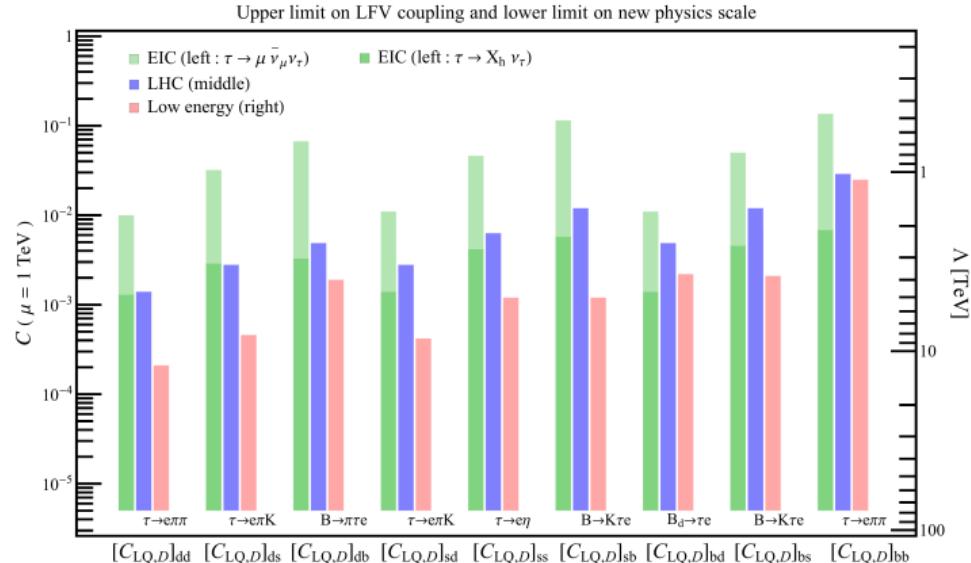
uu  $\tau \rightarrow e\pi\pi$  stronger by  $\sim 5$ , EIC competitive with  $\tau \rightarrow e\pi$  & LHC

cc low-energy loop suppressed, EIC can do better

tt strong constraints from  $\tau$  decays

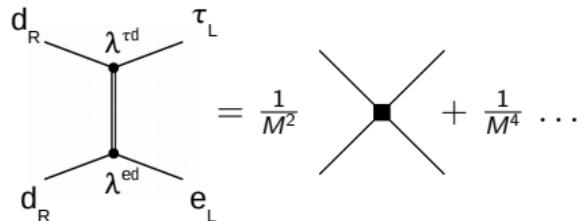
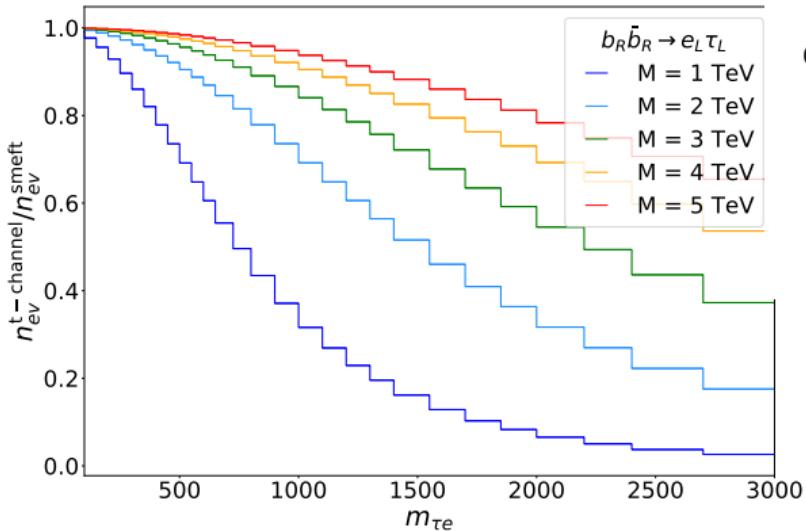
- colliders are only probes of  $u$ -type off-diagonal

## Constraints on $\tau \leftrightarrow e$ transitions: four-fermion operators



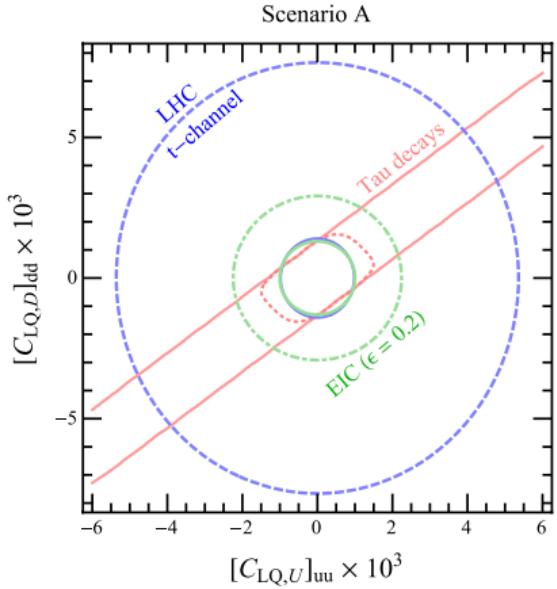
- EIC can compete on  $bb$  component and with  $B$  decays if we improve  $b$  quark analysis

## LHC vs EIC, SMEFT vs models



- LHC vs EIC comparison assumes SMEFT is applicable in DY tail (i.e.  $\Lambda \gg m_{\tau e}$ )
- cross section can be suppressed in BSM models  
e.g.  $t$ -channel exchanges with  $M \sim 1 - 2 \text{ TeV}$
- DY bound weaken by a factor of 2 ( $M = 2 \text{ TeV}$ ) to 5 ( $M = 1 \text{ TeV}$ )
- discovery at EIC and null results at LHC could point to specific (lightish) new physics

## Beyond single coupling



V/A couplings to L leptons & light quarks

$$C_{LQ\,U} = \text{diag}([C_{LQ\,U}]_{uu}, 0, 0)$$

$$C_{LQ\,D} = \text{diag}([C_{LQ\,D}]_{dd}, [C_{LQ\,D}]_{ss}, 0)$$

$$C_{Lu} = \text{diag}([C_{Lu}]_{uu}, 0, 0)$$

$$C_{Ld} = \text{diag}([C_{Ld}]_{dd}, [C_{Ld}]_{ss}, 0)$$

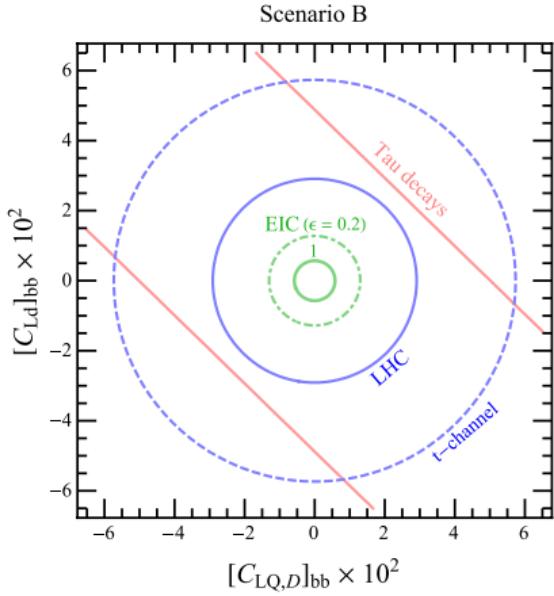
$$c_{L\varphi}$$

- $\pi\pi$  mode dominates, can weaken the limits with multiple couplings
- isoscalar, vector couplings not well constrained,

$$[C_{LQ\,U}]_{uu} + [C_{LQ\,D}]_{dd} + [C_{Lu}]_{dd} + [C_{Ld}]_{dd}$$

- no free directions at colliders!

## Beyond single coupling



V/A couplings to L leptons &  $d$ -type quarks

$$C_{LQD} = \text{diag}([C_{LQD}]_{dd}, [C_{LQD}]_{ss}, [C_{LQD}]_{bb})$$

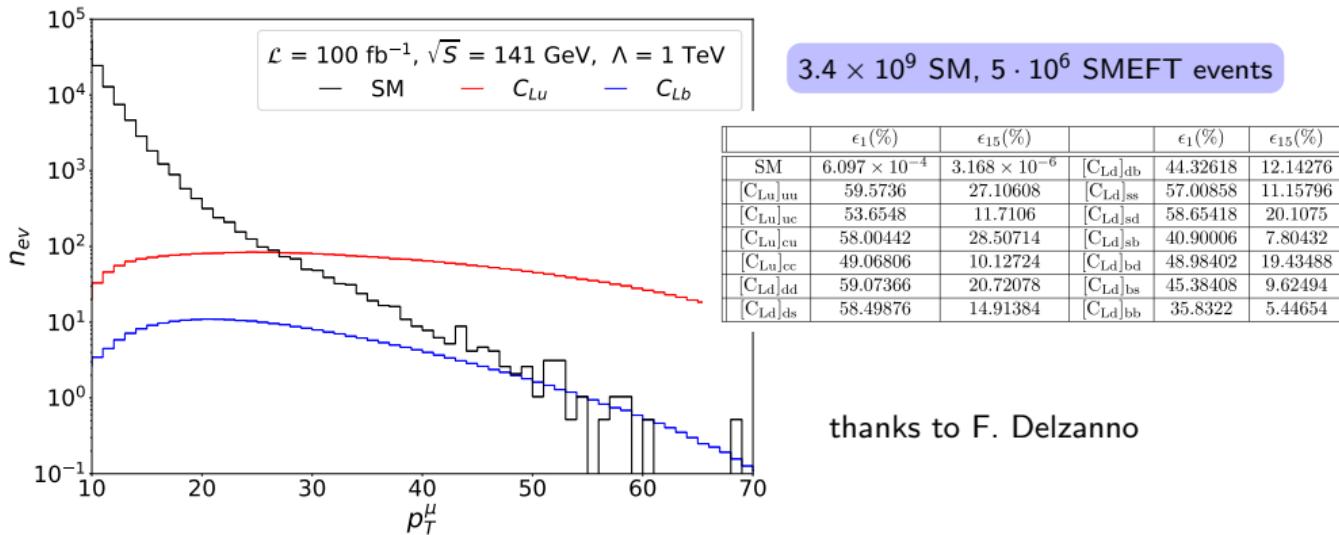
$$C_{Ld} = \text{diag}([C_{Ld}]_{dd}, [C_{Ld}]_{ss}, [C_{Ld}]_{bb})$$

- contributions to hadronic  $\tau$  decays cancel for  $[C_{Ld}]_{bb} \sim -[C_{LQD}]_{bb}$
- $\tau \rightarrow e\ell^+\ell^-$  weaker than current LHC and project EIC

low energy not sufficient to constrain full parameter space  
need complementary info!

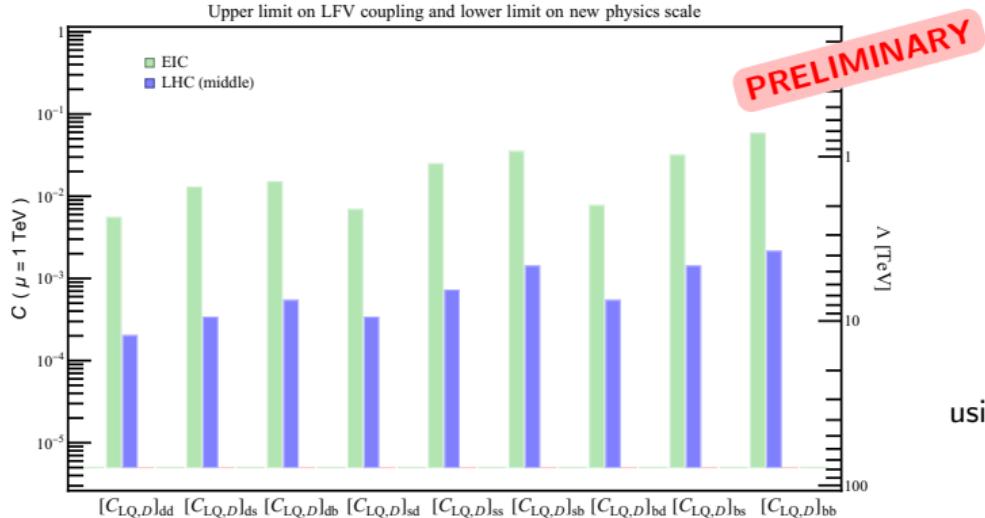
$e \rightarrow \mu$  at the EIC

## $e \rightarrow \mu$ at the EIC



- simpler analysis (still assuming  $\mu \sim e \dots$ )
- investigated 15 cuts with  $p_T^\mu, p_T^{\text{jet}}$  between 5 and 20 GeV, electron veto between 5 and 10 GeV
- hardest cut leaves about  $\sim 50$  SM events behind
- explored role of  $b$ -tagging to allow for softer cuts for heavy flavors

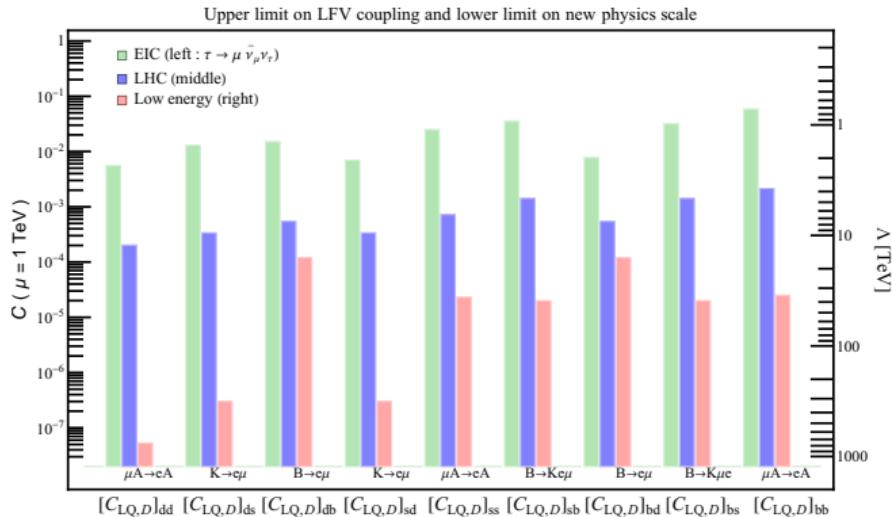
## $e \rightarrow \mu$ at the EIC vs LHC



using CMS arXiv:2205.06709

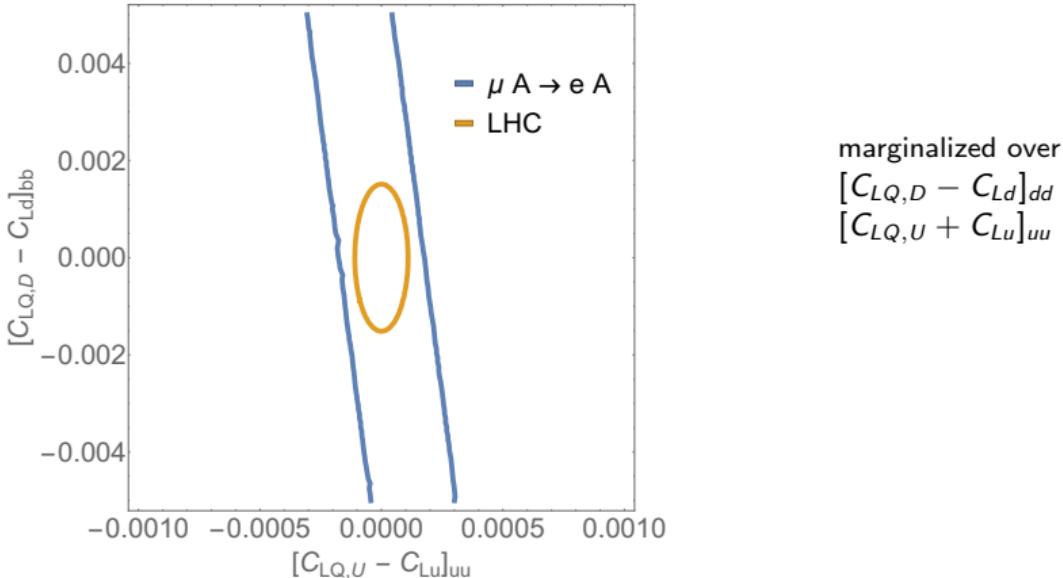
- if SMEFT interpretation is valid, LHC stronger by a factor of 10/20
- and pushing in the  $\Lambda > 10$  TeV regime

## $e \rightarrow \mu$ at the EIC vs LHC and low-energy



- in single coupling analysis, low energy provides stronger constraints on  $\mu \rightarrow e$  interactions
- SI  $\mu \rightarrow e$  conversion in nuclei constrains  $dd$ ,  $ss$  and  $bb$  couplings
- $ss$  suppressed by nucleon strange vector form factor,  $bb$  by electroweak loop,  
still  $100\times$  stronger than LHC/EIC
- $K$ ,  $D$  and  $B$  decays give strong constraints on flavor changing couplings

## Multiple couplings



- spin independent and spin dependent  $eA \rightarrow \mu A$  limits are very strong, but only a few...
- 4 couplings are enough to reveal free directions
- and colliders become competitive on both heavy and light flavors

## Conclusion

- CLFV can unveil/constrain mechanisms of neutrino mass generation
- EIC, LHC,  $B$  factories and  $\mu \rightarrow e$  experiments are complementary especially for heavy flavors and in multiple-coupling scenarios

To do:

- improve EIC calculations and simulations,  
detailed study of heavy quark channels, improve efficiency with  $b$  tagging, study  $e \leftrightarrow \mu$  transitions, ...
- ? can we get away w/o full detector simulations?
- recast ATLAS and CMS analyses in SMEFT language (alongside to benchmark models)
- perform a real global fit & identify unconstrained direction in  $e \leftrightarrow \mu$ ,  $e \leftrightarrow \tau$  and  $\mu \leftrightarrow \tau$  interactions
- extend SMEFT studies to include light sterile neutrinos



## Backup

## The LEFT LNV Lagrangian

- vector-like operators

$$\mathcal{L}_6 = -\frac{4G_F}{\sqrt{2}} \left( C_{VLL}^{eu} \bar{e}_L \gamma^\mu e_L \bar{u}_L \gamma_\mu u_L + C_{VLL}^{ed} \bar{e}_L \gamma^\mu e_L \bar{d}_L \gamma_\mu d_L + C_{VRR}^{eu} \bar{e}_R \gamma^\mu e_R \bar{u}_R \gamma_\mu u_R \right. \\ \left. + C_{VRR}^{ed} \bar{e}_R \gamma^\mu e_R \bar{d}_R \gamma_\mu d_R + C_{VLR}^{ue} \bar{e}_R \gamma^\mu e_R \bar{u}_L \gamma_\mu u_L + C_{VLR}^{de} \bar{e}_R \gamma^\mu e_R \bar{d}_L \gamma_\mu d_L \right. \\ \left. + C_{VLR}^{eu} \bar{e}_L \gamma^\mu e_L \bar{u}_R \gamma_\mu u_R + C_{VLR}^{ed} \bar{e}_L \gamma^\mu e_L \bar{d}_R \gamma_\mu d_R \right),$$

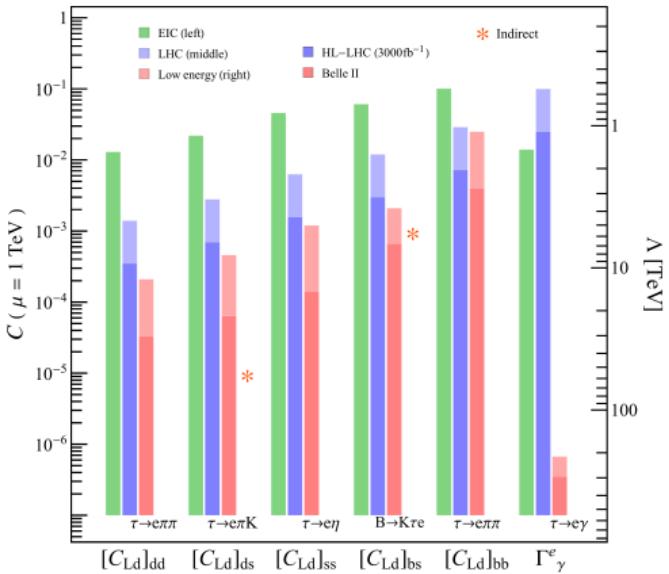
- scalar-tensor type operators

$$\mathcal{L}_6 = -\frac{4G_F}{\sqrt{2}} \left( C_{SRR}^{eu} \bar{e}_L e_R \bar{u}_L u_R + C_{SRR}^{ed} \bar{e}_L e_R \bar{d}_L d_R + C_{TRR}^{eu} \bar{e}_L \sigma^{\mu\nu} e_R \bar{u}_L \sigma_{\mu\nu} u_R \right. \\ \left. + C_{TRR}^{ed} \bar{e}_L \sigma^{\mu\nu} e_R \bar{d}_L \sigma_{\mu\nu} d_R + C_{SRL}^{eu} \bar{e}_L e_R \bar{u}_R u_L + C_{SRL}^{ed} \bar{e}_L e_R \bar{d}_R d_L \right) + \text{h.c.}$$

- vector/axial combinations

$$C_{VLV}^{eq} = \frac{1}{2} (C_{VLR}^{eq} + C_{VLL}^{eq}), \quad C_{VLA}^{eq} = \frac{1}{2} (C_{VLR}^{eq} - C_{VLL}^{eq})$$

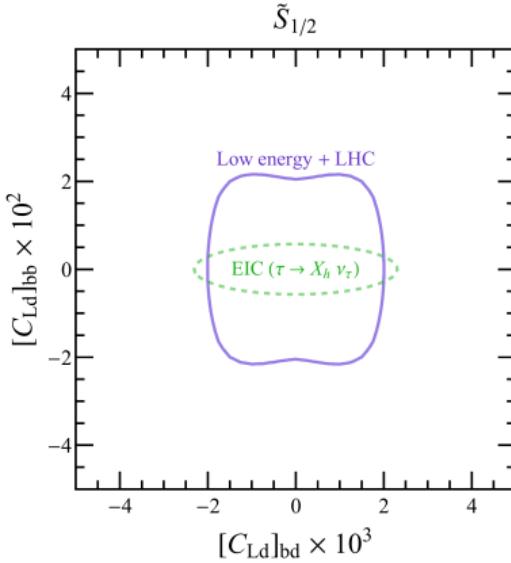
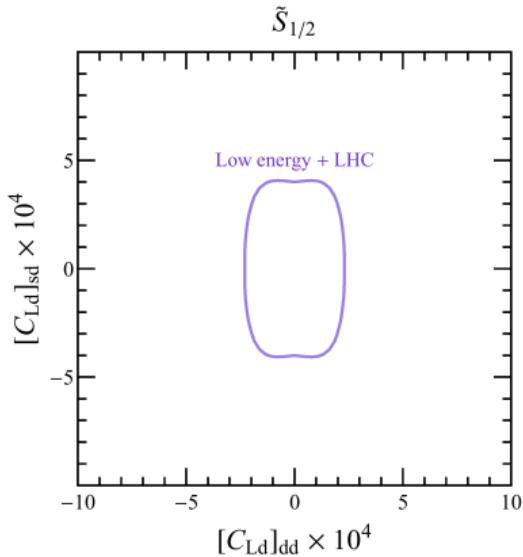
## $\tau \leftrightarrow e$ transitions: future projections



thanks to K. Fuyuto  
arXiv:2203.14919

- Belle-II will improve
- colliders will play an important role in heavy flavor & multi-coupling scenarios

## Leptoquark models



marginalized over remaining couplings

- light-quark components severely constrained by low-energy
- EIC and LHC can improve the  $b$  components

## Polarized cross section

- generic form of polarized cross section

$$\frac{1}{\sigma_0} \frac{d\sigma_{\lambda_e \lambda_T}}{dx dy} = \frac{1}{2} \sum_a \left[ \frac{1 - \lambda_e}{2} (\hat{\sigma}_{LL}^a + \hat{\sigma}_{LR}^a) + \frac{1 + \lambda_e}{2} (\hat{\sigma}_{RL}^a + \hat{\sigma}_{RR}^a) \right] f_a(x, Q^2) .$$

$$+ \frac{1}{2} \sum_a \left[ \frac{1 - \lambda_e}{2} (-\hat{\sigma}_{LL}^a + \hat{\sigma}_{LR}^a) + \frac{1 + \lambda_e}{2} (-\hat{\sigma}_{RL}^a + \hat{\sigma}_{RR}^a) \right] \lambda_T \Delta f_a(x, Q^2) ,$$

- example of  $u$  quarks ( $F_Z = \frac{1}{c_w^4 s_w^4} \frac{Q^4}{(Q^2 + m_Z^2)^2}$ )

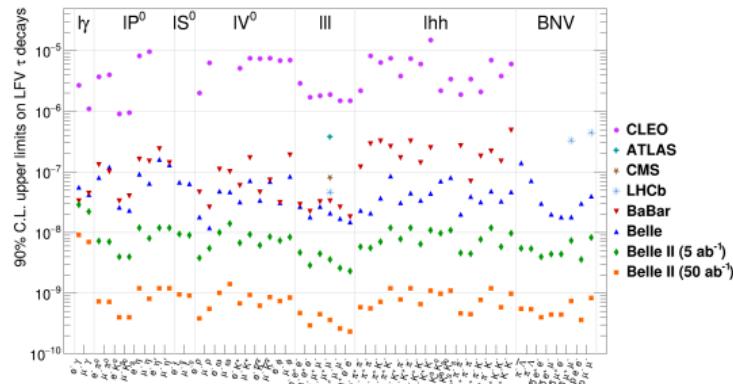
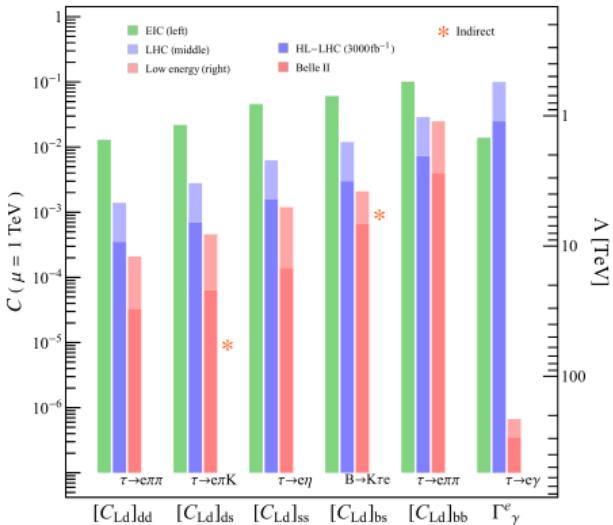
$$\hat{\sigma}_{LL}^{ui} = F_Z \left\{ \left| \left[ c_{L\varphi}^{(1)} + c_{L\varphi}^{(3)} \right]_{\tau e} z_{u_L} + \frac{Q^2 + m_Z^2}{m_Z^2} [C_{LQ}, U]_{\tau eu_i u_i} \right|^2 + \sum_{j \neq i} \left| \frac{Q^2 + m_Z^2}{m_Z^2} [C_{LQ}, U]_{\tau eu_j u_i} \right|^2 \right\}$$

$$\hat{\sigma}_{RR}^{ui} = F_Z \left\{ \left| [c_{e\varphi}]_{\tau e} z_{u_R} + \frac{Q^2 + m_Z^2}{m_Z^2} [C_{eu}]_{\tau eu_i u_i} \right|^2 + \sum_{j \neq i} \left| \frac{Q^2 + m_Z^2}{m_Z^2} [C_{eu}]_{\tau eu_j u_i} \right|^2 \right\}$$

$$\hat{\sigma}_{LR}^{ui} = F_Z (1 - y)^2 \left\{ \left| \left[ c_{L\varphi}^{(1)} + c_{L\varphi}^{(3)} \right]_{\tau e} z_{u_R} + \frac{Q^2 + m_Z^2}{m_Z^2} [C_{Lu}]_{\tau eu_i u_i} \right|^2 + \sum_{j \neq i} \left| \frac{Q^2 + m_Z^2}{m_Z^2} [C_{Lu}]_{\tau eu_j u_i} \right|^2 \right\}$$

$$\hat{\sigma}_{RL}^{ui} = F_Z (1 - y)^2 \left\{ \left| [c_{e\varphi}]_{\tau e} z_{u_L} + \frac{Q^2 + m_Z^2}{m_Z^2} [C_{Qe}]_{\tau eu_i u_i} \right|^2 + \sum_{j \neq i} \left| \frac{Q^2 + m_Z^2}{m_Z^2} [C_{Qe}]_{\tau eu_j u_i} \right|^2 \right\} ,$$

## $\tau \leftrightarrow e$ transitions: future projections



S. Banerjee *et al*, arXiv:2203.14919

- Belle-II will improve  $\tau$  decays BR by a factor of 5 ( $\tau \rightarrow e\gamma$ ) to 40 ( $\tau \rightarrow e\pi\pi$ )
- colliders will play an important role in heavy flavor & multi-coupling scenarios