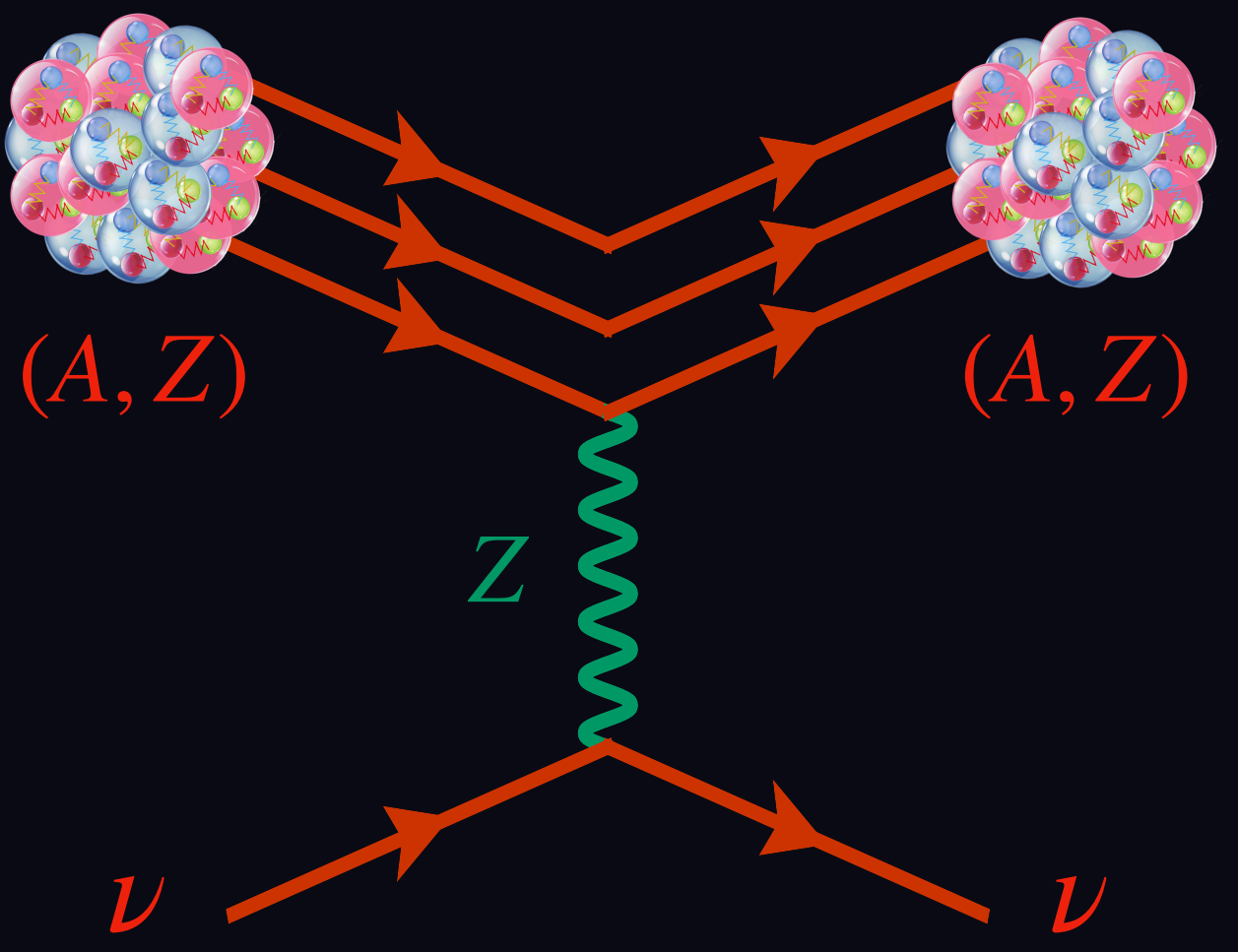
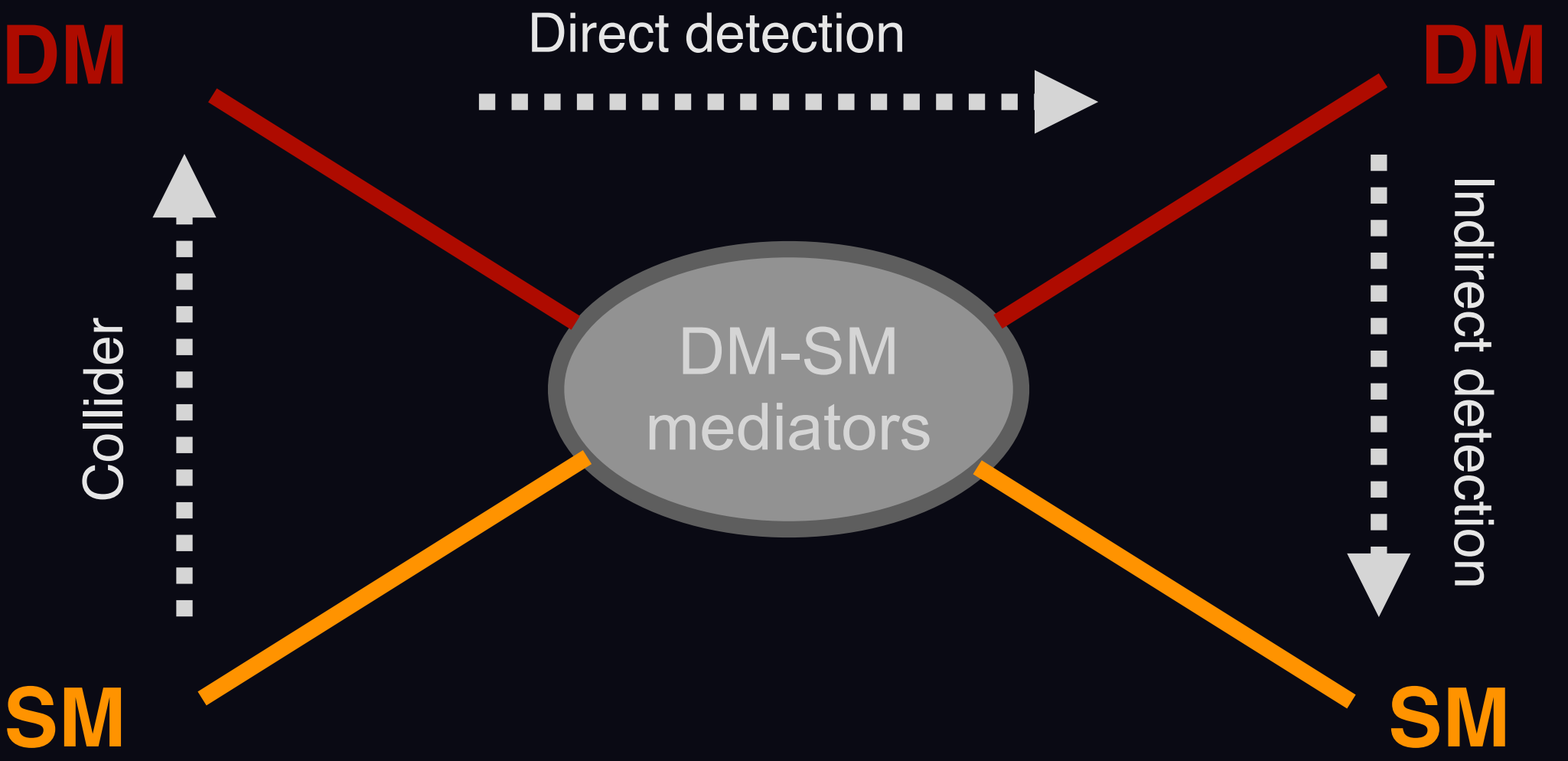
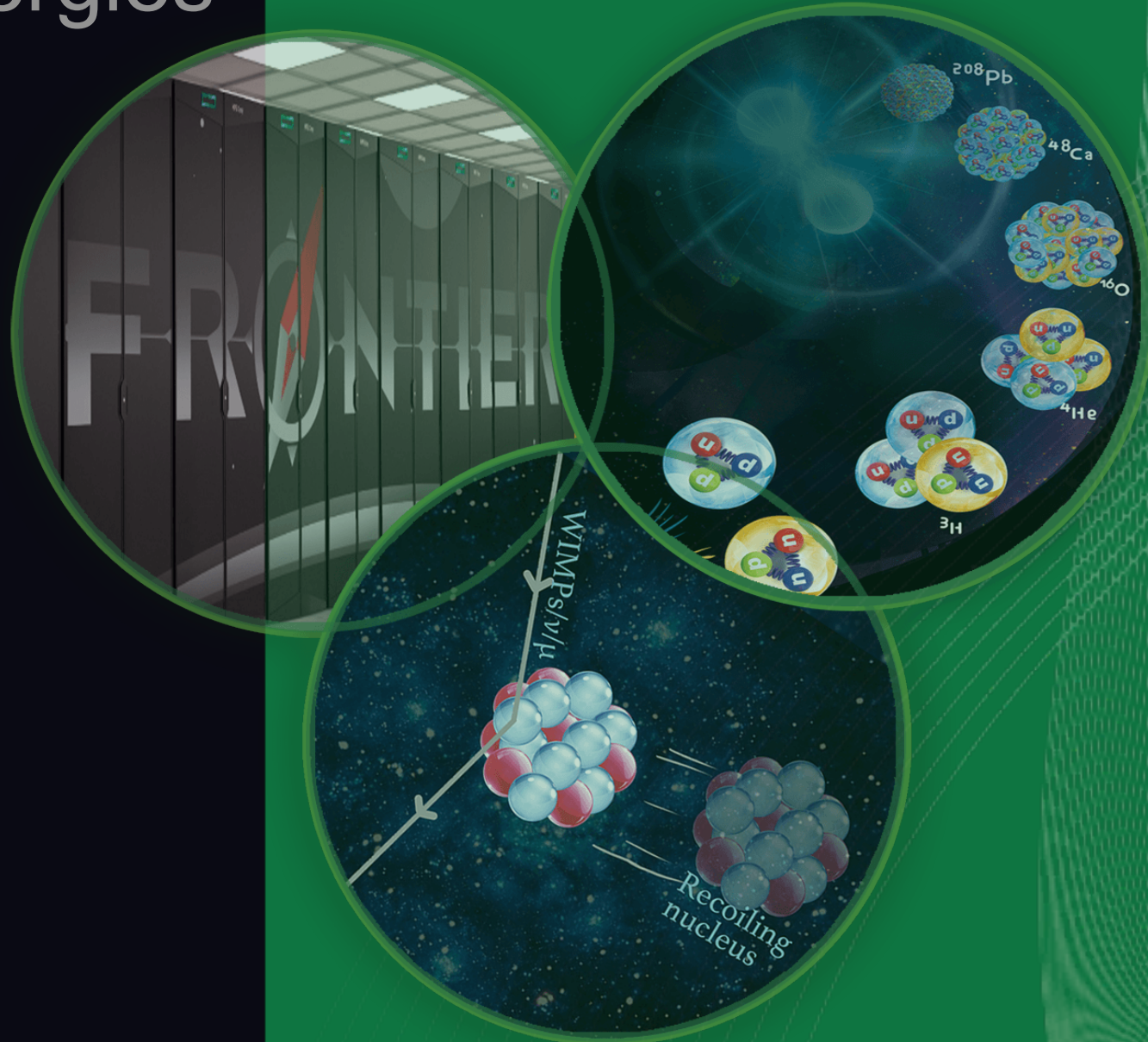


# Ab initio Nuclear Calculations for Dark Matter Detection and CEvNS

Bai-Shan Hu (胡柏山)

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April 17, 2023 @ Seattle

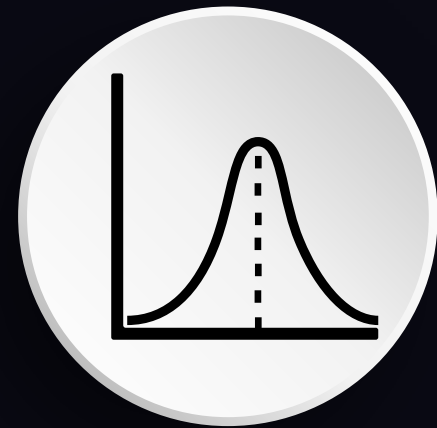




# Outline



**Theoretical steps for WIMP/ $\nu$  scattering off nuclei**



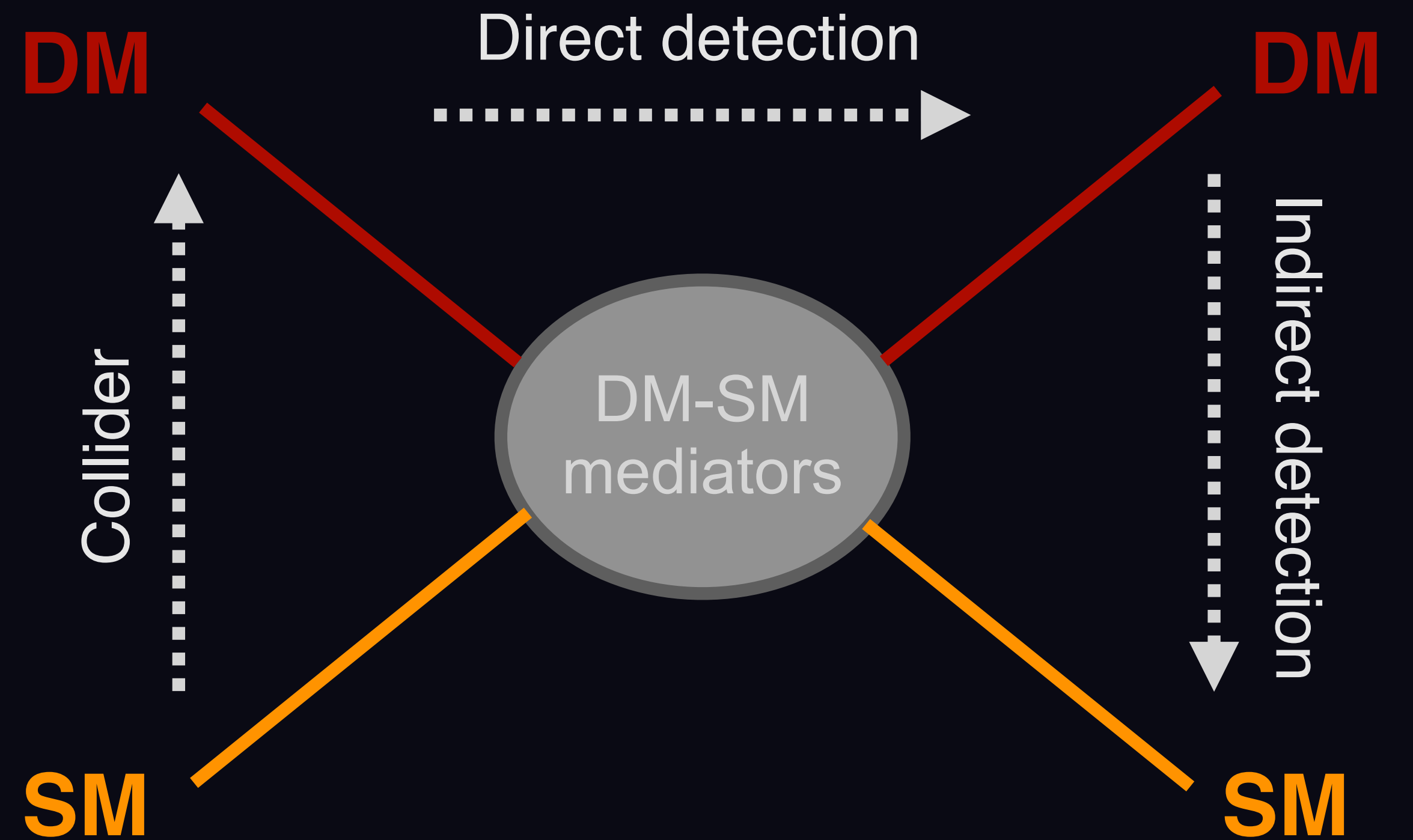
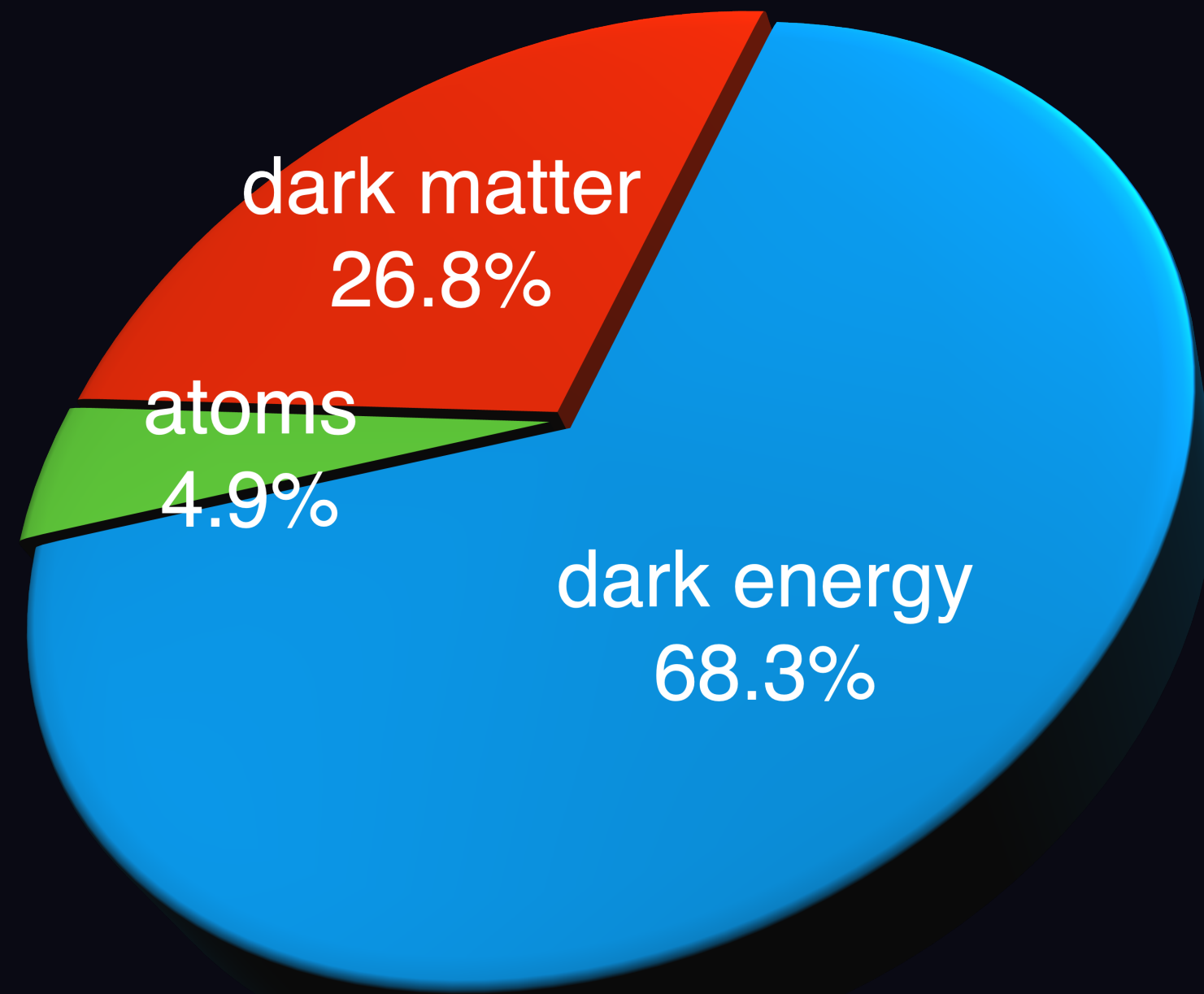
**VS-IMSRG calculations for elastic spin-dependent WIMP scattering and CE $\nu$ NS (Chiral EFT: 1b + 2b currents)**



**Outlook: Spin-independent WIMP scattering;  
Inelastic**



# How to search for DM?



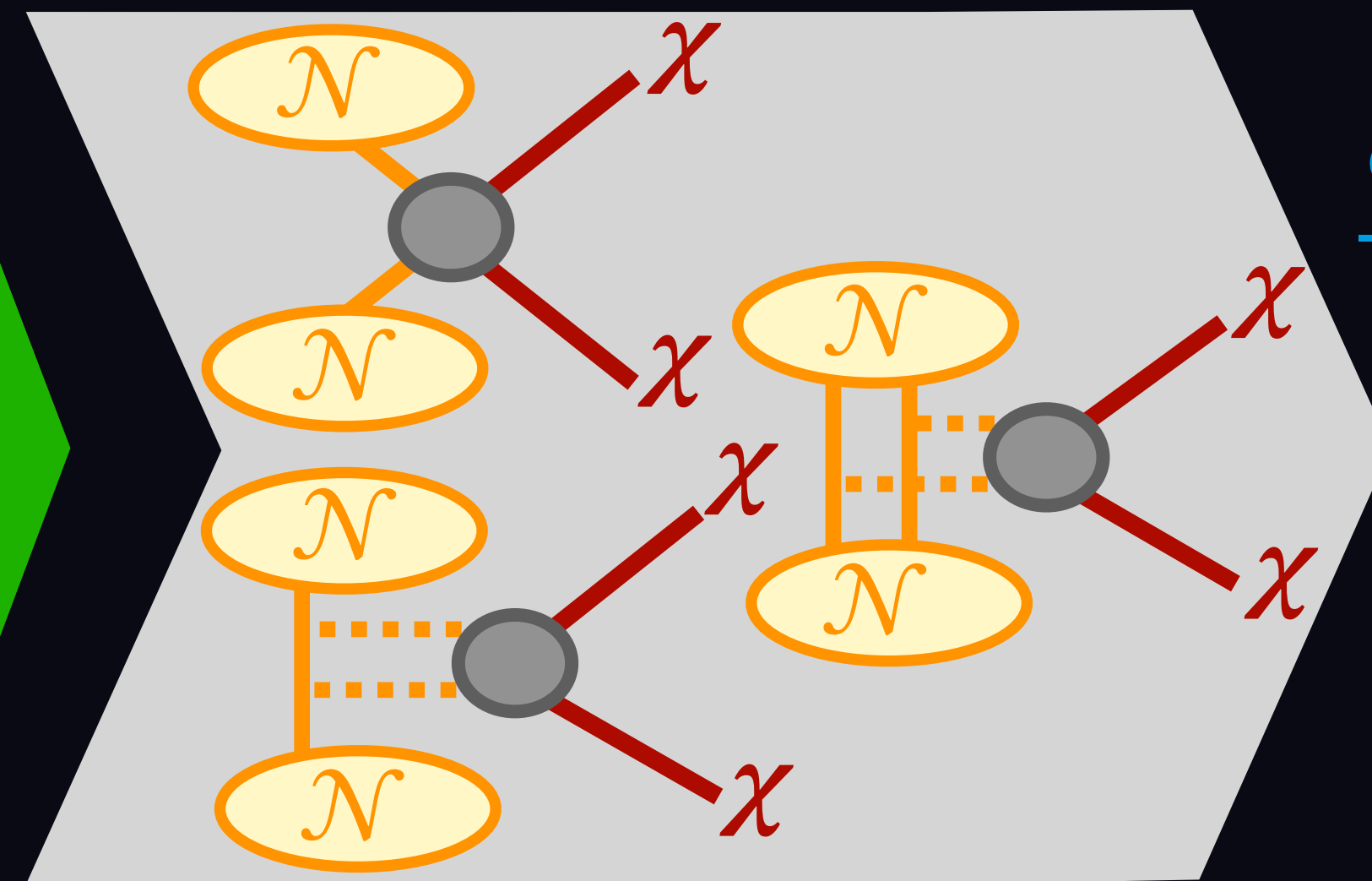
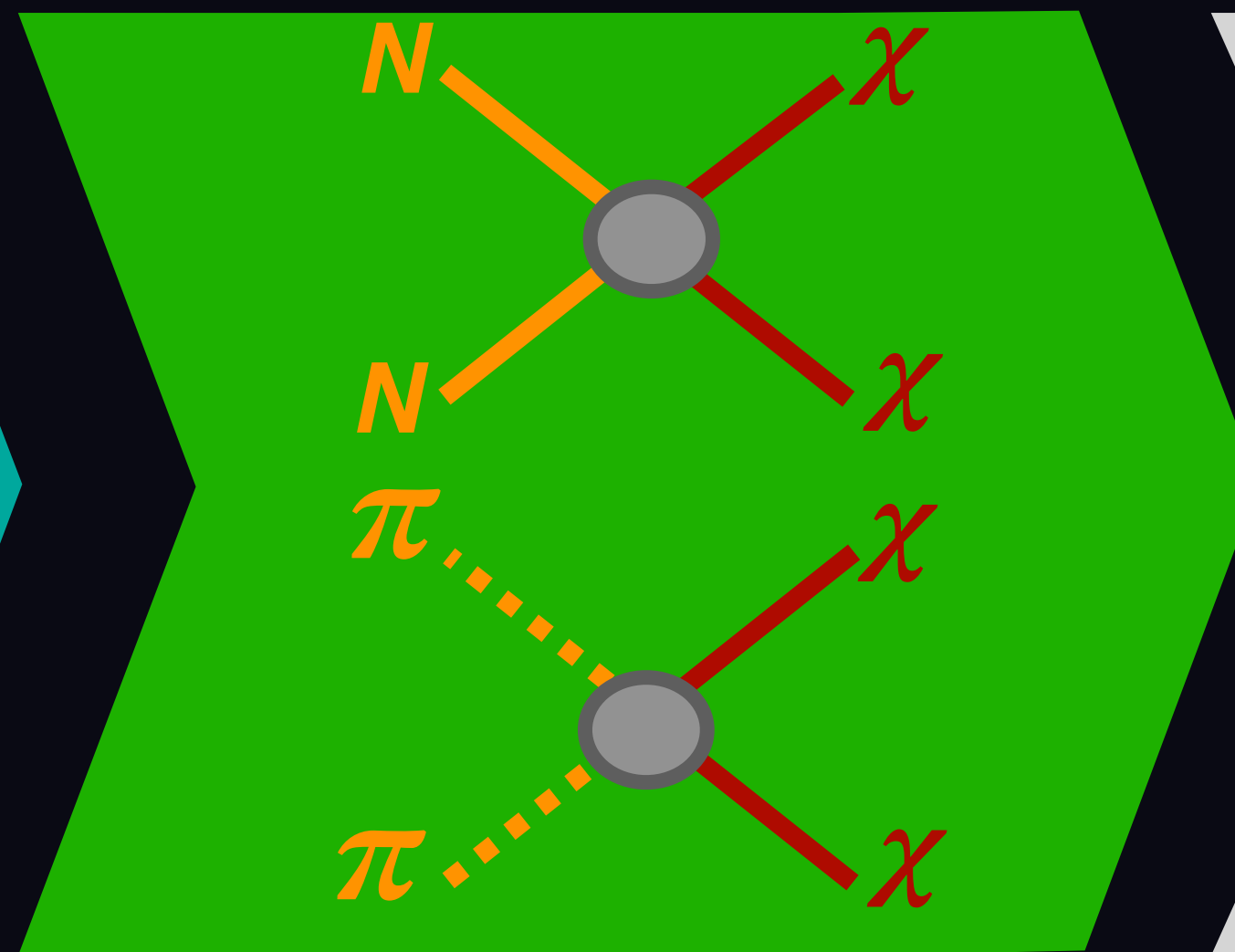
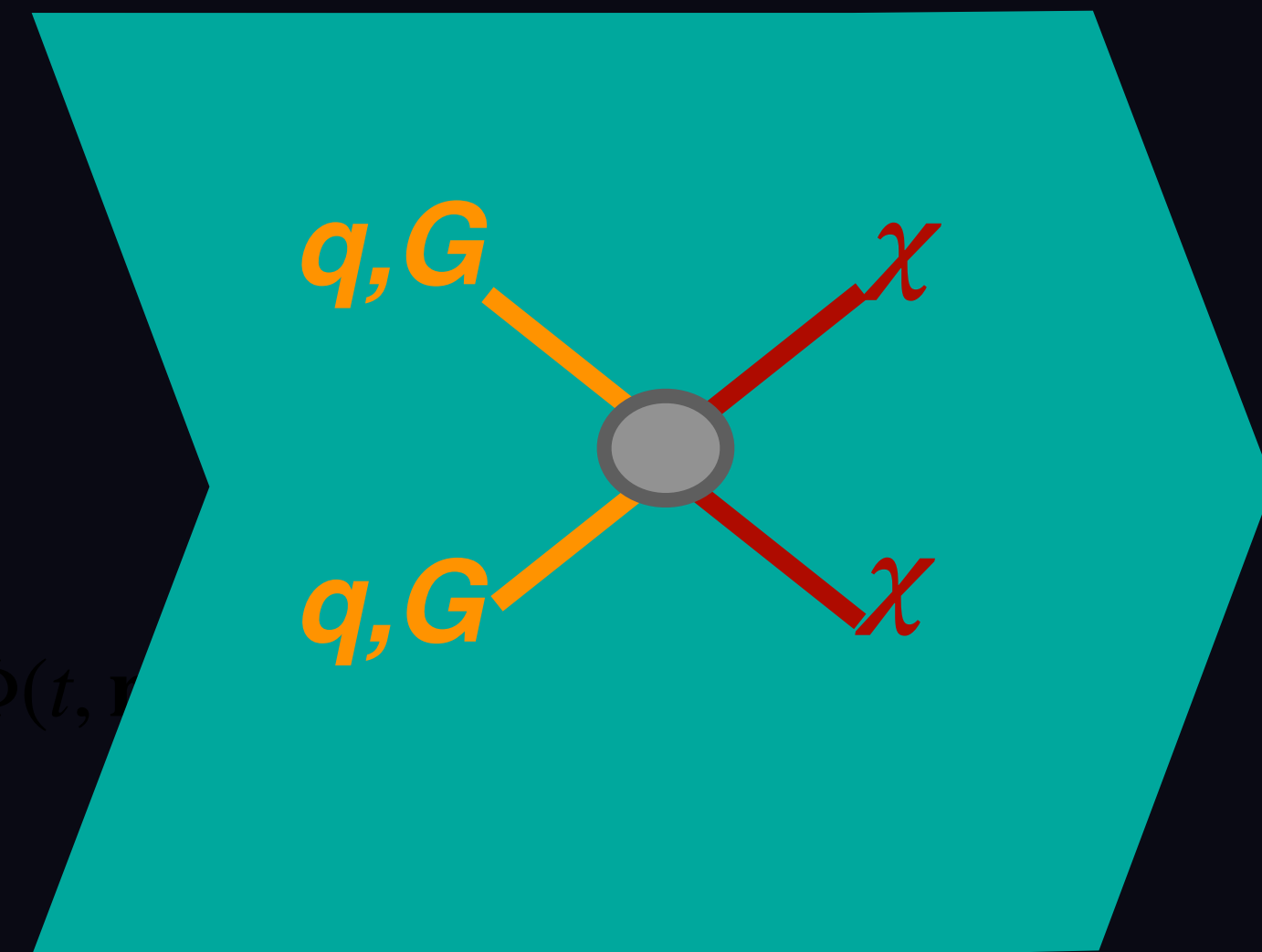
## WIMP $\chi$ scattering elastically off nucleus $\mathcal{N}$

$$\mathcal{N}(p) + \chi(k) \rightarrow \mathcal{N}(p') + \chi(k') \quad \frac{dR}{dE_r} = \underbrace{MT\rho_0 \int_{v_{\min}}^{v_{\text{esc}}} \frac{f(v)}{v} d^3v}_{\text{astrophysics}} \times \underbrace{\frac{\sigma_{\chi N}^{SD/SI}}{m_\chi \mu_N^2}}_{\text{particle+hadronic physics}} \times \underbrace{\left| \mathcal{F}^{SD/SI}(\mathbf{q}^2) \right|^2}_{\text{nuclear physics } \langle \mathcal{N} | H_{\chi A} | \mathcal{N} \rangle}$$

$$q = k' - k = p - p', \quad q^2 = t$$



# Calculation for direct detection of dark matter



$$\frac{d\sigma_{\chi\mathcal{N}}}{dq^2} = \frac{m_N}{2v^2\mu^2} \times \left[ \sigma_{SI} \mathcal{F}_{SI}^2(\mathbf{q}^2) + \sigma_{SD} \mathcal{F}_{SD}^2(\mathbf{q}^2) \right]$$

Effective Lagrangian  $\mathcal{L}_\chi$   
DoF: quarks and gluons

## Hadronic scale

- **Chiral EFT**  
DoF: nucleons and pions  
meson-exchange currents

- **NREFT**  
DoF: nucleons

$$H_{\chi A} = \sum_{i=1}^A \sum_{\tau=0,1} \sum_j c_j^\tau \hat{O}_j^{(i)} t_{(i)}^\tau$$

## Nuclear scale

DoF: nucleons (p and n)  
nuclear wavefunction  $\langle \mathcal{N} | H_{\chi A} | \mathcal{N} \rangle$

- **Shell model**  
commonly used  
not all nucleons active  
no consistent effective operator  
no consistent LECs with nuclear force

- **Ab initio method**

# This talk will focus on spin-dependent case

$$\mathcal{L}_\chi^{\text{SD}} = -\frac{G_F}{\sqrt{2}} \int d^3\mathbf{r} \bar{\chi} \gamma \gamma_5 \chi \cdot \sum_q C_q^{AA} \bar{q} \gamma \gamma_5 q$$

one-nucleon level

isoscalar isovector

$$\rightarrow \mathbf{J}_{i,1b} = \mathbf{J}_{i,1b}^+ + \mathbf{J}_{i,1b}^-$$

## one-body currents

$$\sum_{i=1}^A \mathbf{J}_{i,1b} = \sum_{i=1}^A \frac{1}{2} \left[ a_+ \sigma_i + a_- \tau_i^3 \left( \frac{g_A(p^2)}{g_A} \sigma_i - \frac{g_P(p^2)}{2mg_A} (\mathbf{p} \cdot \sigma_i) \mathbf{p} \right) \right]$$

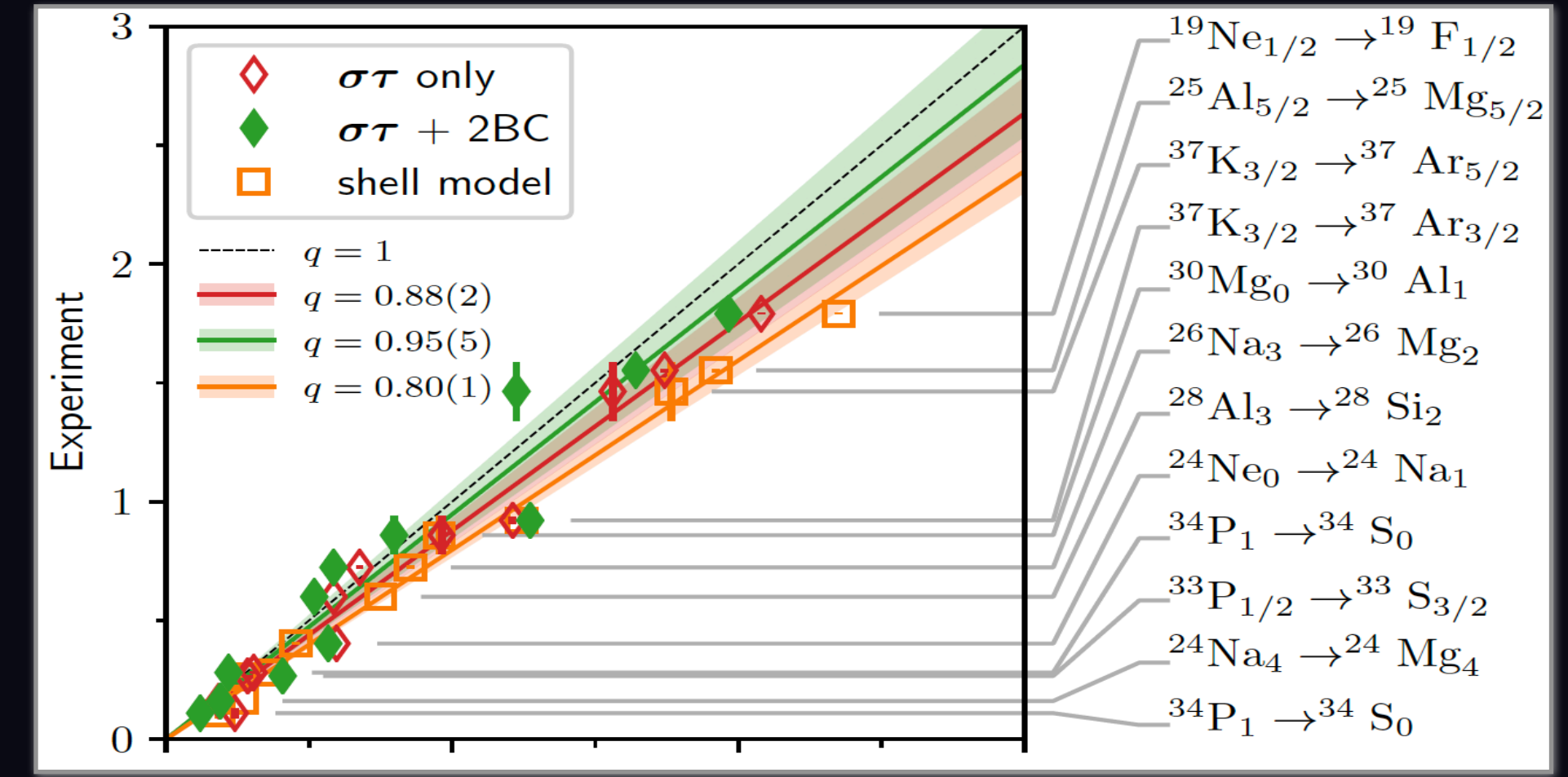
loop corrections
pion propagators

## two-body currents

$$\mathbf{J}_{2b}^- = -\frac{g_A}{2F_\pi^2} [\tau_1 \times \tau_2]^3 \left[ c_4 \left( 1 - \frac{\mathbf{q}}{q^2 + M_\pi^2} \mathbf{q} \cdot \right) (\sigma_1 \times \mathbf{k}_2) + \frac{c_6}{4} (\sigma_1 \times \mathbf{q}) + i \frac{\mathbf{p}_1 + \mathbf{p}'_1}{4m_N} \frac{\sigma_2 \cdot \mathbf{k}_2}{M_\pi^2 + k_2^2} \right]$$

$$-\frac{g_A}{F_\pi^2} \tau_2^3 \left[ c_3 \left( 1 - \frac{\mathbf{q}}{q^2 + M_\pi^2} \mathbf{q} \cdot \right) \mathbf{k}_2 + 2c_1 M_\pi^2 \frac{\mathbf{q}}{q^2 + M_\pi^2} \right] \frac{\sigma_2 \cdot \mathbf{k}_2}{M_\pi^2 + k_2^2}$$

$$-d_1 \tau_1^3 \left( 1 - \frac{\mathbf{q}}{q^2 + M_\pi^2} \mathbf{q} \cdot \right) \sigma_1 + (1 \leftrightarrow 2) - d_2 (\tau_1 \times \tau_2)^3 (\sigma_1 \times \sigma_2) \left( 1 - \frac{\mathbf{q}}{q^2 + M_\pi^2} \mathbf{q} \cdot \right)$$



P Gysbers, et al., Nat. Phys. 15 (2019) 428



**include as density-dependent one-body currents (normal ordering)**

Details:

P. Klos, et al., PRD 88 (2013) 083516;

89 (2014) 029901(E)

M. Hoferichter et al., PRD 102 (2020) 074018

# Structure factors required from nuclear many-body theory

$$\frac{d\sigma_{\chi\mathcal{N}}}{dq^2} = \frac{\zeta^2}{(2J_i + 1) \pi v^2} \sum_{s_f, s_i} \sum_{M_f, M_i} \left| \langle \mathcal{N}_f | \mathcal{L}_\chi^{\text{SD}} | \mathcal{N}_i \rangle \right|^2 = \frac{8G_F^2 \zeta^2}{v^2 (2J_i + 1)} S_A(\mathbf{q}^2)$$

- decompose into longitudinal, transverse electric and transverse magnetic

$$S_A(\mathbf{q}^2) = \sum_{L \geq 0} \left| \langle J_f \parallel \mathcal{L}_L^5 \parallel J_i \rangle \right|^2 + \sum_{L \geq 1} \left( \left| \langle J_f \parallel \mathcal{T}_L^{\text{el}5} \parallel J_i \rangle \right|^2 + \left| \langle J_f \parallel \mathcal{T}_L^{\text{mag}5} \parallel J_i \rangle \right|^2 \right)$$

$$S_A(q) = a_+^2 S_{00}(q) + a_+ a_- S_{01}(q) + a_-^2 S_{11}(q)$$

- $q \rightarrow 0$ , with proton/neutron spin expectation values  $\langle \hat{S}_{p/n} \rangle$

$$S_A(0) = \frac{(2J+1)(J+1)}{4\pi J} \left[ \overbrace{(a_+ + a_-)}^{a_+ + a_- \times (2b \text{ currents effects})} \langle \hat{S}_p \rangle + (a_+ - a_-) \langle \hat{S}_n \rangle \right]^2$$

- commonly use the structure factors  $S_p$  and  $S_n$

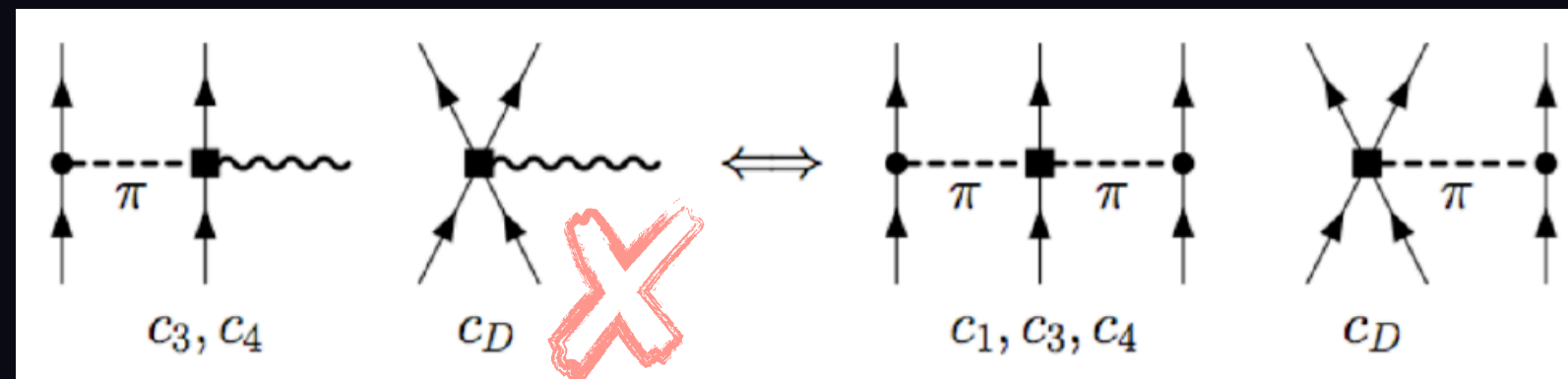
$$\text{proton-only } S_p: \quad a_+ = a_- \quad S_p(q) = S_{00}(q) + S_{01}(q) + S_{11}(q)$$

$$\text{neutron-only } S_n: \quad a_+ = -a_- \quad S_n(q) = S_{00}(q) - S_{01}(q) + S_{11}(q)$$



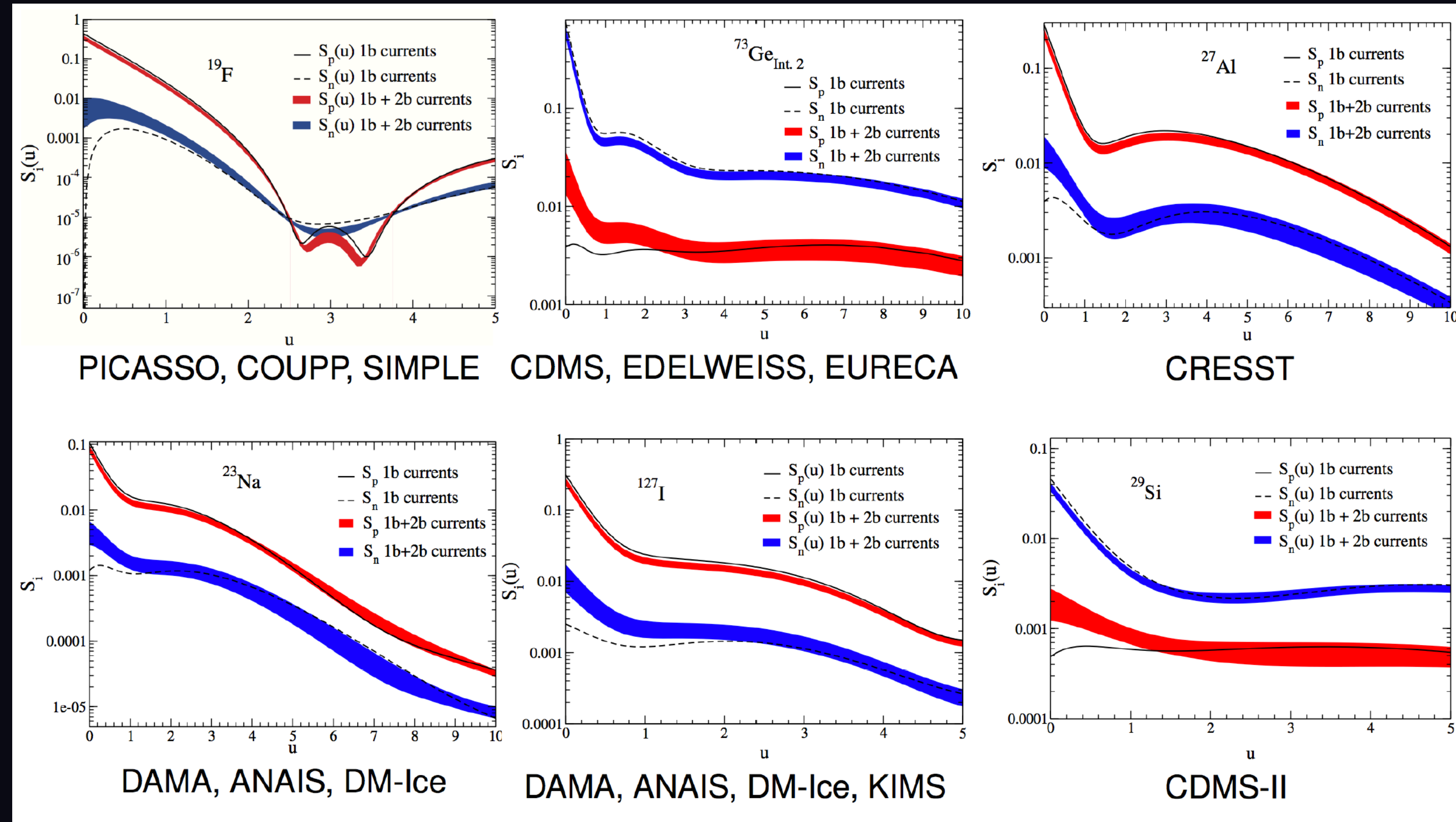
# Spin-dependent WIMP-nucleus response

Standard SM: phenomenological wavefunctions + bare operator  
(with two-body currents of pion exchange)



$$C3 = (-3.2, -2.2, -3.4, -2.4, -4.78, -3.78) \text{ GeV}^{-1}$$

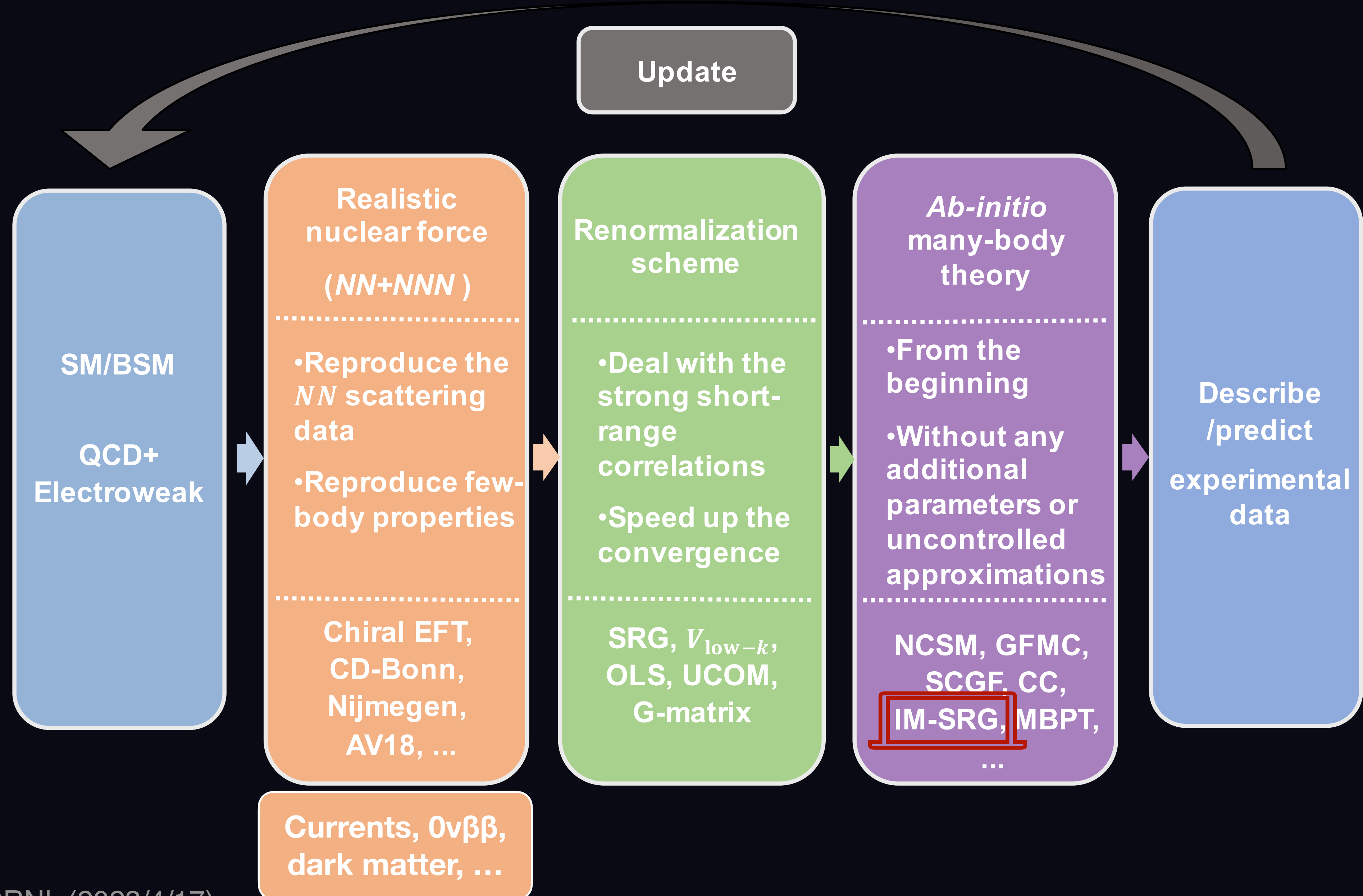
$$C4 = (5.4, 4.4, 3.4, 2.4, 3.96, 2.96) \text{ GeV}^{-1}$$



P. Klos, et al., PRD 88 (2013) 083516



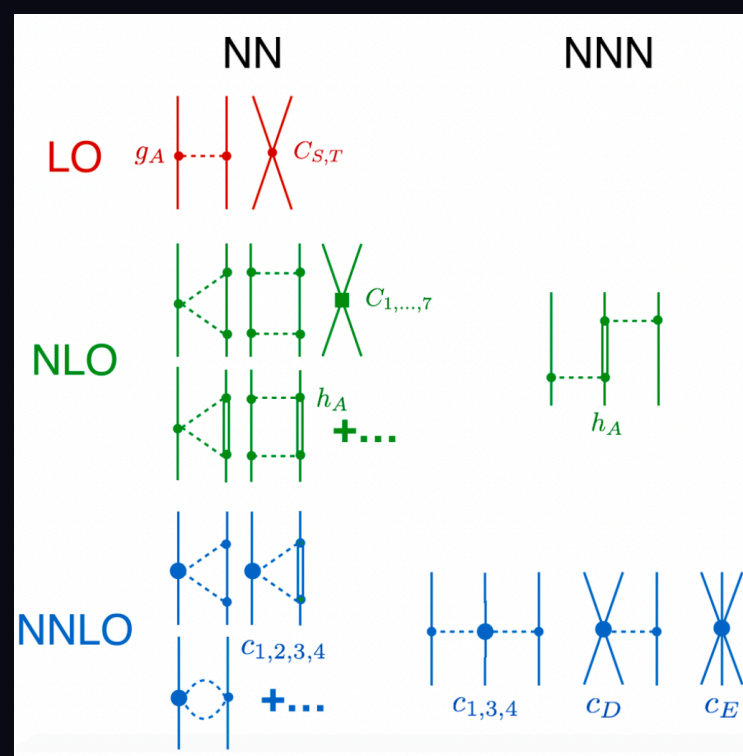
# Workflow of *ab-initio* nuclear calculation





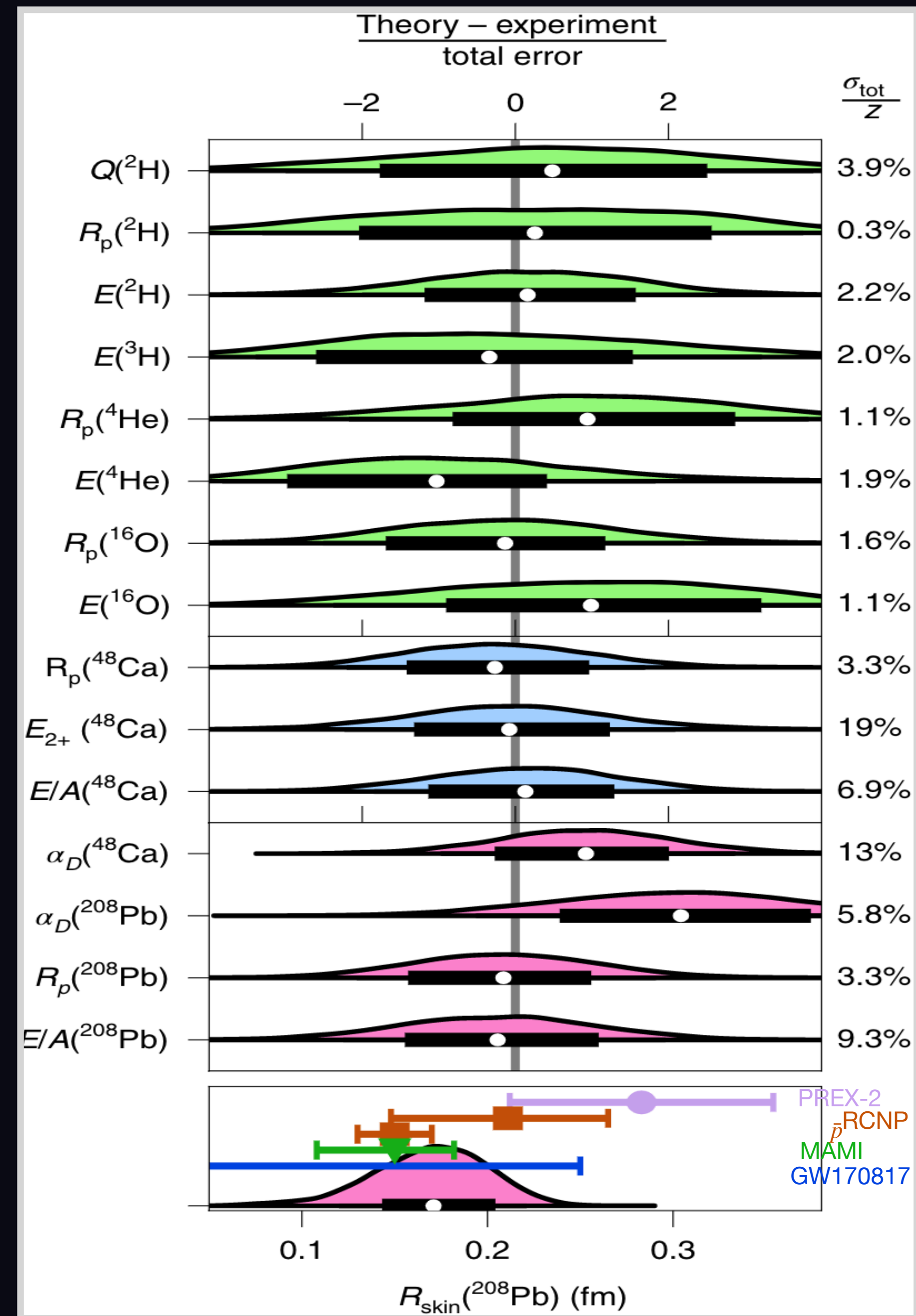
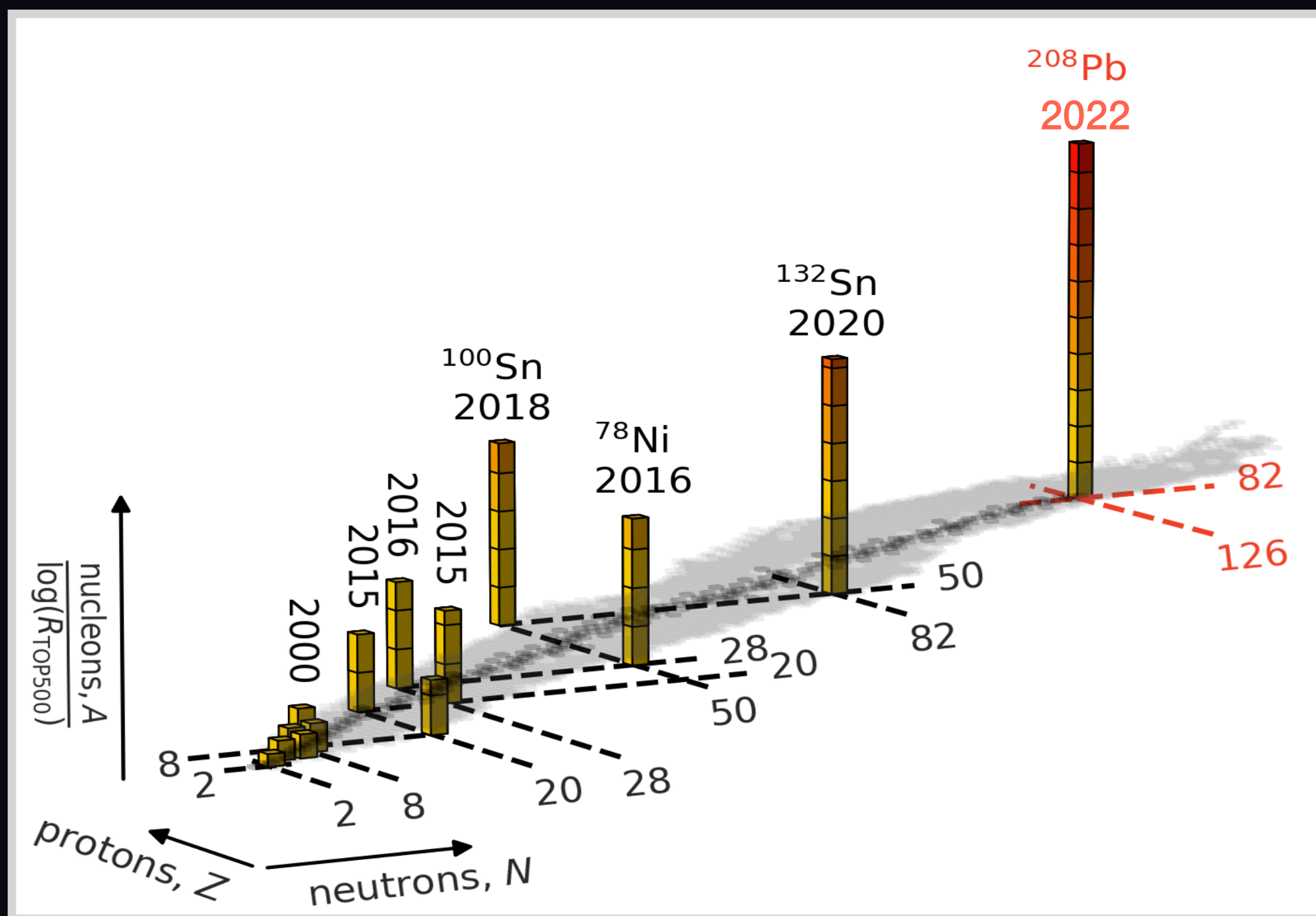
# Ab initio results for $^{208}\text{Pb}$ region

Chiral NN + 3N



History matching  
Emulator technology  
Statistical tools

New 3N storage scheme  
IMSRG, CC, MBPT

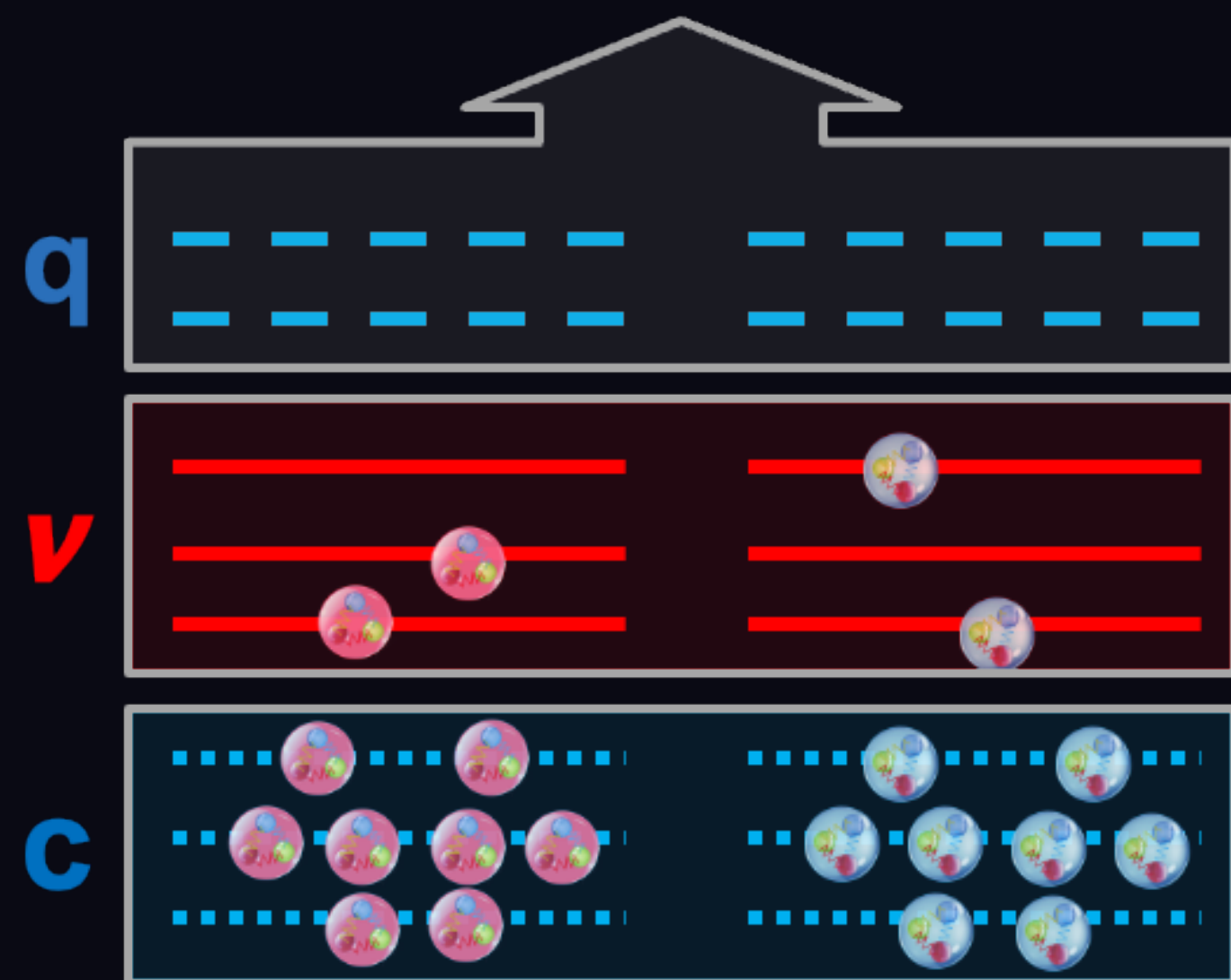


BShu W.G. Jiang, T. Miyagi, Z.H. Sun, et al., Nat. Phys. 18, 1196 (2022)

Baishan Hu - ORNL (2023/4/17)



# Valence-Space In-Medium Similarity Renormalization Group



$$\frac{dH(s)}{ds} = [\eta(s), H(s)]$$

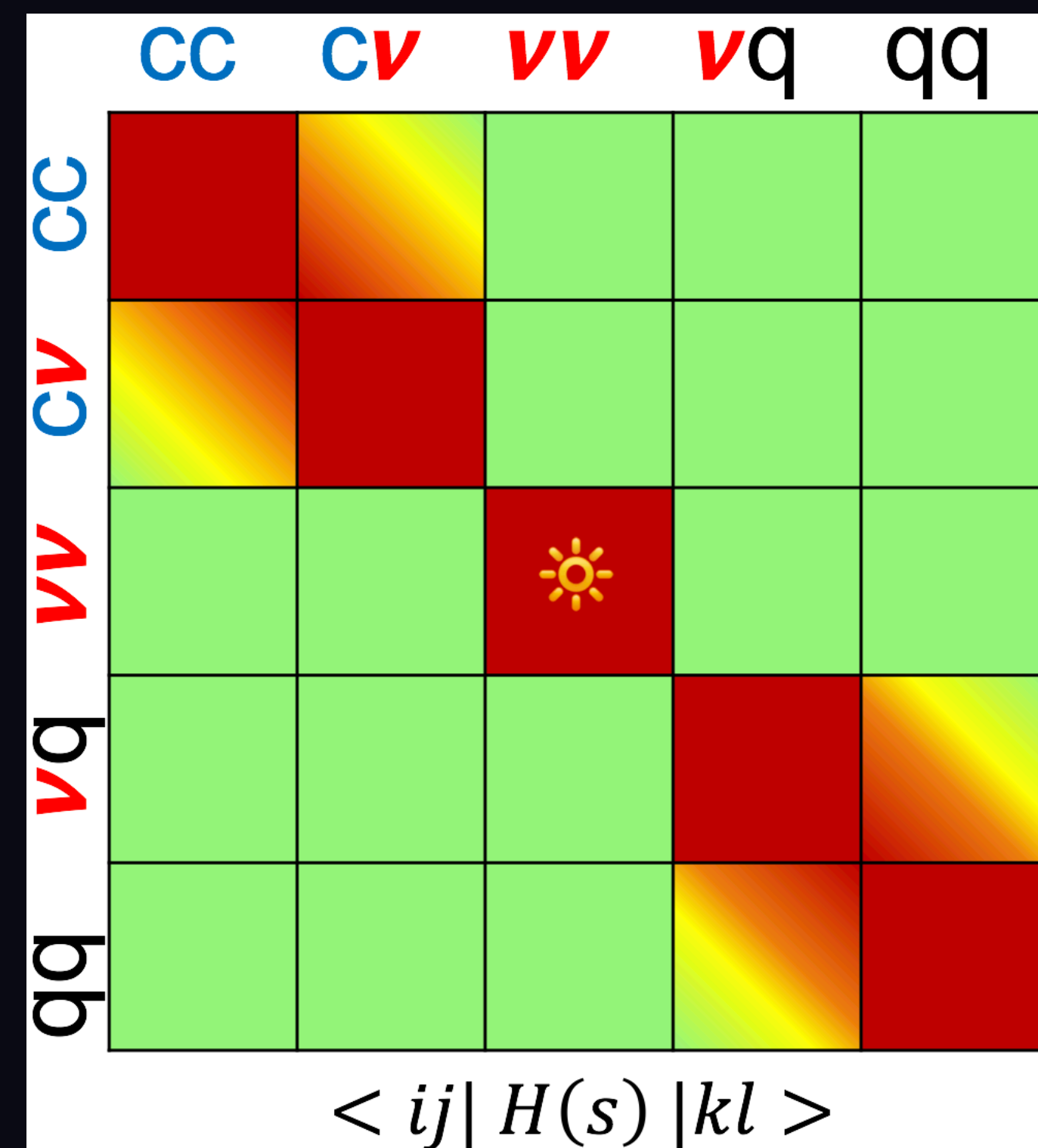
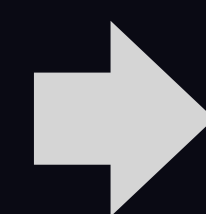
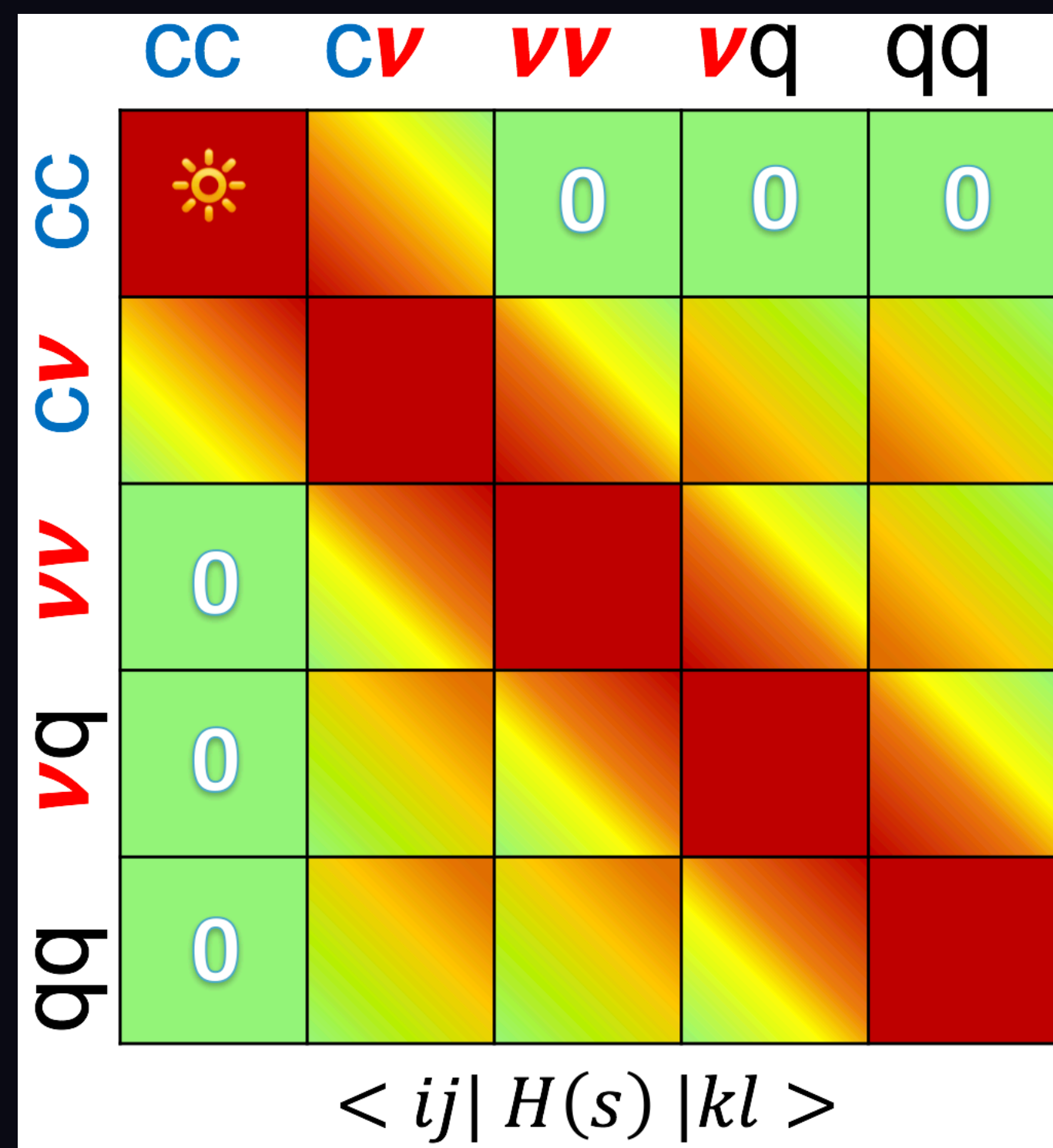
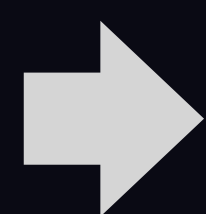
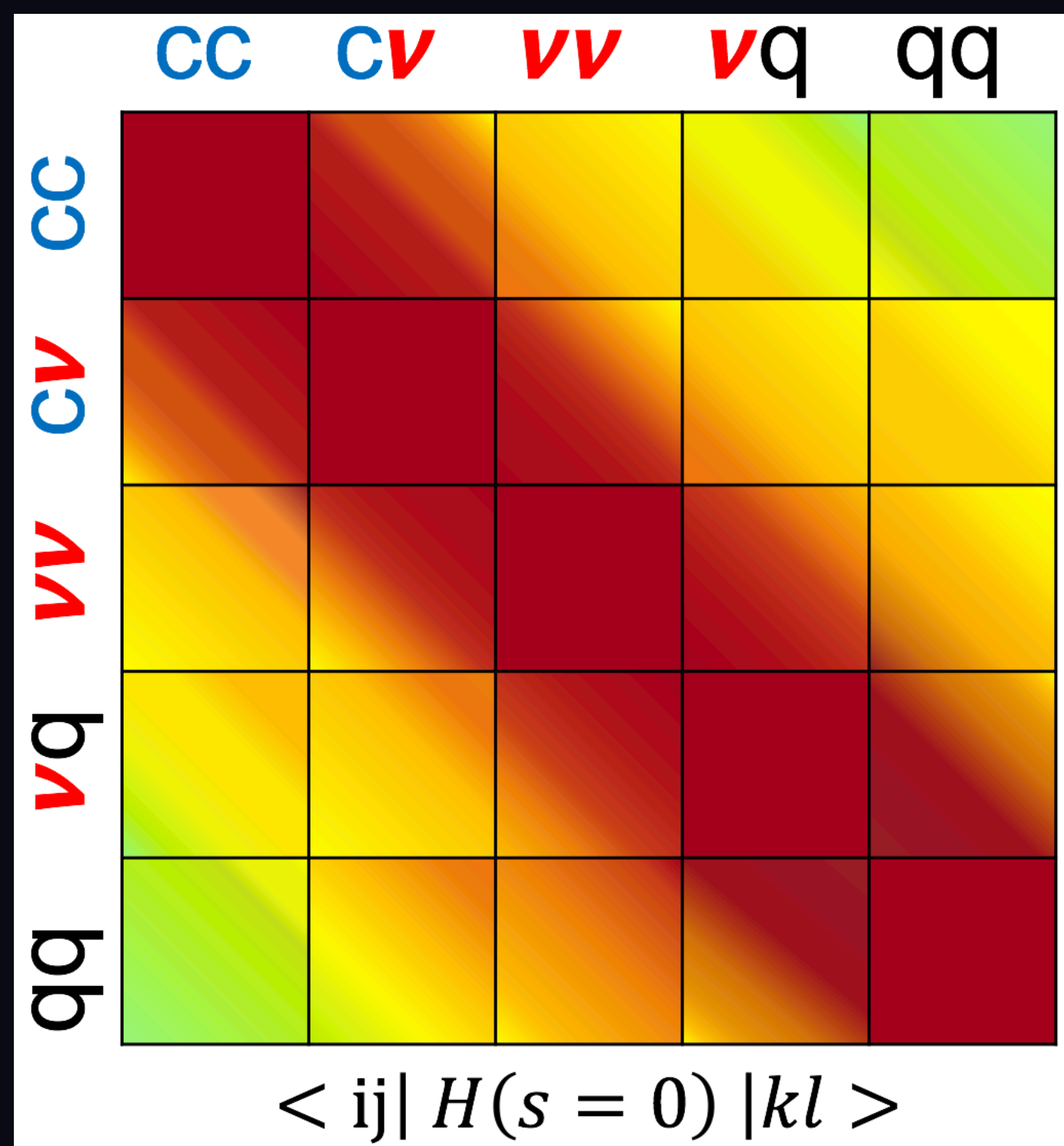
$$H(s) = U(s)H U^{-1}(s) \quad \mathcal{O}(s) = U(s)\mathcal{O}U^{-1}(s)$$

$$\eta(s) = \frac{dU(s)}{s}U^\dagger(s) = -\eta^\dagger(s) \quad U(s) = e^{\Omega(s)}$$

Step1: Decouple core

Step2: Decouple valence space

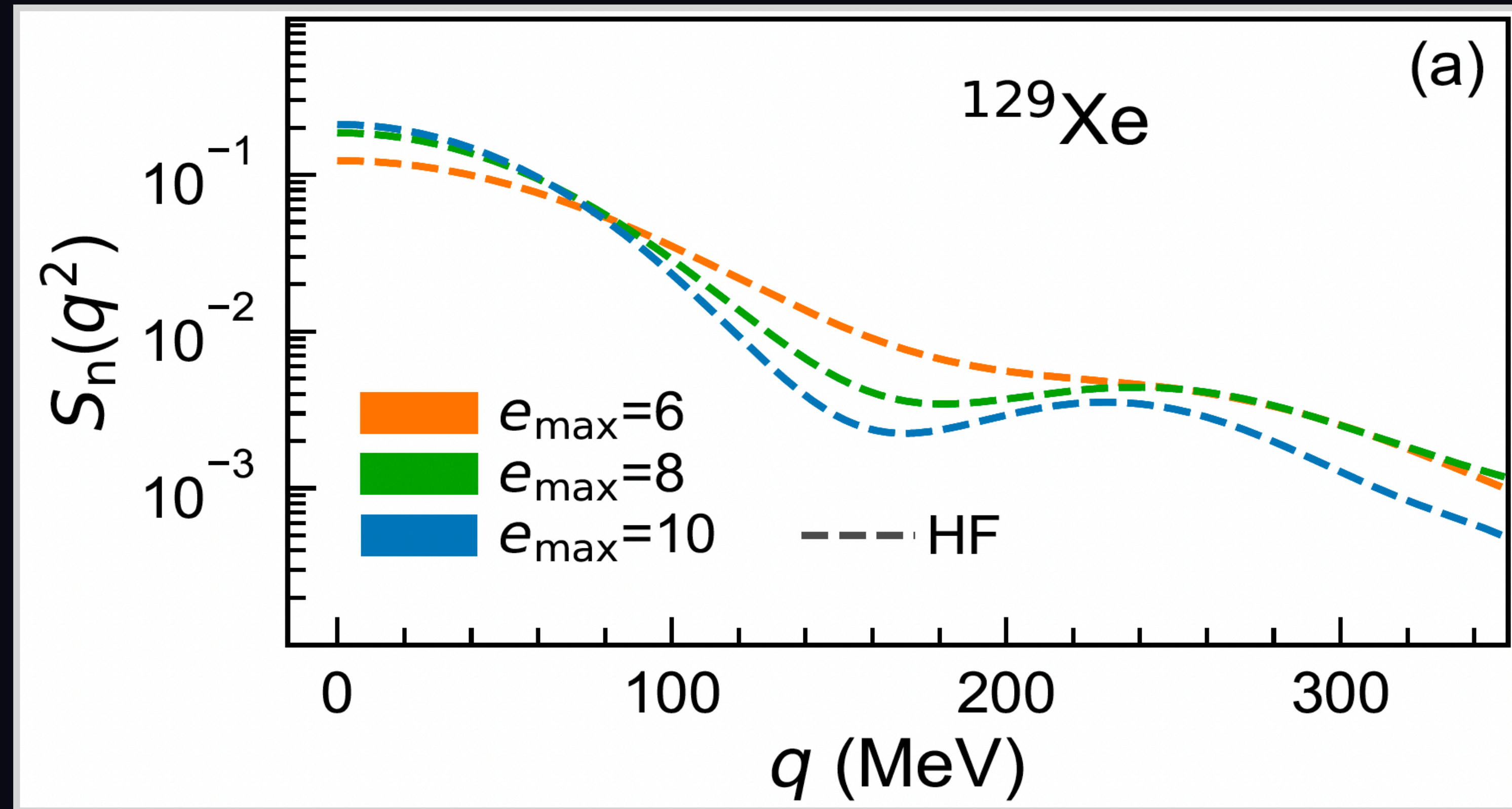
Step3: Decouple additional operators





# Heavy nuclei is challenging current *ab initio* approaches

structure factor for spin-dependent dark matter direct detection  $\mathcal{F}_\tau^{\Sigma'}$ ,  $\mathcal{F}_\tau^{\Sigma''}$



- Tensor operators are very heavy tasks for IMSRG
- Many  $q$  points (operators) need to calculate



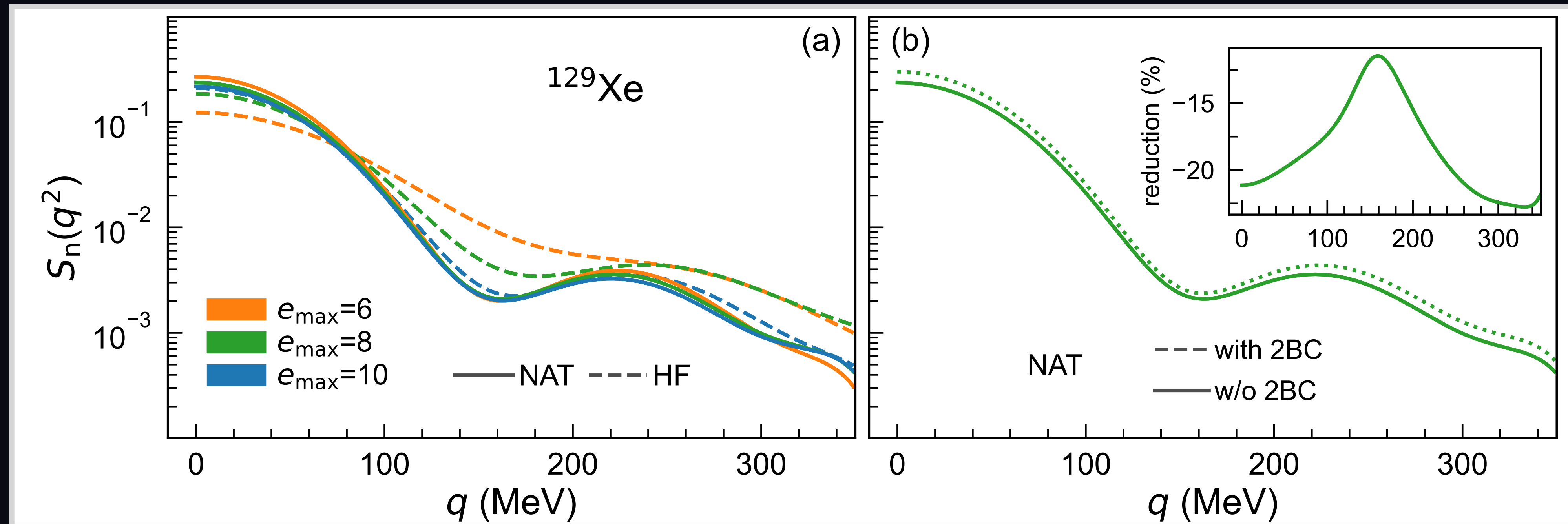
# Heavy nuclei is challenging current *ab-initio* approaches

## Natural orbitals (NAT)

A. Tichai, et al., Phys. Rev. C 99, 034321 (2019)

$$\rho_{pq} = \langle \Psi | c_p^\dagger c_q | \Psi \rangle$$

$$\text{MBPT} \Rightarrow |\Psi\rangle \approx |\Psi^{(0)}\rangle + |\Psi^{(1)}\rangle + |\Psi^{(2)}\rangle$$

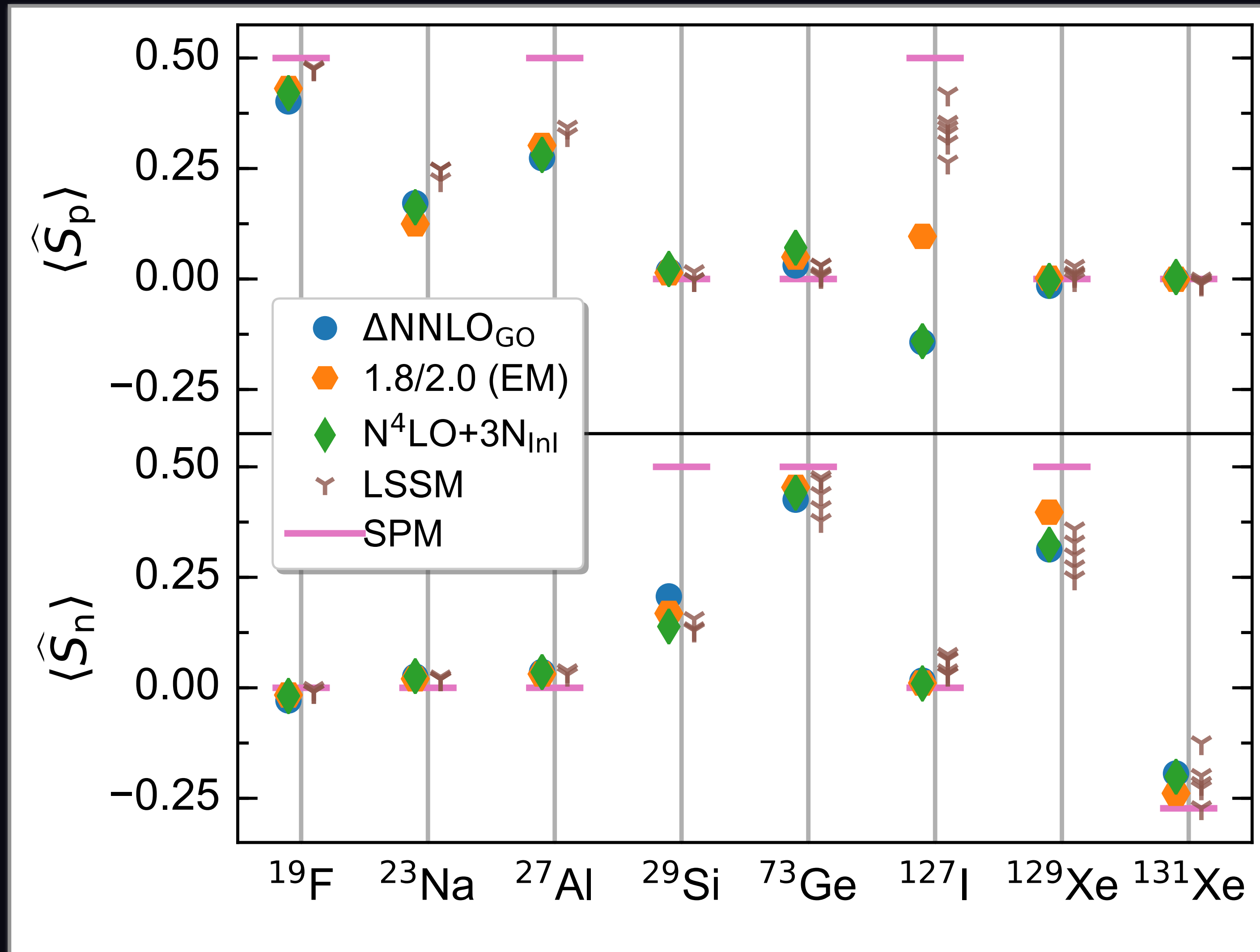


BSH, et al, Phys. Rev. Lett.128, 072502 (2022)

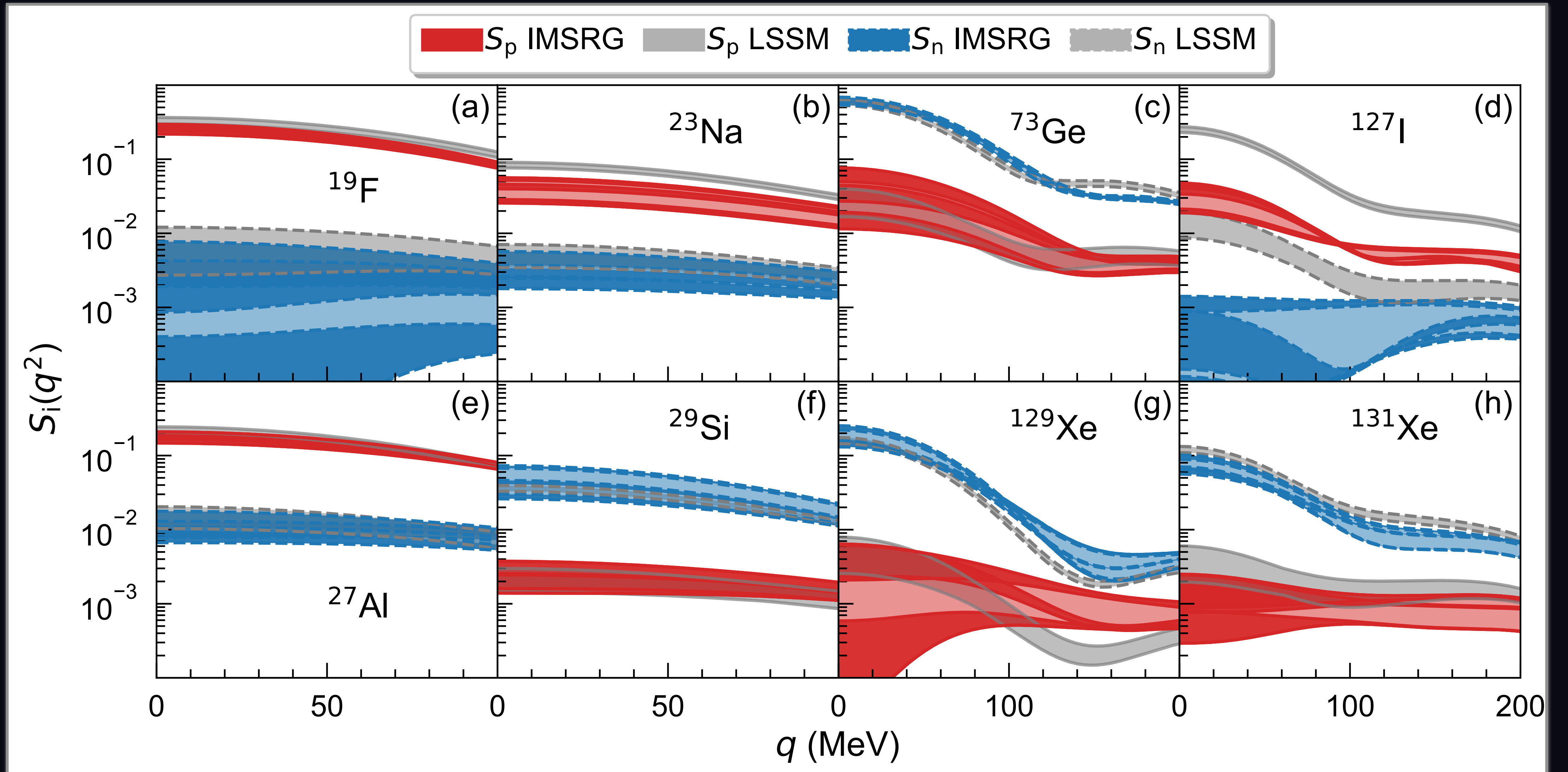
 NAT allows VS-IMSRG for heavy nuclei

# Spin expectation values from VS-IMSRG

$$S_A(0) = \frac{(2J+1)(J+1)}{4\pi J} \left| (a_+ + a'_-) \langle \hat{S}_p \rangle + (a_+ - a'_-) \langle \hat{S}_n \rangle \right|^2$$



# VS-IMSRG results for structure factors



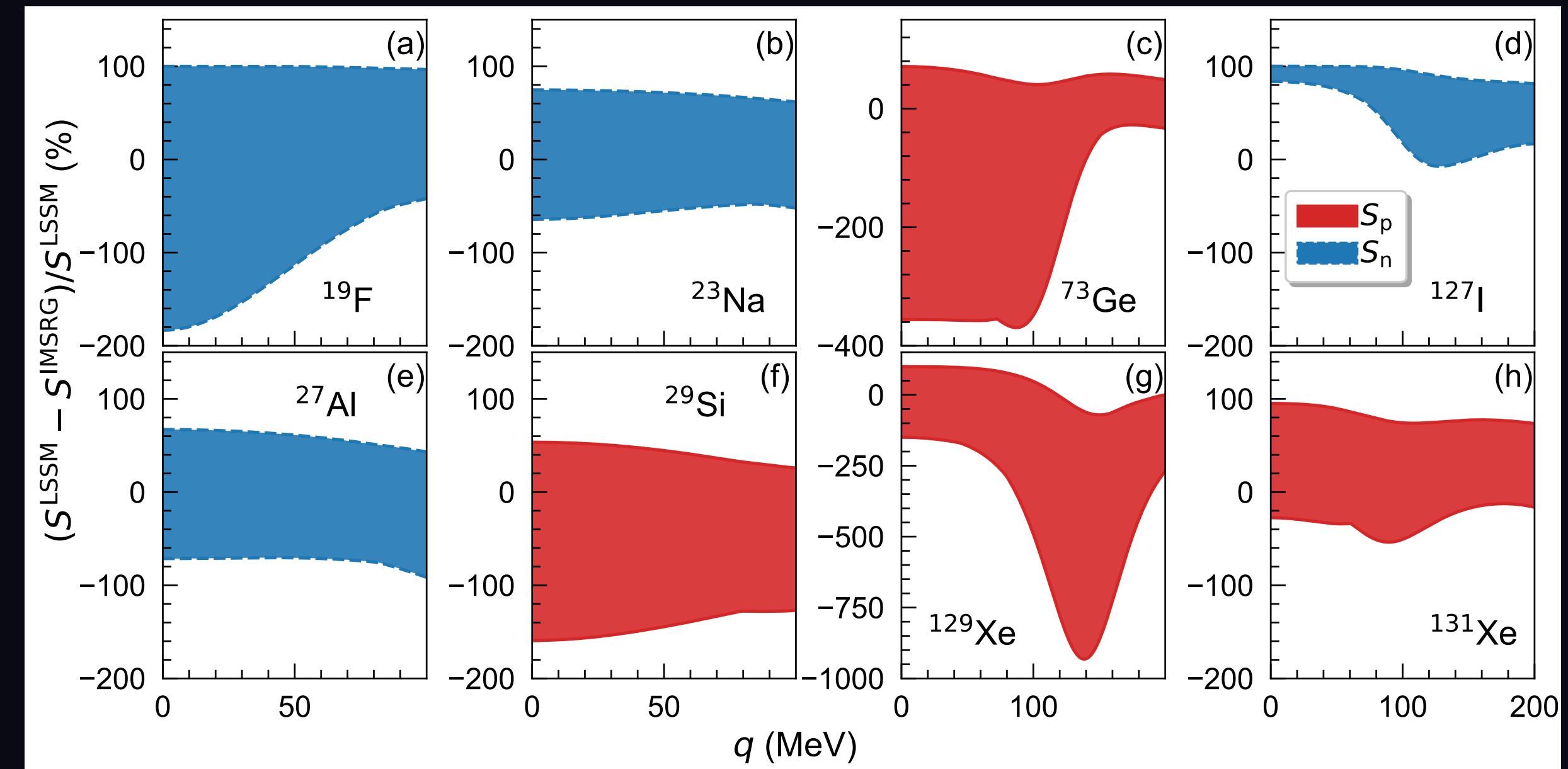
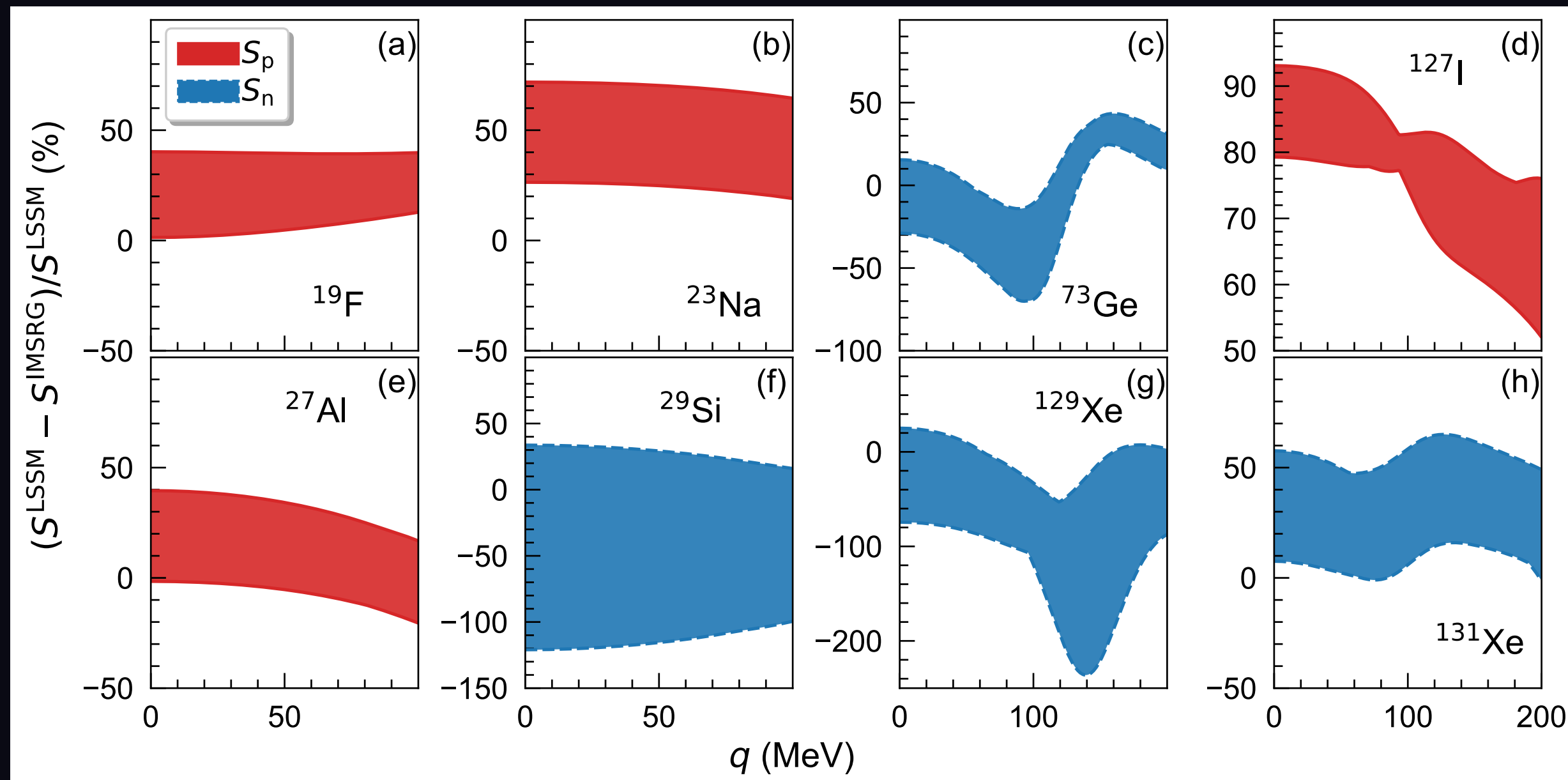
B.S. Hu, et al, Phys. Rev. Lett. 128 (2022) 072502; arXiv: 2109.00193.



# Discrepancy between LSSM and VS-IMSRG

Dominant structure factor

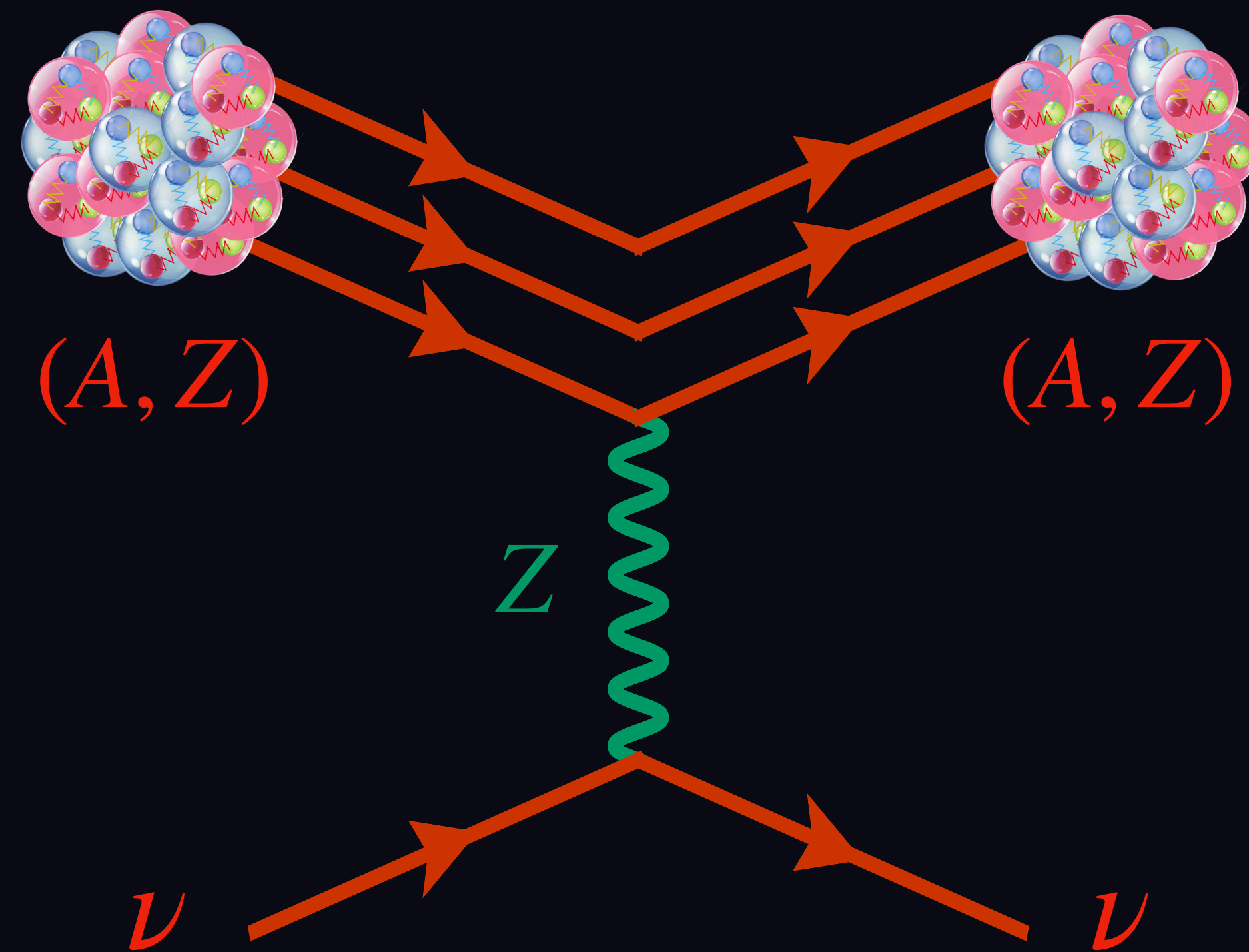
Non-dominant structure factor





# Coherent Elastic Neutrino-Nucleus Scattering (CEvNS)

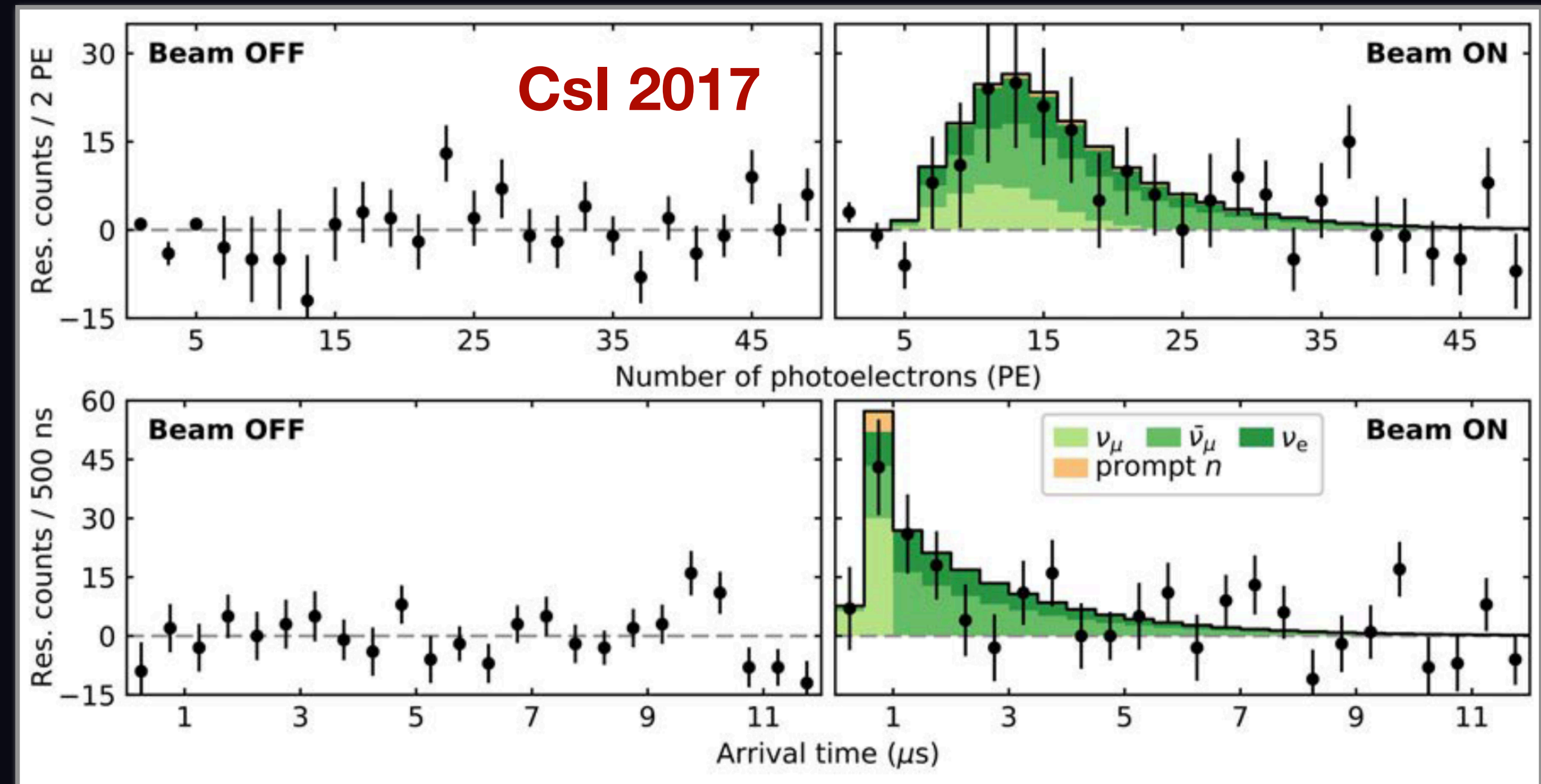
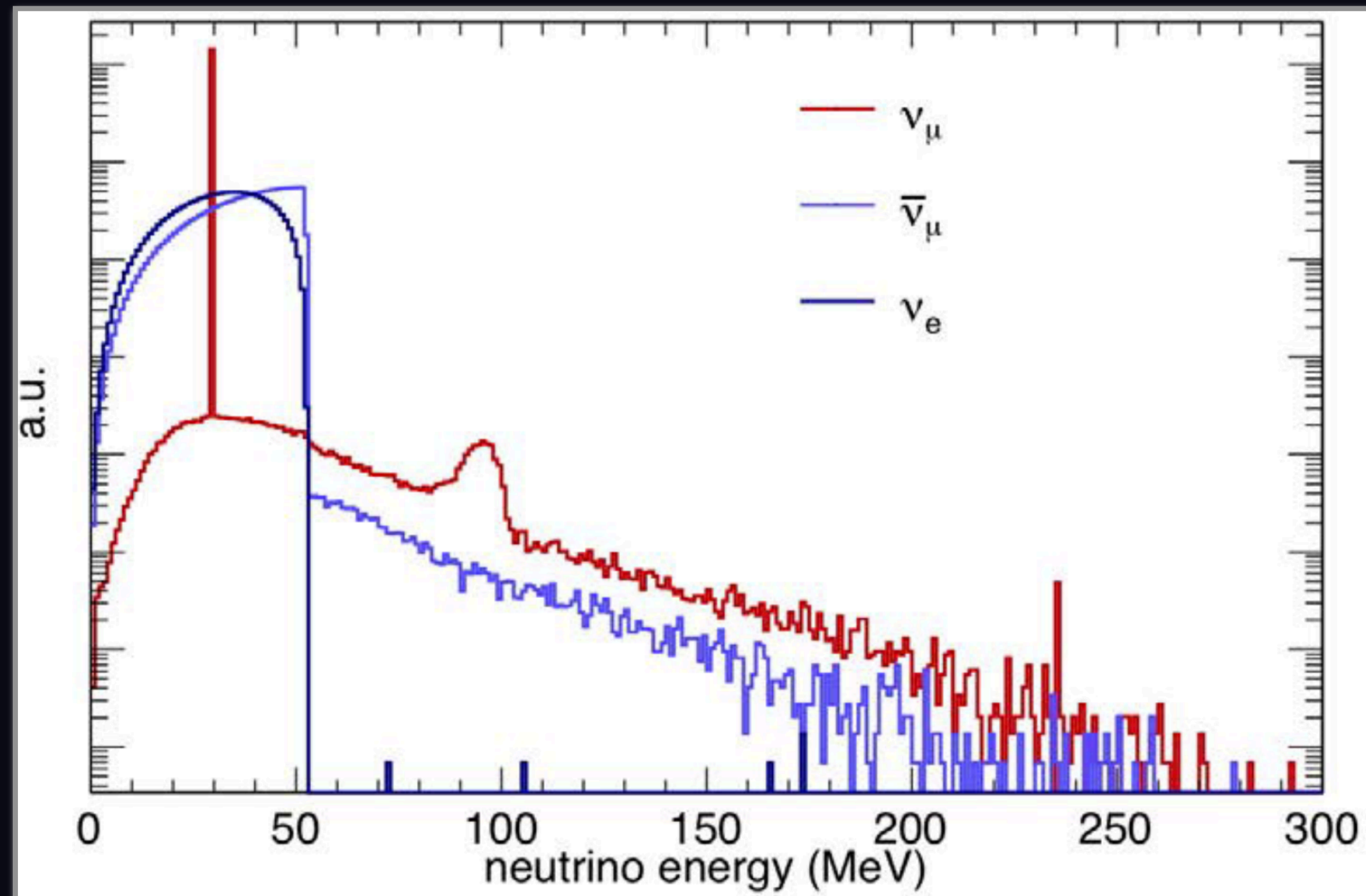
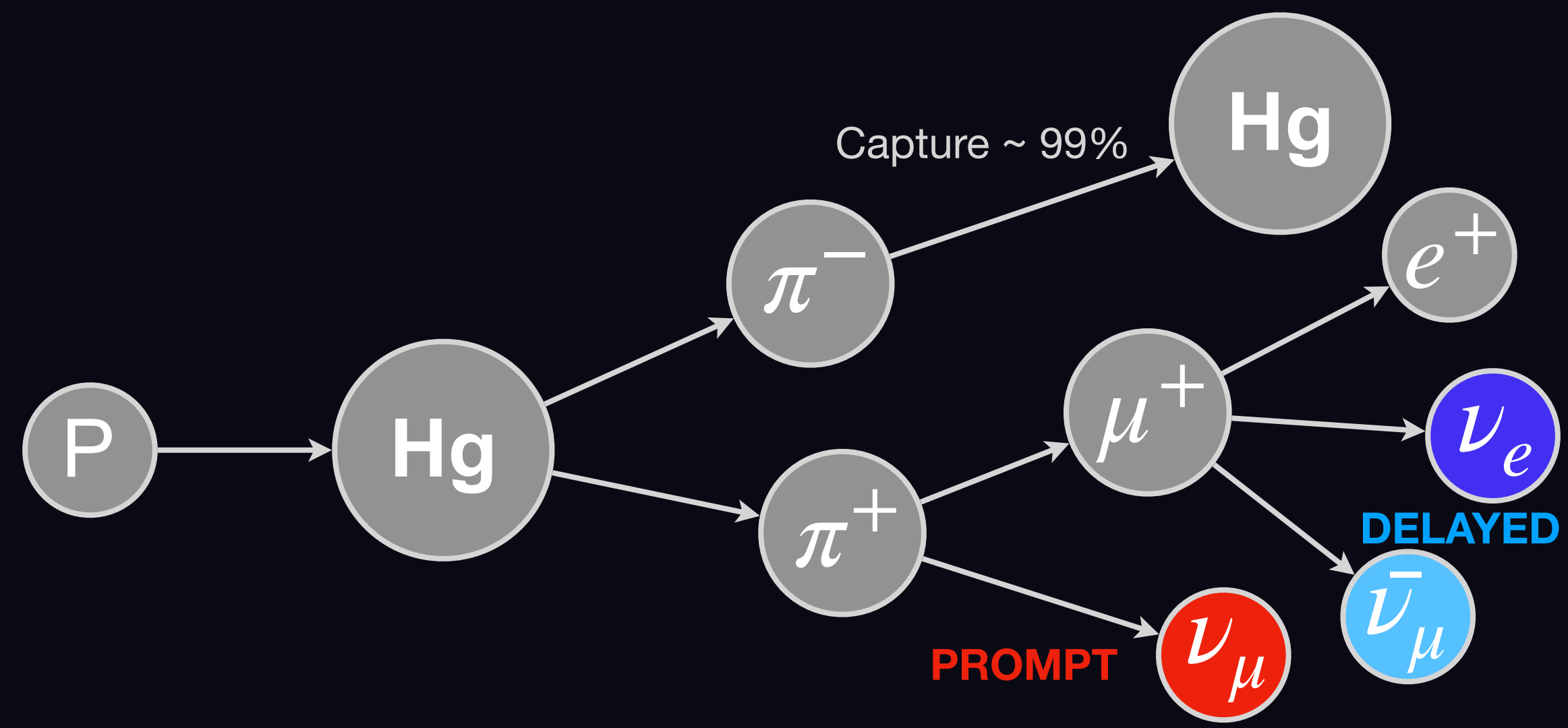
A neutrino interacts a nucleus via exchange of a  $Z$ , and the nucleus recoils as a whole





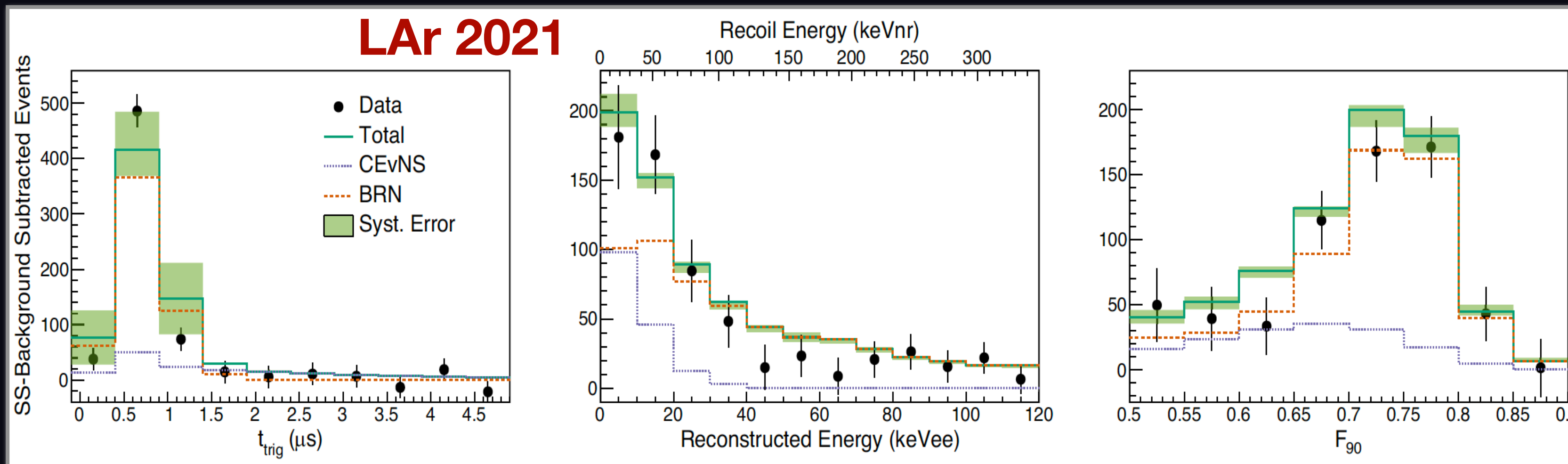
# COHERENT experiment

SNS as a neutrino source

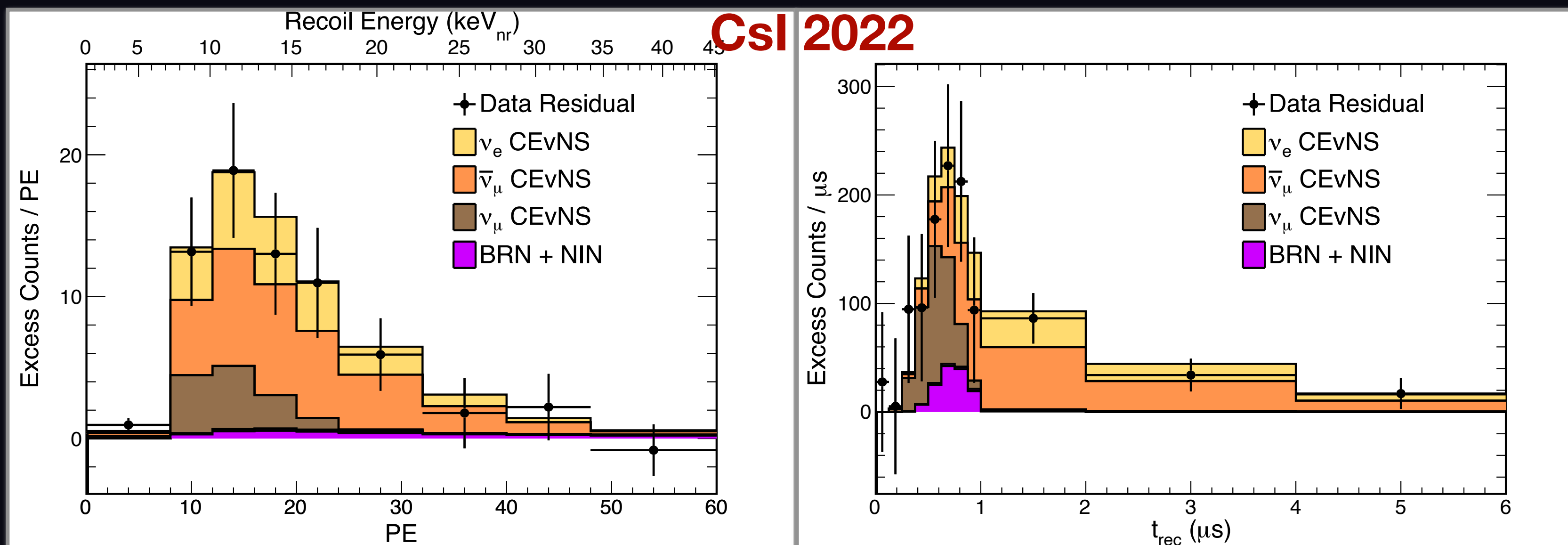


D. Akimov et al. (COHERENT). Science 357, 1123 (2017)

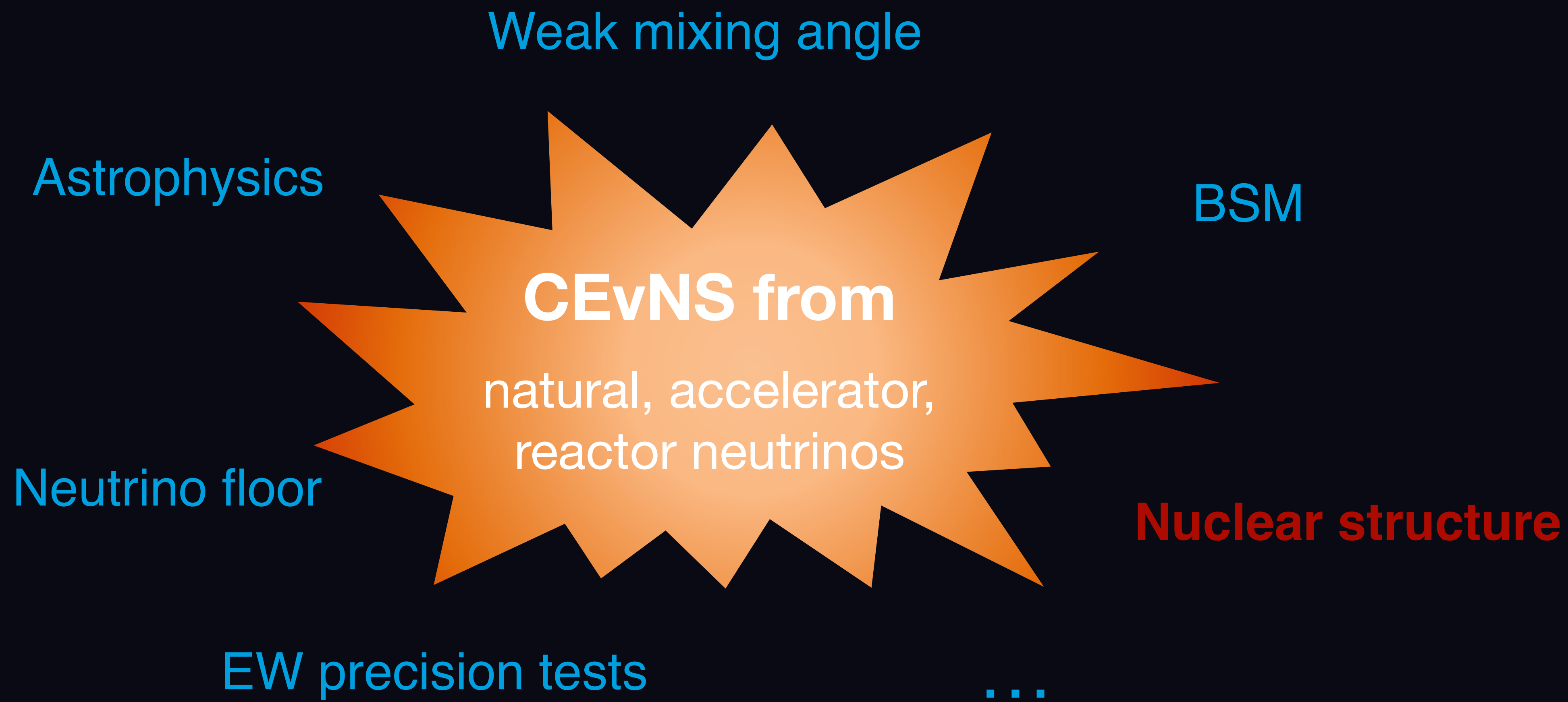
# COHERENT experiment



D. Akimov et al. (COHERENT). Phys. Rev. Lett. 126, 012002 (2021)



D. Akimov et al. (COHERENT). Phys. Rev. Lett. 129, 081801 (2022)





# CEvNS differential cross section

$$\frac{d\sigma_A}{dT}(E_\nu, T) = \frac{G_F^2 M_A}{4\pi} \left( 1 - \frac{M_A T}{2E_\nu^2} - \frac{T}{E_\nu} \right) Q_w^2 \left| F_w(\mathbf{q}^2) \right|^2 + \frac{G_F^2 M_A}{4\pi} \left( 1 + \frac{M_A T}{2E_\nu^2} - \frac{T}{E_\nu} \right) F_A(\mathbf{q}^2)$$

$$q = \sqrt{2M_A E_\nu T / (E_\nu - T)} \approx \sqrt{2M_A T}$$

## Weak charge

$$Q_w = ZQ_w^p + NQ_w^n$$

$$Q_w^p = 0.0714, Q_w^n = -0.9900 ?$$

$$Q_w^n = -1, Q_w^p = 1 - 4\sin^2\theta_w, \sin^2\theta_w = 0.23122 \pm 0.00003 ?$$

Radiative corrections ?

## Axial-vector form factor $F_A$

Negligible ?

## Nuclear weak form factor $F_w$

Phenomenological Helm and Klein-Nystrand

$$F_{\text{Helm}}(q^2) = \frac{3j_1(qR)}{qR} e^{-q^2 s^2 / 2}$$

$$F_{\text{KN}}(q^2) = \frac{3j_1(qR_A)}{qR_A} \frac{1}{1 + q^2 a_{kn}^2}$$

# Chiral EFT: Systematic expansion of nuclear forces and electroweak currents

$$F_w(\mathbf{q}^2) = \frac{1}{Q_w} \left\{ \left[ Q_w^p \left( 1 - \frac{\langle r_E^2 \rangle^p}{6} q^2 - \frac{1}{8m_{\mathcal{N}}^2} q^2 \right) - Q_w^n \frac{\langle r_E^2 \rangle^n + \langle r_{E,s}^2 \rangle^N}{6} q^2 \right] \mathcal{F}_p^M(\mathbf{q}^2) + \left[ Q_w^n \left( 1 - \frac{\langle r_E^2 \rangle^p + \langle r_{E,s}^2 \rangle^N}{6} q^2 - \frac{1}{8m_{\mathcal{N}}^2} q^2 \right) - Q_w^p \frac{\langle r_E^2 \rangle^n}{6} q^2 \right] \mathcal{F}_n^M(\mathbf{q}^2) + \frac{Q_w^p (1 + 2\kappa^p) + 2Q_w^n (\kappa^n + \kappa_s^N)}{4m_{\mathcal{N}}^2} q^2 \mathcal{F}_p^{\Phi''}(\mathbf{q}^2) + \frac{Q_w^n (1 + 2\kappa^p + 2\kappa_s^N) + 2Q_w^p \kappa^n}{4m_{\mathcal{N}}^2} q^2 \mathcal{F}_n^{\Phi''}(\mathbf{q}^2) \right\}.$$

$$F_A(\mathbf{q}^2) = \frac{8\pi}{2J+1} \left[ (g_A^{s,N})^2 S_{00}^{\mathcal{F}}(\mathbf{q}^2) - g_A g_A^{s,N} S_{01}^{\mathcal{F}}(\mathbf{q}^2) + (g_A)^2 S_{11}^{\mathcal{F}}(\mathbf{q}^2) \right]$$

$$S_{00}^{\mathcal{F}} = \sum_L \left[ \mathcal{F}_+^{\Sigma'_L}(\mathbf{q}^2) \right]^2,$$

$$S_{11}^{\mathcal{F}} = \sum_L \left[ \left[ 1 + \delta'(\mathbf{q}^2) \right] \mathcal{F}_-^{\Sigma'_L}(\mathbf{q}^2) \right]^2,$$

$$S_{01}^{\mathcal{F}} = \sum_L 2 \left[ 1 + \delta'(\mathbf{q}^2) \right] \mathcal{F}_+^{\Sigma'_L}(\mathbf{q}^2) \mathcal{F}_-^{\Sigma'_L}(\mathbf{q}^2).$$

Details:

M. Hoferichter et al., PRD 102 (2020) 074018

L.A. Ruso et al., arXiv:2203.09030 (2022)

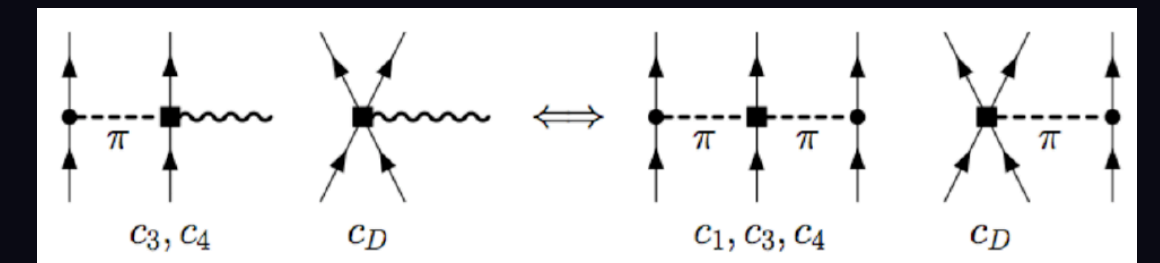


Nuclear  
response  
functions

$\mathcal{F}_\tau^M$  : mainly from neutron distribution

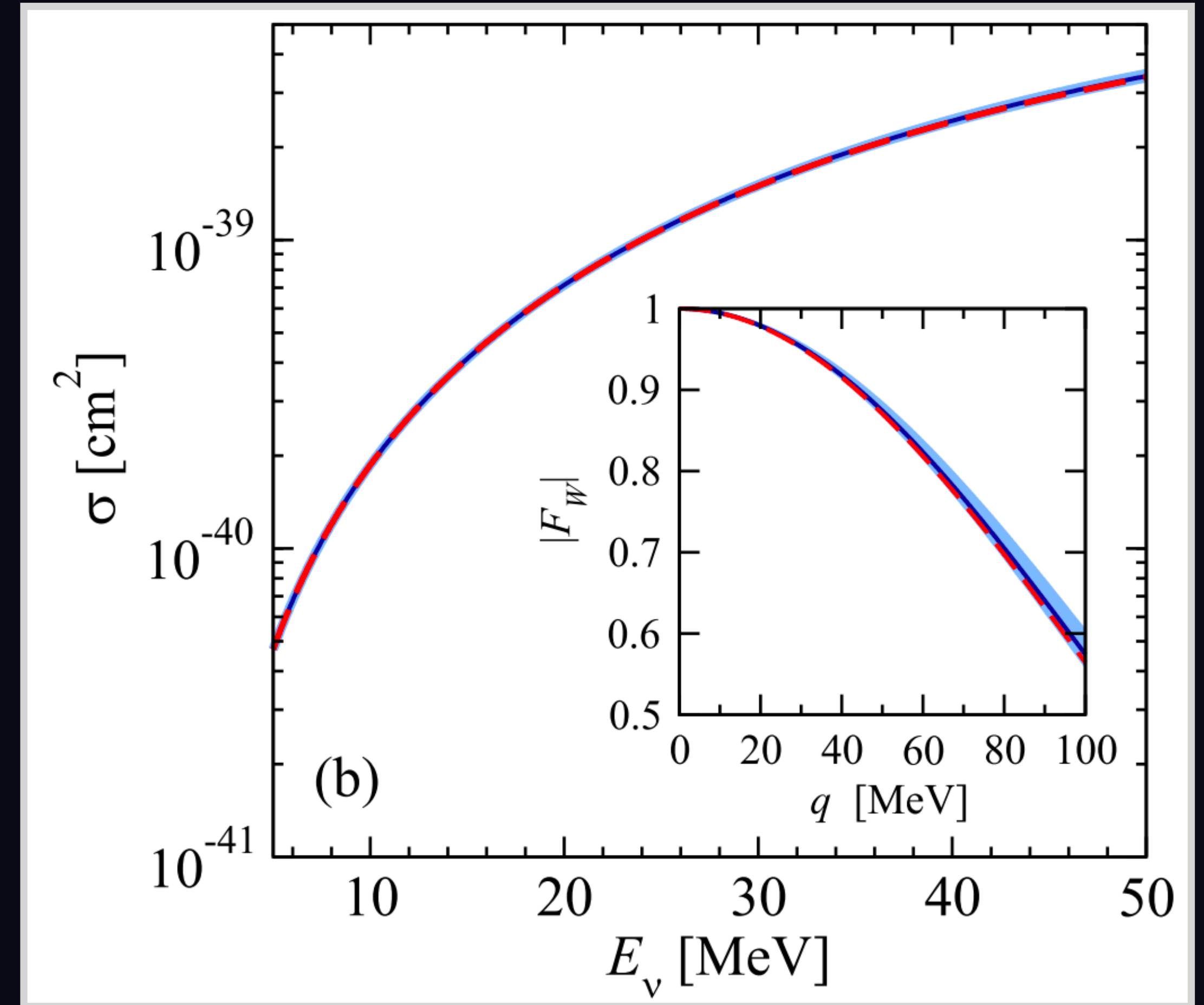
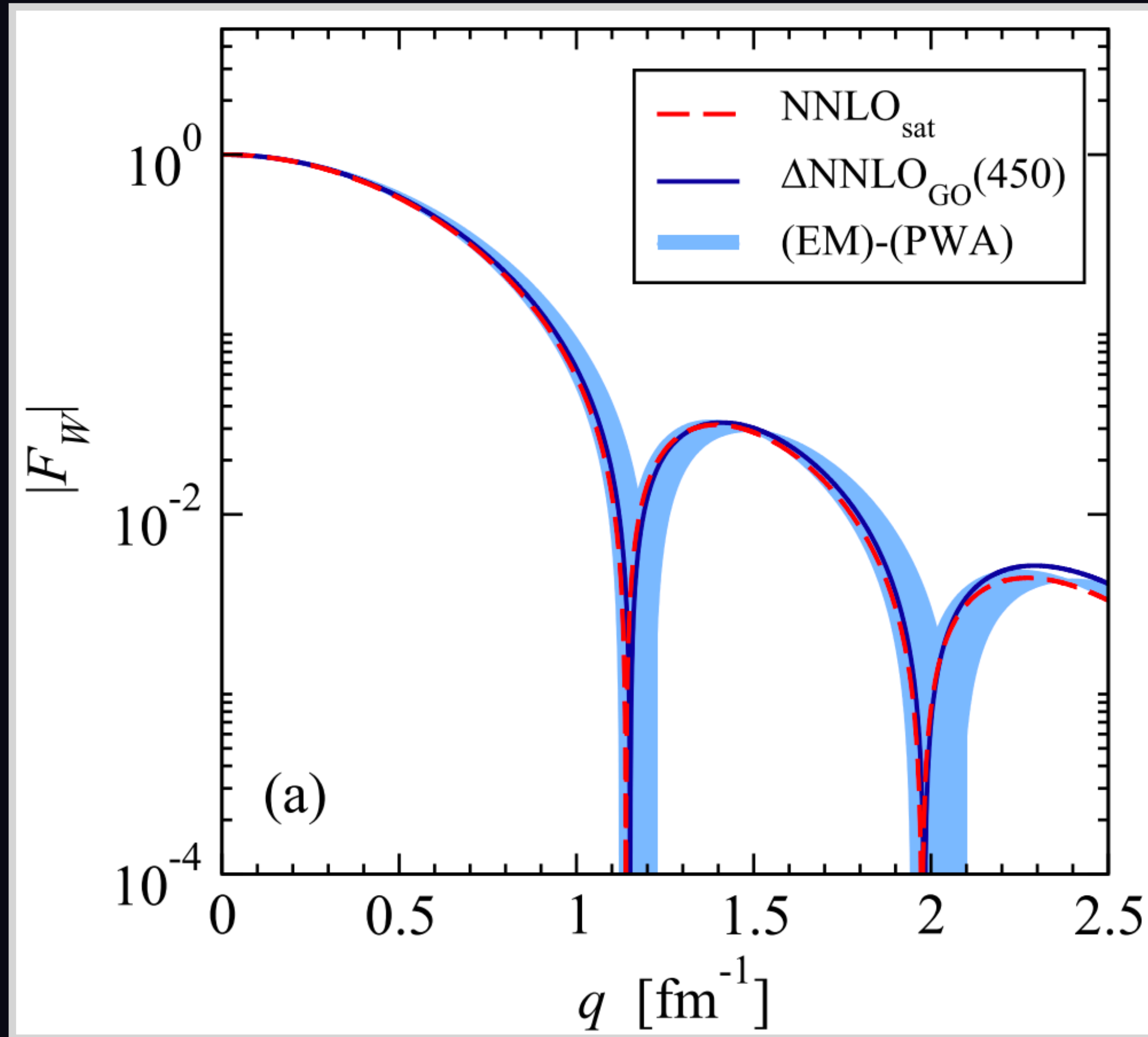
$\mathcal{F}_\tau^{\Phi''}$  : spin-orbit correction

$\mathcal{F}_\tau^{\Sigma'}$  : axial-vector contribution; two-body currents important





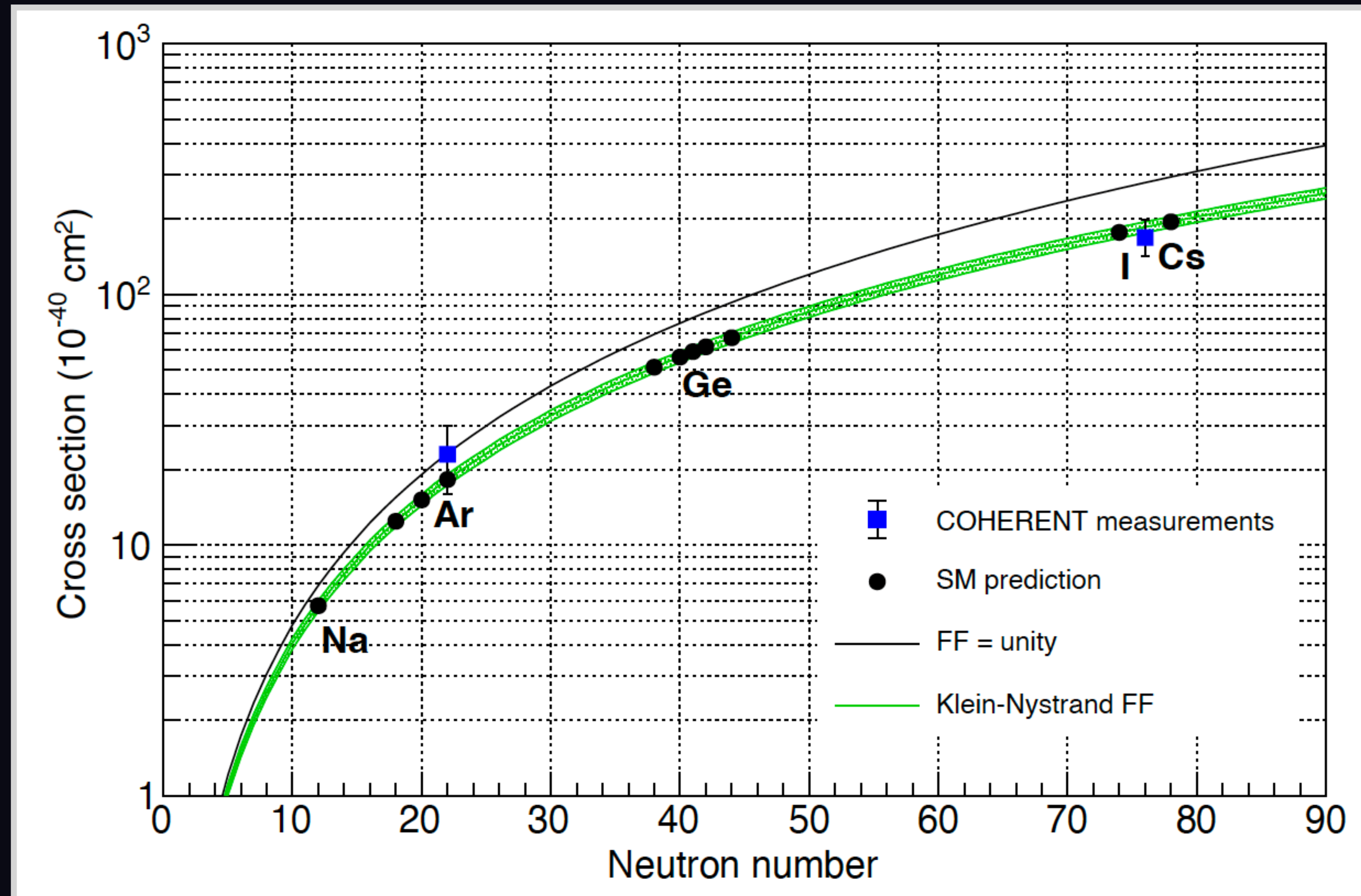
# Ab initio coupled-cluster calculations of CEvNS in $^{40}\text{Ar}$



C.G. Payne, S. Bacca, G. Hagen, W.G. Jiang and T. Papenbrock,  
Phys. Rev. C 100, 061304(R) (2019)



# Nuclear target

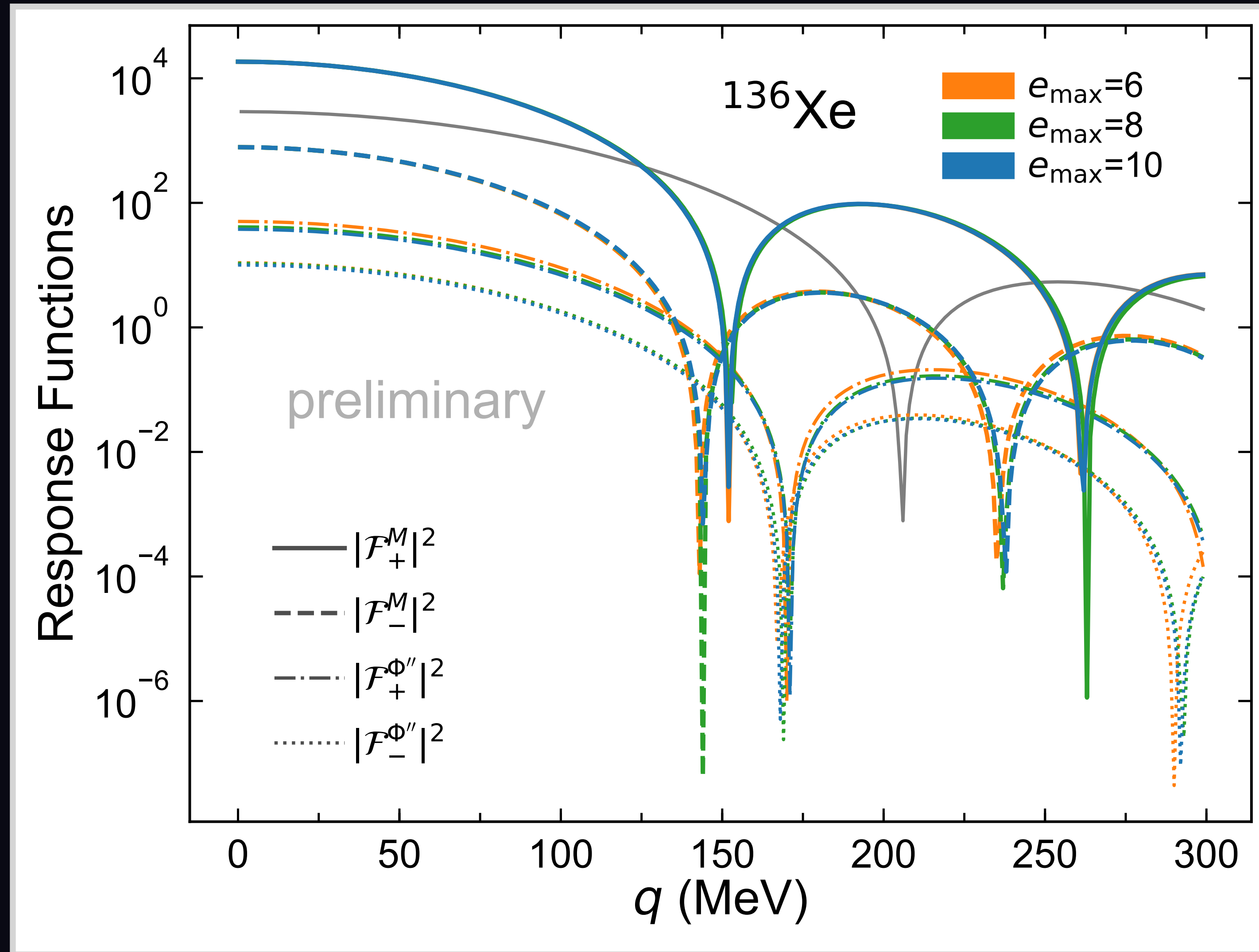


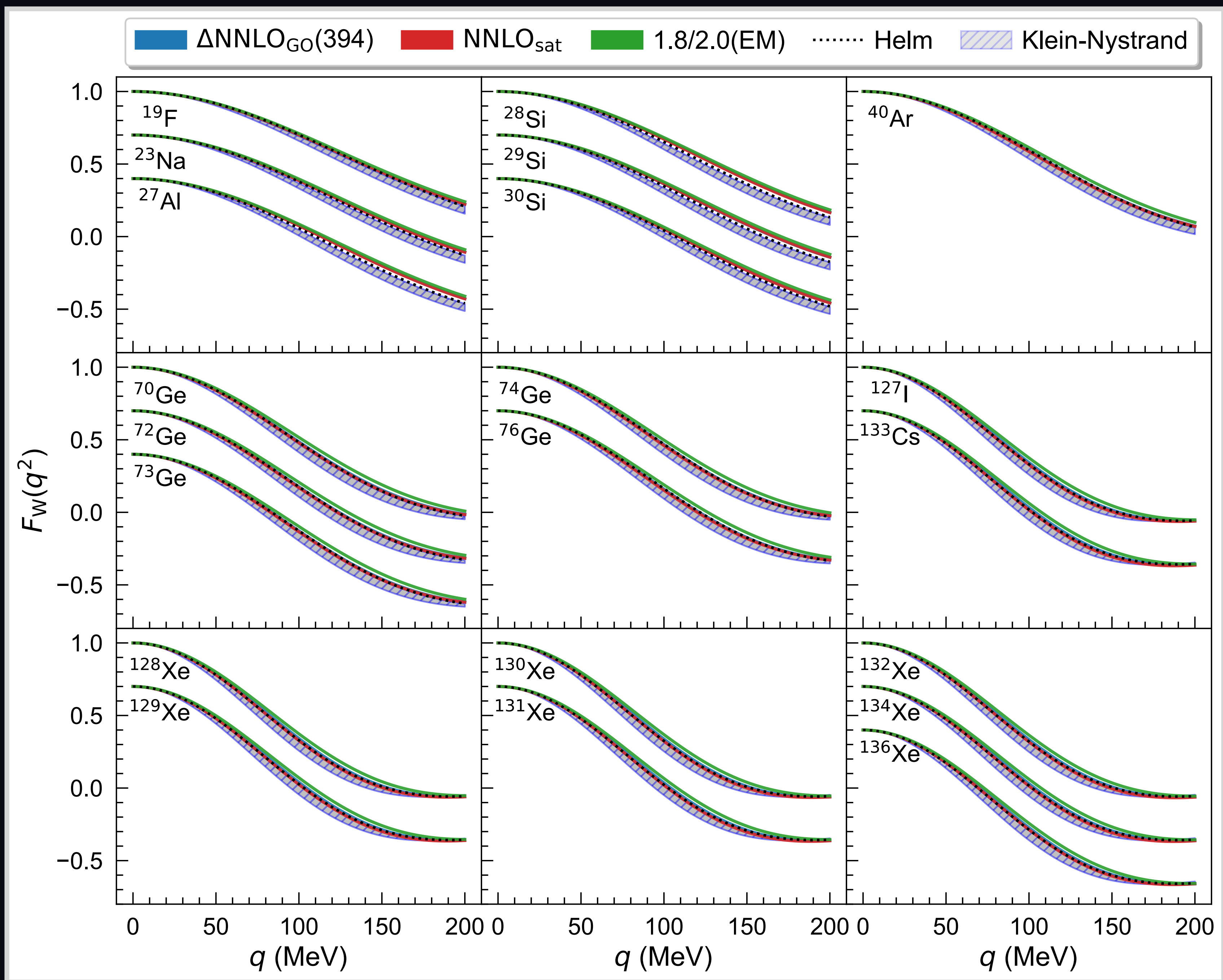
P.S. Barbeau, Yu. Efremenko, K. Scholberg, arXiv:2111.07033 (2021)

📍 Green band from 3% uncertainty on the nuclear radius in the form factor

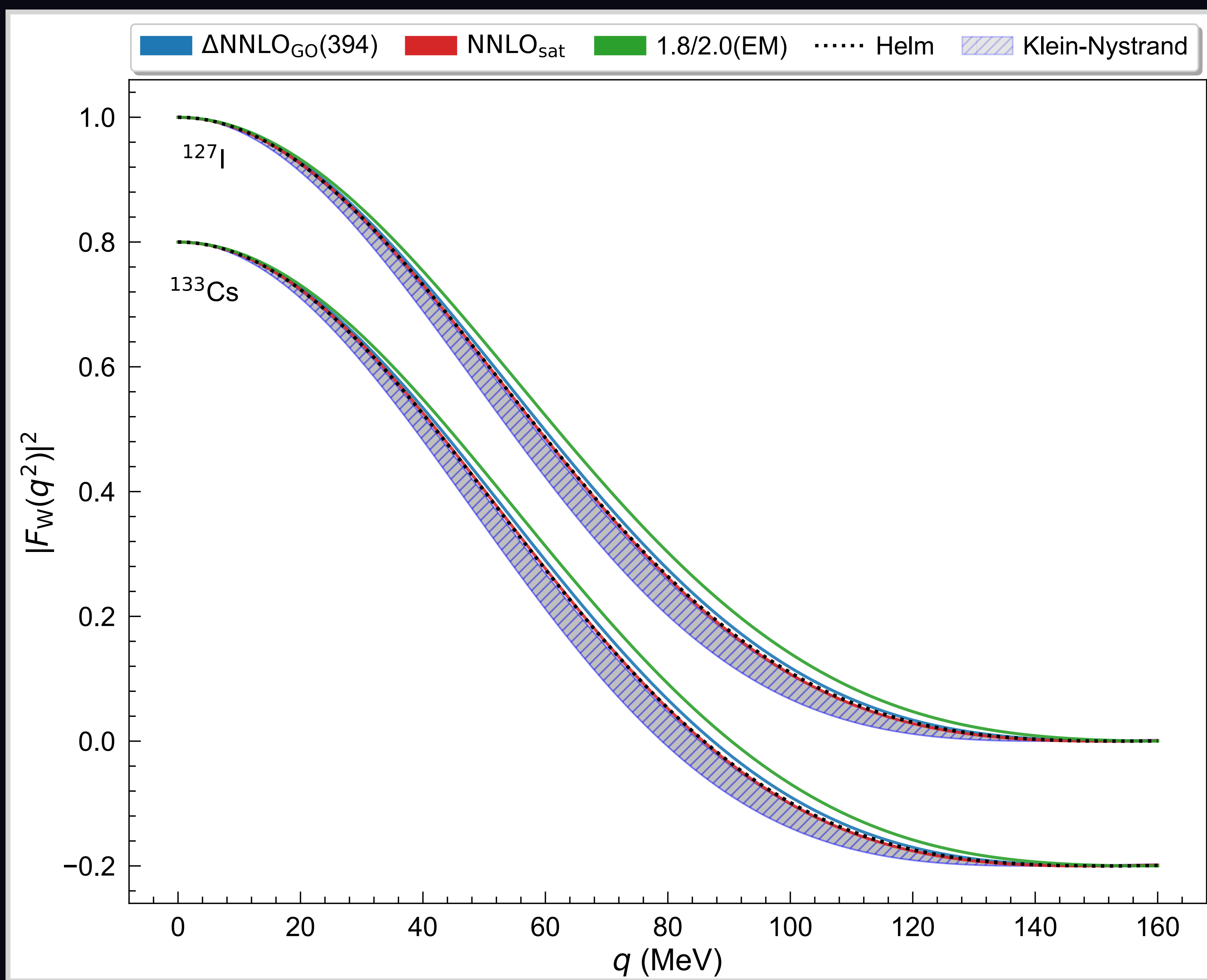
# Convergence of nuclear response functions within NAT basis

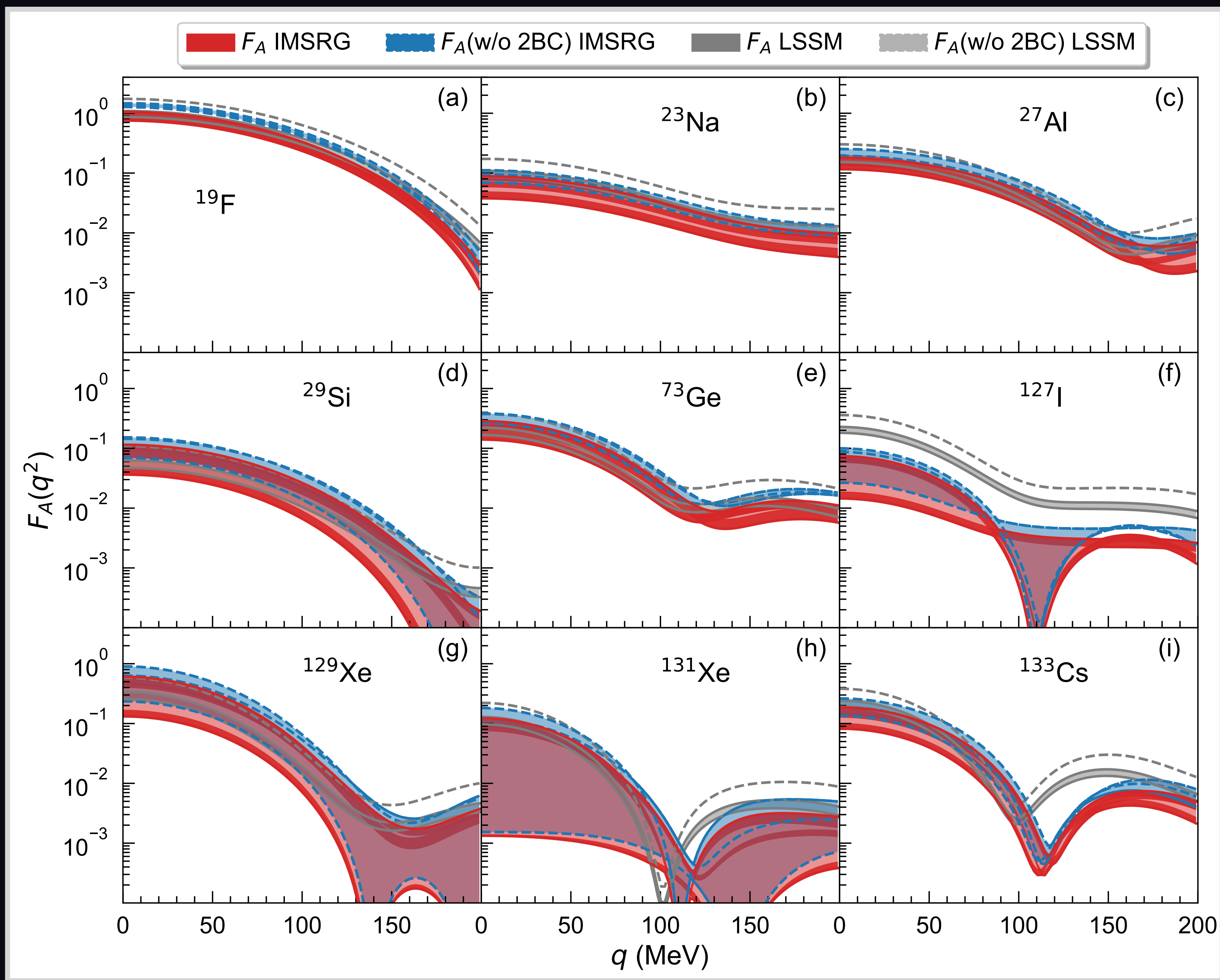
$$\mathcal{F}_\tau^M, \mathcal{F}_\tau^{\Phi''}, \mathcal{F}_\tau^{\Sigma'}$$



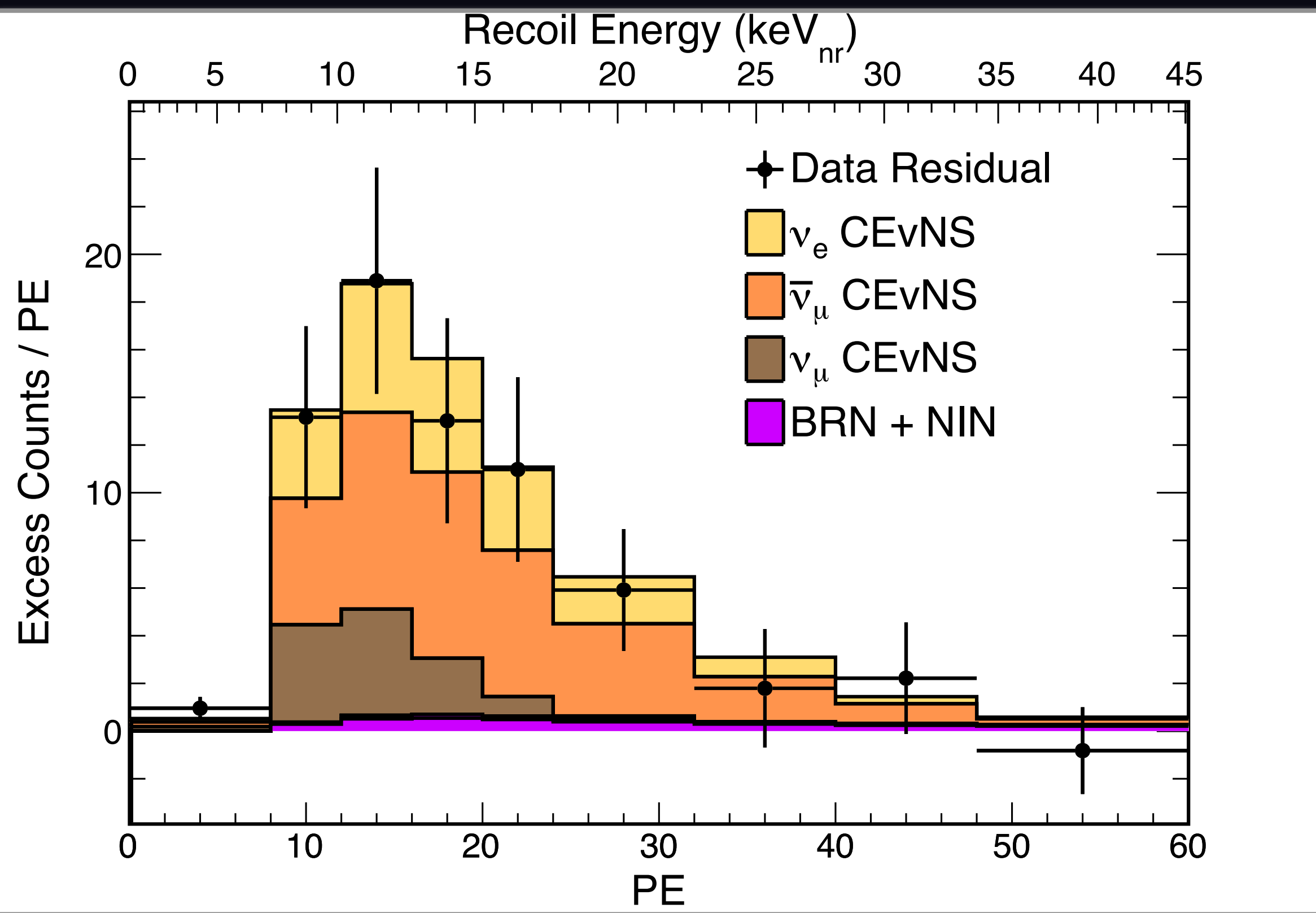




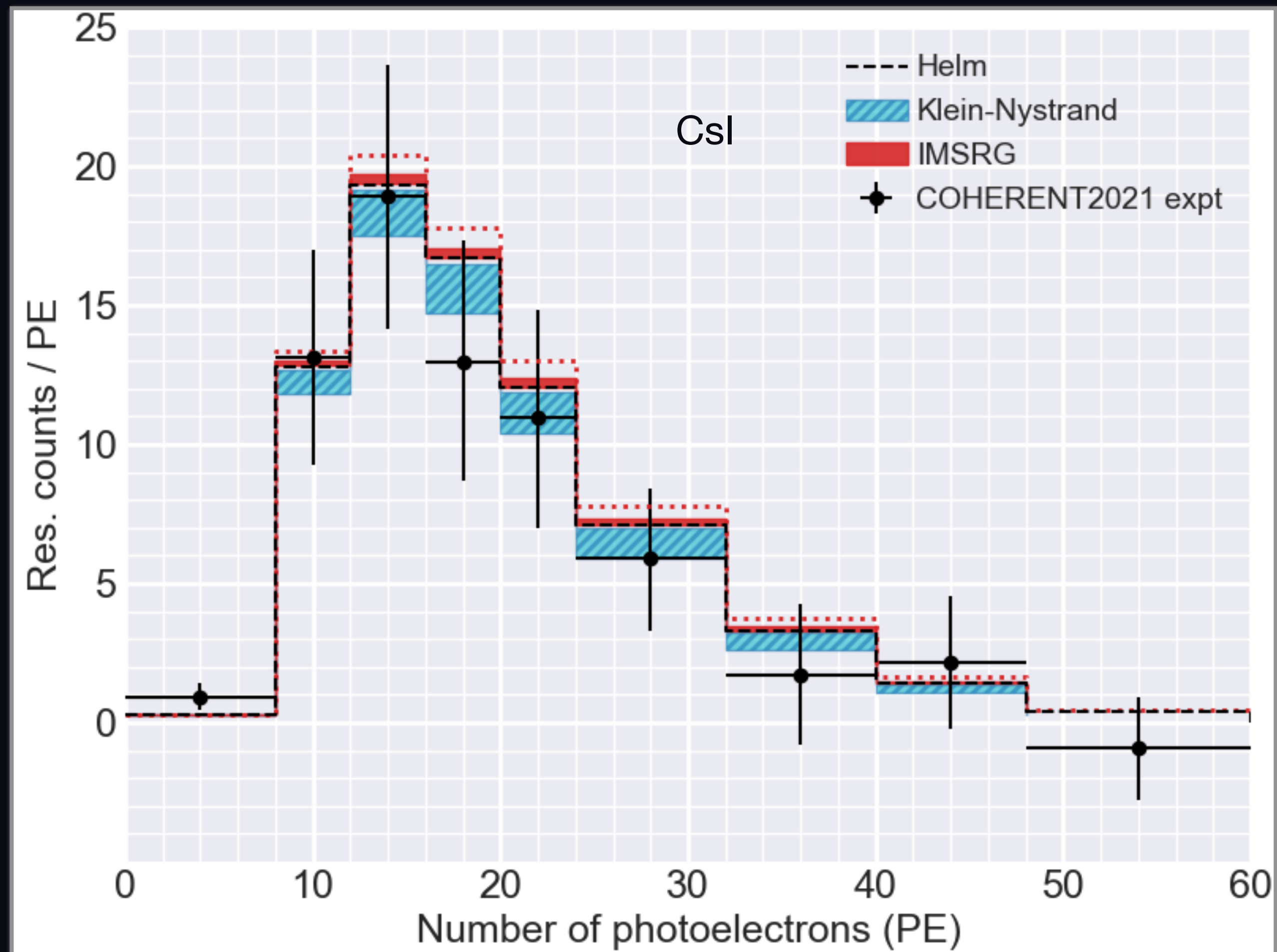




$$\frac{dR}{dT} = \sum_i \left[ N_{\text{target}} X_i \mathcal{N}_\nu \int_{E_\nu^{\text{min}}}^{E_\nu^{\text{max}}} \phi(E_\nu) \frac{d\sigma_i}{dT} dE_\nu \right]$$

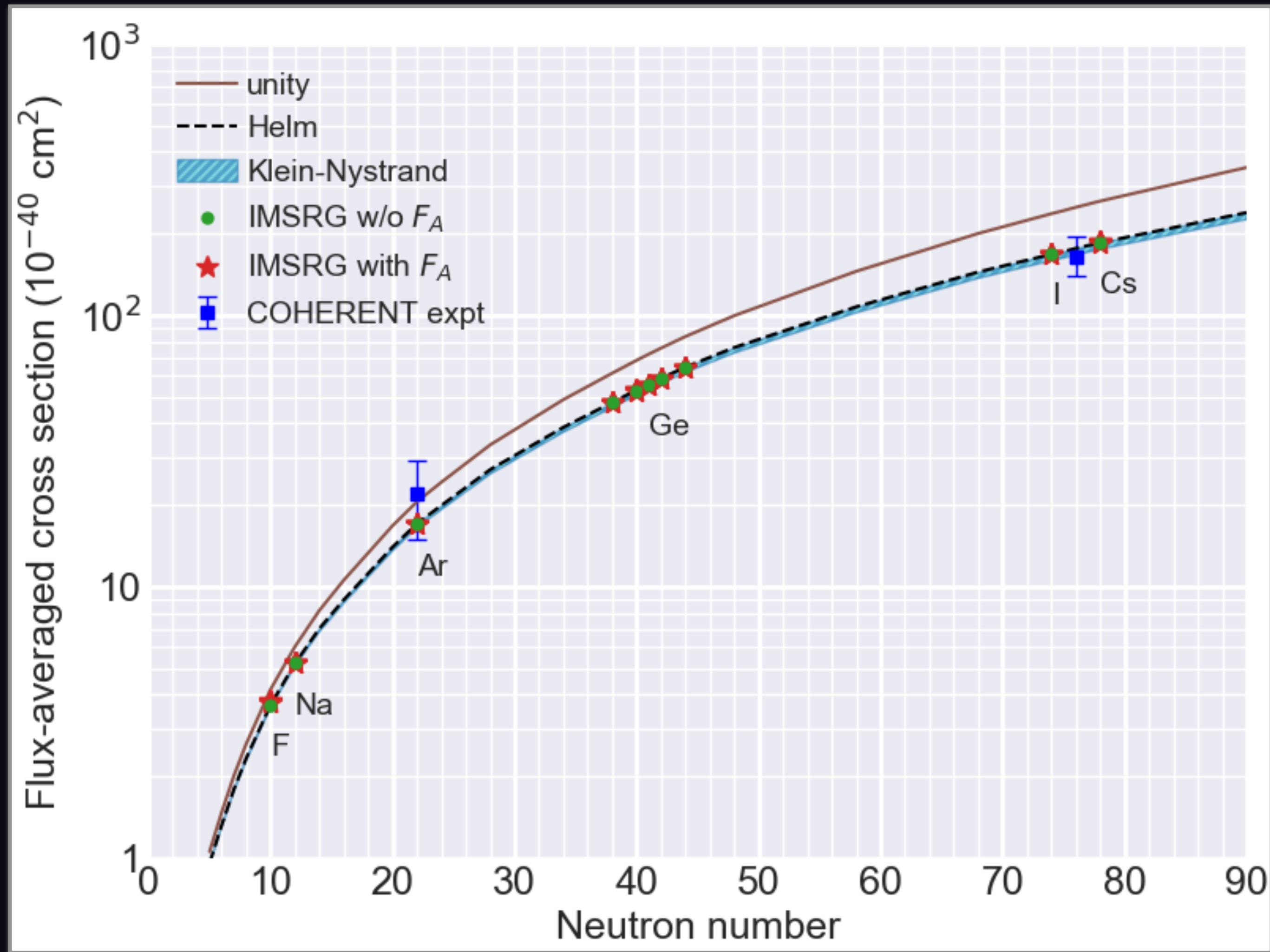


D. Akimov et al. (COHERENT). Phys. Rev. Lett. 129, 081801 (2022)



BSH, et al., In preparation (2023)





BSH, et al., In preparation (2023)

📌 **Helm form factor reproduces ab initio results within NNLOsat well:**

less than 0.3% in heavy nuclei,  
about 1% in light nuclei

$$F_{\text{Helm}}(q^2) = \frac{3j_1(qR)}{qR} e^{-q^2 s^2/2}$$

$$R^2 = c^2 + \frac{7}{3}\pi^2 a^2 - 5s^2$$

$$c = (1.23A^{1/3} - 0.60) \text{ fm}$$

$$a = 0.52 \text{ fm}, s = 0.9 \text{ fm}$$

📌 **Weak charges:** 1.5% level

$$Q_W^p = 0.0714, Q_W^n = -0.9900$$

$$Q_W^n = -1, Q_W^p = 1 - 4\sin^2\theta_W \quad \sin^2\theta_W = 0.23122 \pm 0.00003$$

📌 **Spin-orbit current  $\mathcal{F}_\tau^{\Phi''}$ :**

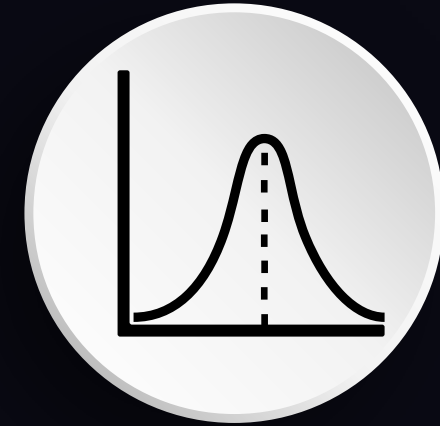
less than  $10^{-6}\%$

📌 **Axial-vector form factor  $F_A$ :**

3% ( $^{19}\text{F}$ ), 0.1% ( $^{23}\text{Na}$ ), 0.03% ( $^{73}\text{Ge}$ ),  
less than 0.007% ( $^{127}\text{I}$  and  $^{133}\text{Cs}$ )

# Summary

**VS-IMSRG**



*Ab initio* structure factors/form factors  
for  $^{19}\text{F}$ ,  $^{23}\text{Na}$ ,  $^{27}\text{Al}$ ,  $\text{Si}$ ,  $^{40}\text{Ar}$ ,  $\text{Ge}$ ,  $^{127}\text{I}$ ,  $^{133}\text{Cs}$ ,  $\text{Xe}$



VS-IMSRG: from light to heavy nuclei  
Chiral EFT 1b + 2b currents



Spin-independent WIMP scattering  
Inelastic scattering



**IMSRG gives converged calculation in heavy nuclei**



# Collaborators:

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Jayden Newstead (University of Melbourne)

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Jason Holt (TRIUMF)

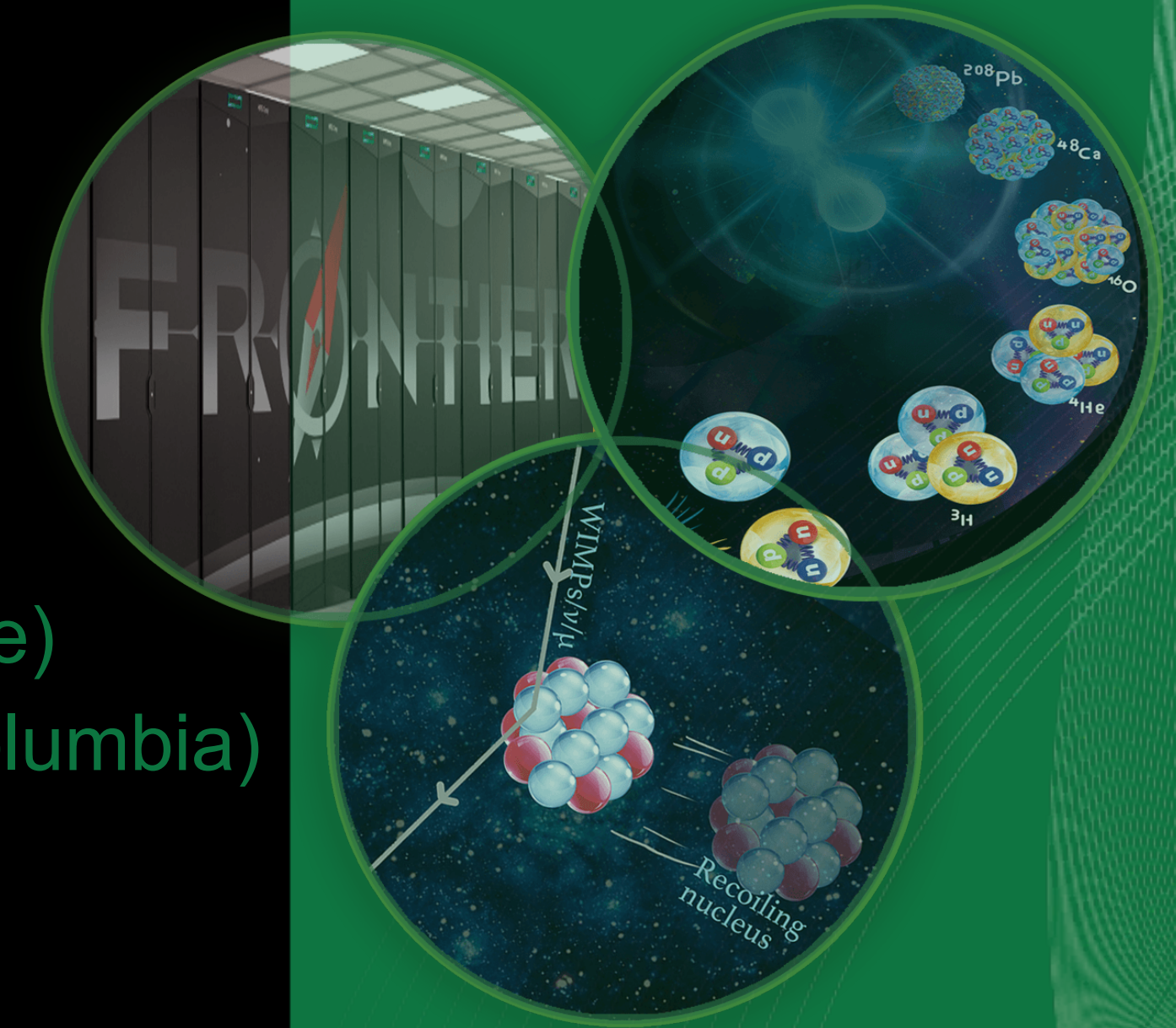
Takayuki Miyagi (TU Darmstadt)

Ragnar Stroberg (University of Notre Dame)

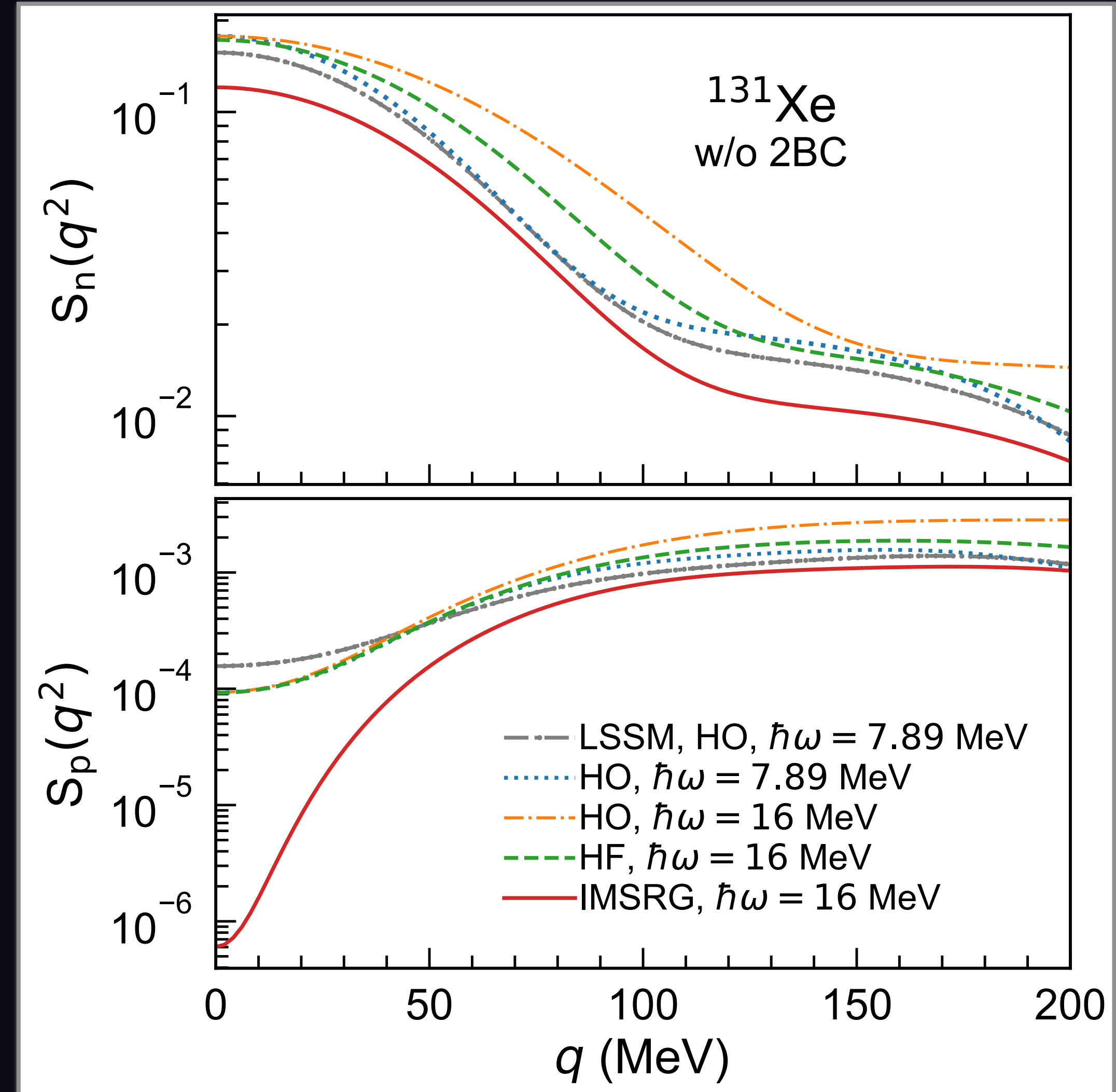
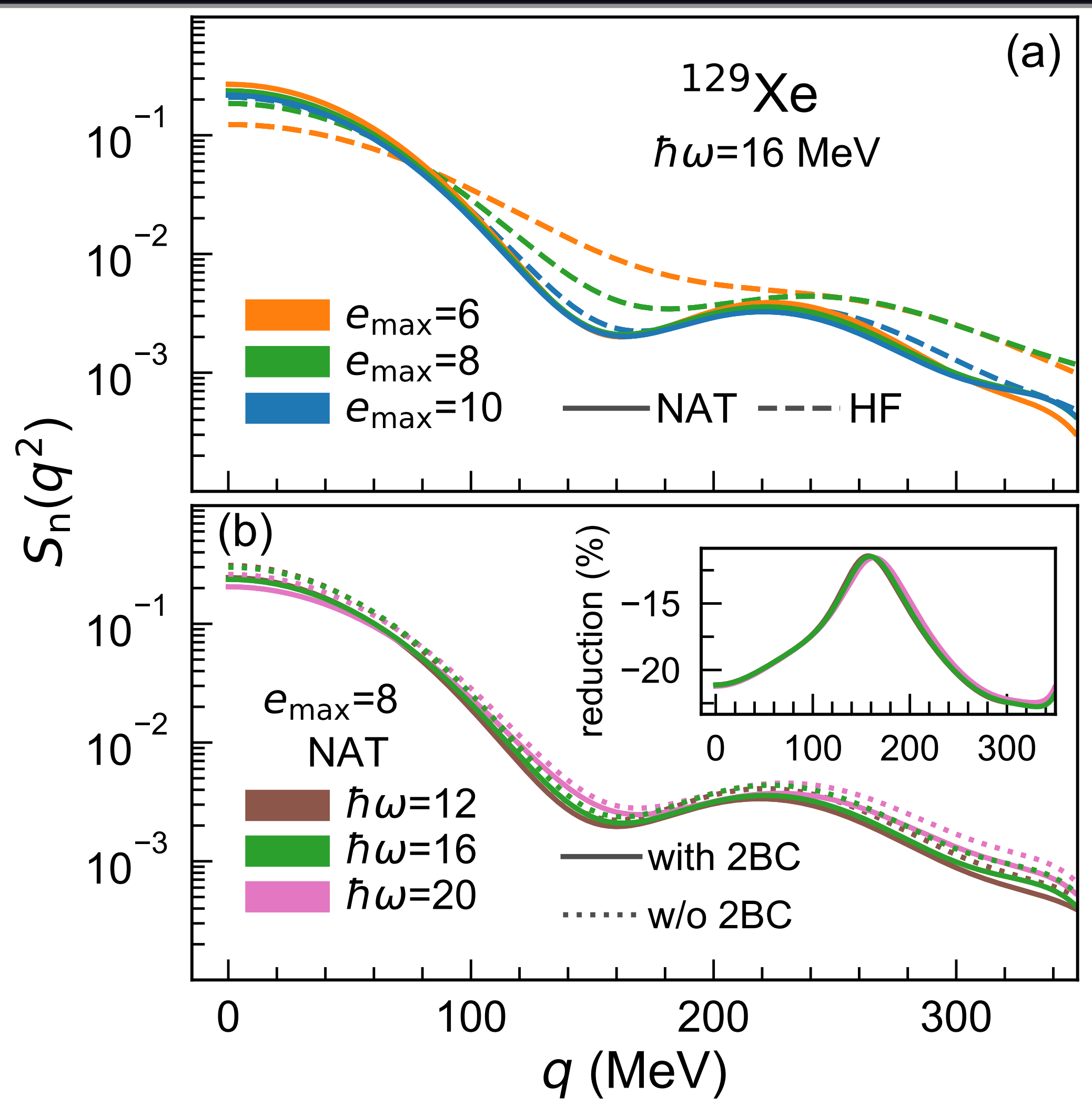
Mathieu Bruneault (University of British Columbia)

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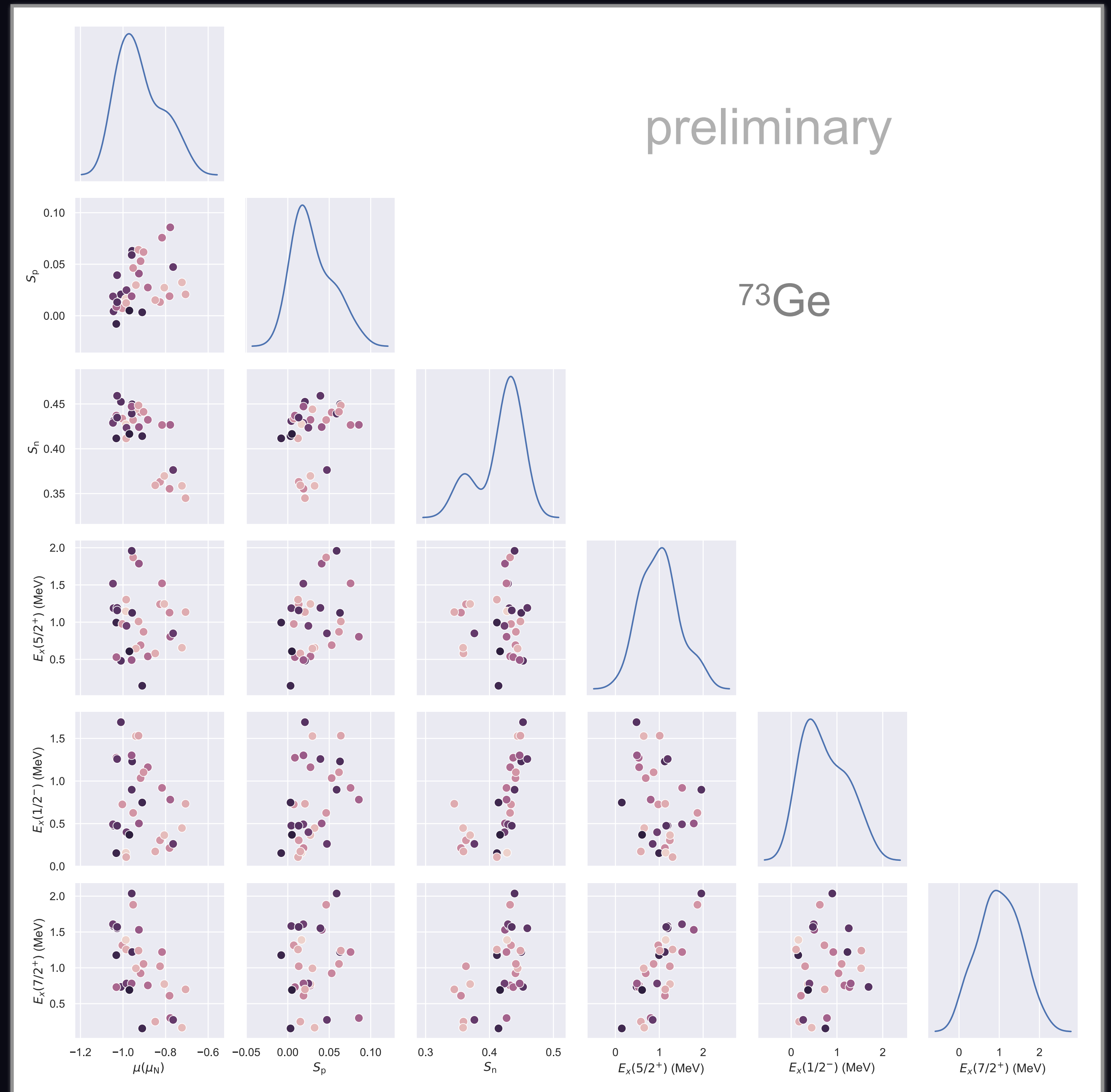
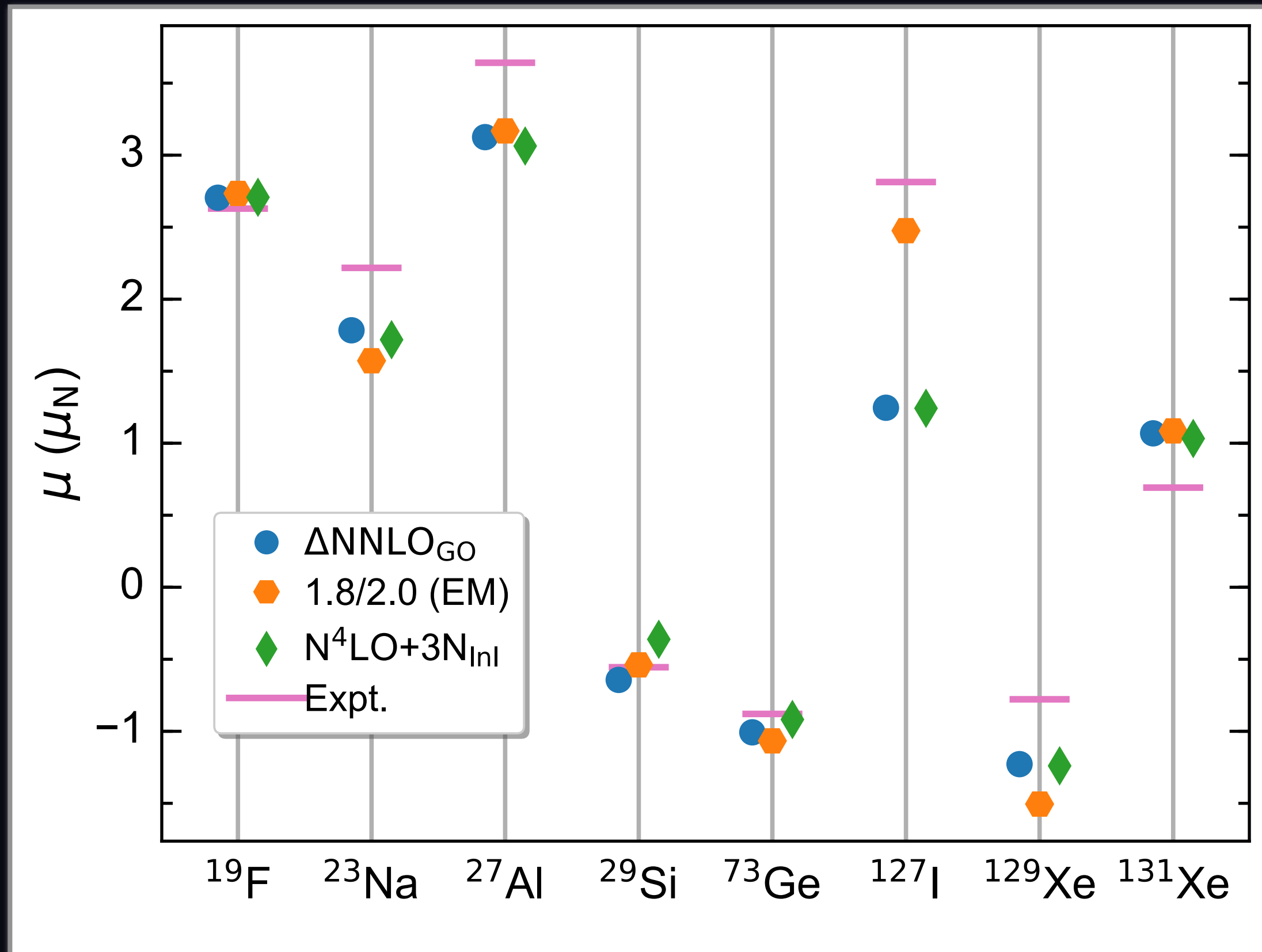
# Thank you !



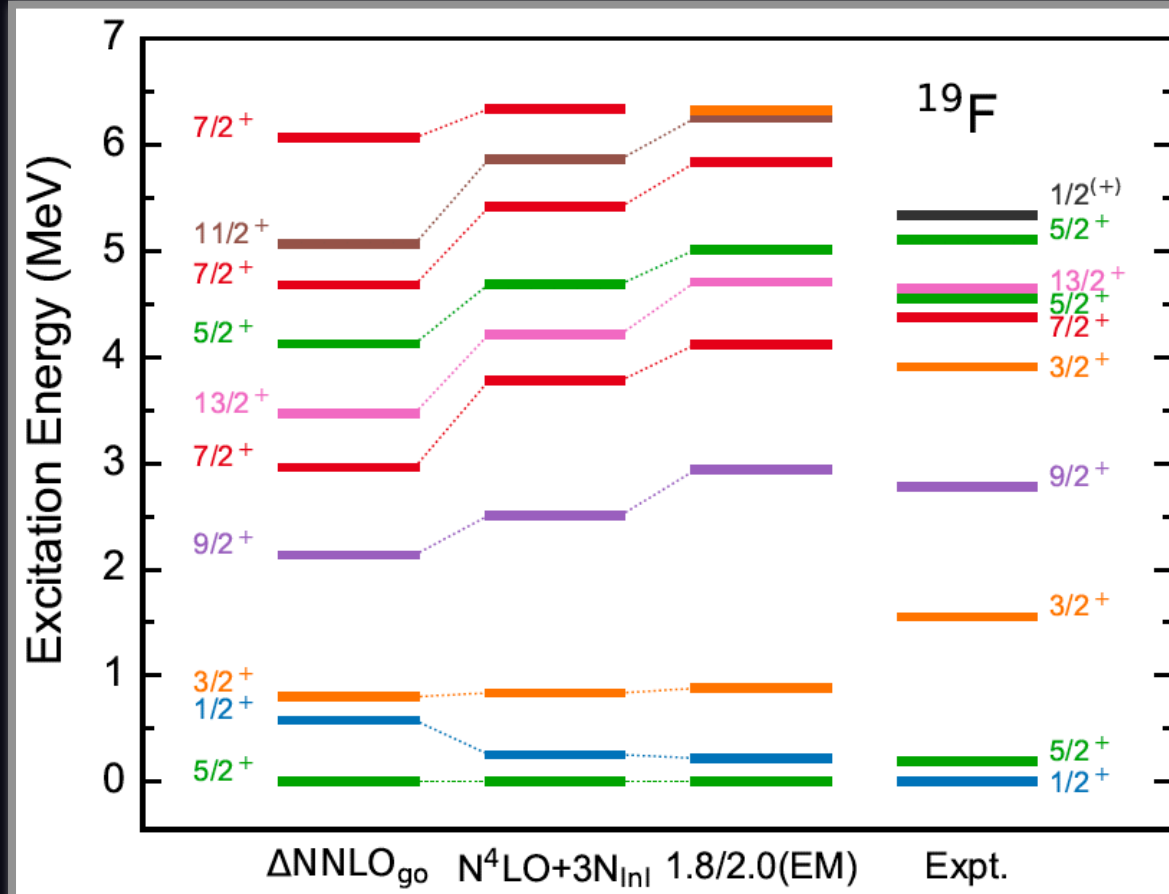




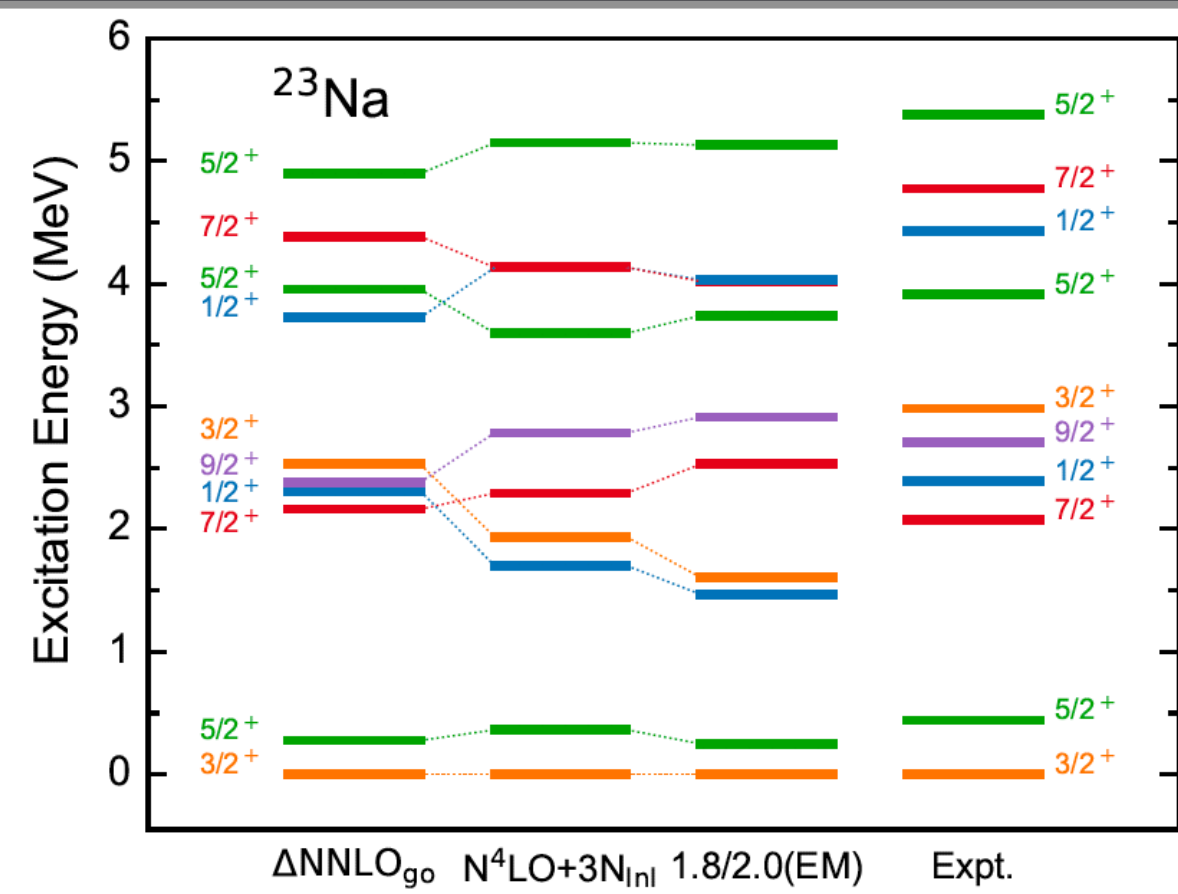
# Magnetic dipole moments



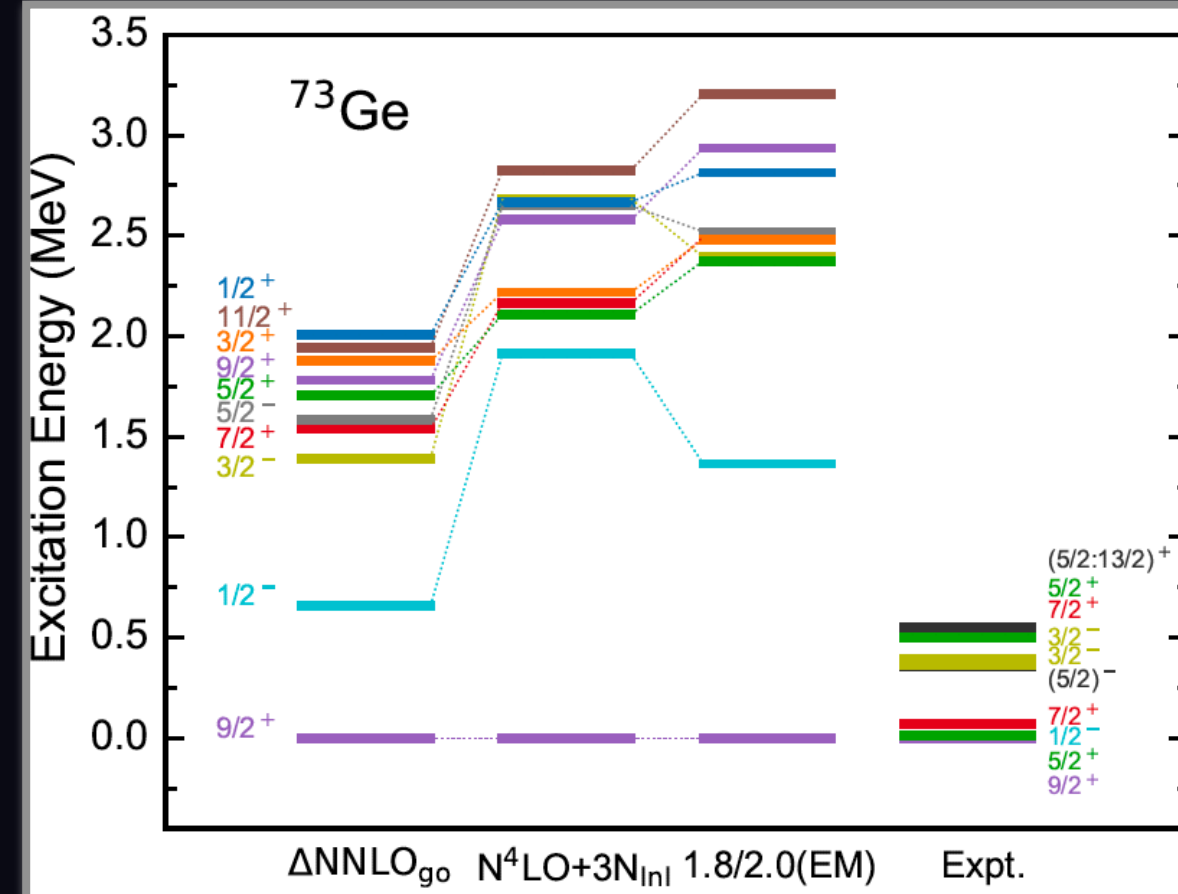
# Spectra from VS-IMSRG within NAT



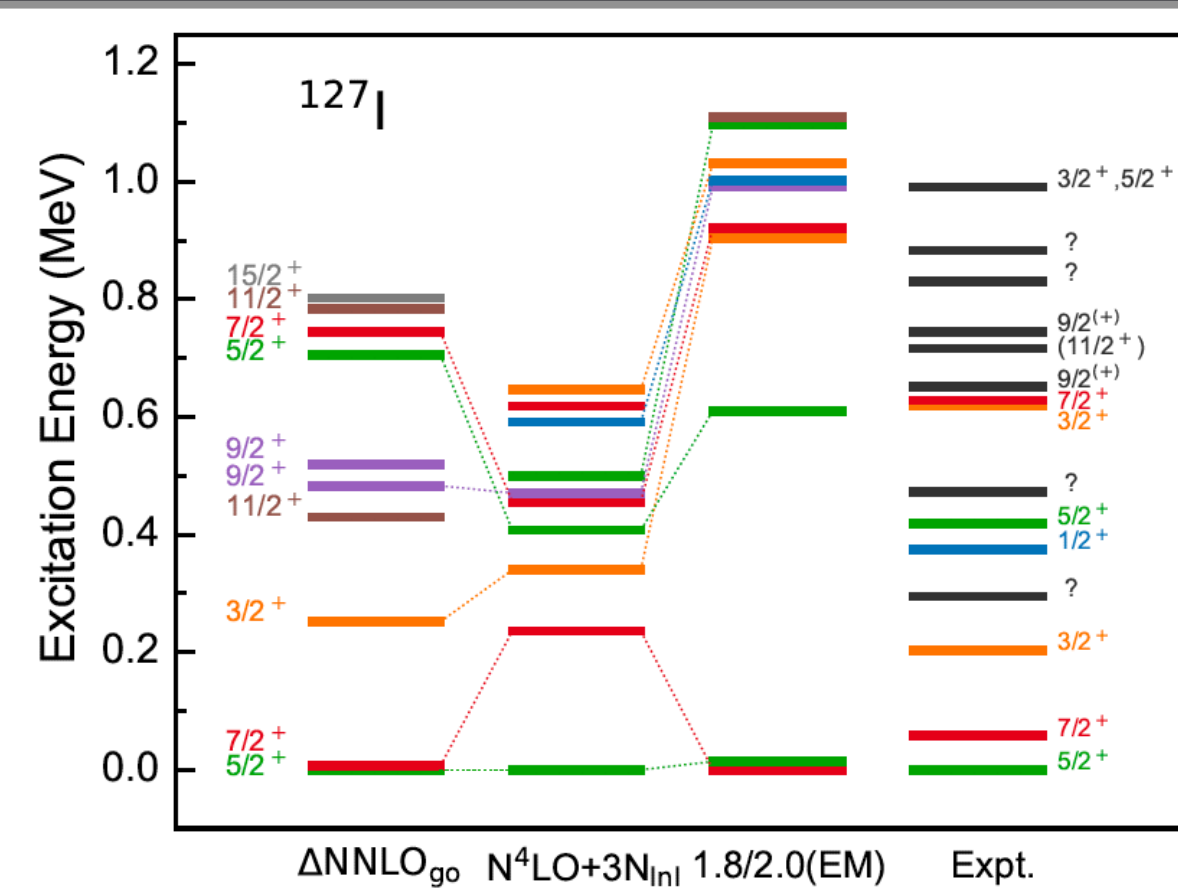
(a)



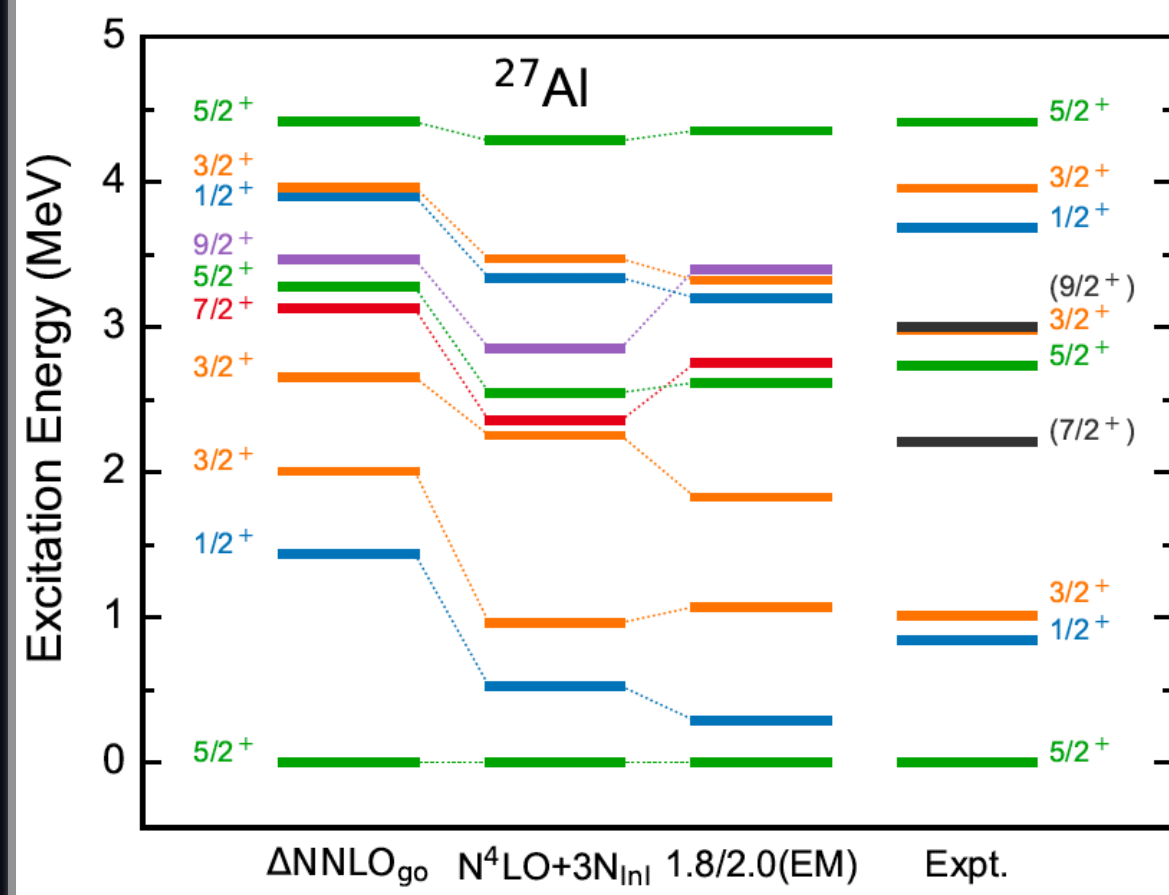
(b)



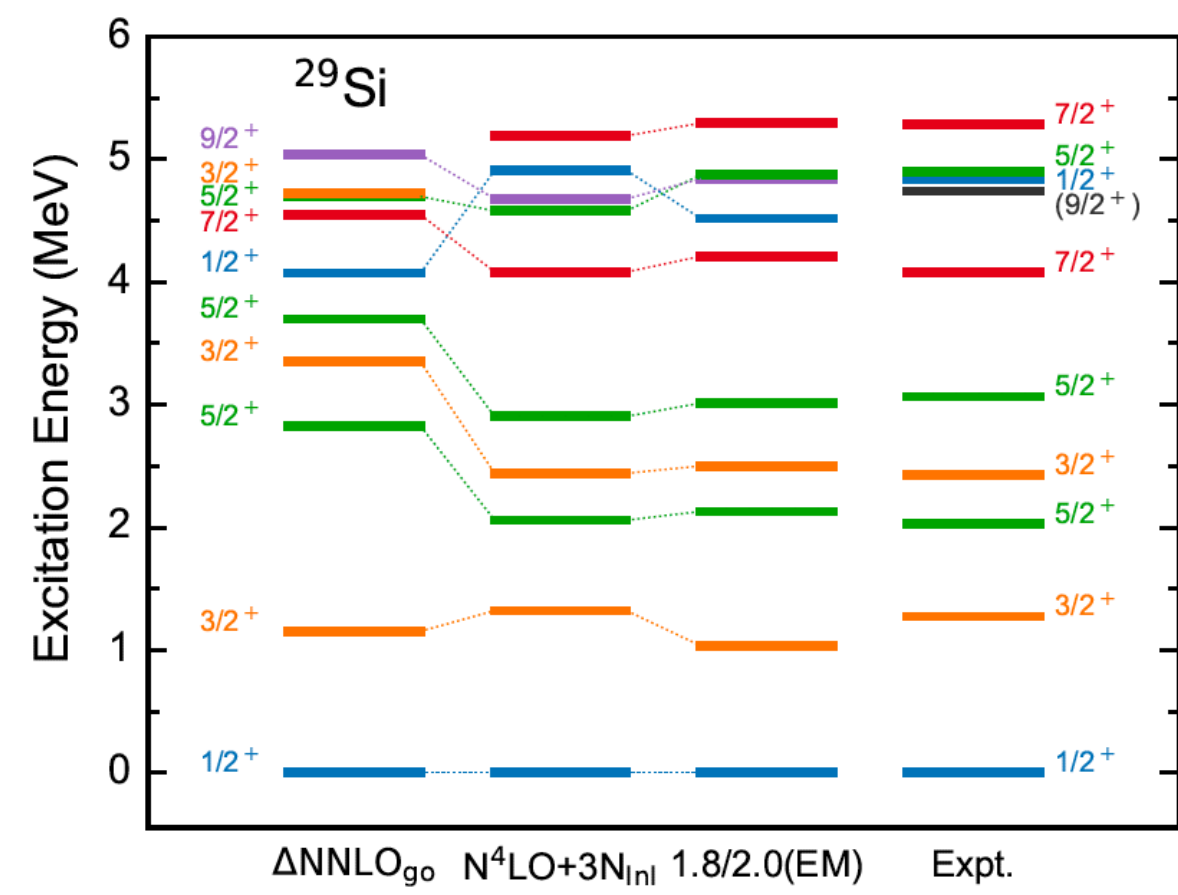
(e)



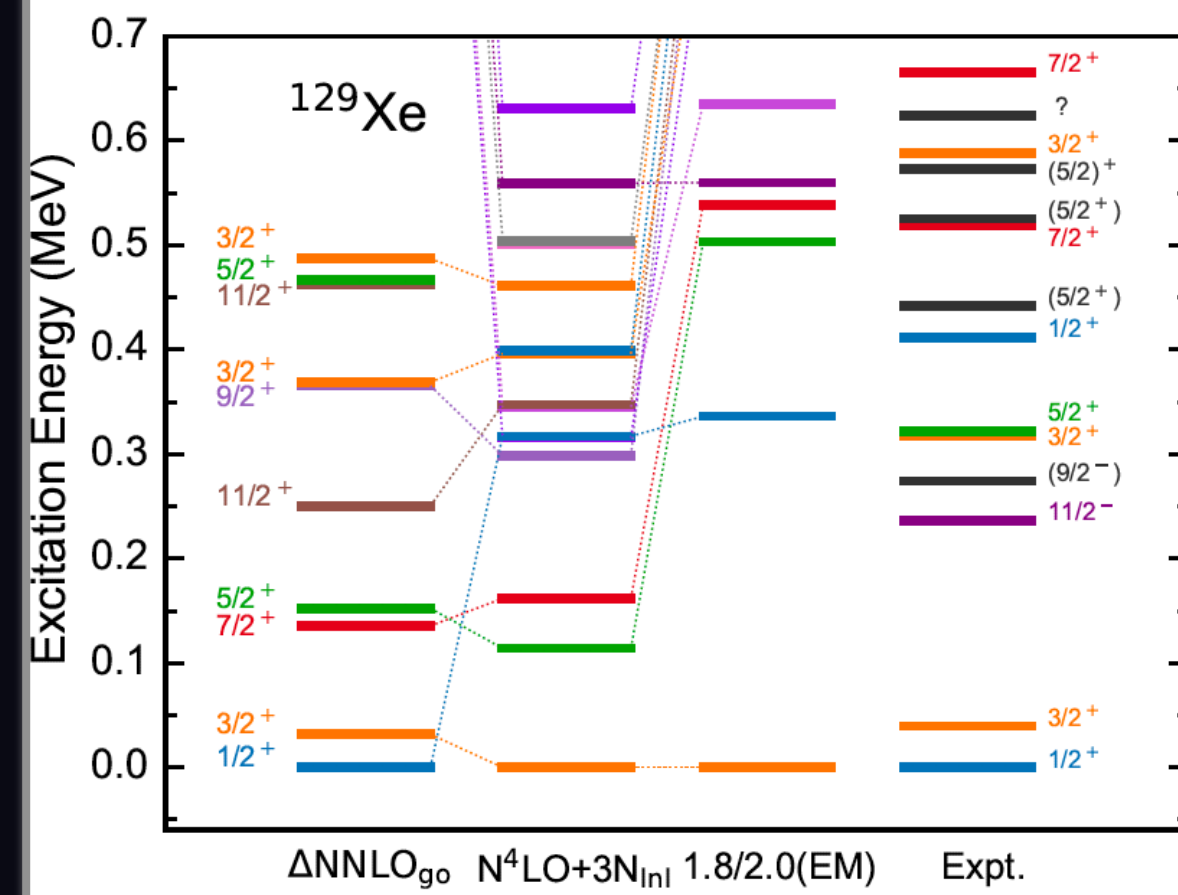
(f)



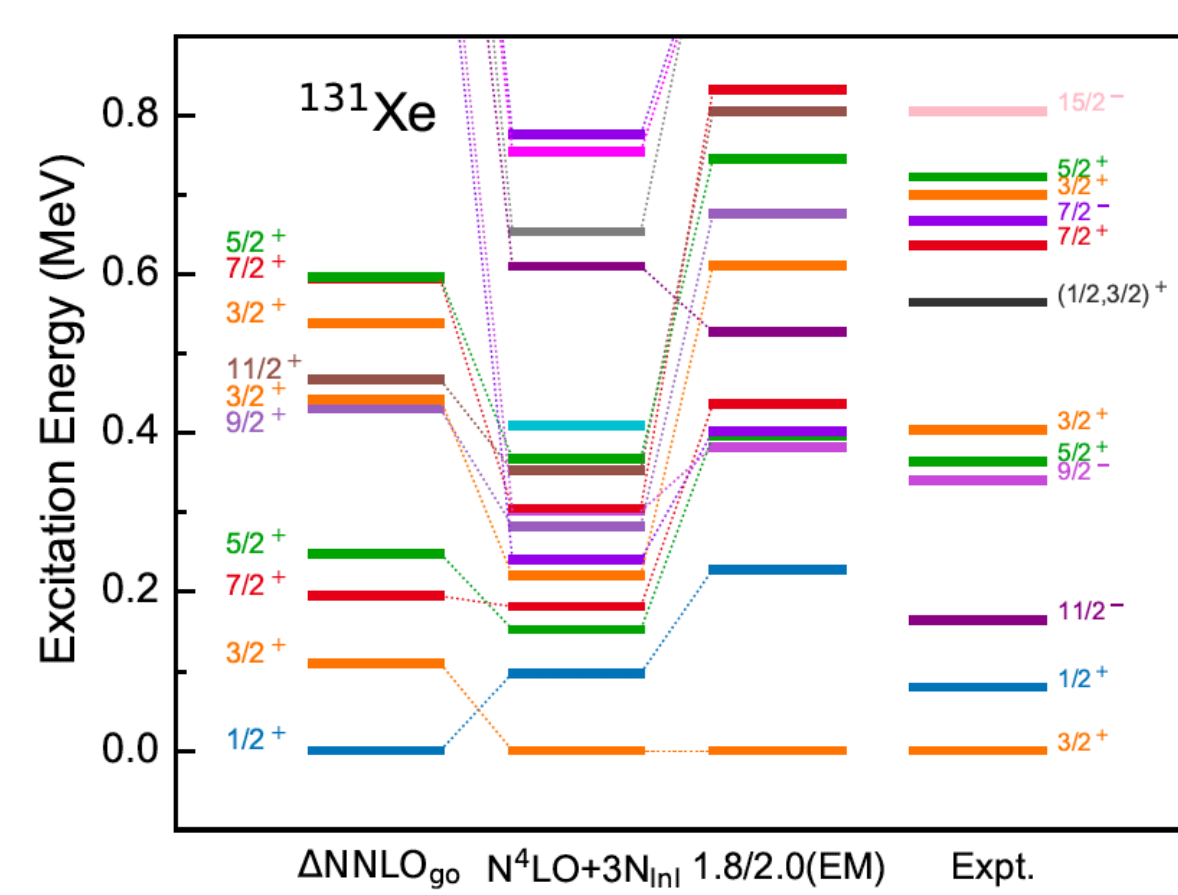
(c)



(d)



(g)



(h)

$\hbar\omega=16$  MeV,  $E3_{\text{max}}=22$