

Nuclear beta decay for fundamental science

Garrett King

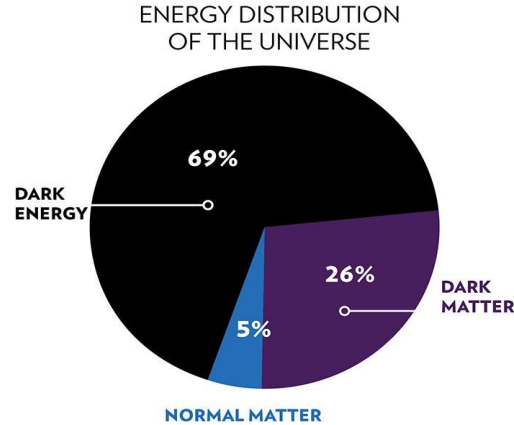
INT Workshop 26-95W
Testing the Standard Model in Charged-Weak Decays
1/14/2026

LA-UR-25-32298

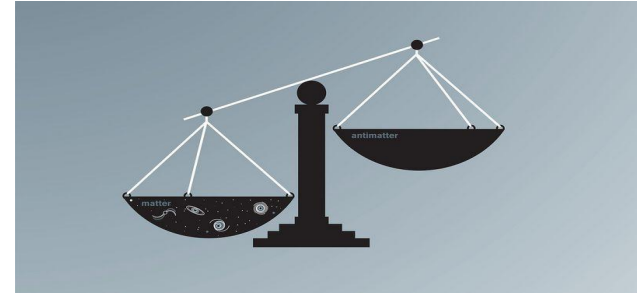
Why beyond Standard Model (BSM) physics?



Fermilab / Sandbox Studio, Chicago

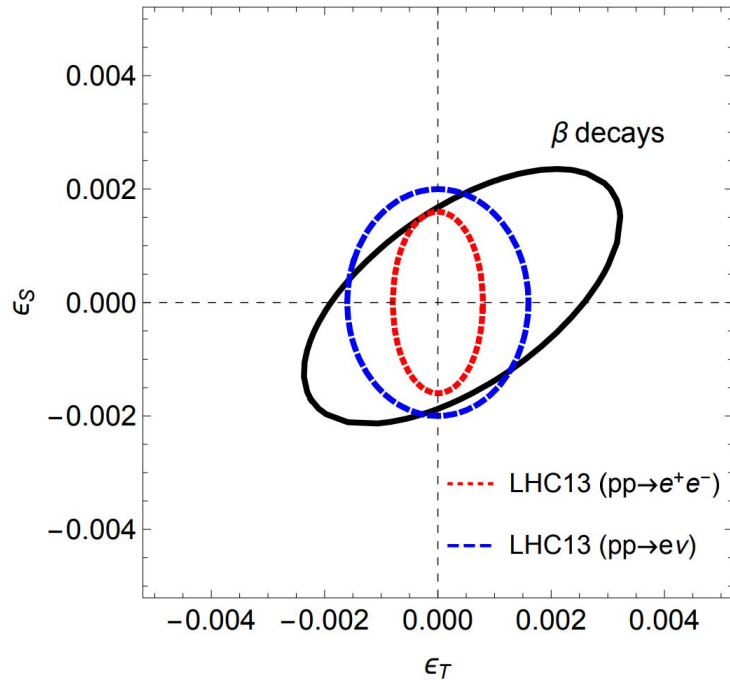


NASA / Chandra X-ray Center/ K. Divona



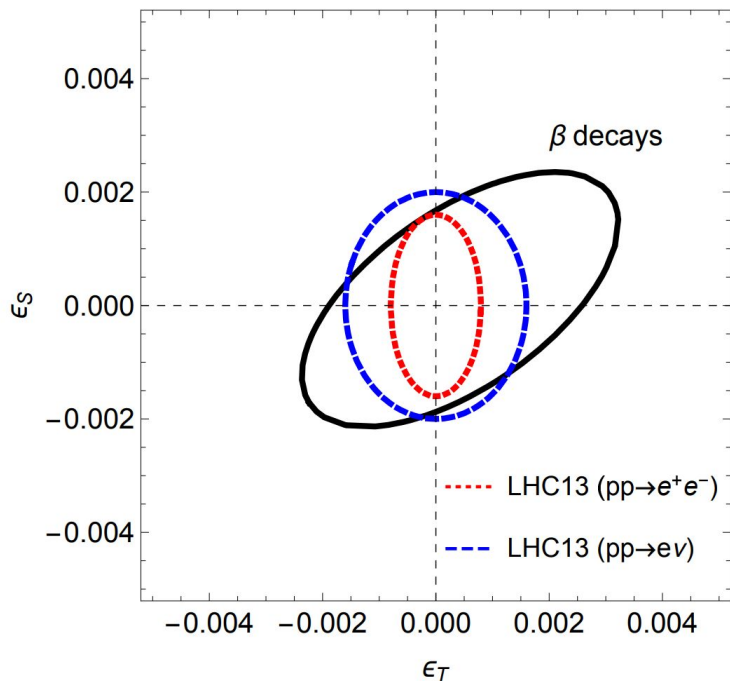
Symmetry Magazine / Sandbox Studio, Chicago

New physics impact of nuclear β -decays



Falkowski et al, JHEP04 (2021) 126

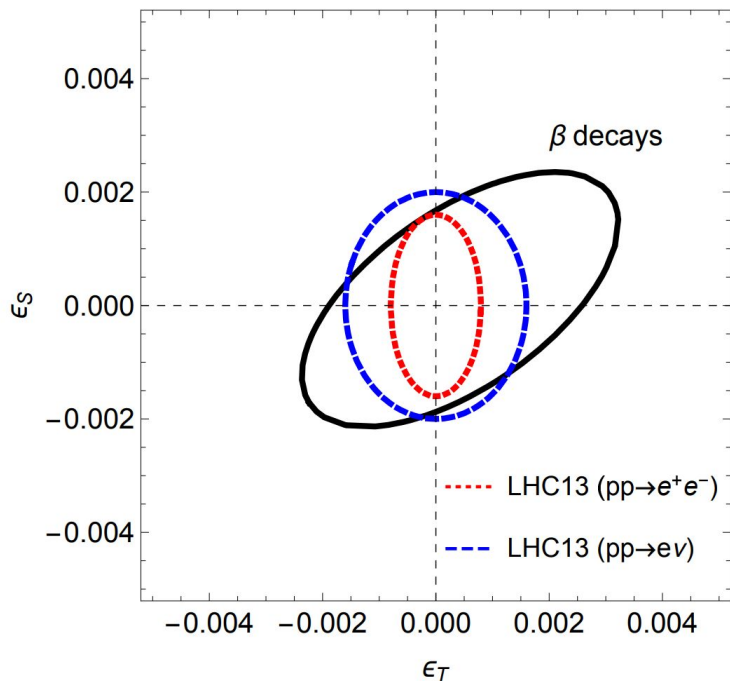
New physics impact of nuclear β -decays



Question: How reliable are the estimates of nuclear uncertainties?

Falkowski et al, JHEP04 (2021) 126

New physics impact of nuclear β -decays

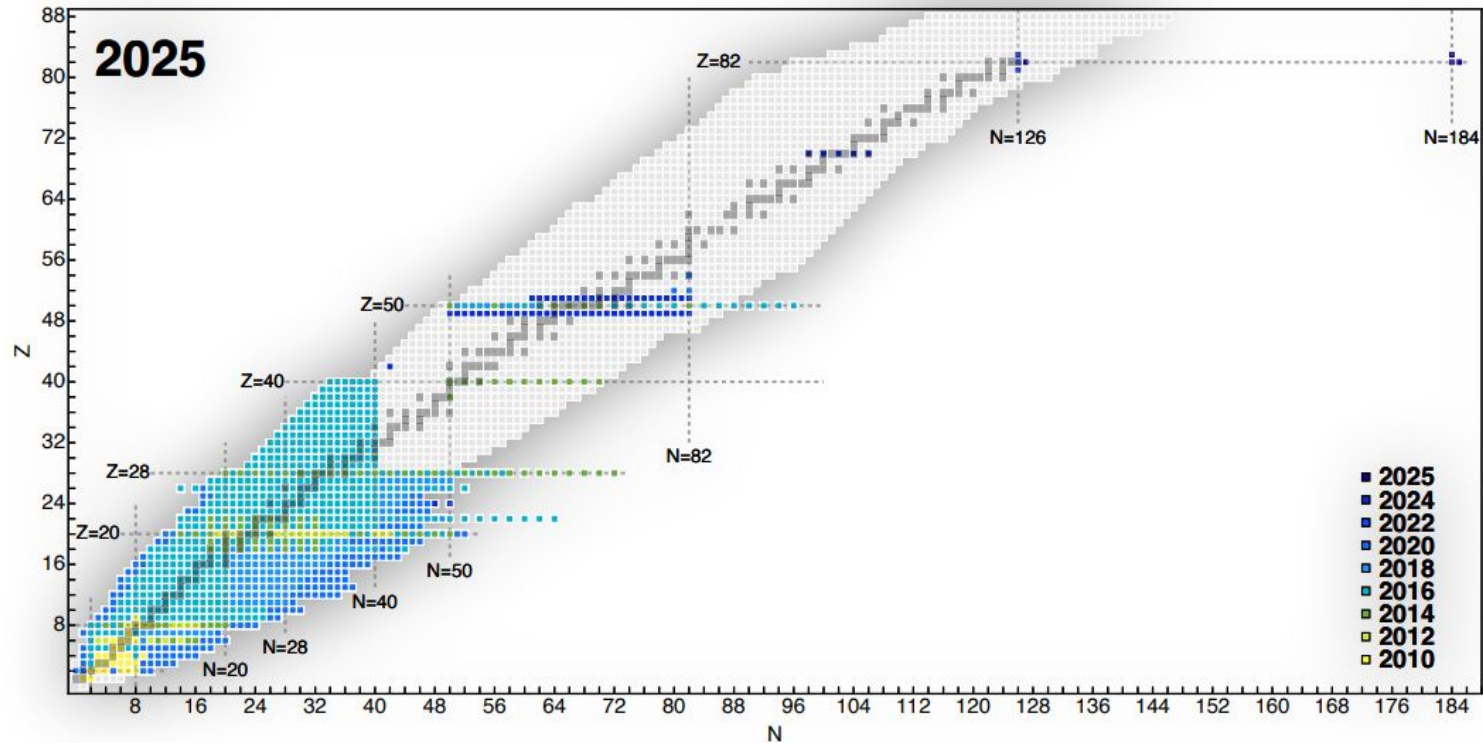


Falkowski et al, JHEP04 (2021) 126

Question: How reliable are the estimates of nuclear uncertainties?

To answer, we need *precise* and *accurate* calculations of nuclear observables

Landscape of *ab initio* calculations



Many-body approaches

- **Coordinate space:**
 - Quantum Monte Carlo
 - Lattice EFT
- **Configuration Space (Particle-Hole Expansions):**
 - No-core shell model (NCSM)
 - Coupled Cluster (CC)
 - In-medium SRG (IMSRG)
 - Self-consistent Green's Functions (SCGF)
 - Many-body perturbation theory (MBPT)
- **Configuration Space (Geometric Expansions):**
 - Symmetry-adapted NCSM
 - Projected GCM
 - Deformed HFB + projection

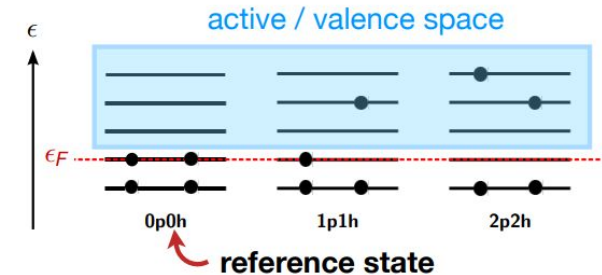
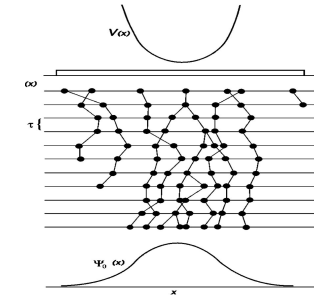


Figure: H. Herget

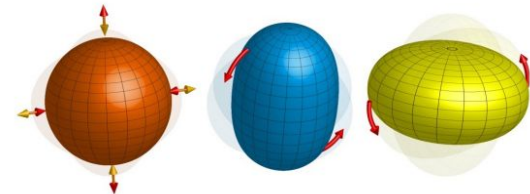


Figure: H. Herget

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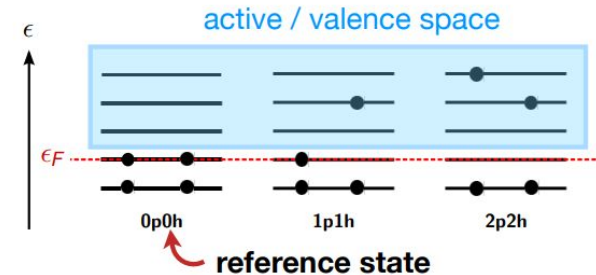
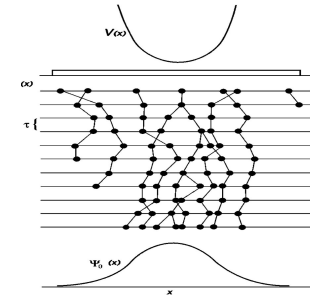


Figure: H. Herget

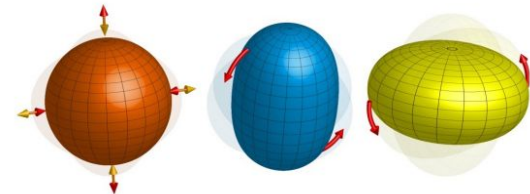
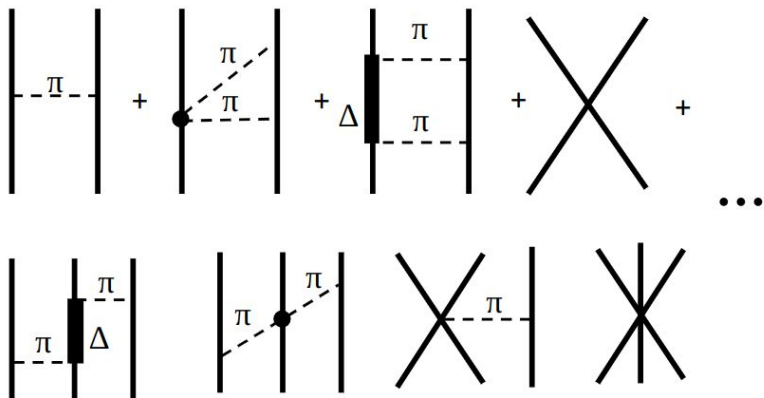


Figure: H. Herget

Chiral effective field theory schematic



**In principle*

Procedure to root NN interaction in symmetries of Quantum Chromodynamics*

Scales: Nucleon momentum $Q \sim m_\pi \sim m_N - m_\Delta$ vs. heavier mesons at the scale $\Lambda \sim 1 \text{ GeV} \rightarrow$

Systematically improvable expansion*

Low-energy constants (LECs) subsume the underlying QCD

van Kolck, Weinberg, Ordóñez, Epelbaum, Hammer, Meißner, Entem, Machleidt, ...

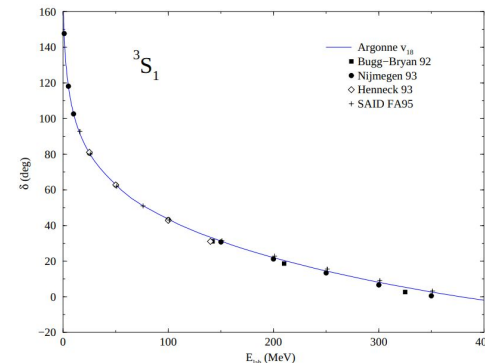
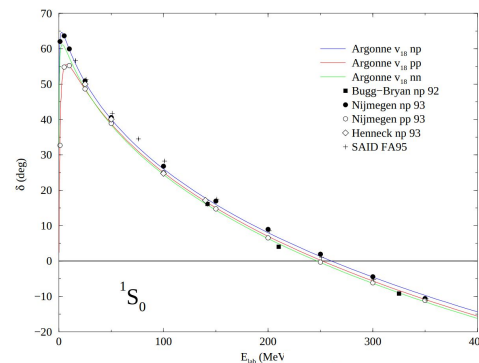
The Argonne v18 (AV18) interaction

Phenomenological nuclear Hamiltonian with 18 operators, 40 parameters

Includes one- and two-pion exchange, and contact terms

Fit to np, pp phase shift data through F waves

Used in conjunction with three-body forces (ex: IL7)



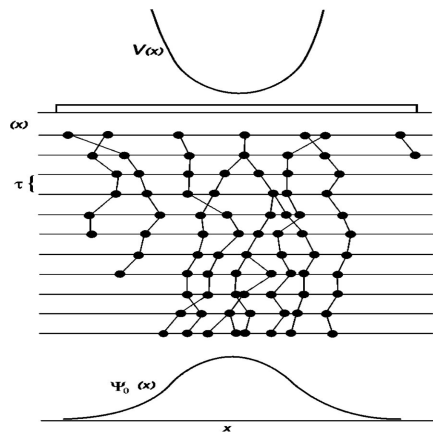
<https://www.phy.anl.gov/theory/research/av18/>

Quantum Monte Carlo

Solving the many-body problem using random sampling to compute integrals

Variational MC wave function $|\Psi_T\rangle = \mathcal{F}|\Phi\rangle$ contains **model wave function** and **many-body correlations** optimized by minimizing:

$$E_V = \min \left\{ \frac{\langle \Psi_T | H | \Psi_T \rangle}{\langle \Psi_T | \Psi_T \rangle} \right\} \geq E_0$$



Green's function MC improves by **removing excited state contamination** and **gives the exact ground state**

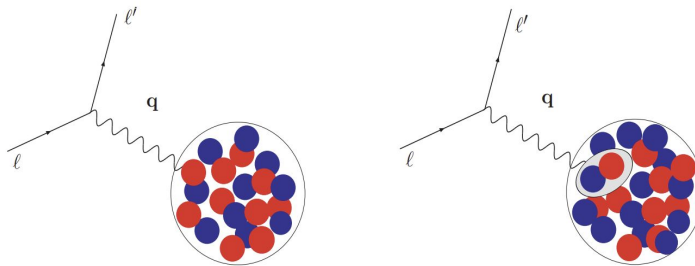
$$\lim_{\tau \rightarrow \infty} e^{-(H-E_0)\tau} \Psi_V = \lim_{\tau \rightarrow \infty} e^{-(H-E_0)\tau} \left(c_0 \psi_0 + \sum_{i=1}^N c_i \psi_i \right) \rightarrow c_0 \psi_0$$

Electroweak charge and current operators

Schematically:

$$\rho = \sum_{i=1}^A \rho_i + \sum_{i<j} \rho_{ij} + \dots$$
$$\mathbf{j} = \sum_{i=1}^A \mathbf{j}_i + \sum_{i<j} \mathbf{j}_{ij} + \dots$$

External field interacts with **single nucleons** and **correlated pairs** of nucleons



Pastore et al. PRC 80, 034004 (2009), Pastore et al. PRC 84, 024001 (2011), Piarulli et al. PRC 87, 014006 (2013), Schiavilla et al. PRC 99, 034005 (2019), Baroni et al. PRC 93, 049902 (2016), ...

${}^6\text{He}$ β -decay spectrum: Overview

Differential rate: $\frac{d\Gamma_0}{dE_e} = |M|^2 G_\beta(E_e)$

New physics can distort this: $\frac{d\Gamma}{dE_e} = \frac{d\Gamma_0}{dE_e} \left[1 + b \frac{m_e}{E_E} \right]$

Similar distortions can be generated when accounting for nuclear recoil

Performed calculation with recoil corrections and two-body physics effects

Vector
Scalar



Fermi

Axial
Tensor
Pseudoscalar



GT

${}^6\text{He}$ β -decay spectrum: Multipole decomposition

$$d\Gamma = 2\pi\delta(M_i - E_f - E_e - E_\nu)G_F^2 V_{ud}^2 \frac{4\pi}{2J_i + 1} \left[(1 + \mathbf{v}_e \cdot \mathbf{v}_\nu) \sum_{l \geq 0} |C_l(q)|^2 + (1 - \mathbf{v}_e \cdot \mathbf{v}_\nu + 2\mathbf{v}_e \cdot \hat{\mathbf{q}} \mathbf{v}_\nu \cdot \hat{\mathbf{q}}) \sum_{l \geq 0} |L_l(q)|^2 - 2\hat{\mathbf{q}} \cdot (\mathbf{v}_e + \mathbf{v}_\nu) \sum_{l \geq 0} \text{Re} [C_l(q) L_l^*(q)] + (1 - \mathbf{v}_e \cdot \hat{\mathbf{q}} \mathbf{v}_\nu \cdot \hat{\mathbf{q}}) \sum_{l \geq 1} [|M_l(q)|^2 + |E_l(q)|^2] \pm 2\hat{\mathbf{q}} \cdot (\mathbf{v}_\nu - \mathbf{v}_e) \sum_{l \geq 1} \text{Re} [M_l(q) E_l^*(q)] \right] \frac{d^3 \mathbf{p}_e}{(2\pi)^3} \frac{d^3 \mathbf{p}_\nu}{(2\pi)^3}$$

Spectrum can be written in terms of multipole operators (C, L, M, E)

Low q value of the decay means we can consider expansion of multipoles

Expand multipoles, kinematics to write down spectrum differential in electron energy

${}^6\text{He}$ β -decay spectrum: Multipoles

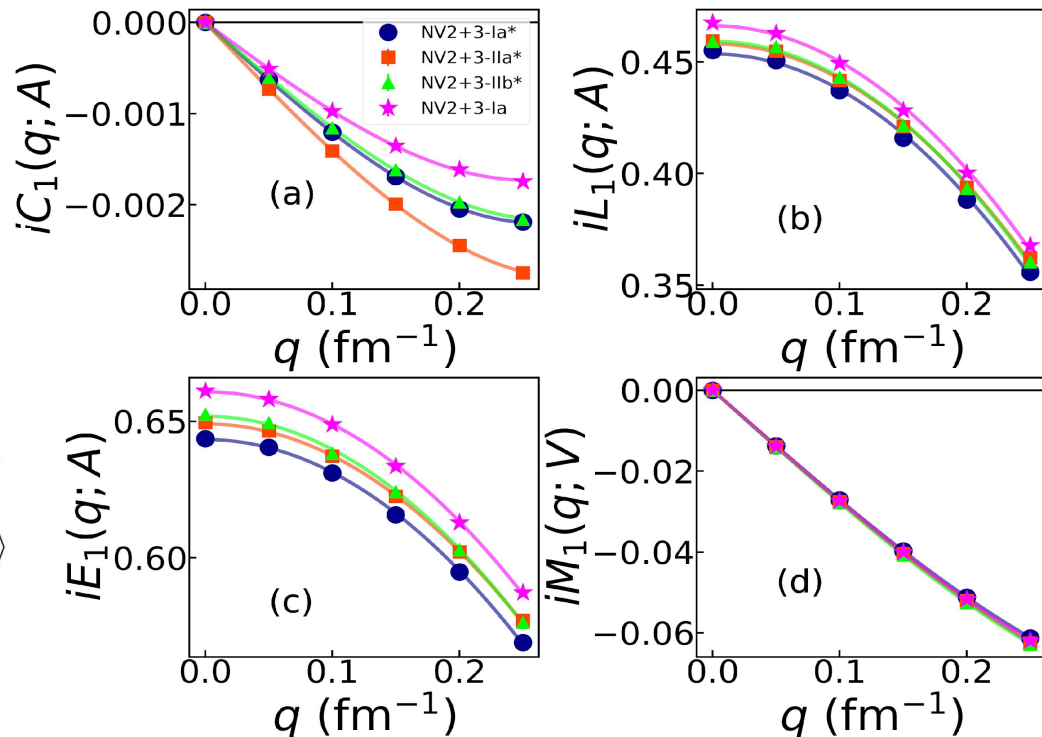
Distortion term is a function of four nuclear matrix elements:

$$C_1(q; A) = \frac{i}{\sqrt{4\pi}} \langle {}^6\text{Li}, 10 | \rho_+^\dagger(q\hat{\mathbf{z}}; A) | {}^6\text{He}, 00 \rangle$$

$$L_1(q; A) = \frac{i}{\sqrt{4\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{z}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{z}}; A) | {}^6\text{He}, 00 \rangle$$

$$E_1(q; A) = -\frac{i}{\sqrt{2\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{z}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{x}}; A) | {}^6\text{He}, 00 \rangle$$

$$M_1(q; V) = -\frac{1}{\sqrt{2\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{y}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{x}}; V) | {}^6\text{He}, 00 \rangle$$



${}^6\text{He}$ β -decay spectrum: Multipoles

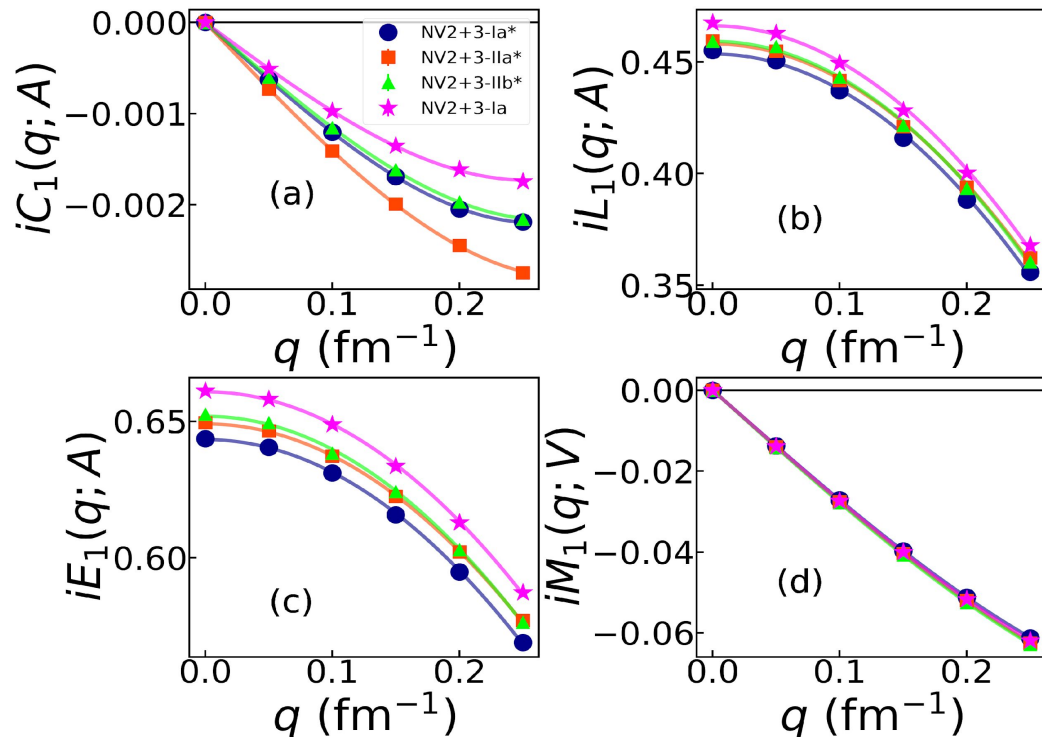
Distortion term is a function of four nuclear matrix elements:

$$C_1(q; A) = -i \frac{qr_\pi}{3} \left(C_1^{(1)}(A) - \frac{(qr_\pi)^2}{10} C_1^{(3)}(A) + \mathcal{O}[(qr_\pi)^4] \right)$$

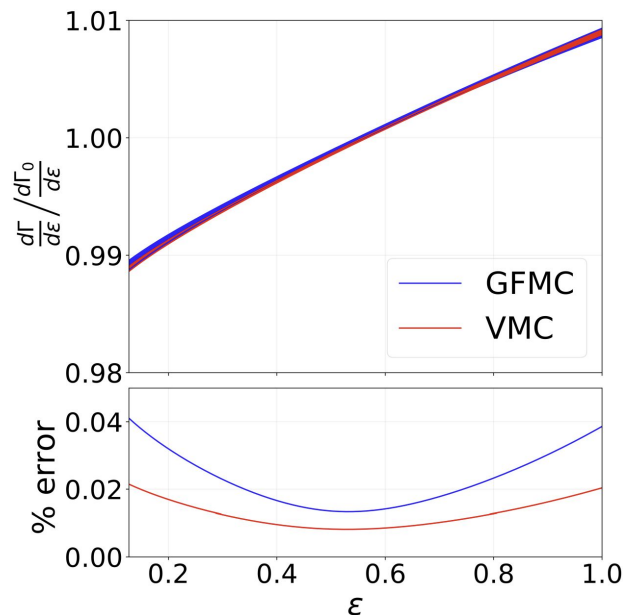
$$L_1(q; A) = -\frac{i}{3} \left(L_1^{(0)}(A) - \frac{(qr_\pi)^2}{10} L_1^{(2)}(A) + \mathcal{O}[(qr_\pi)^4] \right)$$

$$M_1(q; V) = -i \frac{qr_\pi}{3} \left(M_1^{(1)}(V) - \frac{(qr_\pi)^2}{10} M_1^{(3)}(V) + \mathcal{O}[(qr_\pi)^4] \right)$$

$$E_1(q; A) = -\frac{i}{3} \left(E_1^{(0)}(A) - \frac{(qr_\pi)^2}{10} E_1^{(2)}(A) + \mathcal{O}[(qr_\pi)^4] \right)$$



^6He β -decay spectrum: Standard Model results

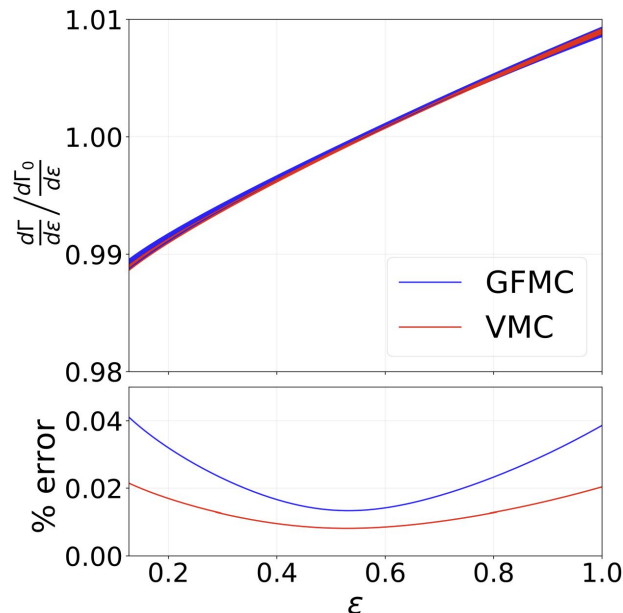


$$\varepsilon = \frac{E_e}{\omega}$$

$$\begin{aligned} \frac{d\Gamma}{d\varepsilon} = & (1 + \Delta_R^V)(1 + \delta_R(Z, \varepsilon)) \frac{G_F^2 W_0^5 V_{ud}^2}{2\pi^3} \sqrt{1 - \frac{\mu_e^2}{\varepsilon^2}} \varepsilon^2 (1 - \varepsilon)^2 F_0(Z, \varepsilon) L_0(Z, \varepsilon) S(Z, \varepsilon) R_N(\varepsilon) \\ & \frac{4\pi}{2J_i + 1} \frac{1}{9} \left\{ 3 \left| L_1^{(0)} \right|^2 \left[1 + \alpha Z W_0 R \left(\frac{2}{35} - \frac{233}{630} \frac{\alpha Z}{W_0 R} - \frac{1}{70} \frac{\mu_e^2}{\varepsilon} - \frac{4}{7} \varepsilon \right) \right] \right. \\ & + 2W_0 r_\pi \left[\left(1 - 2\varepsilon + \frac{\mu_e^2}{\varepsilon} \right) \text{Re}(E_1^{(0)} M_1^{(1)*}) - \left(1 - \frac{\mu_e^2}{\varepsilon} \right) \text{Re}(L_1^{(0)} C_1^{(1)*}) \right] \\ & + \frac{(W_0 r_\pi)^2}{3} \left[\left(3 - 4\varepsilon(1 - \varepsilon) - \mu_e^2 \frac{2 + \varepsilon}{\varepsilon} \right) |C_1^{(1)}|^2 - \frac{3}{5} \left(1 - \frac{\mu_e^2}{\varepsilon} (2 - \varepsilon) \right) \text{Re}(L_1^{(0)} L_1^{(2)*}) \right. \\ & + \left. \left(3 - 10\varepsilon(1 - \varepsilon) + \mu_e^2 \frac{4 - 7\varepsilon}{\varepsilon} \right) \left(\left| M_1^{(1)} \right|^2 - \frac{1}{5} \text{Re}(E_1^{(0)} E_1^{(2)}) \right) \right] \\ & \left. - \frac{4}{7} \frac{\alpha Z W_0 r_\pi^2}{R} (1 - \varepsilon) \left(\frac{E_1^{(0)} E_1^{(2)}}{2} - L_1^{(0)} L_1^{(2)} \right) \right\} \end{aligned}$$

Fully expanded spectrum in terms of multipole coefficients with Behrens-Bühring RC, Coulomb, shielding, and recoil corrections

${}^6\text{He}$ β -decay spectrum: Standard Model results



Model uncertainty plus two-body contribution brings theory precision within needs of experiment

$$T_{\text{VMC}} = 762 \pm 11 \text{ ms}$$

$$T_{\text{GFMC}} = 808 \pm 24 \text{ ms}$$

$$T_{\text{Expt.}} = 807.25 \pm 0.16 \pm 0.11 \text{ ms}$$

[Kanafani et al. PRC 106, 045502 (2022)]

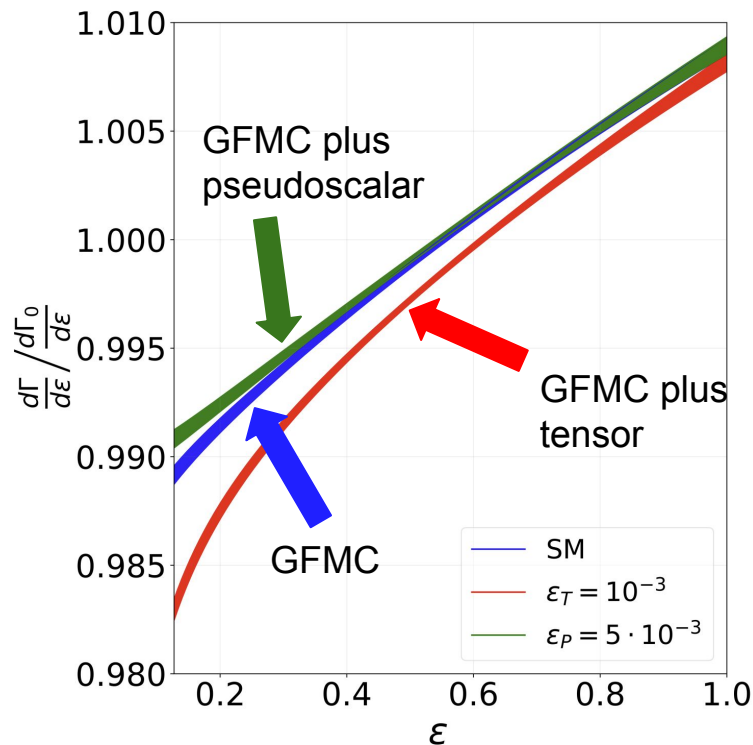
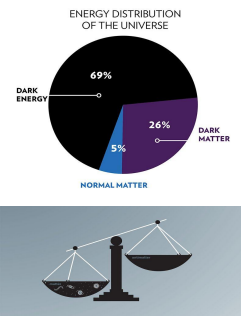
$$\varepsilon = \frac{E_e}{\omega}$$

${}^6\text{He}$ β -decay spectrum: Probing new forces

Included transition operators associated with new physics

With permille precision, it will be possible to further constrain new physics

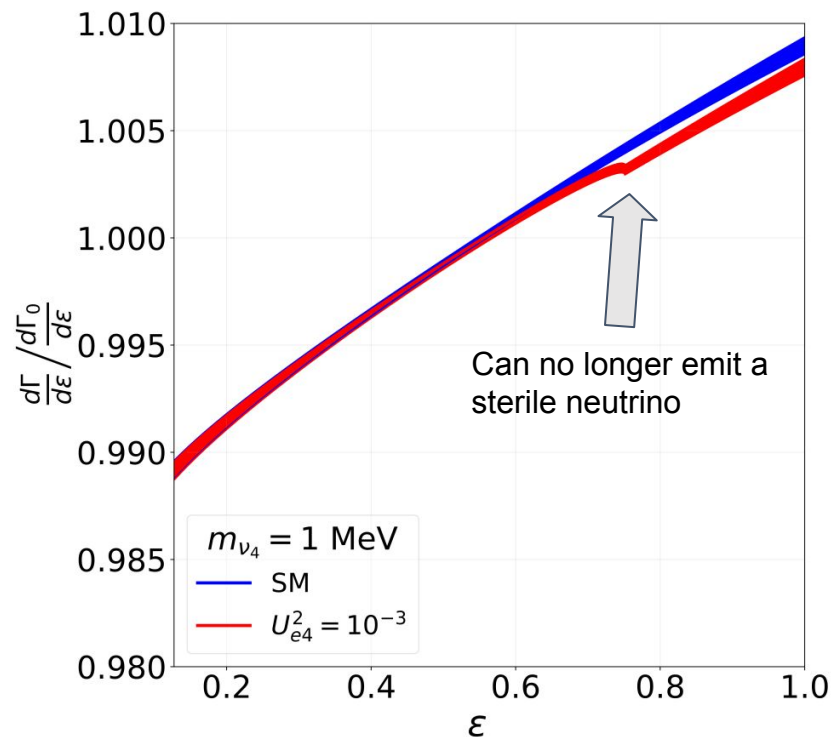
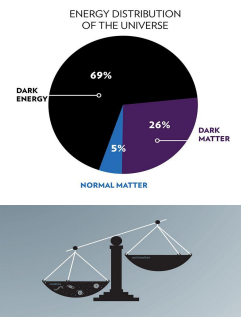
$$\Lambda_{\text{BSM}} \sim \frac{\Lambda_{\text{EW}}}{\sqrt{\epsilon_i}} \sim 1\text{--}10 \text{ TeV}$$



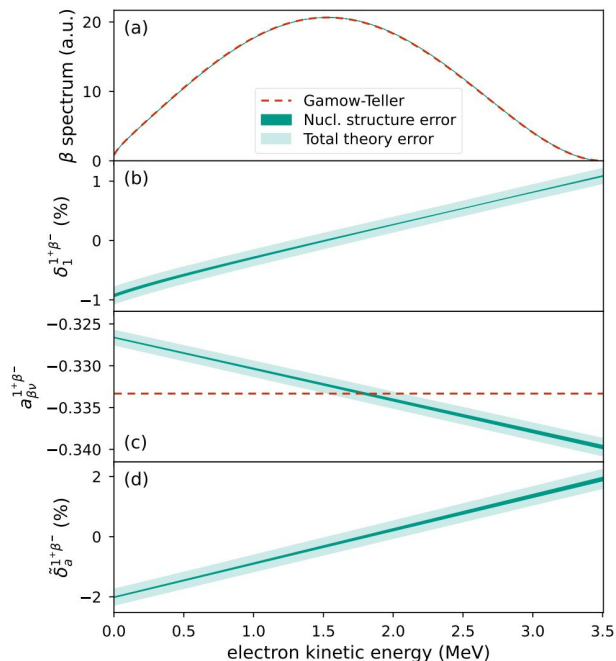
^6He β -decay spectrum: Probing neutrino physics

Can also investigate impacts from production of ~ 1 MeV sterile neutrinos

The shape of the decay endpoint can exclude some parameter space and probe BSM scenarios



Comparison with NCSM results



Favorable comparison with previous result using NCSM with LO currents

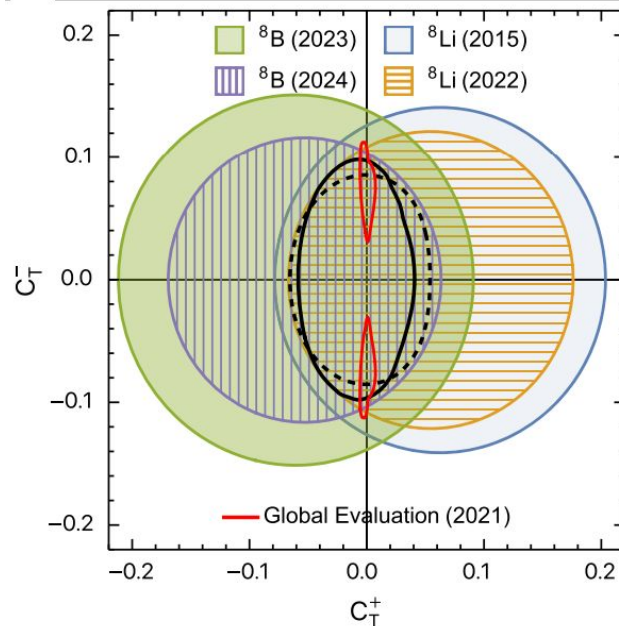
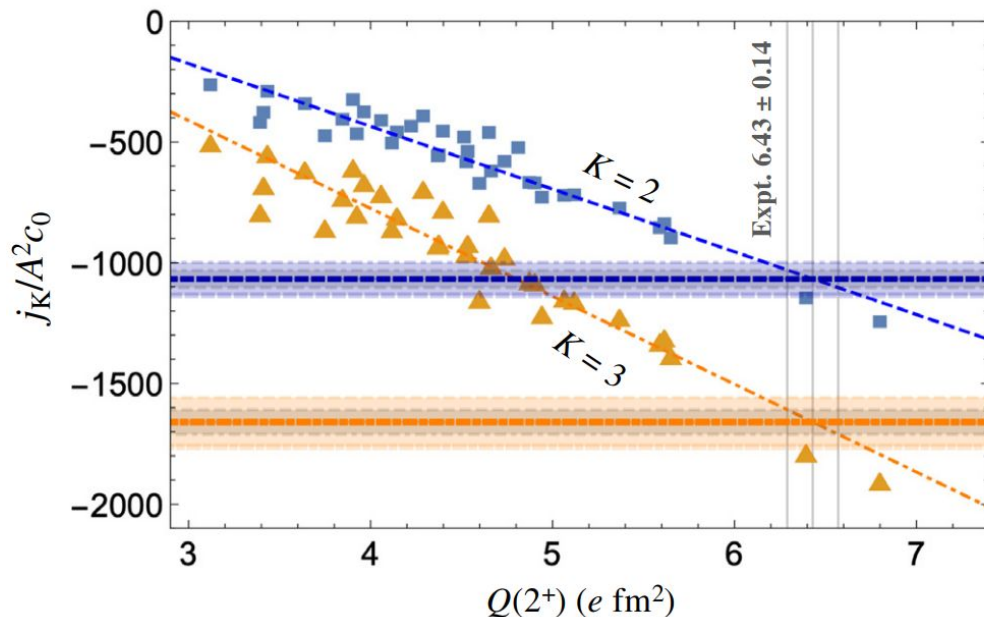
$$b(\text{NCSM}) = -1.52(18) \times 10^{-3}$$

$$b(\text{GFMC}) = -1.47(03) \times 10^{-3}$$

With two-body currents, uncertainty on b Fierz is reduced

Glick-Magid et al. Phys. Lett. B 832 (2022) 137259

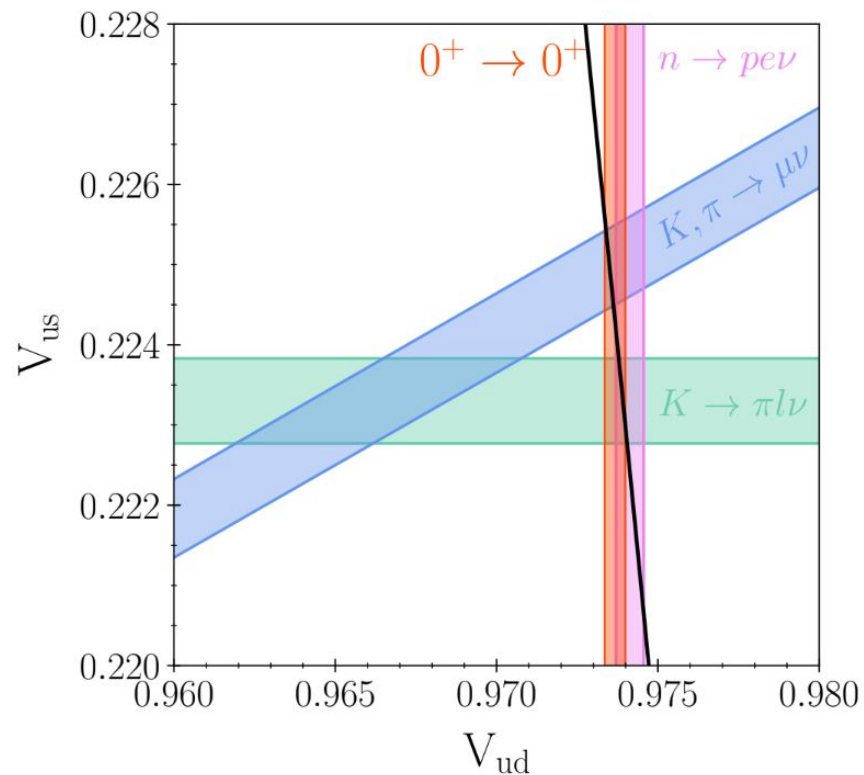
A=8 spectra with SA-NCSM



Longfellow et al. PRL 132, 142502 (2024)

Falkowski et al, JHEP04 (2021) 126

Nuclear β -decay for tests of CKM unitarity



Superaligned $0^+ \rightarrow 0^+$ decays

$$\mathcal{F}t = \frac{K}{2G_F^2 V_{ud}^2 (1 + \Delta_R^V)} = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C)$$

Transition-independent single-nucleon corrections

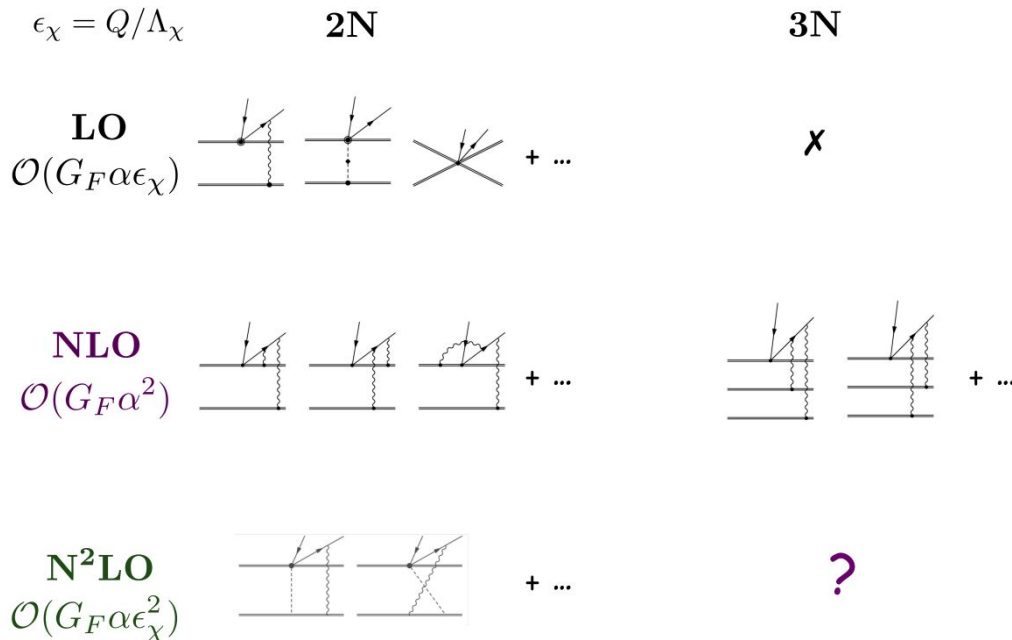
Correction sensitive to charge and electron energy

Sensitive to internal structure of the nucleus

Broken isospin symmetry between protons and neutrons

EFT approach to radiative corrections

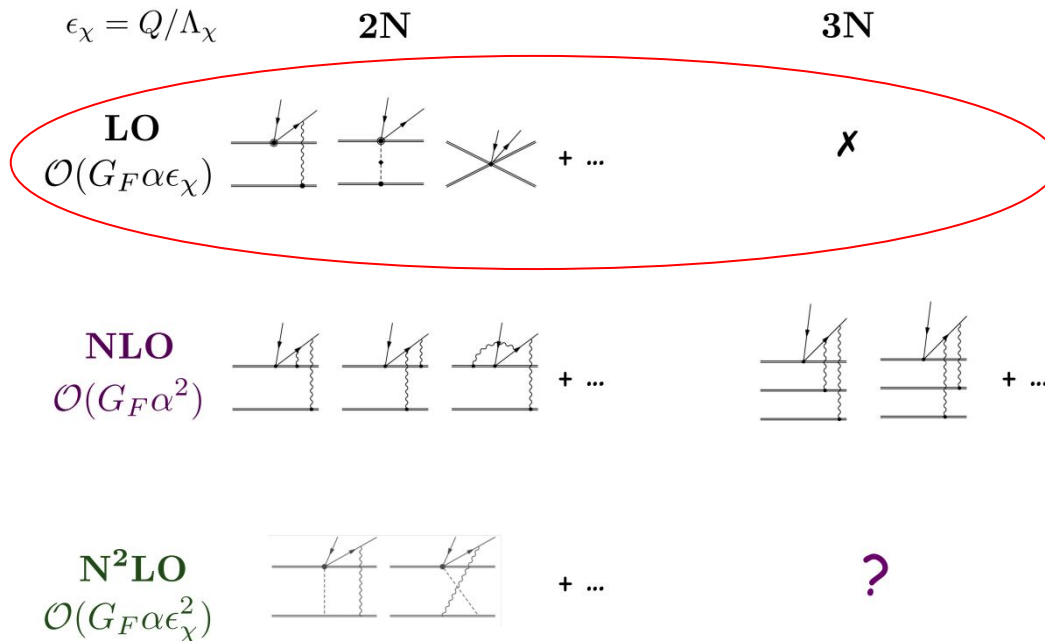
Cirigliano, Dekens,
Hoferichter,
Meregghetti,
Tomalak, + ...



Cirigliano et al. PRL 133, 211801 (2024)

EFT approach to radiative corrections

Cirigliano, Dekens,
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Cirigliano et al. PRL 133, 211801 (2024)

$^{10}\text{C}(0^+) \rightarrow ^{10}\text{B}(0^+) \beta\text{-decay}$

In an effective field theory approach:

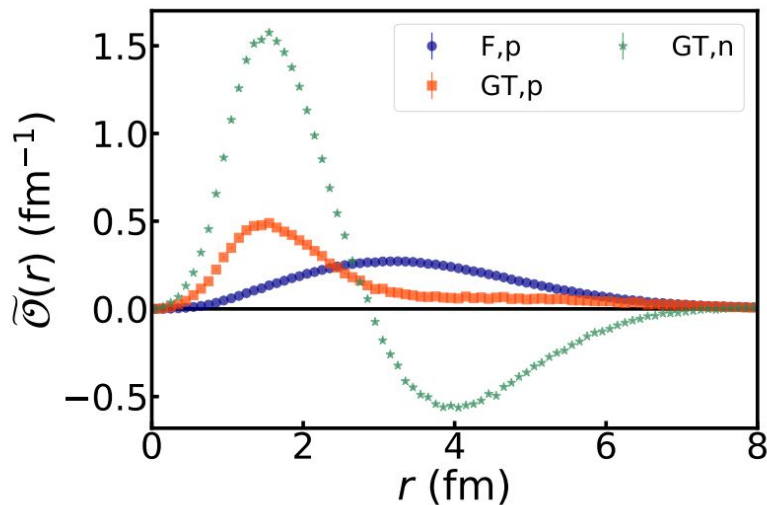
$$\delta_{\text{NS}} = \sum_{m,n,i} \alpha^m E_0^n c_{m,n} M_{m,n}^i$$

Can also evaluate: $M = \int dr C(r) \tilde{\mathcal{O}}(r)$

GPMC: $\delta_{\text{NS}} = -4.46(48) \times 10^{-3} - -4.64(77) \times 10^{-3}$

Hardy and Towner: $\delta_{\text{NS}} = -4.0(5) \times 10^{-3}$

Gennari et al PRL 134, 012501: $\delta_{\text{NS}} = -4.22(32) \times 10^{-3}$



King et al., arXiv:2509.07310v1

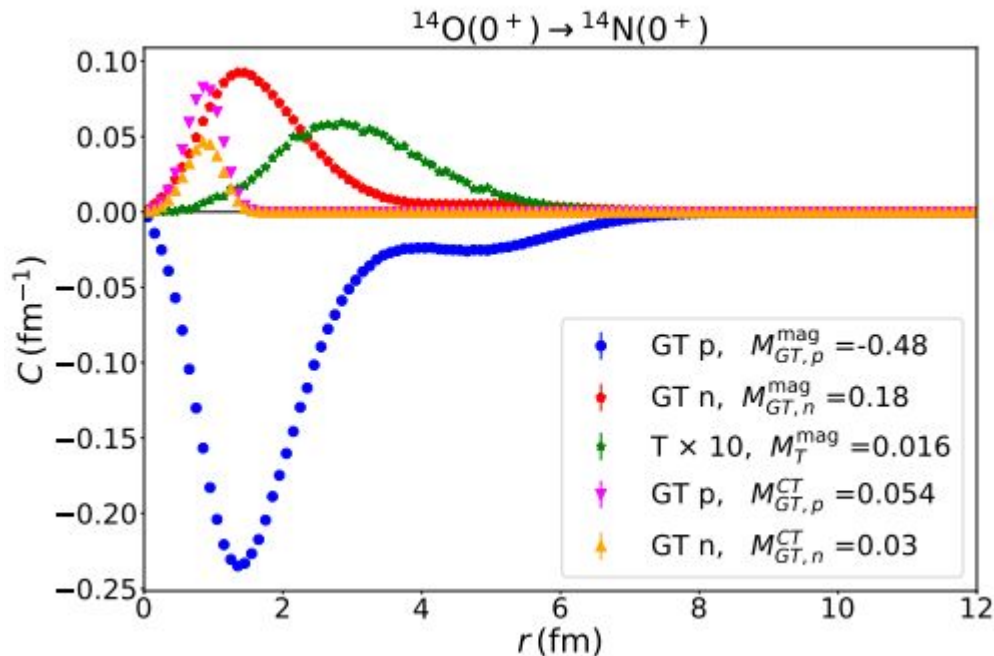
Auxiliary Field Diffusion Monte Carlo (AFDMC)

Use the single particle basis: $\langle S | \Psi \rangle \propto \xi_{\alpha_1}(s_1) \xi_{\alpha_2}(s_2) \dots \xi_{\alpha_A}(s_A)$

Can linearize two-body operators:
$$e^{-\frac{\lambda}{2}\mathcal{O}^2} = \frac{1}{\sqrt{2\pi}} \int dx e^{-\frac{x^2}{2}} e^{x\sqrt{-\lambda}\mathcal{O}}$$

Polynomial scaling in particle number, but technically more complicated to operate on the wave function

$^{14}\text{O}(0^+)$ decay using AFDMC



Cirigliano et al. PRC 110, 055502 (2024)

Evaluation using one chiral EFT potential

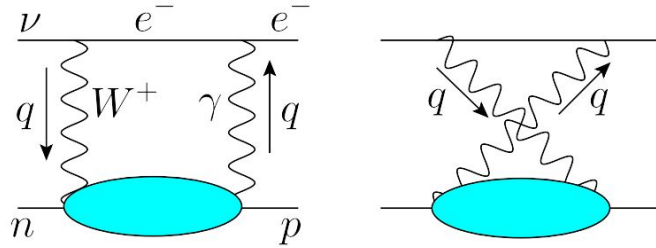
Results in $\delta_{\text{NS}} = -2.84(88) \times 10^{-3}$

Agrees with standard result:

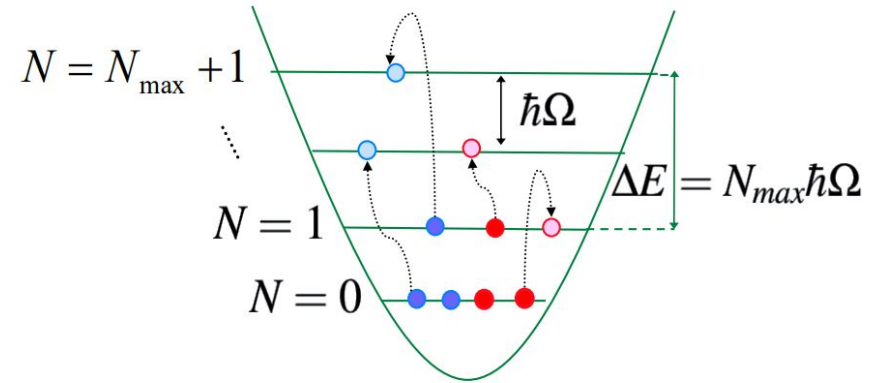
$$\delta_{\text{NS}} = -2.83(64) \times 10^{-3}$$

Future work to quantify uncertainty by varying interactions

NCSM + Dispersive approach

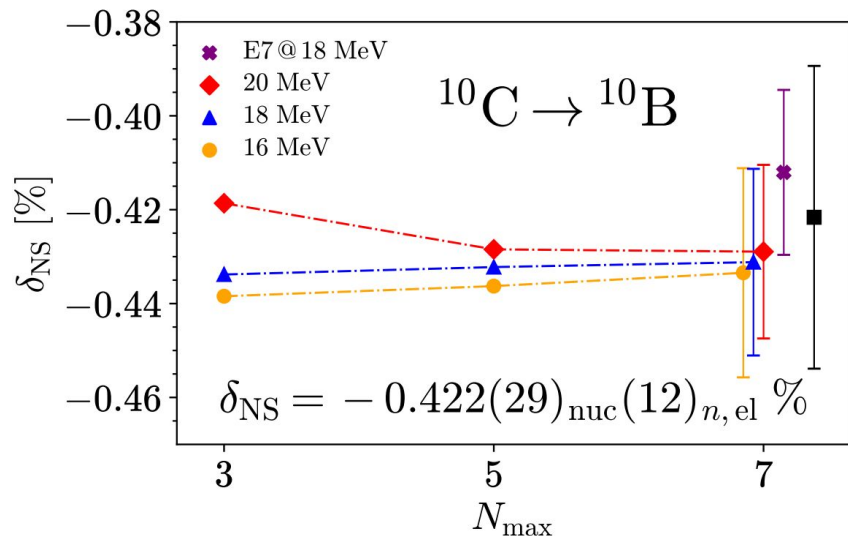


C.-Y. Seng PRD 100, 013001 (2019)

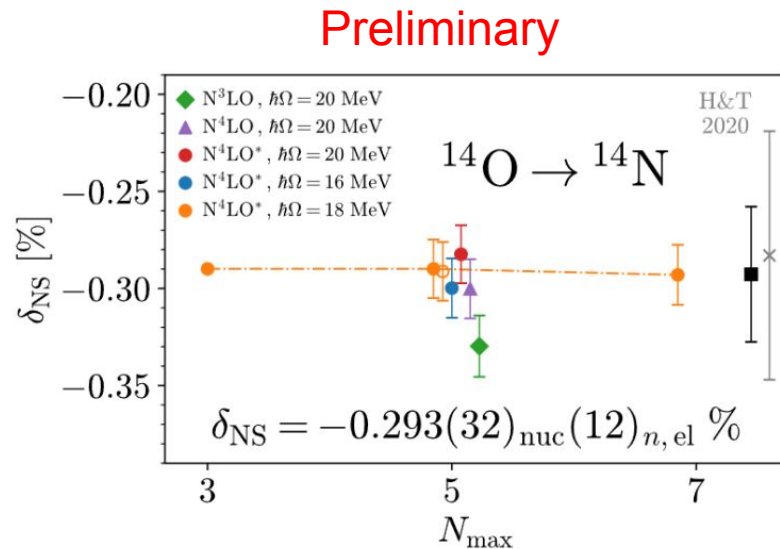


cf. talk by Misha Gorshteyn

NCSM + Dispersive approach

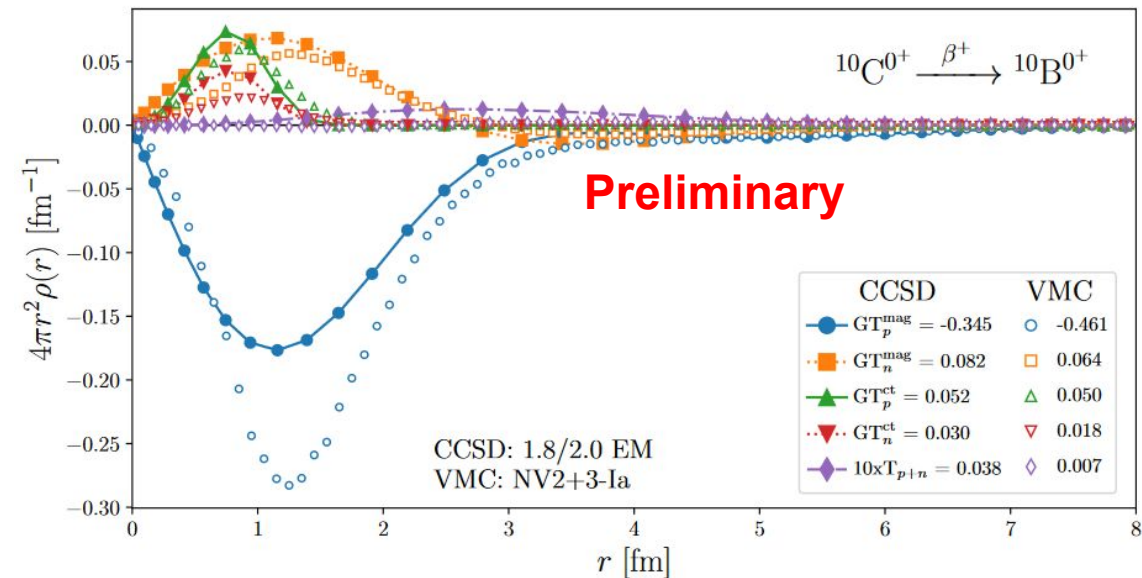


M. Gennari et al. PRL 134, 012501 (2025)



M. Gennari, “Electroweak Radiative Corrections in Super-Allowed Beta Decays from Ab Initio Theory” (2025)

Outlook: Benchmark QMC + Coupled-cluster



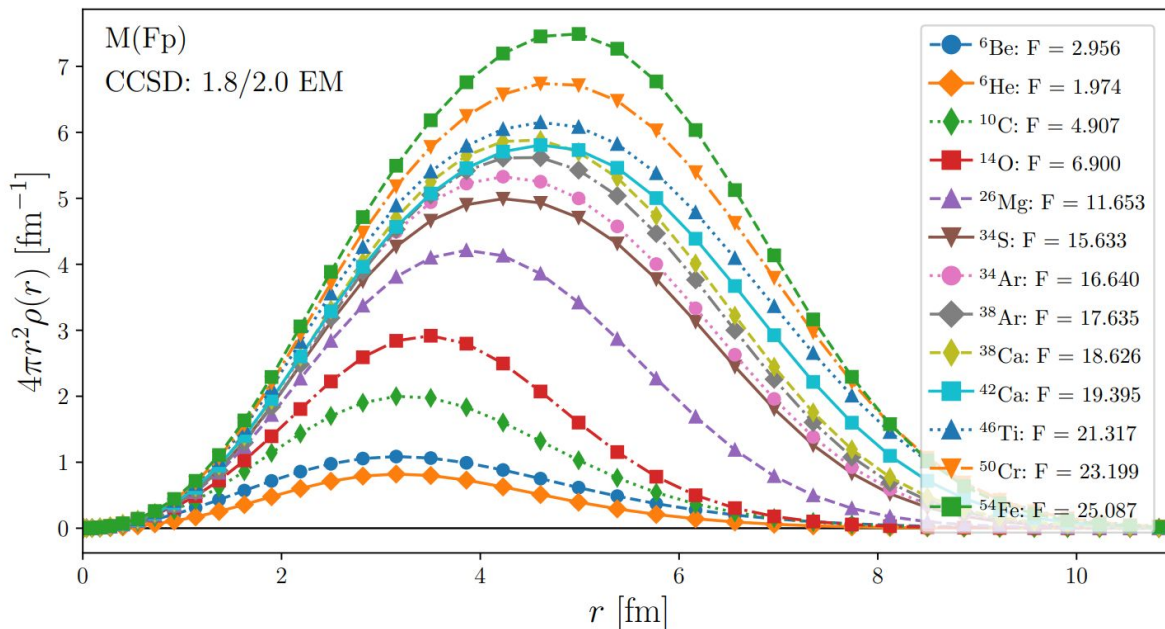
Benchmarking different models, methods in first step toward global analysis

Qualitative agreement, but further analysis necessary

Figure courtesy of Sam Novario

Outlook: Global analysis Coupled-cluster

Preliminary



S. J. Novario, “Nuclear-Structure Corrections in Superaligned Beta Decay” (2025)

Outlook: Higher-order EFT operators

G. Chambers-Wall,
 Cirigliano, Dekens,
 Hoferichter,
 Mereghetti, Tomalak,
 + ...

$$\epsilon_\chi = Q/\Lambda_\chi \quad 2\text{N}$$

LO
 $\mathcal{O}(G_F \alpha \epsilon_\chi)$

+ ...

NLO
 $\mathcal{O}(G_F \alpha^2)$

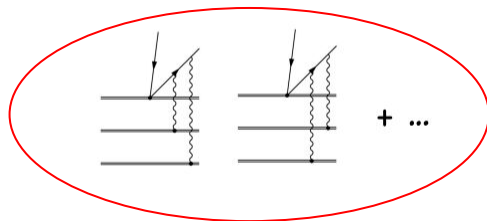
+ ...

N²LO
 $\mathcal{O}(G_F \alpha \epsilon_\chi^2)$

+ ...

3N

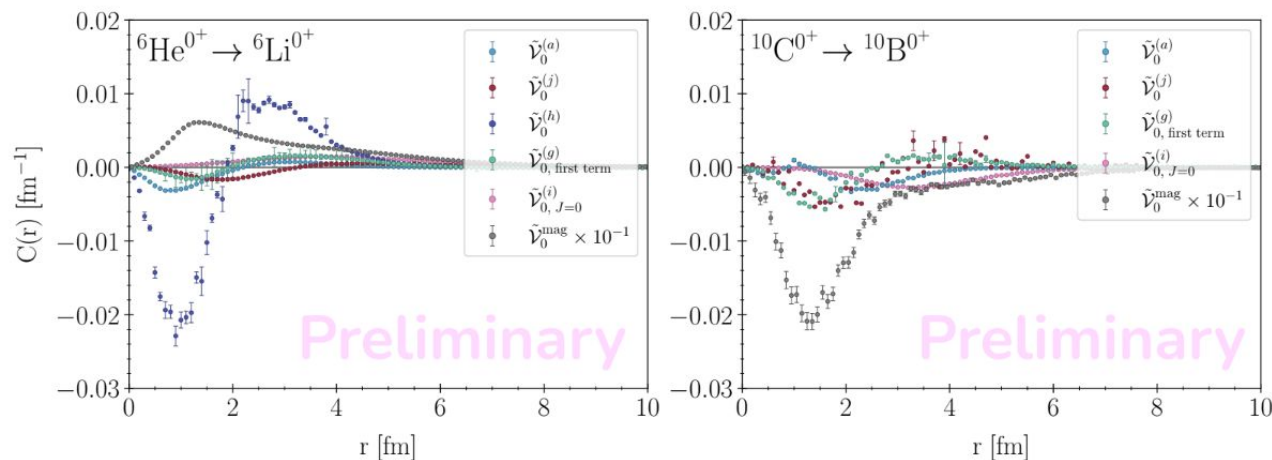
~~X~~



?

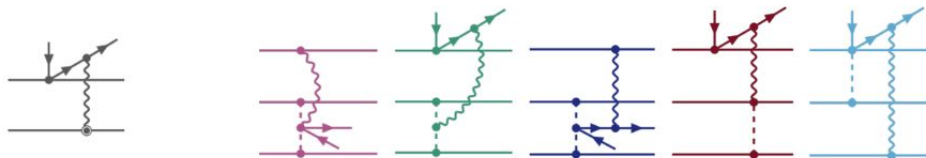
Outlook: Higher-order EFT operators

G. Chambers-Wall



Preliminary calculation of NLO contributions

~5% corrections to LO two-body from NLO

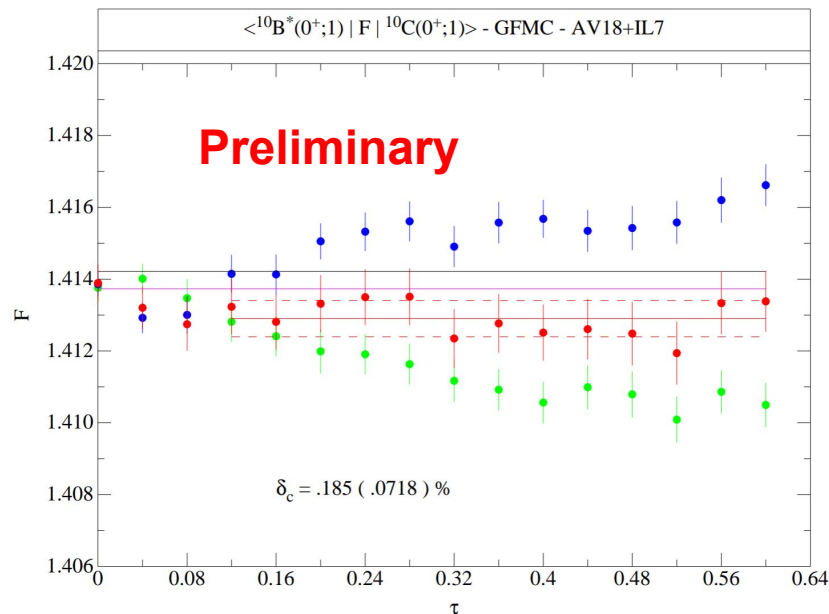


Isospin breaking corrections with GFMC

Fermi matrix element evaluated using wave functions with isospin breaking correlations

AV18+IL7 results consistent with Hardy and Towner with ~2.6 times smaller error bar

Chiral interaction predicts ~1.4 times larger correction, ~2 times larger error



Outlook



Two questions/challenges

Model uncertainty procedures are presently ad hoc– can we leverage emulations techniques in order to provide robust error bars on theory?

There are a number of EFT interactions on the market– how can we establish consistent benchmarks between the methods?



Conclusions

Reach of ab initio methods has progressed over the last 15 years

Recent studies of spectra, superallowed decays in light nuclei contributing to precision beta decay studies

Methods amenable to heavy nuclei can expand reach of cases ab initio nuclear theory can help interpret

Uncertainties and benchmarks remain a challenge, should be addressed

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Additional slides



Variational Monte Carlo

Slater determinant of nucleons in s- and p-shell coupled to the appropriate quantum numbers

Pair correlation operator encoding appropriate cluster structure

Two- and three-body correlation operator to reflect impact of nuclear interaction at short distances

Optimize when you minimize:

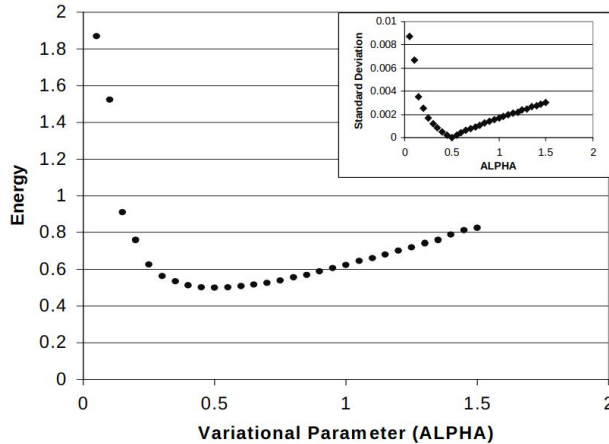
$$E_V = \frac{\langle \Psi_V | H | \Psi_V \rangle}{\langle \Psi_V | \Psi_V \rangle} \geq E_0$$

Variational Monte Carlo: 1D Example

$$V(x) = \frac{1}{2}x^2$$
$$\Psi_0(x) = \left(\frac{1}{\pi}\right)^{1/4} e^{-x^2/2}$$
$$E_0 = \frac{1}{2}$$

Use Monte Carlo to compute:

$$\frac{\langle \Psi_T | H | \Psi_T \rangle}{\langle \Psi_T | \Psi_T \rangle} = \frac{\int d\mathbf{R} |\Psi_T(\mathbf{R})|^2 E_L(\mathbf{R})}{\int d\mathbf{R} |\Psi_T(\mathbf{R})|^2}; \quad E_L(\mathbf{R}) = \frac{H\Psi_T(\mathbf{R})}{\Psi_T(\mathbf{R})}$$



Can tune $\Psi_T = \left(\frac{2\alpha}{\pi}\right)^{1/4} e^{-\alpha x^2}$ to solve

Pottorf et al, Eur. J. Phys. 20 205 (1999)

Green's function Monte Carlo

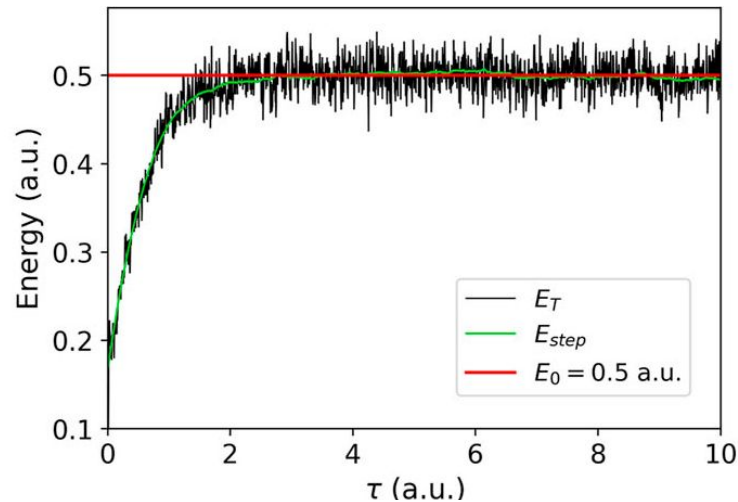
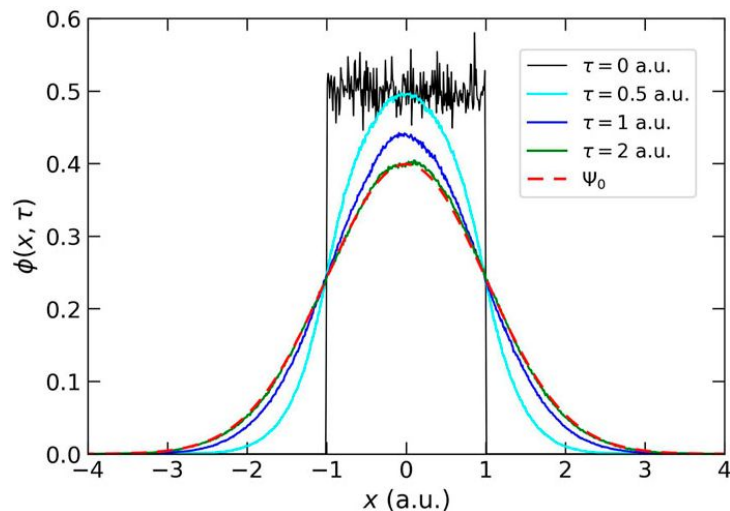
Recast $i\frac{\partial}{\partial t} |\Psi(t)\rangle = (H - E_T) |\Psi(t)\rangle$ as $-\frac{\partial}{\partial \tau} |\Psi(\tau)\rangle = (H - E_T) |\Psi(\tau)\rangle$

Solution: $|\Psi(\tau)\rangle = e^{-(H-E_T)\tau} |\Psi(0)\rangle$

Recall $|\Psi(0)\rangle = \sum_i c_i |\psi_i\rangle$ and note $e^{-(H-E_0)\tau} |\Psi(0)\rangle = c_0 \psi_0 + \sum_i e^{-\alpha_i \tau} c_i |\psi_i\rangle; \alpha_i > 0$

For a proper offset $\lim_{\tau \rightarrow \infty} e^{-(H-E_0)\tau} |\Psi(0)\rangle \rightarrow c_0 \psi_0$

Green's function Monte Carlo: 1D example



$$G(\mathbf{R}', \mathbf{R}) = \langle \mathbf{R}' | e^{-(H-E_0)\Delta\tau} | \mathbf{R} \rangle$$

$$\Psi(\mathbf{R}_N; \tau) = \int d\mathbf{R}_{N-1} \dots d\mathbf{R}_1 d\mathbf{R}_0 G(\mathbf{R}_N, \mathbf{R}_{N-1}) \dots G(\mathbf{R}_2, \mathbf{R}_1) G(\mathbf{R}_1, \mathbf{R}_0) \Psi(\mathbf{R}_0; 0)$$

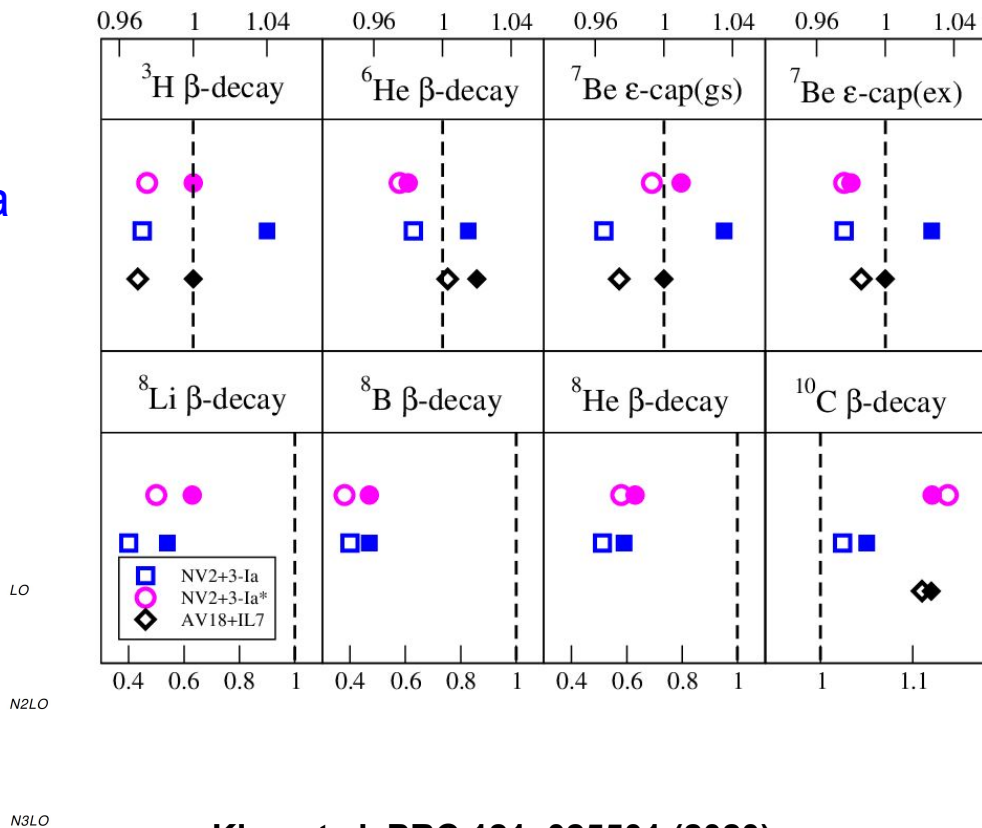
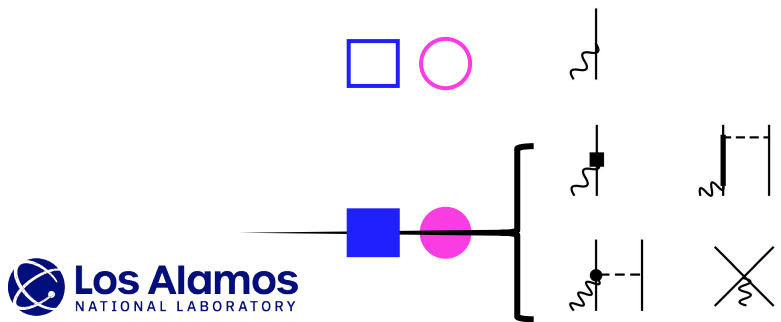
β -decay rates

Computed with two models:

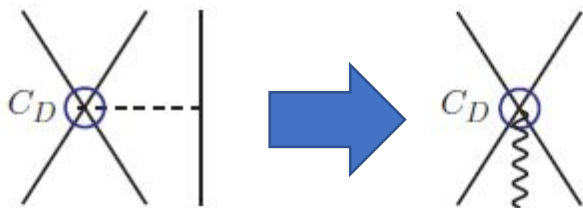
Fit to ^3H beta decay or purely strong data

Many-body correlations important

Two-body can be ~few % to several %



Three-body LECs and sub-leading contact



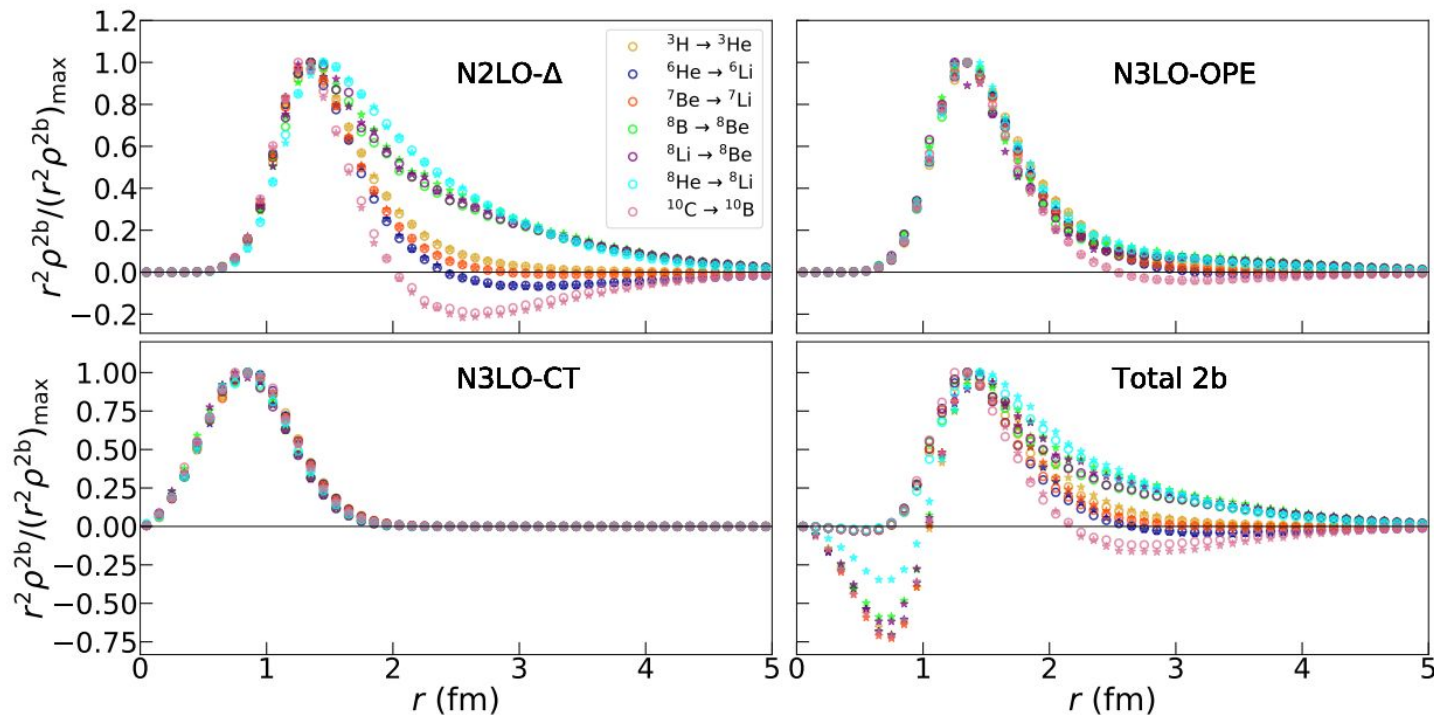
$$\mathbf{j}_{5,a}^{\text{N}^3\text{LO}}(\mathbf{q}; \text{CT}) = z_0 \mathcal{O}_{ij}(\mathbf{q})$$

$$z_0 \propto (c_D + \text{known LECs})$$

Specific parameter in the **three-nucleon force** is **connected to** a parameter in the **two-body weak transition operator**

Short-range dynamics will depend on these values, influenced by fit

Universal behavior in GT densities



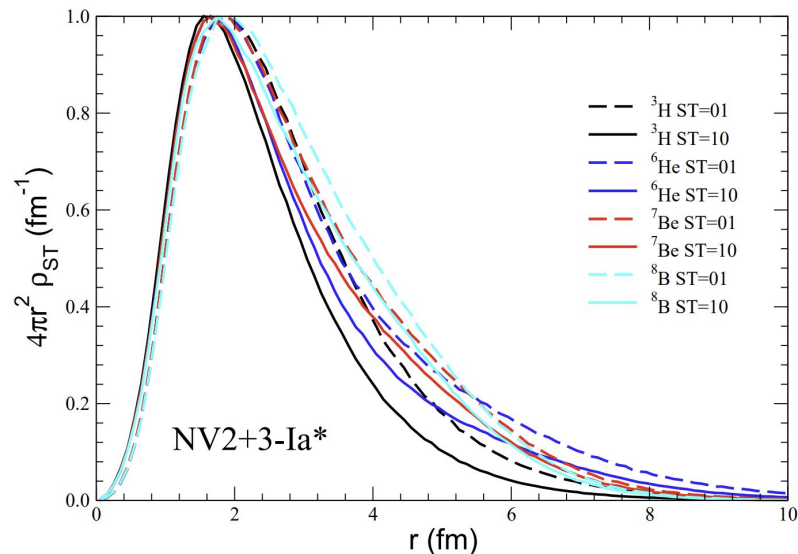
Interpreting universal and tail behaviors

Decay takes nn/np (ST=01/10) pair
to an np/pp (ST=10/01) pair

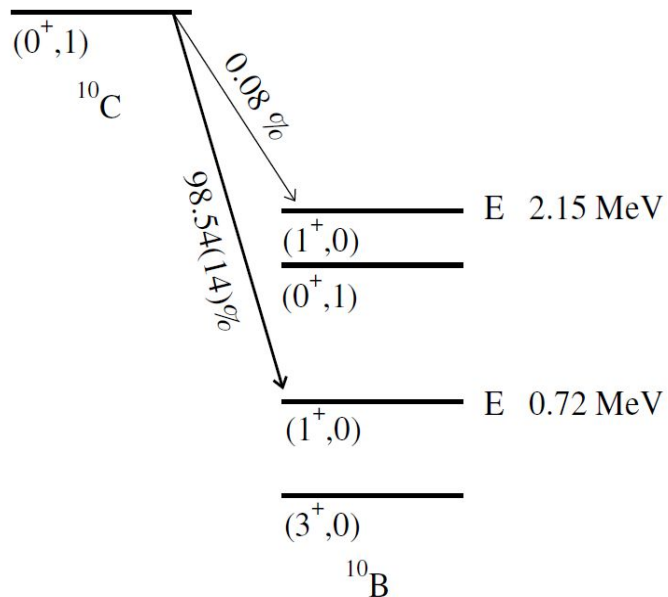
The ST=01 and 10 pair densities at
short distances scale

Consequence of how pairs form in
the nucleus

$$N_{ST} = \int dr_{ij} 4\pi r_{ij}^2 \rho_M^{2b}(r_{ij})$$



^{10}B β -decay



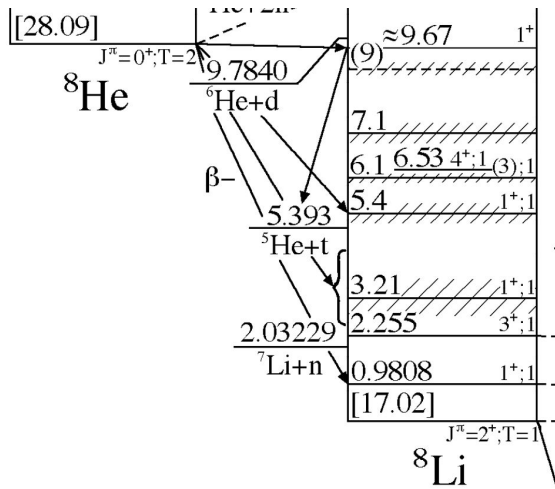
Two states of the same quantum numbers nearby

The result depends strongly on the LS mixing of the p -shell

Particularly sensitive to the 3S_1 and 3D_1 mixing because S to S produces a larger m.e. and ^{10}C is predominantly S wave

<https://nuclldata.tunl.duke.edu/>

^8He β -decay



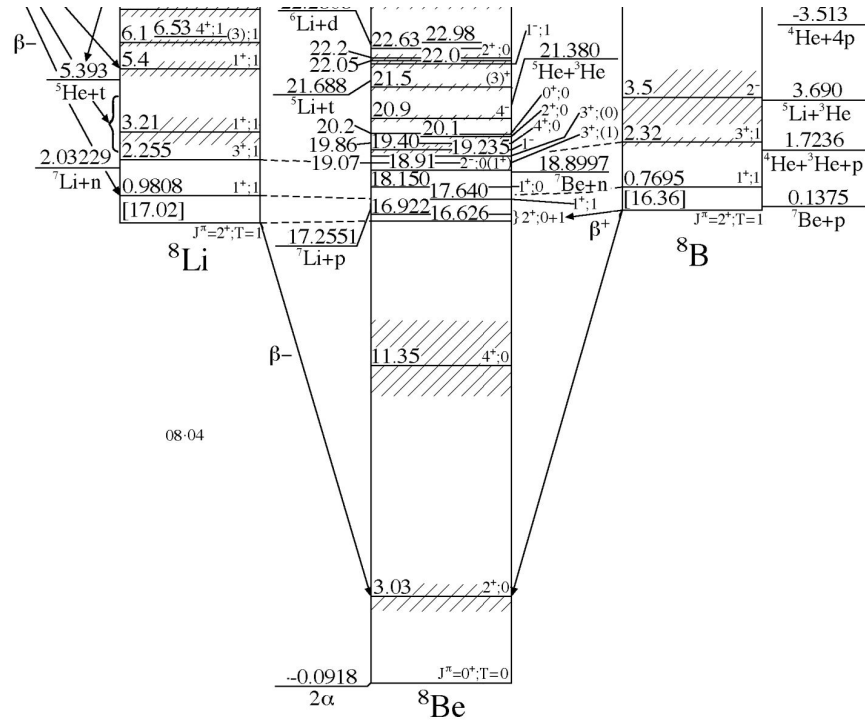
Three $(1^+; 1)$ states within a few MeV

Different dominant spatial symmetries \rightarrow sensitivity to the precise mixing of small components in the wave function

Improving the mixing of the small components in the $(1^+; 1)$ states is crucial to getting an improved m.e.

<https://nucldata.tunl.duke.edu/>

A=8 level scheme



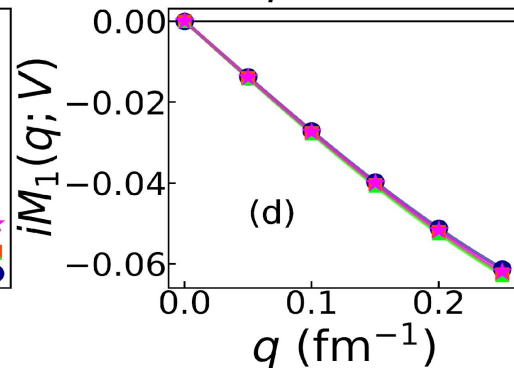
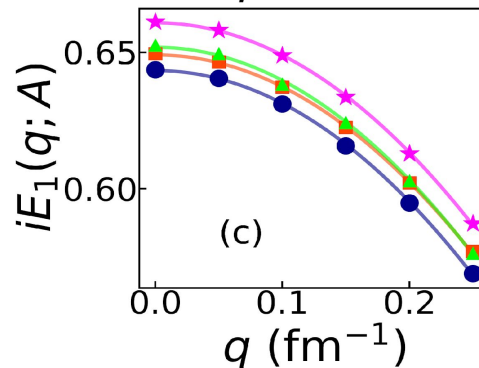
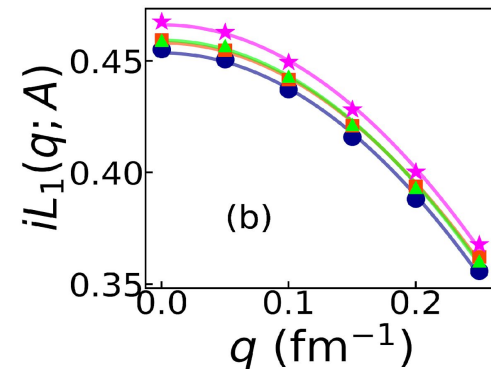
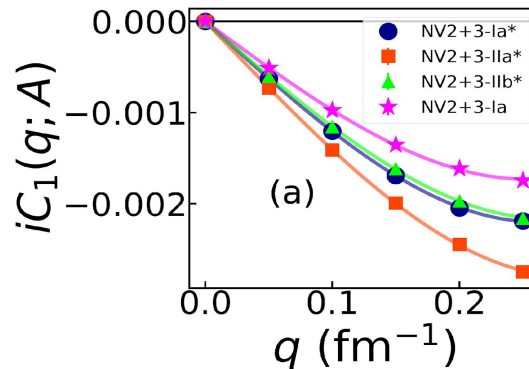
${}^6\text{He}$ β -decay spectrum: Multipoles

$$C_1(q; A) = \frac{i}{\sqrt{4\pi}} \langle {}^6\text{Li}, 10 | \rho_+^\dagger(q\hat{\mathbf{z}}; A) | {}^6\text{He}, 00 \rangle$$

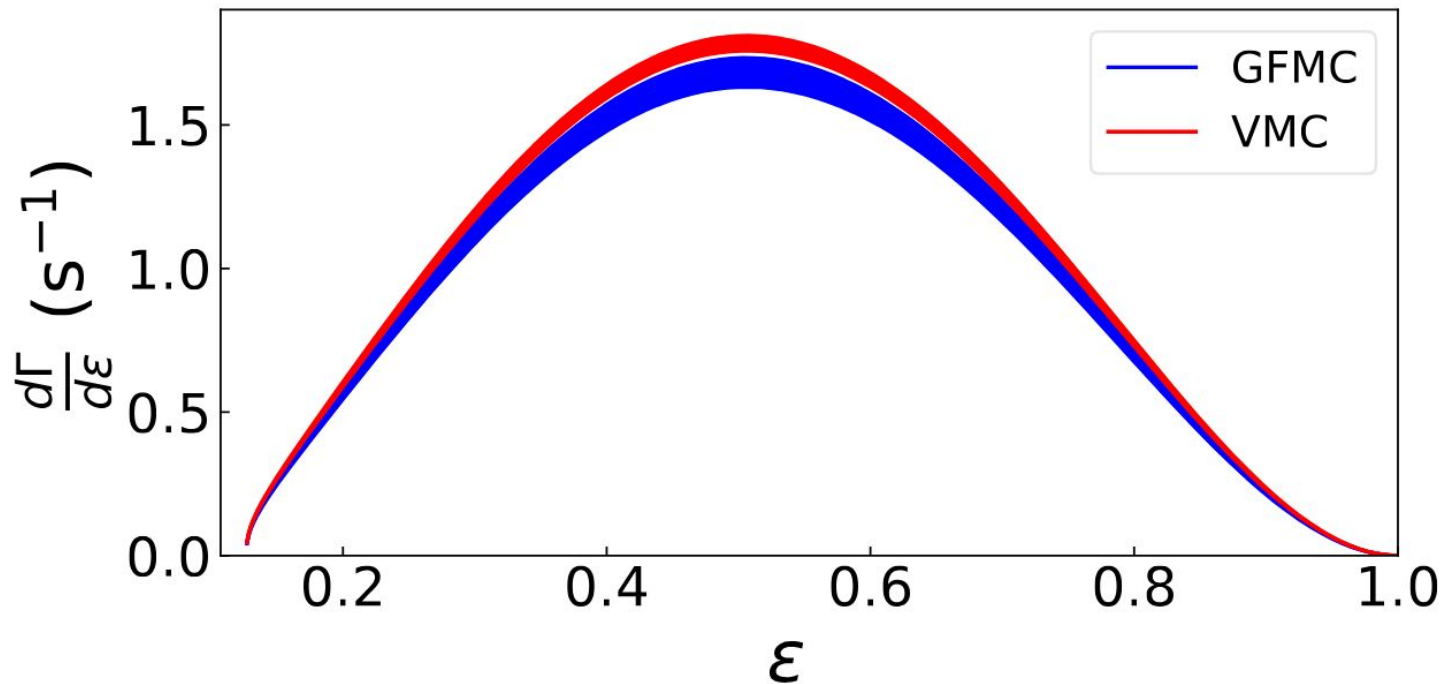
$$L_1(q; A) = \frac{i}{\sqrt{4\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{z}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{z}}; A) | {}^6\text{He}, 00 \rangle$$

$$E_1(q; A) = -\frac{i}{\sqrt{2\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{z}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{x}}; A) | {}^6\text{He}, 00 \rangle$$

$$M_1(q; V) = -\frac{1}{\sqrt{2\pi}} \langle {}^6\text{Li}, 10 | \hat{\mathbf{y}} \cdot \mathbf{j}_+^\dagger(q\hat{\mathbf{x}}; V) | {}^6\text{He}, 00 \rangle$$



${}^6\text{He}$ β -decay spectrum: Absolute spectrum



${}^6\text{He}$ β -decay spectrum: SM corrections

