

TOWARDS A SELF-CONSISTENT DESCRIPTION OF ν INTERACTIONS IN MERGERS:

CHALLENGES & ACHIEVEMENTS

Zidu Lin

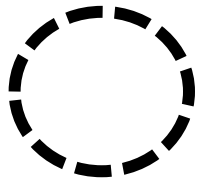
University of Tennessee, Knoxville and University of New Hampshire

@INT Seattle, 9/9/2025

Collaborators: A. W. Steiner (UTK), A. Stinson (UTK), J. Margueron (IRL-NPA), G. Colo (INFN),
F. Foucart (UNH), S. Rath (UNH), P. Hammond (UNH, NP3M)



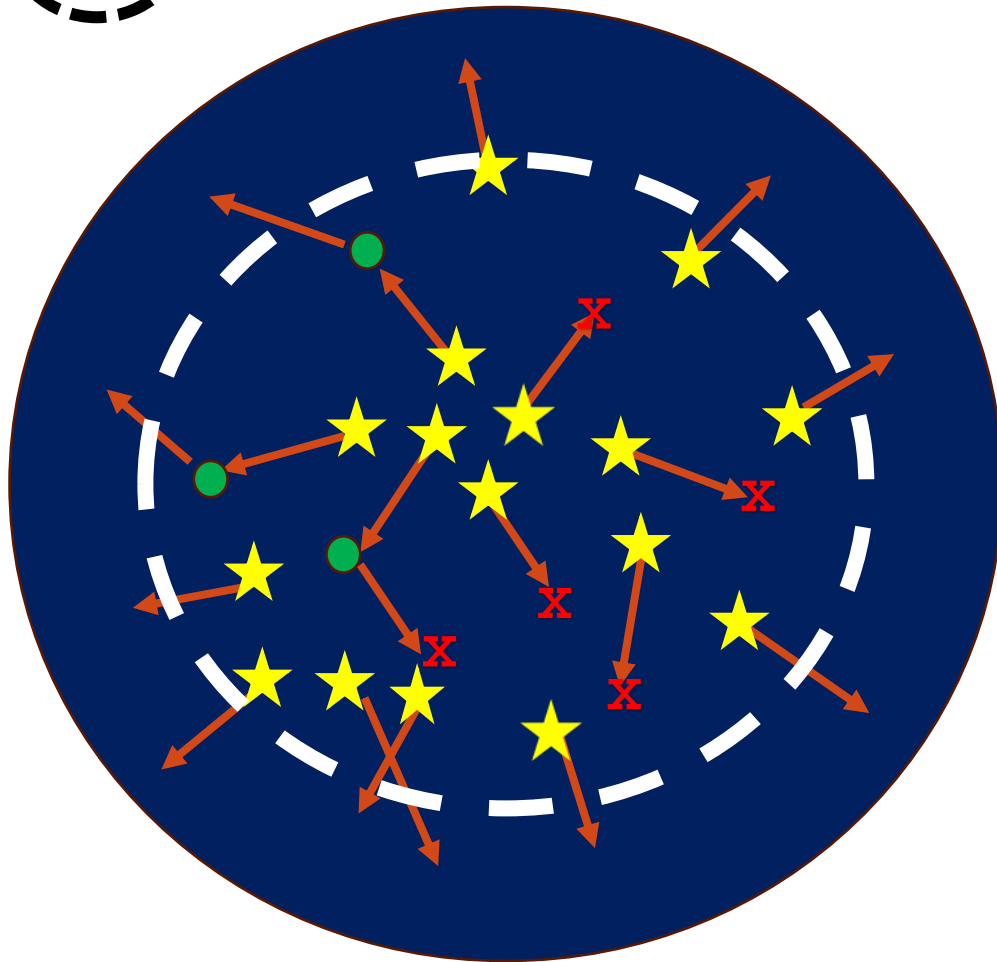
Neutrinos in compact stars



: neutrino sphere



: neutrino flavor oscillation



★ : neutrino emission ● : neutrino scattering

✕ : neutrino absorption

ν are **emitted** from:
(1) Electron capture
(2) Pair process
(3) URCA ?
(4) ...

ν are **scattered** by:
(1) Electrons
(2) Nucleons
(3) Nuclei
(4) Quarks?
(5) ...

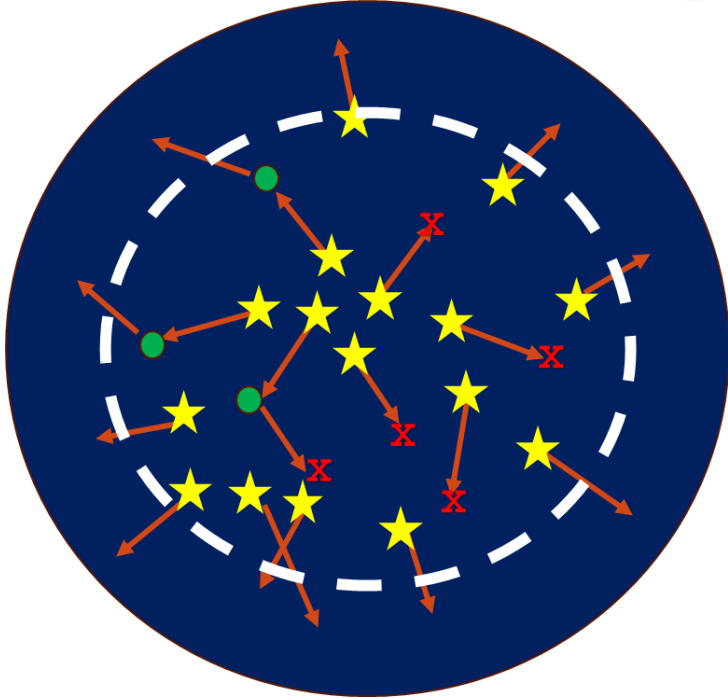
ν are **absorbed** by:
(1) Electrons
(2) Nucleons
(3) Nuclei
(4) ...

The **emission**, **scattering**, and **absorption** rates depend on component, thermal properties, and interactions of dense matter

1. Neutrino sphere location
2. neutrino oscillation
3. neutrino spectra

1. The speed of reaching equilibrium
2. Ye distribution
3. Bulk viscosity and so on...

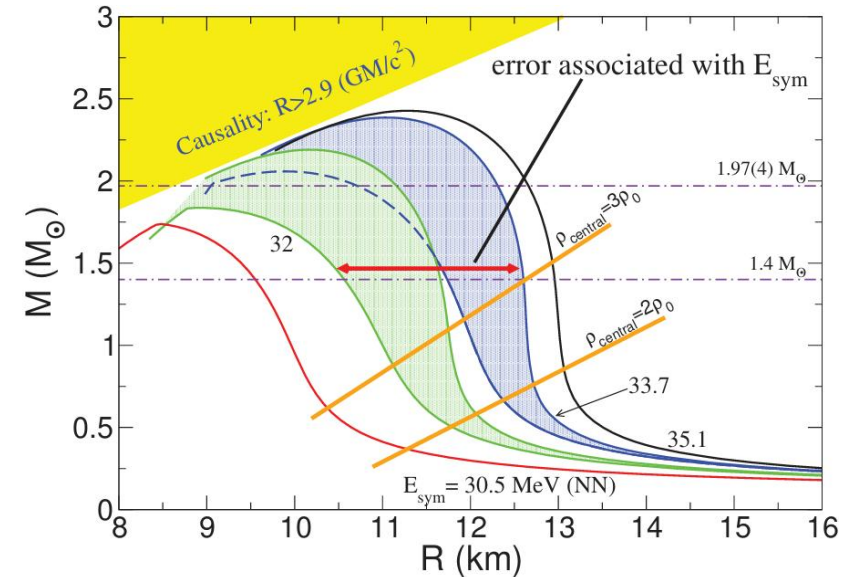
Goals (Dreams?): Self-consistent nuclear models
describing both macroscopic compact star properties
and microscopic neutrino interactions inside the stars



Microscopic neutrino reactions

Nuclear models

J. Phys.: Conf. Ser. 665 012063 S Gandolfi and A W Steiner

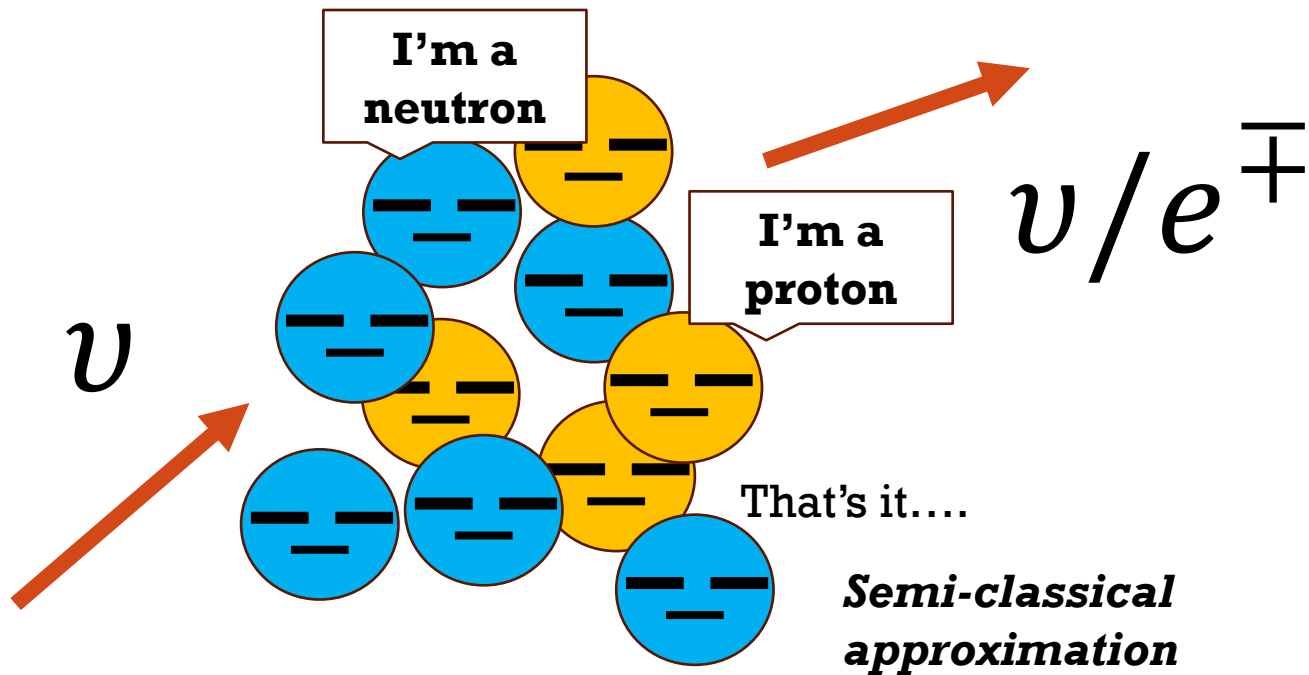


Macroscopic compact star properties

Self-consistency?

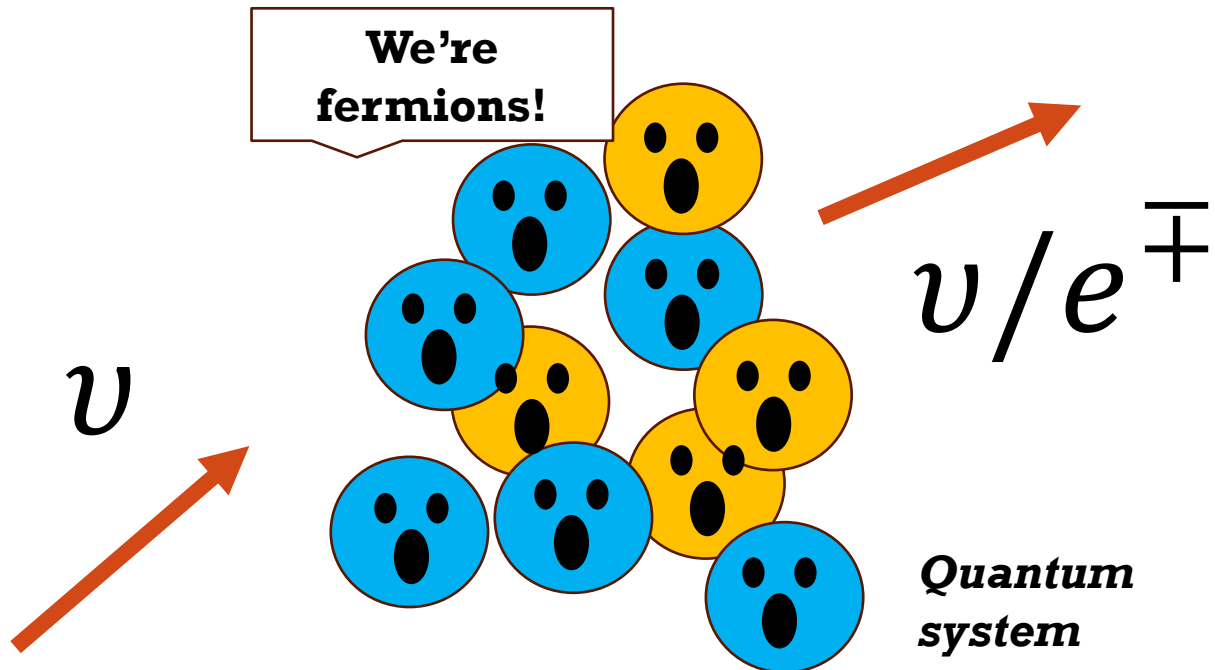
What does it mean?

How challenging it could be?



$$\lambda^{-1} = \sigma_0^{n/p} \times n_{n/p}$$

Self-consistency: Y_e , density ✓ ✓



$$\eta = 2 \int \frac{d^3 p_{n/p}}{(2\pi)^3} f_{n/p} (1 - f_{p/n})$$

$$\lambda^{-1} = \sigma_0 \times \eta$$

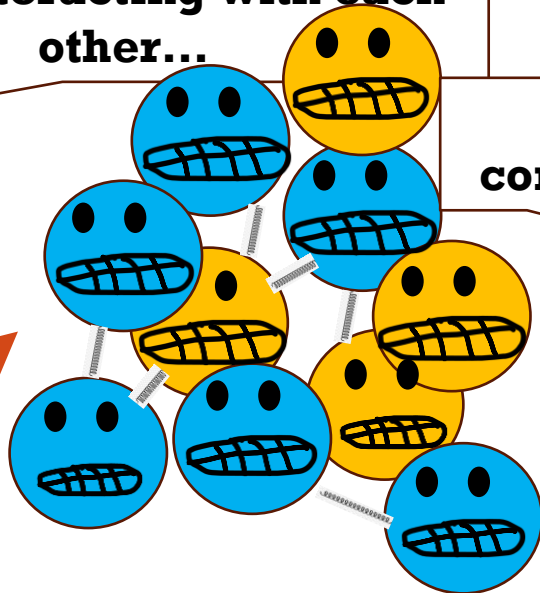
Stephen W. Bruenn, ApJS, 58:771-8411(1985)
(most nuLib data is based on this version)

Self-consistency: Y_e , density, μ_n , μ_p , μ_e , T ✓ ✓ ✓ ✓ ✓ ✓

We're interacting with each other...

We need conservation rules

v



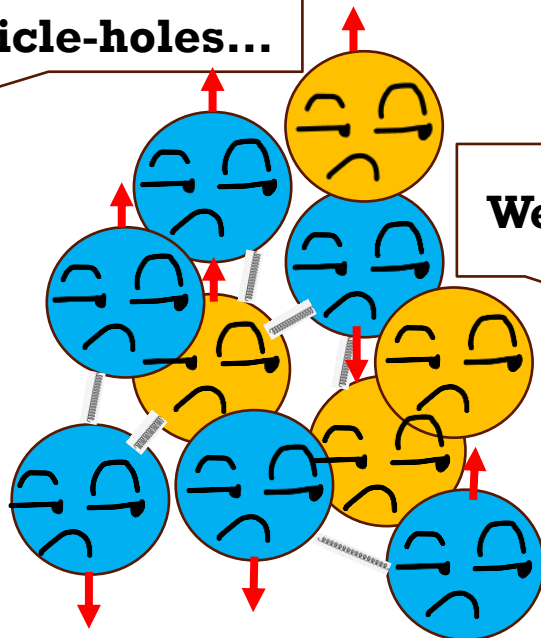
$v/e^{\mp}$

Mean-field

We have particle-holes...

We have spins!

v



$v/e^{\mp}$

RPA

$$\lambda^{-1} = \sigma_0 \int dq dq_0 S(q, q_0) \dots$$

$$S(q_0, q) = \frac{1}{2\pi^2} \int d^3p_2 \delta(q_0 + E_2 - E_4) f_2(E_2) (1 - f_4(E_4))$$

$$E_i(p_i) = \frac{p_i^2}{2M_i^*} + U_i, \quad i = n, p$$

S. Reddy, et al., PRD **58**, 013009 (1997)

Self-consistency: ..., $+U_n, U_p, M_n^*, M_p^*$

S. Reddy et al., PRC 59, 2888(1999)
A. Burrows et al., PRC 58, 554 (1998)
C. J. Horowitz et al. Phys. Rev. C 95, 025801(2017)

$S(q, q_0)$

$S_V(q, q_0)$

Spin-independent

$S_A(q, q_0)$

Spin-dependent

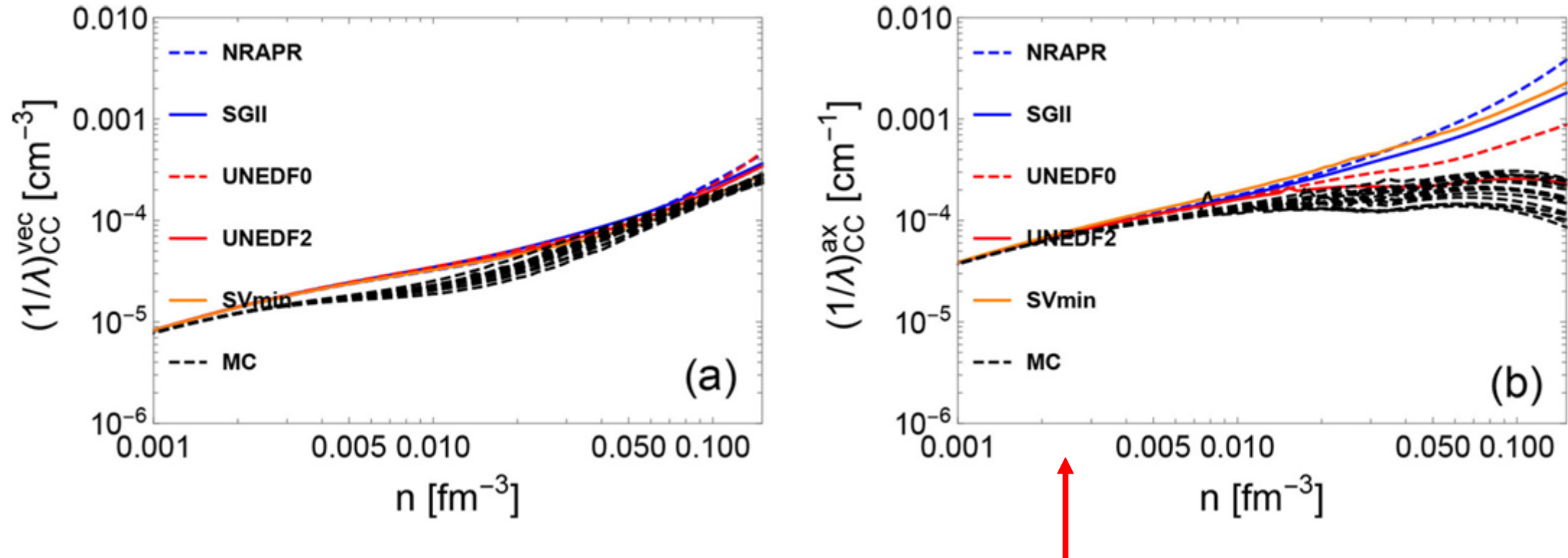
$$S(q_0, q) = \frac{2 \text{Im} \Pi}{1 - \exp[(-q_0 - \mu^\tau + \mu^{\tau'})/T]}$$

$$\Pi_{\text{RPA}}^\alpha = \frac{\Pi_0}{1 - V_{ph}^\alpha \Pi_0}$$

Self-consistency: ..., $+V_{ph}^\alpha$

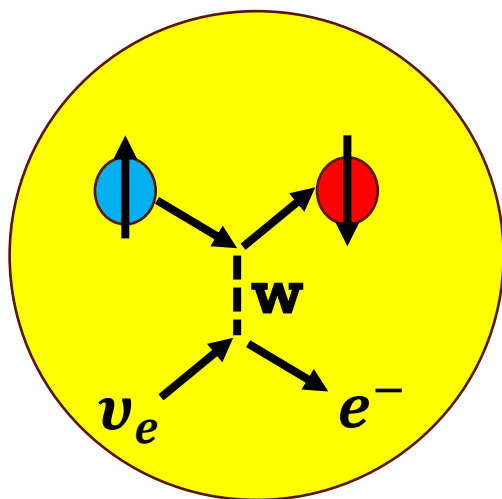
Do we have enough information to perform self-consistent calculations?

Zidu Lin, Andrew W. Steiner, and Jérôme Margueron, Phys. Rev. C **107**, 015804

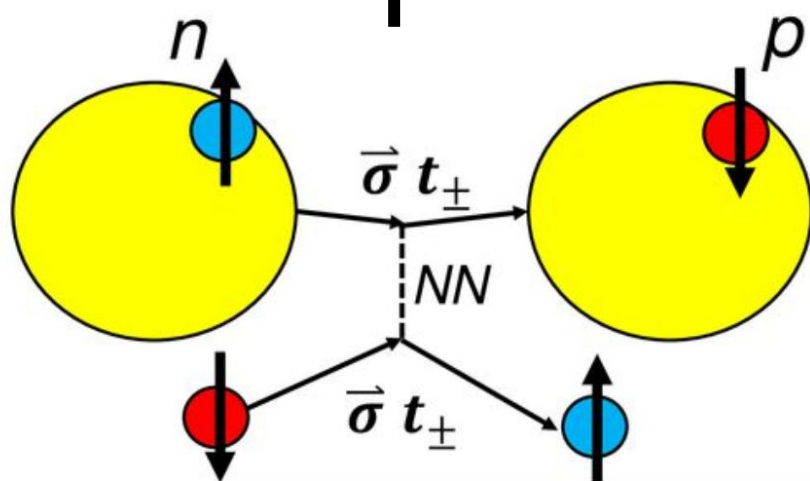


Our ignorance of **spin-dependent** nucleon-nucleon interactions results in larger uncertainties of **axial current** neutrino-nucleon reaction rates.

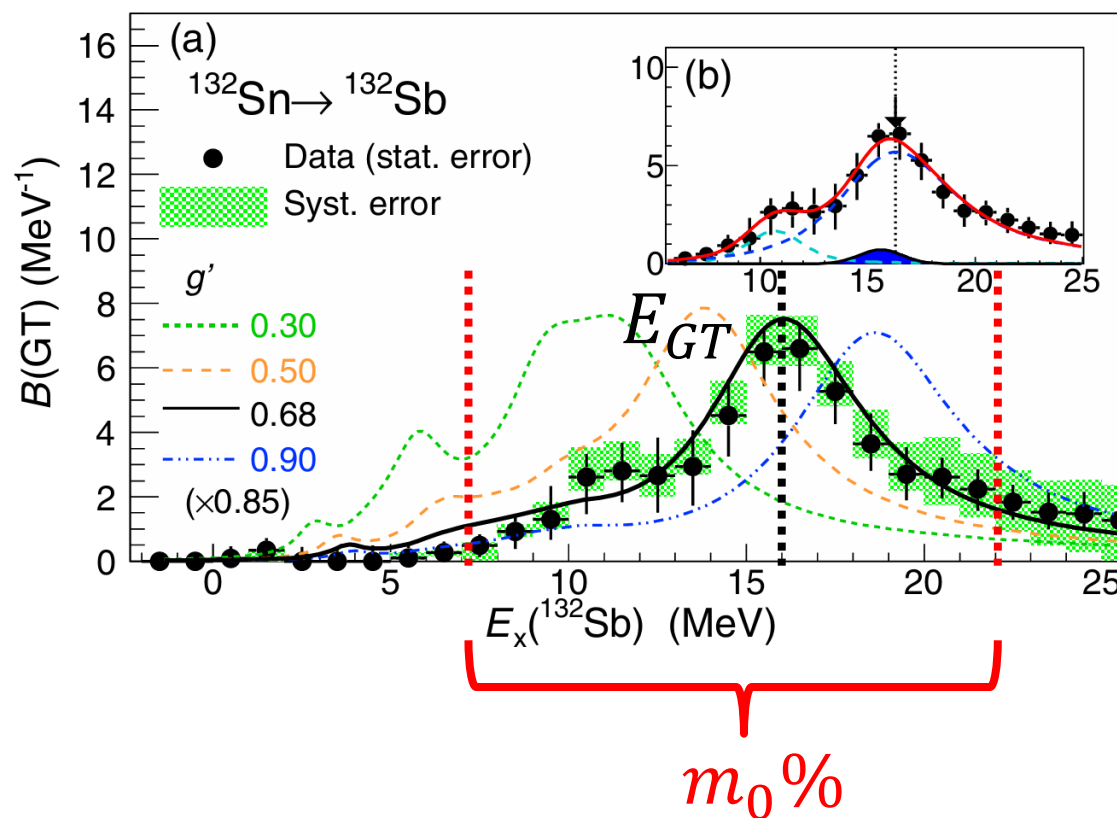
NS:

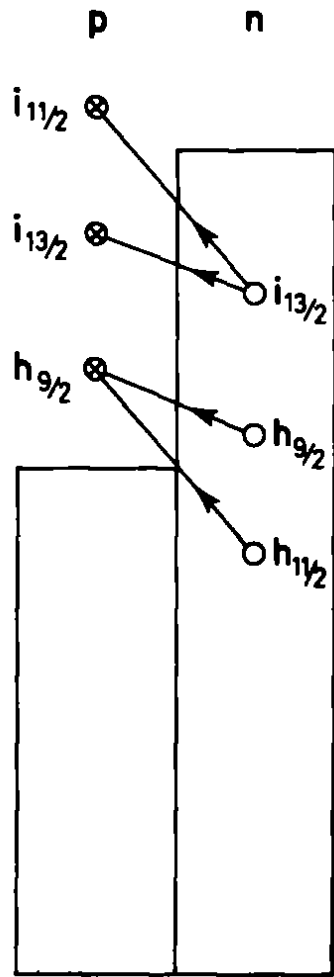


Nuclei:

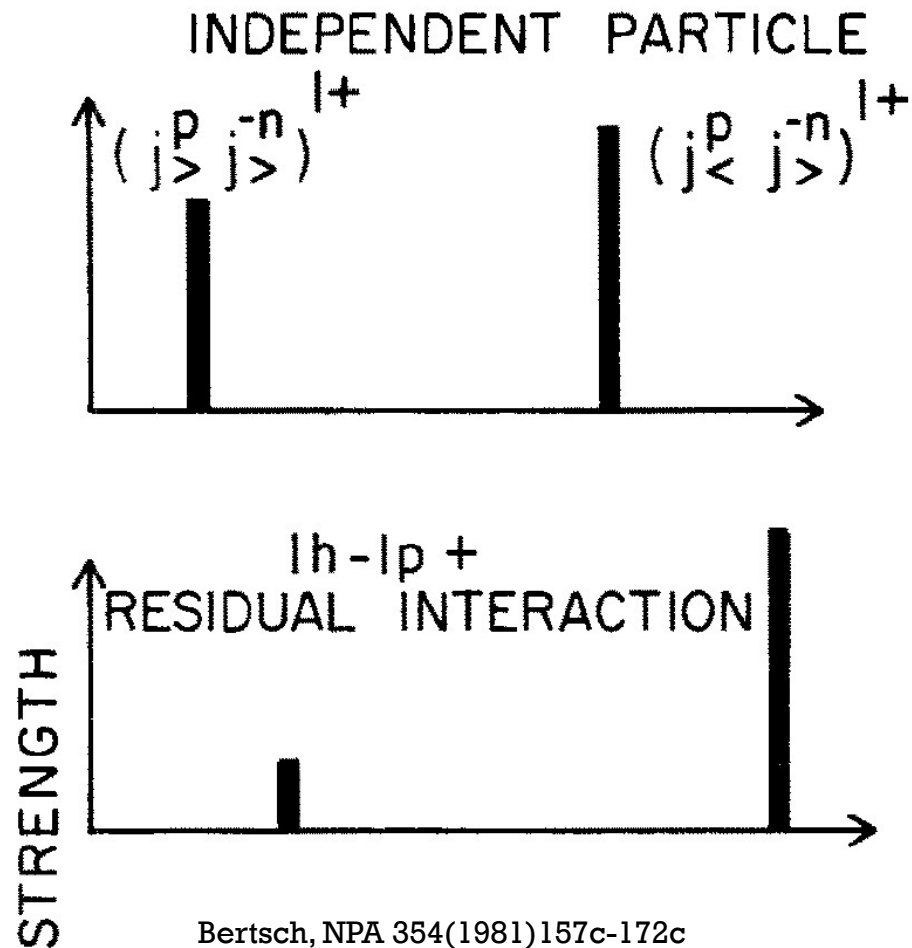


THE GAMOW-TELLER (GT) TRANSITION IN NS AND NUCLEI





Brown and Rho, NPA 372(1981)397-417

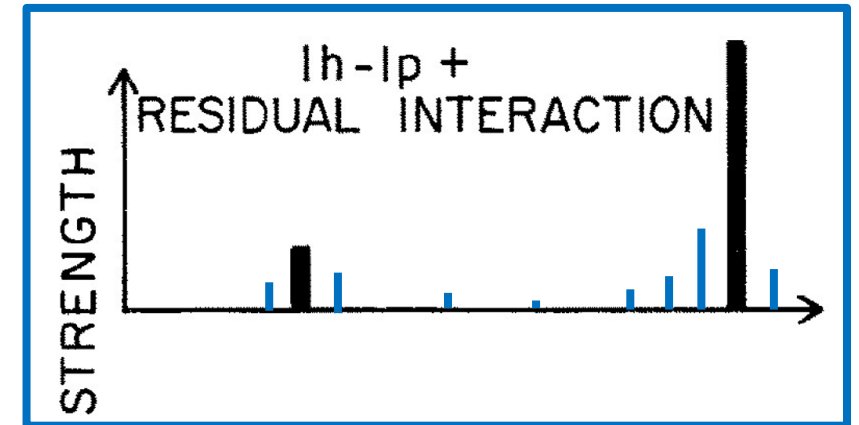


Bertsch, NPA 354(1981)157c-172c

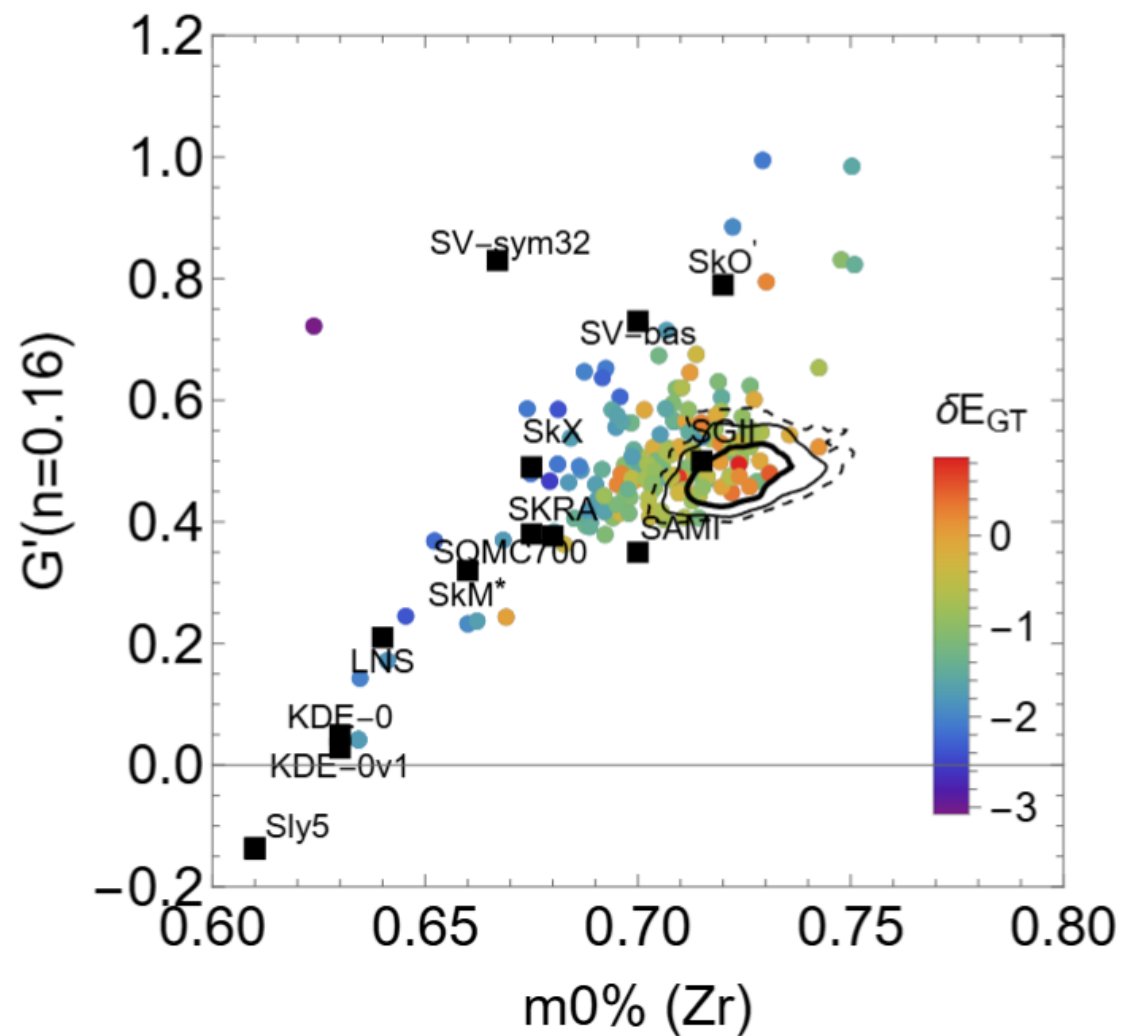
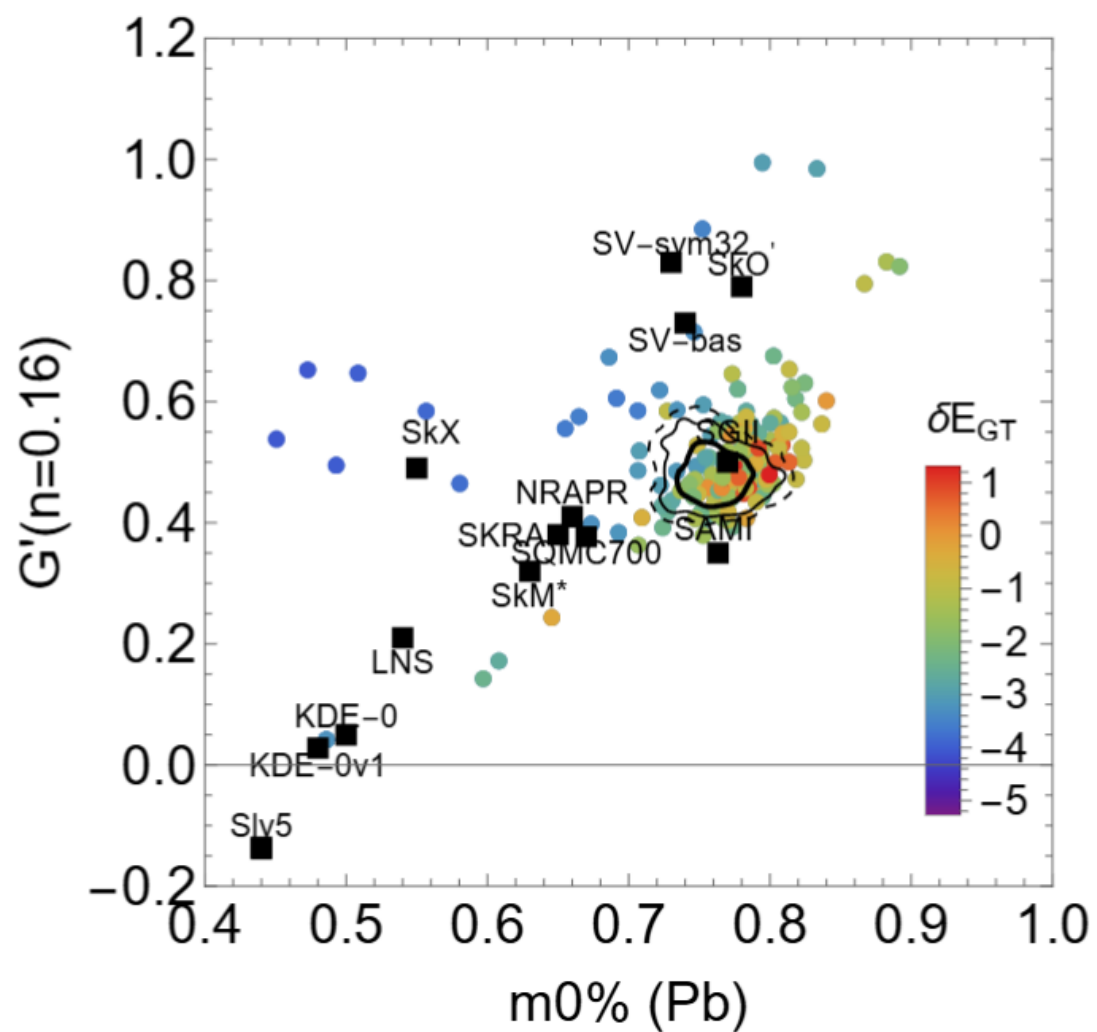
A few Experimental single particle state energy as inputs of the schematic calculation

A self-consistent calculation of single-particle energies and residual p-h interactions

$$\begin{pmatrix} A & B \\ -B^* & -A^* \end{pmatrix} \begin{pmatrix} X^n \\ Y^n \end{pmatrix} = E_n \begin{pmatrix} X^n \\ Y^n \end{pmatrix}$$



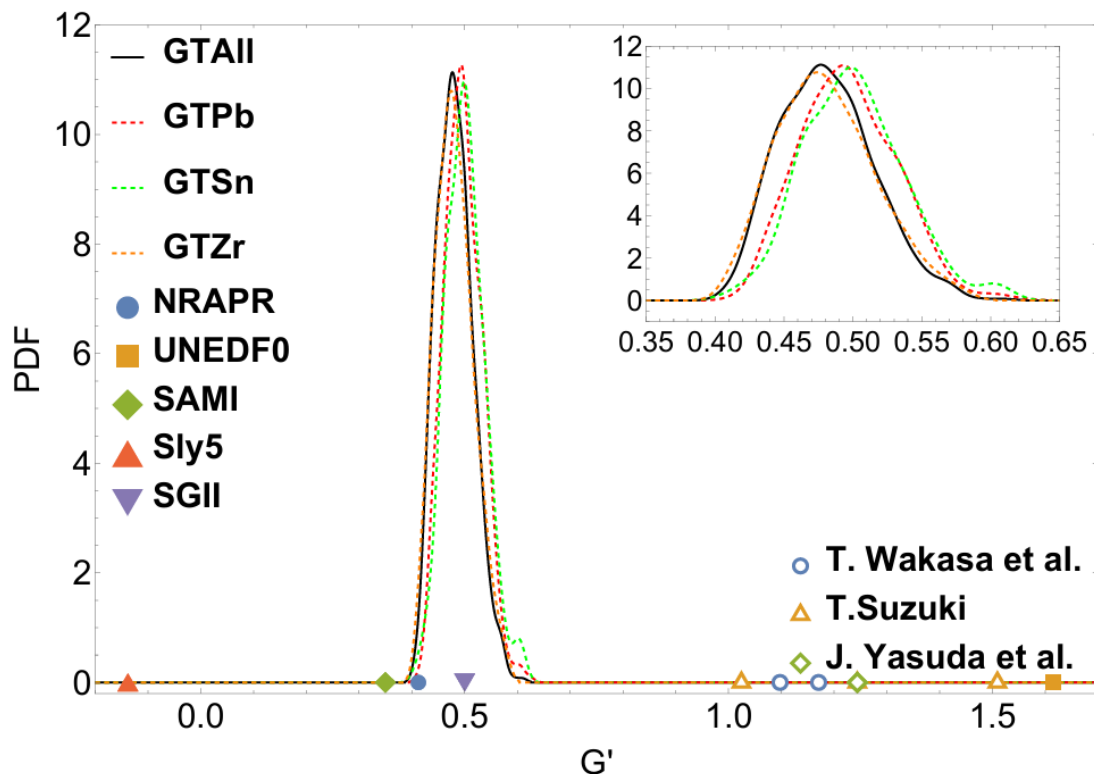
Consider many single-particle states in a self-consistent model (this work)



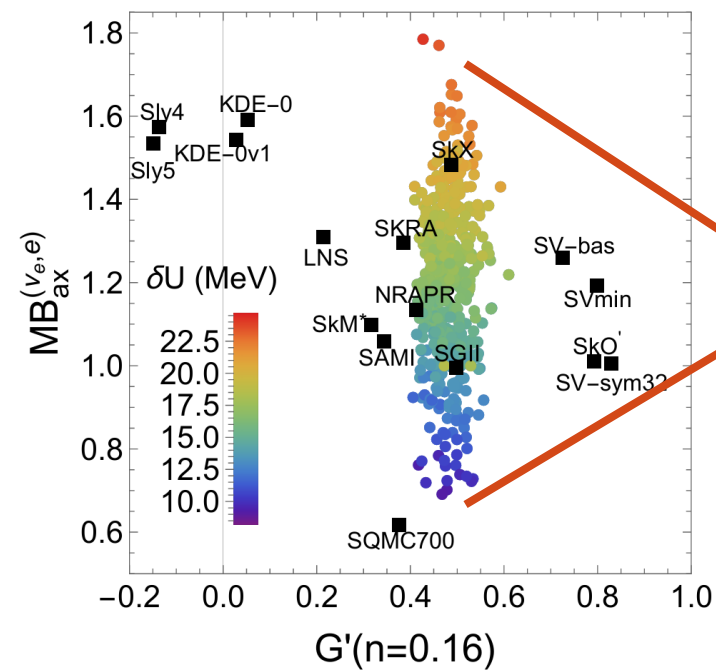
Zidu Lin, Gianluca Colò, A. W. Steiner, Amber Stinson, arXiv:2506.05564

$$MB_{ax}^{(\nu_e/\bar{\nu}_e, e^-/e^+)} = \frac{\int \frac{1}{V} \frac{d^2 \sigma_{ax}^\pm}{d\cos\theta dE_{e^-/e^+}} d\cos\theta dE_{e^-/e^+}}{\int \frac{1}{V} \frac{d^2 \sigma_{0,ax}^\pm}{d\cos\theta} d\cos\theta}$$

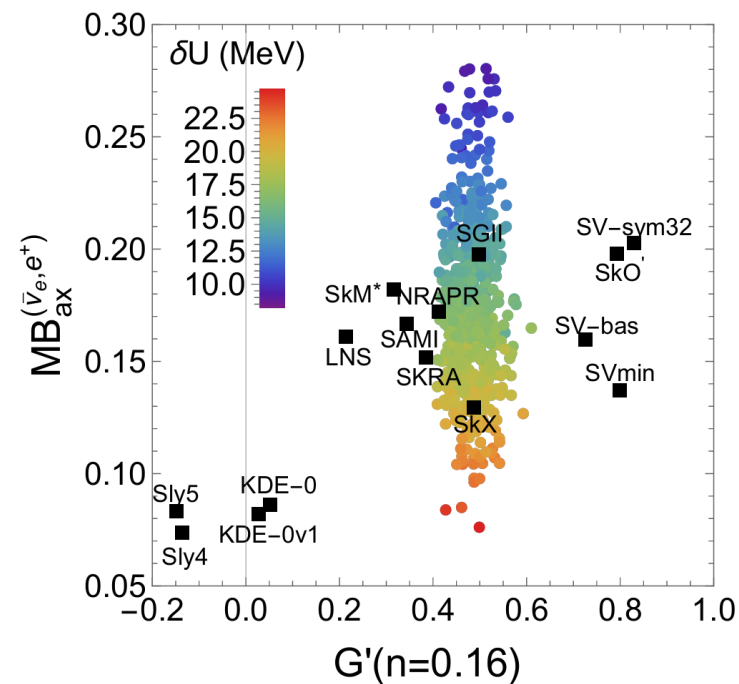
$$\frac{1}{V} \frac{d^2 \sigma_{ax}^\pm}{d\cos\theta dE_{e^-/e^+}} = \frac{G_F^2 g_A^2 p_{e^-/e^+} E_{e^-/e^+}}{4\pi^2} \times (3 - \cos\theta) S_A(q_0, q).$$



Zidu Lin, Gianluca Colò, A. W. Steiner, Amber Stinson, arXiv:2506.05564



Uncertainty
due to
ignorance of
symmetry
energy at
 $n=0.02 \text{ fm}^{-3}$

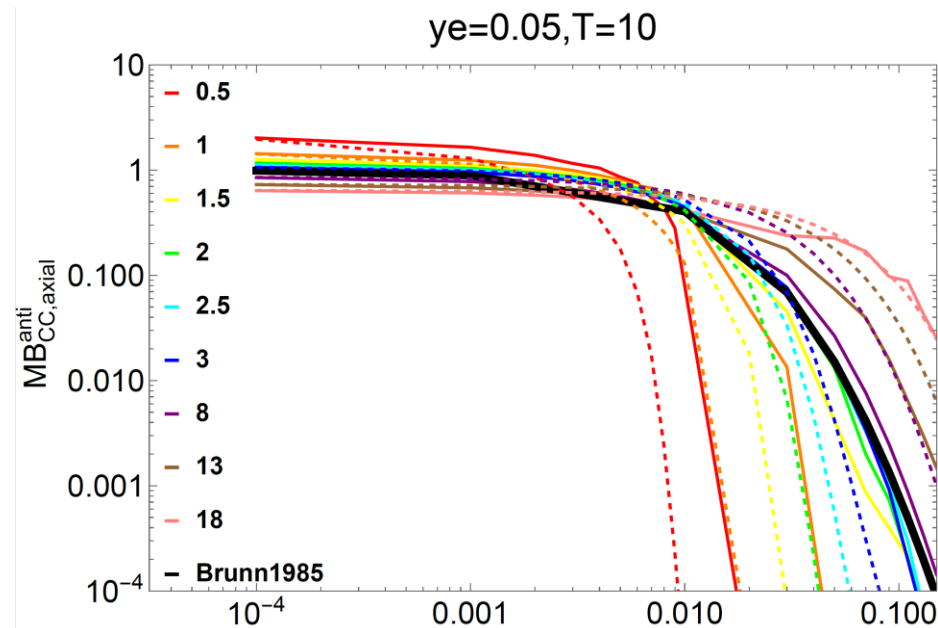
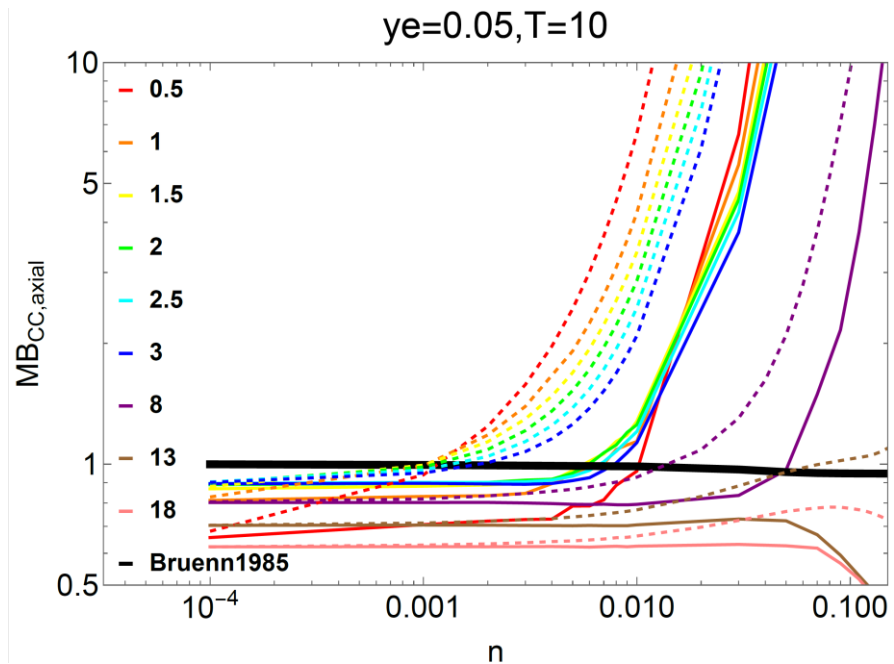


T=10 MeV
 Ye=0.05
 $E_\nu=30 \text{ MeV}$

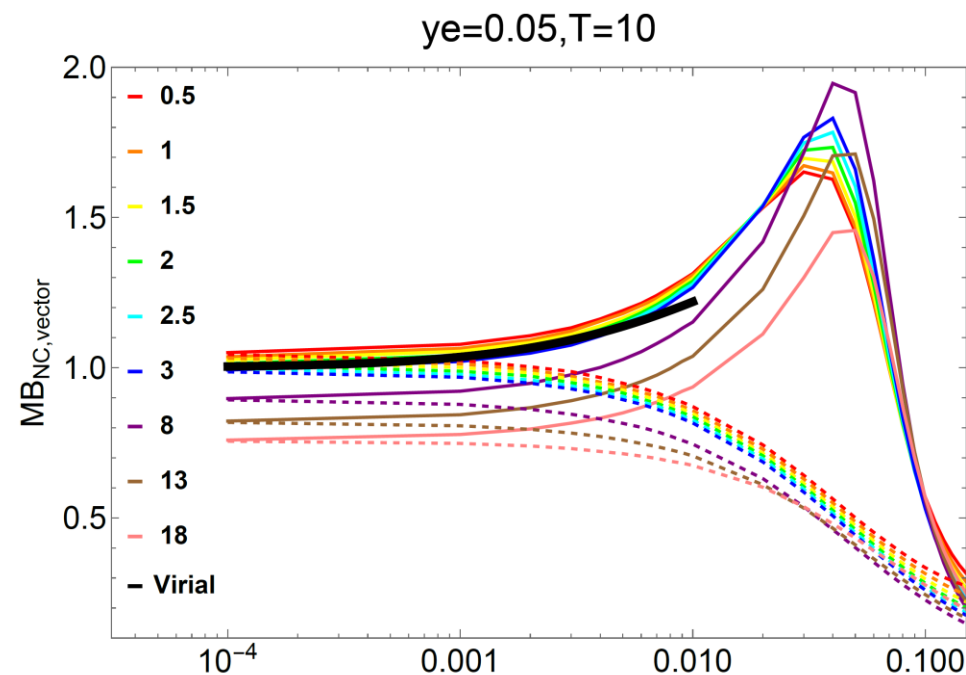
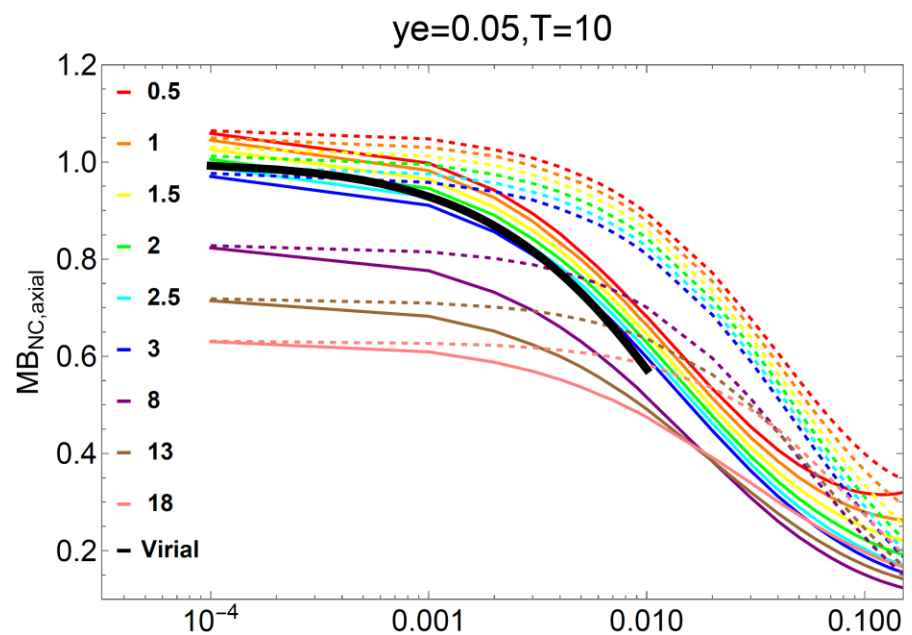
Ground&
excited
states of
finite nuclei

		Experiment	nuSkyI	nuSkyII	nuSkyIII	
²⁰⁸ Pb	B/A [MeV]	7.87 [44, 45]	7.73	7.89	7.89	
	R_{ch} [fm]	5.50 [44, 45]	5.47	5.44	5.44	
	F_{ch} []	0.409 [46]	0.412	0.418	0.417	
	ΔF []	0.041±0.013 [46]	0.0241	0.0185	0.0288	
	E_{GT} [MeV]	19.2 [47, 48]	20.04	20.05	19.46	
	$m_0\%$ []	74% ± 1.48% [47, 48]	75.6%	77.0%	74.8%	
¹³² Sn	B/A [MeV]	8.355 [44, 45]	8.25	8.36	8.37	
	R_{ch} [fm]	4.71 [44, 45]	4.69	4.67	4.67	
	E_{GT} [MeV]	13.97 [43]	14.66	14.56	13.97	
	$m_0\%$ []	81% ± 16% [43]	79.23%	79.54%	78.72%	
⁹⁰ Zr	B/A [MeV]	8.71 [44, 45]	8.65	8.74	8.79	
	R_{ch} [fm]	4.27 [44, 45]	4.23	4.23	4.22	
	E_{GT} [MeV]	15.8 [49]	16.2	16.0	16.15	
	$m_0\%$ []	68% ± 1.4% [49]	69.8%	72.8%	70.7%	
⁴⁸ Ca	B/A [MeV]	8.67 [44, 45]	8.78	8.82	8.86	
	R_{ch} [fm]	3.48 [44, 45]	3.46	3.48	3.46	
	F_{ch} []	0.158 [50]	0.155	0.154	0.155	
	ΔF []	0.0277±0.0055 [50]	0.0423	0.036	0.0422	
	E_{GT} [MeV]	10.5 [51]	11.0	10.6	10.8	
Landau-Migdal Parameter		G'_0 []	0.44 ± 0.09 (this work)	0.35	0.44	0.41
NS	$R_{1.4}$ [km]	12.71 ^{+1.14} _{-1.19} [52] ; 13.02 ^{+1.24} _{-1.06} [53]	12.12	N/A	12.20	
	M_{max} [$M_\odot$]	> 2.0	2.08	N/A	2.05	

Infinite dense
matter
properties



Colored curves: $\frac{E_v}{T}$
Solid curves: RPA
Dashed Curves: MF



To understand the influence of **microscopic** nuclear many-body calculations on **macroscopic** numerical simulations.

A calculation at representative environment is not enough.

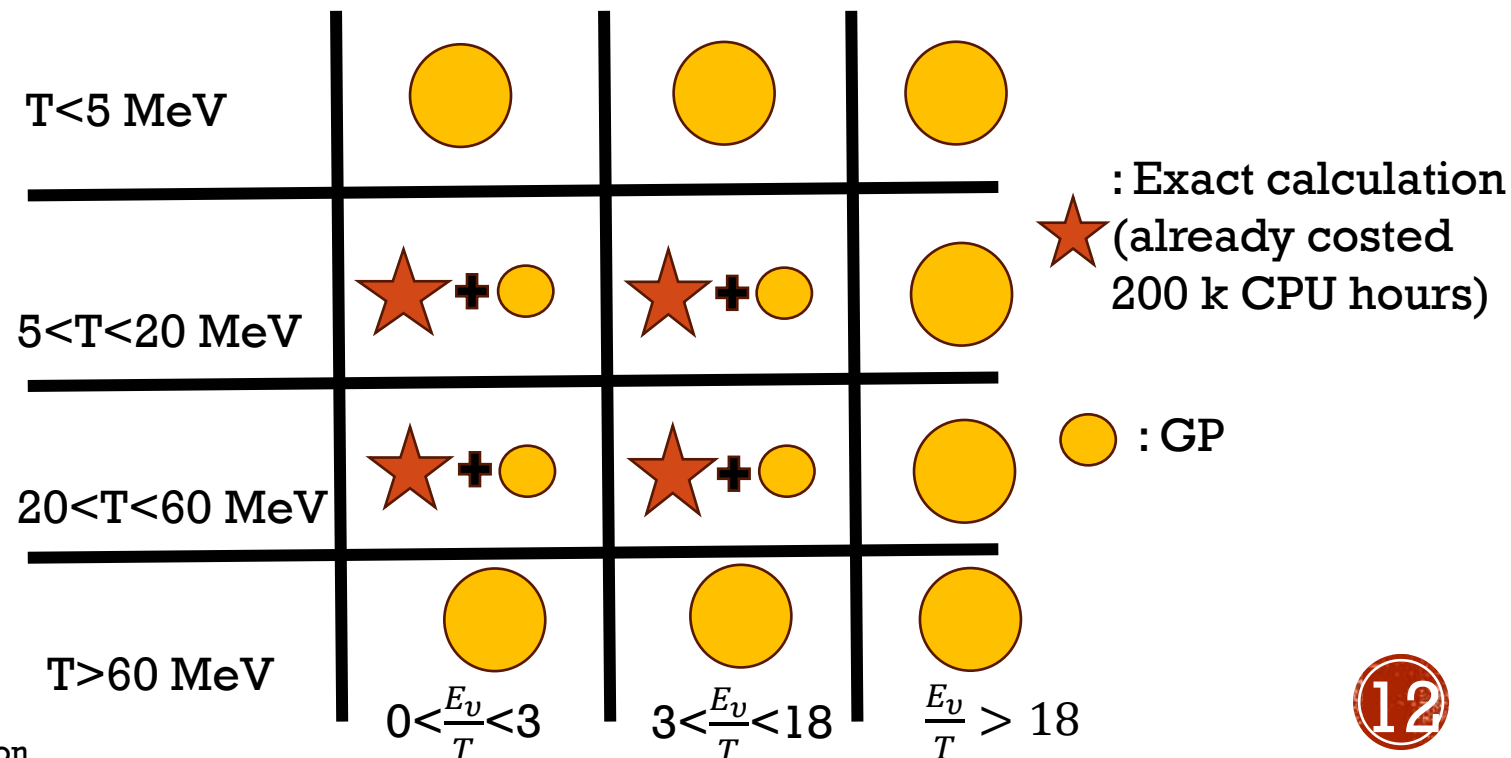
MANY many-body calculations at various conditions are needed

Exact RPA calculations + Gaussian Process (GP)

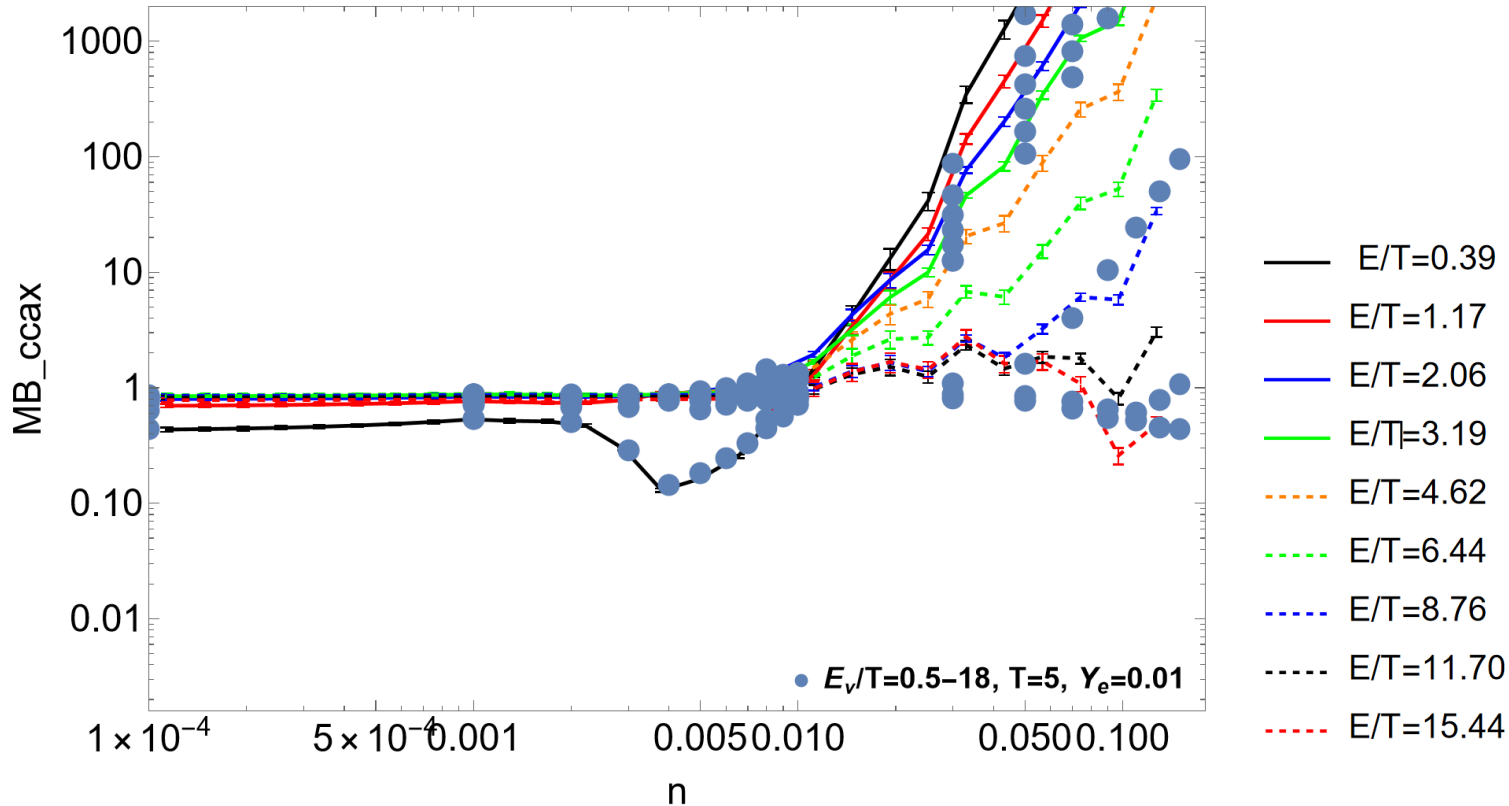
Need for high-fidelity many-body calculations (from nuclear physics side)



Need for high-resolution and wide-spreading grids of ν opacity (from simulation side)



$\sigma_{mb}=0.5$, no data noise

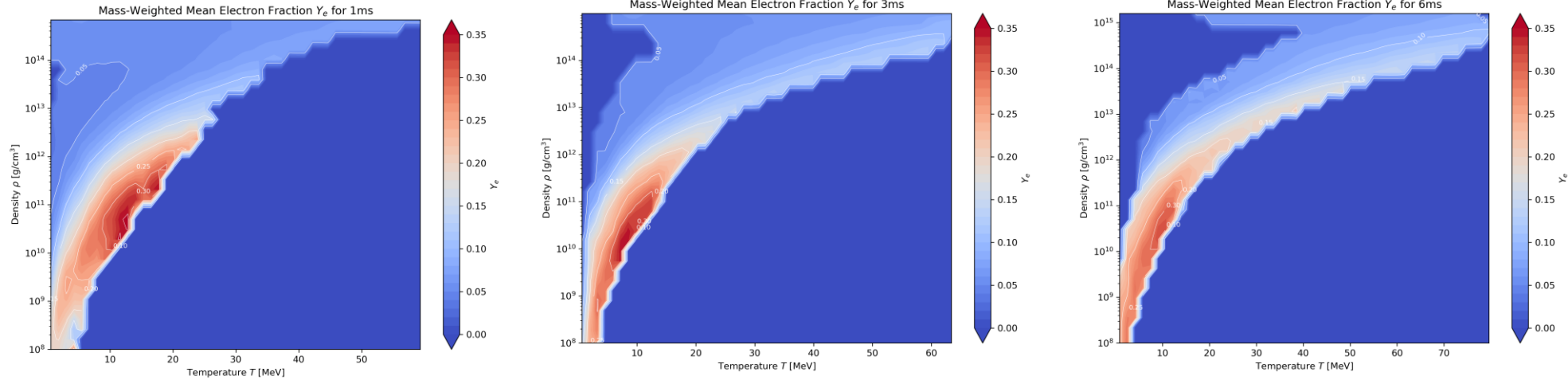


GP:
 $\text{Prob}(\vec{F}_{pre} | \vec{F}_D)$

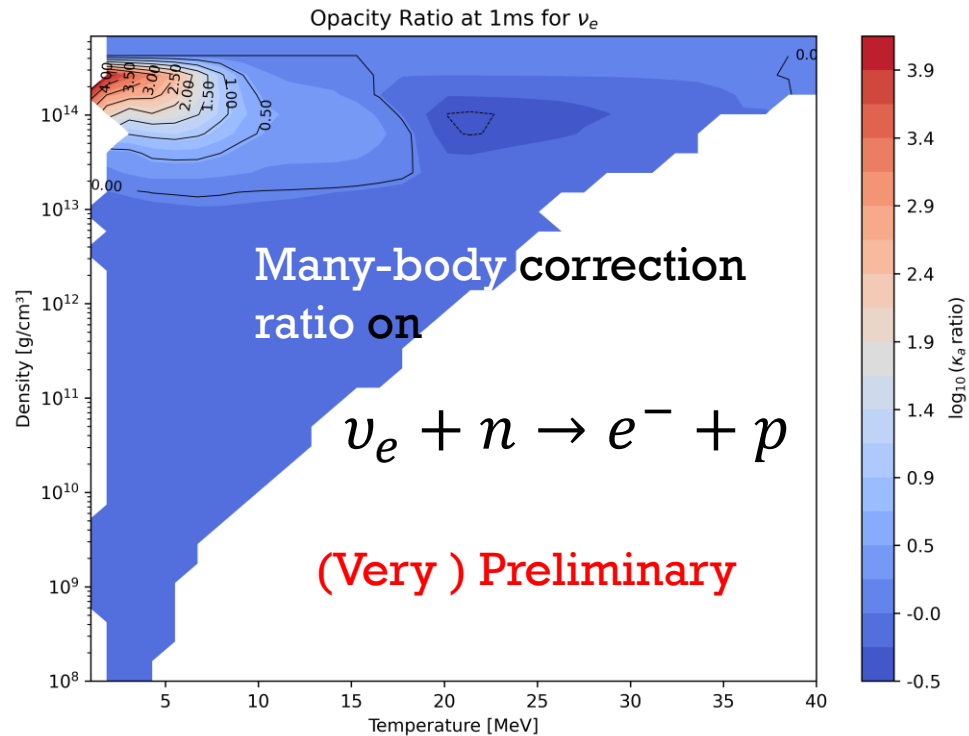
GP gives conditional probability of
 interpolated (extrapolated)
 neutrino many-body correction
 based on the data (with/without
 uncertainties)

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{y} \end{bmatrix} \sim \mathcal{N} \left(\begin{bmatrix} \mu_x \\ \mu_y \end{bmatrix}, \begin{bmatrix} A & C \\ C^\top & B \end{bmatrix} \right) \quad \mathbf{x} | \mathbf{y} \sim \mathcal{N}(\mu_x + CB^{-1}(\mathbf{y} - \mu_y), A - CB^{-1}C^\top)$$

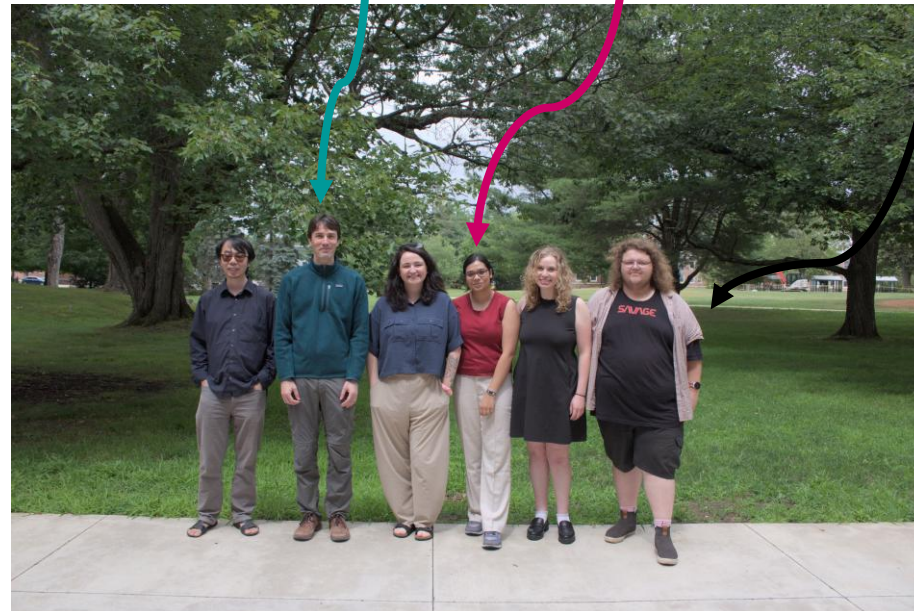
New opacity in BNS mergers



Y_e distribution in the first 6 ms after the merger



Credit to *F. Foucart*, *S. Rath*, *P. Hammond*



Thanks!



Backup



Solving for RPA equations

$$G_{RPA}^{\alpha}(q_0, q, \vec{k}_1) = G_{HF}(q_0, q, \vec{k}_1) + G_{HF}(q_0, q, \vec{k}_1) \\ \times \sum_{\alpha'} \int \frac{d^3 k_2}{(2\pi)^3} V_{ph}^{\alpha, \alpha'}(q, \vec{k}_1, \vec{k}_2) \times G_{RPA}^{\alpha'}(q_0, q, \vec{k}_2)$$

$$\langle G \rangle_{RPA} = (\beta_0 + 2W_2^{\alpha}(\beta_0\beta_3 - \beta_1^2)q^2) \\ / \{1 - W_1^{\alpha}\beta_0 + 2q^2W_2^{\alpha}[-\beta_2 + \beta_3 + W_1^{\alpha}(\beta_1^2 - \beta_0\beta_3)] + q^4(W_2^{\alpha})^2[-\beta_0\beta_5 + 4(\beta_1\beta_4 - \beta_2\beta_3) + \beta_2^2] \\ + 2q^6(W_2^{\alpha})^3[-\beta_0\beta_3\beta_5 + \beta_0\beta_4^2 + \beta_1^2\beta_5 - 2\beta_1\beta_2\beta_4 + \beta_2^2\beta_3]\},$$

$$\beta_l = \int \frac{d^3 k}{(2\pi)^3} G_{HF} F_l$$

$$F_{0-5} = \left\{1, \frac{\vec{k} \cdot \vec{q}}{q^2}, \frac{k^2}{q^2}, \frac{(\vec{k} \cdot \vec{q})^2}{q^4}, \frac{\vec{k} \cdot \vec{q} k^2}{q^4}, \frac{k^4}{q^4}\right\}$$

E. S. Hernandez, J. Navarro, and A. Polls, Nucl. Phys. A 658, 327 (1999).

J. Margueron, J. Navarro, and N. Van Giai, Phys. Rev. C 74, 015805 (2006)

