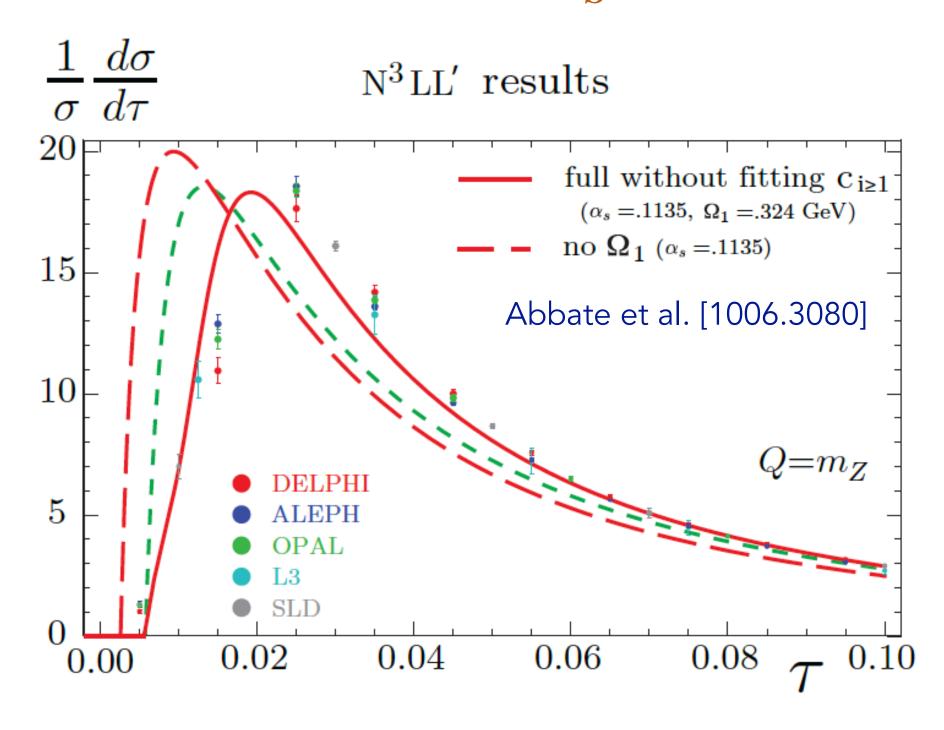
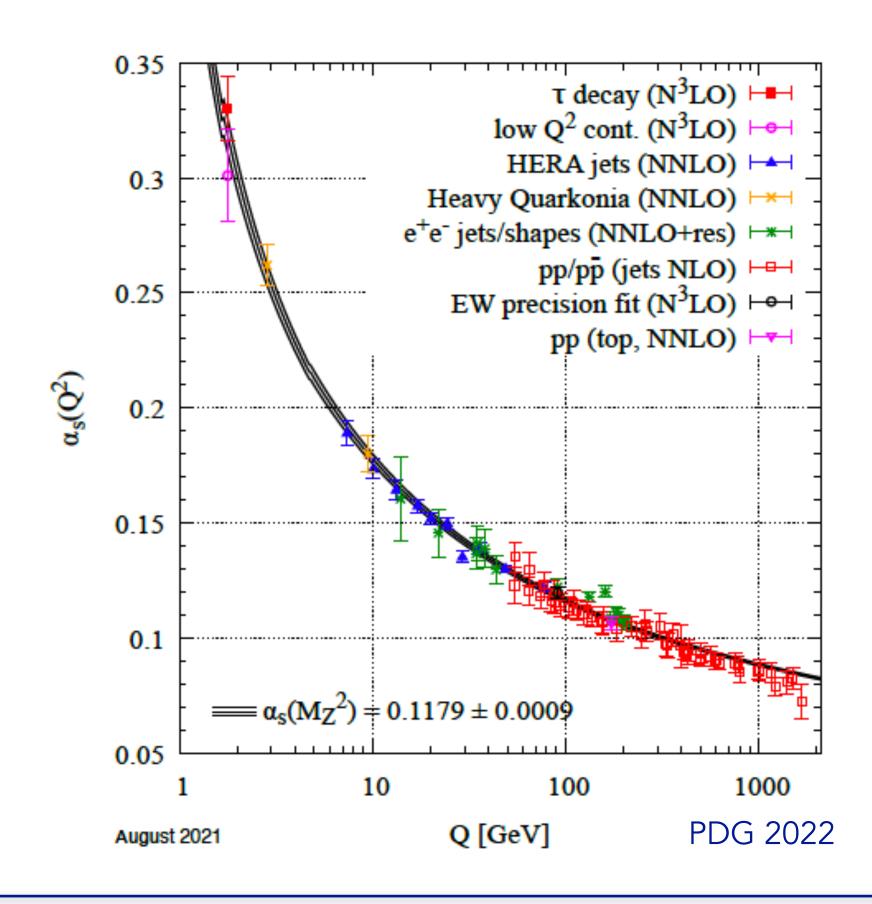
# Impact of nonperturbative effects on determination of $\alpha_s$ from event shapes

#### Christopher Lee (LANL)



INT Workshop on Probing QCD at High Energy and Density with Jets







#### Collaborators

- ■G. Bell, Y. Makris, J. Talbert, B. Yan, [arXiv:soon]
- See also G. Bell, A. Hornig, CL, J. Talbert, [arXiv:1808.07867]

#### Outline of the talk

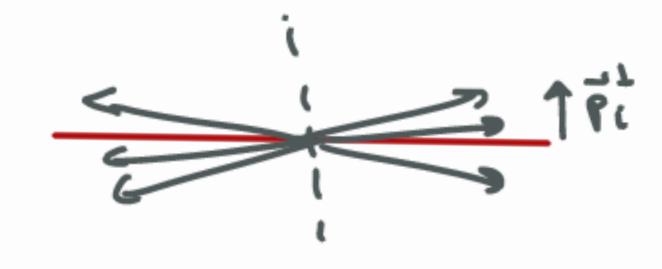
- Event shapes and the strong coupling
- ■EFT, factorization, resummation of perturbative logs
- Nonperturbative corrections and renormalon subtraction schemes
- •Effects of perturbative and nonperturbative scale & scheme choices on fits for  $\alpha_{\rm s}$ 
  - In a nutshell: some of these choices have a few % effect on the tails of event shape distributions and the values of  $\alpha_s$  extracted by comparing them to data
- Motivations for more data on more event shapes

HADRONIC EVENT SHAPES: Global measures of "jety" structure

ete -> hadrons SAT

T= 1 max 2 [Pi. E] THRUST:

B= & ZIPil BROADENING:

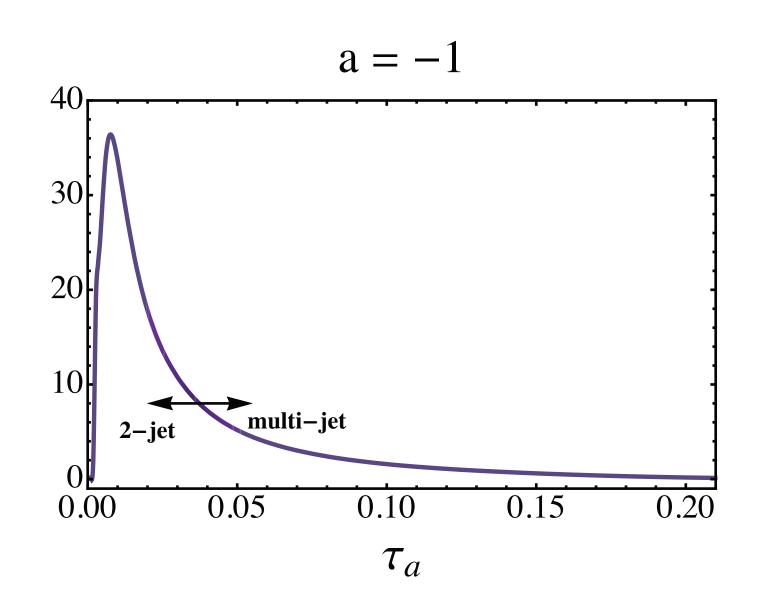


# Angularity event shapes in e+e- collisions

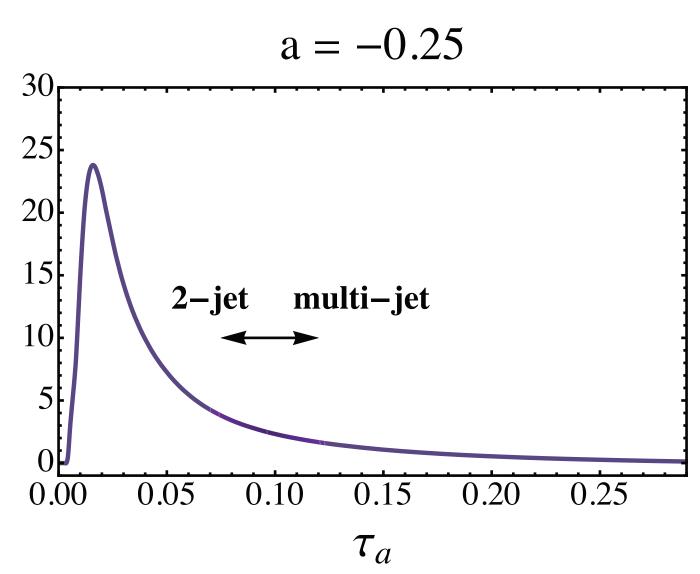
■ Consider Angularities, which can be defined in terms of the rapidity and  $p_T$  of a final state particle 'i', with respect to the thrust axis:

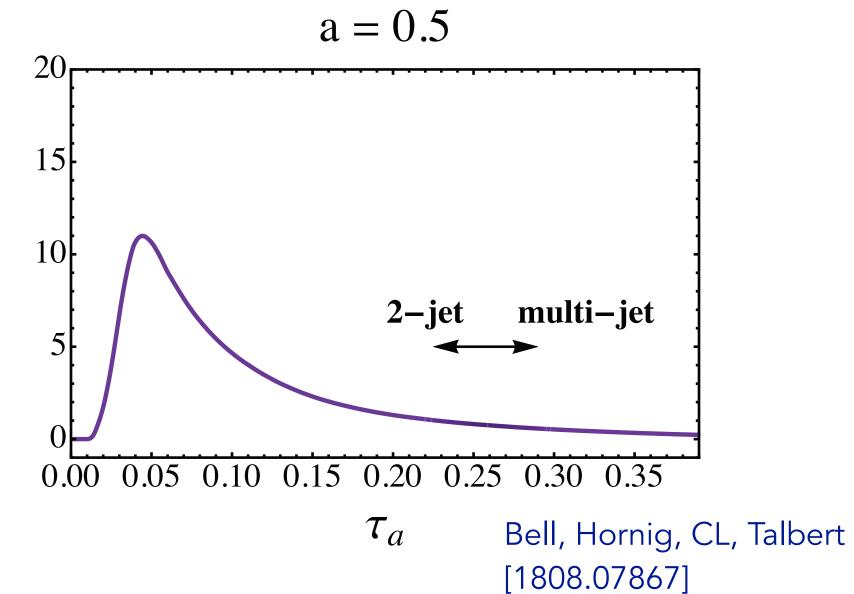
Berger, Kucs, Sterman [hep-ph/0303051]

IR safe for  $a \in \{-\infty, 2\}$ 



$$\tau_a = \frac{1}{Q} \sum_i |\mathbf{p}_{\perp}^i| e^{-|\eta_i|(1-a)}$$

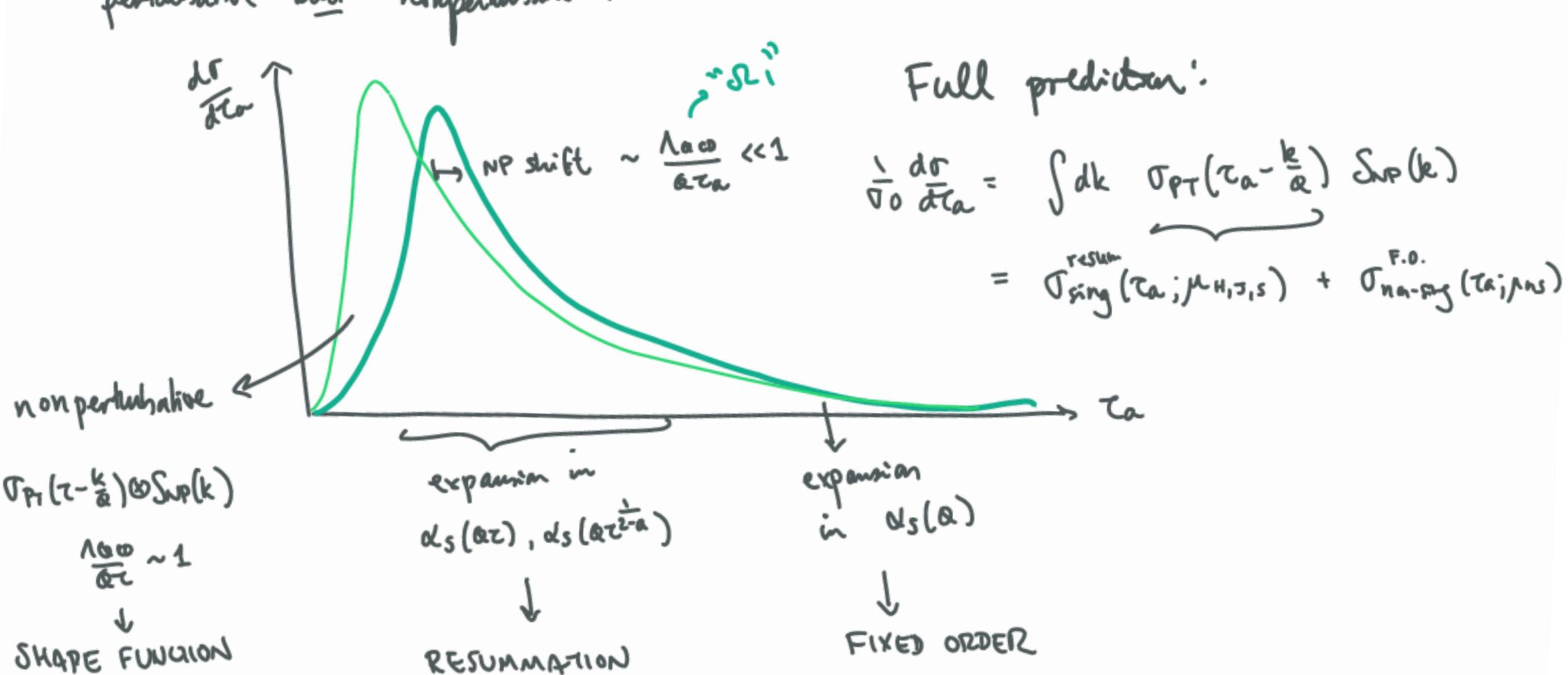




(for some arbitrary, but uniform, definition of "2-jet")

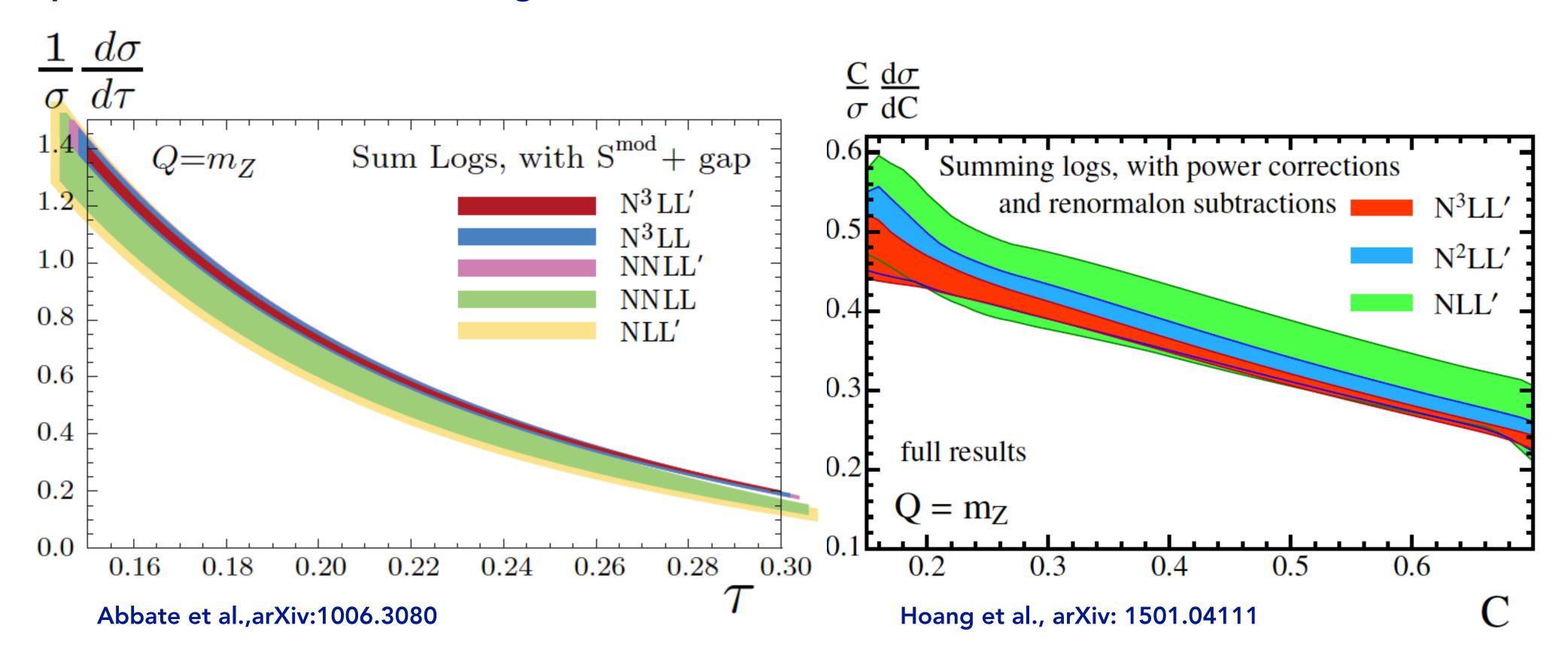
# EVENT SHAPES & SENSITIVITY TO WS

Ta's and similar event shapes probe QD effects over wide range of scales, perhabative and nonperturbative:



# Event shapes to high precision

■ First N³LL' resummed event shape distributions with state-of-the-art treatment of nonperturbative corrections, e.g.:



Makes e+e- event shapes one of the most precise ways, in principle, to determine  $\alpha_s$ 

Event shapes and the strong coupling

Abbate et al., PRD 83 (2011) 074021

0.115

0.120

 $\blacksquare$  N<sup>3</sup>LL'

ightharpoonup  $m N^3LL$ 

NNLL'

NNLL

- NLL'

0.125

0.130

 $\alpha_s(m_Z)$ 

full

results

(GeV)

0.8

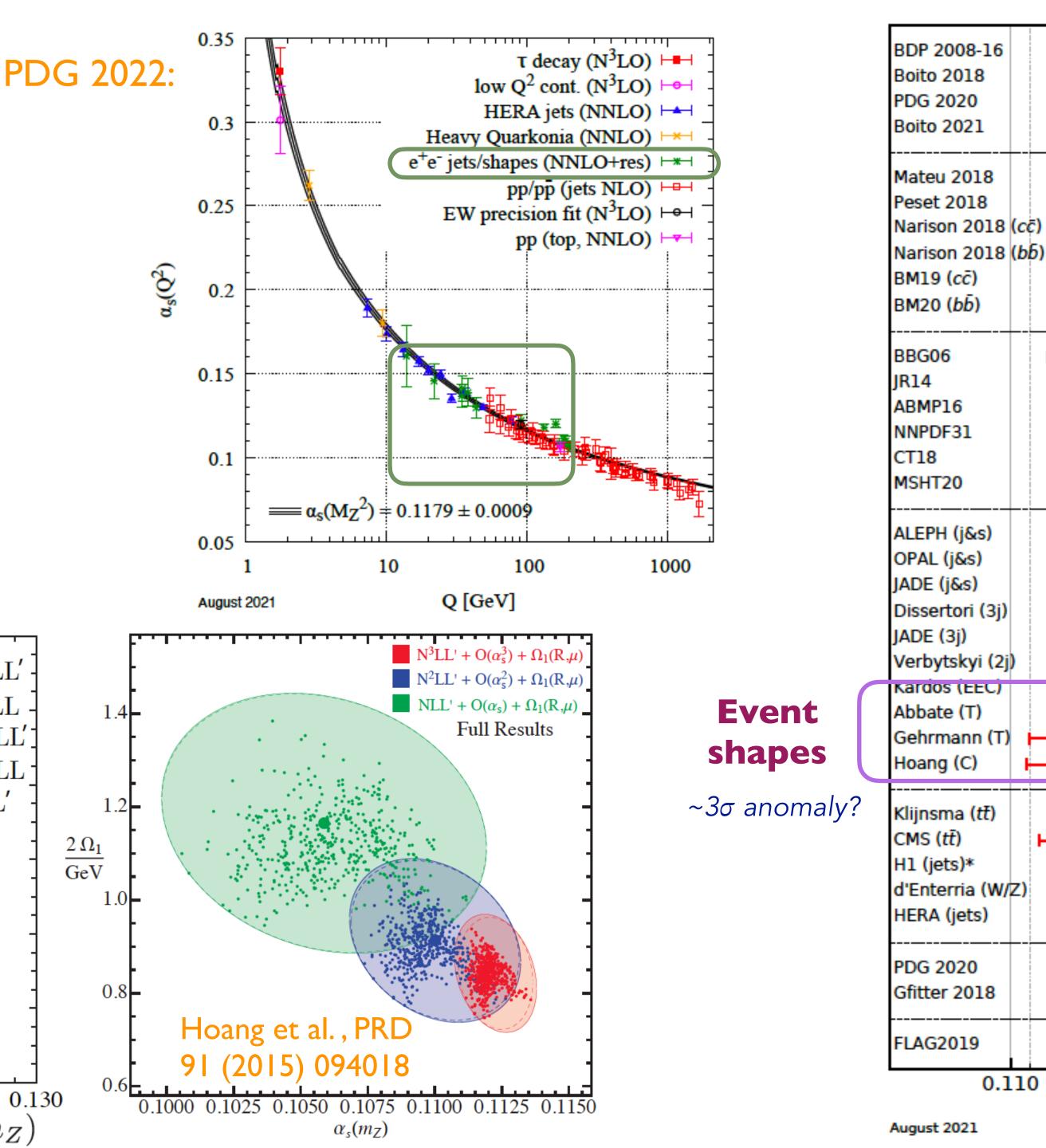
0.6

0.4

0.2

0.0

0.110



τ decays

low Q<sup>2</sup>

 $Q\overline{Q}$ 

bound

states

PDF fits

e+e

jets

shapes

hadron

collider

electroweak

lattice

0.130

 $\alpha_s(M_Z^2)$ 

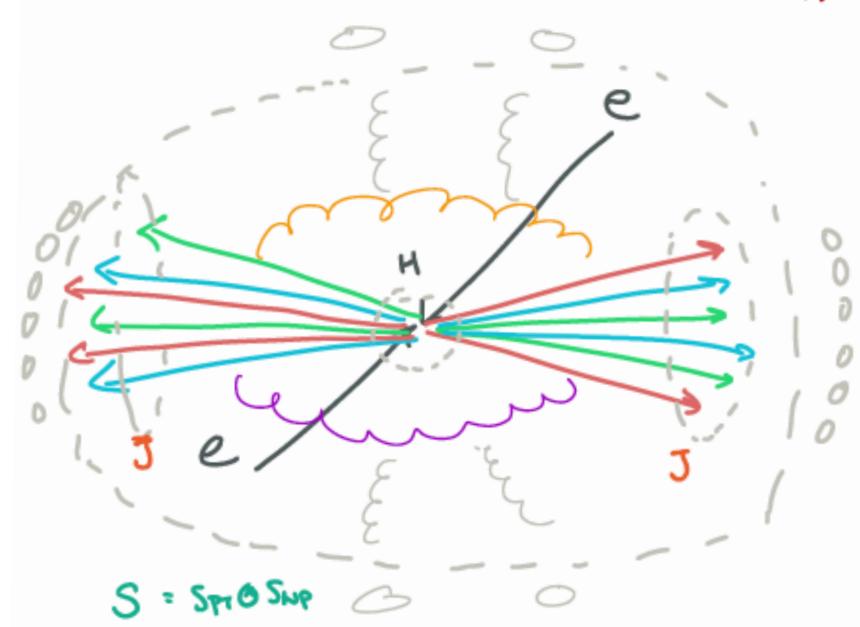
0.125

0.110

0.115

0.120

# Factorization, Resummation and Nonperturbative Effects in EFT



$$\times \int dt_3 dt_3 dk_3 = \delta \left( z_a - \frac{t_3 t_3}{a^{2-a}} - \frac{k_3}{a} \right)$$

$$X \left\{ \begin{array}{c} \mathcal{E} \\ \mathcal{E}$$

defined as matrix elemente.
of opendors in SCET

$$K_{S} = \sum_{i}^{k} (n_{i}k_{i})^{t_{i}} (n_{i}k_{i})^{t_{i}}$$

$$= \sum_{i}^{k} (k_{i}m_{i})^{t_{i}}$$

# Evolution and resummation of logs

An all-order dijet factorization theorem for the observable is easily derived in SCET:

$$d\sigma \sim H \cdot \mathcal{J} \otimes \mathcal{J} \otimes \mathcal{S}$$

RGE 
$$\frac{dH(Q^2, \mu)}{d \ln \mu} = \left[ 2\Gamma_{cusp} \ln(\frac{Q^2}{\mu^2}) + 4\gamma_H(\alpha_s) \right] H(Q^2, \mu)$$

hep-ph/0303051 hep-ph/1401.4460

Evolving all scales to/from their 'natural' settings, one arrives at the resummed cross section:

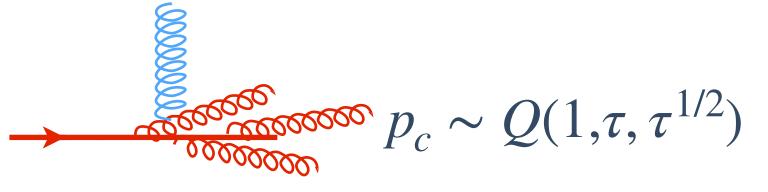
$$\frac{\sigma_{\text{sing}}(\tau_a)}{\sigma_0} = e^{K(\mu,\mu_H,\mu_J,\mu_S)} \left(\frac{\mu_H}{Q}\right)^{\omega_H(\mu,\mu_H)} \left(\frac{\mu_J^{2-a}}{Q^{2-a}\tau_a}\right)^{2\omega_J(\mu,\mu_J)} \left(\frac{\mu_S}{Q\tau_a}\right)^{\omega_S(\mu,\mu_S)} H(Q^2,\mu_H) \qquad \mathcal{F}(\Omega) = \frac{e^{\gamma_E \Omega}}{\Gamma(-\Omega)} \times \widetilde{J} \left(\partial_{\Omega} + \ln \frac{\mu_J^{2-a}}{Q^{2-a}\tau_a}, \mu_J\right)^2 \widetilde{S} \left(\partial_{\Omega} + \ln \frac{\mu_S}{Q\tau_a}, \mu_S\right) \times \begin{cases} \frac{1}{\tau_a} \mathcal{F}(\Omega) & \sigma = \frac{d\sigma}{d\tau_a} \\ \mathcal{G}(\Omega) & \sigma = \sigma_c \end{cases} \qquad \mathcal{G}(\Omega) = \frac{e^{\gamma_E \Omega}}{\Gamma(1-\Omega)}$$

**Hard** 

$$\mu_H = Q$$

$$p_S \sim Q(\tau, \tau, \tau)$$

$$\mu_I = Q \tau^{1/2}$$



Soft

$$\mu_S = Q\tau$$

$$\gamma_F(\mu) = -j_F \kappa_F \Gamma_{\text{cusp}}[\alpha_s(\mu)] \ln \frac{Q_F}{\mu} + \gamma_F[\alpha_s(\mu)]$$

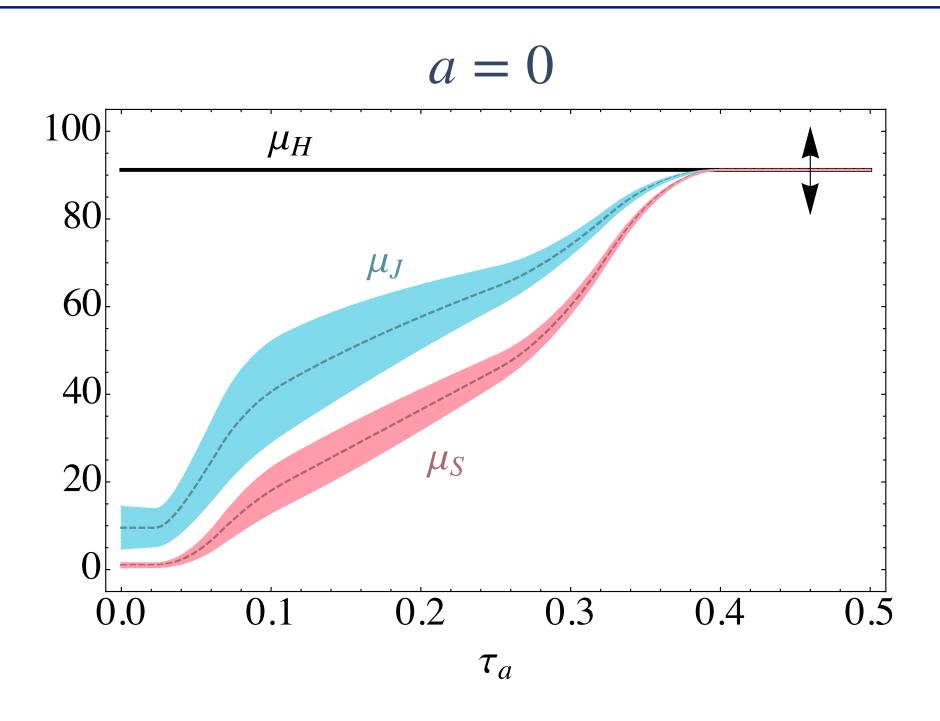
$$\Omega = 2\omega_J + \omega_S$$

$$\omega_F = -2\kappa_F \int_{\mu_F}^{\mu} \frac{d\mu'}{\mu'} \Gamma_{\text{cusp}}[\alpha_s(\mu')]$$

$$\Sigma \int_{\mu_F}^{\mu} d\mu'$$

$$K = \sum_{F=H,J,S} \int_{\mu_F}^{\mu} \frac{d\mu'}{\mu'} \gamma_F(\mu')$$

# Perturbative scale profiles



Will consider two non-singular scale choices "2010" and "2018":

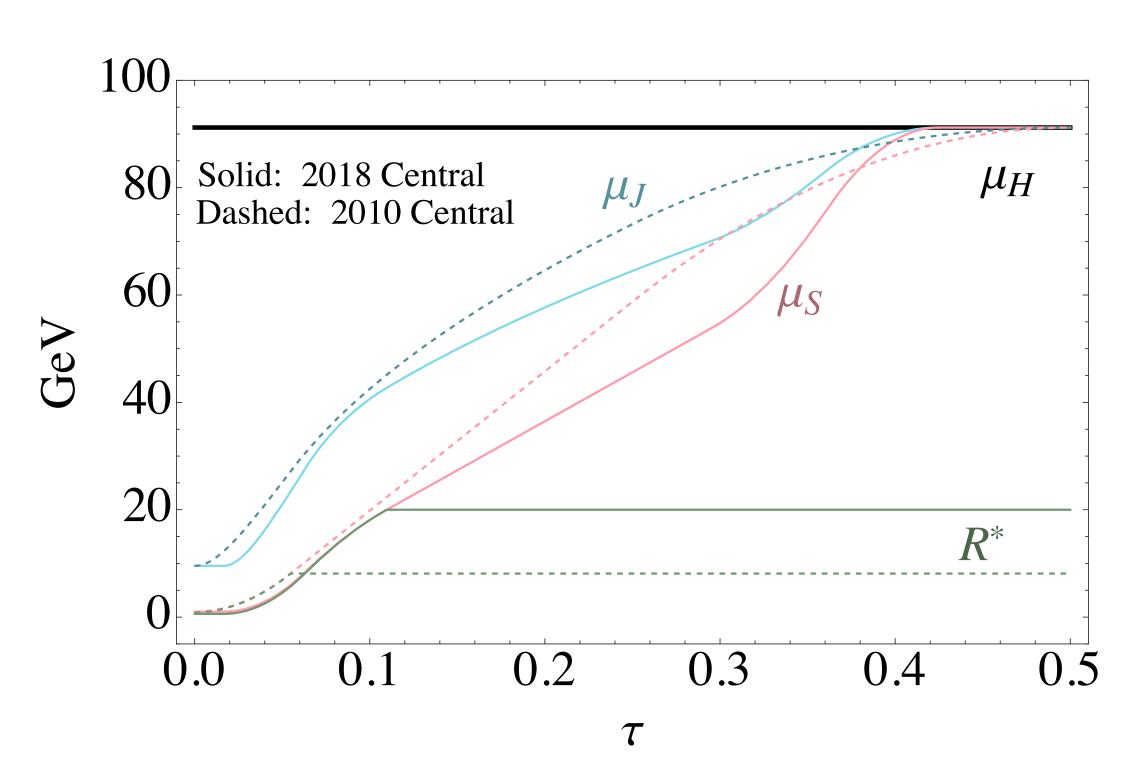
$$\mu_{\rm ns} = \begin{cases} \mu_J & \text{default} \\ (\mu_J + \mu_S)/2 & \text{lo} \\ \mu_H & \text{hi} \end{cases} \qquad \mu_{\rm ns} = \begin{cases} \mu_H & \text{default} \\ (\mu_H + \mu_J)/2 & \text{lo} \\ (3\mu_H - \mu_J)/2 & \text{hi} \end{cases}$$
[1006.3080]
$$[1808.07867, \\ 1501.04111]$$

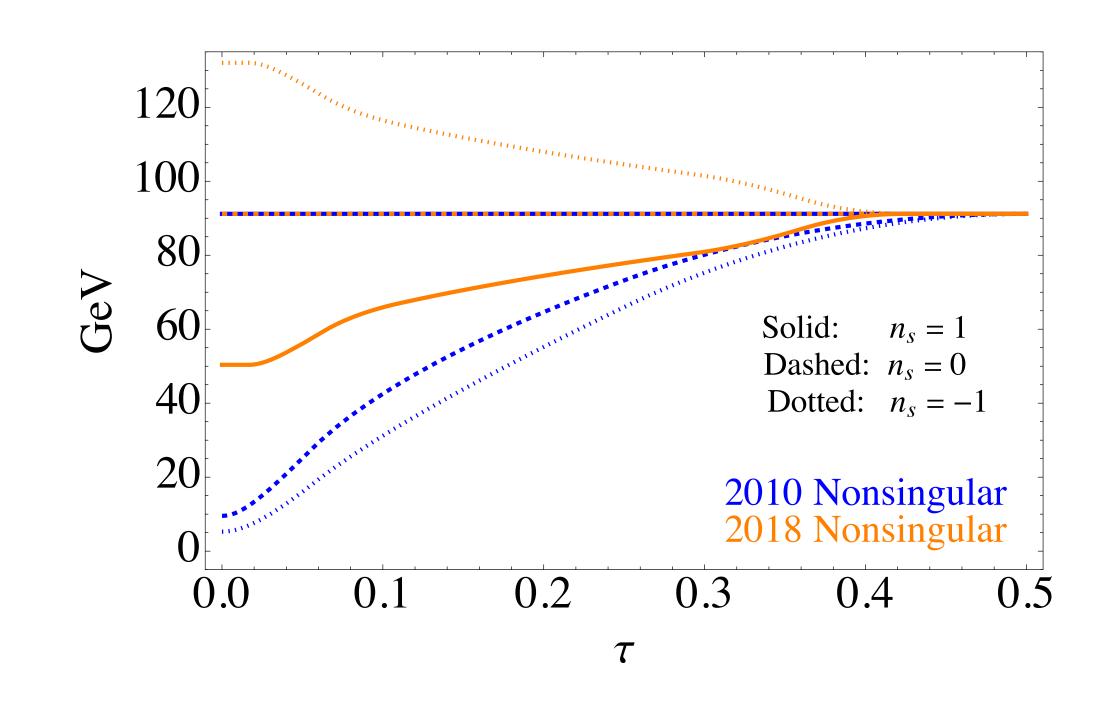
# Perturbative scale profiles

■ Scale choices for resummed and fixed-order parts:

2010: [1006.3080]

2018: [1808.07867] based on [1501.04111]





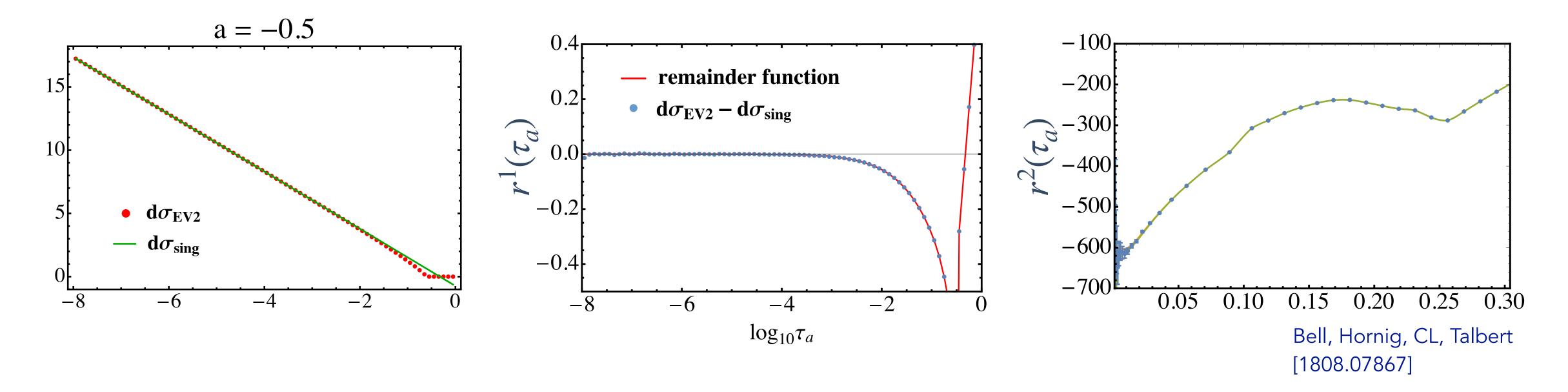
$$\sigma_{PT}(\tau) = \sigma_{sing}(\tau; \mu_H, \mu_J, \mu_S) + \sigma_{ns}(\tau; \mu_{ns})$$

$$\sigma(\tau) = \sigma_{PT}(\tau; \mu_i, R) \otimes f_{mod}(\tau, \Delta(R))$$

#### Fixed-order tails

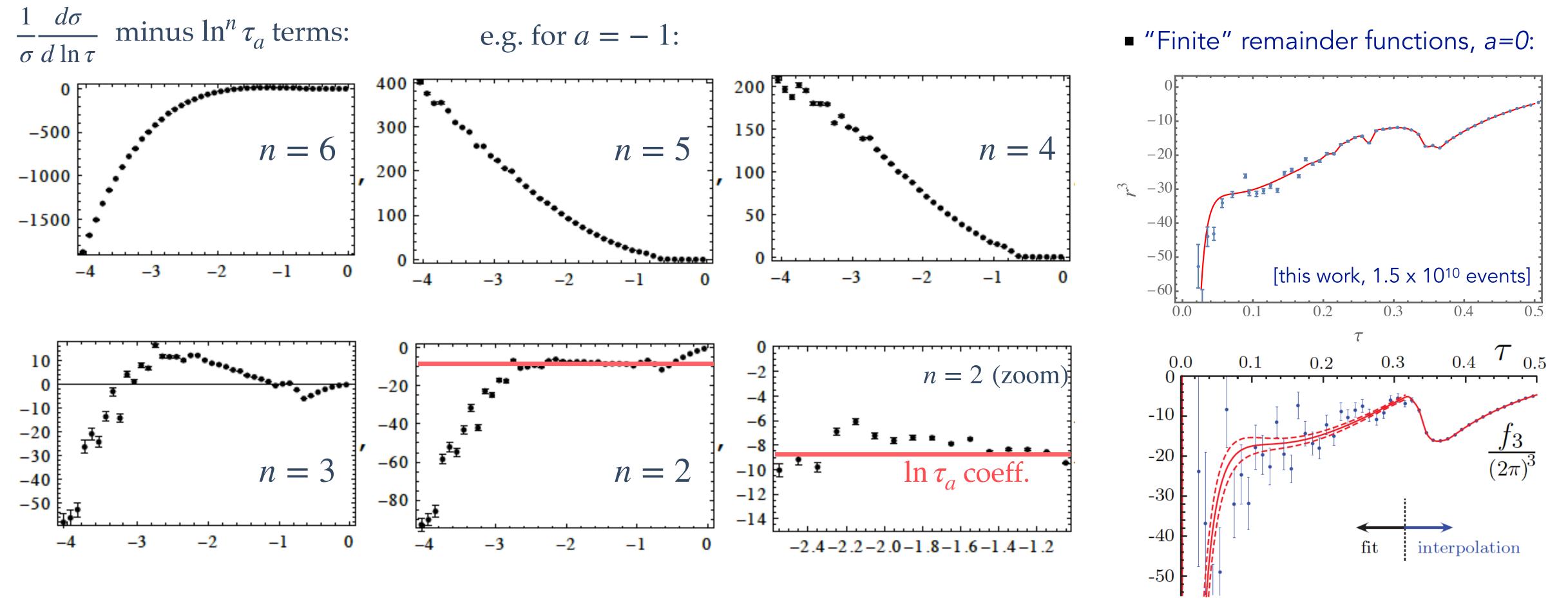
■ The above predicts the (resummed) singular component of the cross section. One must then match to fixed-order QCD for large  $\tau$ :

$$\frac{\sigma_c(\tau_a)}{\sigma_0} - \frac{\sigma_{c,\text{sing}}(\tau_a)}{\sigma_0} = r_c(\tau_a) = \theta(\tau_a) \left\{ \frac{\alpha_s(Q)}{2\pi} r_c^1(\tau_a) + \left(\frac{\alpha_s(Q)}{2\pi}\right)^2 r_c^2(\tau_a) \right\} + \dots$$



#### New remainder functions

■ Results for 3-loop fixed-order angularity distributions from EERAD3 (IR cutoff  $10^{-7}$ ,  $1.5 \times 10^{10}$  events)



■ N.B.: 3-loop results computed but not included in  $\alpha_s$  determinations presented in this talk: single log coefficient for a=0 (thrust) **differs** from QCD predictions: needs to be revisited

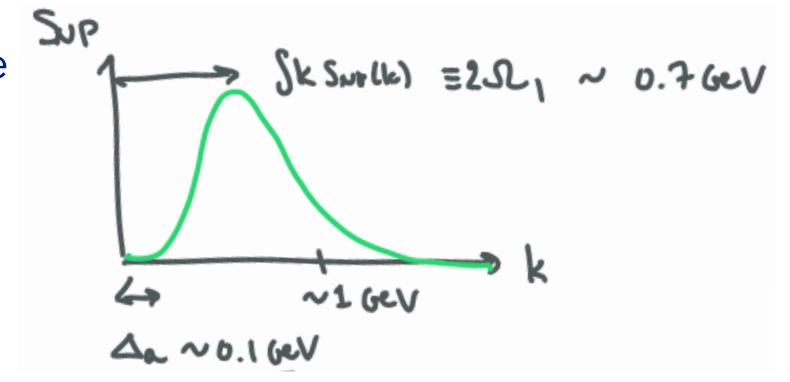
[ $1006.3080, 6 \times 10^7 \text{ events}$ ]

# Non-perturbative effects and gapped soft function

- Additionally, a treatment of non-perturbative effects is critical in  $e^+e^- -> hadrons$
- When dominant power corrections come from the soft function, NP effects can be parameterized into a shape function  $f_{mod}$ :

$$S(k,\mu) = \int dk' \, S_{\text{PT}}(k-k',\mu) \, f_{\text{mod}}(k'-2\overline{\Delta}_a)$$
 [0709.3519] [0807.1926]

'Gap' parameter accounting for parton -> hadron transition

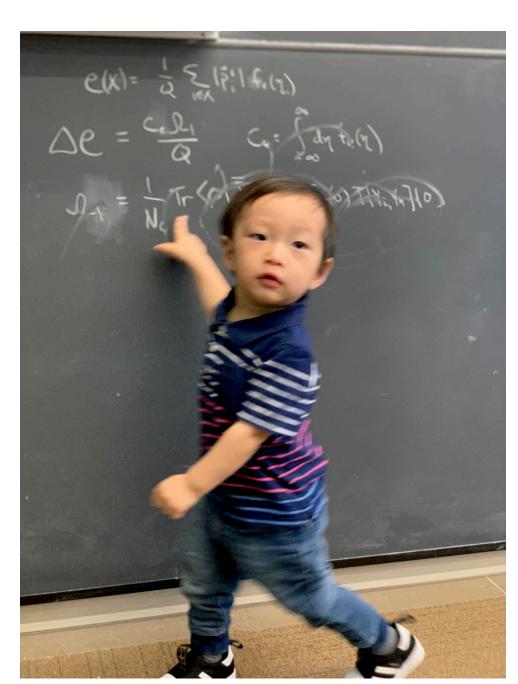


■ The effect of  $f_{\text{mod}}$  is to shift the first moment of the perturbative distribution:

$$\langle \tau_a \rangle = \langle \tau_a \rangle_{\text{PT}} + \frac{2\Omega_1}{Q(1-a)}$$
 
$$\frac{2\Omega_1}{1-a} = 2\overline{\Delta}_a + \int dk \, k f_{\text{mod}}(k)$$

lacktriangle This scaling and the *universality* of  $\Omega_1$  can be proven from QCD / SCET factorization:

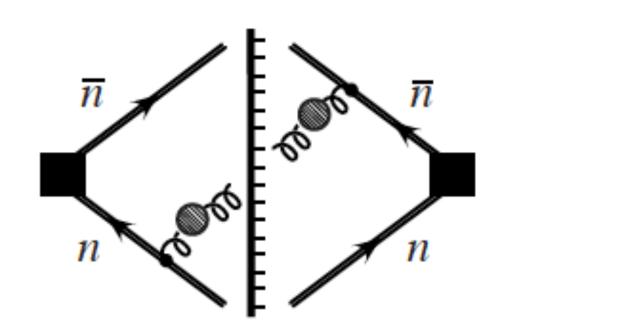
C. Lee & G. Sterman [hep-ph/0611061]



# Non-perturbative effects and gapped soft function

• However, both the perturbative soft function and gap parameter suffer renormalon ambiguities.

$$S(k,\mu) = \int dk' \, S_{\text{PT}}(k-k',\mu) \, f_{\text{mod}}(k'-2\overline{\Delta}_a)$$



$$\dots + mOmm - mOmm + mmOmm + \dots$$

lacksquare  $\mathcal{O}(\Lambda_{ ext{QCD}})$  ambiguity in gap  $\overline{\Delta}_a$ 

■ Subtract a series with the same/canceling ambiguity from both PT and NP pieces:

$$\overline{\Delta}_a = \Delta_a(\mu) + \delta_a(\mu) \qquad \xrightarrow{\text{Laplace space}} \qquad \widetilde{S}(\nu,\mu) = \left[e^{-2\nu\Delta_a(\mu)}\widetilde{f}_{\mathrm{mod}}(\nu)\right] \left[e^{-2\nu\delta_a(\mu)}\widetilde{S}_{\mathrm{PT}}(\nu,\mu)\right] \qquad \qquad \text{renormalon free}$$

# R<sub>gap</sub> scheme

• Choosing the  $R_{gap}$  scheme to cancel the leading renormalon,

$$Re^{\gamma_E} \frac{d}{d \ln \nu} \Big[ \ln \widehat{S}_{PT}(\nu, \mu) \Big]_{\nu=1/(Re^{\gamma_E})} = 0 \qquad \longrightarrow \qquad \delta_a(\mu, R) = \frac{1}{2} Re^{\gamma_E} \frac{d}{d \ln \nu} \Big[ \ln \widetilde{S}_{PT}(\nu, \mu) \Big]_{\nu=1/(Re^{\gamma_E})},$$

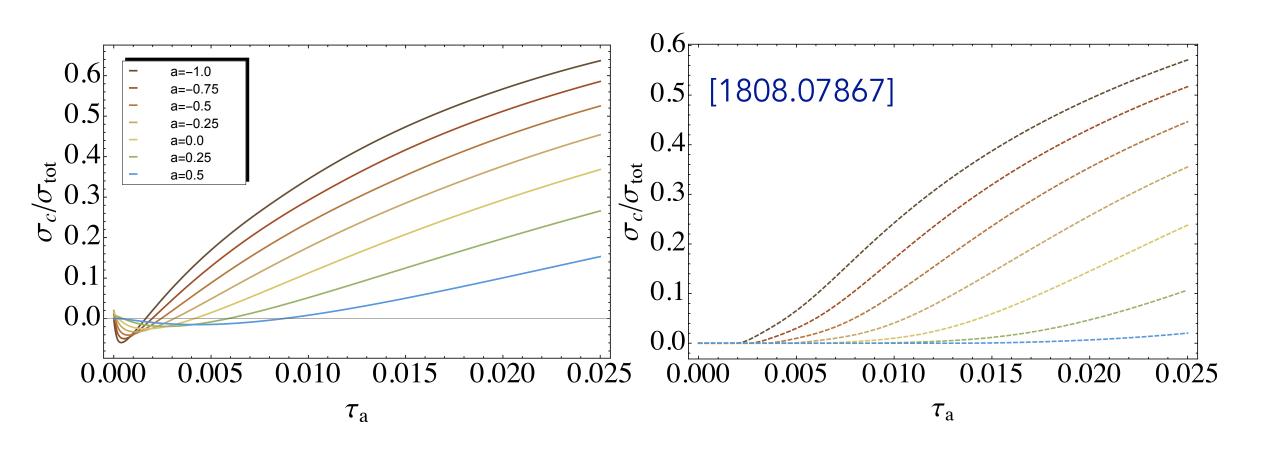
$$\widehat{S}_{PT}(\nu, \mu) = e^{-2\nu \delta_a(\mu)} \widetilde{S}_{PT}(\nu, \mu)$$

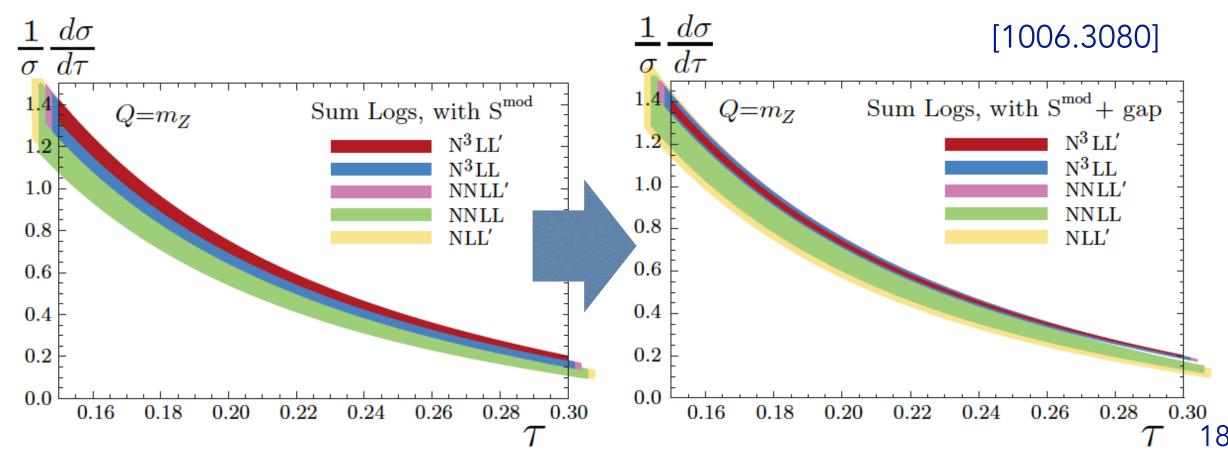
Gapped and renormalon free soft function 
$$S(k,\mu) = \int dk' \, S_{\mathrm{PT}}(k-k',\mu) \left[ e^{-2\delta_a(\mu,R) \frac{d}{dk'}} \, f_{\mathrm{mod}}(k'-2\Delta_a(\mu,R)) \right]$$

Final cross section is expanded orderby-order in bracketed term

$$\frac{1}{\sigma_0} \sigma(\tau_a) = \int dk \, \sigma_{\text{PT}} \left( \tau_a - \frac{k}{Q} \right) \left[ e^{-2\delta_a(\mu_S, R) \frac{d}{dk}} f_{\text{mod}} \left( k - 2\Delta_a(\mu_S, R) \right) \right]$$

■ Improves small  $\tau_a$  behavior and perturbative convergence:





# R<sub>gap</sub> scheme

• Choosing the  $R_{gap}$  scheme to cancel the leading renormalon,

$$Re^{\gamma_E} \frac{d}{d \ln \nu} \Big[ \ln \widehat{S}_{\text{PT}}(\nu, \mu) \Big]_{\nu=1/(Re^{\gamma_E})} = 0 \qquad \longrightarrow \qquad \delta_a(\mu, R) = \frac{1}{2} Re^{\gamma_E} \frac{d}{d \ln \nu} \Big[ \ln \widetilde{S}_{\text{PT}}(\nu, \mu) \Big]_{\nu=1/(Re^{\gamma_E})},$$
 
$$\delta(\mu, R) = \frac{Re^{\gamma_E}}{2} \sum_{n=1}^{\infty} \left( \frac{\alpha_S(\mu)}{4\pi} \right)^n \delta^n(\mu_S, R)$$
 
$$\delta^1(\mu_S, R) = 2\Gamma_s^0 \ln \frac{\mu_S}{R}$$
 
$$\delta^2(\mu_S, R) = 2\Gamma_s^0 \beta_0 \ln^2 \frac{\mu_S}{R} + 2\Gamma_s^1 \ln \frac{\mu_S}{R} + \gamma_s^1 + 2c_{\tilde{S}}^1 \beta_0$$

 $\delta^3(\mu_{\rm S}, R) = \cdots$ 

#### R-evolution

■ Want to keep R near IR scales, but also avoid large logs  $\ln \frac{\mu_S}{R}$  in subtraction terms

• but  $\mu_S$  grows to be as large as Q:

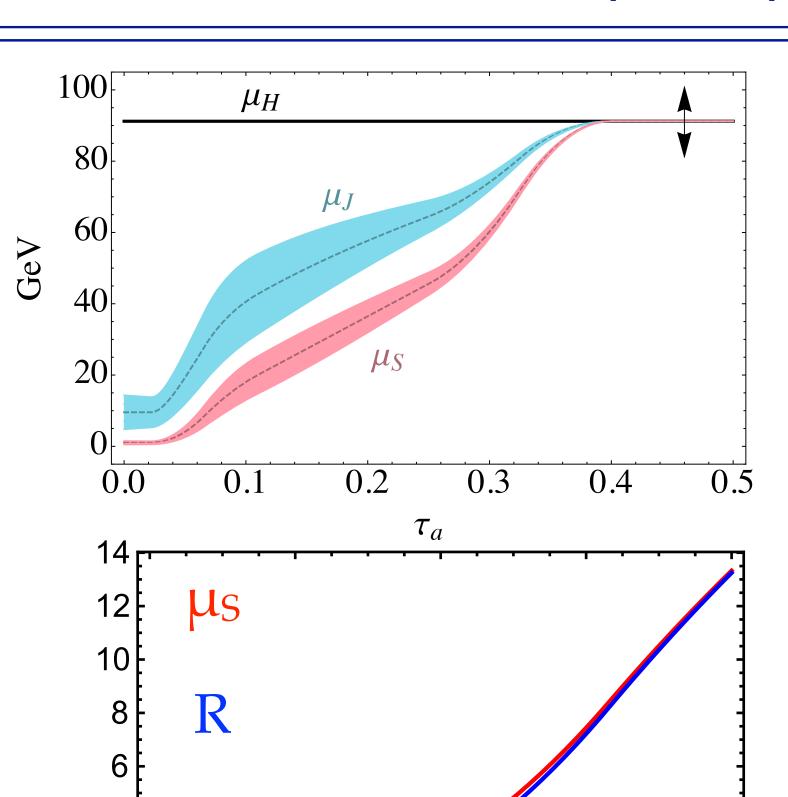
■ Sum logs by  $\mu$  and R evolution:  $\mu \frac{d}{d\mu} \Delta_a(\mu,R) = -\mu \frac{d}{d\mu} \delta_a(\mu,R) \equiv \gamma_\Delta^\mu [\alpha_s(\mu)]$ 

$$\frac{d}{dR} \Delta_a(R,R) = -\frac{d}{dR} \delta_a(R,R) \equiv -\gamma_R[\alpha_s(R)].$$

Anomalous dimensions:

$$\gamma_{\Delta}^{\mu}[\alpha_s(\mu)] = -Re^{\gamma_E}\Gamma_S[\alpha_s(\mu)]$$

$$\gamma_R[\alpha_s(R)] = \sum_{n=0}^{\infty} \left(\frac{\alpha_s(R)}{4\pi}\right)^{n+1} \gamma_R^n \qquad \gamma_R^0 = 0 \,, \quad \gamma_R^1 = \frac{e^{\gamma_E}}{2} \left[\gamma_S^1(a) + 2c_{\widetilde{S}}^1 \beta_0\right]$$



0.04

0.06

0.02

0.00

0.08

# Effective non-perturbative shifts

■ Before considering gapped renormalons, the leading-order NP effect is a constant shift:

$$\frac{d\sigma}{d\tau_a} \left(\tau_a\right) \xrightarrow{\text{NP}} \frac{d\sigma}{d\tau_a} \left(\tau_a - c_{\tau_a} \frac{\Omega_1}{Q}\right) \qquad c_{\tau_a} = \frac{2}{1-a} \qquad \qquad \Omega_1 = \frac{1}{N_C} \text{Tr} \left\langle 0 \middle| \overline{Y}_{\bar{n}}^{\dagger} Y_n^{\dagger} \mathcal{E}_T \left(0\right) Y_n \overline{Y}_{\bar{n}} \middle| 0 \right\rangle$$

Note: this is only valid in the tail region!

■ Define an 'effective shift' of the distribution in the  $R_{gap}$  scheme:

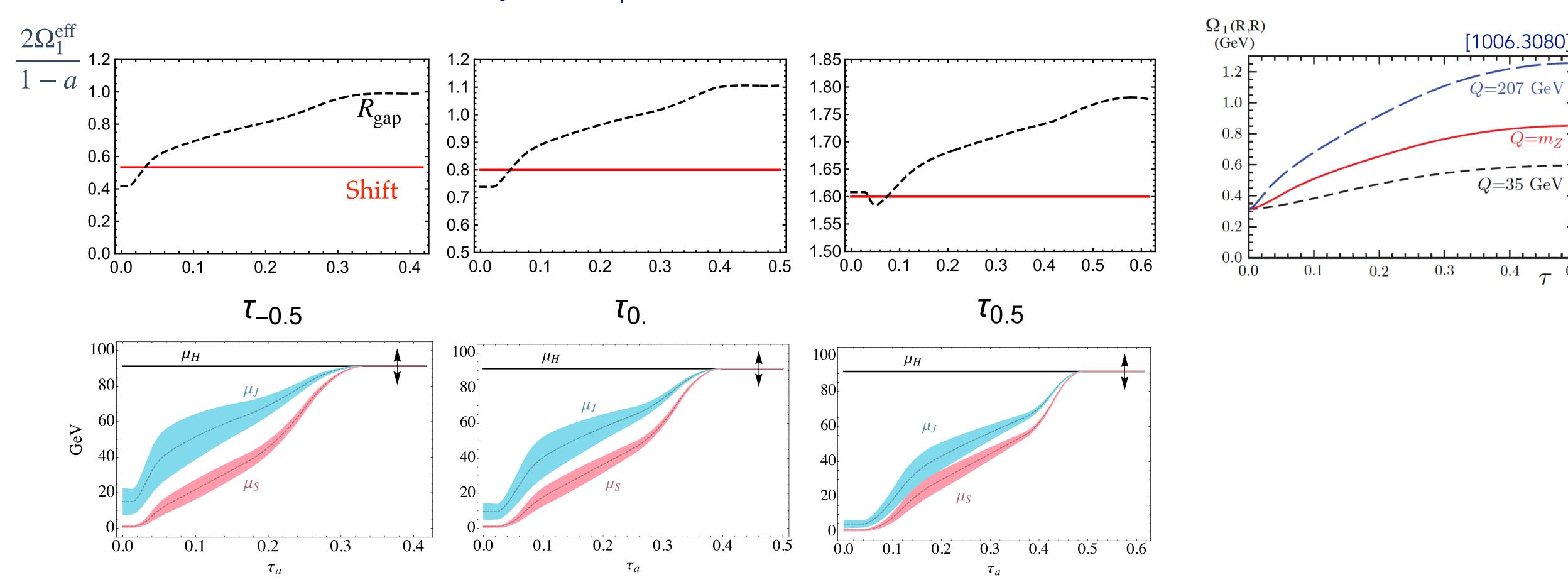
$$\int dk \, k \, e^{-2\delta_a(\mu_S, R)\frac{d}{dk}} f_{\text{mod}}\left(k - 2\Delta_a\left(\mu_S, R\right)\right) = \int dk \, k \left[\sum_i f_{\text{mod}}^{(i)}\left(k - 2\Delta_a\left(\mu_S, R\right)\right)\right] \quad \equiv \frac{2}{1 - a} \mathbf{\Omega}_1^{\text{eff}}$$

Shape function expanded order-by-order depending on logarithmic accuracy:

$$\begin{split} f_{\text{mod}}^{(0)}(k-2\Delta_{a}(\mu_{S},R)) &= f_{\text{mod}}(k-2\Delta_{a}(\mu_{S},R)) \,, \\ f_{\text{mod}}^{(1)}(k-2\Delta_{a}(\mu_{S},R)) &= -\frac{\alpha_{s}(\mu_{S})}{4\pi} \, 2\delta_{a}^{1}(\mu_{S},R)Re^{\gamma_{E}} f_{\text{mod}}'(k-2\Delta_{a}(\mu_{S},R)) \,, \\ f_{\text{mod}}^{(2)}(k-2\Delta_{a}(\mu_{S},R)) &= \left(\frac{\alpha_{s}(\mu_{S})}{4\pi}\right)^{2} \left[ -2\delta_{a}^{2}(\mu_{S},R)Re^{\gamma_{E}} f_{\text{mod}}'(k-2\Delta_{a}(\mu_{S},R)) + 2(\delta_{a}^{1}(\mu_{S},R)Re^{\gamma_{E}})^{2} f_{\text{mod}}''(k-2\Delta_{a}(\mu_{S},R)) \right] \,, \end{split}$$

# Growing shifts in event shape tails

■ Distributional shifts at NNLL' accuracy (central profile scales):



• Effectively, we shift the distribution to the right by *larger* amounts as we move from the 2-jet region out to the multi-jet tail. Is this reasonable? What might be the effect on extracting  $\alpha_s$ ?

22

# Limiting the growth of the shift

■ Can we find a way to cut off the growth of this shift? i.e. turn off R-evolution above some  $\tau = \tau_{\text{max}}$ :

$$\gamma_R \to \theta(R_{\text{max}} - R)\gamma_R$$
  $R = R(\tau)$ 

need: 
$$\frac{d}{dR}\delta_a(R,R) = \gamma_R[\alpha_s(R)]\theta(R_{\text{max}} - R)$$

recall: 
$$\delta_a(R,R) = Re^{\gamma_E} \left[ \frac{\alpha_s(R)}{4\pi} \delta_a^1(R,R) + \left( \frac{\alpha_s(R)}{4\pi} \right)^2 \delta_a^2(R,R) + \cdots \right]$$

to the order we need, just change *R to*:

$$R^* \equiv \begin{cases} R & R < R_{\text{max}} \\ R_{\text{max}} & R \ge R_{\text{max}} \end{cases}$$

Pmr 1 - der

however this can reintroduce large logs of  $\mu_S/R_{\rm max}$  ...

$$\delta^{1}(\mu_{S}, R) = 2\Gamma_{s}^{0} \ln \frac{\mu_{S}}{R}$$

$$\delta^{2}(\mu_{S}, R) = 2\Gamma_{s}^{0} \beta_{0} \ln^{2} \frac{\mu_{S}}{R} + 2\Gamma_{s}^{1} \ln \frac{\mu_{S}}{R} + \gamma_{s}^{1} + 2c_{\tilde{S}}^{1} \beta_{0}$$

#### Another scheme

"
$$R^*$$
 scheme"

$$\delta_a^*(R) = \frac{1}{2} R^* e^{\gamma_E} \frac{d}{d \ln \nu} \left[ \ln S_{\text{PT}}(\nu, \mu = R^*) \right]_{\nu = 1/(R^* e^{\gamma_E})}$$

Bell et al. [this work]

we are not forced to set  $\mu = \mu_S$  in the subtraction series, we can pick  $\mu = R$ 

Bachu, Hoang, Mateu, Pathak, Stewart [2012.12304]

$$\delta_a^*(R) = \frac{Re^{\gamma_E}}{2} \left[ \frac{\alpha_s(R)}{4\pi} \cdot 0 + \left( \frac{\alpha_S(R)}{4\pi} \right)^2 (\gamma_S^1 + 2c_{\tilde{S}}^1 \beta_0) + \mathcal{O}(\alpha_s^3) \right]$$

$$\gamma_R^* = e^{\gamma_E} \left[ \frac{\alpha_S(R)}{4\pi} \cdot 0 + \left( \frac{\alpha_S(R)}{4\pi} \right)^2 (\gamma_S^1 + 2c_{\tilde{S}}^1 \beta_0) + \mathcal{O}(\alpha_S^3) \right]$$

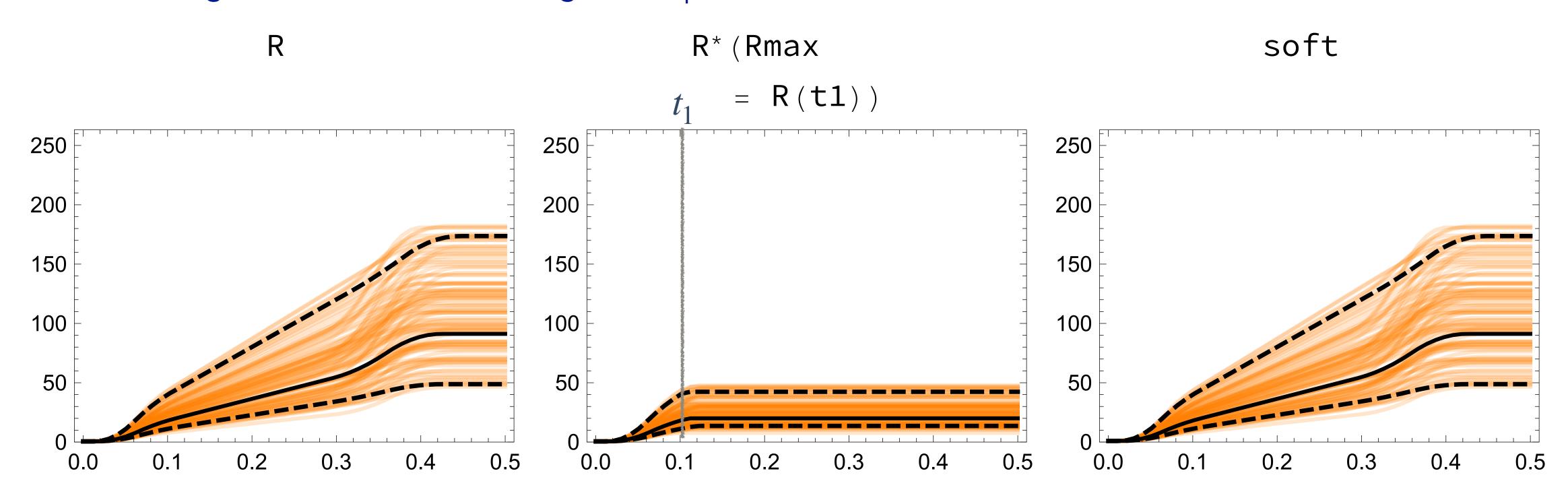
$$\mu$$
-evolution:

$$\gamma_{\Delta}[\alpha_{S}(\mu)] = 0$$

■ Nothing special about this scheme, just a way to test the impact of changing the effective shift in event shapes.

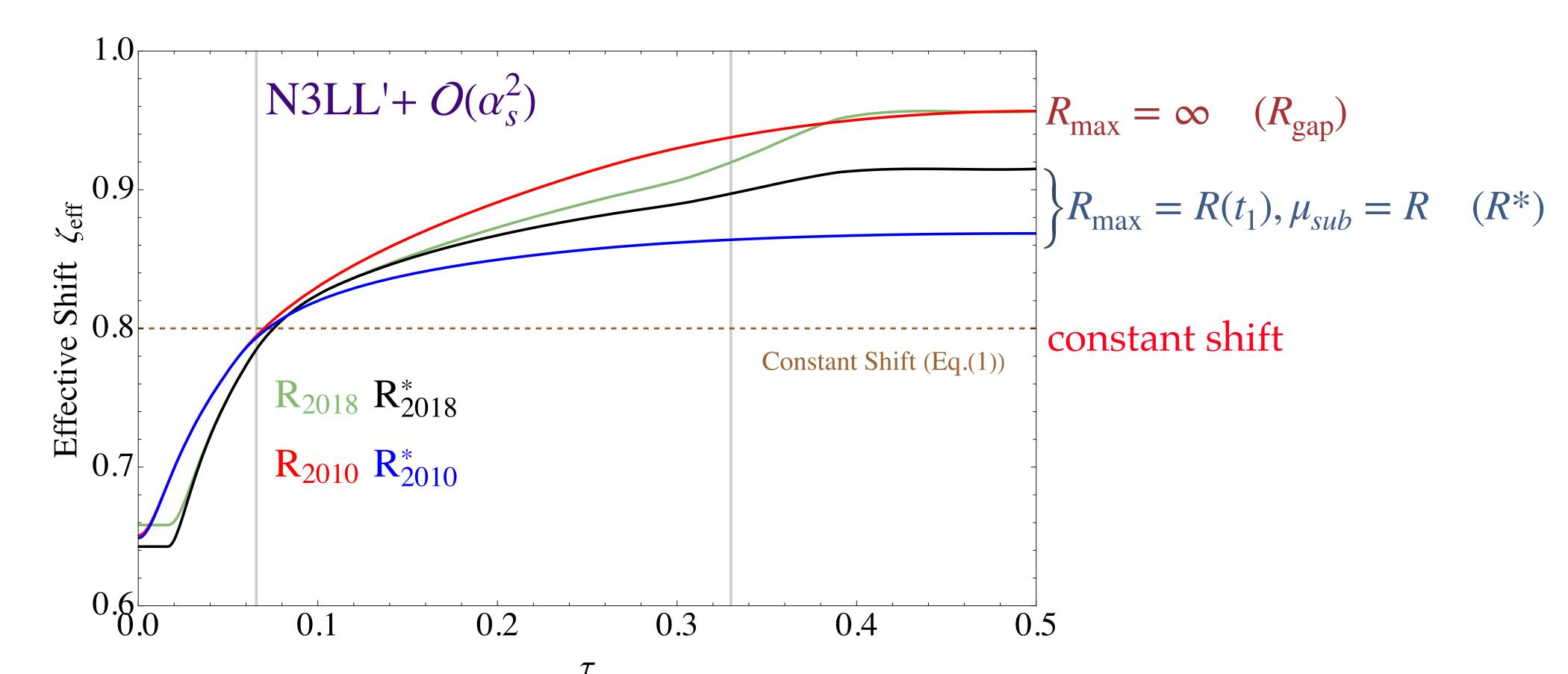
# R vs R\* profiles

■ In our results, we let  $R^*$  grow until we hit  $\tau_a = t_1(a)$ , where we finish transitioning from "shape function" region to "resummation region" in profile functions:



■ Different  $R_{max}$  values are probed in tandem with variation of the  $t_1$  profile parameter

#### Flattened shifts in tails



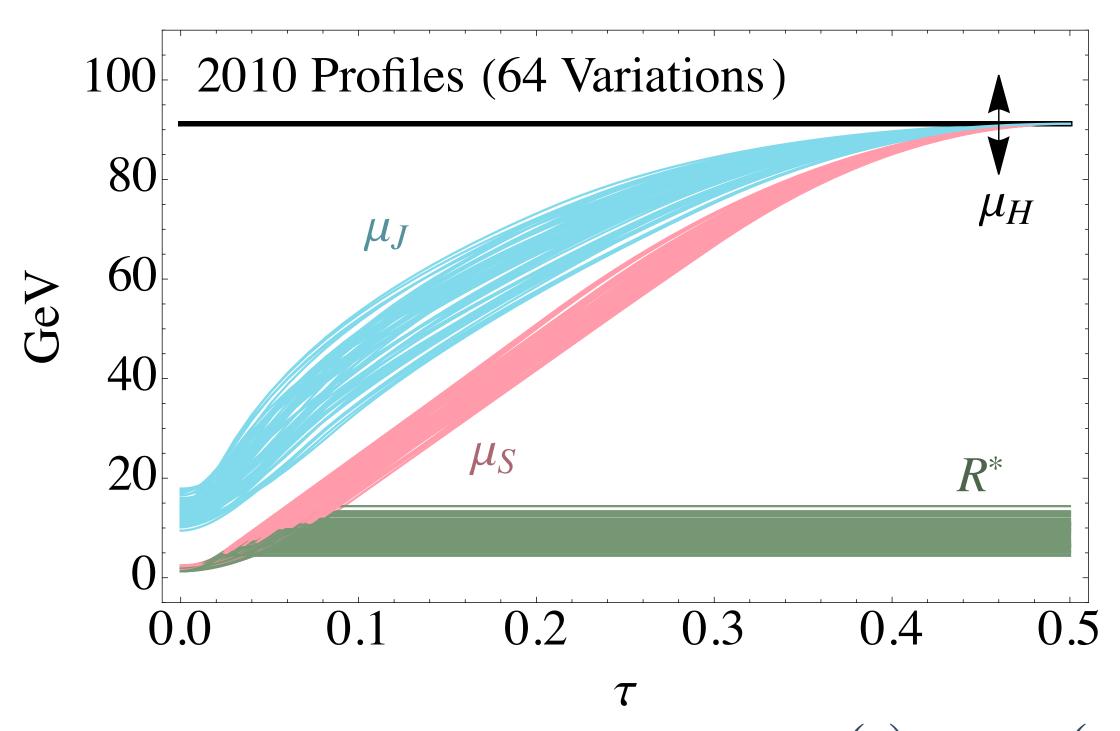
- This can be compared to studies of models of hadronization corrections to 3-jet events in the far tail region, e.g. Luisoni et al. [2012.00622].
- Our method is a way to study variations of how we treat power corrections within a 2-jet factorization framework

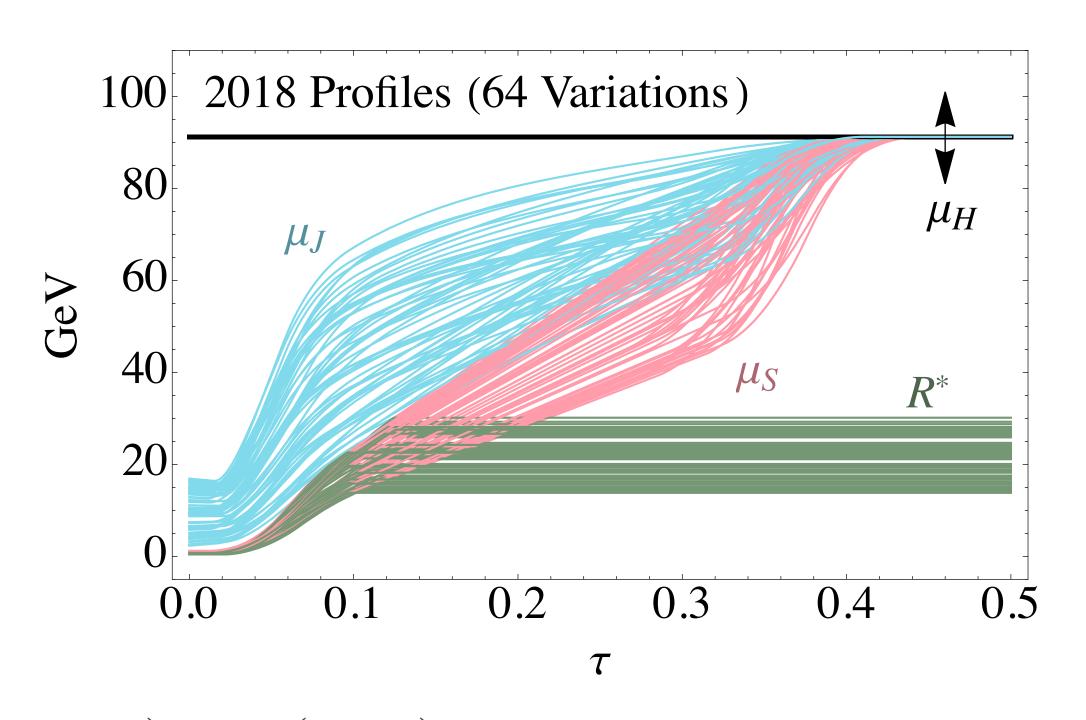
#### Scale variations

■ Random scans over profile function parameters:

2010: [1006.3080]

2018: [1808.07867] based on [1501.04111]



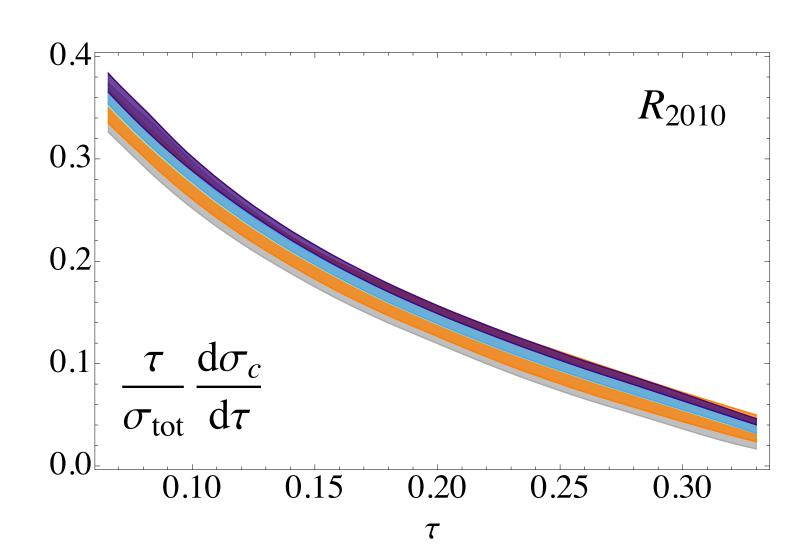


$$\sigma_{PT}(\tau) = \sigma_{sing}(\tau; \mu_H, \mu_J, \mu_S) + \sigma_{ns}(\tau; \mu_{ns})$$

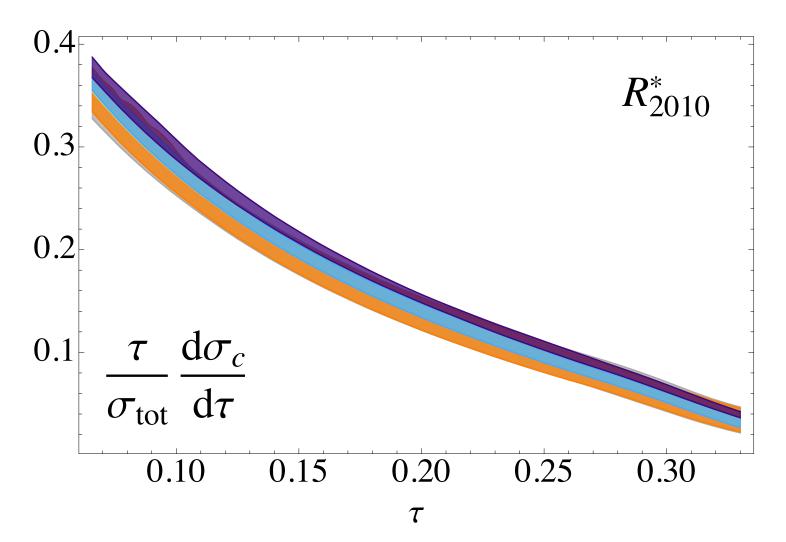
$$\sigma(\tau) = \sigma_{PT}(\tau; \mu_i, R) \otimes f_{mod}(\tau, \Delta(R))$$

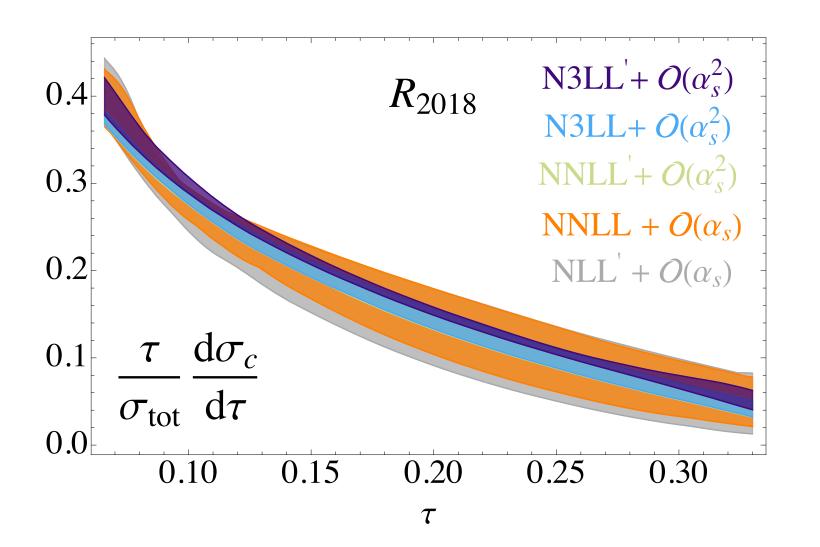
# Convergence in R vs R\* schemes

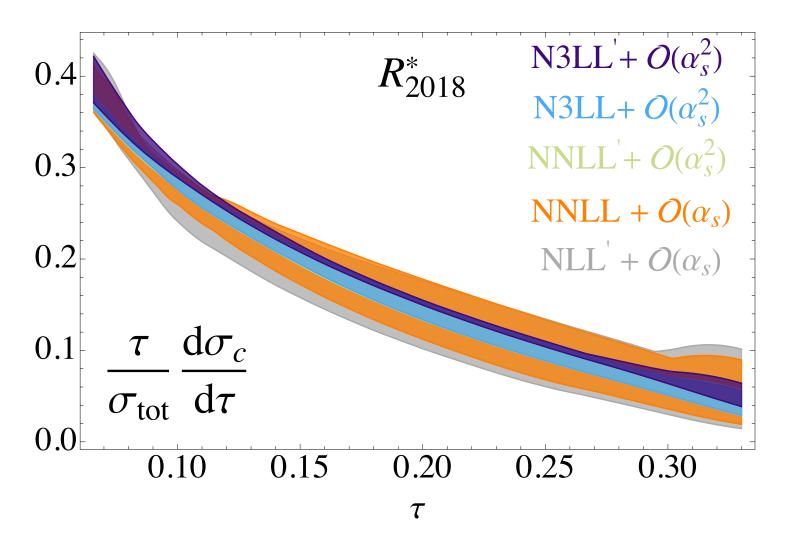
#### Rgap scheme:

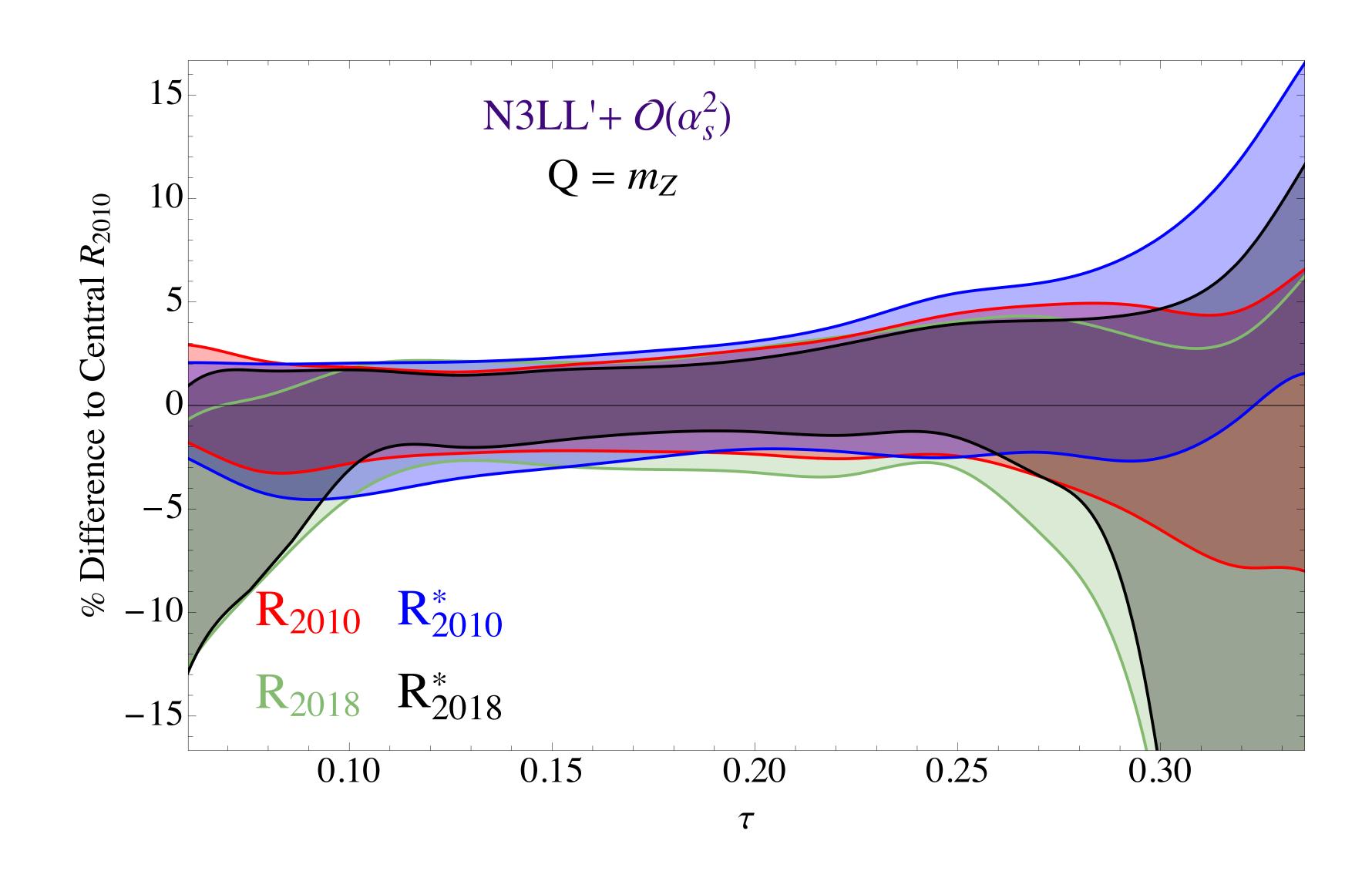












# Comparison with data and determination of $\alpha_s$

#### Data sets

#### ■For thrust:

```
L3-2004: 172.3 GeV (12)
ALEPH-2004: 133. GeV (7)
                           L3-2004: 182.8 GeV (12)
ALEPH-2004: 161. GeV (7)
                           L3-2004: 188.6 GeV (12)
ALEPH-2004: 172. GeV (7)
                           L3-2004: 194.4 GeV (12)
ALEPH-2004: 183. GeV (7)
ALEPH-2004: 189. GeV (7)
                           L3-2004: 200. GeV (11)
                           L3-2004: 206.2 GeV (12)
ALEPH-2004: 200. GeV (6)
                           L3-2004: 41.4 GeV (5)
ALEPH-2004: 206. GeV (8)
ALEPH-2004: 91.2 GeV (26)
                           L3-2004: 55.3 GeV (6)
                           L3-2004: 65.4 GeV (7)
AMY-1990: 55.2 GeV (5)
                           L3-2004: 75.7 GeV (7)
DELPHI-1999: 133. GeV (7)
                           L3-2004: 82.3 GeV (8)
DELPHI-1999: 161. GeV (7)
                           L3-2004: 85.1 GeV (8)
DELPHI-1999: 172. GeV (7)
                           L3-2004: 91.2 GeV (10)
DELPHI-1999: 89.5 GeV (11)
                           OPAL-1997: 161. GeV (7)
DELPHI-1999: 93. GeV (12)
DELPHI-2000: 91.2 GeV (12)
                           OPAL-2000: 172. GeV (8)
                           OPAL-2000: 183. GeV (8)
DELPHI-2003: 183. GeV (14)
DELPHI-2003: 189. GeV (15)
                           OPAL-2000: 189. GeV (8)
                           OPAL-2005: 133. GeV (6)
DELPHI-2003: 192. GeV (15)
                           OPAL-2005: 177. GeV (8)
DELPHI-2003: 196. GeV (14)
                           OPAL-2005: 197. GeV (8)
DELPHI-2003: 200. GeV (15)
                           OPAL-2005: 91. GeV (5)
DELPHI-2003: 202. GeV (15)
                           SLD-1995: 91.2 GeV (6)
DELPHI-2003: 205. GeV (15)
DELPHI-2003: 207. GeV (15) TASSO-1998: 35. GeV (4)
DELPHI-2003: 45. GeV (5)
                           TASSO-1998: 44. GeV (5)
DELPHI-2003: 66. GeV (8)
DELPHI-2003: 76. GeV (9)
                             ---- Summary ----
JADE-1998: 35. GeV (5)
                            Totlal: 516
JADE-1998: 44. GeV (7)
                             Q > 95 : 345
L3-2004: 130.1 GeV (11)
                            Q < 88 : 89
L3-2004: 136.1 GeV (10)
                            Q \sim MZ : 82
L3-2004: 161.3 GeV (12)
```

#### For angularities:

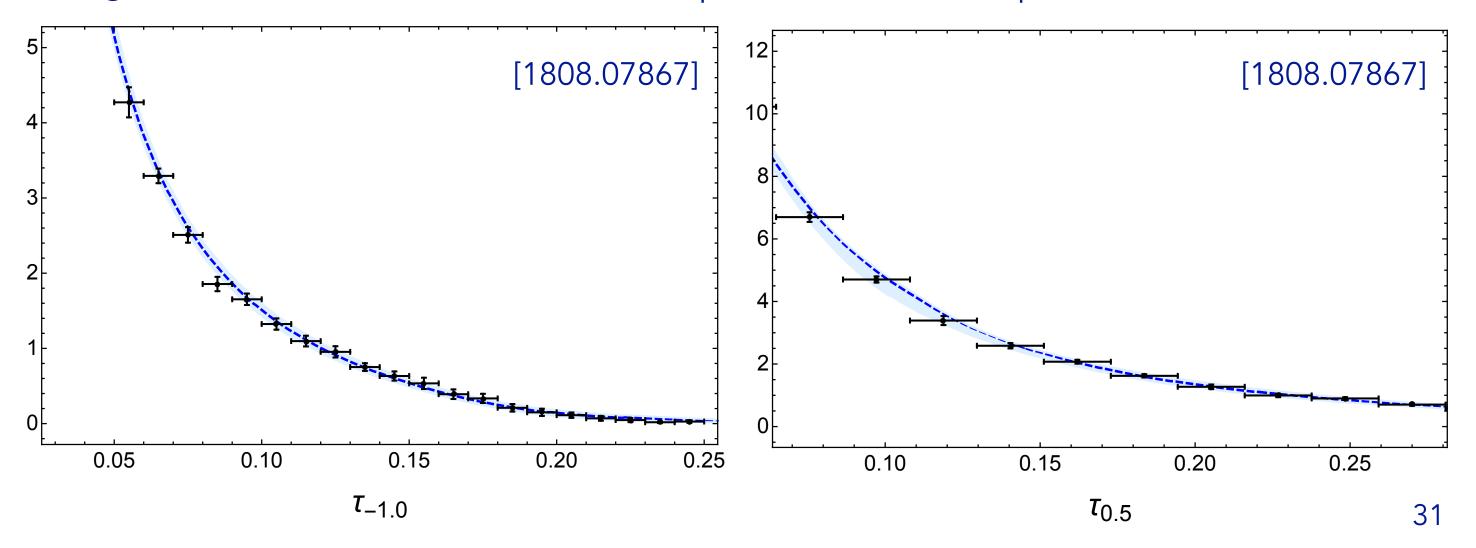
Generalized event shape and energy flow studies in  $\rm e^+e^-$  annihilation at  $\sqrt{s}=91.2\text{-}208.0\,\rm{GeV}$ 

L3 Collaboration

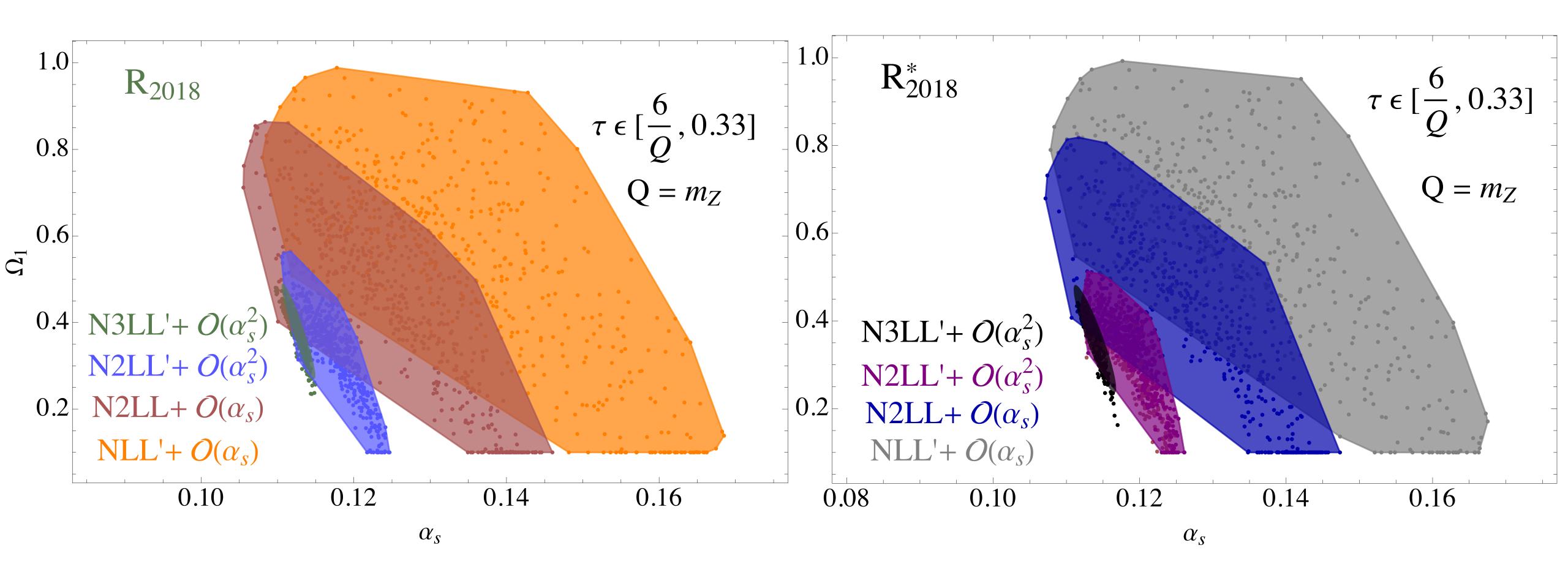
JHEP 10 (2011) 143

Also see PhD thesis by P. Jindal, Panjab University

- Data for a = {-1.0, -0.75. -0.5, -0.25, 0.0, 0.25, 0.5, 0.75} at 91.2 and 197 GeV
- Total number of bins = (bins per a) x (number of a) =  $25 \times 7 = 175$  bins @ Q = 91.2 GeV
- e.g. a = -1 and 0.5, Q = 91.2 GeV, compared to our NNLL' prediction:

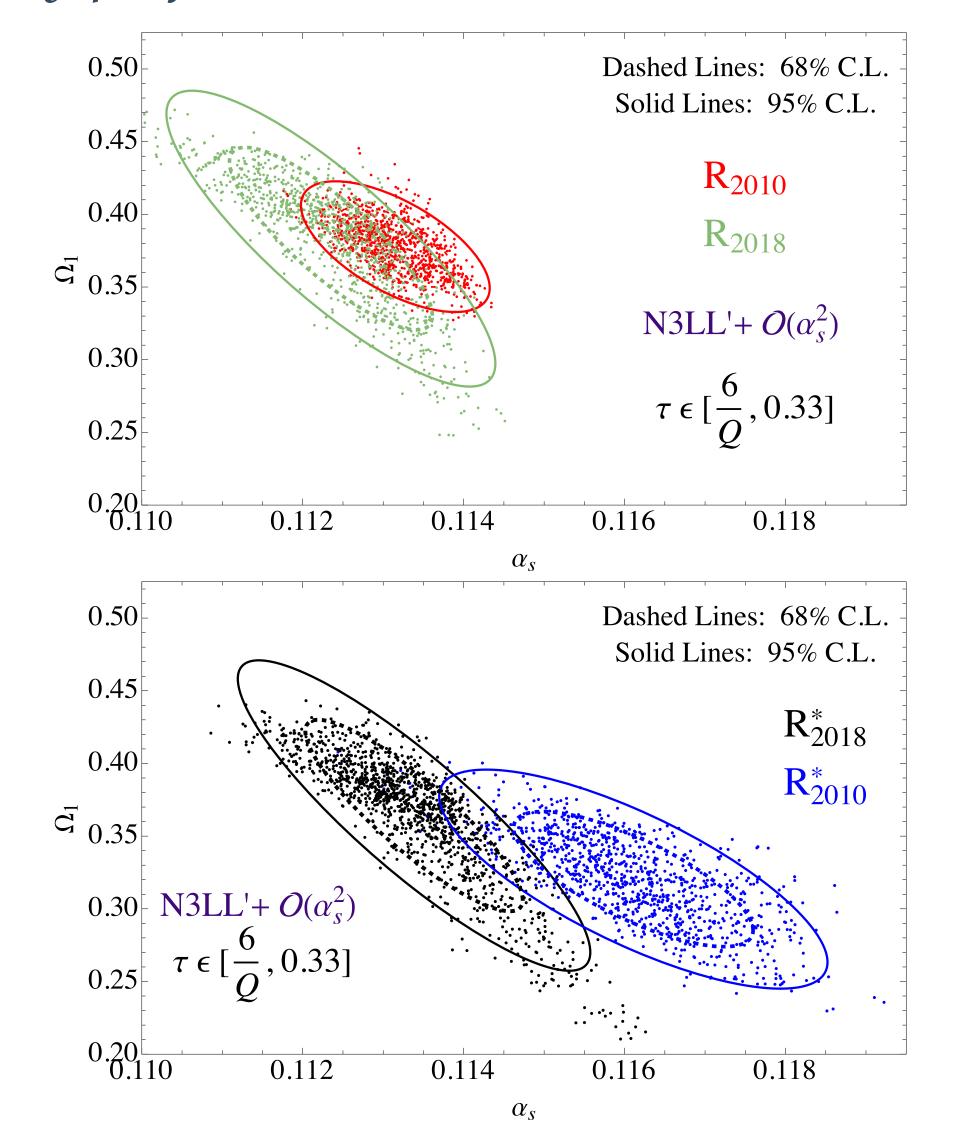


### Effect on thrust fits $[N^3LL' + \mathcal{O}(\alpha_s^2)]$

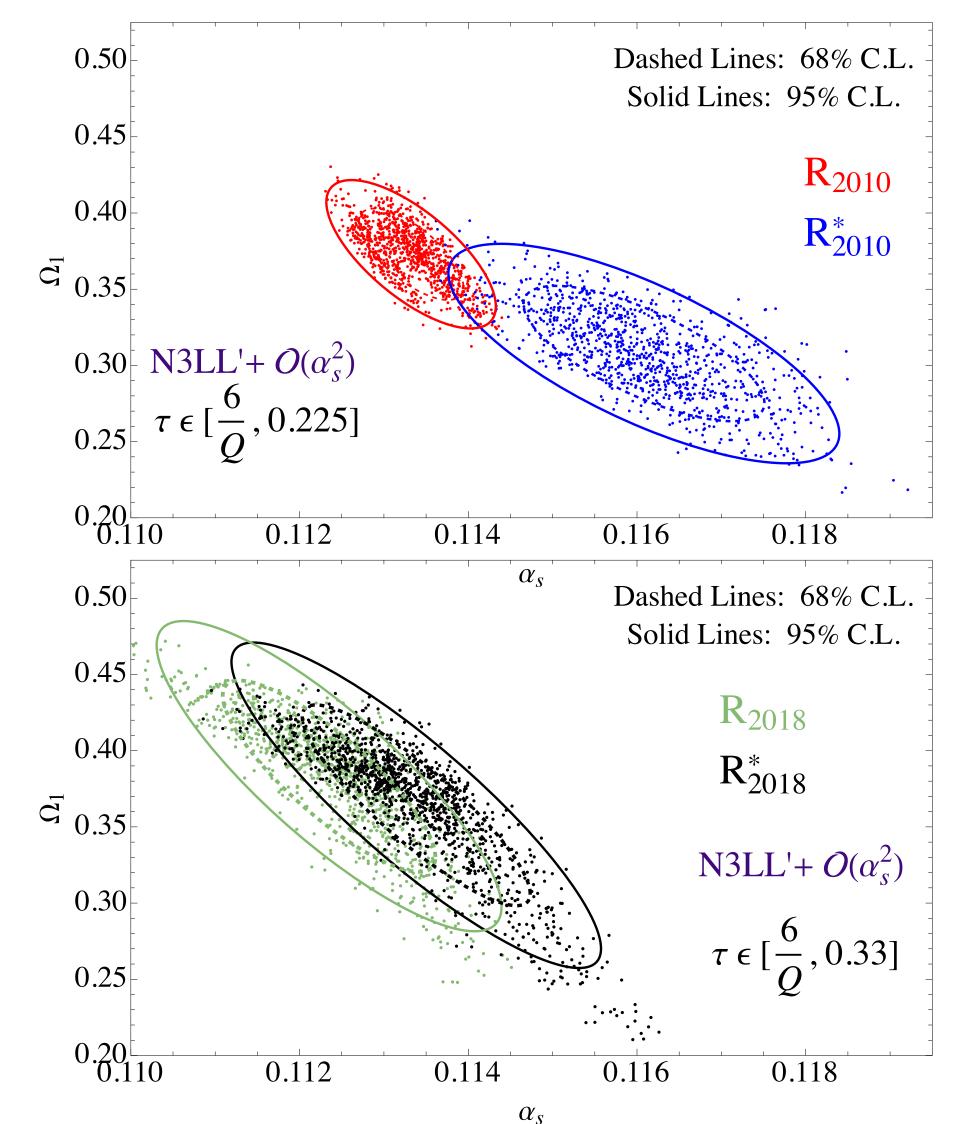


# Effect on thrust fits $[N^3LL' + \mathcal{O}(\alpha_s^2)]$

#### Vary profiles:

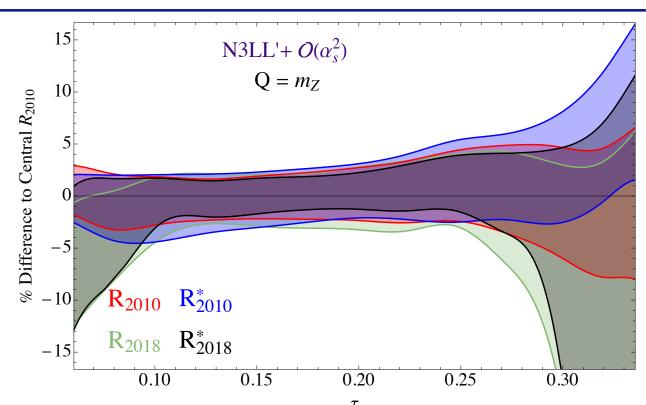


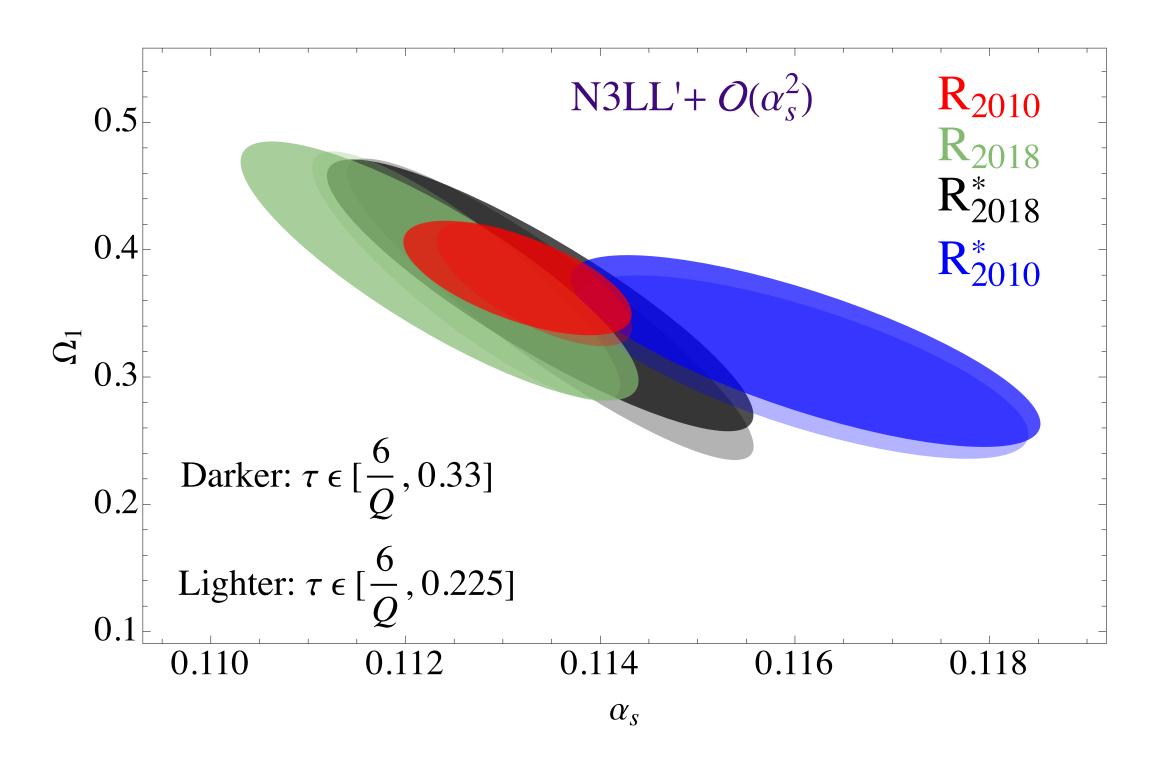
#### Vary renormalon schemes:

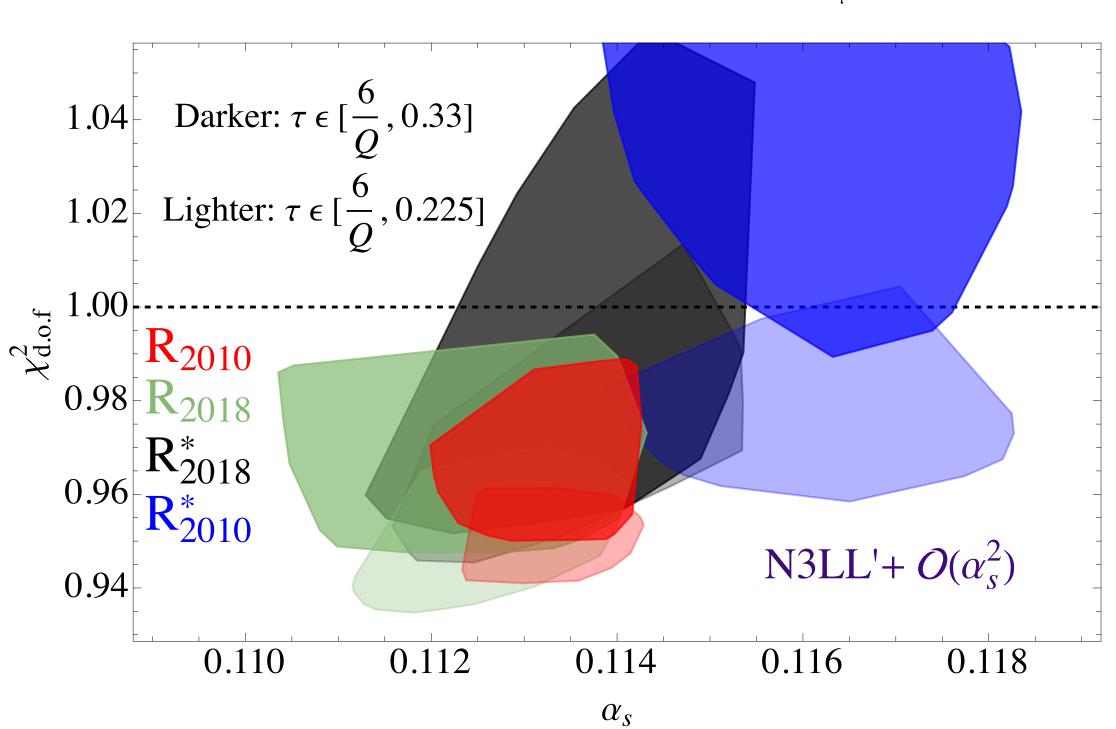


# Fit in a narrower 2-jet region

- Variability by scheme lessened in more 2-jet like region vs multi jet tail
- Try limiting fit window to, e.g,  $\tau$  < 0.225:
- Not too much shift in the fit ellipses, but improved quality of fit:

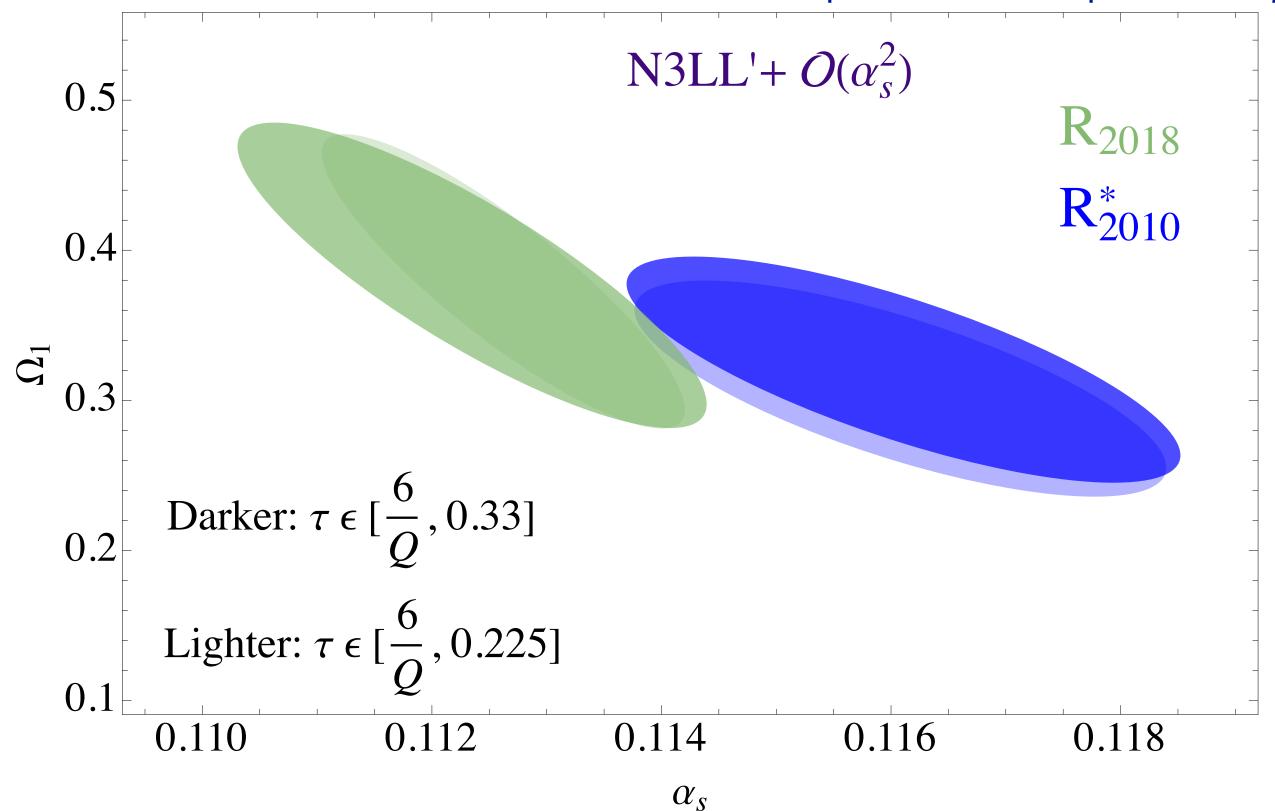


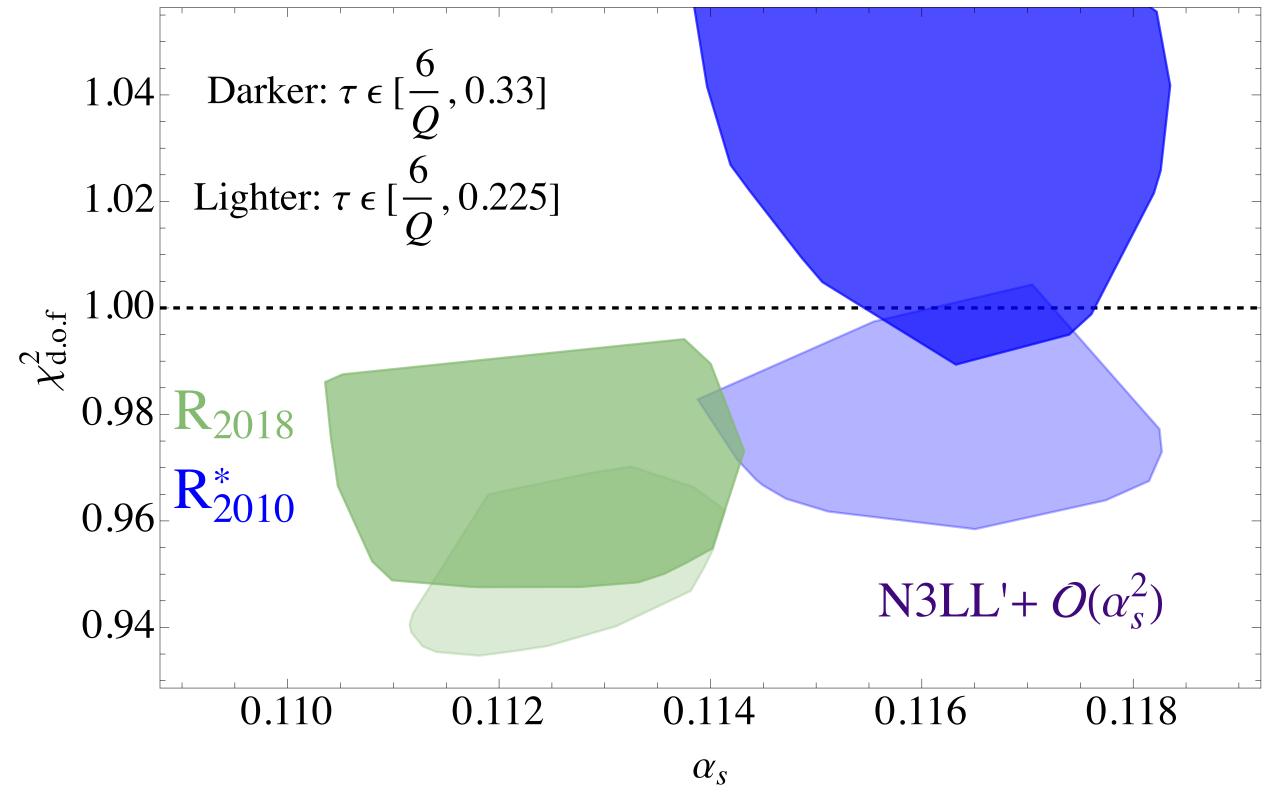




# Fit in a narrower 2-jet region

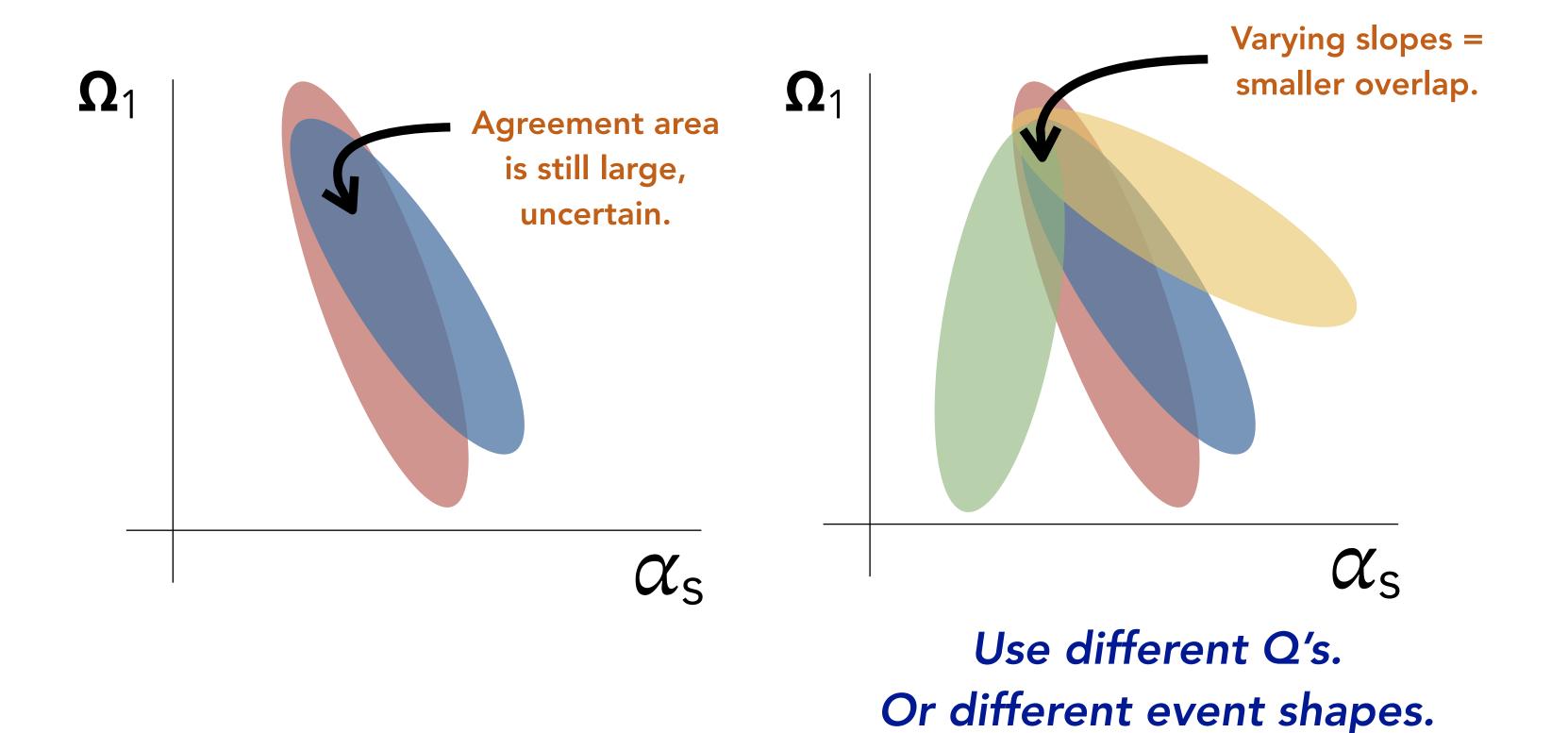
- Variability by scheme lessened in more 2-jet like region vs multi jet tail
- Try limiting fit window to, e.g,  $\tau$  < 0.225:
- Not too much shift in the fit ellipses, but improved quality of fit:





# Future outlook: angularities break degeneracies

• In tail region, leading nonperturbative effect is a shift by  $c_e\Omega_1/Q$ 



- Angularities: Leading nonperturbative shift is  $\frac{2\Omega_1}{Q(1-a)}$ : changing a is like changing Q.
- We have preliminary fits based on angularities, but with quite a small amount of data. More would be welcome!

# Looking ahead

- Welcome more work to understand robust estimation of theoretical uncertainty due to renormalon schemes
- Encouraging signs pointing to the purely 2-jet-like region for fitting, welcome more analysis / data from future LC
- Better computation of 3-loop fixed-order thrust distribution also welcome, extracting small contributions out of large singular background challenging
- •You (and we!) are not allowed to quote a value of  $\alpha_s$  or  $\Omega_1$  coming from this talk!! [our results limited to N<sup>3</sup>LL'+ $\mathcal{O}(\alpha_s^2)$ ]
- •We observe a shift in  $\alpha_s$  of up to a few percent when switching from standard R<sub>gap</sub> to R\* scheme or between some perturbative scale choices.
- Shifted values are within uncertainties, but might alleviate tension with PDG value.
  - Similar conclusion, from different considerations, as G. Luisoni, P. Monni, G. Salam [2012.00622] who tried varying size of nonperturbative shift in C-parameter distribution as function of C (smaller shifts for large  $C \Rightarrow$  larger values of  $\alpha_s$  by a few percent)
- Dedicated new analyses or measurements of data in the *true* two-jet region may yield the best results for fits from two-jet event shapes, complementing more rigorous understanding of nonperturbative effects on 3-jet tail to reduce uncertainties that may be induced by variations in that region

# Backups

### RELEVANT PHYSICAL SCALES

Thrust: 
$$M^2 = M_A^2 + M_B^2 = Q^2 z$$
 ( $(a^2)$ )

Now St.: 
$$h$$
 and  $h$  are  $h$  and  $h$  and  $h$  are  $h$  and  $h$  are  $h$  are  $h$  are  $h$  and  $h$  are  $h$  are  $h$  and  $h$  are  $h$  are  $h$  are  $h$  and  $h$  are  $h$  are  $h$  and  $h$  are  $h$ 

presente

jet mans

Collinear 
$$Pc \sim (Q, \frac{M^2}{Q}, M) \sim Q(1, 2, \sqrt{2})$$

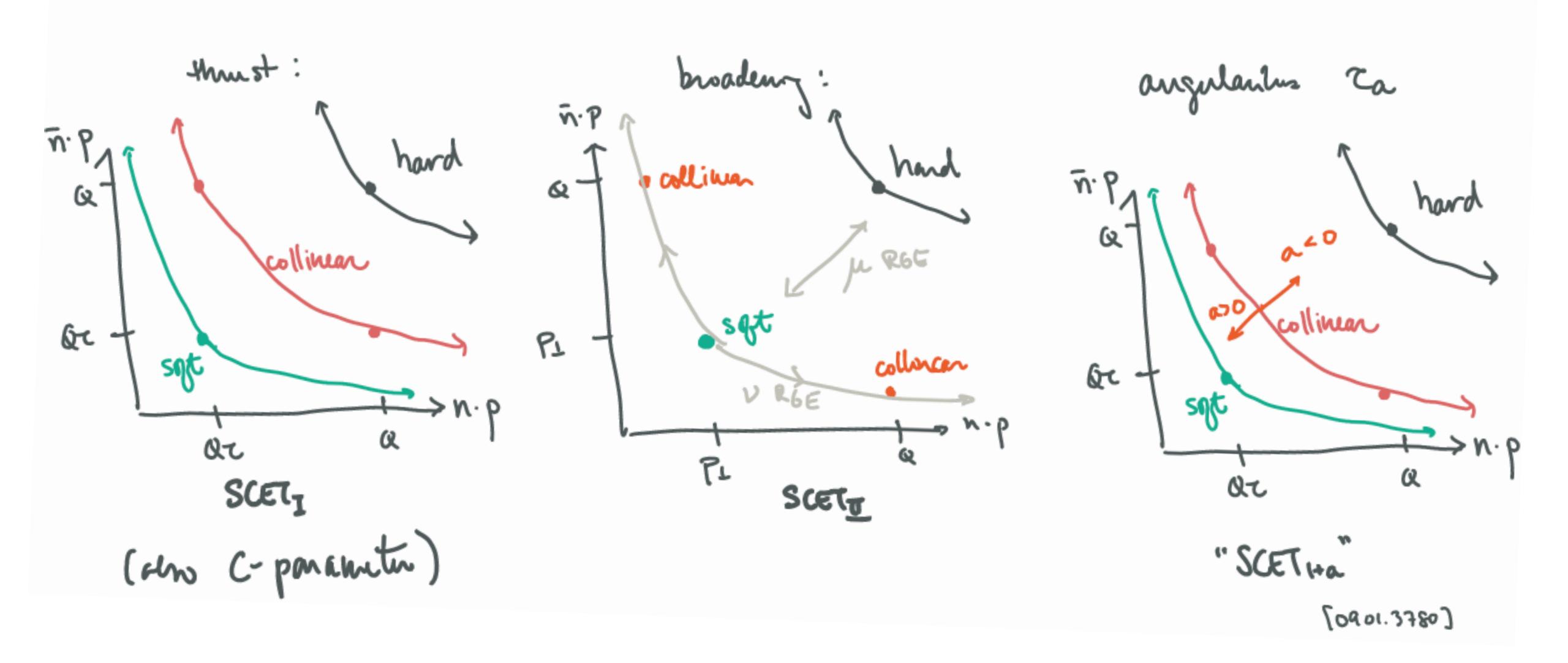
Source

Soft  $K_S \sim (\frac{M^2}{Q}, \frac{M^2}{Q}, \frac{M^2}{Q}) \sim Q(2, 2, 2)$ 

(Angularities:)

 $Pc \sim Q(1, 2^{\frac{2}{2}}, 2^{\frac{2}{2}})$ 

# SCALES & Morres:



NP Shape Function SNP Key properties: SK Swelle) =252, ~ 0.7 GeV · Si, has a fild they def: 21 = 1 Tr 2014n Yn & Yn 4n 10) ~1 GeV De ~ 0.1 GeV technial details: · needs renamelar subtraction · we adopt "R-gap" scheme Hoong & Stevento Many of Klunh Hoory, Jain, Scimeri, Starret "R- evalution" L, Steumens (2006) (appears in thrust, C. panemeter) Scaling à l'a is a prediction of actinization

