

# The Theoretical Cross Section Needs of Future Long Baseline Experiments

Kendall Mahn, Michigan State University

[INT workshop](#)

*“Theoretical physics  
uncertainties to  
empower neutrino  
experiments”  
Oct 30th, 2023*

*Support provided by U.S. DOE  
Award DE-SC0015903*



Thank you to the organizers for this invitation!  
Thank you to the INT for the support to be here.

Disclaimer: I get excited, and I talk too fast. My intent is for a dialogue-- *interruptions are OK! Let's clarify*

I will also want to follow up with others not present for the workshop -

- *I may not be aware of the latest progress, and welcome correction*
- *I want to share my ideas for the future and hear yours*

# What I want: *dream big, make specific plans*

Big dream: a baseline model with theory motivated degrees of freedom and with genuine exclusive predictive power I can use on T2K and DUNE

Outline for my talk:

- What I want this for - *oscillation, exotic physics results*
- Why are theoretical uncertainties important - *fast overview*
- Which uncertainties are important - *T2K current status, specific problems which need theoretical insight or development*
- Planning how we can work effectively - *formats, interfaces, ways to collaborate*
- Conclusion: *Wishlist! - and let's talk!*

## Current:

**Atmospheric:** Super-Kamiokande, IceCube

**Accelerator:** T2K, NOvA, Short-Baseline Neutrino Program (SBN)

## Future:

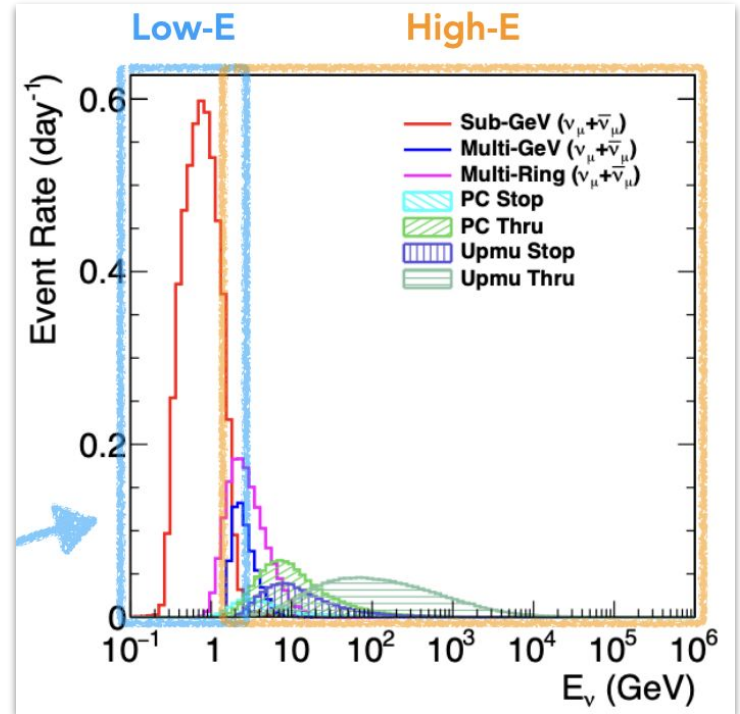
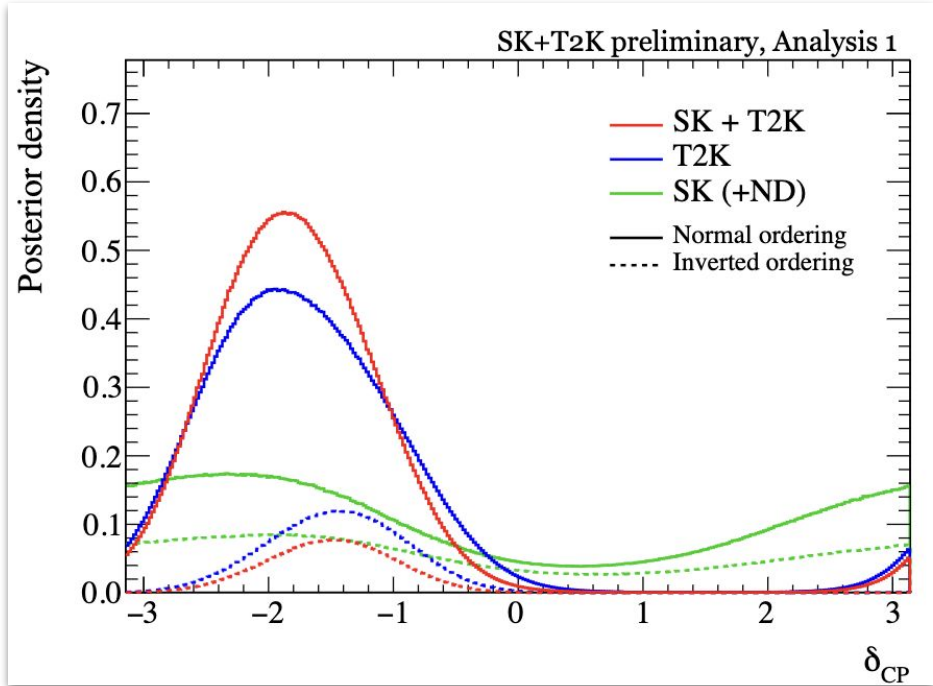
**Accelerator/Atmospheric:** Hyper-Kamiokande, Deep Underground Neutrino Experiment

**Current program is broad.**

Neutrino oscillation, exotica (e.g. sterile neutrino, dark matter searches), proton decay

Signal (or background) processes are 0.1-20 GeV charged current (CC) or neutral current (NC) neutrino or antineutrino interactions for **atmospheric and accelerator based programs**

# Shameless example: new SK+T2K joint analysis



Current and future experiments need to have models and uncertainties across energy ranges - here, 0.2 - 100 GeV

- More details: A. Eguchi @ [NNN2023](#)

# Neutrino oscillation fast primer

Oscillation depends on:

- Amplitude determined by mixing angles:  $\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$
- Frequency determined by mass splittings:  $|\Delta m^2_{32/31}|, \Delta m^2_{21}$
- CP violating phase (CPV)

*Is  $\sin^2(\theta_{23})=0.5$ ? (maximal mixing?)*

*What is the ordering of the masses ( $\Delta m^2_{32/31} > 0$ ?)*

*Is there CPV in neutrinos?*

# Neutrino oscillation fast primer

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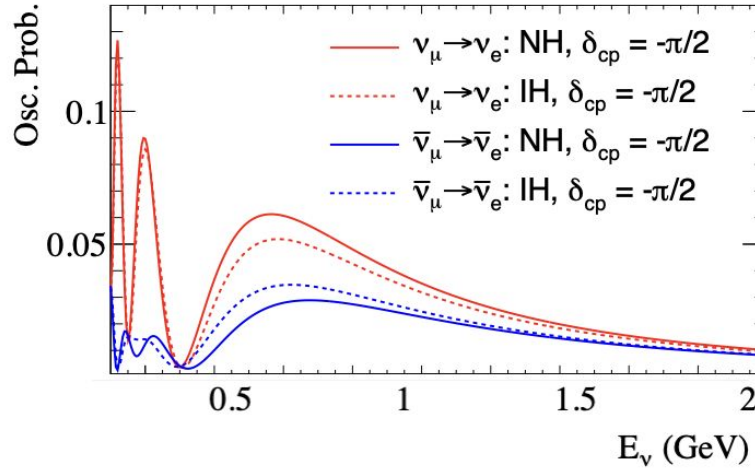
***$\nu_e$  and  $\bar{\nu}_e$  appearance channel***

SAMPLE	PREDICTED			
	$\delta_{CP}=-\pi/2$	$\delta_{CP}=0$	$\delta_{CP}=\pi/2$	$\delta_{CP}=\pi$
$\nu_e$ appearance	73.8	61.6	50.0	62.2
$\bar{\nu}_e$ appearance	11.8	13.4	14.9	13.2

*Changing  $\delta_{CP}$  increases  $\nu_e$  and decreases anti- $\nu_e$  appearance rates*

# Neutrino oscillation fast primer

- Amplitude determined by mixing angles:  $\theta_{12}, \theta_{23}, \theta_{13}$
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- CP violating phase (CPV)



SAMPLE	PREDICTED			
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$\nu_e$ appearance	73.8	61.6	50.0	62.2
$\bar{\nu}_e$ appearance	11.8	13.4	14.9	13.2

*Normal to inverted hierarchy suppresses  $\nu_e$  appearance, enhances  $\bar{\nu}_e$  appearance*



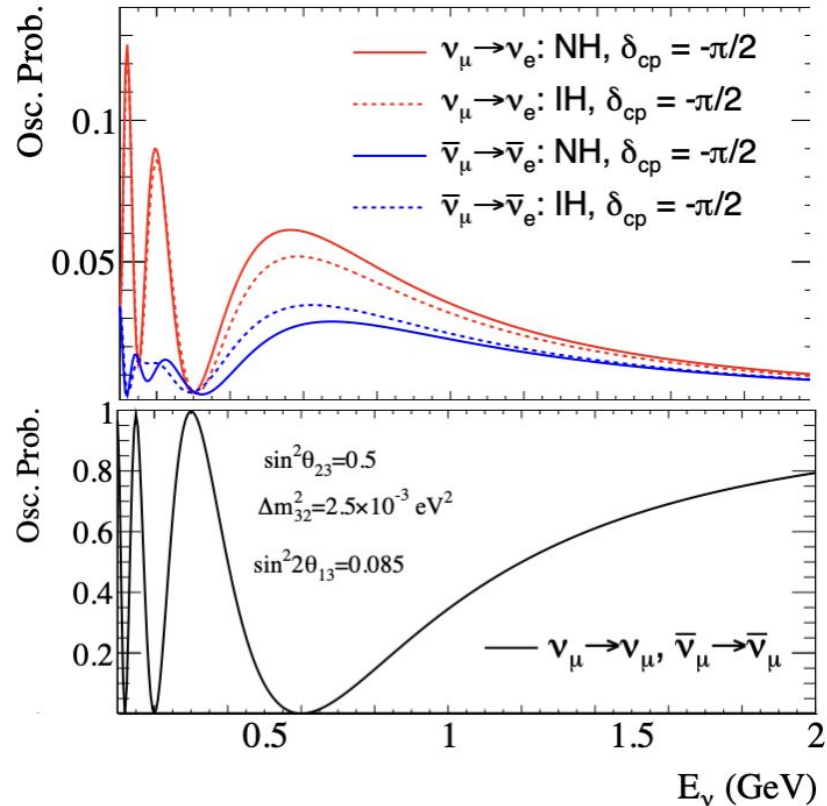
# Neutrino oscillation fast primer

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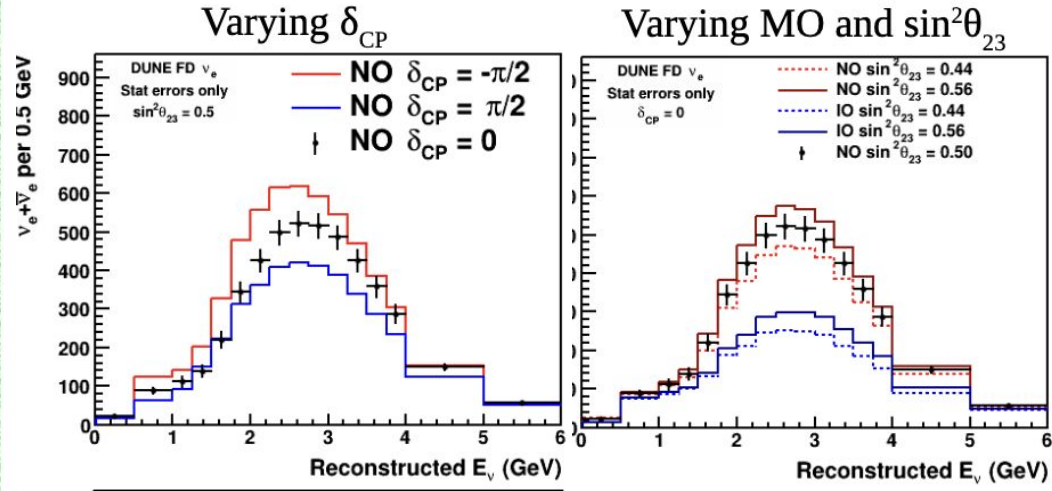
*Largely independent of  $\delta_{CP}$  effects*

## $\nu_\mu$ and $\bar{\nu}_\mu$ disappearance channel



# Neutrino oscillation fast primer

- Amplitude determined by mixing angles:  $\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$
- Frequency determined by mass splittings:  $|\Delta m^2_{32/31}|, \Delta m^2_{21}$
- CP violating phase (CPV)



C. Marshall, [P5\\_town\\_hall@FNAL](mailto:P5_town_hall@FNAL)

$$N_{FD}^{\alpha \rightarrow \beta}(E_{reco}) = \sum_i \phi_\alpha(E_{true}) \times \sigma_\beta^i(E_{true}) \times P_{\alpha\beta}(E_{true}) \times \epsilon_\beta(E_{true}) \times R_i(E_{true}; E_{reco})$$

*Event rate used to infer oscillation physics*

# Oscillation analysis depends on interaction model

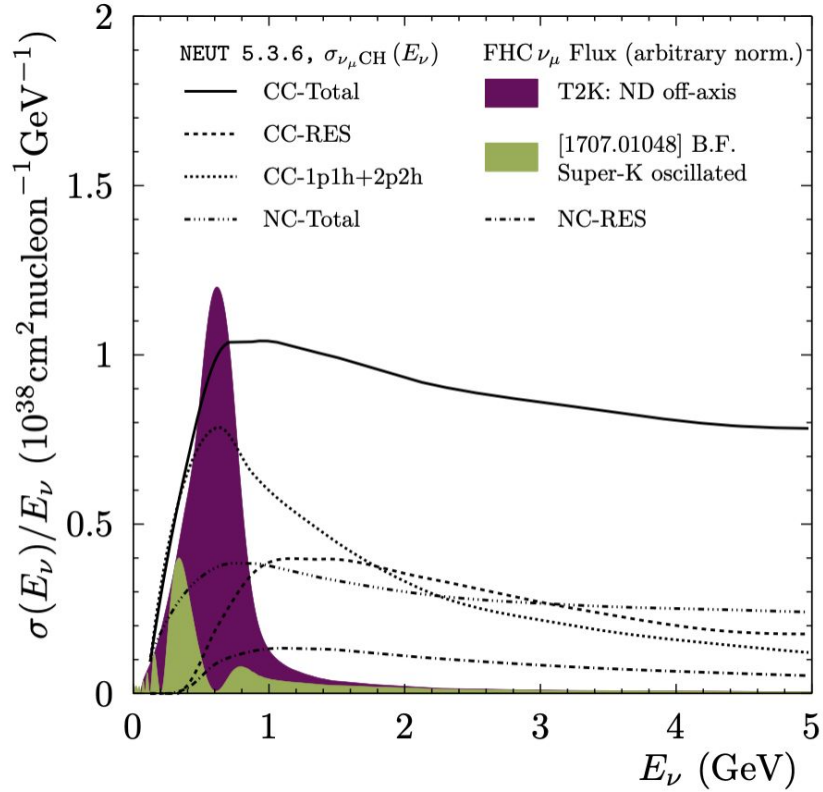
**Cross section (true kinematics)**

**Efficiency (true kinematics)**

**Relationship between true and reconstructed kinematics)**

$$N_{FD}^{\alpha \rightarrow \beta}(E_{reco}) = \sum_i \phi_\alpha(E_{true}) \times \sigma_\beta^i(E_{true}) \times P_{\alpha\beta}(E_{true}) \times \epsilon_\beta(E_{true}) \times R_i(E_{true}; E_{reco})$$

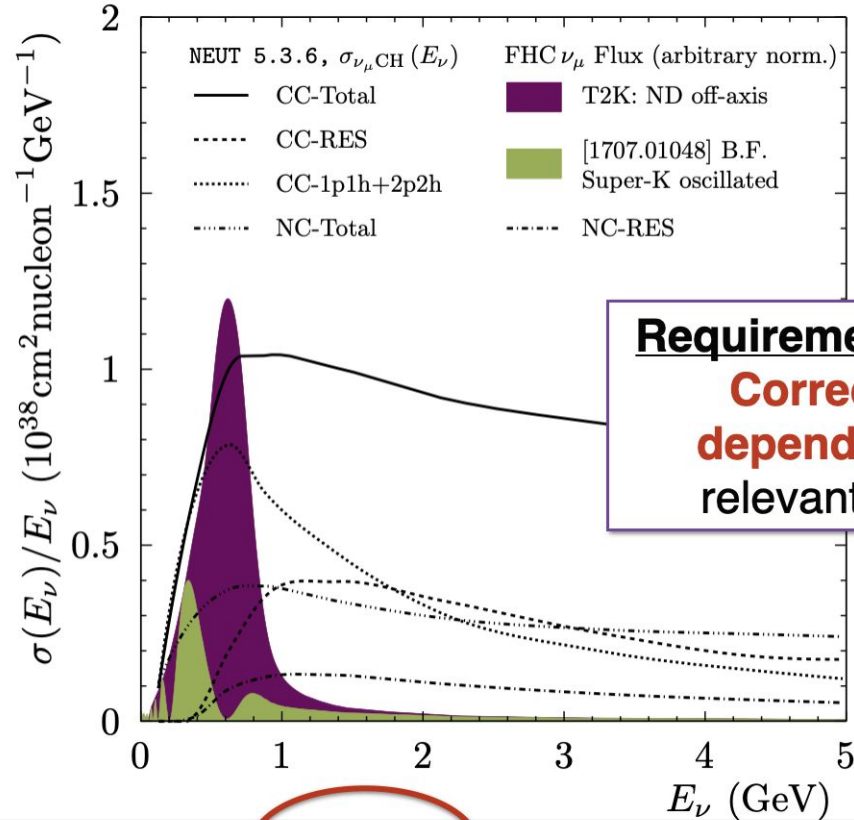
# Oscillation analysis depends on interaction model



*All plots this pretty are from L. Pickering*

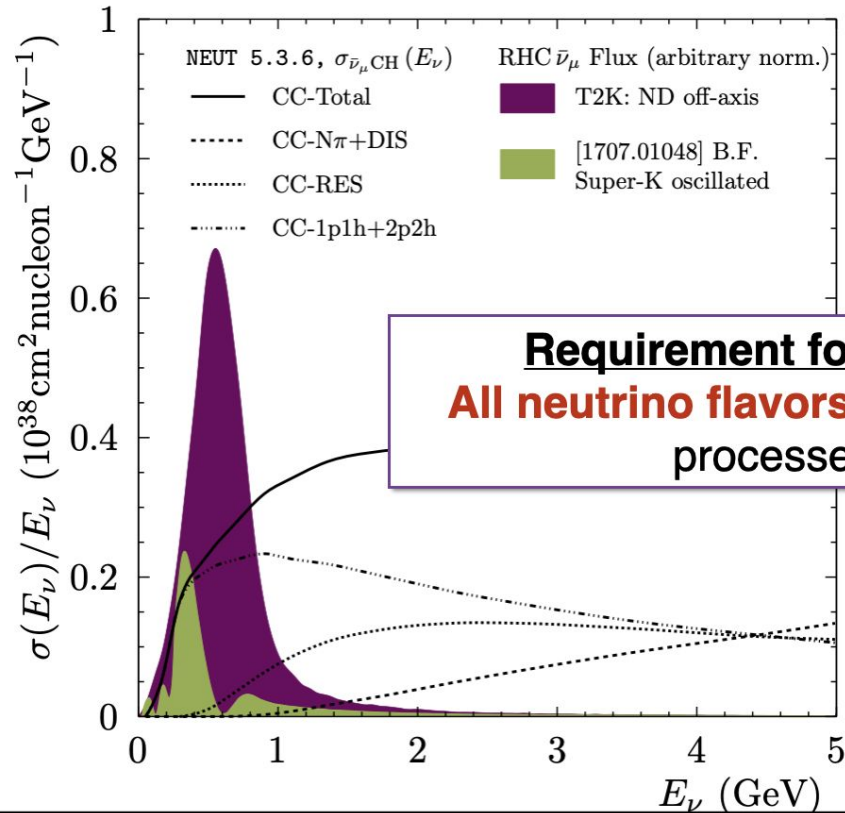
*Incident energy is not known. Spread of beam is larger than nuclear effects.*

# Oscillation analysis depends on interaction model



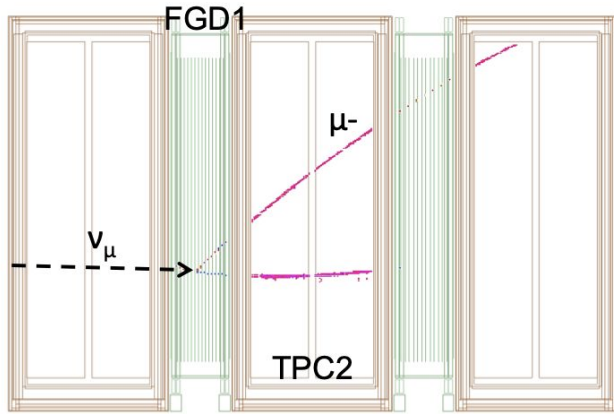
$$N_{FD}^{\alpha \rightarrow \beta}(E_{reco}) = \sum_i \phi_\alpha(E_{true}) \times \sigma_\beta^i(E_{true}) \times P_{\alpha\beta}(E_{true}) \times \epsilon_\beta(E_{true}) \times R_i(E_{true}; E_{reco})$$

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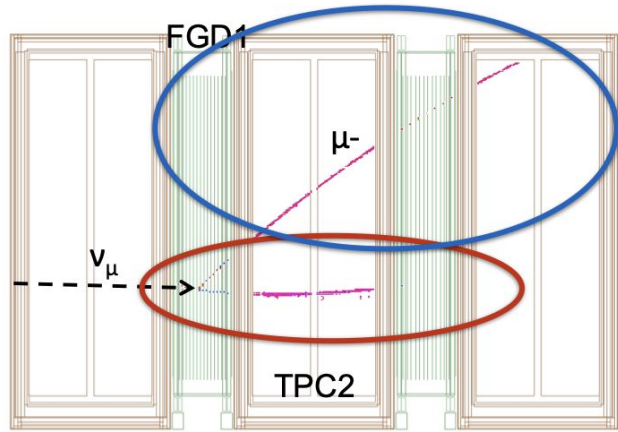
# Need: hadronic state description



- T2K event display
- CC0 $\pi$  “topology”: 1 muon, no pion
- Includes CCQE, 2p2h, CC1 $\pi$  (pion absorbed in nucleus)



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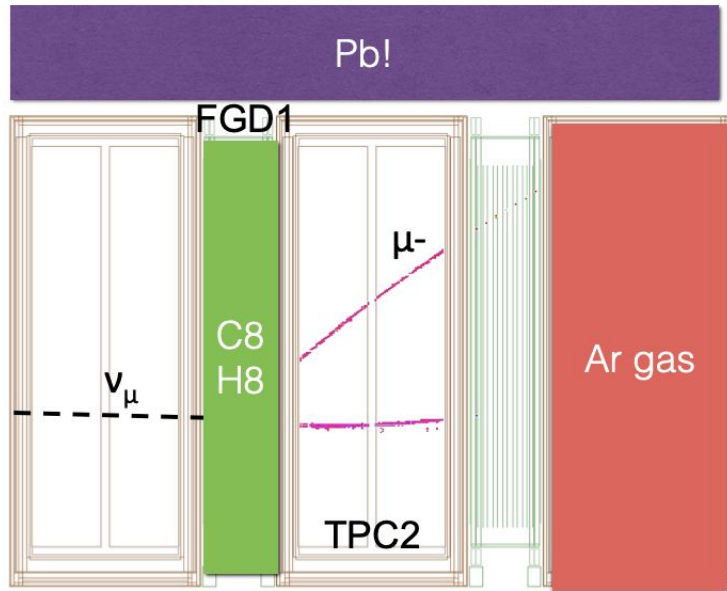
## Requirement for model:

- All visible particles for efficiency (background) and energy estimates

$$N_{FD}^{\alpha \rightarrow \beta}(E_{reco}) = \sum_i \phi_\alpha(E_{true}) \times \sigma_\beta^i(E_{true}) \times P_{\alpha\beta}(E_{true}) \times \epsilon_\beta(E_{true}) \times R_i(E_{true}; E_{reco})$$



# Needs: target material



Target materials:

- T2K: H<sub>2</sub>O
- NOvA: CH+Cl
- SBN, DUNE: Ar

## Requirement for model:

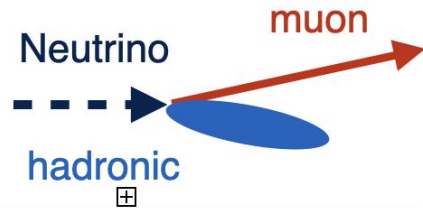
- Most nuclear targets, esp C, O, Ar

**Also:** Uncertainties and correlations between nuclear targets

# Needs: energy estimation

- Oscillation depends on energy
- Estimate from hadronic and/or leptonic information

$$E_\nu^{QE} = \frac{m_p^2 - m_n'^2 - m_\mu^2 + 2m_n' E_\mu}{2(m_n' - E_\mu + p_\mu \cos \theta_\mu)} \quad E_\nu = E_\mu + \sum E_{hadronic}$$



**T2K**  
**Super-Kamiokande**

**SBN**  
**DUNE**

**NOvA**

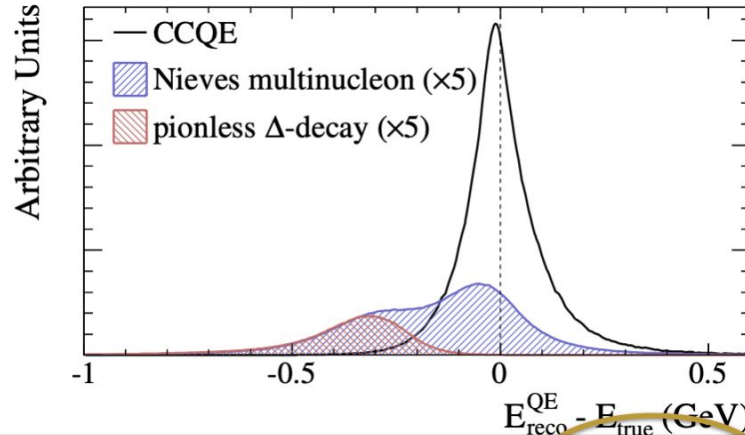
# Needs: energy estimation

- Nuclear effects bias true and estimated neutrino energy

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## Requirement for model:

- Correct mix of processes per topology
- true - reconstructed kinematic relationship



$$N_{FD}^{\alpha \rightarrow \beta}(E_{reco}) = \sum_i \phi_{\alpha}(E_{true}) \times \sigma_{\beta}^i(E_{true}) \times P_{\alpha\beta}(E_{true}) \times \epsilon_{\beta}(E_{true}) \times R_i(E_{true}; E_{reco})$$

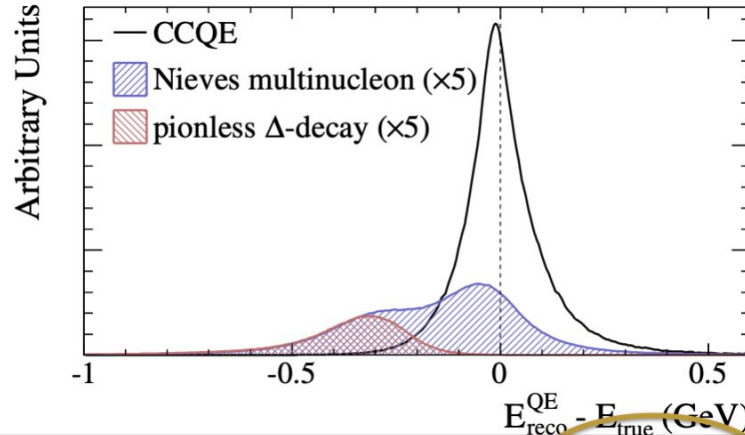
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## Requirement for model:

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**Also:** models which can work simultaneously in both estimators

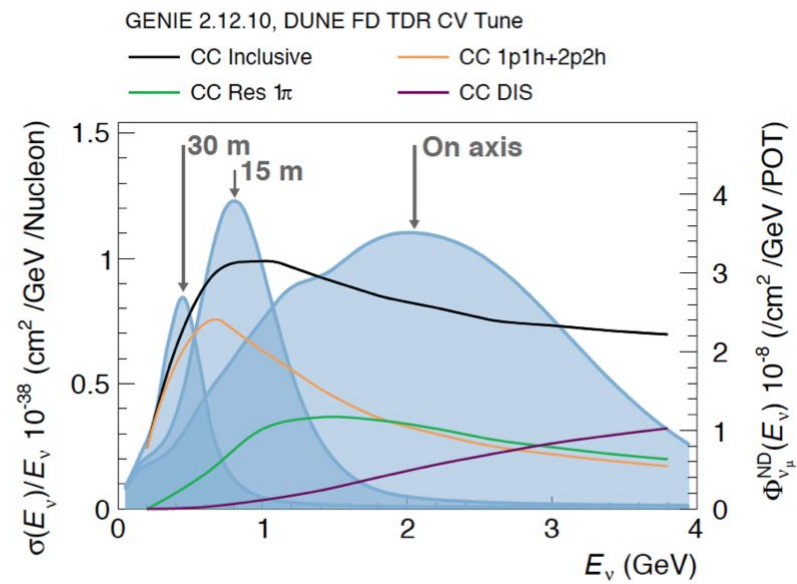
Recent MINERvA paper: [PRL 129 \(2022\) 2, 021803](#)

$$N_{FD}^{\alpha \rightarrow \beta}(E_{reco}) = \sum_i \phi_{\alpha}(E_{true}) \times \sigma_{\beta}^i(E_{true}) \times P_{\alpha\beta}(E_{true}) \times \epsilon_{\beta}(E_{true}) \times R_i(E_{true}; E_{reco})$$

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$$N_{ND}^\alpha(E_{reco}) = \sum_i \phi_\alpha(E_{true}) \times \sigma_\alpha^i(E_{true}) \times \epsilon_\alpha(E_{true}) \times R_i(E_{true}; E_{reco})$$

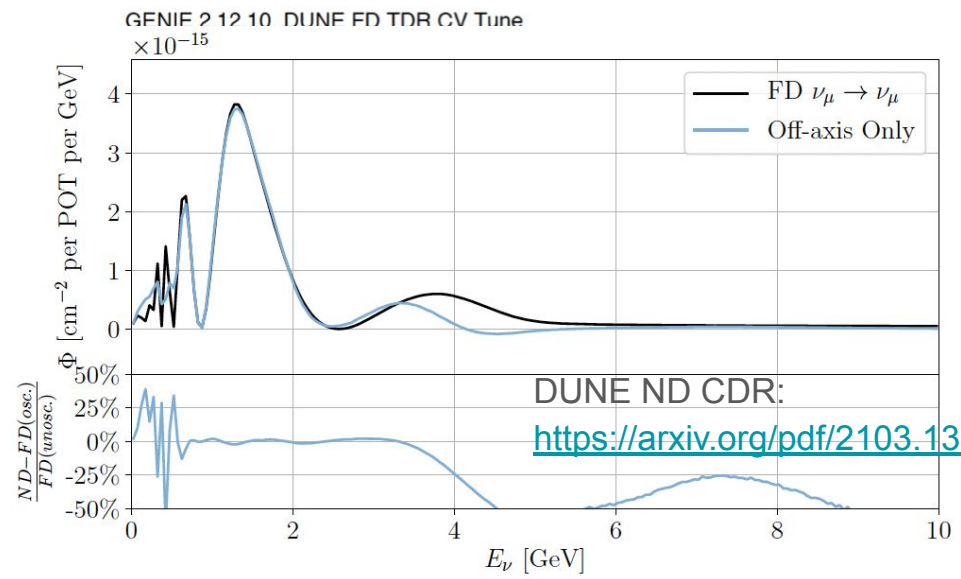
- **Near detector information** provide stability monitoring, improved event rate prediction and reduces shared systematic uncertainty from flux, interaction model
- Example ND sample: nu-e scattering (low rate, but well known cross section, direct constraint of flux)
- Example: PRISM, ND rates will be sampled at a range of energies

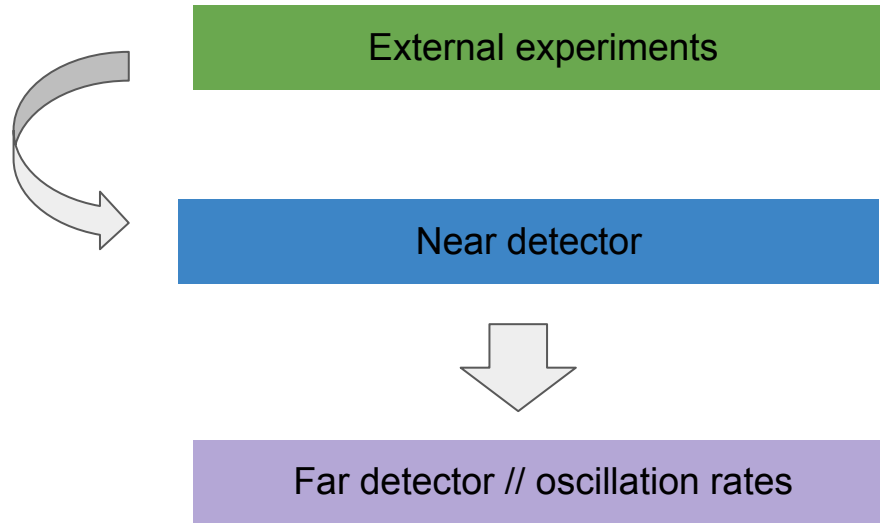


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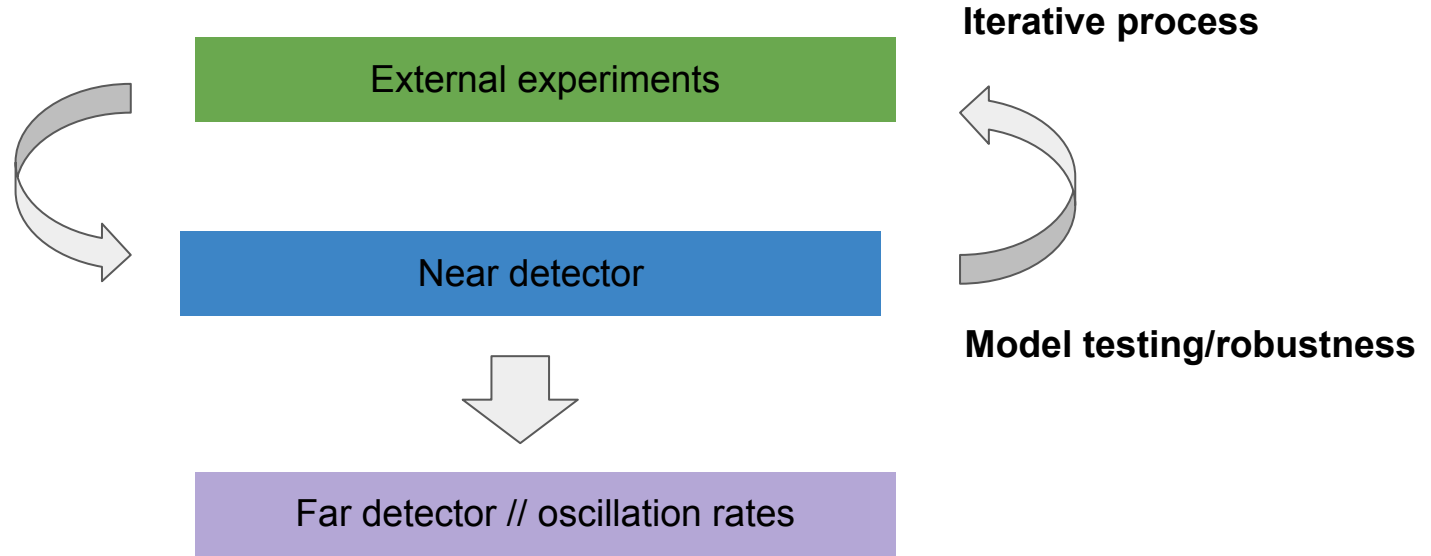


**External experiments and theory are very important;** determine parameterization, uncertainties

- Electron, pion scattering
- Neutrino H/D data
- Neutrino nucleus scattering

Snowmass Neutrino Cross Section  
Topical Group report:

<https://arxiv.org/abs/2209.06872>



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**Iteration is necessary, and takes time**



# Persistent challenges: addiction to ad hoc

Simulations are using inclusive calculations (quasielastic plus 2p2h plus pion production) with a fragmentation model, plus an FSI cascade or transport.

- “Franken-model”
- “Paper over problems”

We have been building ourselves a layer cake with shaky foundation

- Difficult to attribute correctly which layer is crumbling under pressure

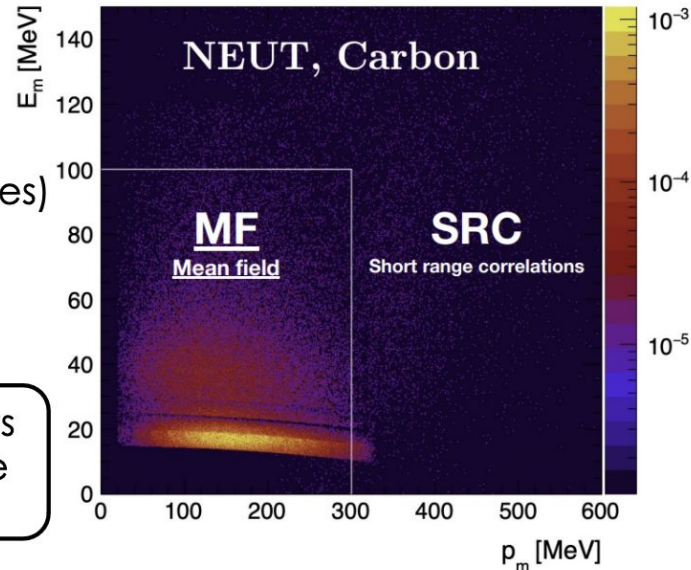
We’re trying to break this habit, by moving toward theoretically motivated degrees of freedom



# Recent work to theoretically motivated uncertainties

- **Fermi motion and removal energy** in the mean field region:
  - Change **relative occupancy** of the shells (2 shells for C, 3 for O)
  - Change **shape of the momentum distribution** of each shell
  - Shift the **whole removal energy distribution**
  - Plausible alterations derived from  $(e \rightarrow e', p)$  data
- **Short range correlations:**
  - **Normalisation of the SRC contribution** (high nucleon momentum tail, 2 nucleon final states)
  - NEUT predicts 5%, other models predict closer to 20%

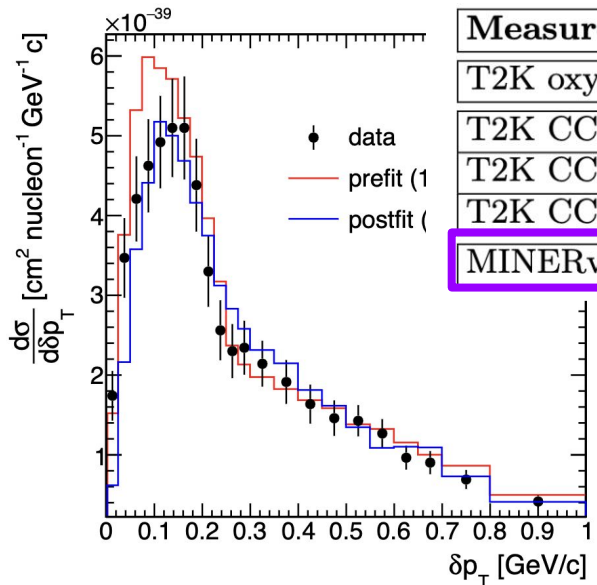
Crucial check: the parameter constraints from T2K's near detector are reasonable given electron scattering data



Based on  
Benhar SF  
model

More  
details: S.  
Dolan,  
[NuInt2022](#)

# Persistent challenges: disagreement with experimental data



Measurement	Prefit $\chi^2$	Postfit $\chi^2$	Number of bins
T2K oxygen + carbon (Sec. IV B 1)	98.79	30.30	58
T2K CC0 $\pi$ Np $\delta p_T$ only (Sec. IV B 2)	15.72	8.48	8
T2K CC0 $\pi$ 0p ( $p_\mu, \cos \theta_\mu$ ) only (Sec. IV B 2)	107.57	62.55	50
T2K CC0 $\pi$ 0p + CC0 $\pi$ Np (Sec. IV B 2)	107.57 + 16.76	64.19 + 11.83	50 + 8
MINERvA $\delta p_T$ (Sec. IV B 3)	114.32	76.14	24

**We need semi-inclusive theory for the hadronic state (NOvA, SBN DUNE... and T2K's neutron tagging...)**

**We must continue to interrogate simplifications/approximations/extrapolations**

Disagreements in semi-inclusive data seen for some time (e.g. MINERvA, PRL 121, 022504 (2018))  
 MINERvA data compared to newer T2K model:

<https://arxiv.org/pdf/2308.01838.pdf>

# Planning how to work together - *lowering barriers*

“Implementation of some of the exclusive models that are available in such a way that we can easily access the parameters that plausibly alter model predictions.” - *how do we make this simple and easy for all of us?*

- Generator format standardization - NEW: <https://arxiv.org/pdf/2310.13211.pdf>
- Data comparisons (format again)
- Shared tools, defined interfaces

# Planning how to work together - *collaboration mechanisms*

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On T2K, we regularly have guest members join our interaction development meetings, and we also do smaller author papers ('opt in'). We also try to cite theoretical effort within our oscillation papers.

**Let us know how we can support 'external' effort.** Where are there barriers to progress we can work on together or simplify workflow?

# Model development and uncertainties wishlist

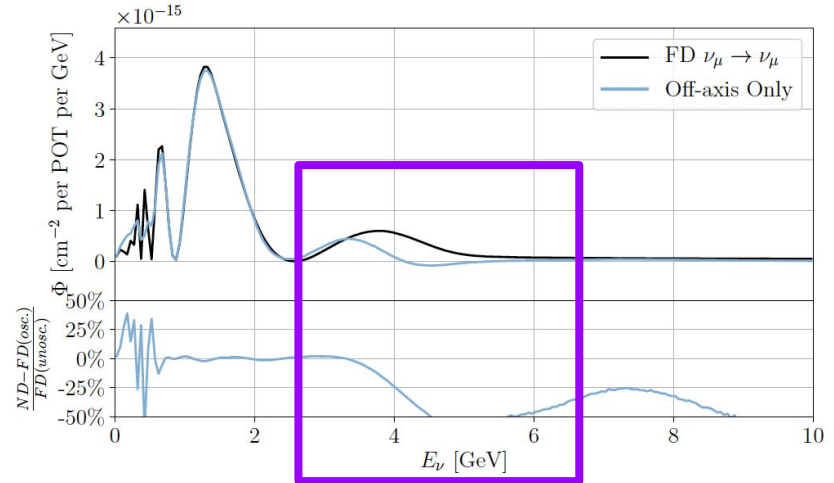
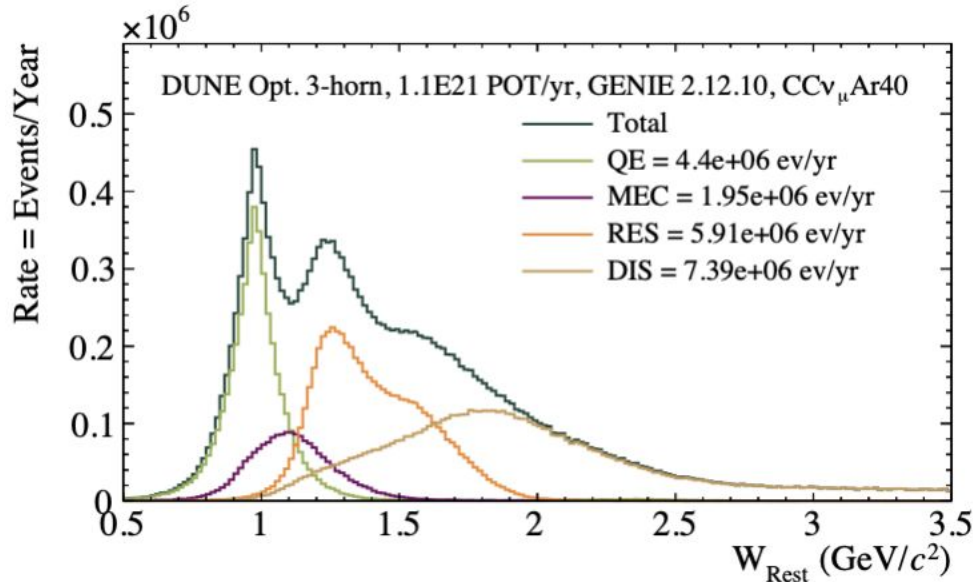
- Resonance model development
  - Fudge is here! This is a major process for DUNE
  - CC (osc signal) and NC (exotic physics, background)
  - Description of pion, proton kinematics; FSI beyond cascades)
  - Leverage electron scattering data here?



*Obscure reference to Jujutsu Kaisen, “resonance” ability, though, I do often daydream of smashing my laptop*

# Model development and uncertainties wishlist

- Resonance model development
- Transition region - *Incomplete experimental and theoretical footing*
  - Little to no single nucleon data
  - How do we handle double counting? Extrapolations/approximations?



# Model development and uncertainties wishlist

- Resonance model development
- Transition region
- Continued work on QE/multinucleon processes
  - Heavier targets (Ar) and uncertainties which relate C,O to Ar



# Model development and uncertainties wishlist

- Resonance model development
- Transition region
- Continued work on QE/multinucleon processes
- nue/numu uncertainties - *important for all appearance measurements*

Error source	FHC1Re	RHC1Re
Flux	2.90%	3.09%
Cross-section	4.31%	4.20%
2p2h Edep	0.20%	0.18%
IsoBkg Low-p $\tau$	0.05%	1.76%
$\sigma(\nu_e), \sigma(\bar{\nu}_e)$	2.40%	1.40%
NC $\gamma$	1.28%	2.22%
NC Other SK	0.20%	0.40%
Flux x cross-section	3.16%	3.70%
SK det	3.06%	3.92%
Total Syst.	4.57%	5.65%

Uncertainties are from: [second class currents](#), radiative corrections, and (soon) [collective nuclear effects](#) which lead to differences in electron-muon and neutrino-antineutrino cross section

2020 T2K analysis, [Eur. Phys. J. C 83, 782 \(2023\)](#)

# Summary

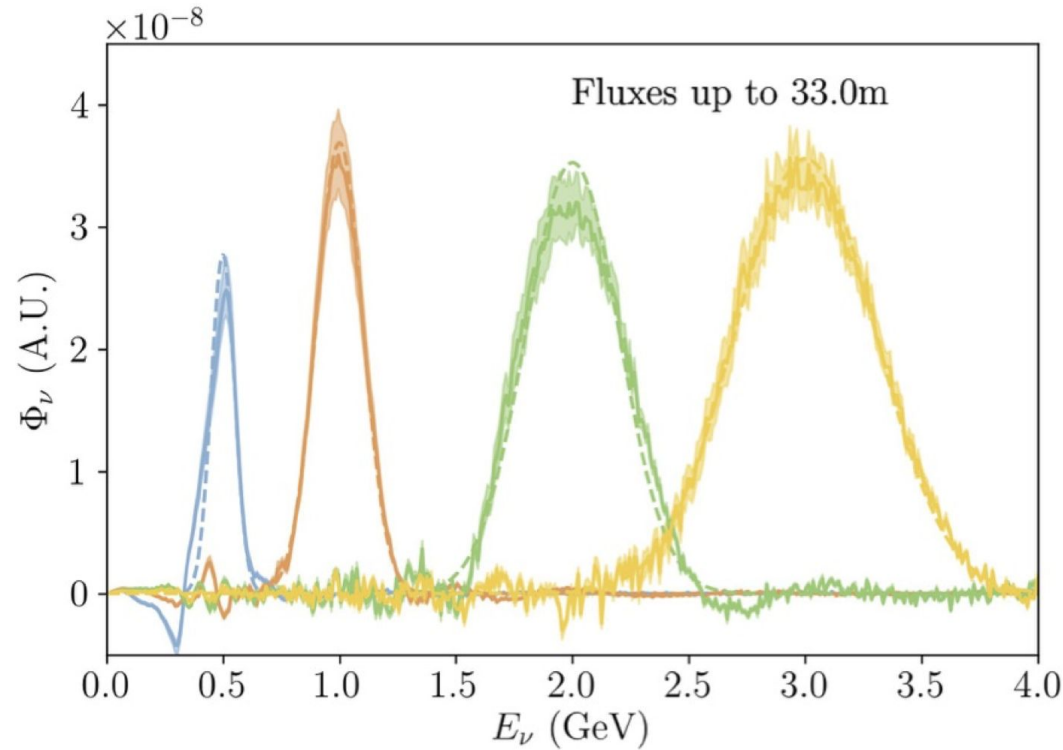
- We continue to need theory for robust interpretation of oscillation, cross section and exotic physics
  - *“We know that all our models are strongly rejected by global cross section measurements (even when we fit the uncertainties within them) and that we know from T2K that the scope for bias from mismodelling is close to 100% of our existing systematic uncertainty budget on  $\Delta m^2$ .”*
- Dream big: *“Implementation of exclusive models that are available in such a way that we can easily access the parameters that plausibly alter model predictions.”*
  - On T2K, we are trying to move toward a baseline model with theory motivated degrees of freedom and with genuine exclusive predictive power
- Plan specific: We have a wishlist of work we would benefit from theoretical help
  - Let’s discuss: What specific topics are of interest to the folks here?
  - Let’s discuss: How we can work together effectively

# Backup

# Another view of the necessity of precision modelling

From: DUNE ND CDR:

<https://arxiv.org/pdf/2103.13910.pdf>



# What we learn at the ND: parameter constraints

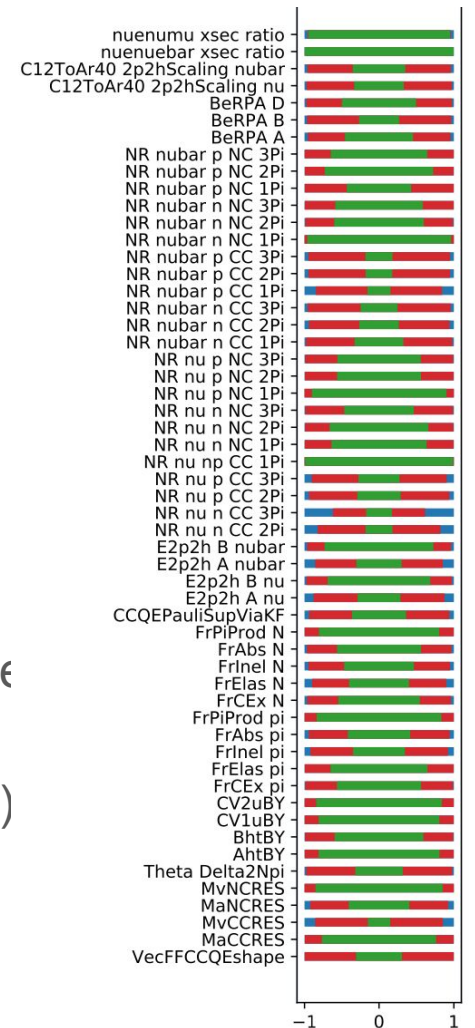
From: DUNE Physics TDR, Fig 5.34

<https://arxiv.org/pdf/2002.03005.pdf>

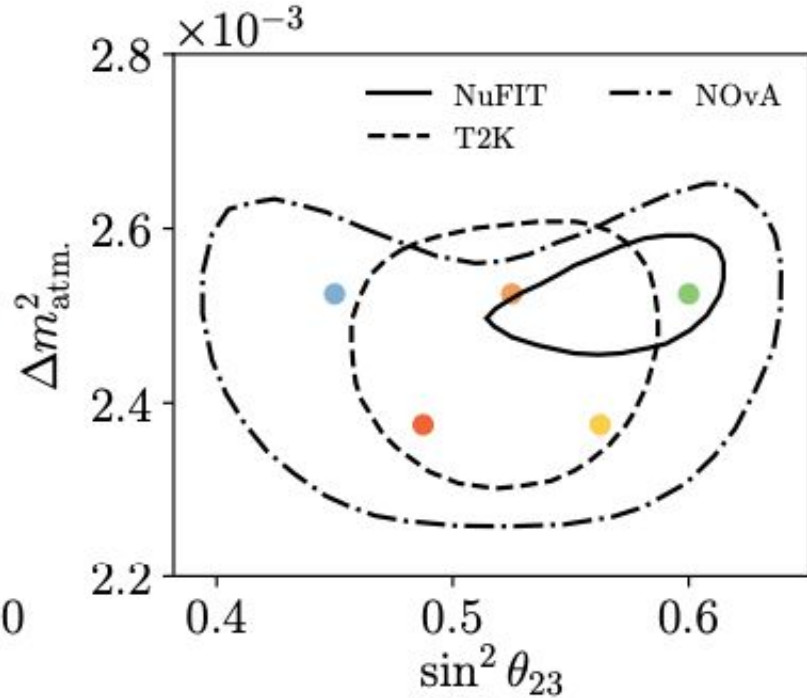
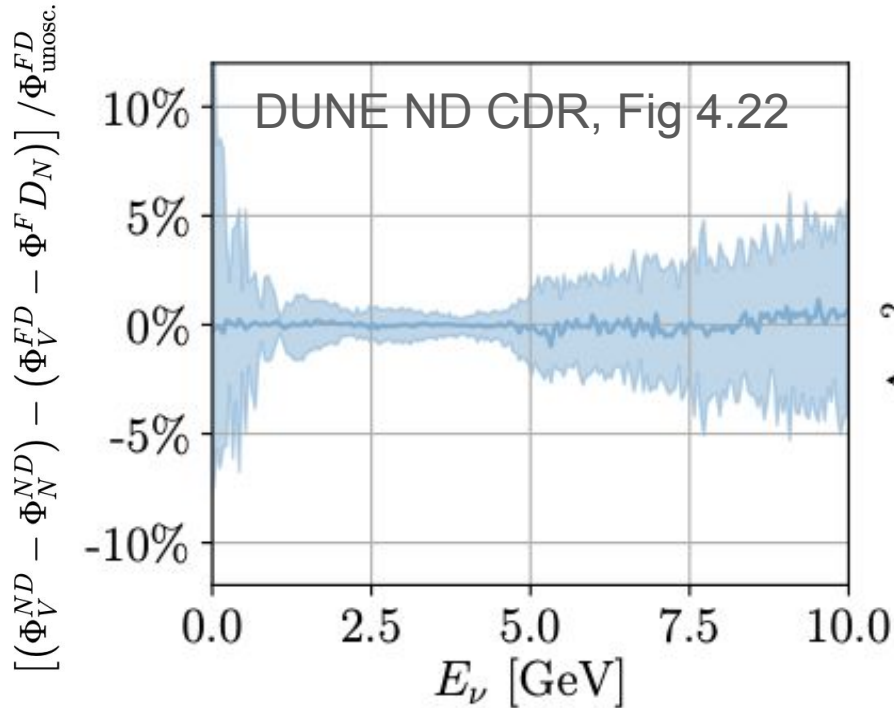
What's not obvious here:

- Important measurements needed by THEORY from electron scattering
- How the model development needs go with time (iterative process takes time, this is at the end)
- What if the model is wrong? (PRISM, electron scattering)

■ Prior     
 ■ FD-only     
 ■ ND+FD



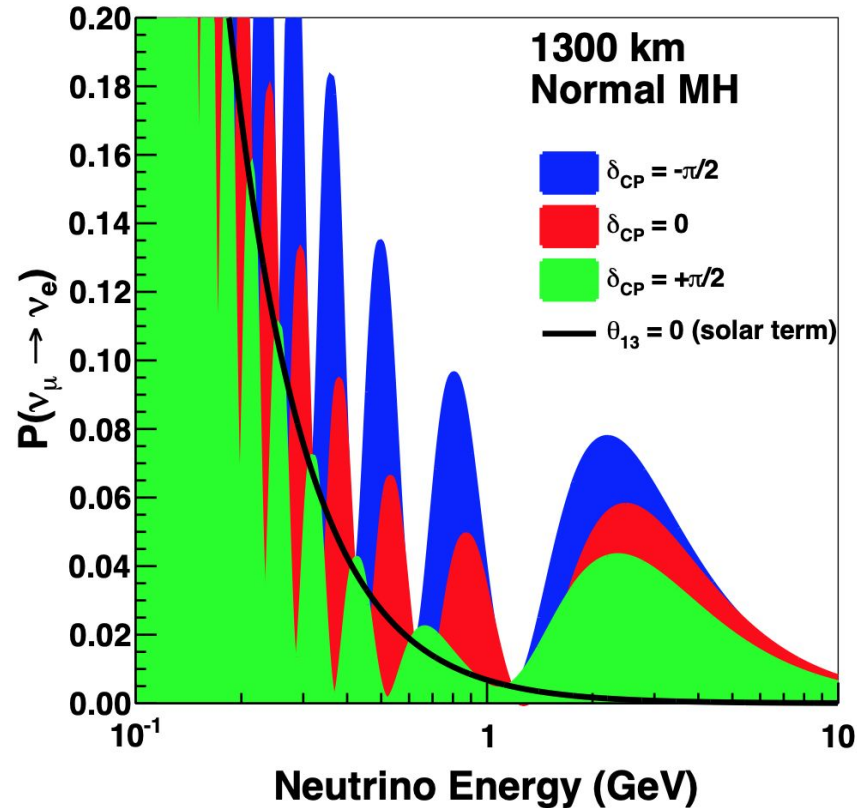
# What we learn at the ND: robustness tests w/ PRISM



PRISM needs a reasonable initial model with correct parameterization -  
*electron scattering is very useful to accomplish that goal*

# What is the amount of tolerable uncertainty on dCP? *Hot take*

- Event rates tell you about dCP.
  - Current experiments and future may be dominated by FD or ND detector response
- However, we need a robust model
  - Note the interesting behavior of how dCP changes the location of 2nd osc max
  - $\Delta m^2$  also modifies this feature
  - $\Delta m^2$  can be sensitive to the incorrect model
  - **It's important to measure all parameters! Correctly**
- We need to assess role of residual systematics AND robustness
  - What physics is not currently captured sufficiently well?
  - Don't forget atm nu or NC measurements for completeness of 3 flavor model



# Why is electron scattering a key component of the current and future program?

From: Electron scattering white paper <https://arxiv.org/abs/2203.06853> - *credit of many here!*

To have a robust model requires multiple tests of the model

- *Elec scattering is highly complementary to the ND program, and enhances ND physics reach in a novel way;*
- *Resonance region expected to be very important - major discrepancies and need for electron measurements for theory*

We know next to nothing in transition region, which is also where the power of PRISM decreases

- *need H/D measurements and need to build a basic and complete model of multiplicity and final state composition; atm nu physics may also really need this region*

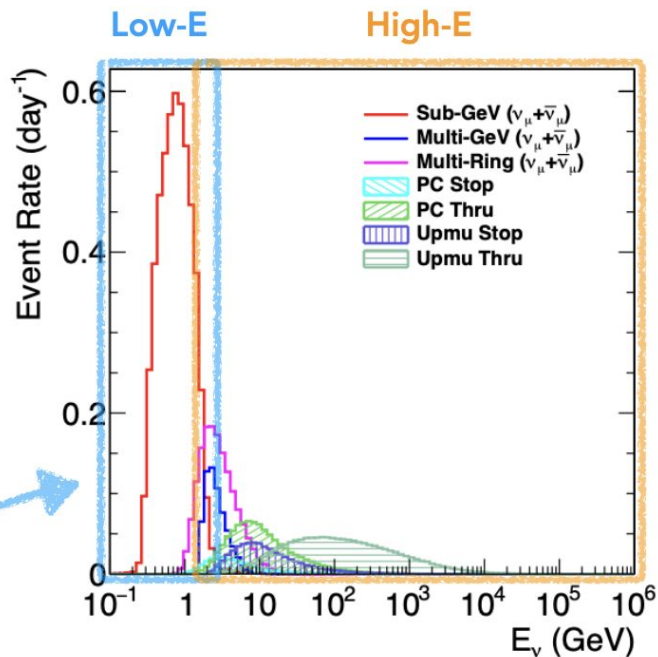
Both of these problems need TIME and DATA to confront

- *mature state of T2K/NOvA combined with electron scattering program is exciting*



# A. Eguchi, NNN2023, SK+T2K combined analysis

- SK atmospheric covers a wider range of energies than T2K.
- Use different models for low-energy and high-energy samples.



Use a common cross-section model with T2K

	Low-energy sub-GeV atm + beam	High-energy multi-GeV atm
<b>CCQE</b>	T2K model with ND280 constraint, correlated in low-E/high-E (except for high-Q <sup>2</sup> )	
	high-Q <sup>2</sup> params w/ND280 add $\nu_e/\nu_\mu$ ratio unc. (CRPA)	high-Q <sup>2</sup> params w/o ND
<b>2p2h</b>	T2K model w/ND280	SK model (100% error) + T2K-style shape
<b>Resonant</b>	T2K model w/ND280 + new pion momentum dial + NC1 $\pi$ 0 uncertainties	SK model for 3 dials common with T2K, use more recent larger T2K priors
<b>DIS</b>	T2K model w/ND280	SK model
$\nu_\tau$	SK model (25% norm on top of other syst) for other systematics checked that we have no numerically unstable values	
<b>FSI</b>	T2K model w/ND280	T2K model w/o ND280 should be mostly same as SK model
<b>SI</b>	T2K model, correlated in low-E/high-E only applied to FC and PC for atm, PN not applied to atm	

## A. Eguchi, NNN2023, SK+T2K combined analysis

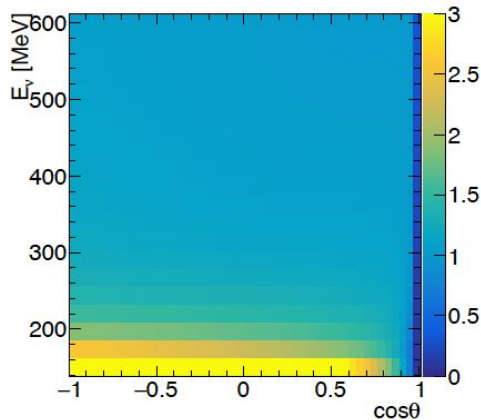
- SK atmospheric covers a wider range of energies than T2K.
  - Use different models for low-energy and high-energy samples.

- Low energy** (beam and atmospheric Sub-GeV samples)
  - Use the T2K model [ref] as the base which is **constrained by the T2K near detector**.
  - Some extra parameters are added to cover important uncertainties for the atmospheric analysis.
- High energy** (rest of atmospheric samples)
  - Use a modified SK model [ref] including additional systematics uncertainties.

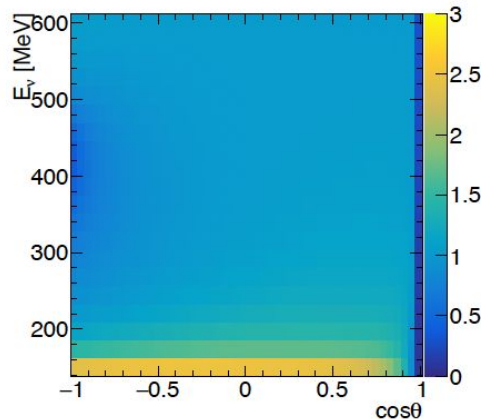
	Low-energy sub-GeV atm + beam	High-energy multi-GeV atm
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	high-Q <sup>2</sup> params w/ND280 add $\nu_e/\nu_\mu$ ratio unc. (CRPA)	high-Q <sup>2</sup> params w/o ND
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DIS	T2K model w/ND280	SK model
$\nu_\tau$		SK model (25% norm on top of other syst) for other systematics checked that we have no numerically unstable values
FSI	T2K model w/ND280	T2K model w/o ND280 should be mostly same as SK model
SI	T2K model, correlated in low-E/high-E only applied to FC and PC for atm, PN not applied to atm	

# Model development and uncertainties wishlist

- Resonance model development
- Transition region
- Continued work on QE/multinucleon processes
- nue/numu uncertainties - *important for all appearance measurements*



(c) Ratio of  $d\sigma_{\nu_e}/d\sigma_{\nu_\mu}$  for CRPA model.



(d) Ratio of  $d\sigma_{\bar{\nu}_e}/d\sigma_{\bar{\nu}_\mu}$  for CRPA model.

Uncertainties are from: [second class currents](#), radiative corrections, and [collective nuclear effects](#) which lead to differences in electron-muon and neutrino-antineutrino cross section