

Neutrinoless double-beta decay from an ab initio (and machine learning) perspective

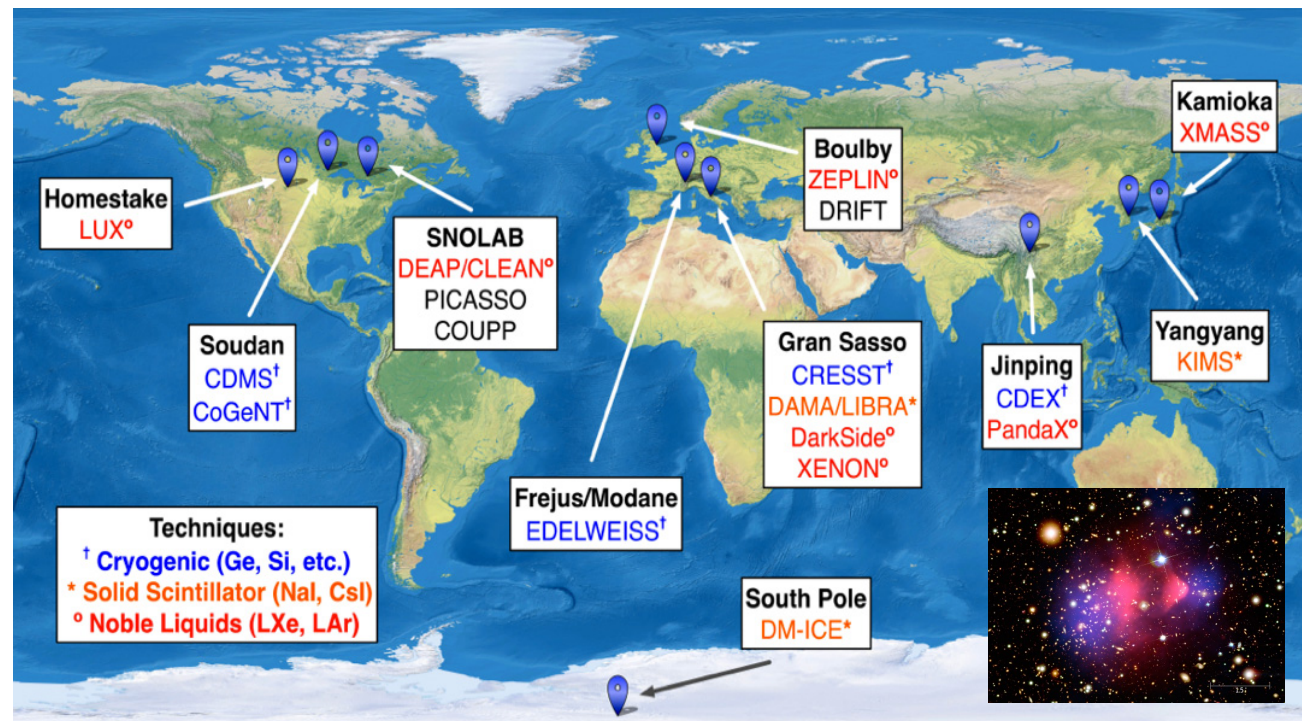
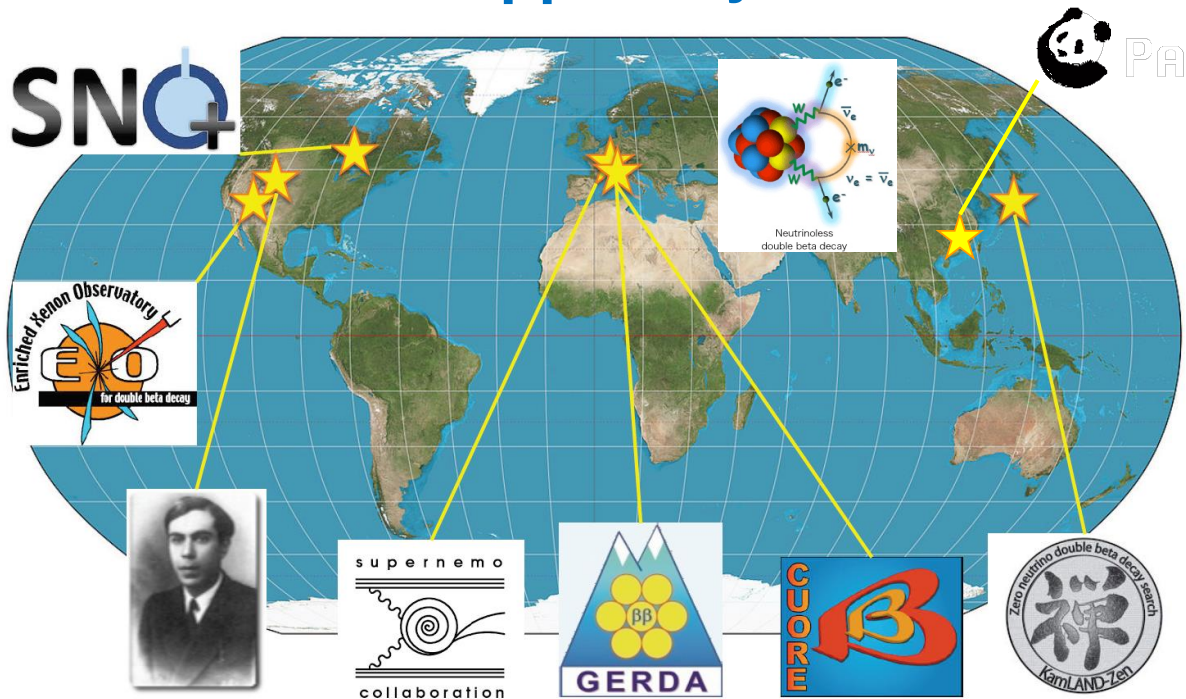
Jason D. Holt
TRIUMF, Theory Department
INT Program: New Physics Searches
'May 19, 2023



Worldwide searches for BSM physics involving neutrinos and dark matter

$0\nu\beta\beta$ Decay

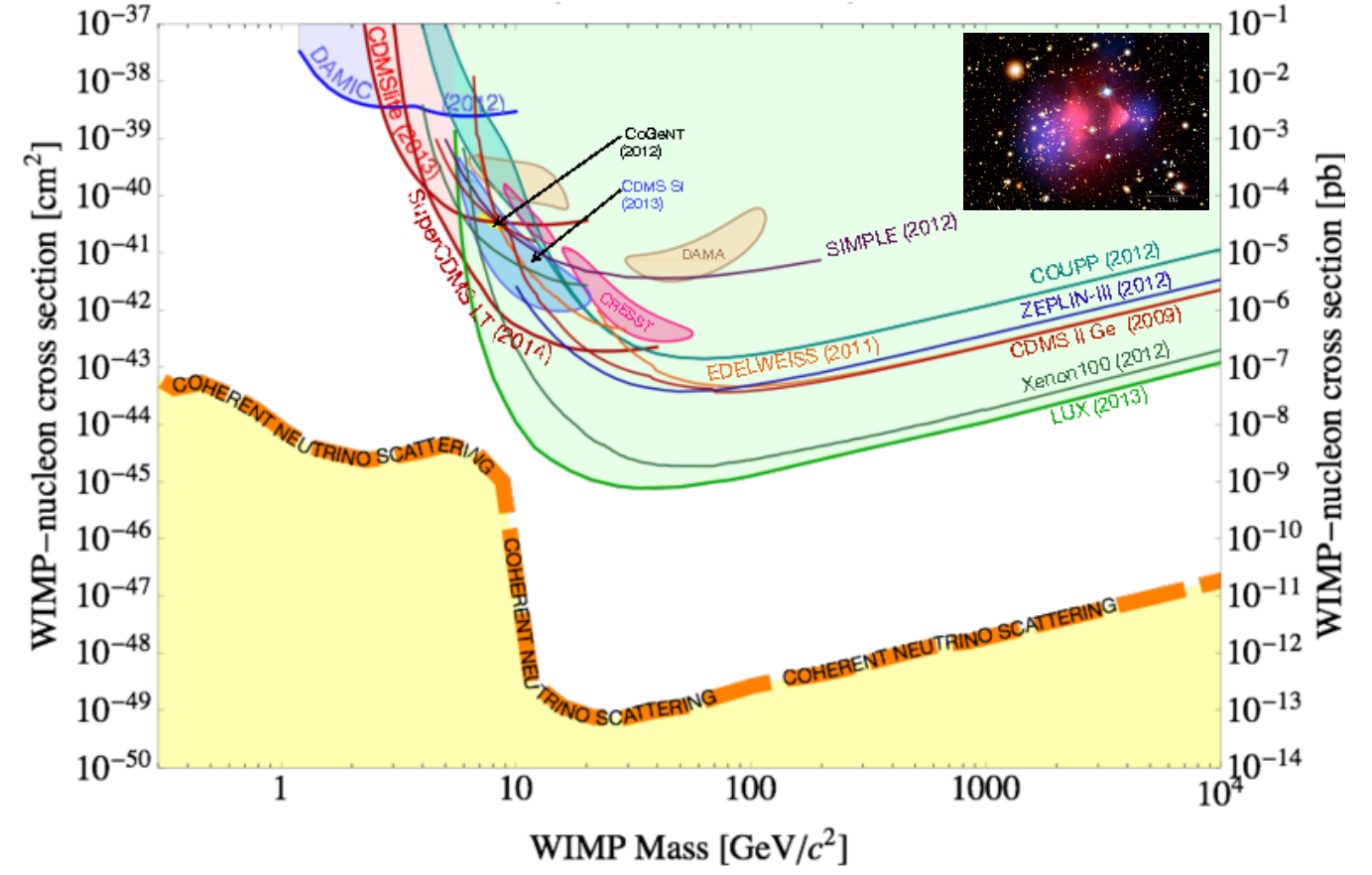
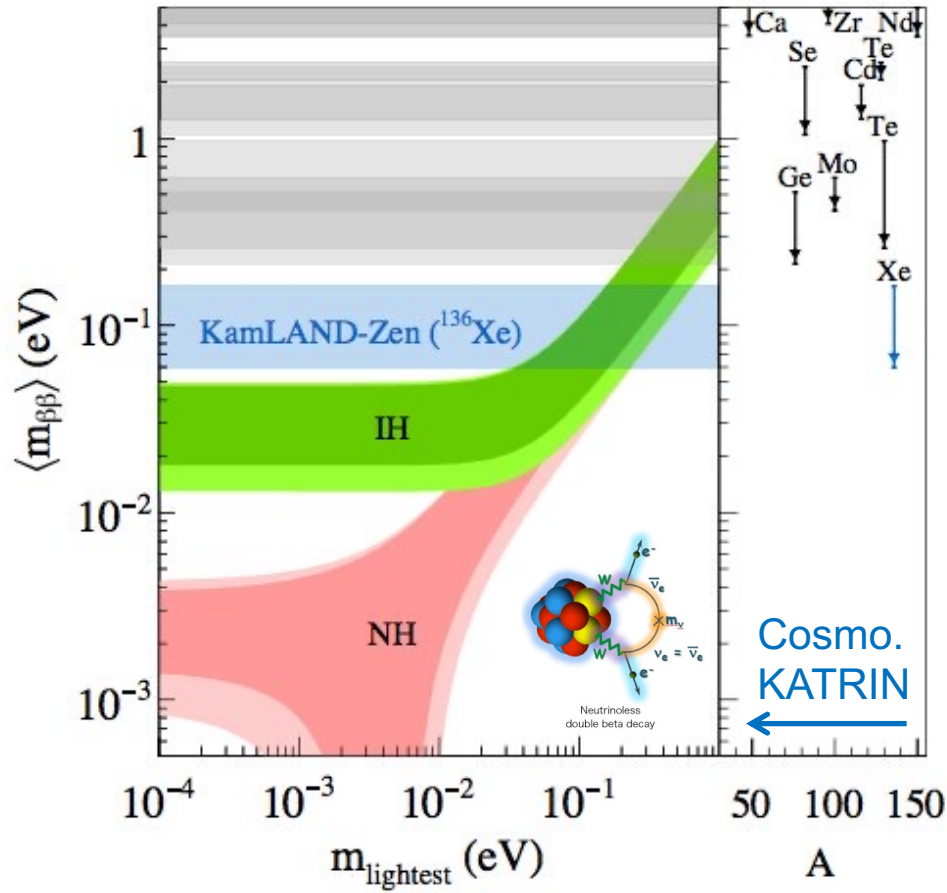
Dark Matter Direct Detection



Billions invested worldwide

Theory essential for: strategic planning for discovery (**motivation**) + **interpretation**

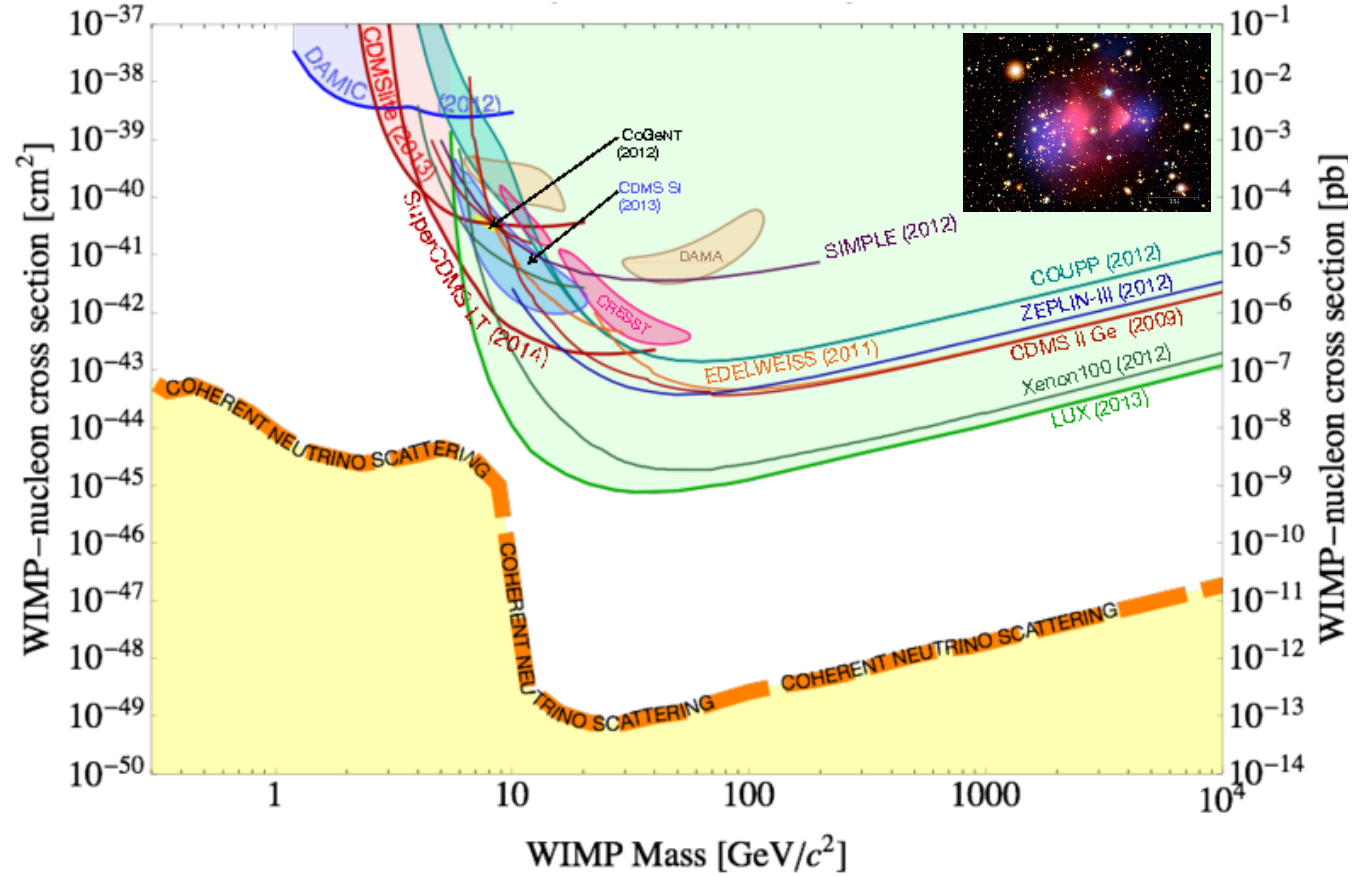
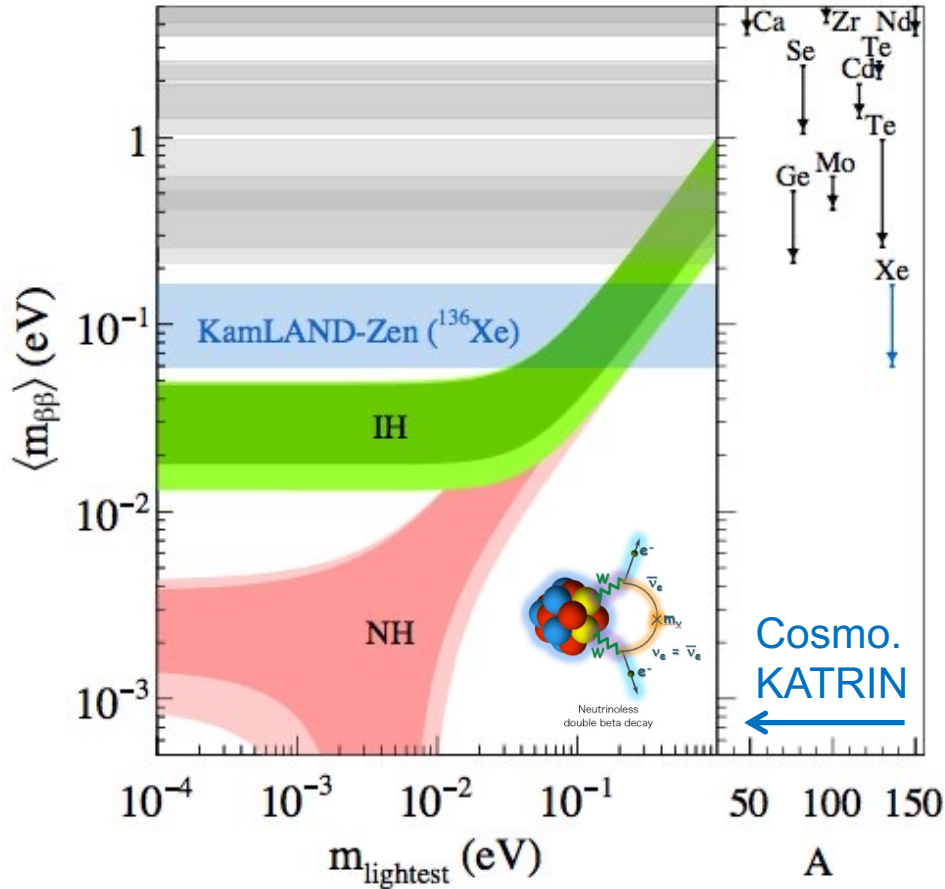
Exclusion plots for $0\nu\beta\beta$ decay + WIMP/ ν scattering require nuclear theory



$$\left(T_{1/2}^{0\nu\beta\beta}\right)^{-1} = G^{0\nu} |M^{0\nu}|^2 \langle m_{\beta\beta} \rangle^2$$

$$\frac{d\sigma}{dq^2} = \frac{8G_F^2}{(2J+1)v^2} S_A(\mathbf{q}^2)$$

Exclusion plots for $0\nu\beta\beta$ decay + WIMP/ ν scattering require nuclear theory



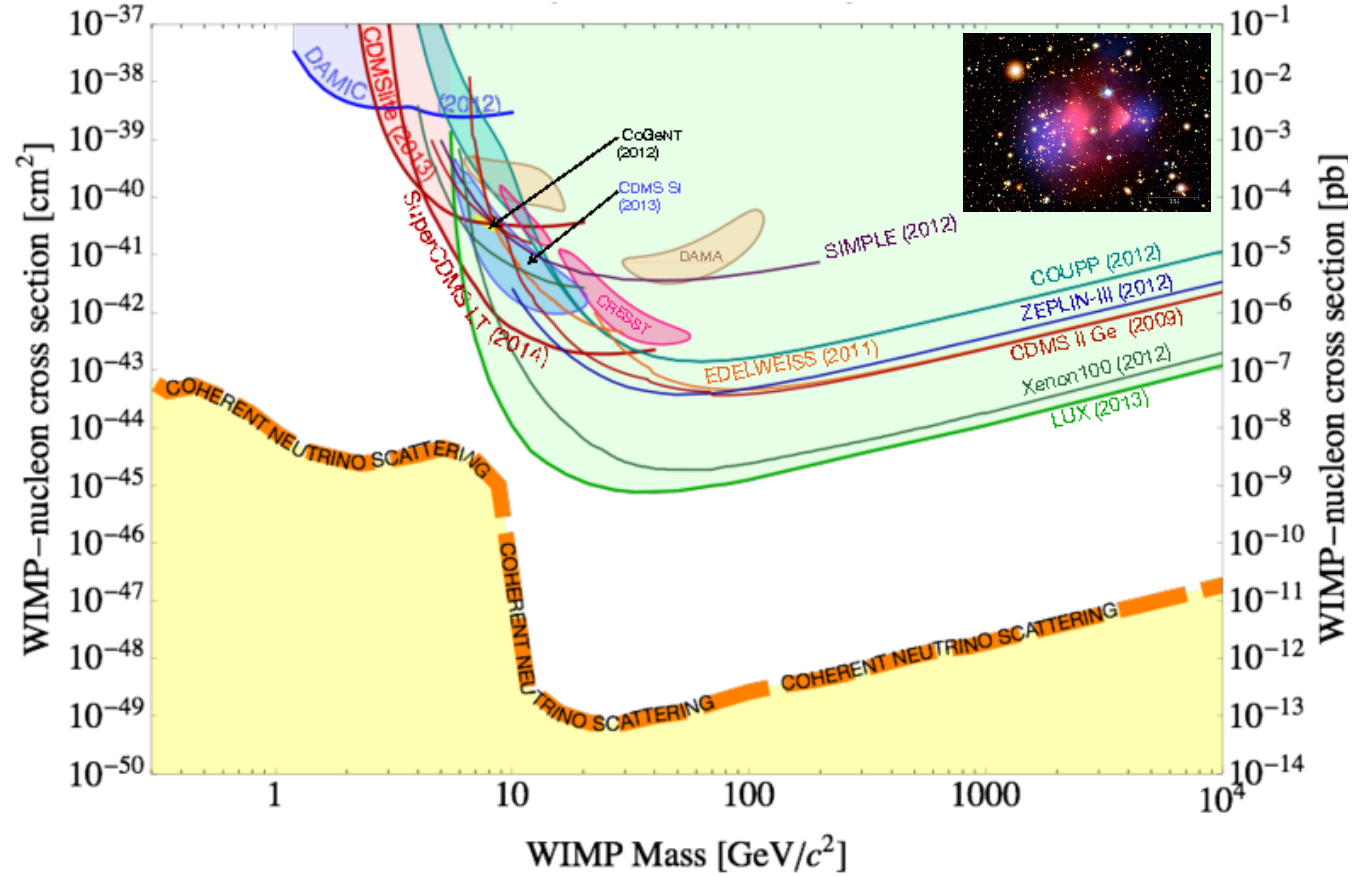
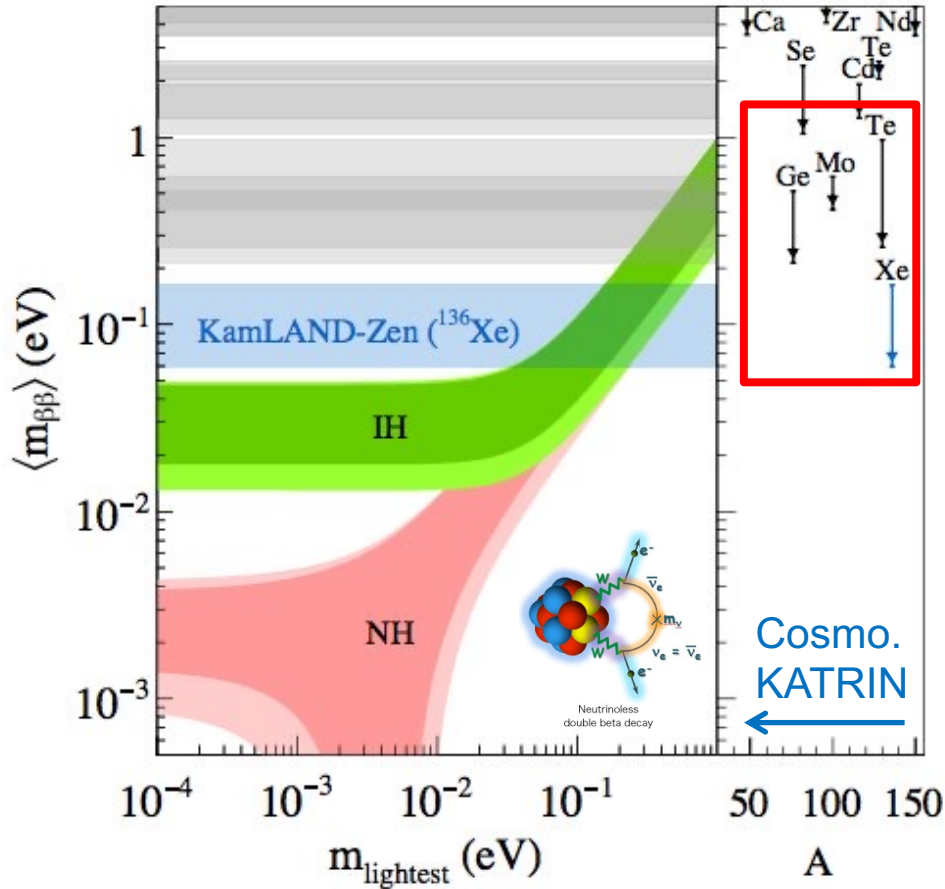
$$\left(T_{1/2}^{0\nu\beta\beta}\right)^{-1} = G^{0\nu} \left|M^{0\nu}\right|^2 \langle m_{\beta\beta} \rangle^2$$

Nuclear matrix element: rate of decay

$$\frac{d\sigma}{dq^2} = \frac{8G_F^2}{(2J+1)v^2} S_A(\mathbf{q}^2)$$

Structure functions for WIMP/ ν scattering

Exclusion plots for $0\nu\beta\beta$ decay + WIMP/ ν scattering require nuclear theory



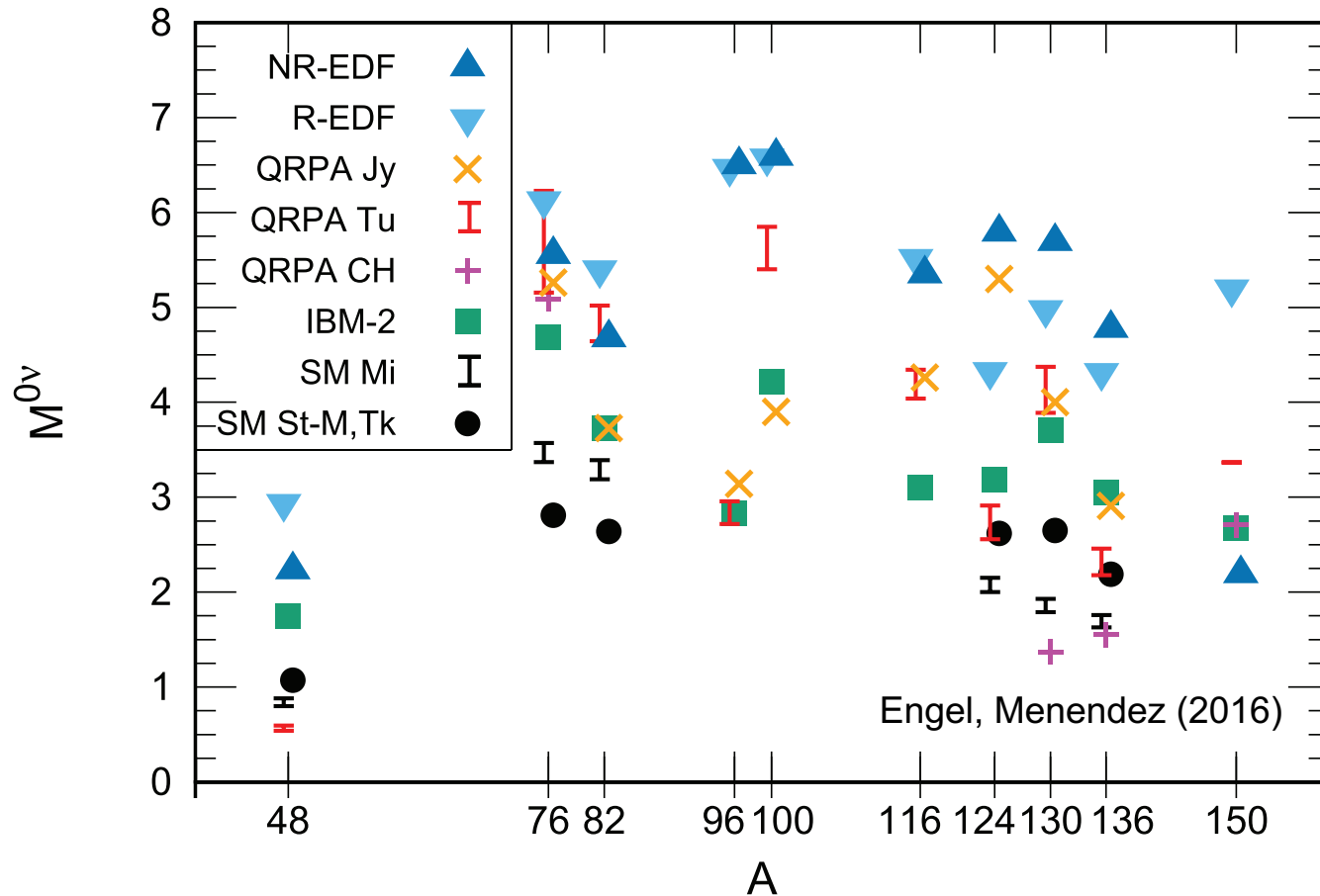
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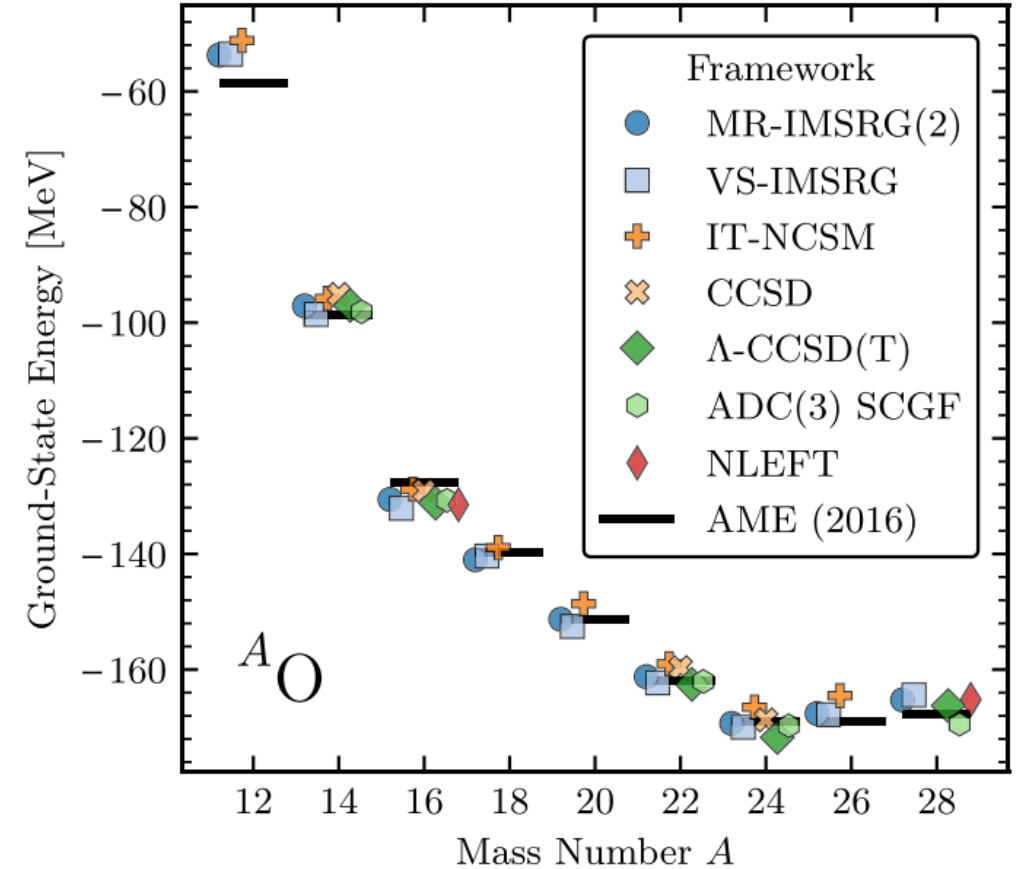
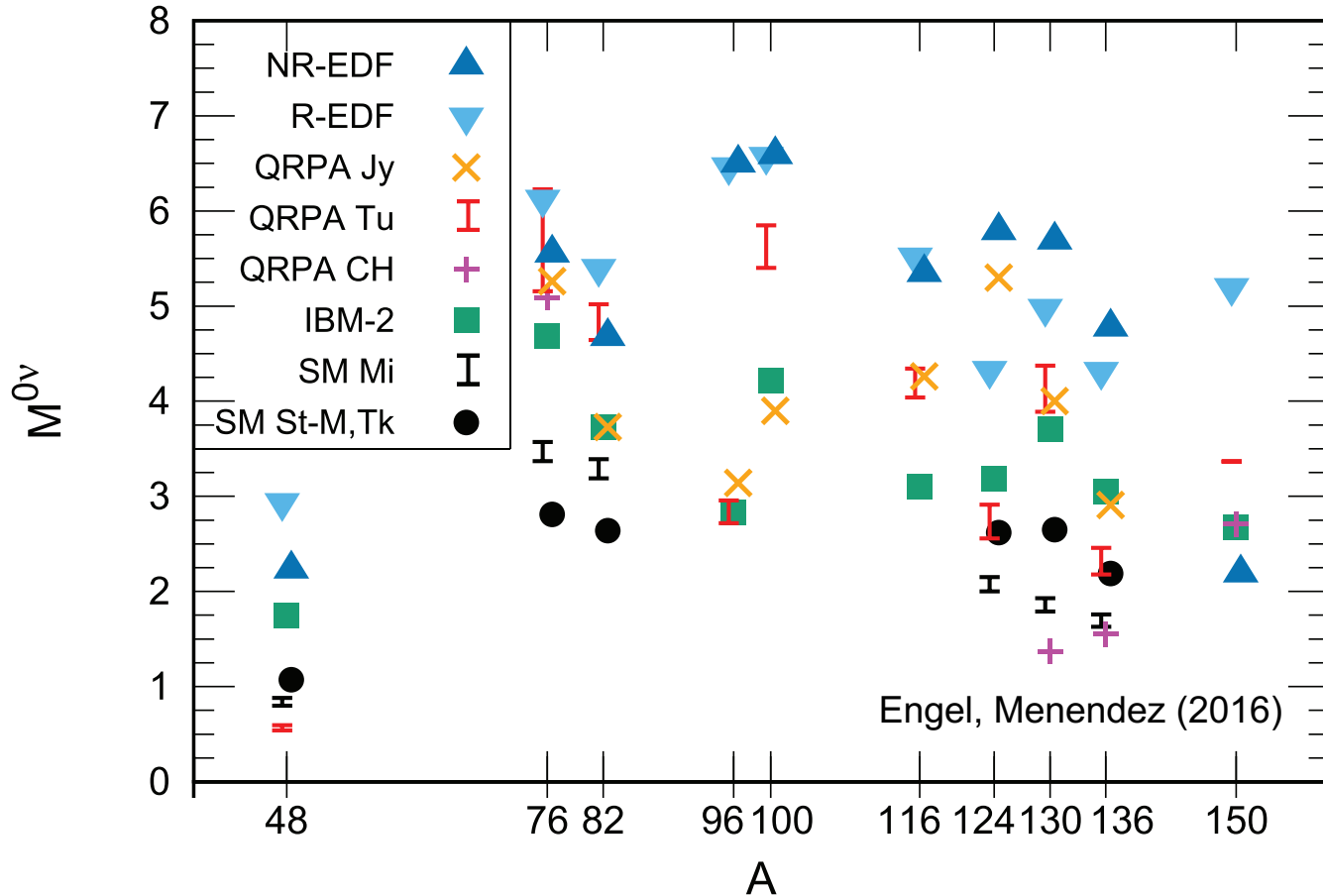
Structure functions for WIMP/ ν scattering

All calculations to date from **extrapolated** phenomenological models; large spread in results



All models missing essential physics: correlations, single-particle levels, two-body currents

All calculations to date from extrapolated phenomenological models; large spread in results

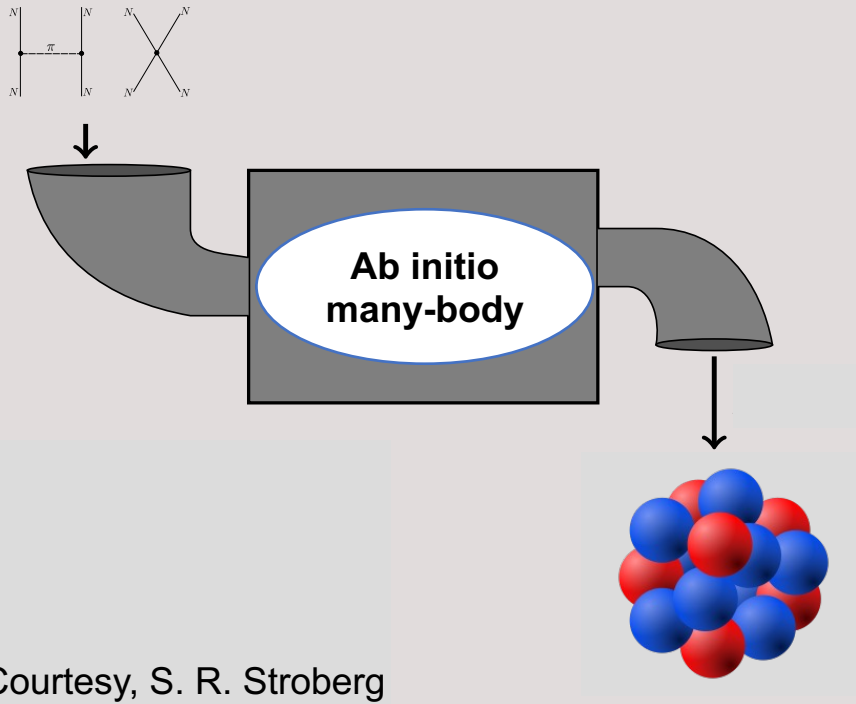


Rethink approach to NME calculations: **ab initio theory** consistent when extrapolated

Aim of modern nuclear theory: develop unified *first-principles* picture of structure and reactions

(Approximately) solve nonrelativistic Schrödinger equation

$$H\psi_n = E_n\psi_n$$

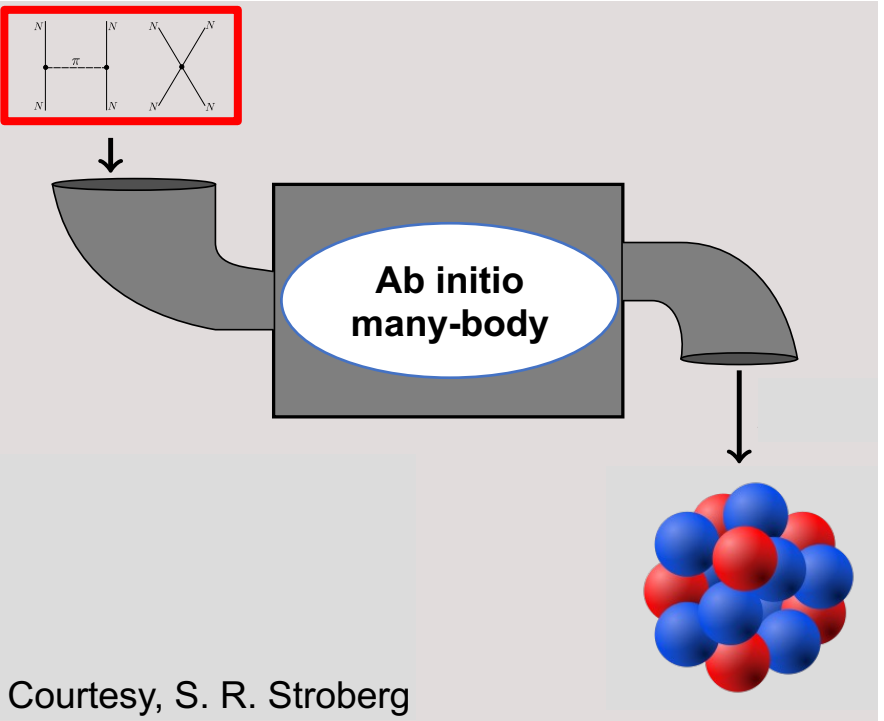
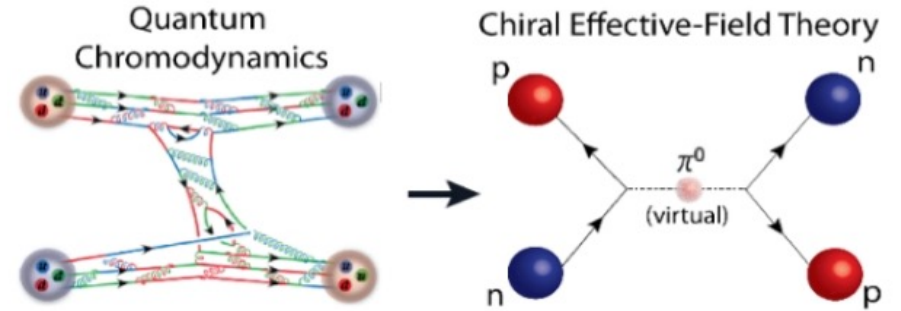


Courtesy, S. R. Stroberg

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Chiral Effective Field Theory

- Consistent treatment of
- 2N, 3N, 4N, ... forces
- Electroweak physics

Quantifiable uncertainties

Interactions

1.8/2.0, N2LO_{GO}, N3LO_{LNL}

(2.0/2.0, N4LO_{LNL})

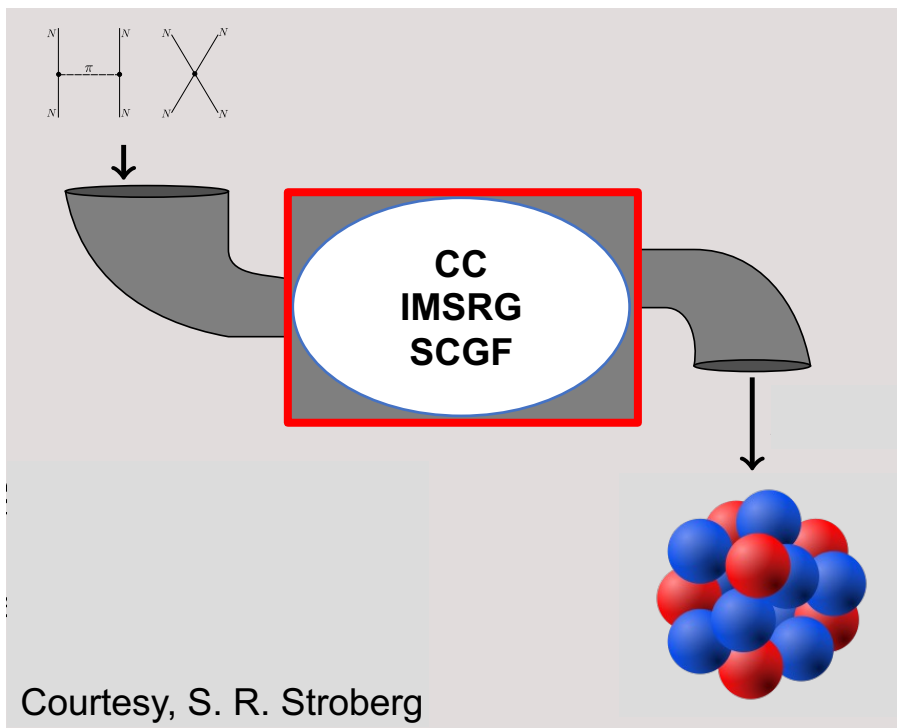
34 non-implausible

	NN force	NNN force	NNNN force
Q ⁰ LO			
Q ² NLO			
Q ³ N ² LO			
Q ⁴ N ³ LO			

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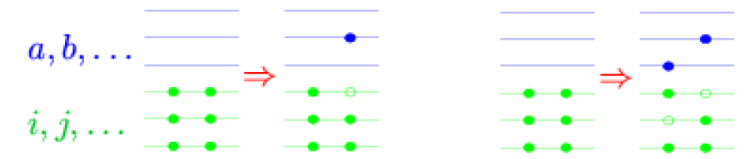
$$H\psi_n = E_n\psi_n$$



Courtesy, S. R. Stroberg

Ab Initio Cheat Sheet (polynomial scaling methods)

CC: Coupled cluster theory



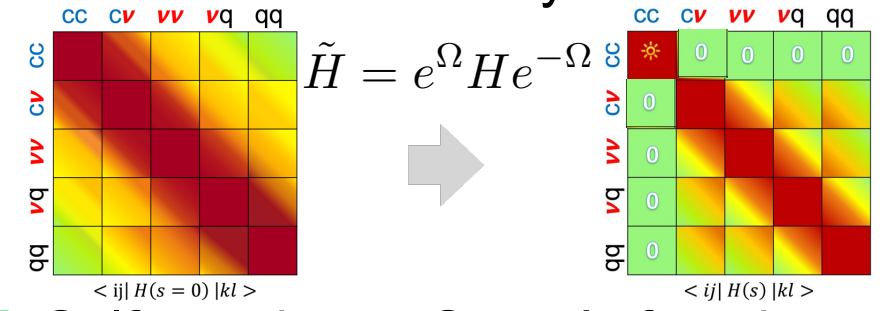
$$E = \langle \Phi | \bar{H} | \Phi \rangle$$

$$0 = \langle \Phi_i^a | \bar{H} | \Phi \rangle$$

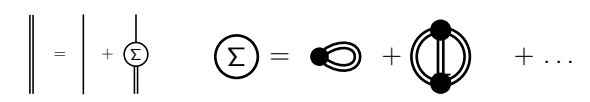
$$0 = \langle \Phi_{ij}^{ab} | \bar{H} | \Phi \rangle$$

$$\bar{H} \equiv e^{-T} H e^T = (H e^T)_c$$

IMSRG: In-medium similarity renormalization group



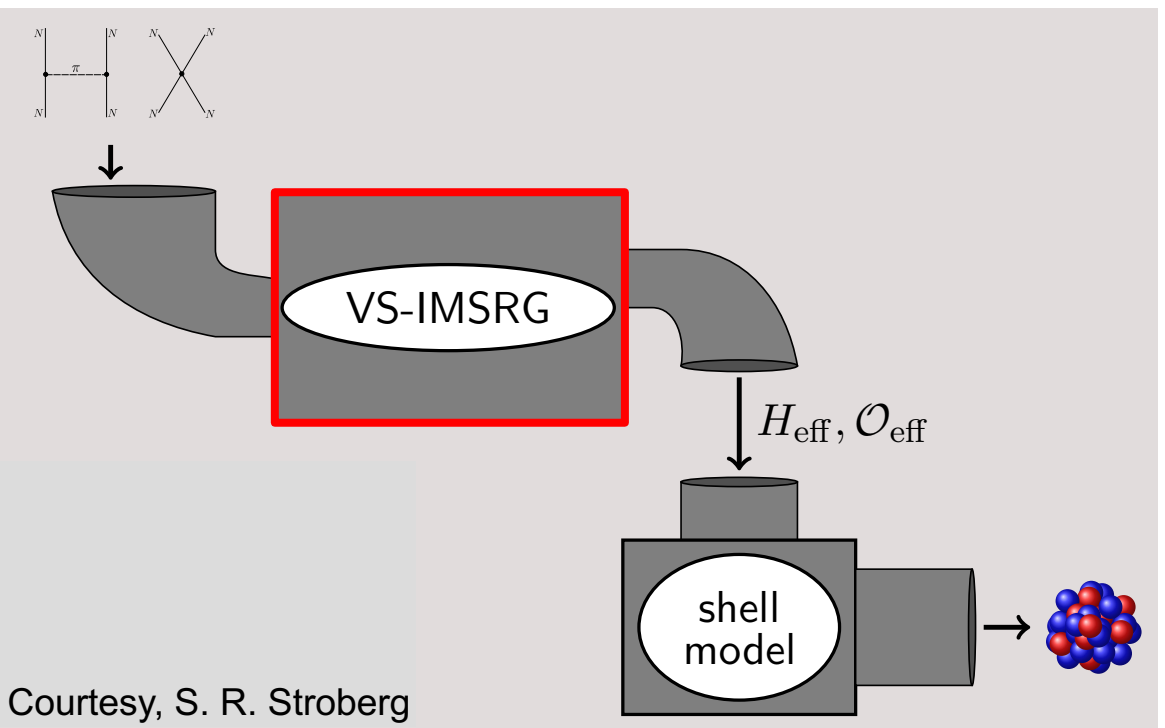
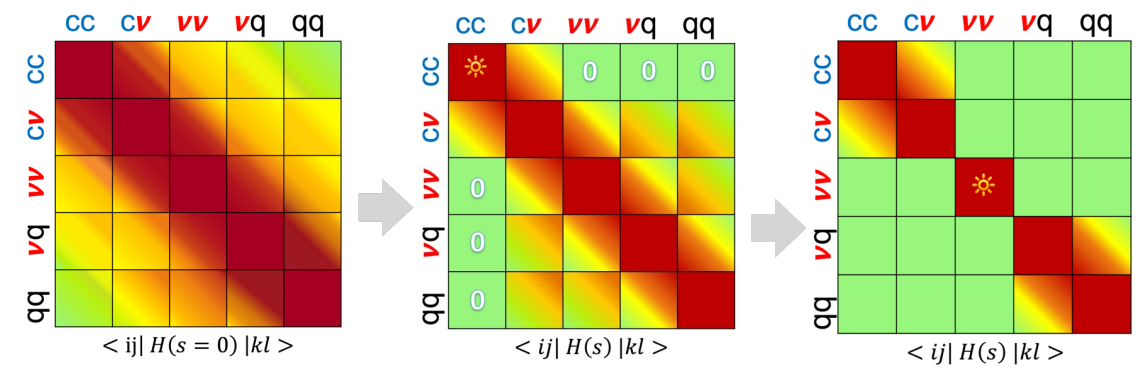
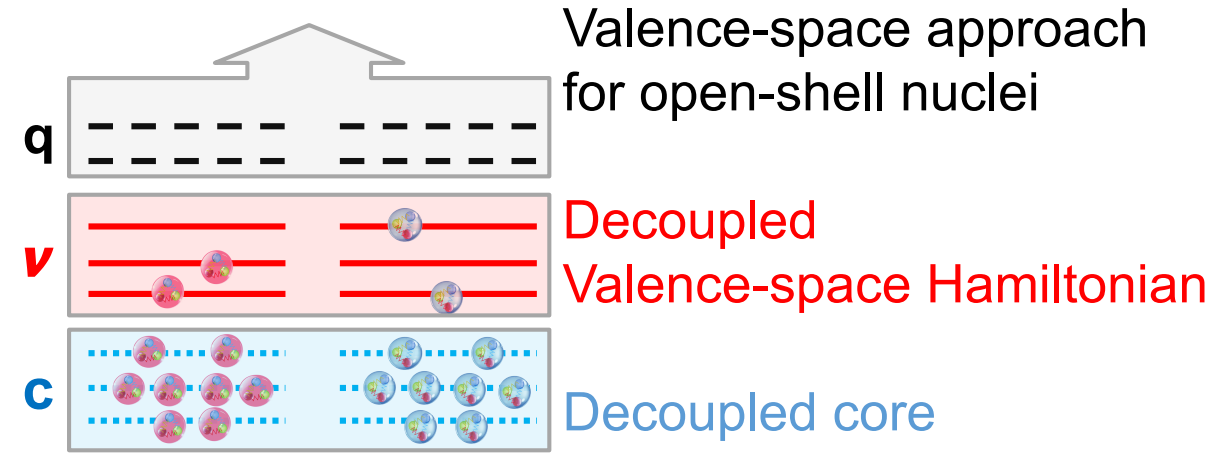
SCGF: Self-consistent Green's function



Aim of modern nuclear theory: develop unified *first-principles* picture of structure and reactions

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Courtesy, S. R. Stroberg

Extends ab initio to scope of traditional nuclear shell model

Explicitly construct unitary transformation from sequence of rotations

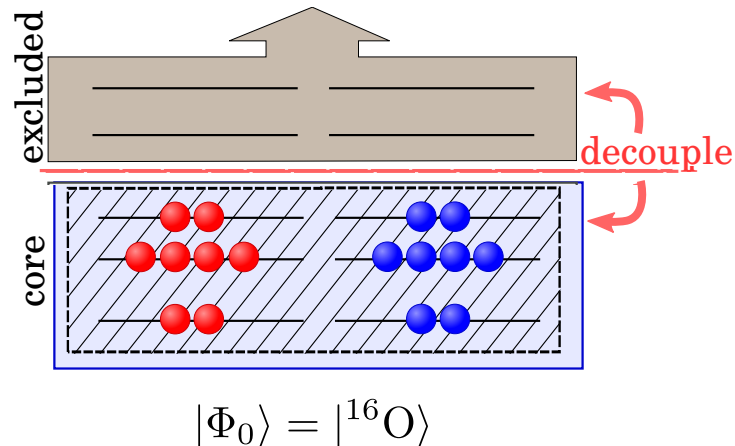
$$U = e^{\Omega} = e^{\eta_n} \dots e^{\eta_1} \quad \eta = \frac{1}{2} \arctan \left(\frac{2H_{\text{od}}}{\Delta} \right) - \text{h.c.}$$

$$\tilde{H} = e^{\Omega} H e^{-\Omega} = H + [\Omega, H] + \frac{1}{2} [\Omega, [\Omega, H]] + \dots$$

All operators truncated at two-body level IMSRG(2)
IMSRG(3) in progress

Tsukiyama, Bogner, Schwenk, PRC 2012
 Morris, Parzuchowski, Bogner, PRC 2015

Step 1: Decouple core



Can we achieve accuracy
of large-space methods?

$$\langle \tilde{\Psi}_n | P \tilde{H} P | \tilde{\Psi}_n \rangle \approx \langle \Psi_i | H | \Psi_i \rangle$$

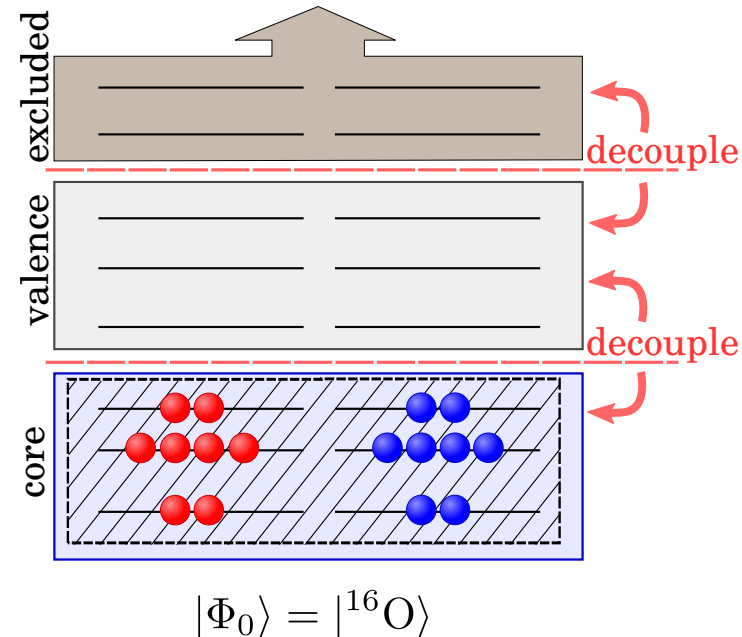
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Step 1: Decouple core

Step 2: Decouple valence space

Can we achieve accuracy
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$$\langle \tilde{\Psi}_n | P \tilde{H} P | \tilde{\Psi}_n \rangle \approx \langle \Psi_i | H | \Psi_i \rangle$$

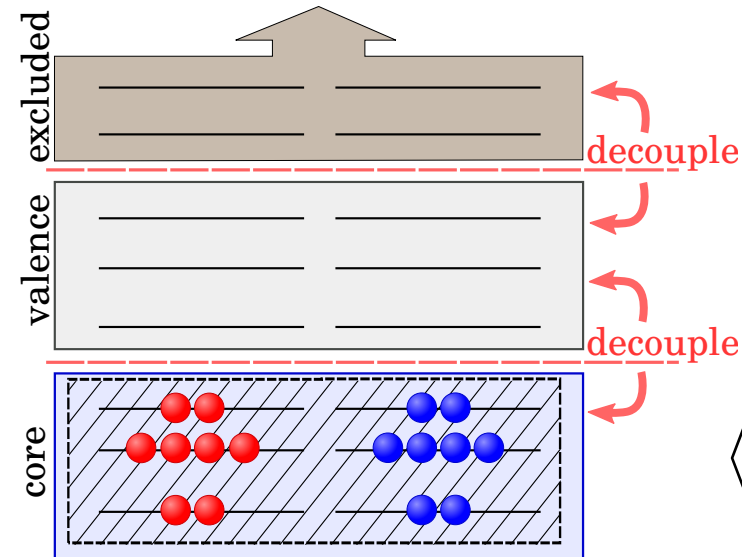
$\langle P H P \rangle$	$\langle P H Q \rangle \rightarrow 0$
$\langle Q H P \rangle \rightarrow 0$	$\langle Q H Q \rangle$

Explicitly construct unitary transformation from sequence of rotations

$$U = e^\Omega = e^{\eta_n} \dots e^{\eta_1} \quad \eta = \frac{1}{2} \arctan \left(\frac{2H_{\text{od}}}{\Delta} \right) - \text{h.c.}$$

$$\tilde{H} = e^\Omega H e^{-\Omega} = H + [\Omega, H] + \frac{1}{2} [\Omega, [\Omega, H]] + \dots$$

$$\tilde{\mathcal{O}} = e^\Omega \mathcal{O} e^{-\Omega} = \mathcal{O} + [\Omega, \mathcal{O}] + \frac{1}{2} [\Omega, [\Omega, \mathcal{O}]] + \dots$$



Step 1: Decouple core

Step 2: Decouple valence space

Step 3: Decouple additional operators

$$\langle \tilde{\Psi}_n | P \tilde{H} P | \tilde{\Psi}_n \rangle \approx \langle \Psi_i | H | \Psi_i \rangle$$

$$\langle \tilde{\Psi}_n | P \tilde{M}_{0\nu} P | \tilde{\Psi}_n \rangle \approx \langle \Psi_i | M_{0\nu} | \Psi_i \rangle$$

$$|\Phi_0\rangle = |^{16}\text{O}\rangle$$

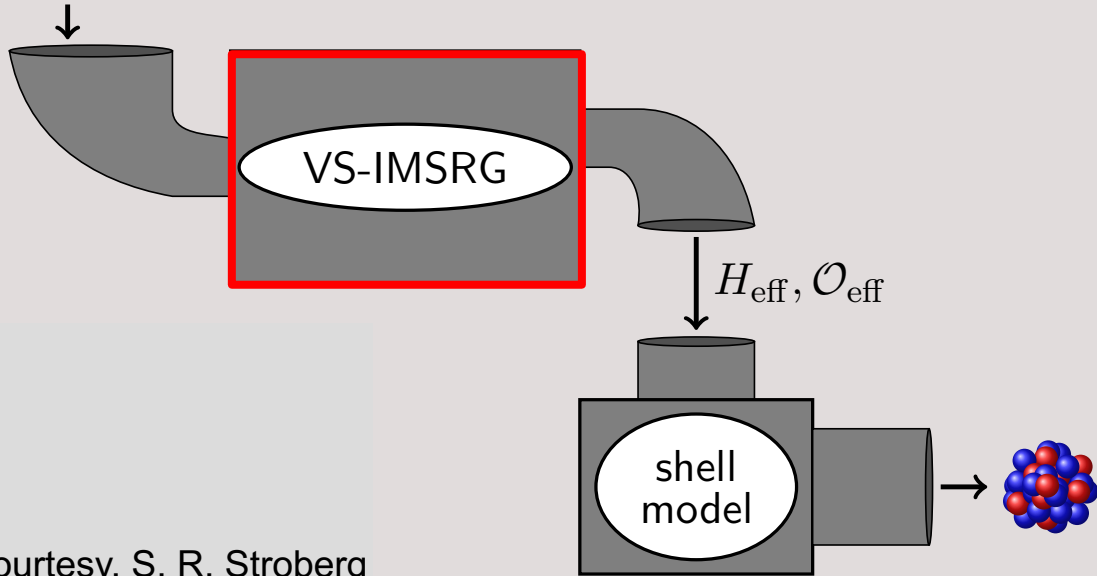
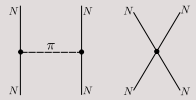
Careful benchmarking essential

$\langle P H P \rangle$	$\langle P H Q \rangle \rightarrow 0$
$\langle Q H P \rangle \rightarrow 0$	$\langle Q H Q \rangle$

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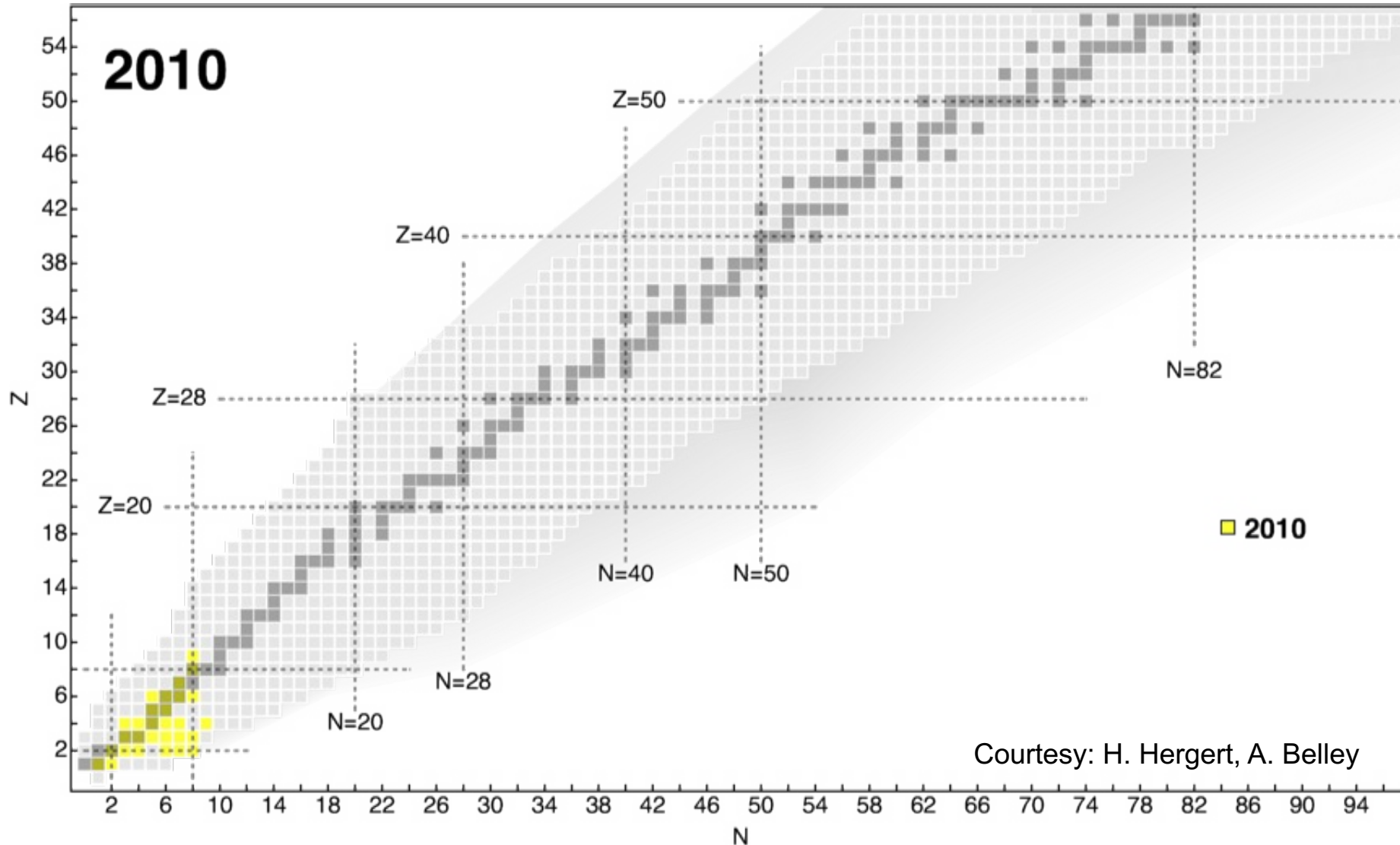


Courtesy, S. R. Stroberg

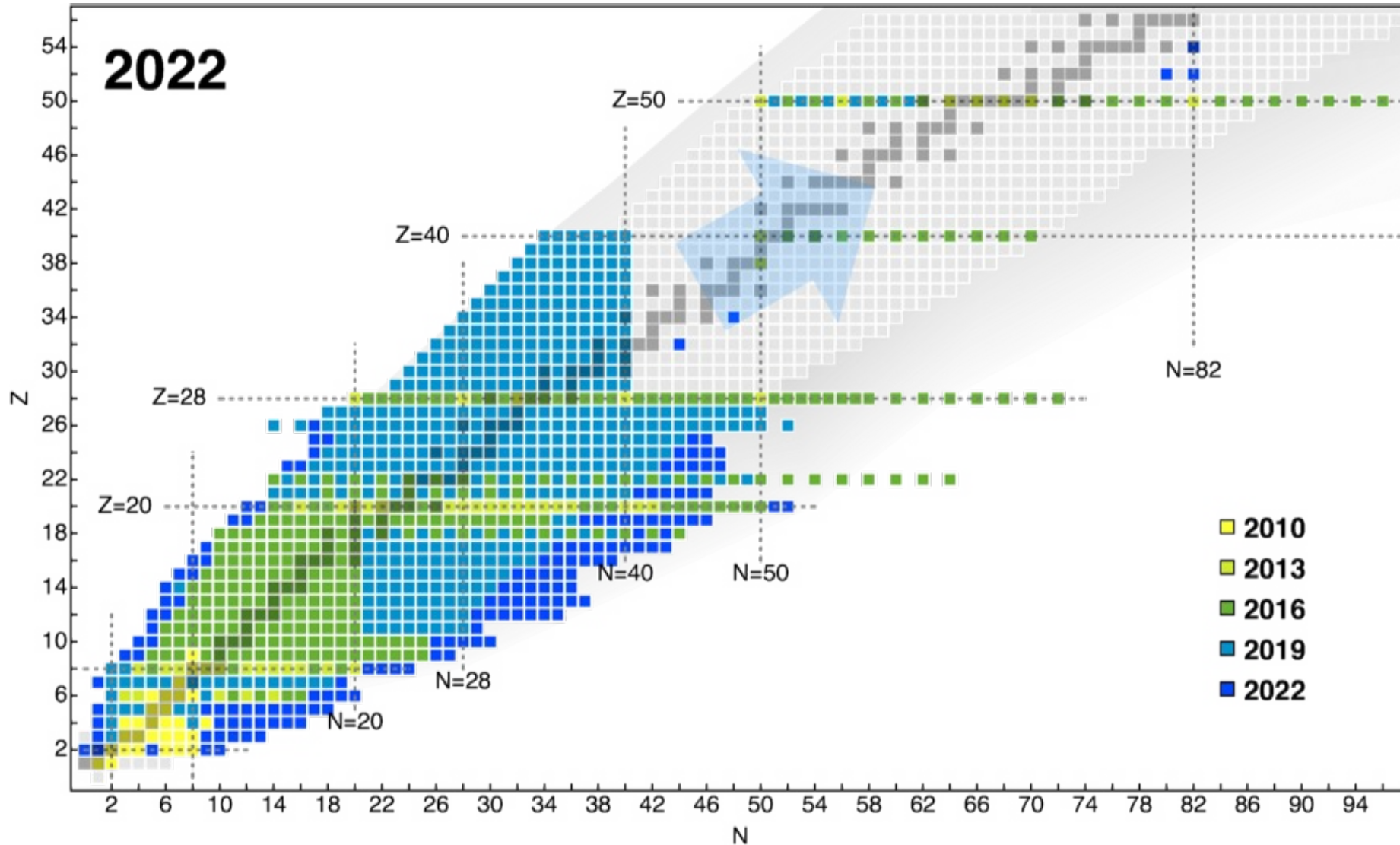
Methods Exact up to Truncations

- ✓ Single-particle basis $e_{\max} = 2n + l$
- ✓ Storage limits of 3N forces $e_1 + e_2 + e_3 \leq E_{3\max}$
- 👤 Many-body operators: e.g., CCSD(T), IMSRG(2)

2010: Limited capabilities for 3N forces; ^{16}O heaviest



Tremendous progress in ab initio reach, largely due to polynomially scaling methods!



Global Ab Initio Calculations: Proton/Neutron Driplines



Featured in Physics

Editors' Suggestion

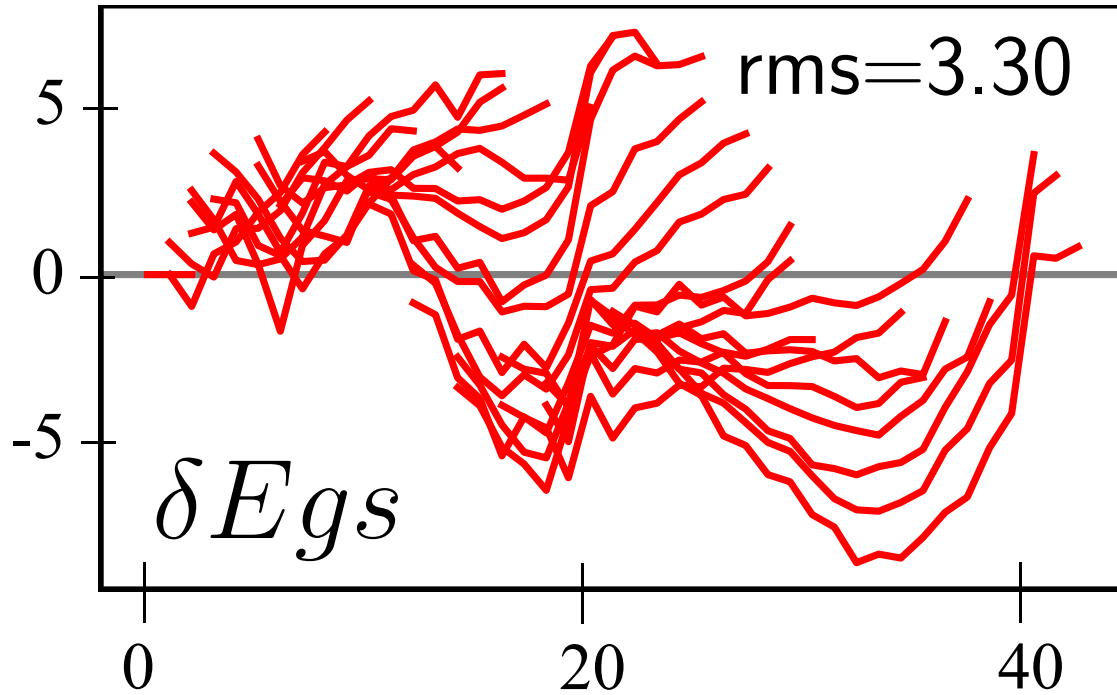
Ab Initio Limits of Atomic Nuclei

S. R. Stroberg, J. D. Holt, A. Schwenk, and J. Simonis
Phys. Rev. Lett. **126**, 022501 – Published 12 January 2021

PhysICS See synopsis: [Predicting the Limits of Atomic Nuclei](#)

Long considered the domain of DFT or shell model

Ab initio calculations of ~700 nuclei from He to Fe!



$$\delta \mathcal{O} \equiv \mathcal{O}^{(th)} - \mathcal{O}^{(exp)}$$

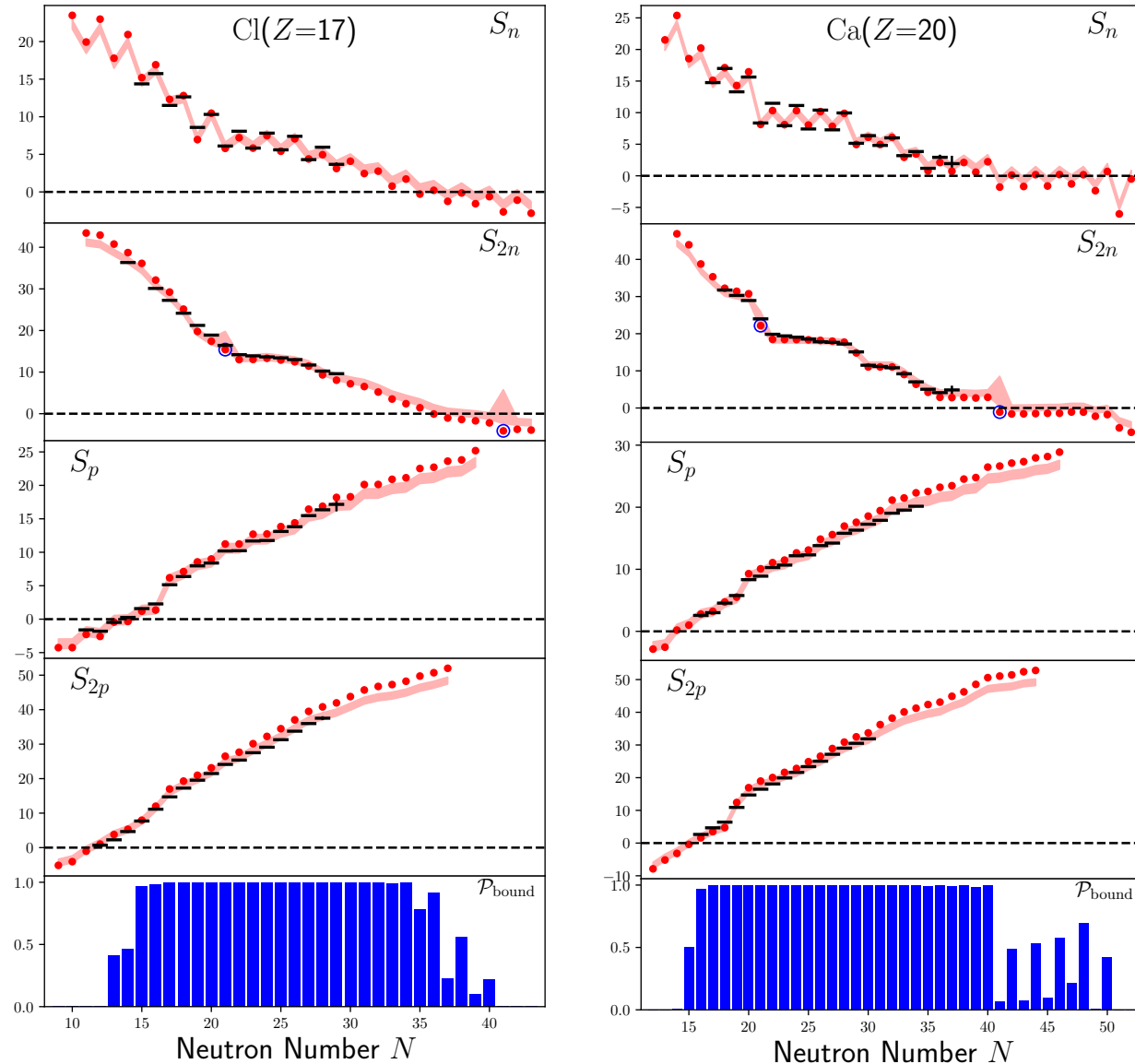
B-W Mass formula: ~3.5 MeV (Z < 28)

DFT: 0.6-2.0 MeV

Input Hamiltonians fit to A=2,3,4 – **not biased towards known data**

Apply to proton/neutron driplines separation energies?

rms deviation from experiment → model for theoretical uncertainties



rms = 0.7-1.4MeV

Obtain PPD for separation energies

$$p(\tilde{S}^{\text{exp}} | \tilde{S}^{\text{th}}, S^{\text{th}}, S^{\text{exp}})$$

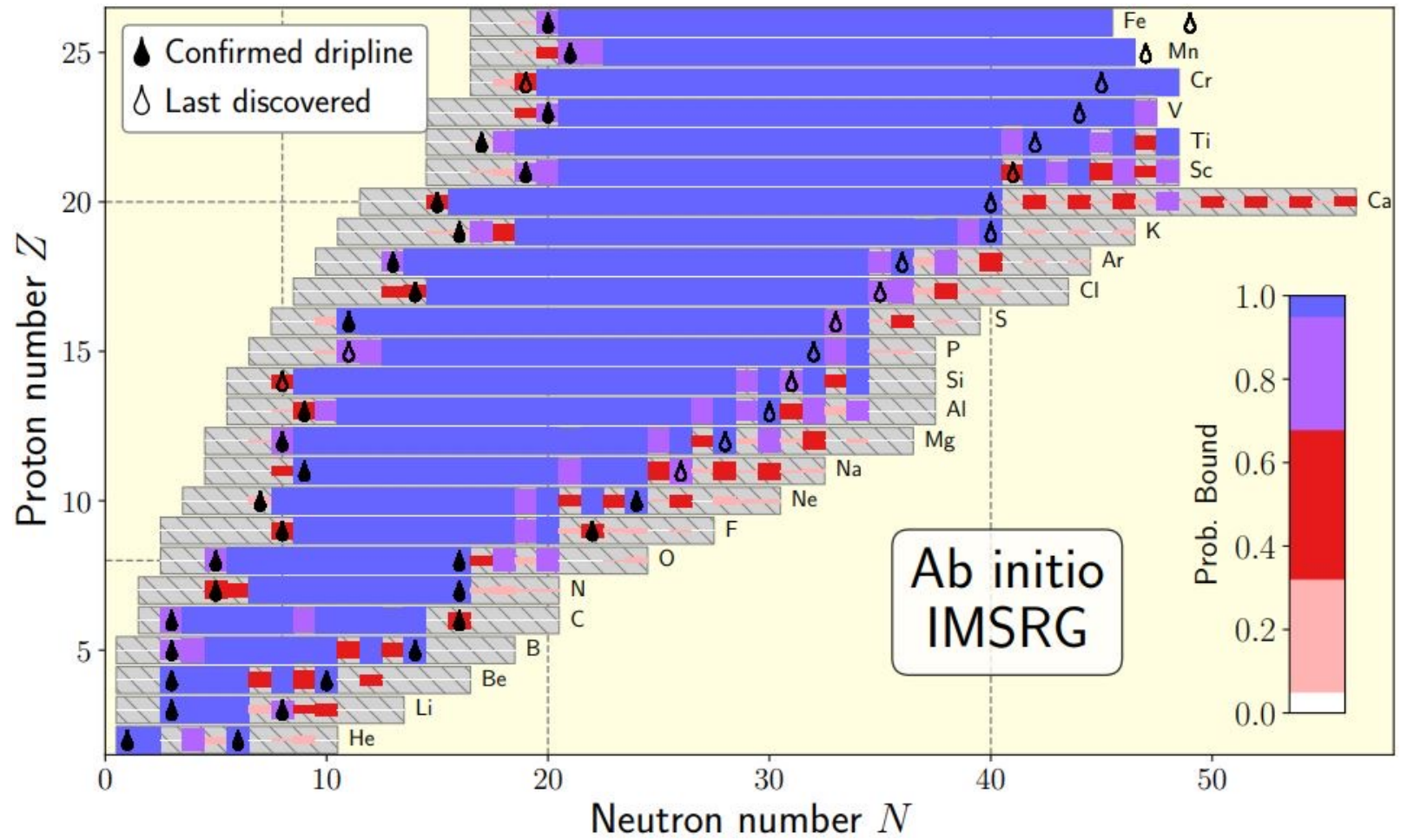
Total probability to be bound

$$\mathcal{P}_{\text{bound}} = \prod_{\alpha} \int_0^{\infty} d\tilde{S}_{\alpha}^{\text{exp}} p(\tilde{S}_{\alpha}^{\text{exp}} | \tilde{S}^{\text{th}}, S^{\text{th}}, S^{\text{exp}})$$

$$\alpha \in \{n, p, 2n, 2p\}$$

Determine probabilities for each nucleus

Predictions of proton and neutron driplines from first principles

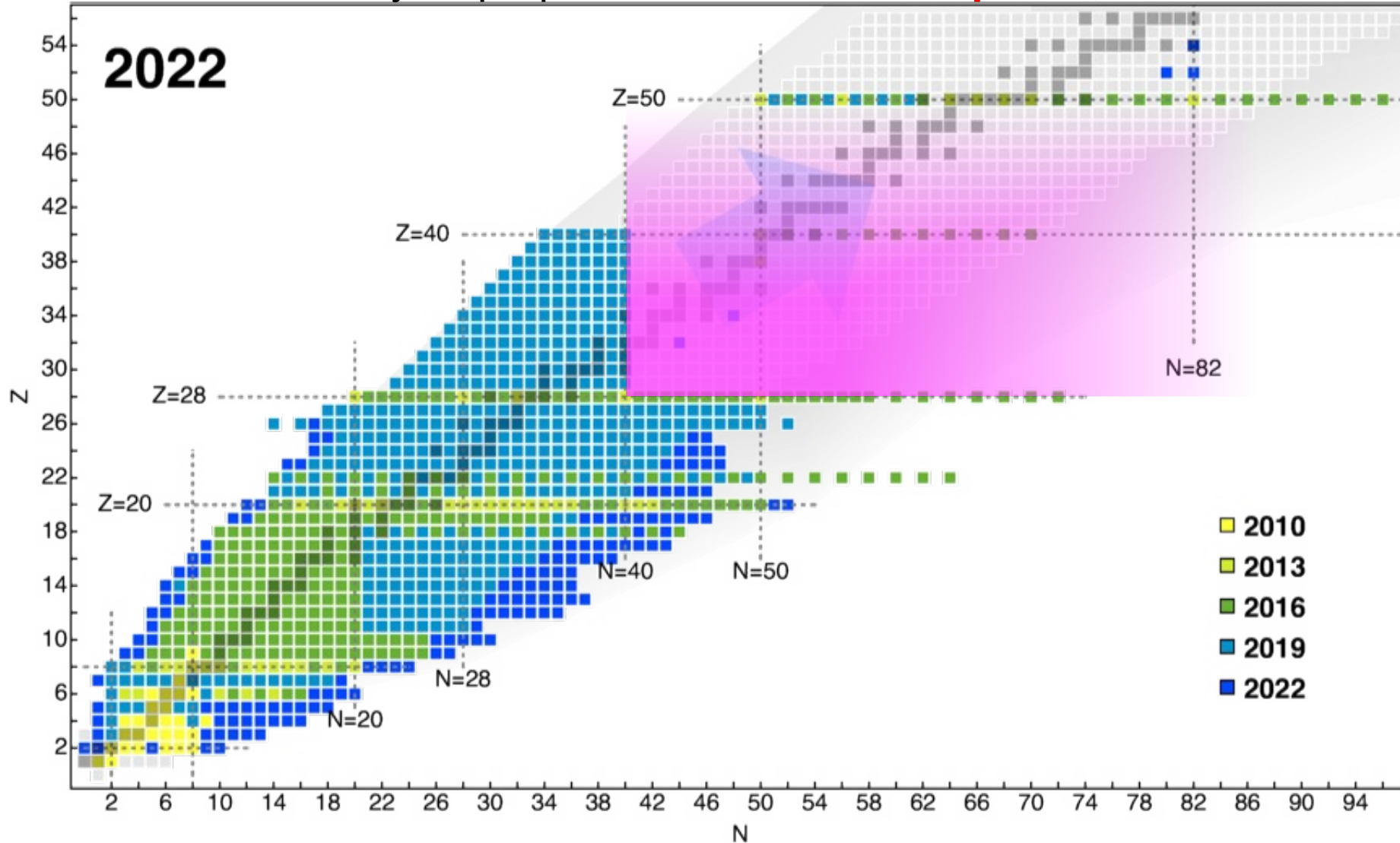


Known drip lines predicted within uncertainties (artifacts at shell closures)

Ab initio guide for neutron-rich driplines

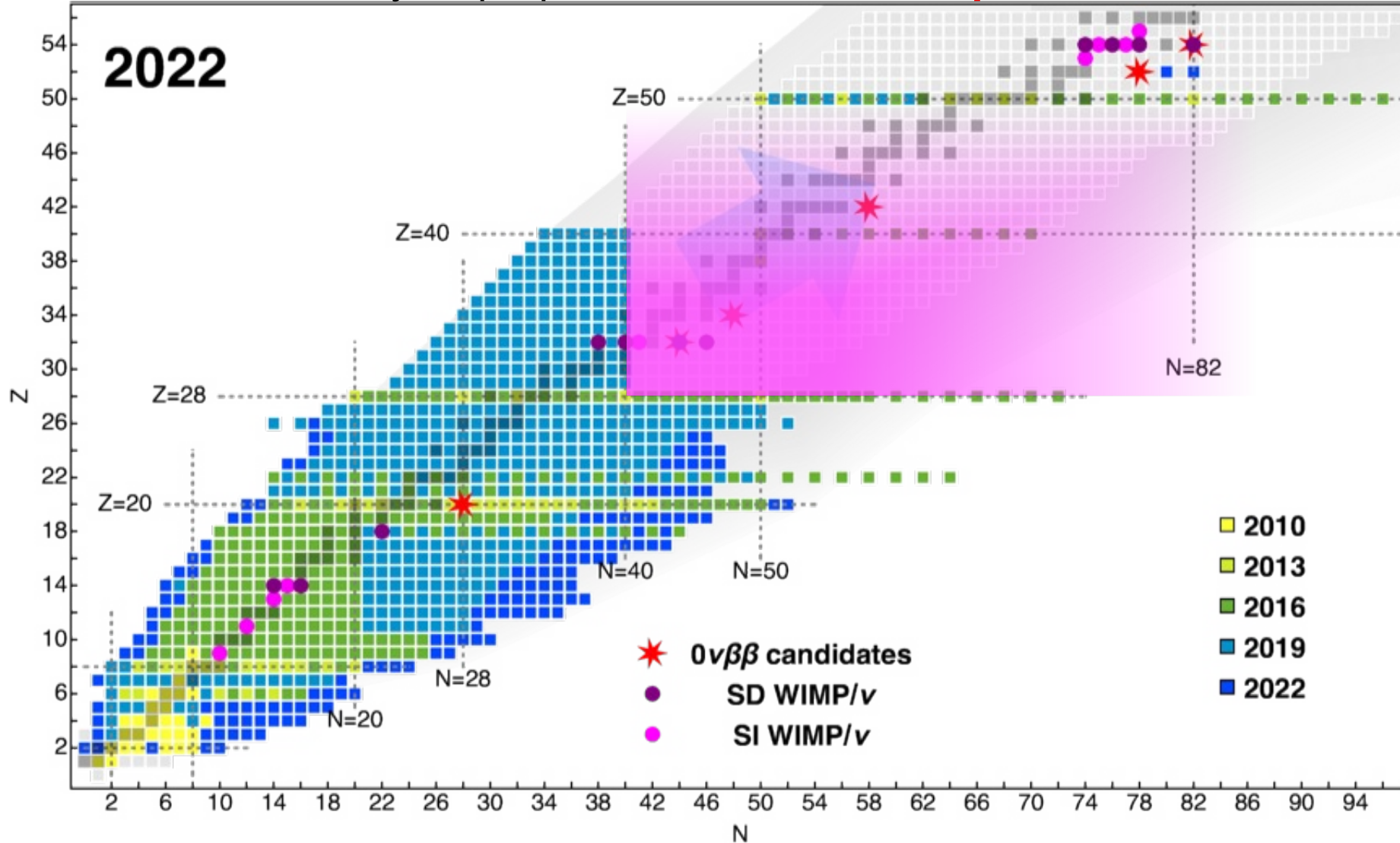
Tremendous progress in ab initio reach, largely due to polynomially scaling methods!

Calculate essentially all properties all of nuclei... **up to N, Z ~ 50**



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Calculate essentially all properties all of nuclei... **up to N, Z ~ 50**



Key Limitation

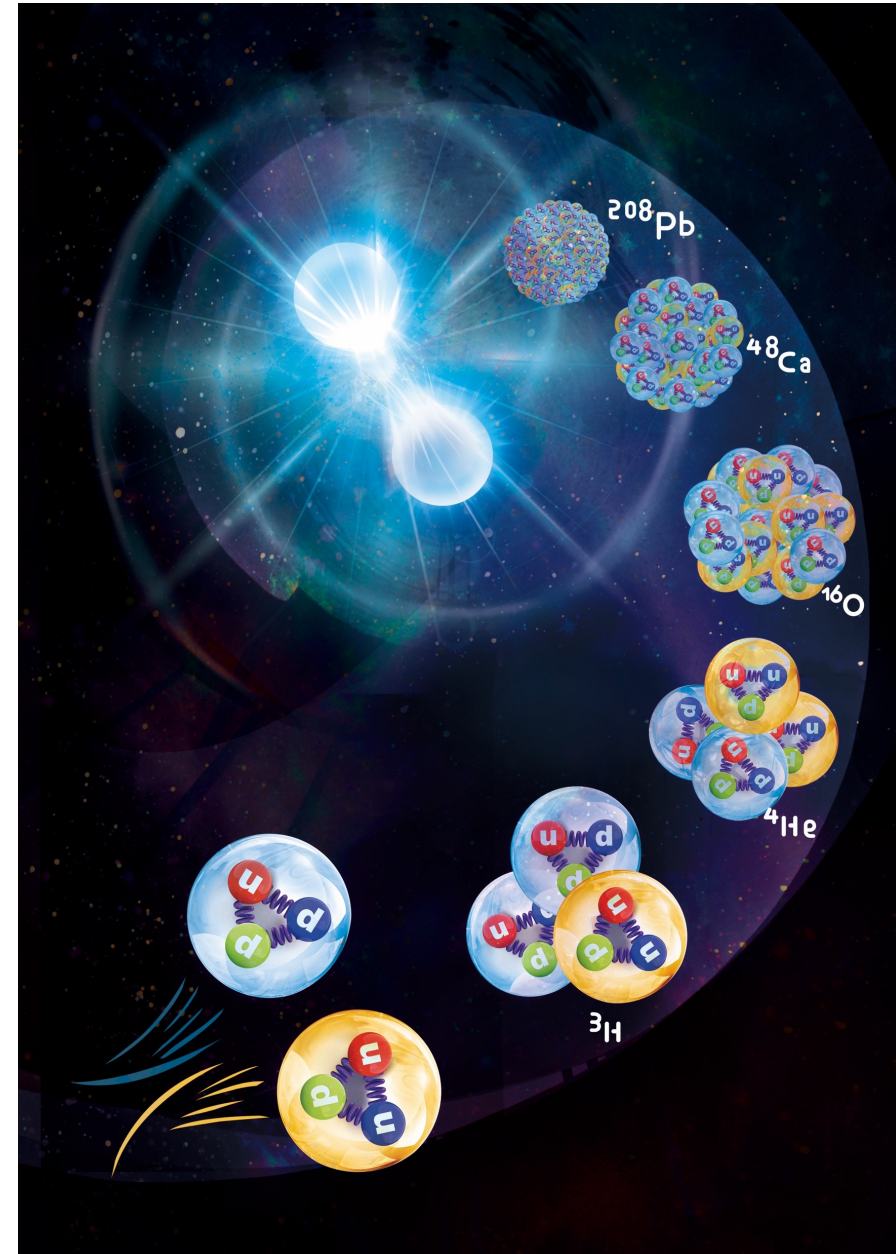
3NF matrix element storage

$$e_1 + e_2 + e_3 \leq E_{3\max}$$

Converged Calculations in Heavy Nuclei

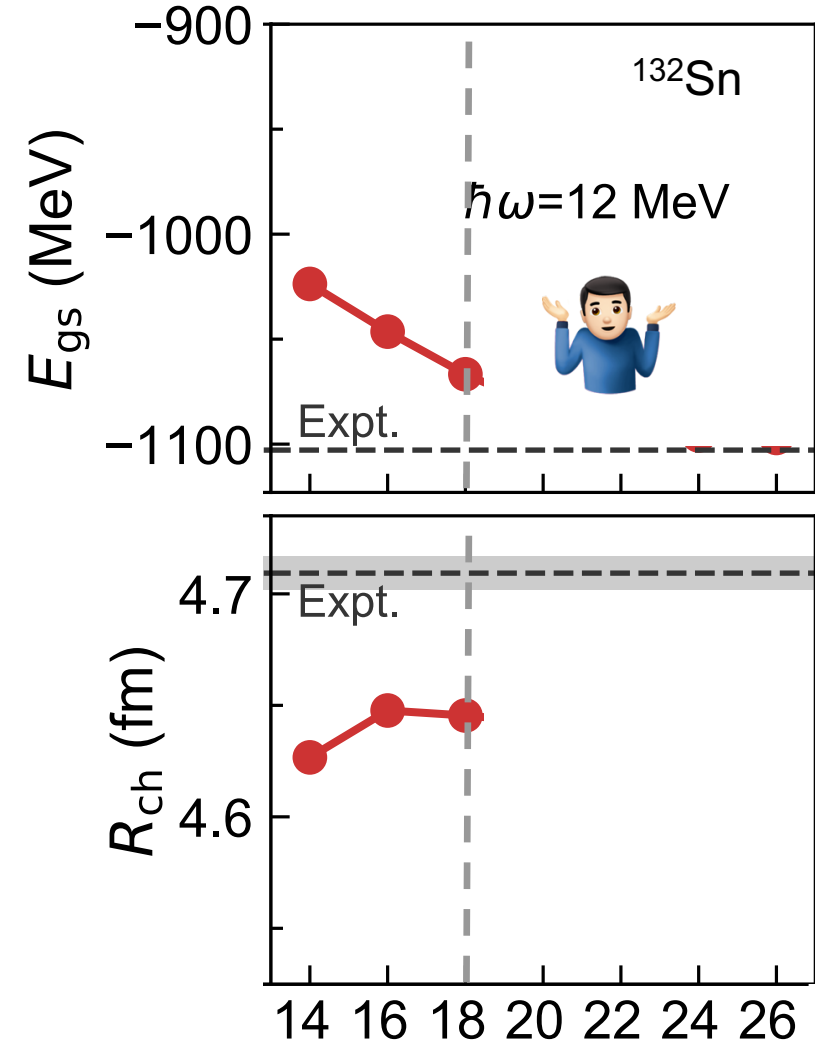
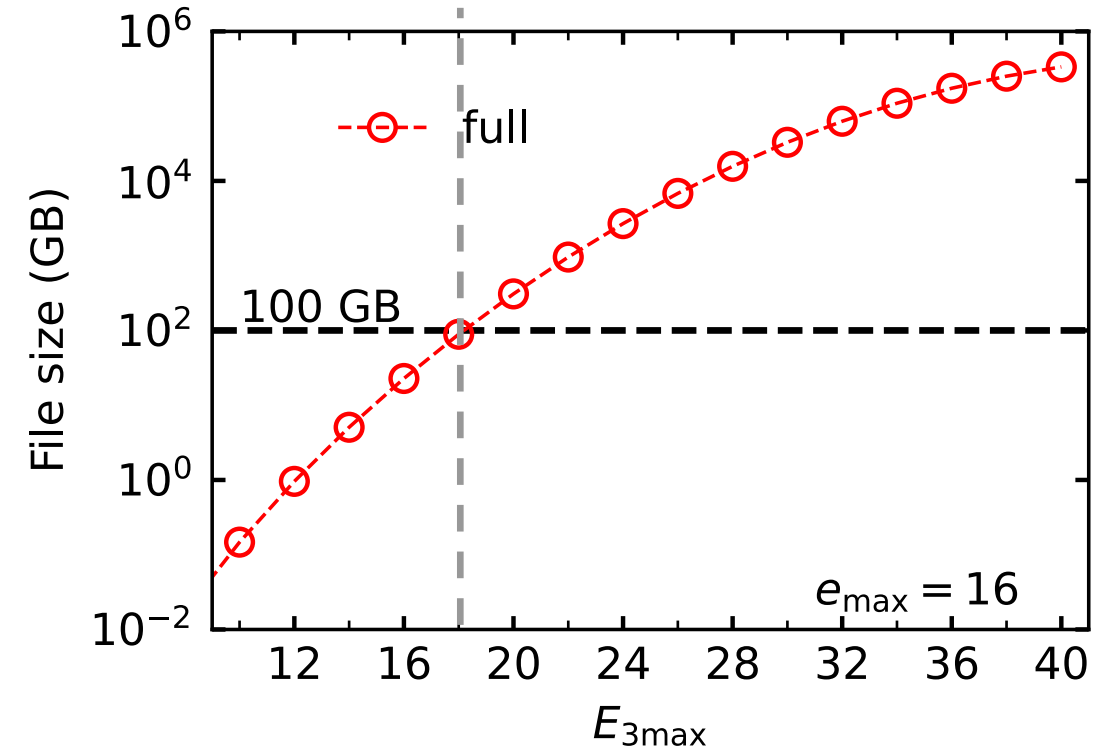
Converged *ab initio* calculations of heavy nuclei

T. Miyagi, S. R. Stroberg, P. Navrátil, K. Hebeler, and J. D. Holt
Phys. Rev. C **105**, 014302 – Published 3 January 2022



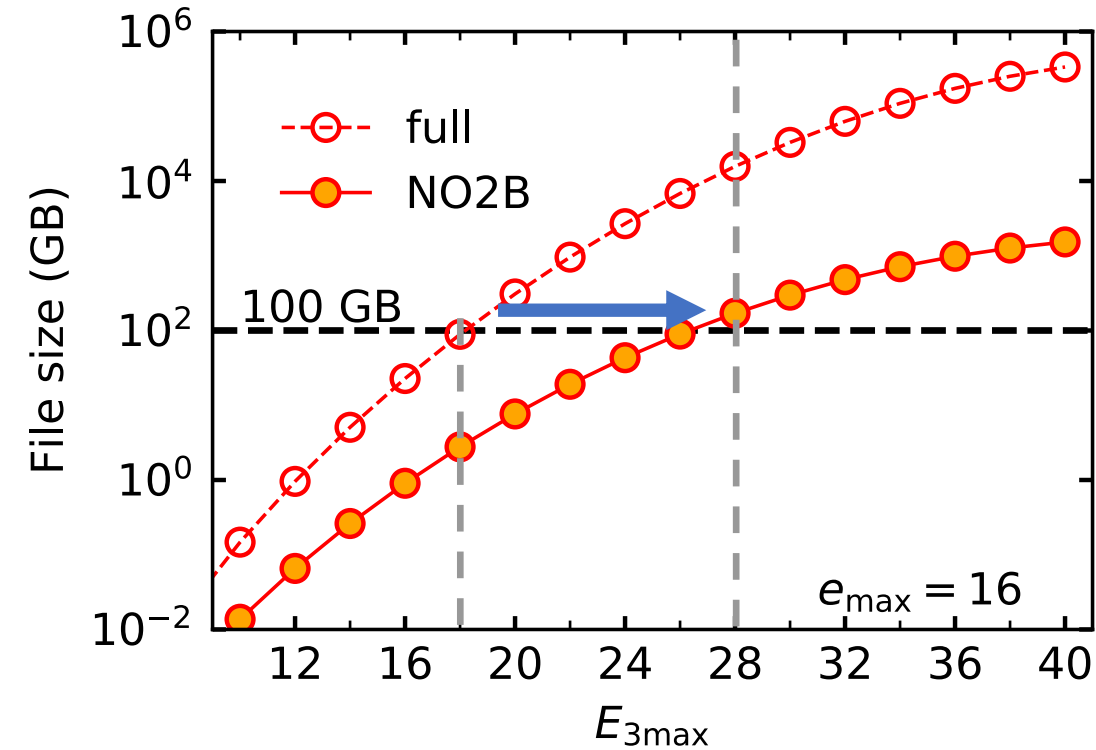
Limited by typical memory/node: $e_1 + e_2 + e_3 \leq E_{3\max} = 18$

No sign of convergence in ^{132}Sn - E_{gs} or R_{ch}



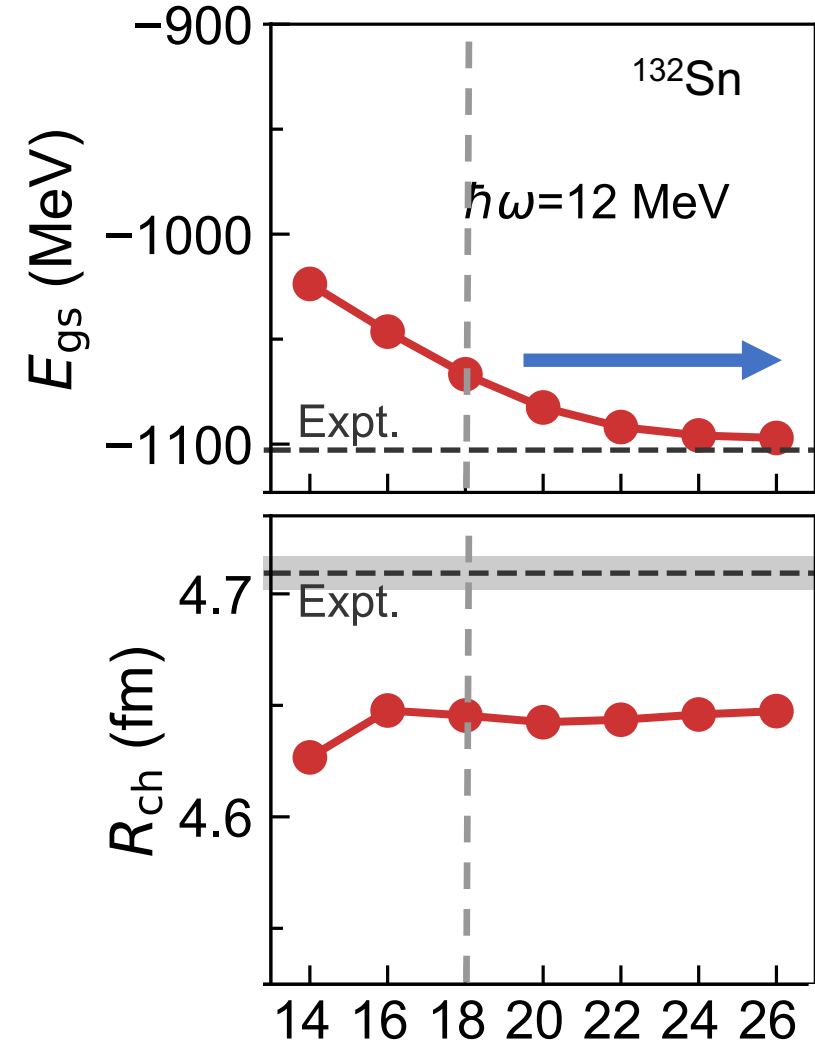
Limited by typical memory/node: $e_1 + e_2 + e_3 \leq E_{3\max} = 18$

Clever storage reduces needs by factor of 100!

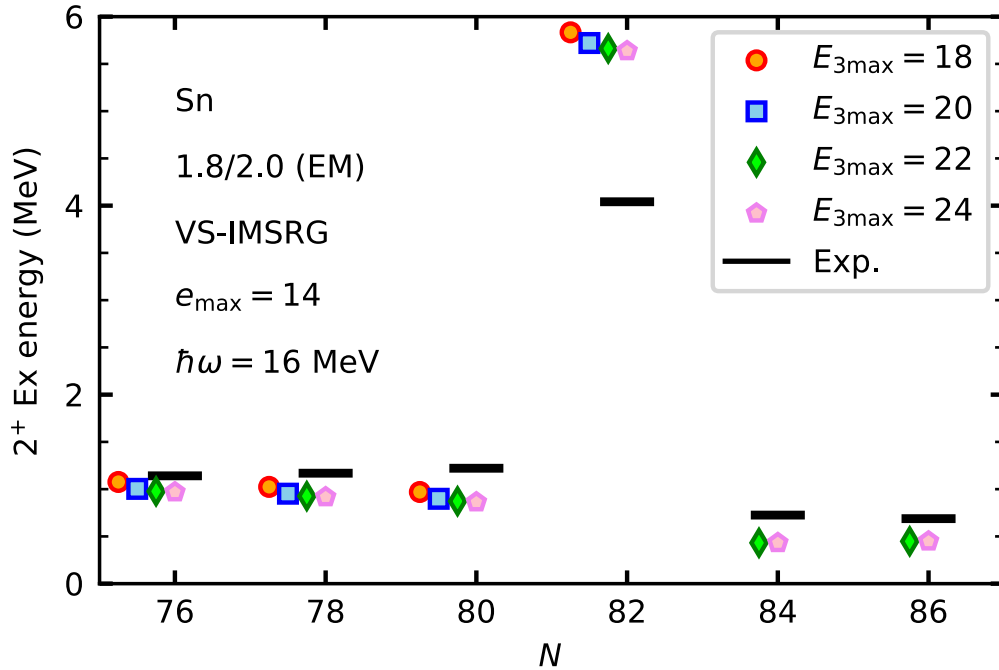
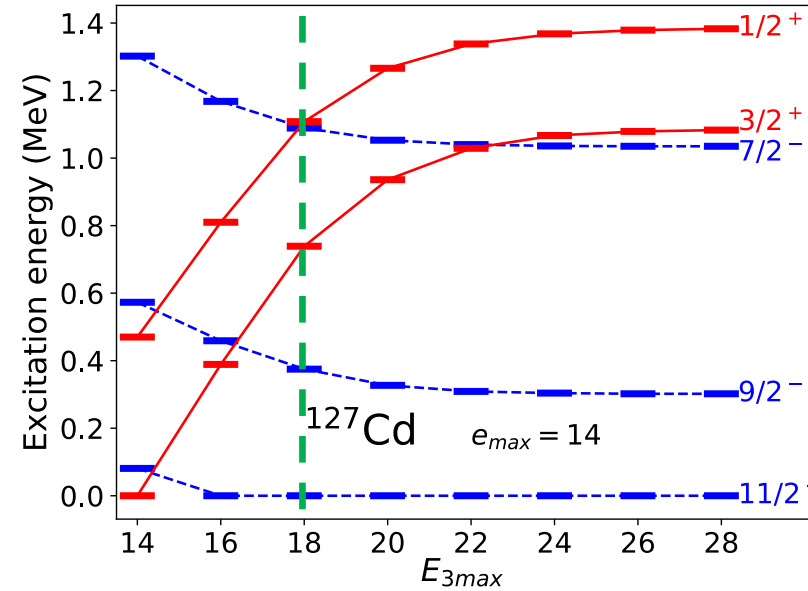
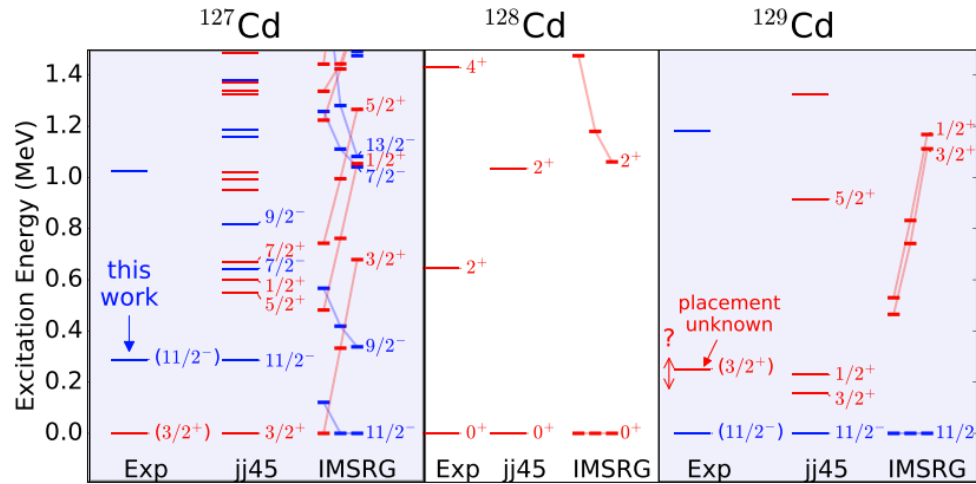


First converged ground-state properties of ^{132}Sn !

Opens heavy region to ab initio...



Size of N=70 gap **well** converged at $E_{3\max} = 28$ for neutron-rich Sn, In, Cd!

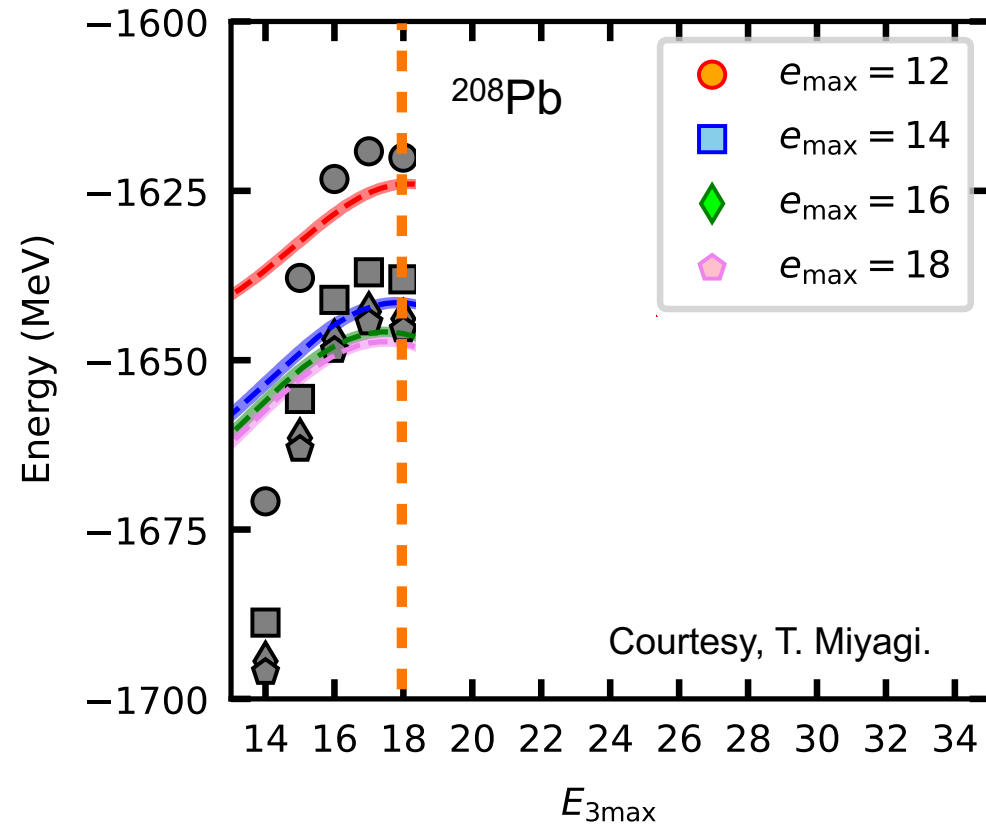


New capabilities: converged spectra in N=82 region

Converged (overpredicted) doubly magic ^{132}Sn

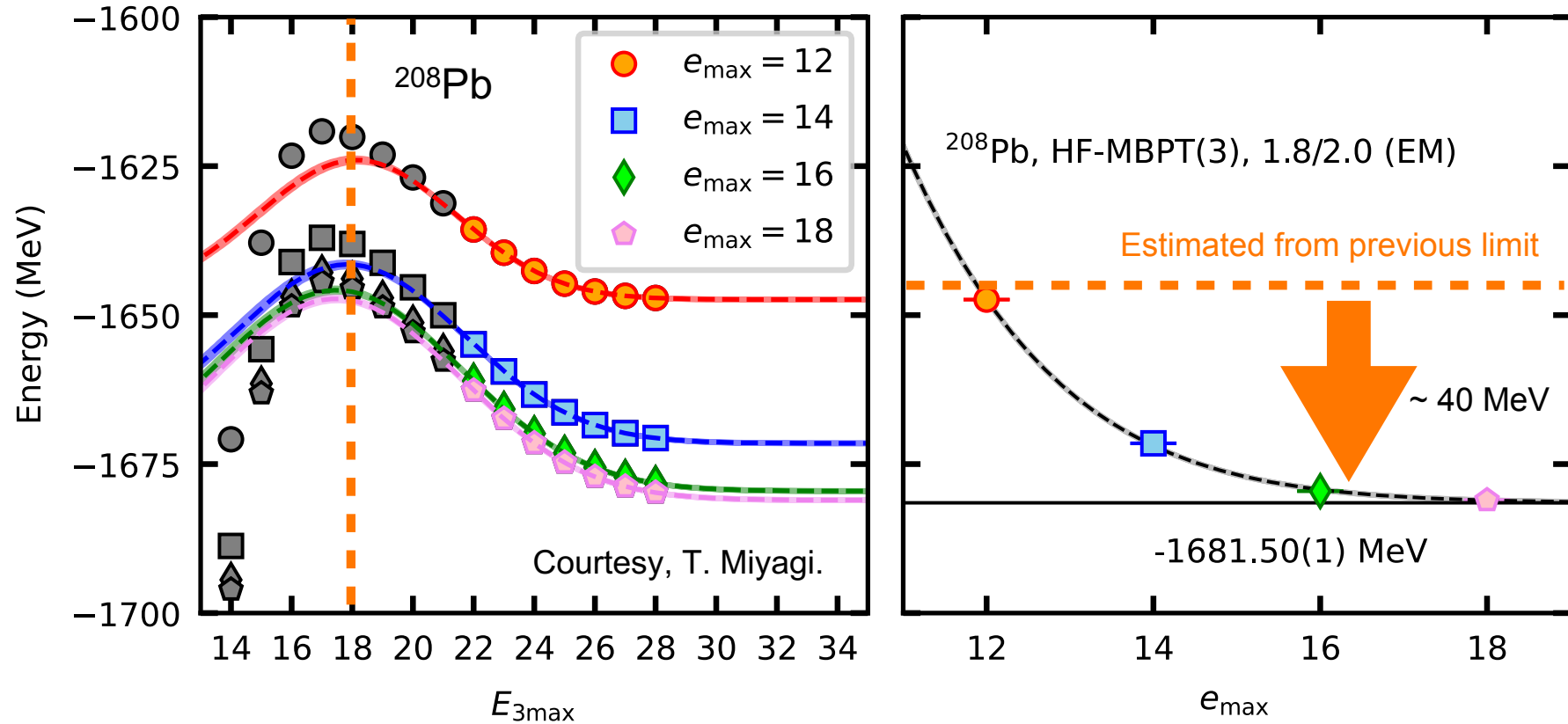
Can we go heavier?

Previous limit, no hope of convergence in ^{208}Pb g.s. energy...



Previous limit, no hope of convergence in ^{208}Pb g.s. energy

Improved $E_{3\text{max}} = 18 \rightarrow 28$ clear convergence



First converged ab initio calculation of ^{208}Pb !

Ab Initio Analysis: Neutron Skin of ^{208}Pb Linked with neutron star properties

nature
physics

ARTICLES

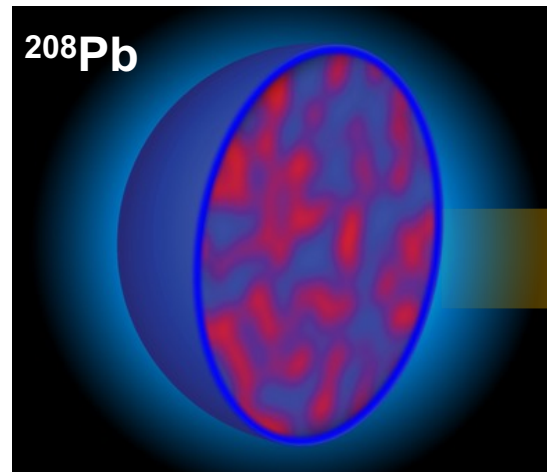
<https://doi.org/10.1038/s41567-022-01715-8>

 Check for updates

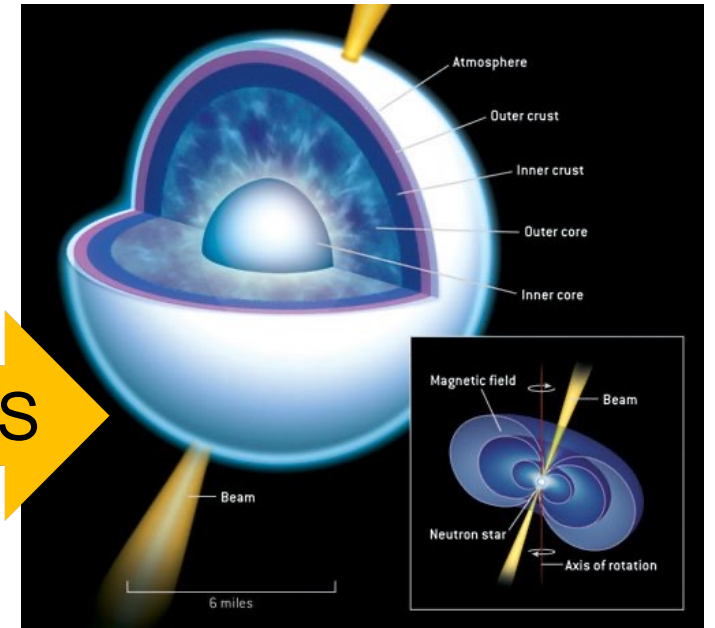
OPEN

Ab initio predictions link the neutron skin of ^{208}Pb to nuclear forces

Baishan Hu^{1,11}, Weiguang Jiang^{2,11}, Takayuki Miyagi^{1,3,4,11}, Zhonghao Sun^{5,6,11}, Andreas Ekström²,
Christian Forssén², Gaute Hagen^{1,5,6}, Jason D. Holt^{1,7}, Thomas Papenbrock^{5,6},
S. Ragnar Stroberg^{8,9} and Ian Vernon¹⁰



Nuclear EOS

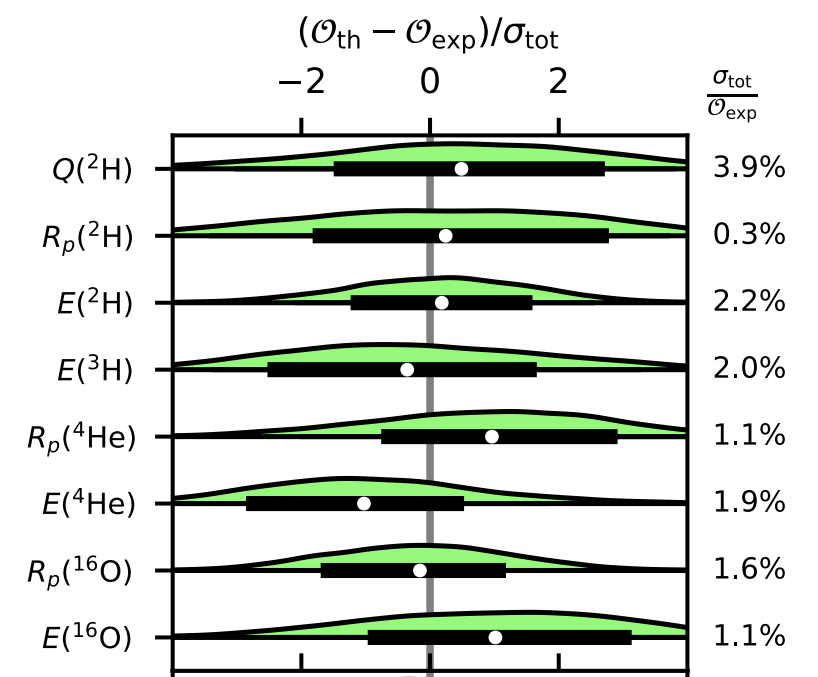


Combine TRIUMF/ORNL/Chalmers advances!

I: History Matching confronted with $A=2,3,4$ data + ^{16}O

10^9 calculations spanning EFT parameter space at N^2LO

34 non-implausible interactions



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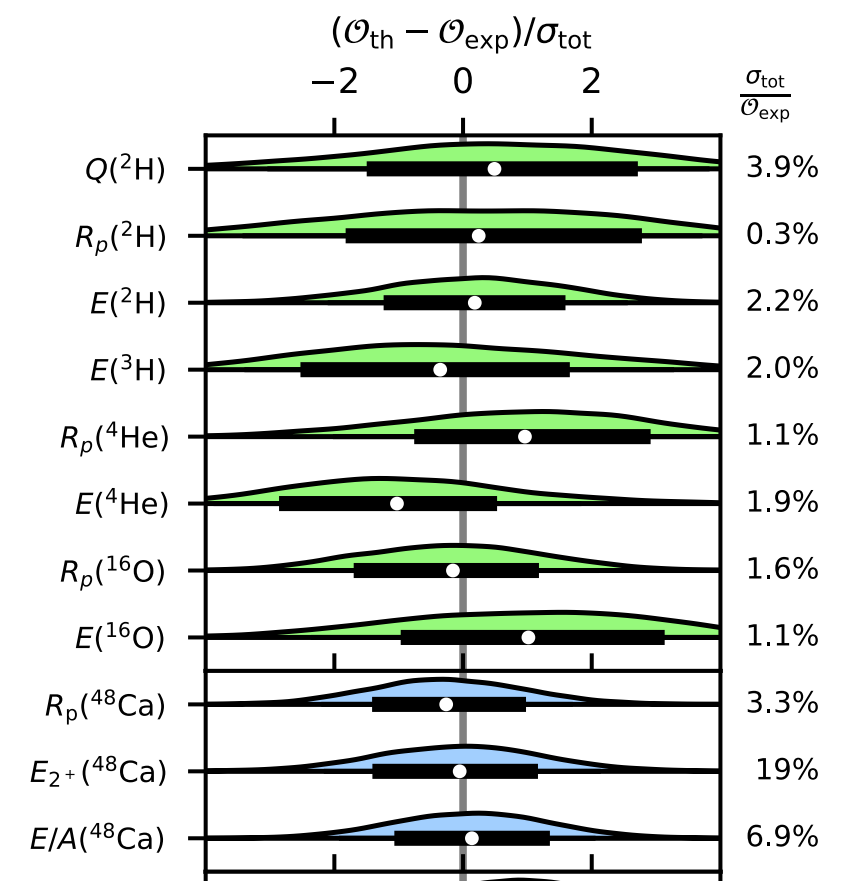
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II: Calibration use ^{48}Ca E/A , $E(2^+)$, R_p , dipole polarizability

Importance resampling – statistically weight interactions



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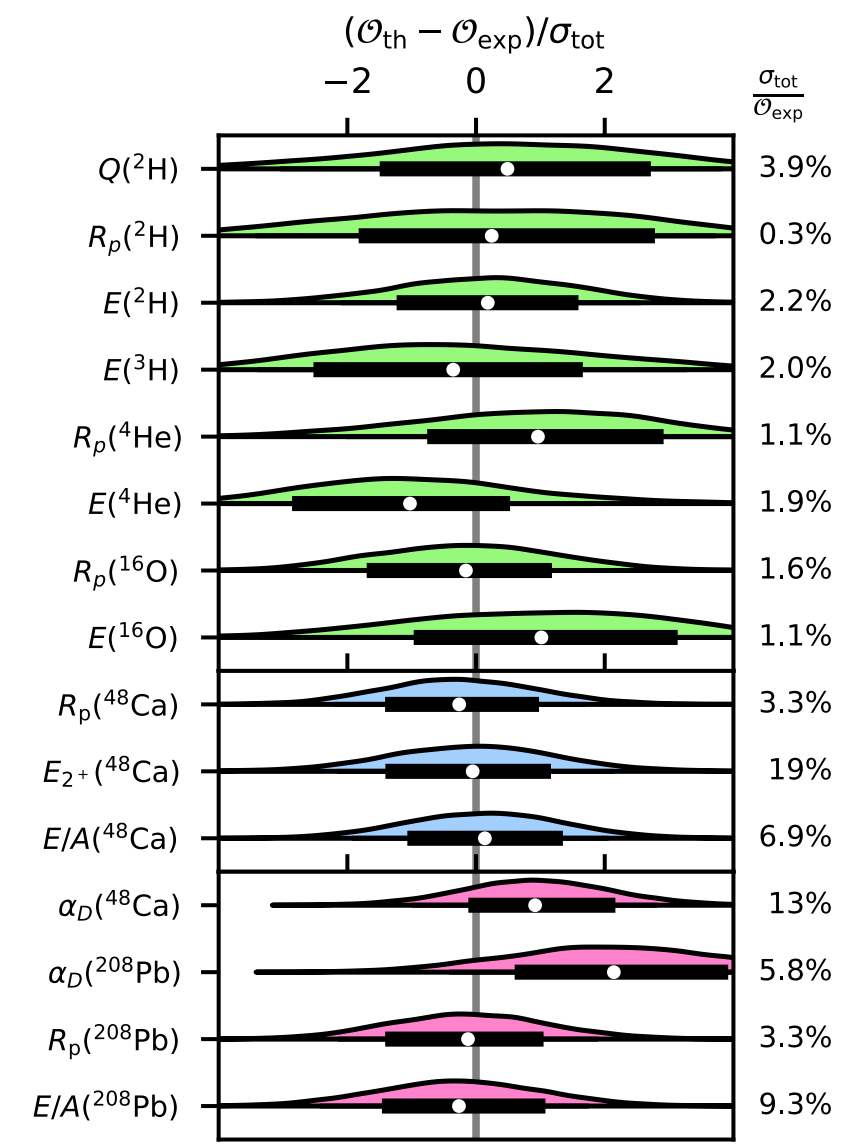
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Importance resampling – statistically weight interactions

III: Validation ^{208}Pb E/A , R_p + $^{48}\text{Ca}/^{208}\text{Pb}$ DP from ab initio

Clear quality description of data



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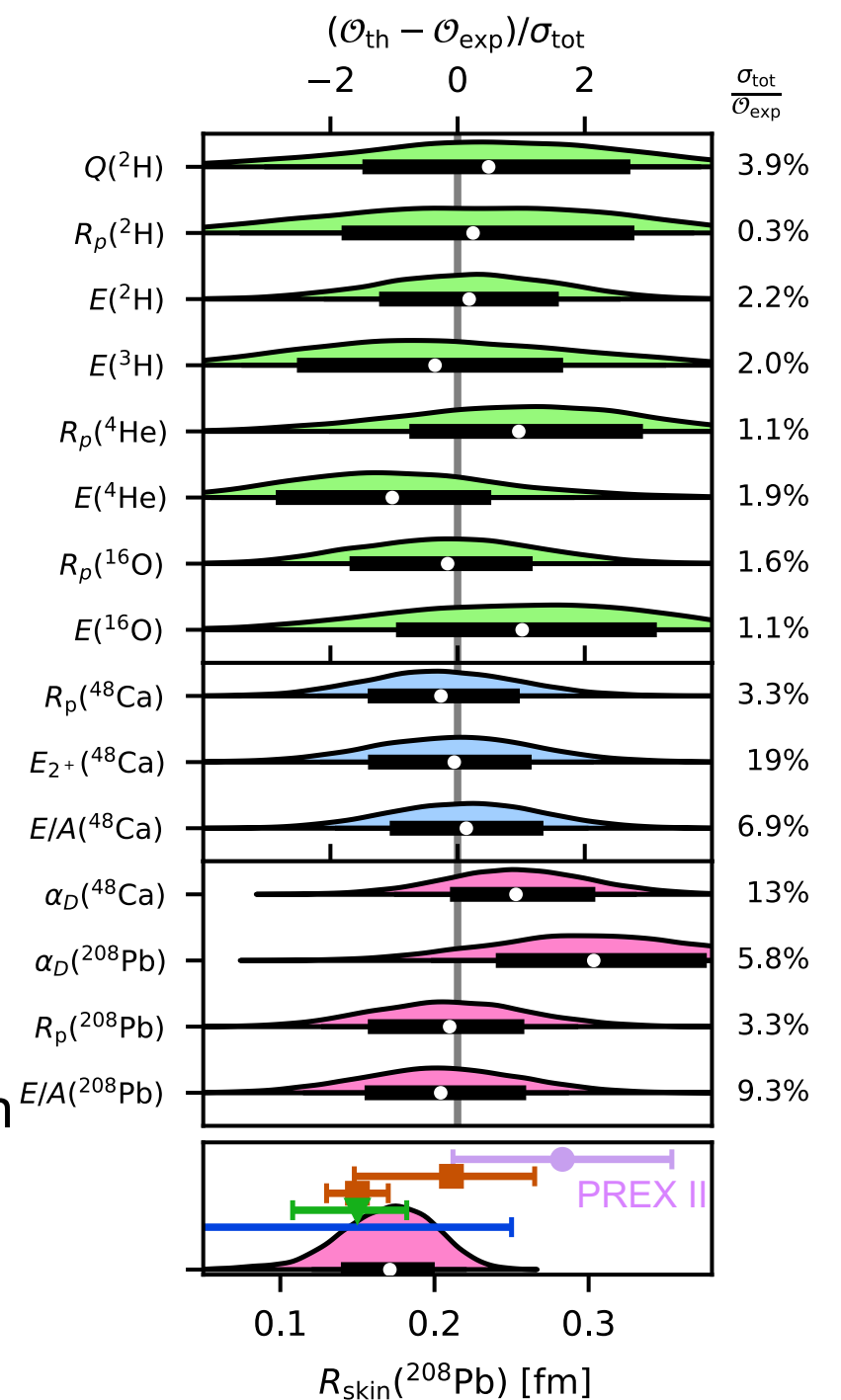
III: Validation ^{208}Pb E/A , R_p + $^{48}\text{Ca}/^{208}\text{Pb}$ DP from ab initio

Clear quality description of data

IV: Prediction - posterior predictive distribution for neutron skin

$R_{\text{skin}}(^{208}\text{Pb}) = 0.14\text{-}0.20\text{fm}$ (68% credible level)

Consistent(ish) with extracted **PREXII result**



Explore correlations between finite nuclei and nuclear EOS

Use same 34 non-implausible interactions

Reveals correlation as seen in mean field models

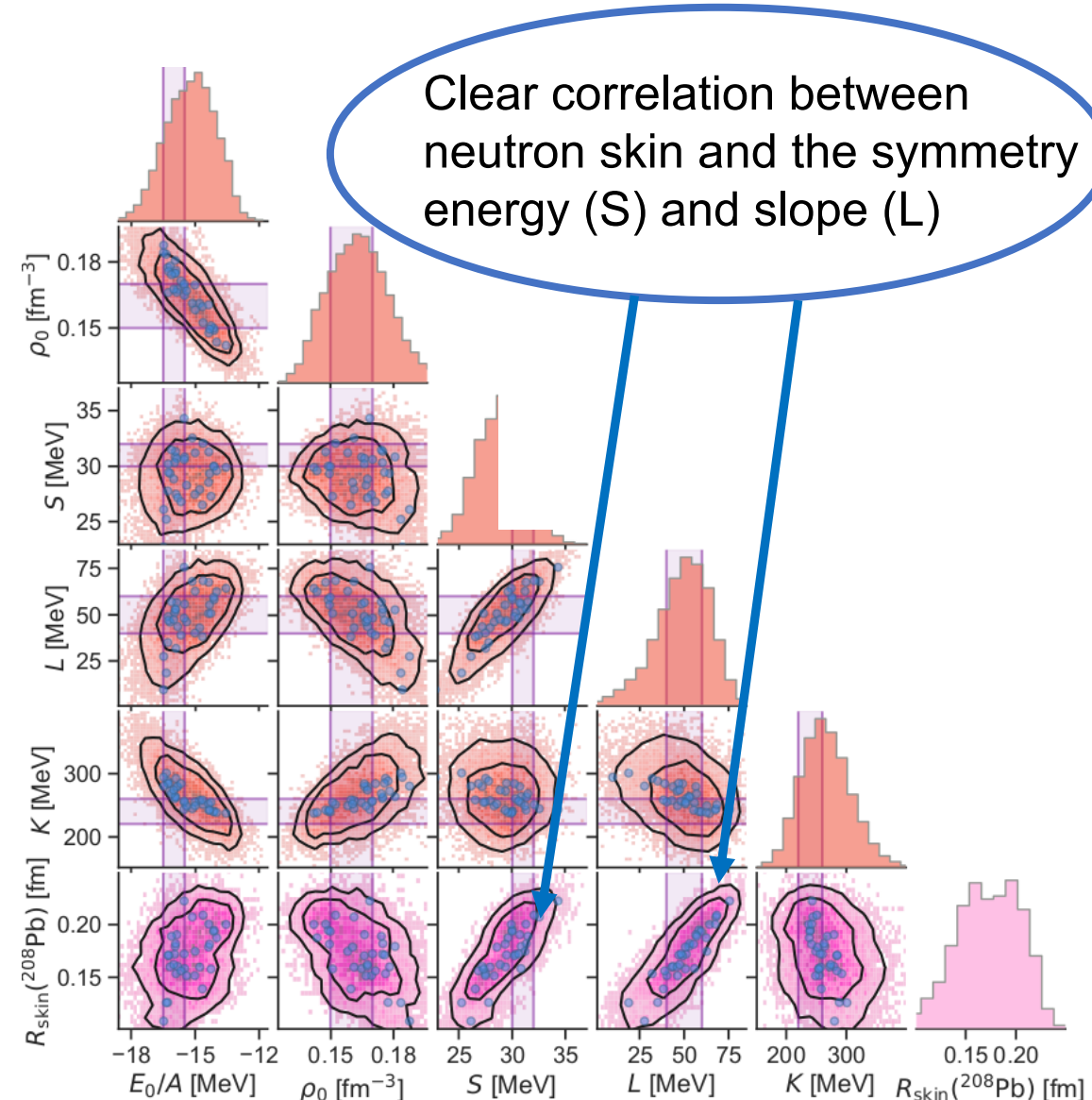
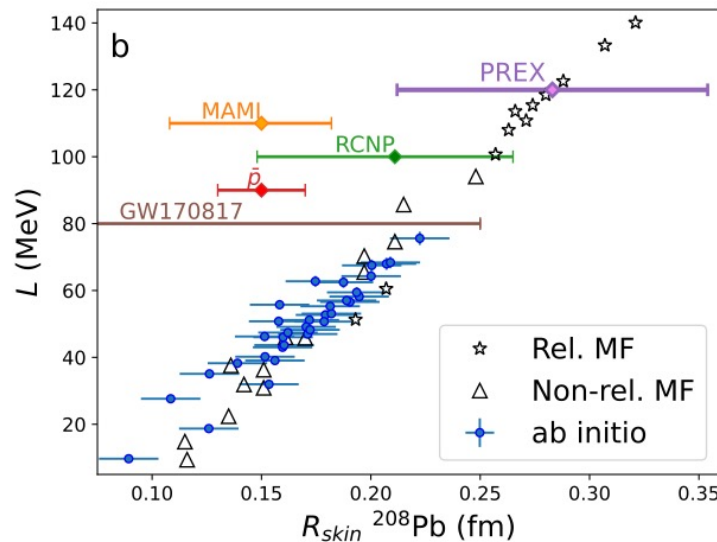
L = 37-63 MeV

Constrain forces potentially from:

Neutron star radii/mergers

Mean field accommodates large range of skins

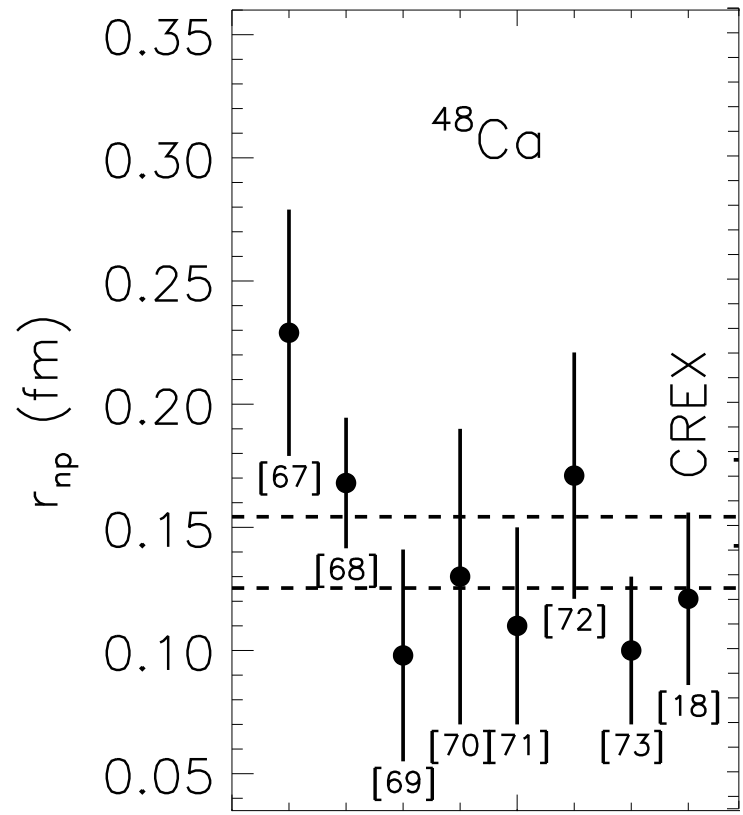
Tighter range from
ab initio calculations





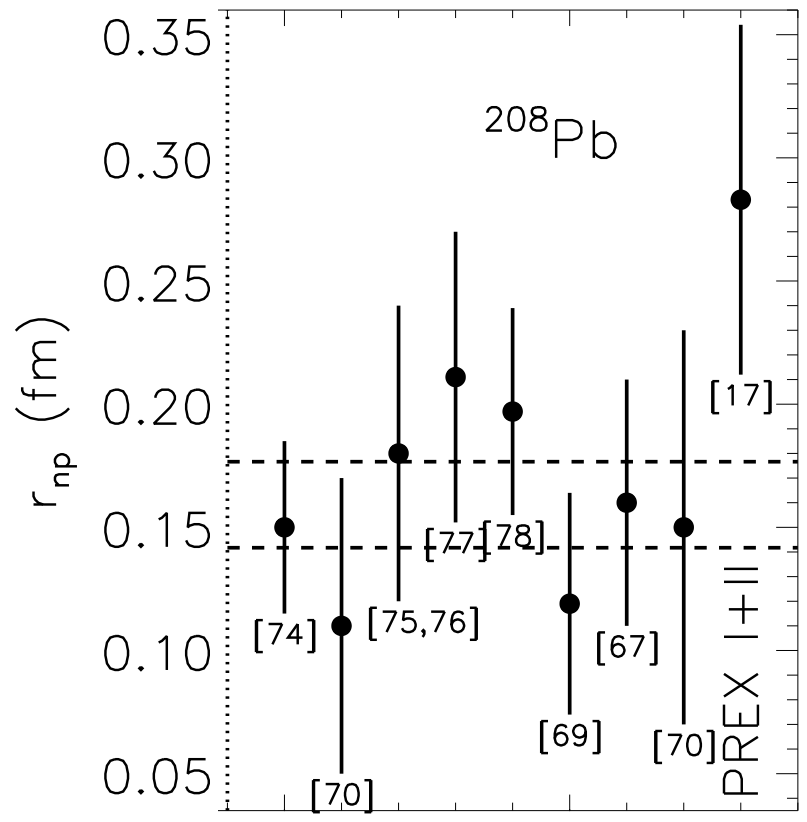
Newly extracted neutron skin in ^{48}Ca

Use same 34 interactions – predictions in good agreement with CREX result

Constraints on Nuclear Symmetry Energy Parameters
 J. Lattimer (2023)



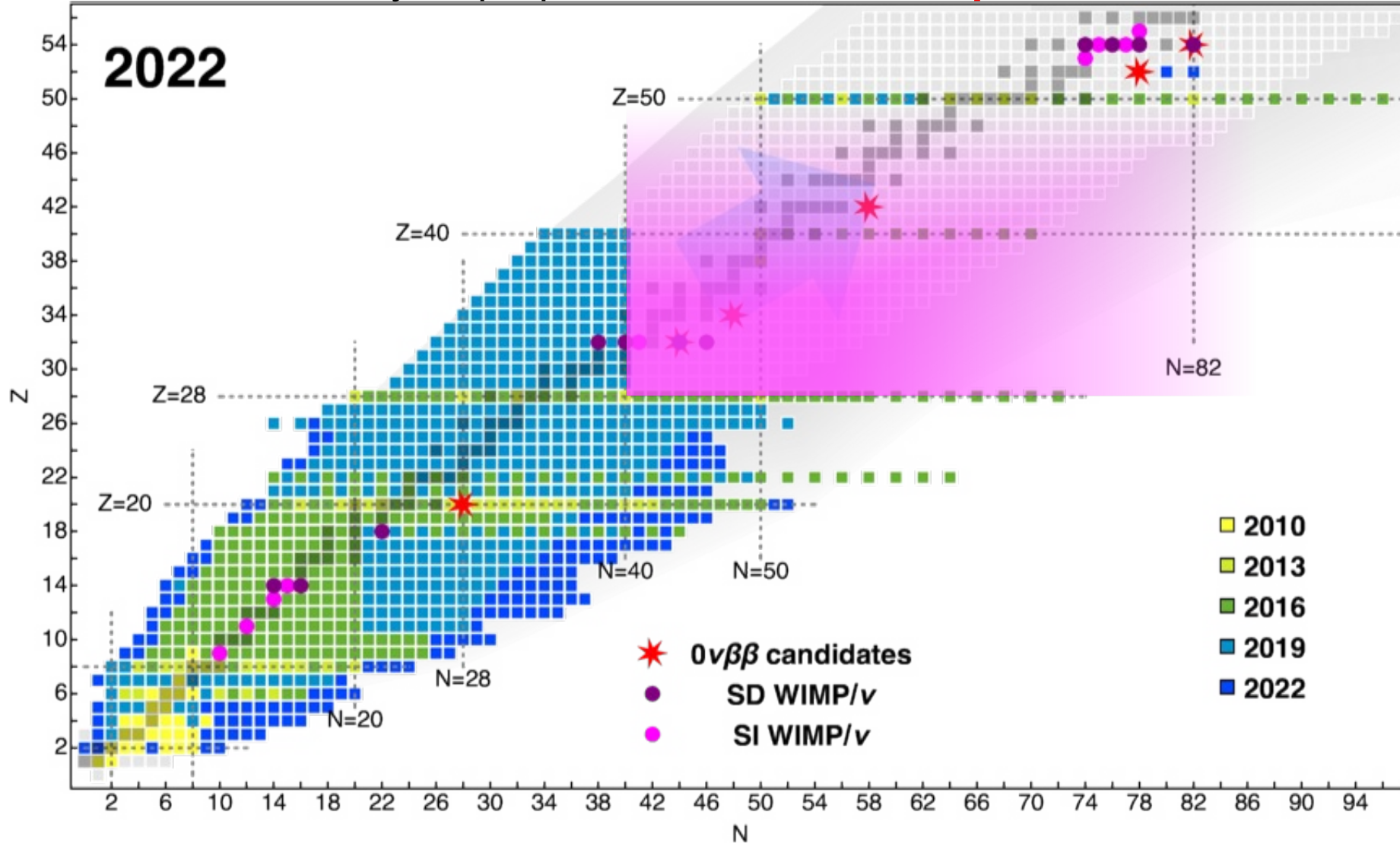
 G. Hagen et al
 B. Hu et al



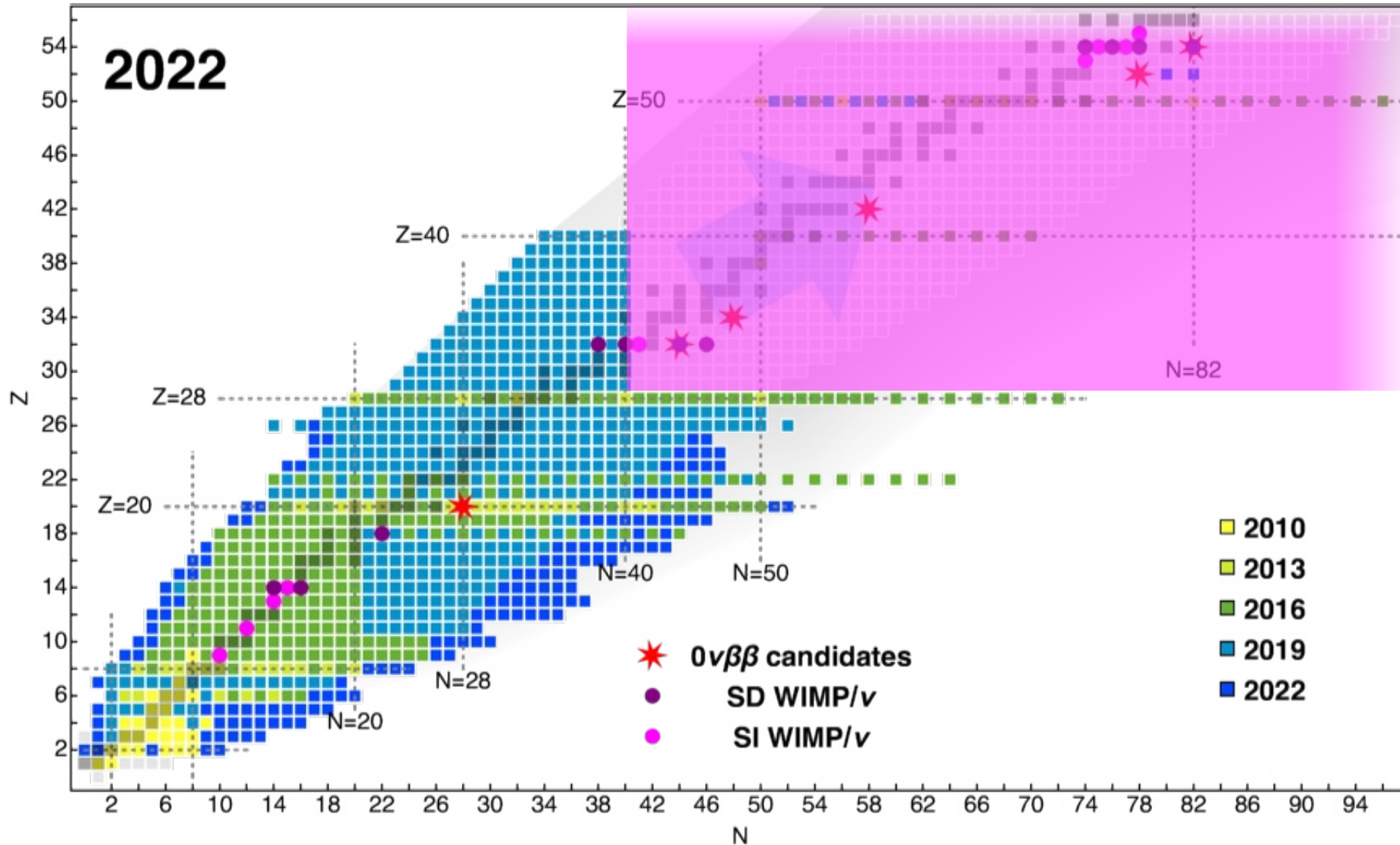
 B. Hu et al

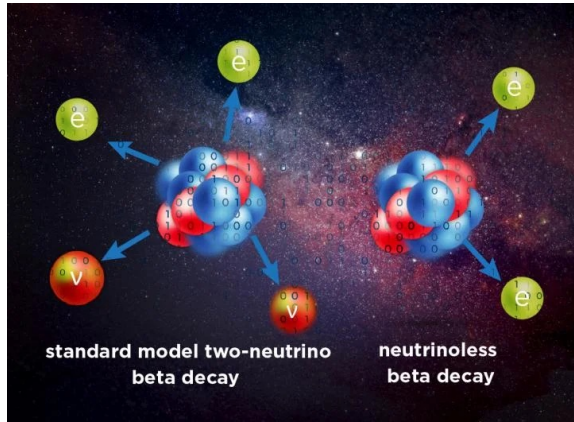
Tremendous progress in ab initio reach, largely due to polynomially scaling methods!

Calculate essentially all properties all of nuclei... **up to N, Z ~ 50**

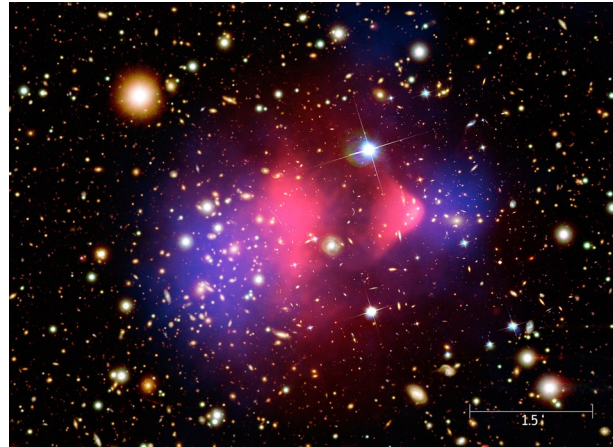


Rapid progress in ab initio reach, due to valence-space approach... up to...

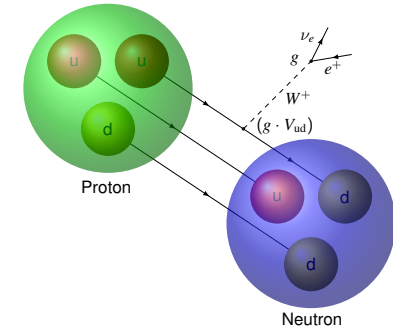




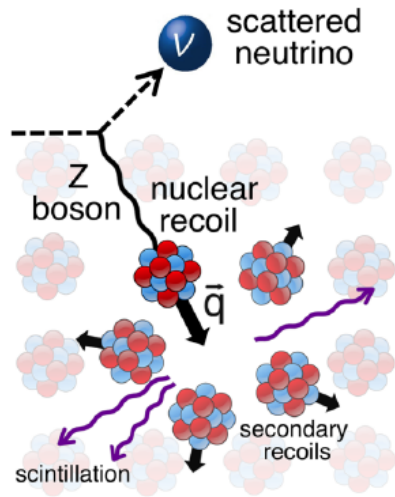
Neutrinoless double beta decay



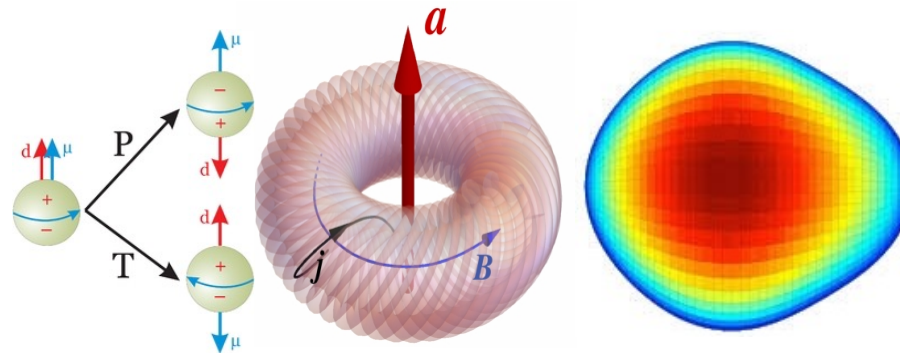
Dark matter direct detection



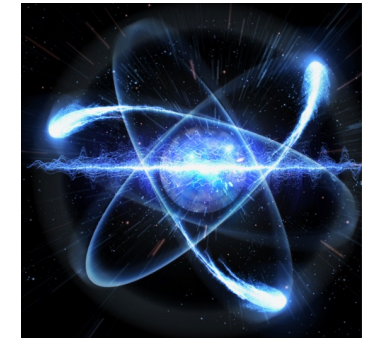
Superallowed Fermi transitions



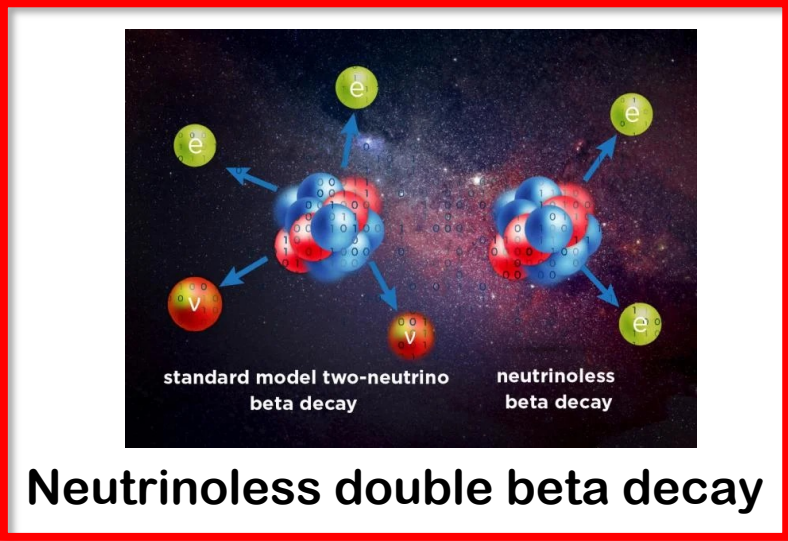
Neutrino scattering



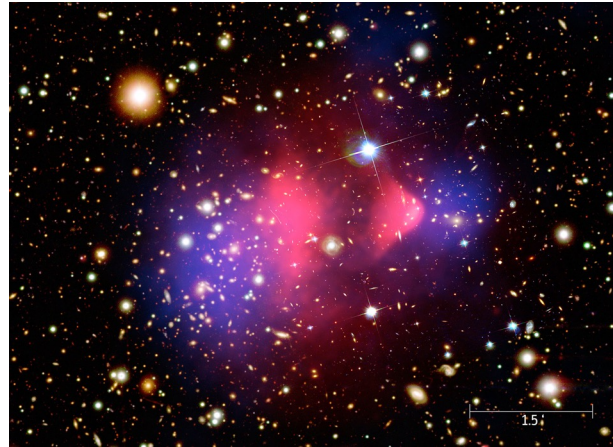
Symmetry-violating moments



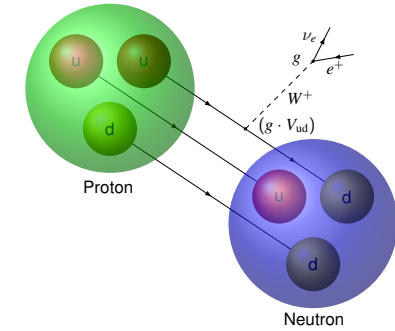
Atomic theory



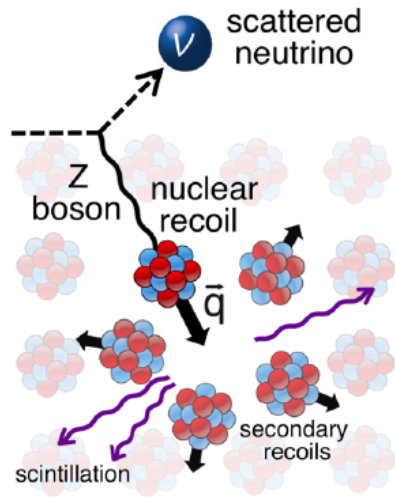
Neutrinoless double beta decay



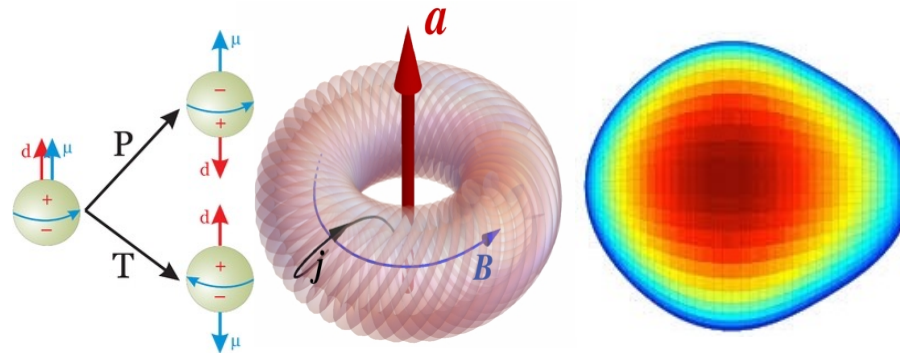
Dark matter direct detection



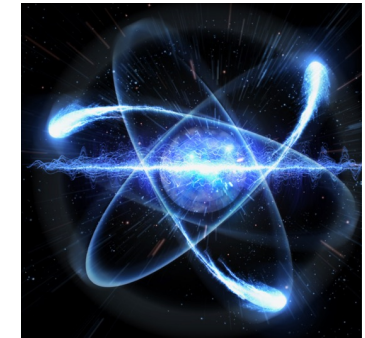
Superallowed Fermi transitions



Neutrino scattering



Symmetry-violating moments



Atomic theory

Two-Body Currents for Gamow-Teller Transitions and g_A Quenching

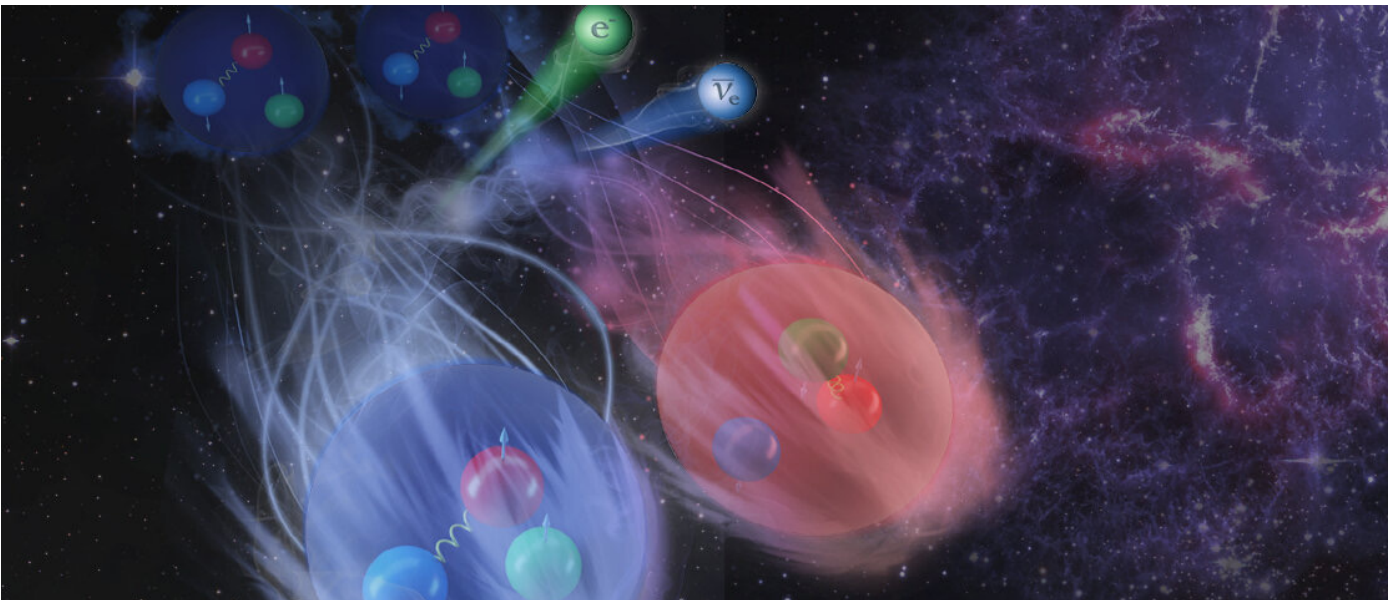
LETTERS

<https://doi.org/10.1038/s41567-019-0450-7>

nature
physics

Discrepancy between experimental and theoretical β -decay rates resolved from first principles

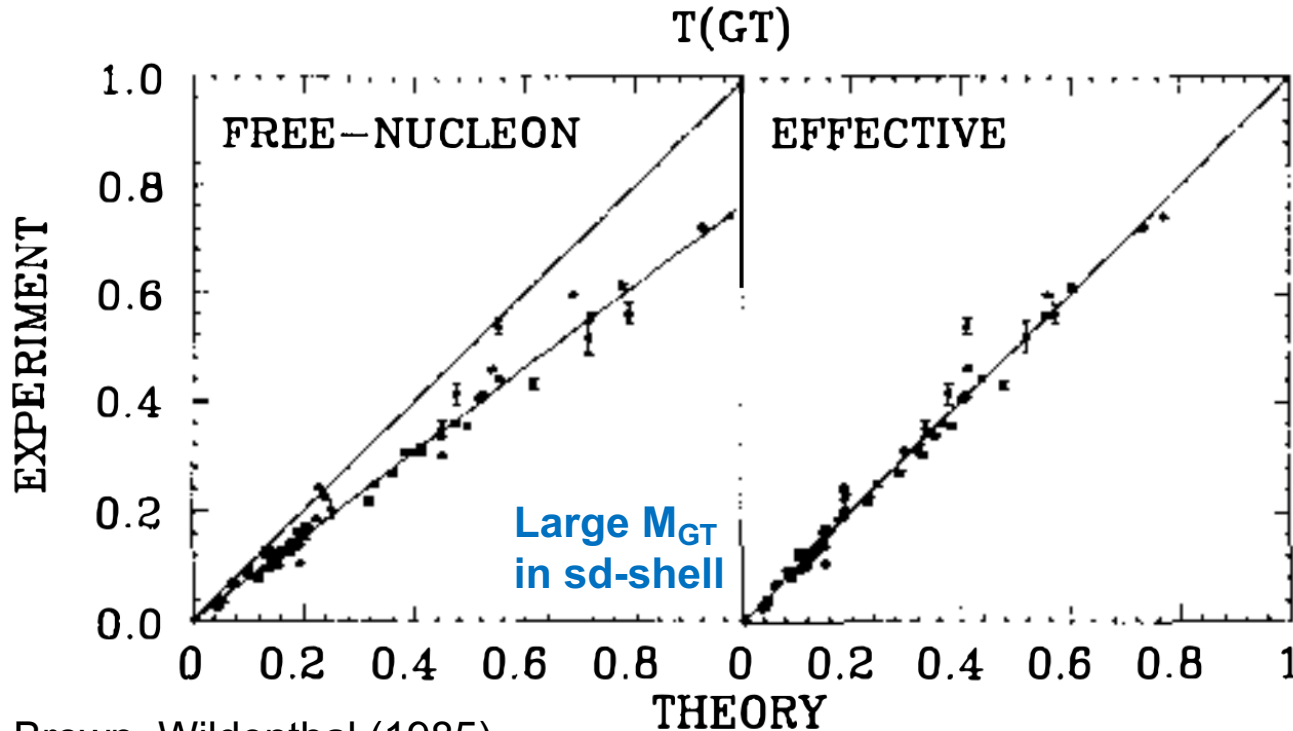
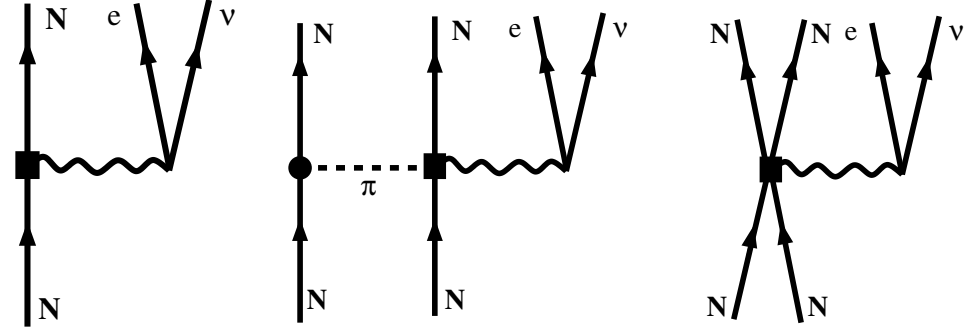
P. Gysbers^{1,2}, G. Hagen^{3,4*}, J. D. Holt¹, G. R. Jansen^{3,5}, T. D. Morris^{3,4,6}, P. Navrátil¹, T. Papenbrock^{3,4}, S. Quaglioni⁷, A. Schwenk^{8,9,10}, S. R. Stroberg^{1,11,12} and K. A. Wendt⁷



Long-standing problem in weak decays: **experimental values systematically smaller than theory**

$$M_{GT} = g_A \langle f | \mathcal{O}_{GT} | i \rangle \quad \mathcal{O}_{GT} = \mathcal{O}_{\sigma\tau}^{1b} + \mathcal{O}_{2BC}^{2b}$$

Using $g_A^{\text{eff}} \approx 0.77 \times g_A^{\text{free}}$ agrees with data



Brown, Wildenthal (1985)

- Missing wavefunction correlations
- Renormalized VS operator?
- Neglected two-body currents?
- Model-space truncations?

Explore in ab initio framework

Calculate **large GT matrix elements**

$$M_{GT} = g_A \langle f | \mathcal{O}_{GT} | i \rangle$$

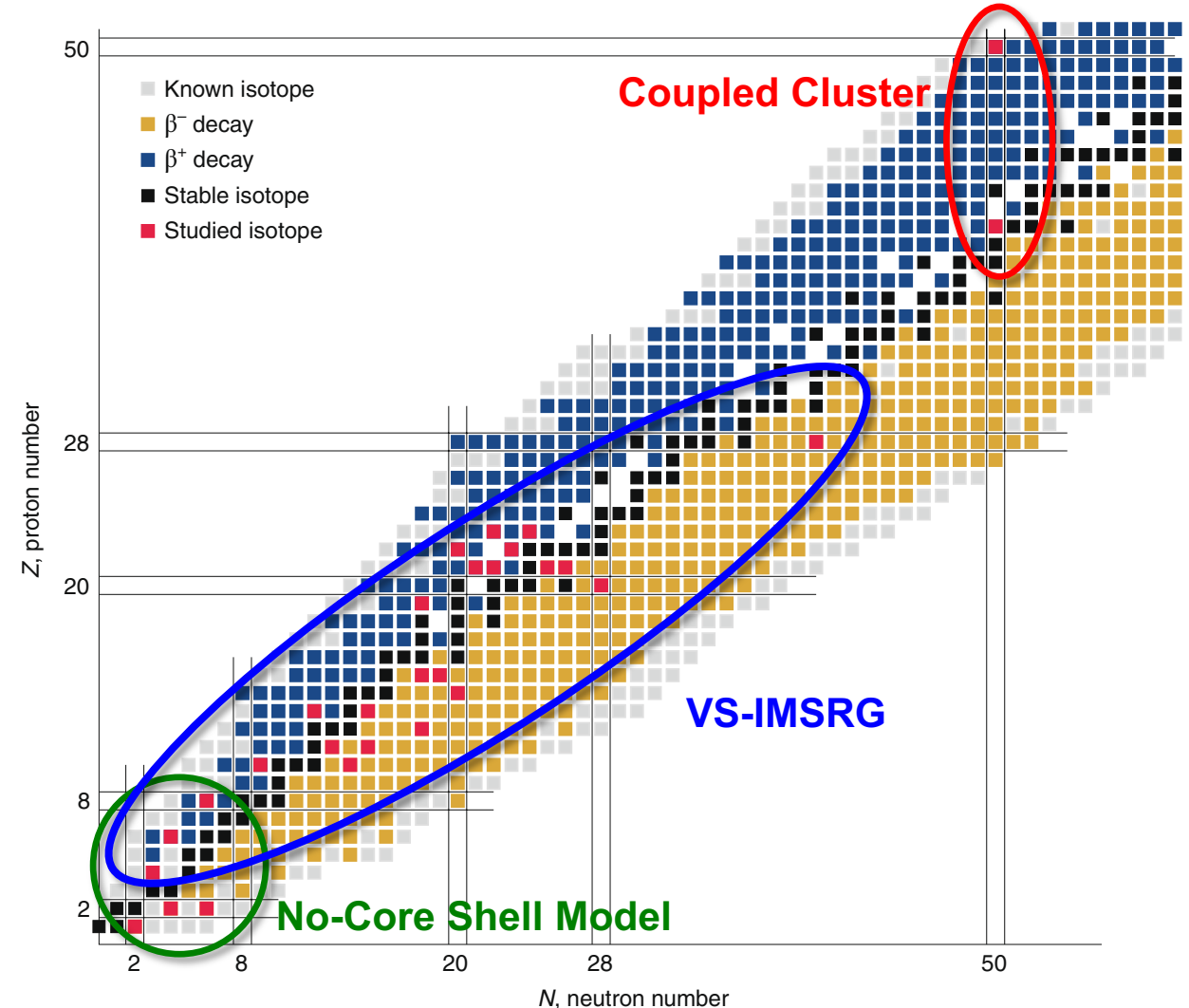
$$\mathcal{O}_{GT} = \mathcal{O}_{\sigma\tau}^{1b} + \mathcal{O}_{2BC}^{2b}$$

- Light, medium, and heavy regions
- Benchmark different ab initio methods
- Range of NN+3N forces
- Consistent inclusion of 2BC

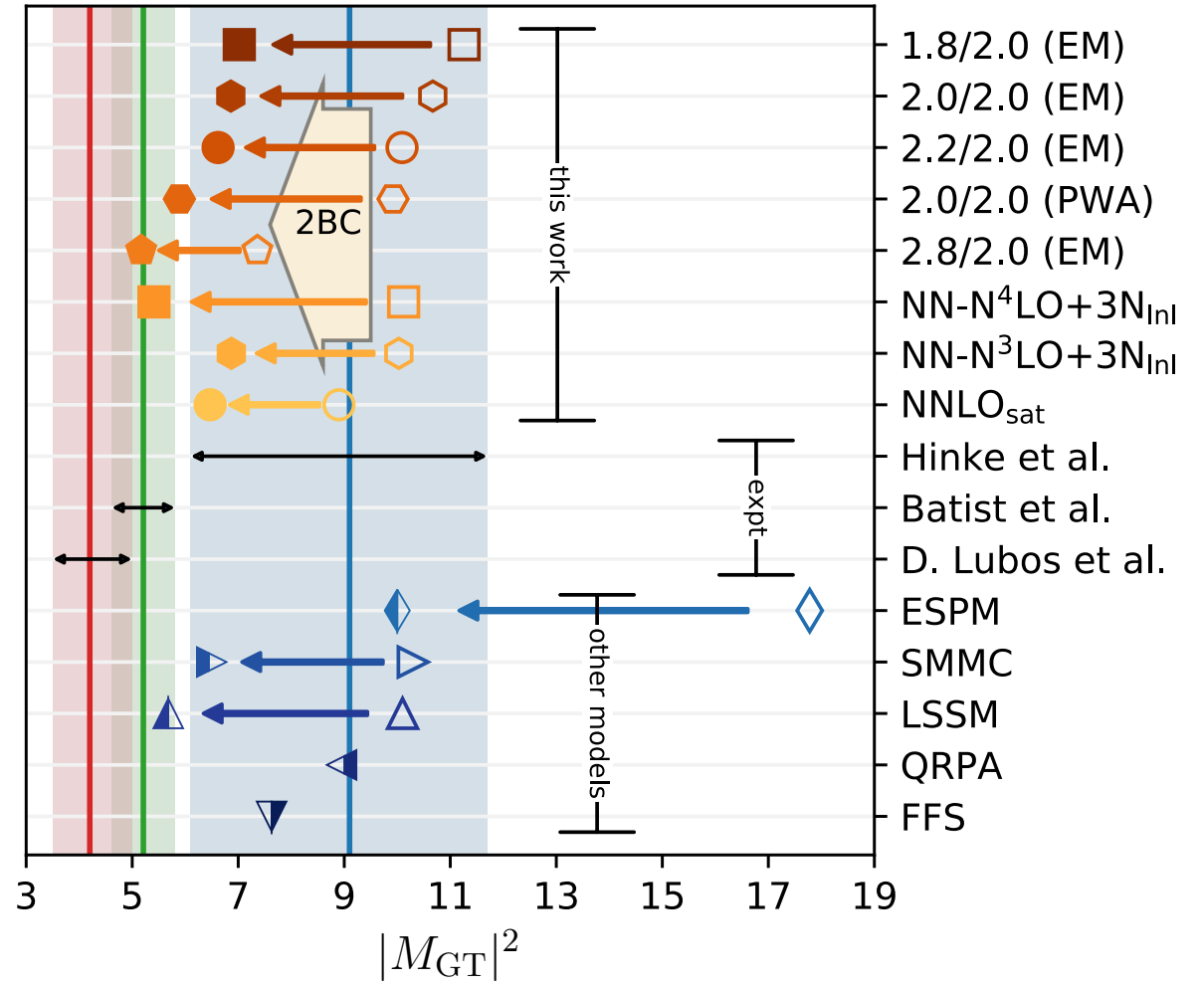
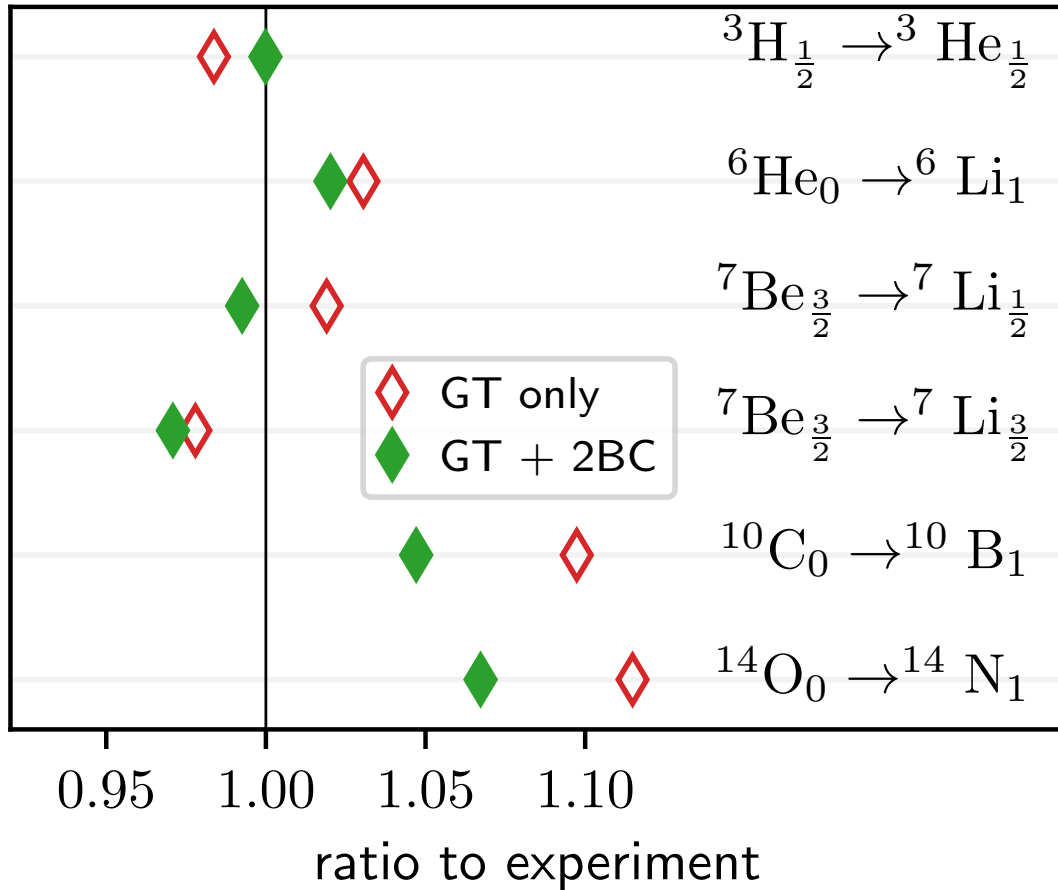
NUCLEAR PHYSICS

Beta decay gets the ab initio treatment

One of the fundamental radioactive decay modes of nuclei is β decay. Now, nuclear theorists have used first-principles simulations to explain nuclear β decay properties across a range of light- to medium-mass isotopes, up to ^{100}Sn .



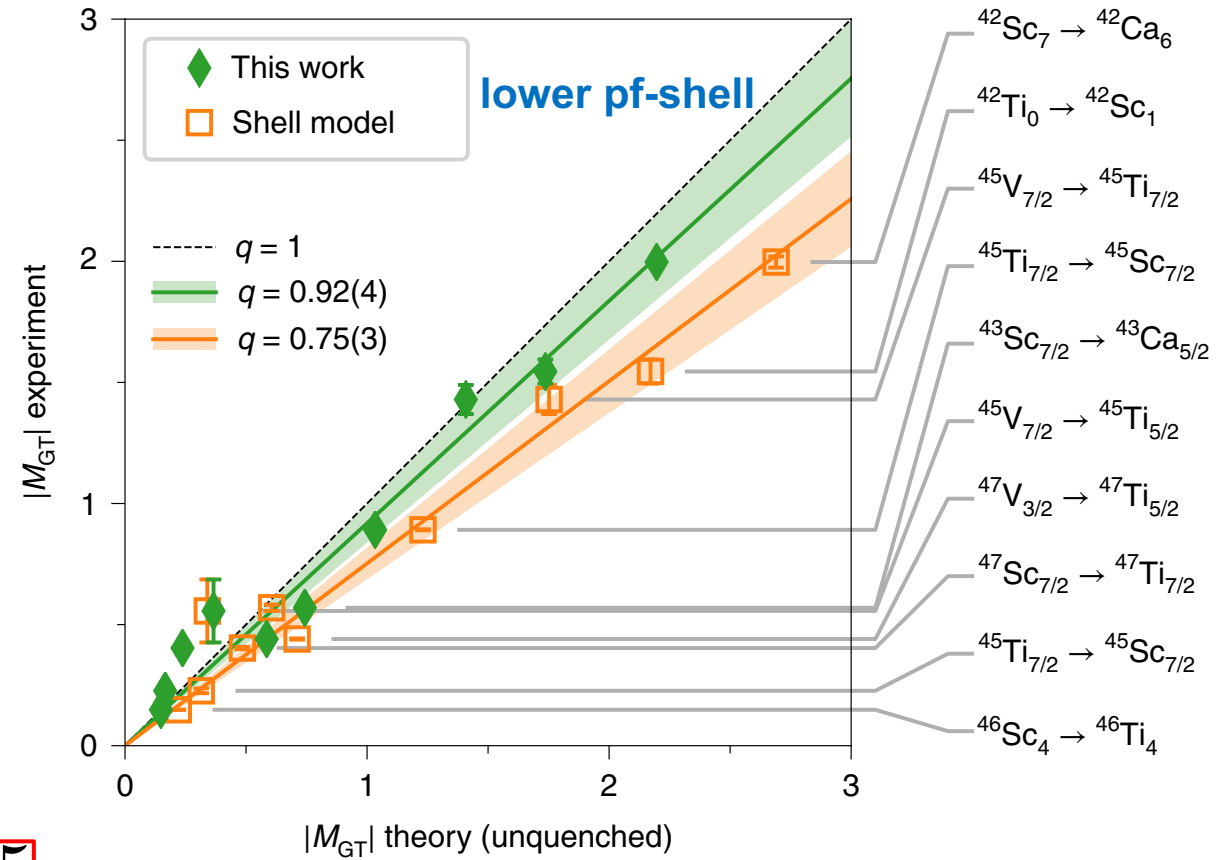
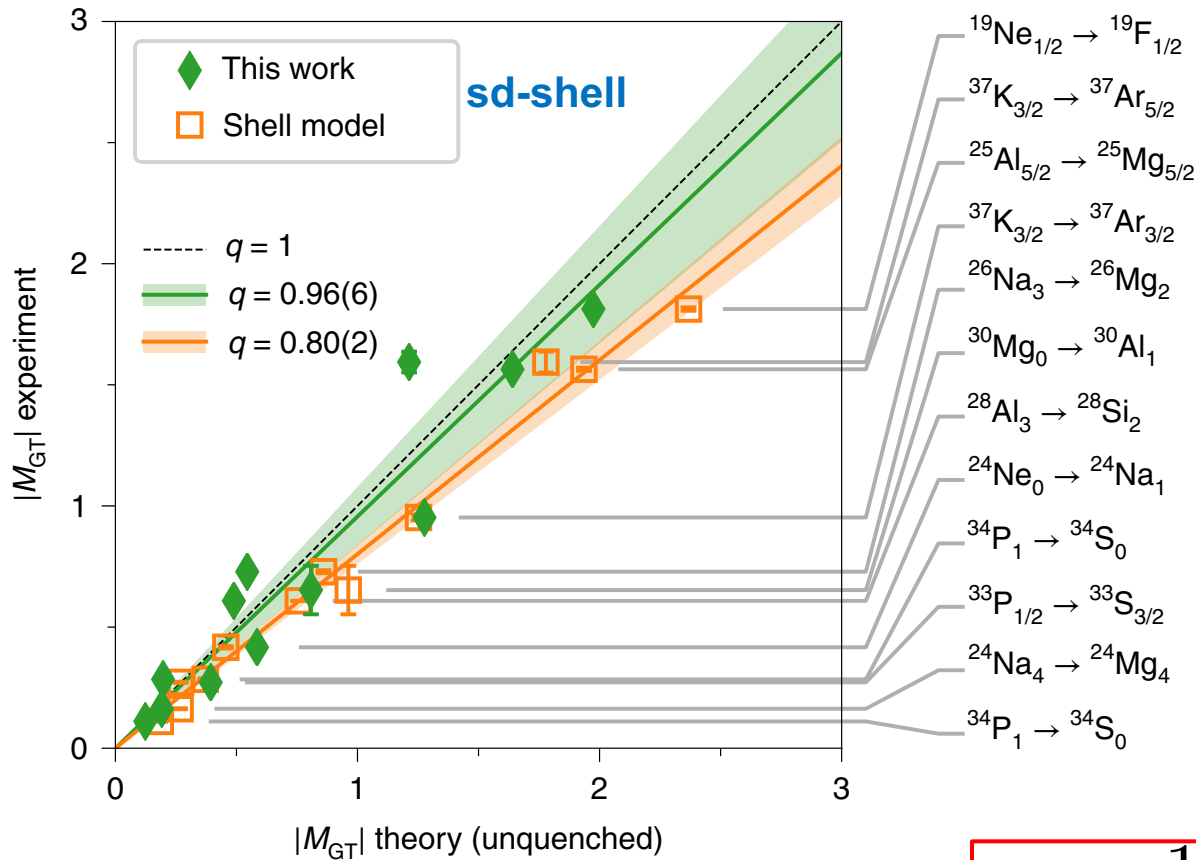
NCSM in light nuclei, CC calculations of GT transition in ^{100}Sn from different forces



Large quenching from correlations in ^{100}Sn

Addition of 2BC further quenches; reduces spread in results

VS-IMSRG calculations throughout sd and pf shells

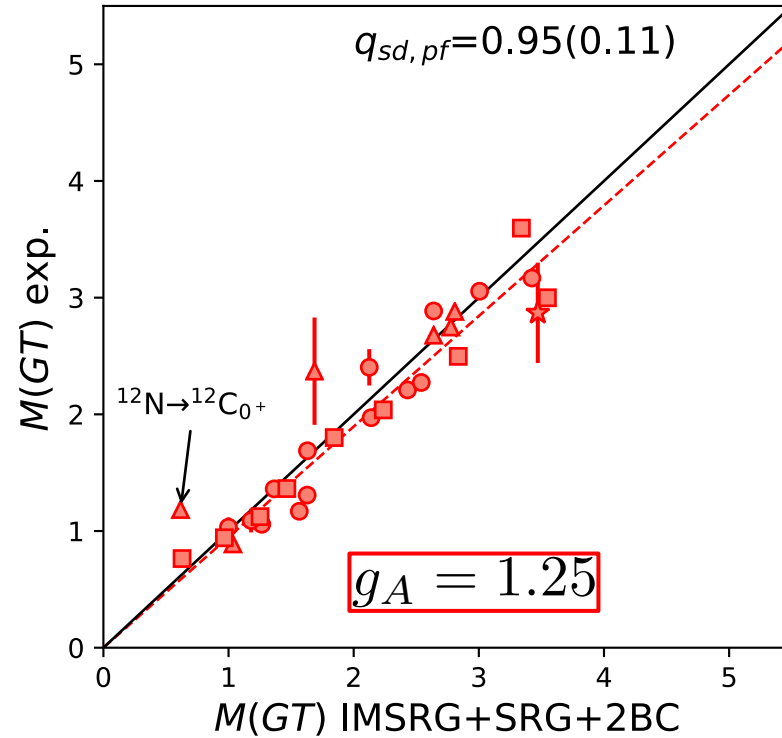
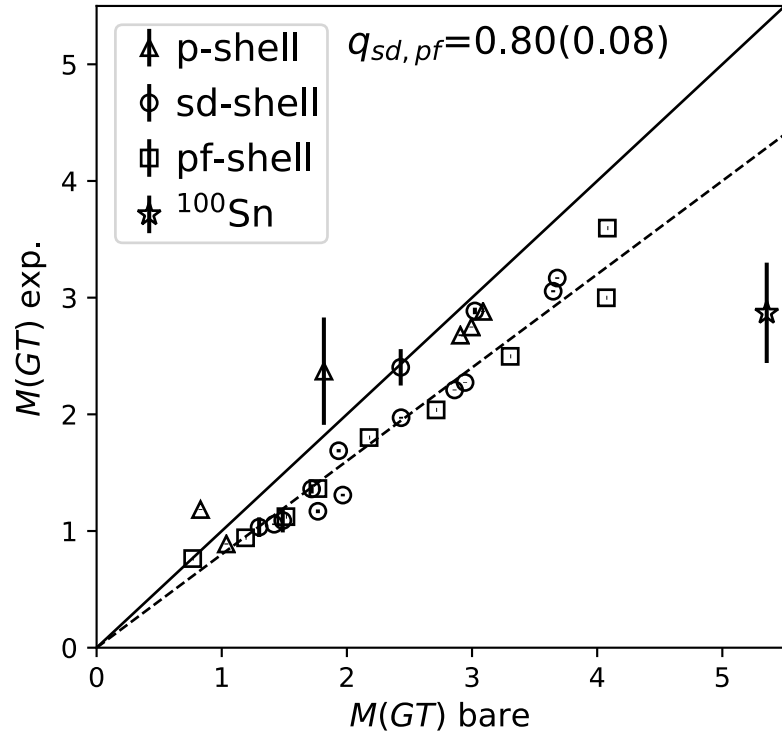


$$g_A = 1.25$$

Ab initio calculations across the chart explain data with unquenched g_A

Refine results: improvements in forces and many-body methods

Ab initio calculations throughout sd and pf shells

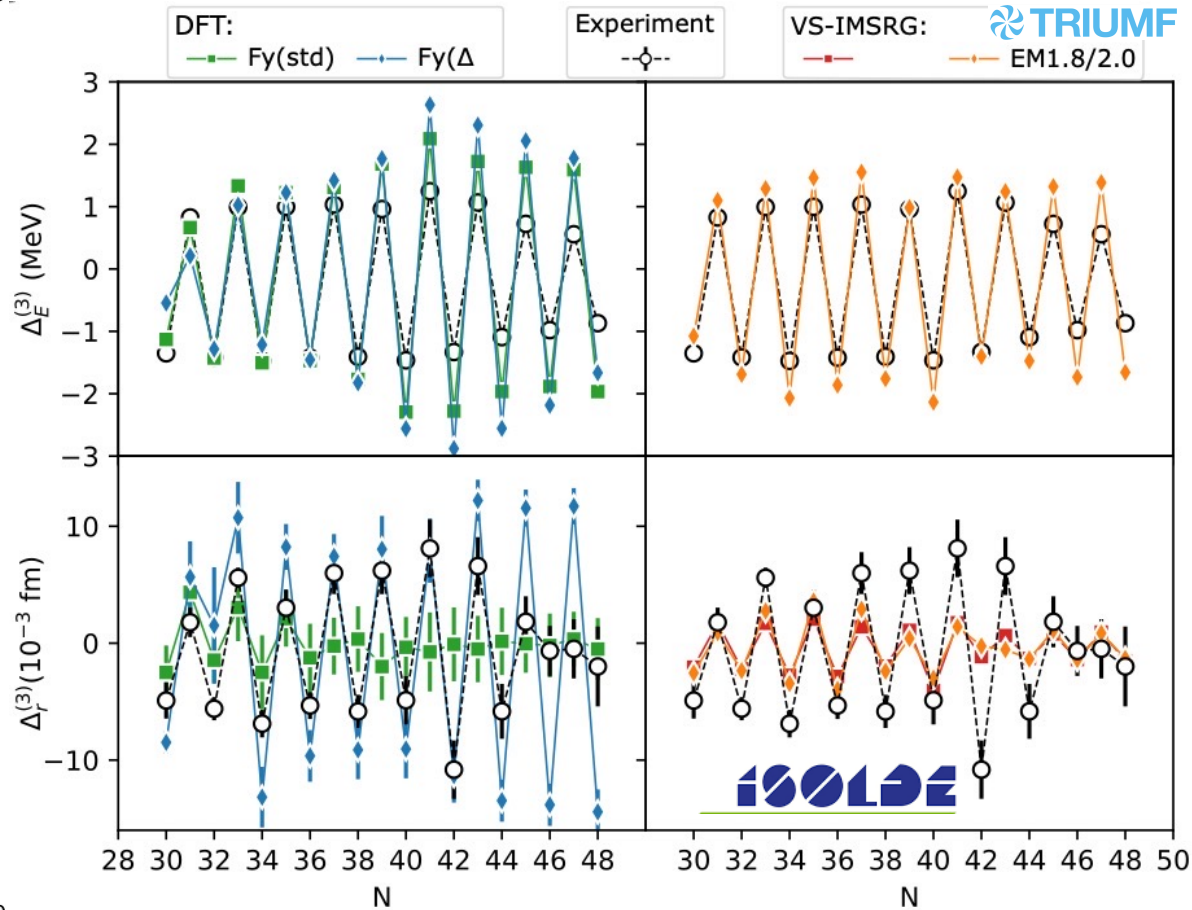
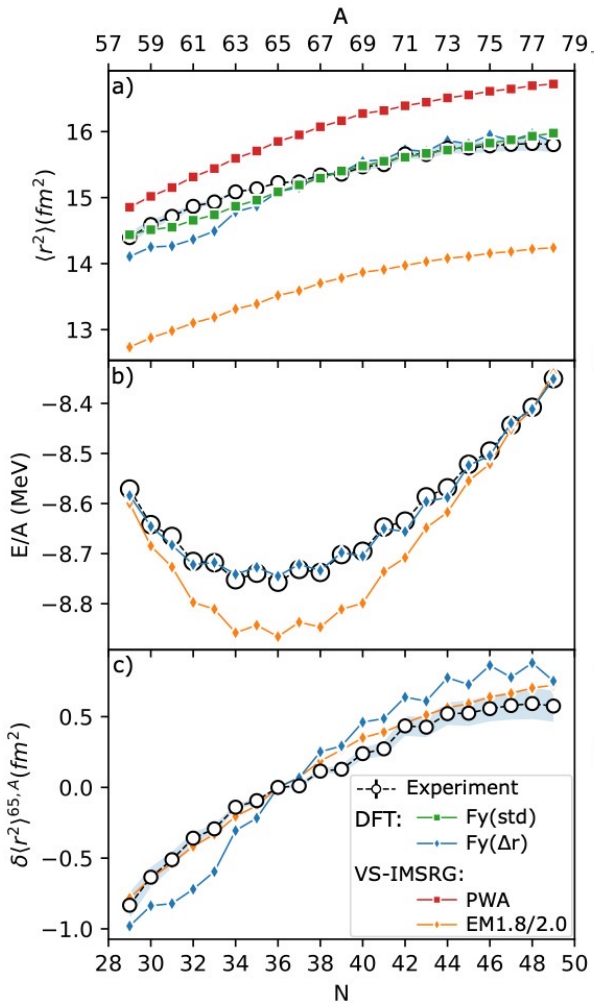


Stroberg (2021)

Ab initio calculations across the chart explain data with unquenched g_A

Including p-shell: $q=0.99(21)$

Odd-even staggering of charge radii across Cu chain



LETTERS
<https://doi.org/10.1038/s41567-020-0868-y>

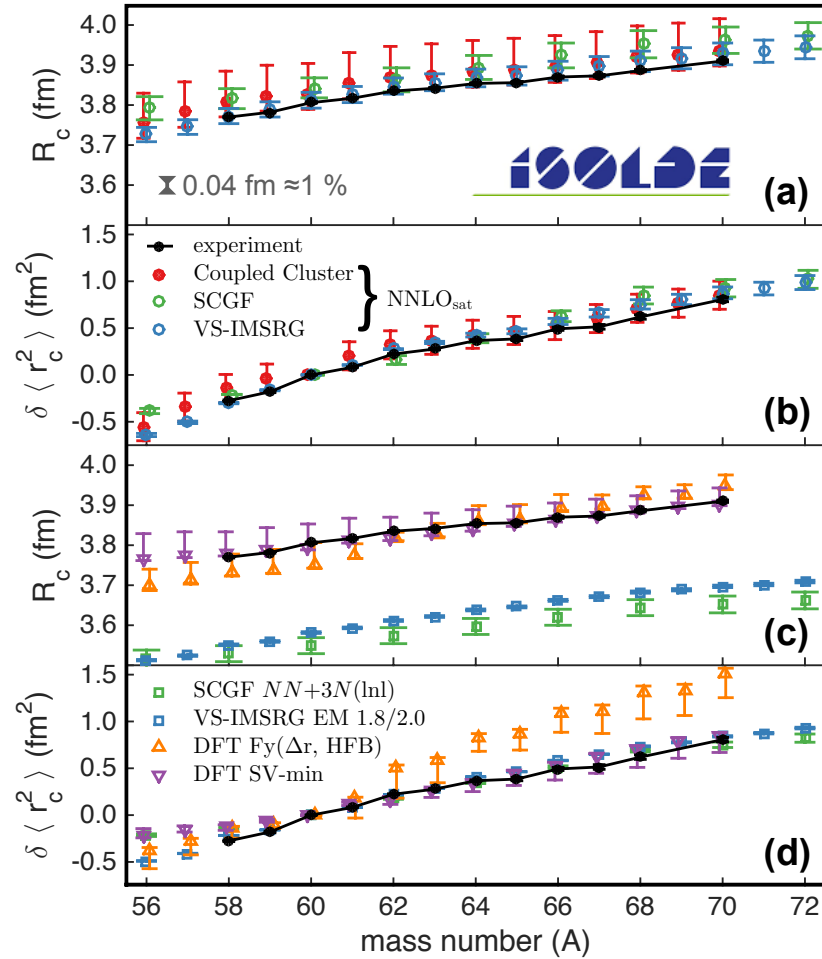
OPEN
Measurement and microscopic description of odd-even staggering of charge radii of exotic copper isotopes

R. P. de Groot^{1,2,3}, J. Billowes³, C. L. Binnersley³, M. L. Bissell³, T. E. Cocolios¹, T. Day Goodacre^{4,5}, G. J. Farooq-Smith¹, D. V. Fedorov⁶, K. T. Flanagan³, S. Franchoo⁷, R. F. Garcia Ruiz^{3,8,9}, W. Gins^{1,2}, J. D. Holt^{5,10}, Á. Koszorus¹, K. M. Lynch⁹, T. Miyagi⁵, W. Nazarewicz¹¹, G. Neyens¹², P.-G. Reinhard¹², S. Rothe^{3,4}, H. H. Stroke¹³, A. R. Vernon^{1,3}, K. D. A. Wendt¹⁴, S. G. Wilkins^{3,4}, Z. Y. Xu¹ and X. F. Yang^{1,15}

Cu isotopes, odd-even staggering well reproduced

Ab initio competitive with DFT (fit to reproduce odd-even staggering)

Study charge radii systematics across Ni isotopic chain



Nuclear Charge Radii of the Nickel Isotopes ^{58–68,70}Ni

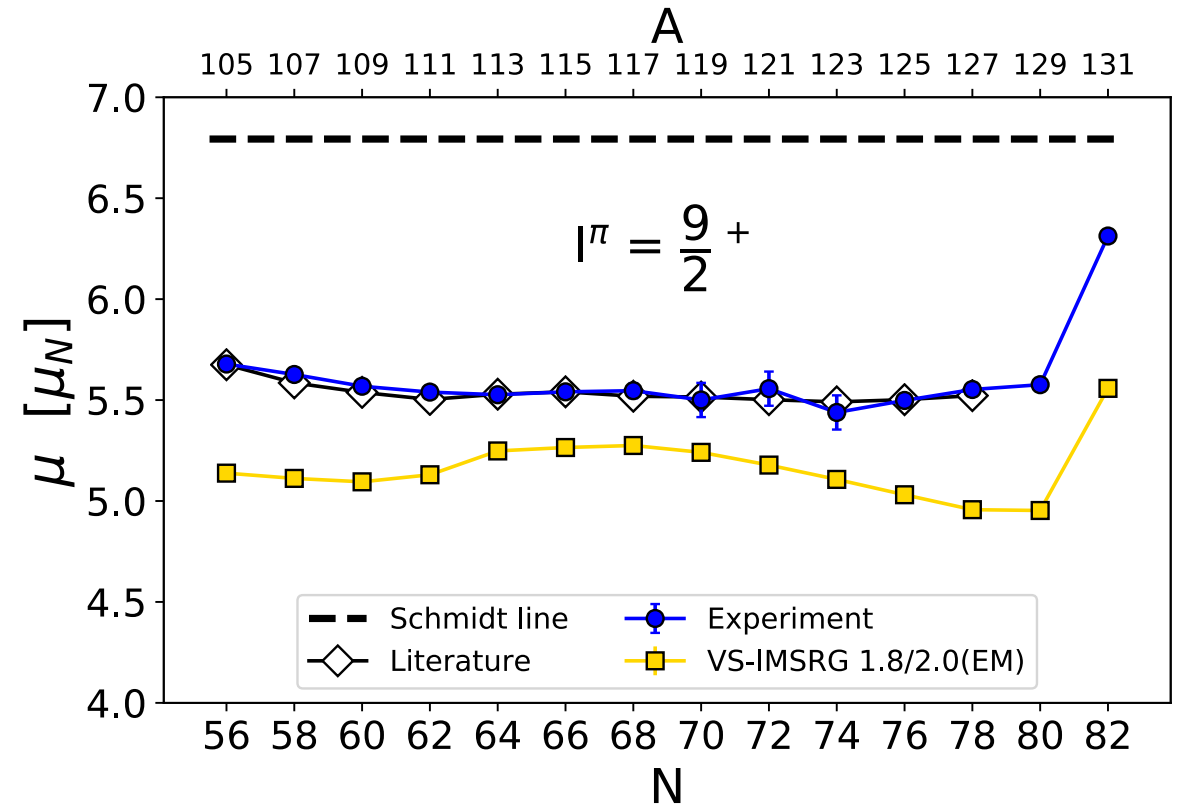
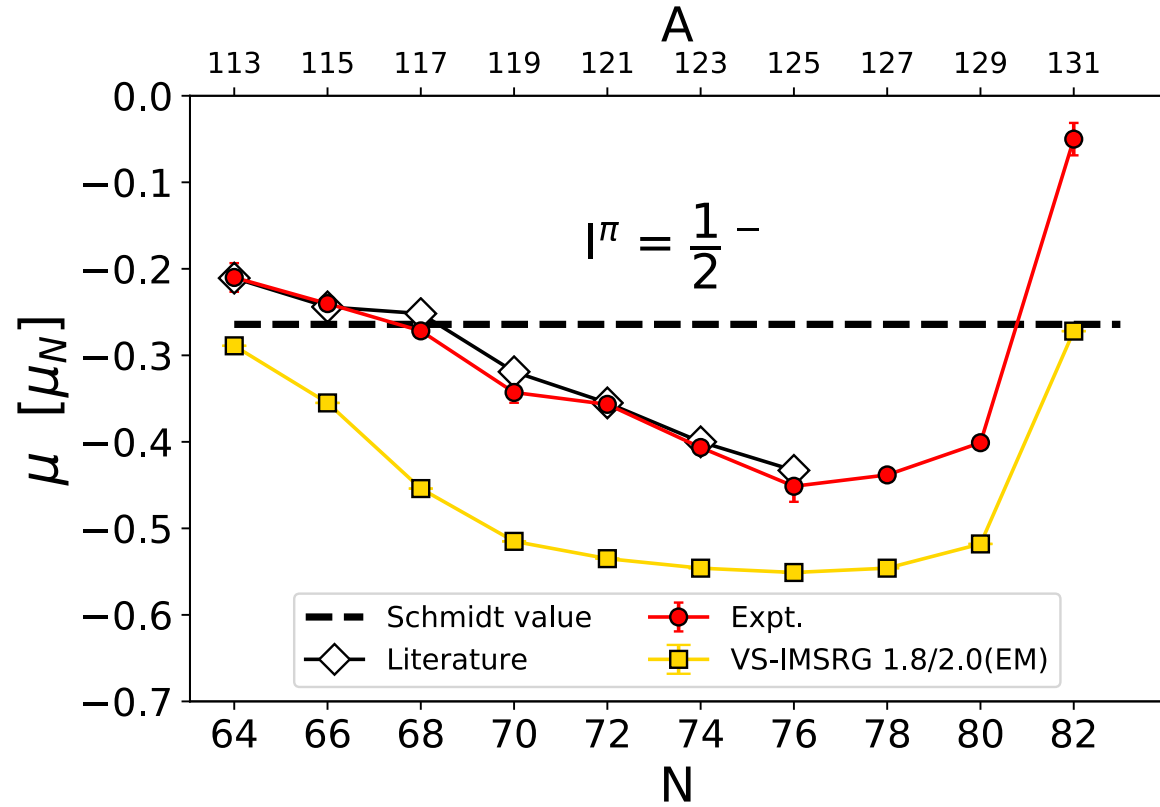
S. Malbrunot-Ettenauer *et al.*

Phys. Rev. Lett. **128**, 022502 – Published 14 January 2022

Multiple **ab-initio methods** largely agree within uncertainties

Ab initio (again) competitive with DFT

Electromagnetic moments of entire In chain – sharp increase at N=82



Ab initio reproduces trends of new measurements

Neglected physics: two-body meson-exchange currents

Article

Nuclear moments of indium isotopes reveal abrupt change at magic number 82

<https://doi.org/10.1038/s41586-022-04818-7>

Received: 10 June 2021

Accepted: 28 April 2022

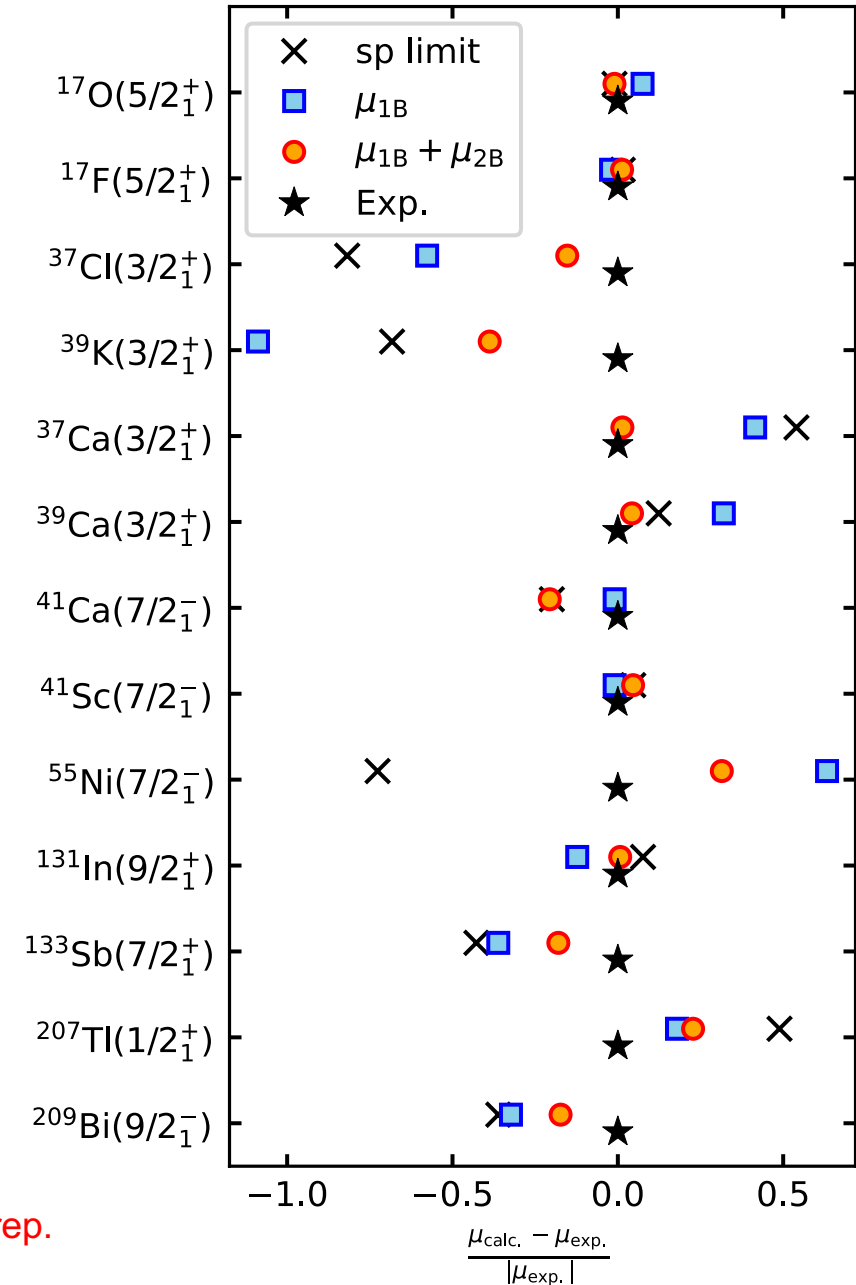
Published online: 13 July 2022

A. R. Vernon^{1,2,3}, R. F. Garcia Ruiz^{2,4}, T. Miyagi⁵, C. L. Binnersley¹, J. Billowes¹, M. L. Bissell¹, J. Bonnard⁶, T. E. Cocolios³, J. Dobaczewski^{6,7}, G. J. Farooq-Smith³, K. T. Flanagan^{1,8}, G. Georgiev⁹, W. Gins^{3,10}, R. P. de Groot^{3,10}, R. Heinke^{4,11}, J. D. Holt^{5,12}, J. Hastings³, Á. Koszorus³, D. Leimbach^{11,13,14}, K. M. Lynch⁴, G. Neyens^{3,4}, S. R. Stroberg¹⁵, S. G. Wilkins¹², X. F. Yang^{3,16} & D. T. Yordanov^{4,9}

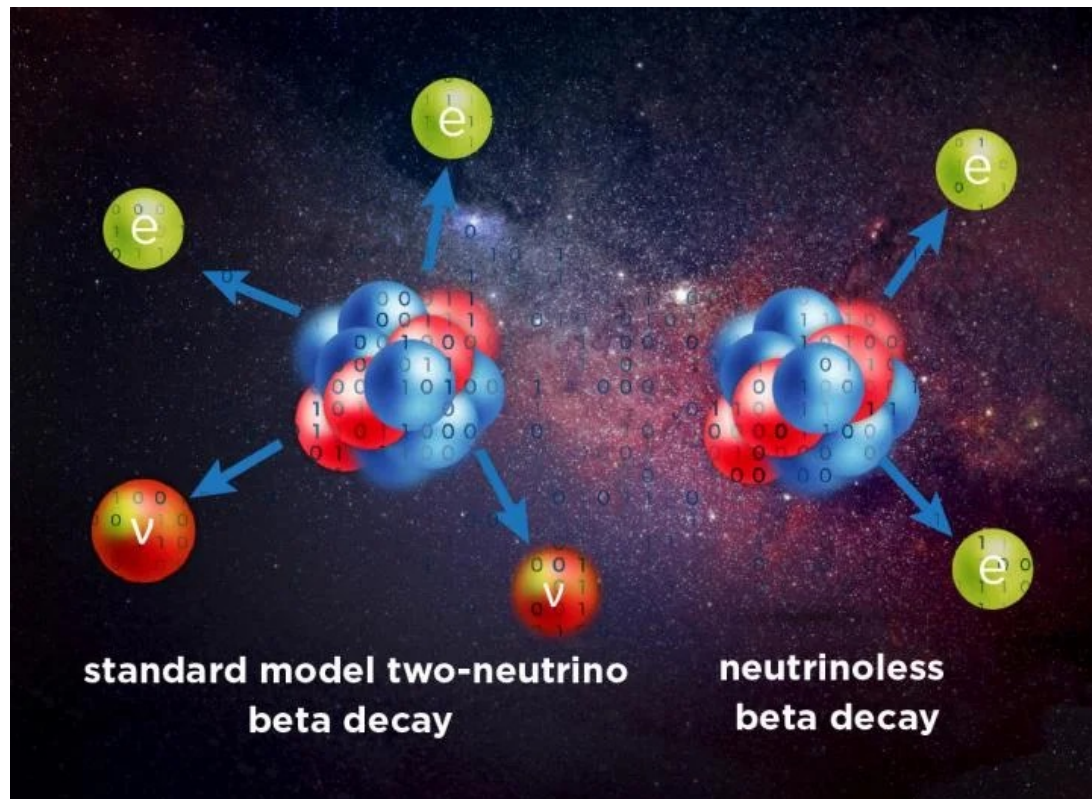
Ab initio calculations throughout the nuclear chart

Including 2bc consistent with input forces

Magnetic moments significantly improved



Neutrinoless Double Beta Decay NMEs for Major Players: ^{76}Ge , (^{100}Mo), ^{130}Te , ^{136}Xe



Ab Initio Treatment of Collective Correlations and the Neutrinoless Double Beta Decay of ^{48}Ca

J. M. Yao, B. Bally, J. Engel, R. Wirth, T. R. Rodríguez, and H. Hergert
Phys. Rev. Lett. **124**, 232501 – Published 11 June 2020

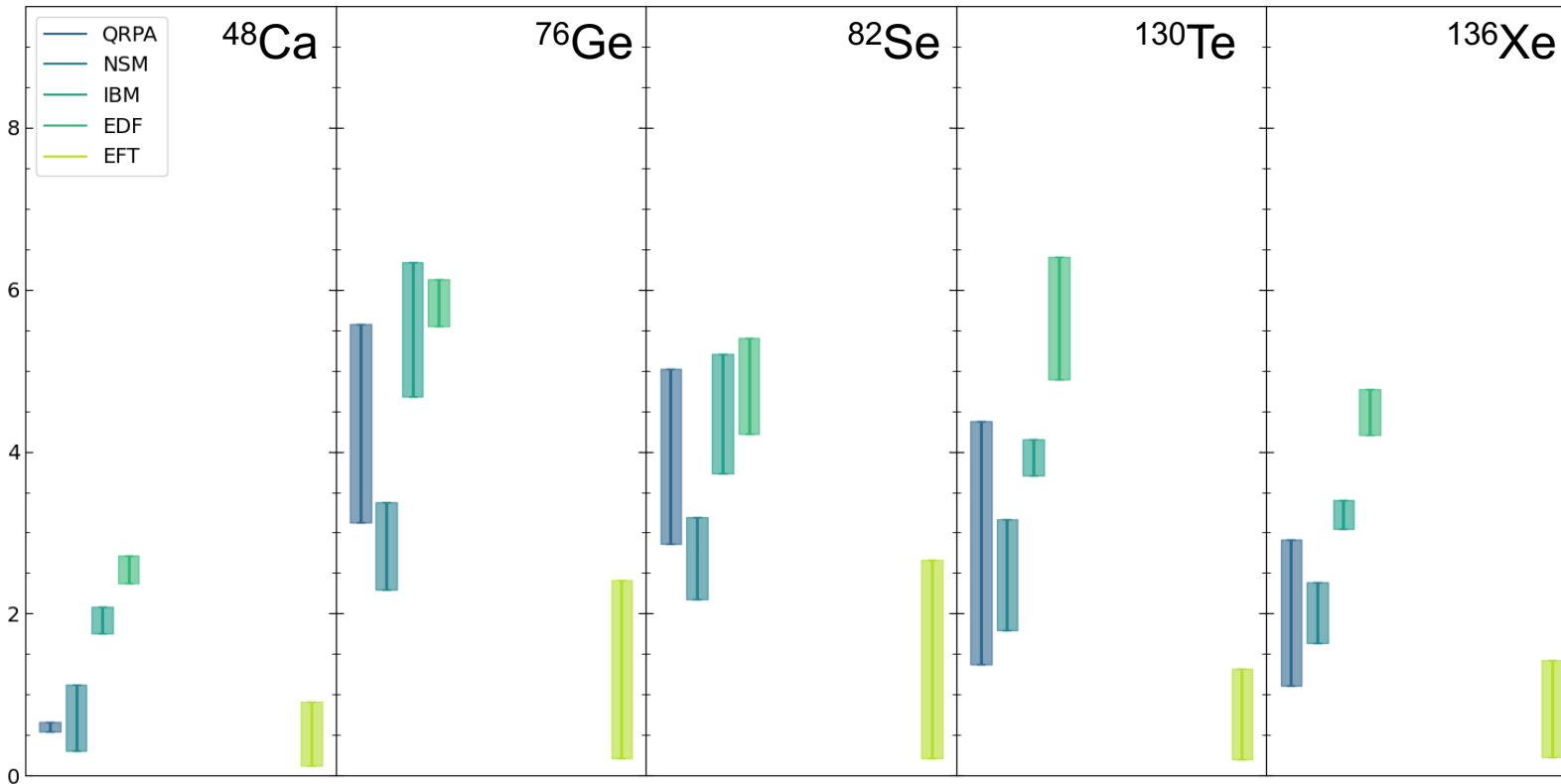
Ab Initio Neutrinoless Double-Beta Decay Matrix Elements for ^{48}Ca , ^{76}Ge , and ^{82}Se

A. Belley, C. G. Payne, S. R. Stroberg, T. Miyagi, and J. D. Holt
Phys. Rev. Lett. **126**, 042502 – Published 29 January 2021

Coupled-Cluster Calculations of Neutrinoless Double- β Decay in ^{48}Ca

S. Novario, P. Gysbers, J. Engel, G. Hagen, G. R. Jansen, T. D. Morris, P. Navrátil, T. Papenbrock, and S. Quaglioni
Phys. Rev. Lett. **126**, 182502 – Published 7 May 2021

Calculations to date from phenomenological models; large spread in results

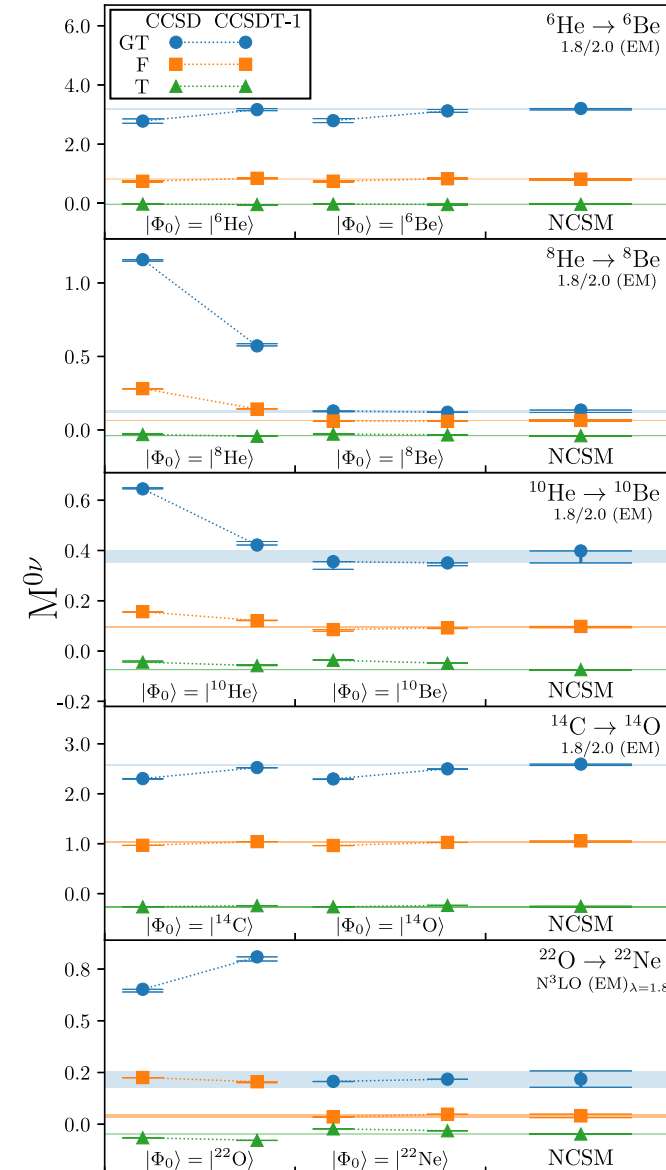
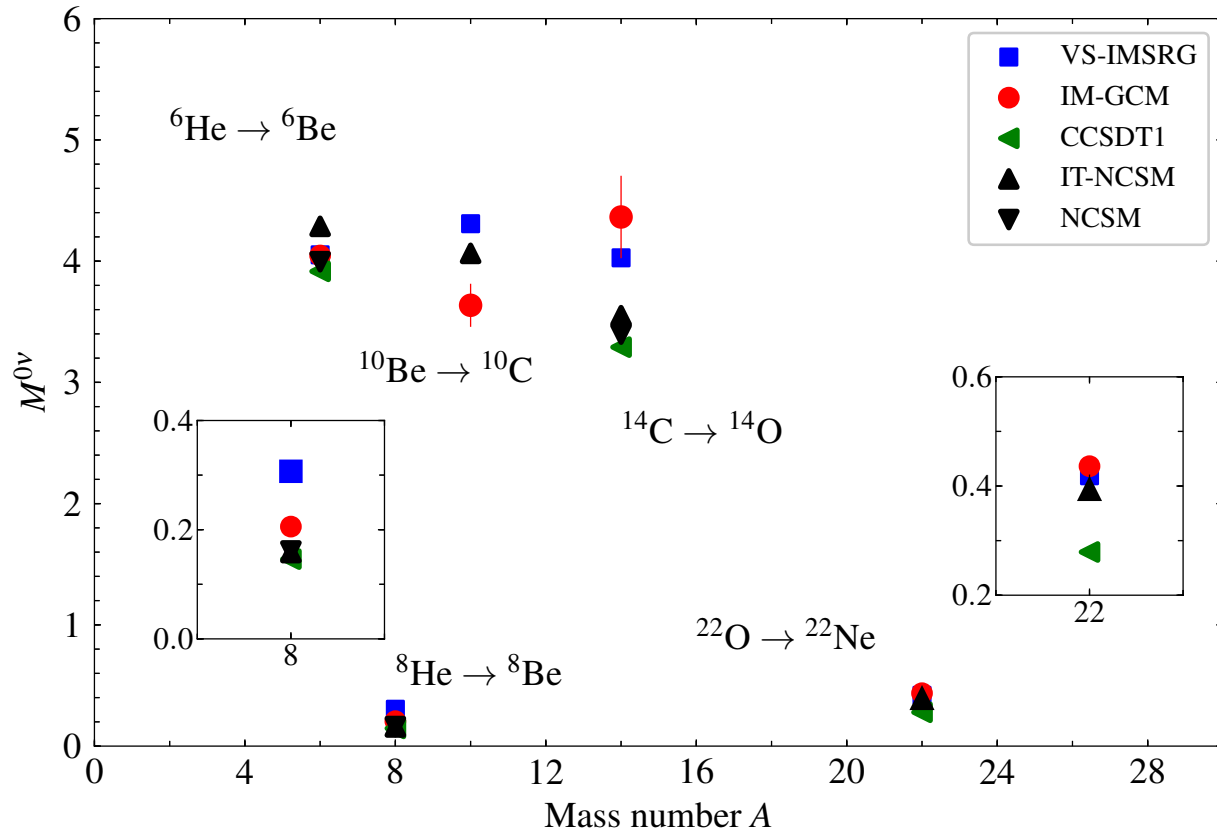


Compiled values from: Engel and Menéndez (2017); Brase et al, PRC (2022)

All models missing essential physics: correlations, single-particle levels, two-body currents

Address with ab initio theory

Benchmark with **quasi-exact NCSM**, IT-NCSM, IM-GCM, and CC in light systems: $A=6-22$

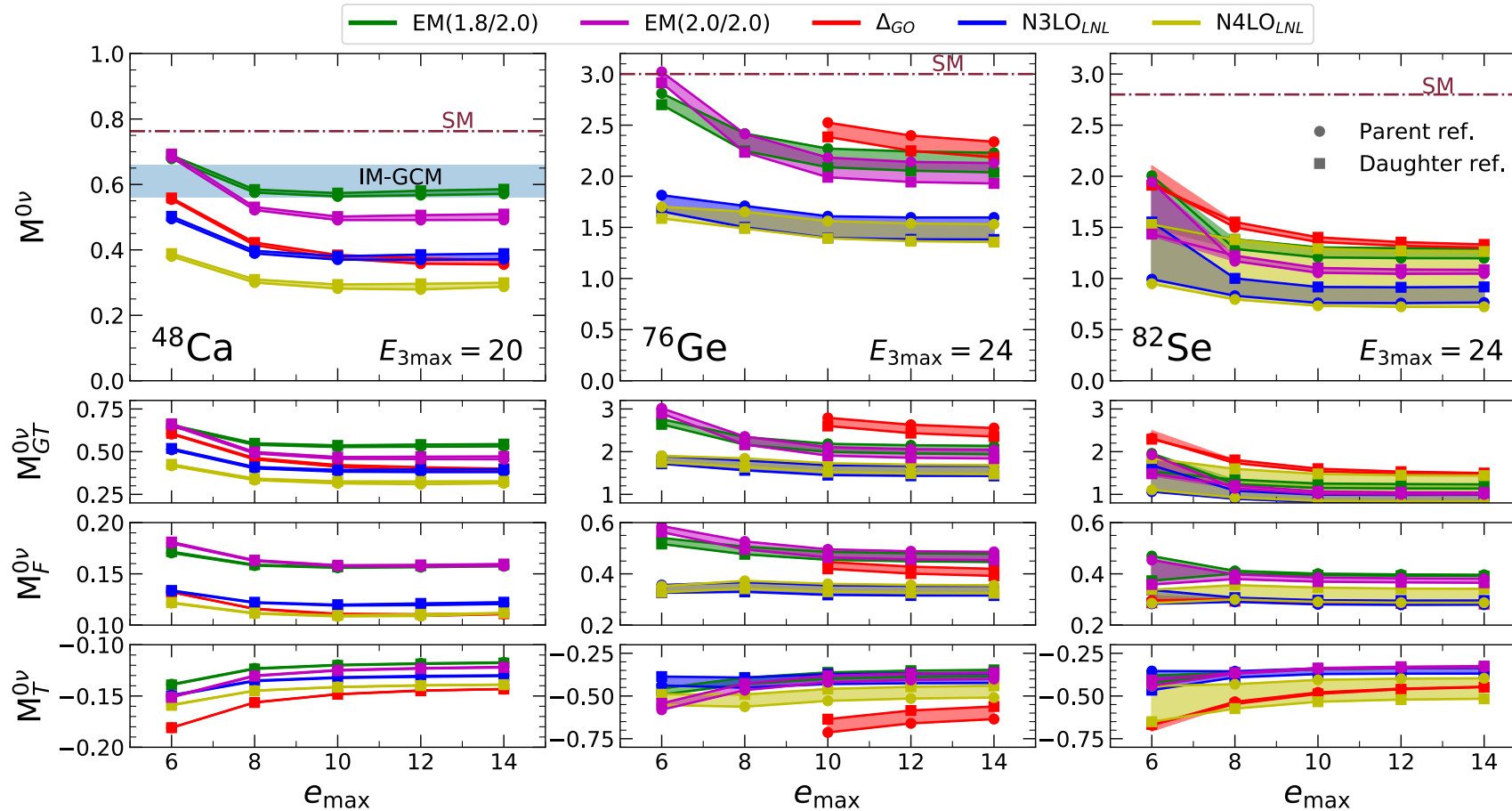


Reasonable to good agreement in all cases

Pursue true double-beta decay candidates!

“Uncertainty” bands from input NN+3N forces with **5 chiral Hamiltonians**

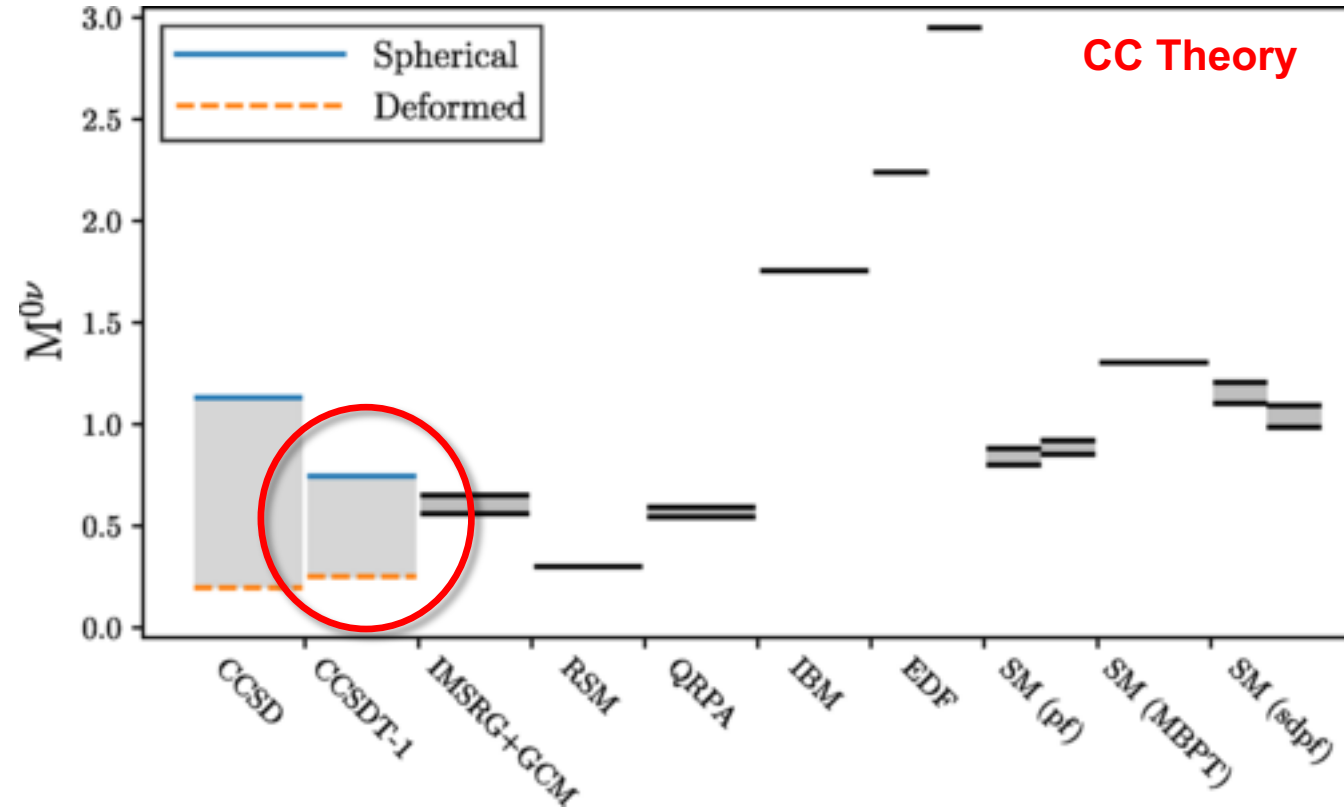
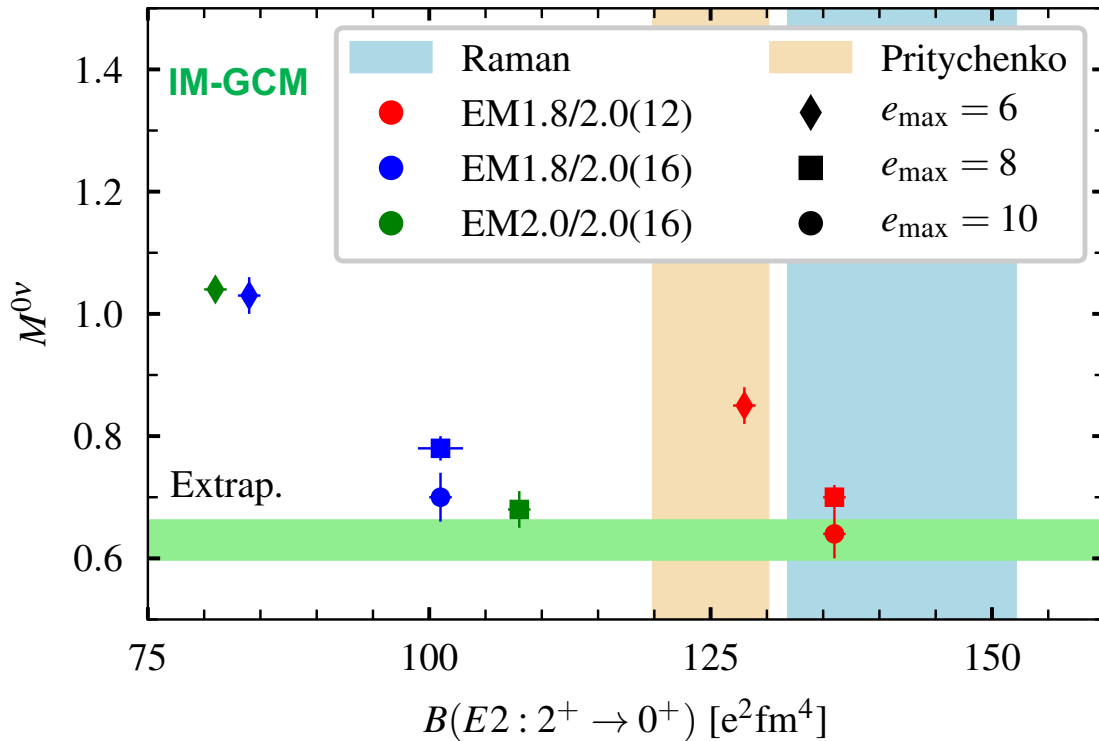
VS-IMSRG: clear convergence for ^{48}Ca , ^{76}Ge , ^{82}Se



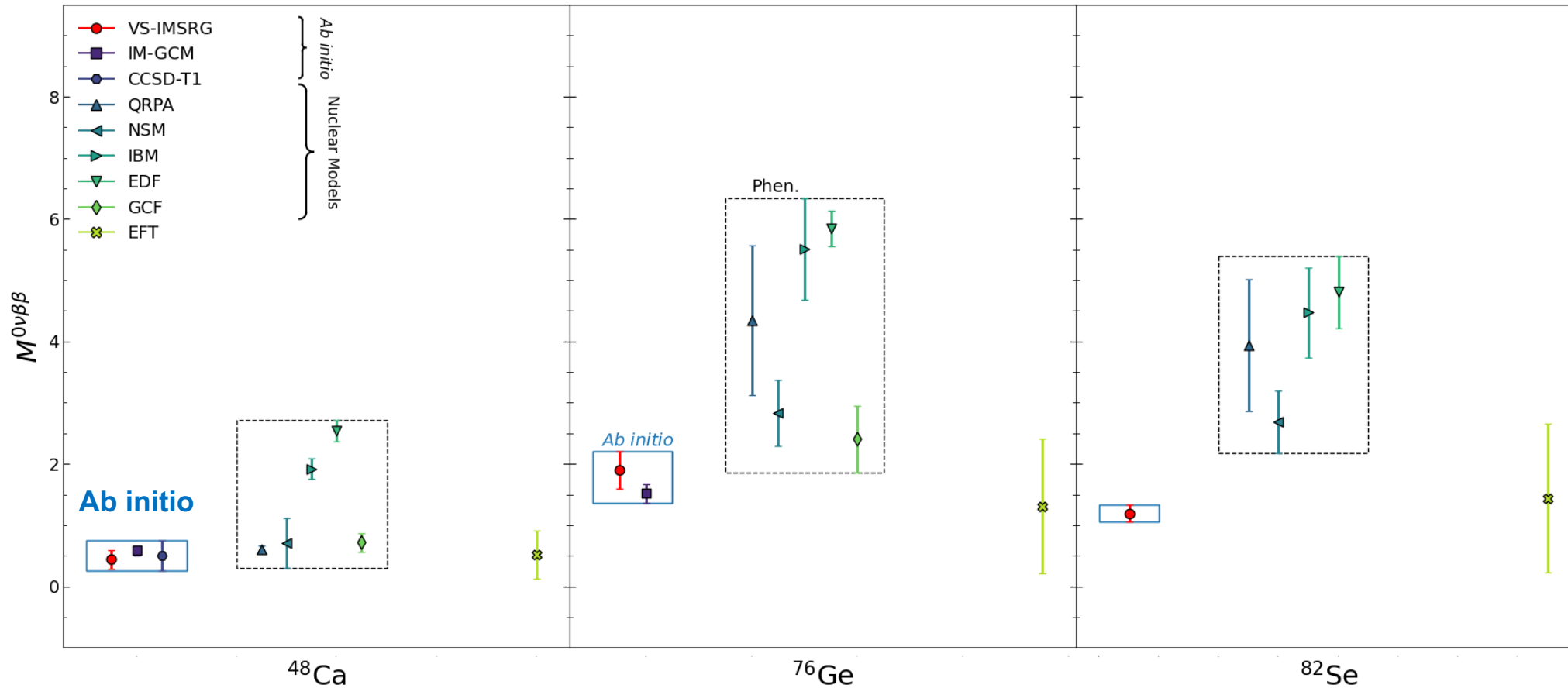
TRIUMF Strategy II: “Uncertainties” from Many-Body Methods

Calculations in ^{48}Ca from IM-GCM and CC theory using same interactions

Key development: **treatment of deformation** in **CC** and **IMSRG**



Ab initio NMEs generally smaller than phenomenology; less spread from uncertainties



Ab initio results agree within uncertainties!

Promising results, but...

Proper renormalization requires short-range contact term at leading order

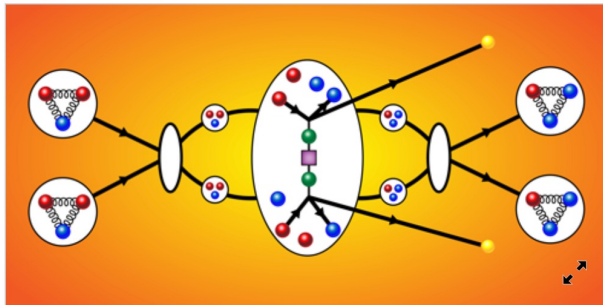


SYNOPSIS

A Missing Piece in the Neutrinoless Beta-Decay Puzzle

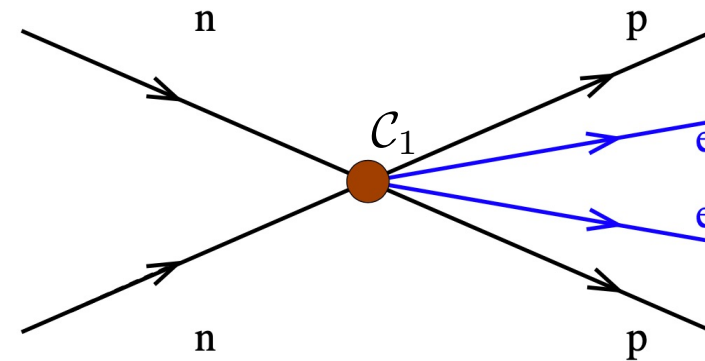
May 16, 2018 • *Physics* 11, s58

The inclusion of short-range interactions in models of neutrinoless double-beta decay could impact the interpretation of experimental searches for the elusive decay.



J. de Vries/Nikhef, adapted by APS/Alan Stonebraker

Cirigliano et al. PRL (2018)

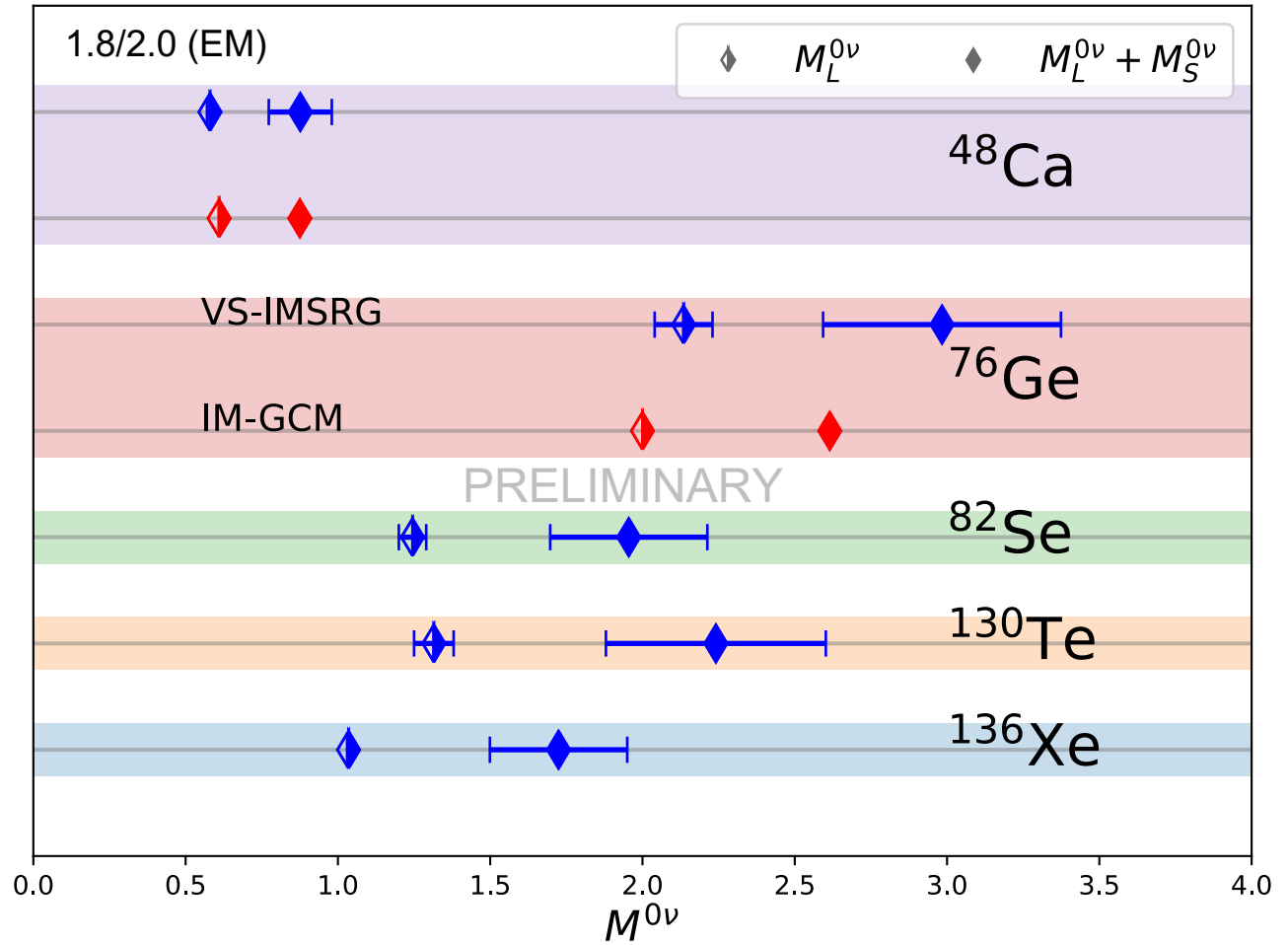
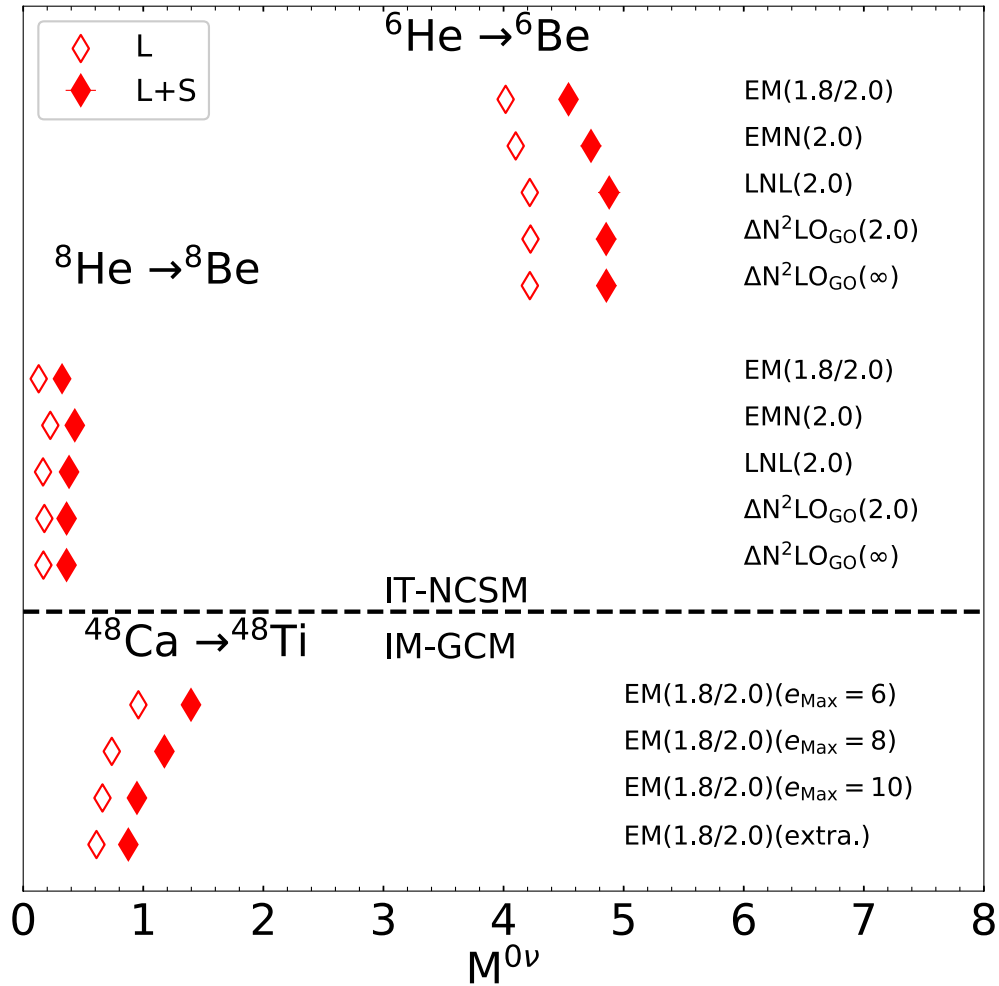


New physics inside blob:
High-energy ν exchange

New paradigm for $0\nu\beta\beta$ decay: include long- and short-range terms

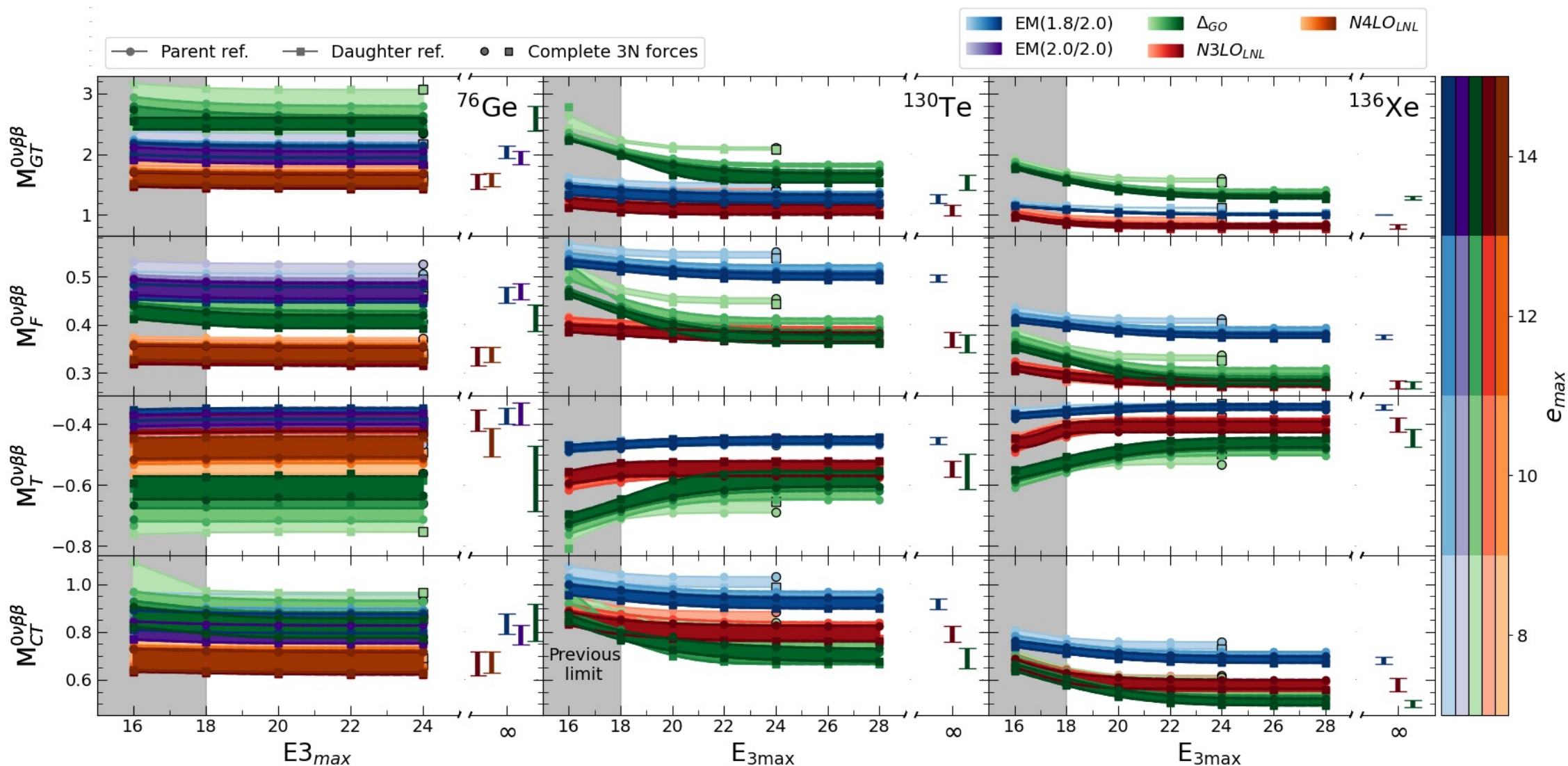
$$M^{0\nu} \rightarrow M_L + M_S = M_{GT} + \frac{M_F}{g_A^2} + M_T + M_{CT}$$

Match $nn \rightarrow pp+ee$ amplitude from approximate QCD methods: **estimate contact term to 30%**



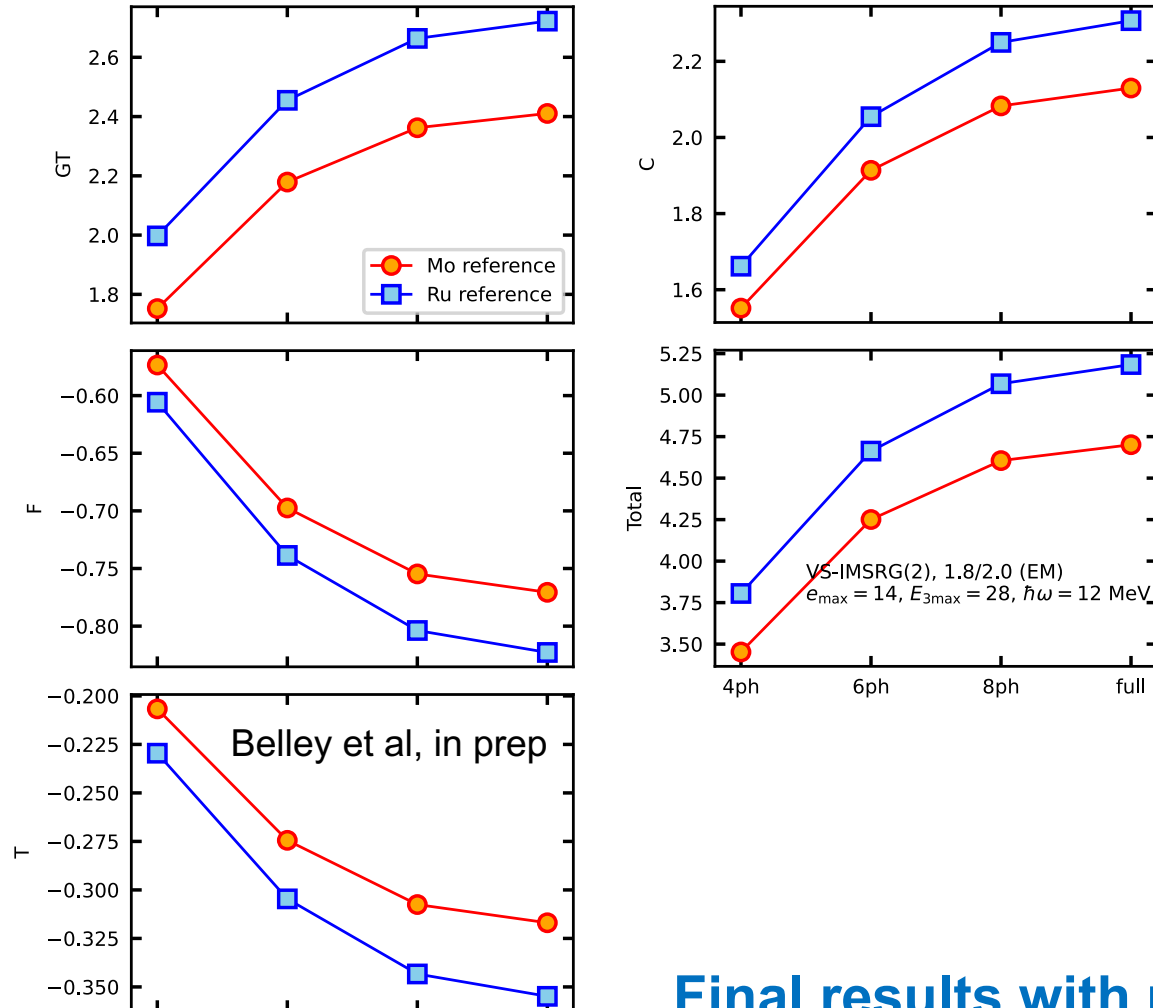
Increase of 40% (${}^{76}\text{Ge}$) to 60% (${}^{130}\text{Te}/{}^{136}\text{Xe}$)

Converged NMEs for major players in global searches: ^{76}Ge , ^{130}Te , ^{136}Xe



Final competitive candidate in worldwide searches: AMoRE, NEMO 3, CUORE...

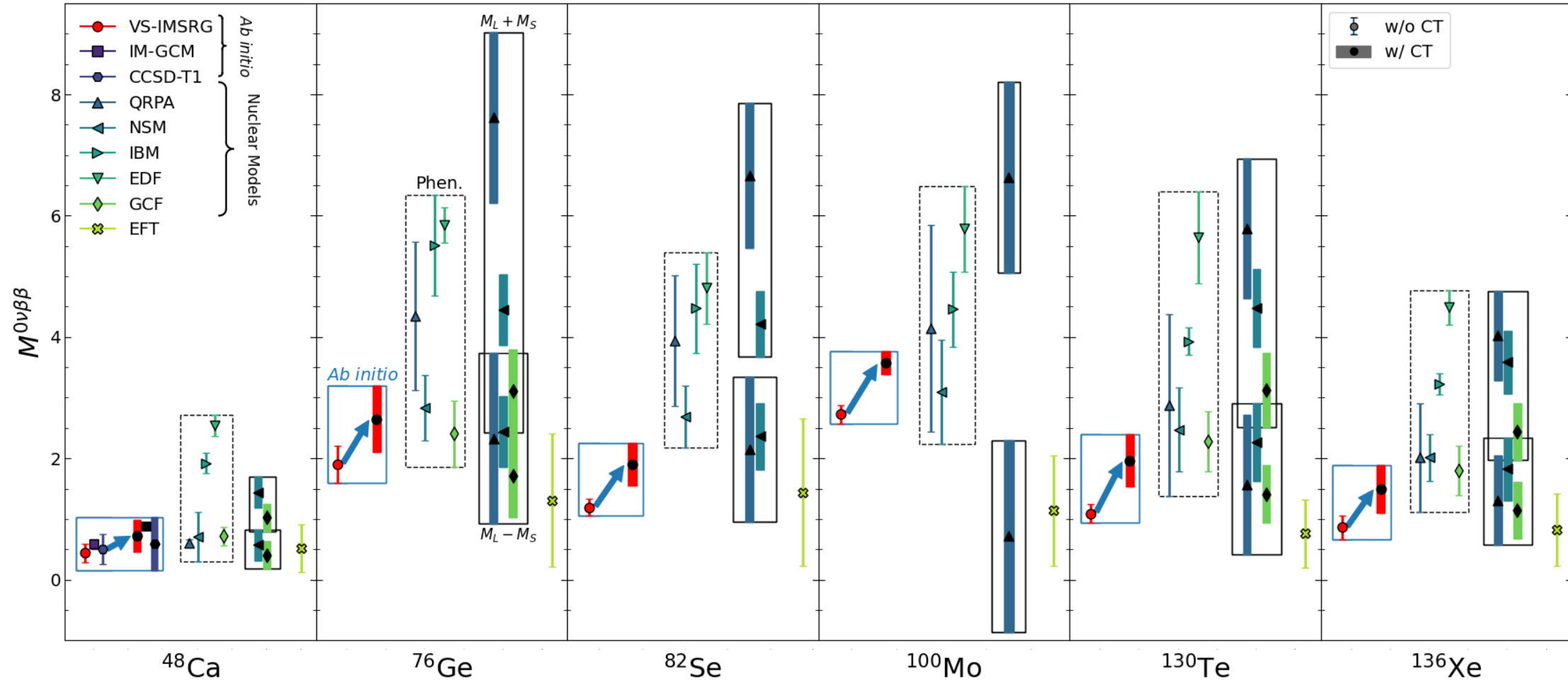
Highly mid-shell, difficult for SM - access with p-h truncations in KSHELL



Final results with multiple NN+3N forces coming soon!

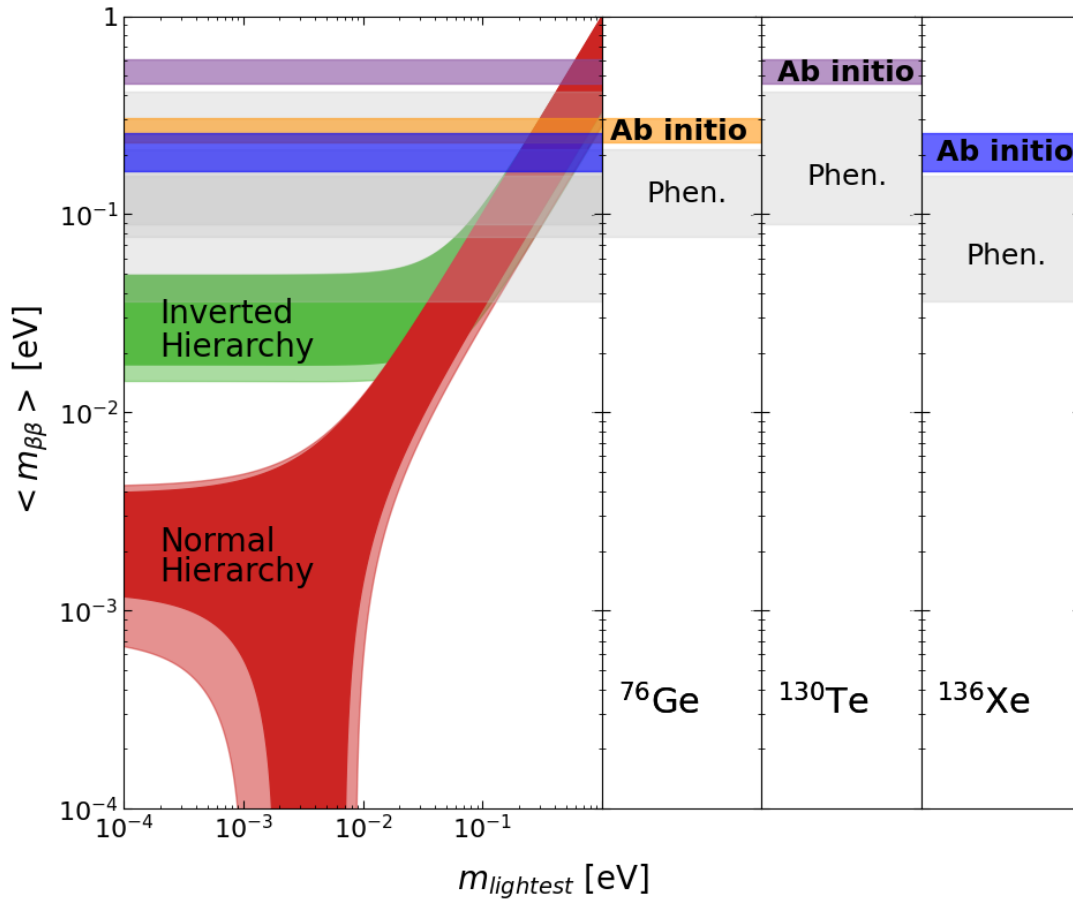
Converged NMEs for major players in global searches: ^{76}Ge , ^{100}Mo , ^{130}Te , ^{136}Xe

Ab initio results: differences from models; **large NMEs strongly disfavored**



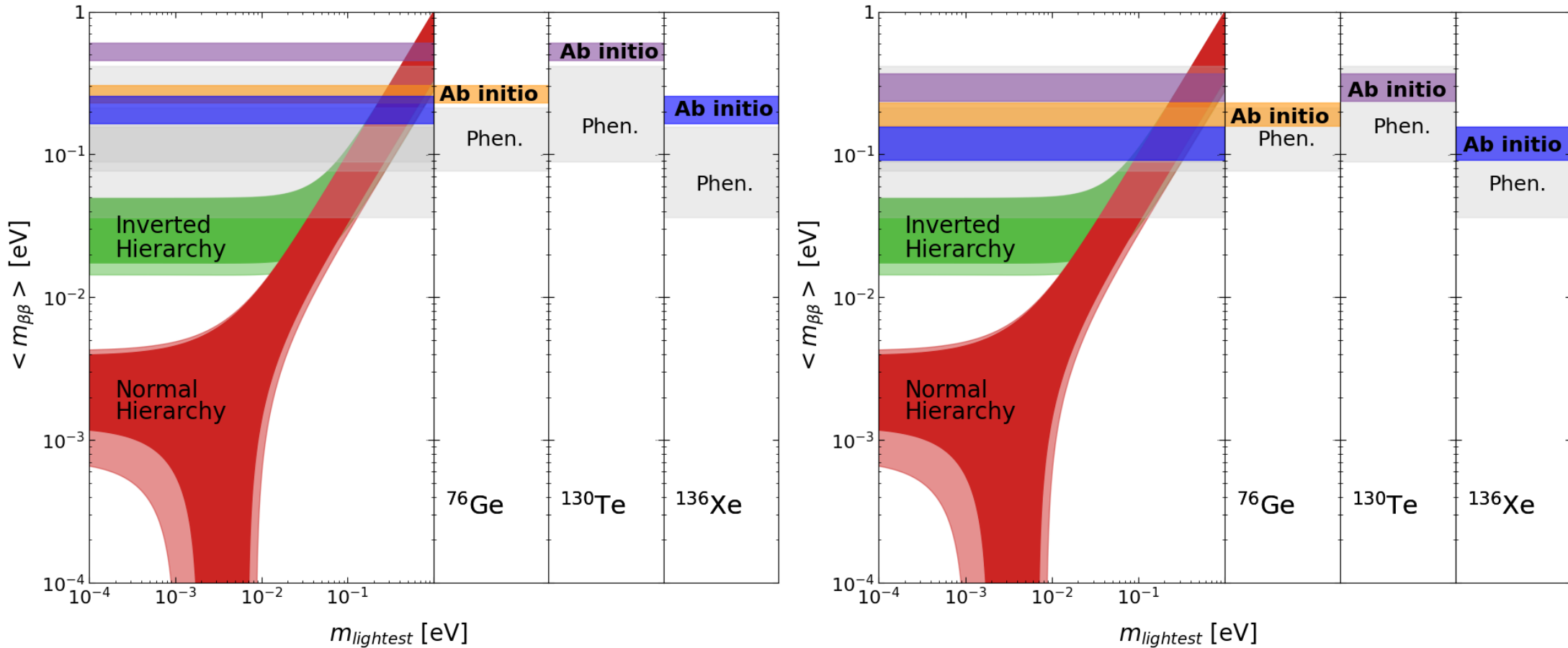
Impact for next-generation searches: Large matrix elements disfavored, lowers expected rates

Current experimental reach – more than an order of magnitude diminished



Impact for next-generation searches: Large matrix elements disfavored, lowers expected rates

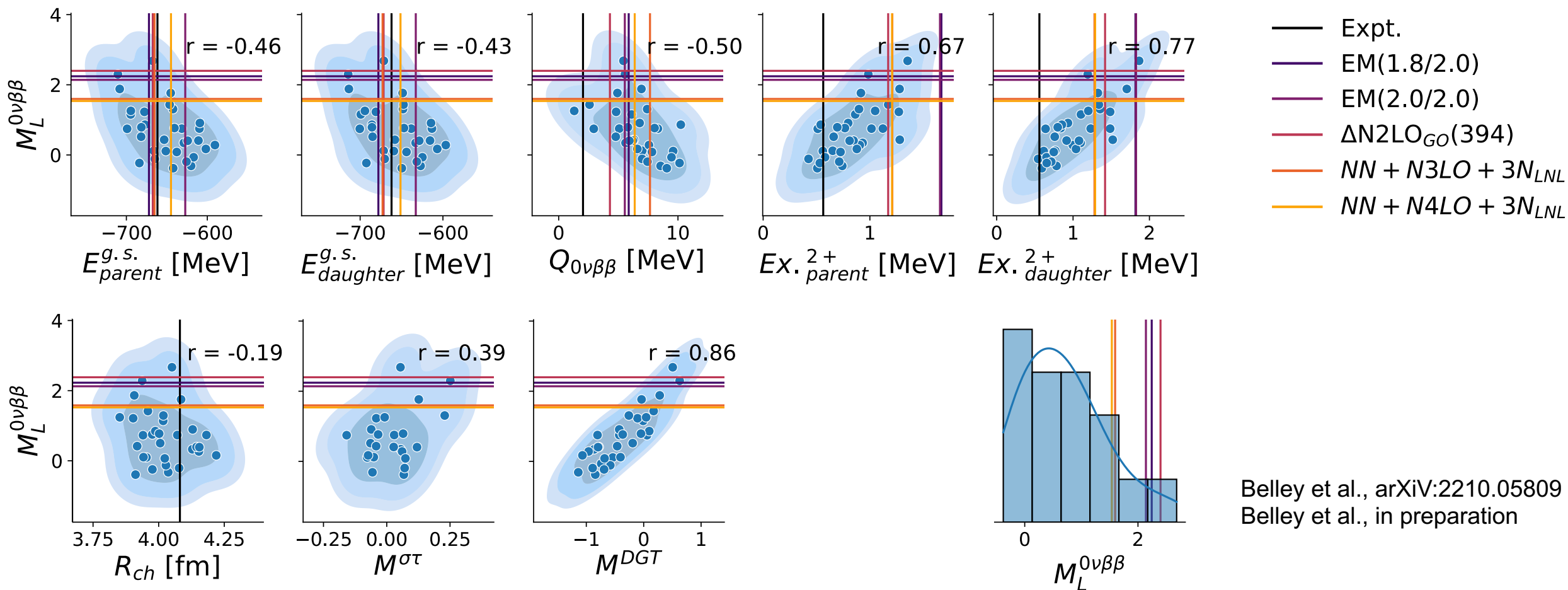
Current experimental reach – improved with effects of contact term,



Not the end of the story: estimate three-body corrections + two-body currents

^{76}Ge : Explore correlations with other observables from systematic analysis (34 interactions)

Few clear correlations, except DGT



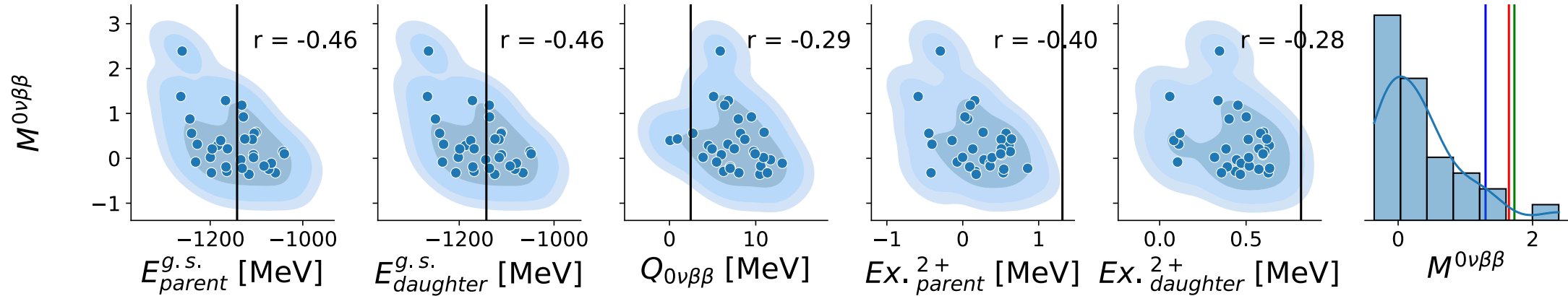
Belley et al., arXiv:2210.05809
 Belley et al., in preparation

Maybe with first excited 2^+ states?

Explore correlations with other observables from systematic analysis (34 interactions)

Few clear correlations, except DGT

Similar picture in ^{136}Xe ... BUT no correlation with 2^+

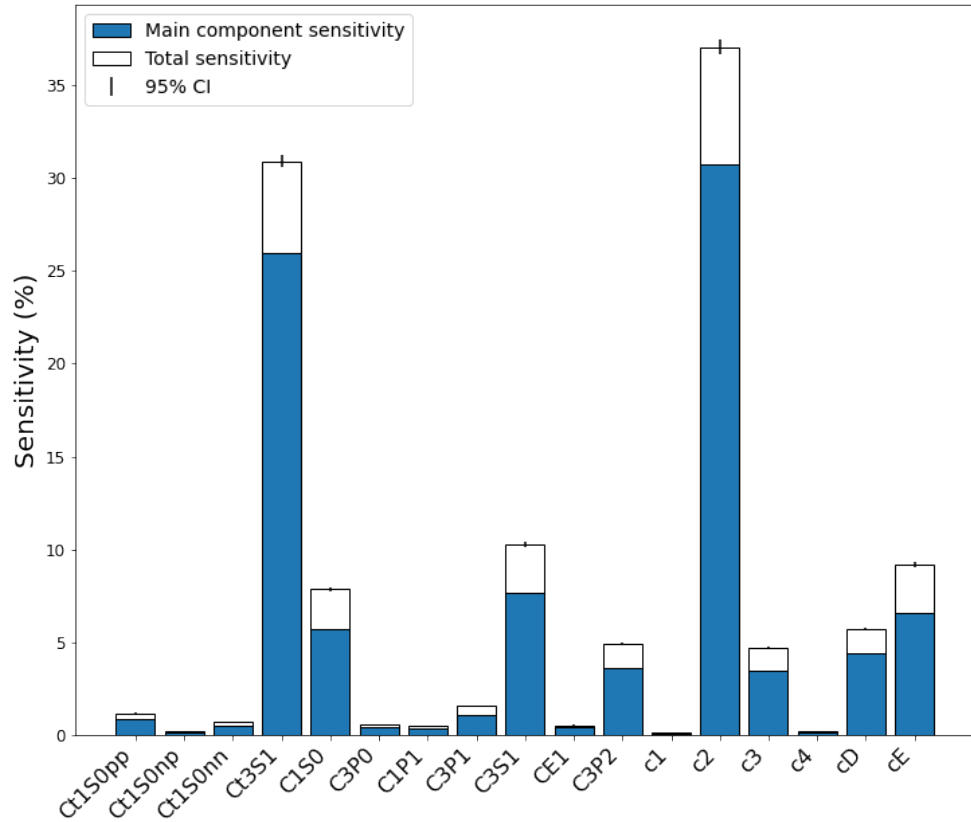


Explore correlations with other observables from systematic analysis (34 interactions)

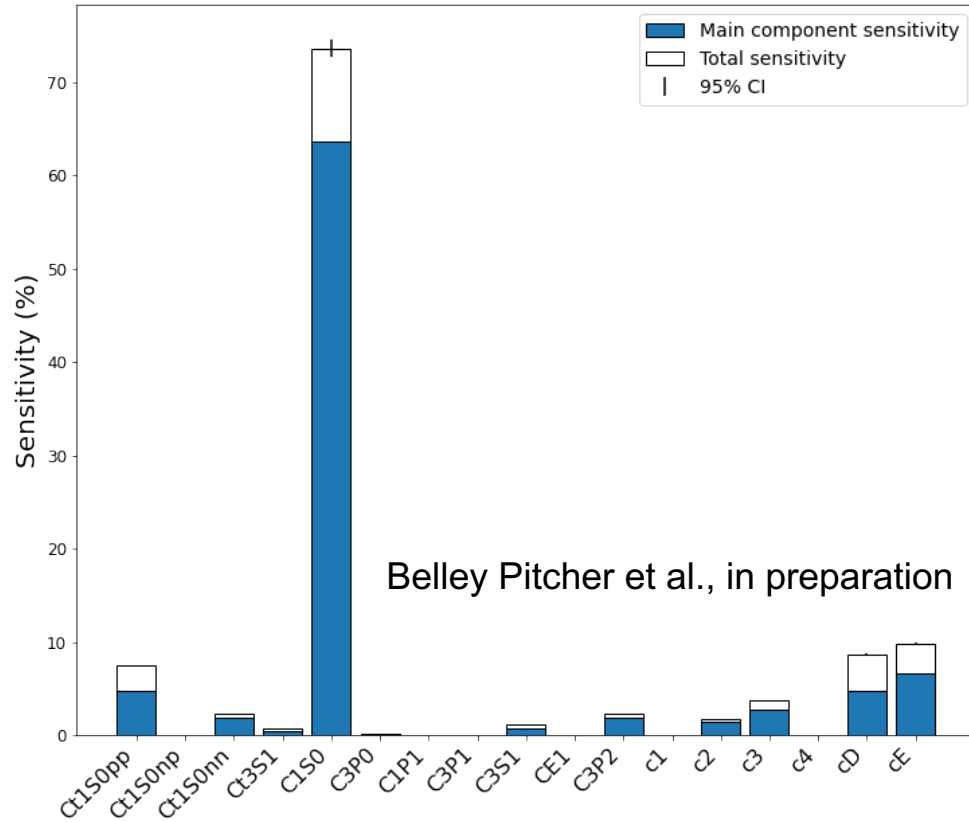
Similar sensitivity as found in ^{208}Pb study!

26

Ground state energies



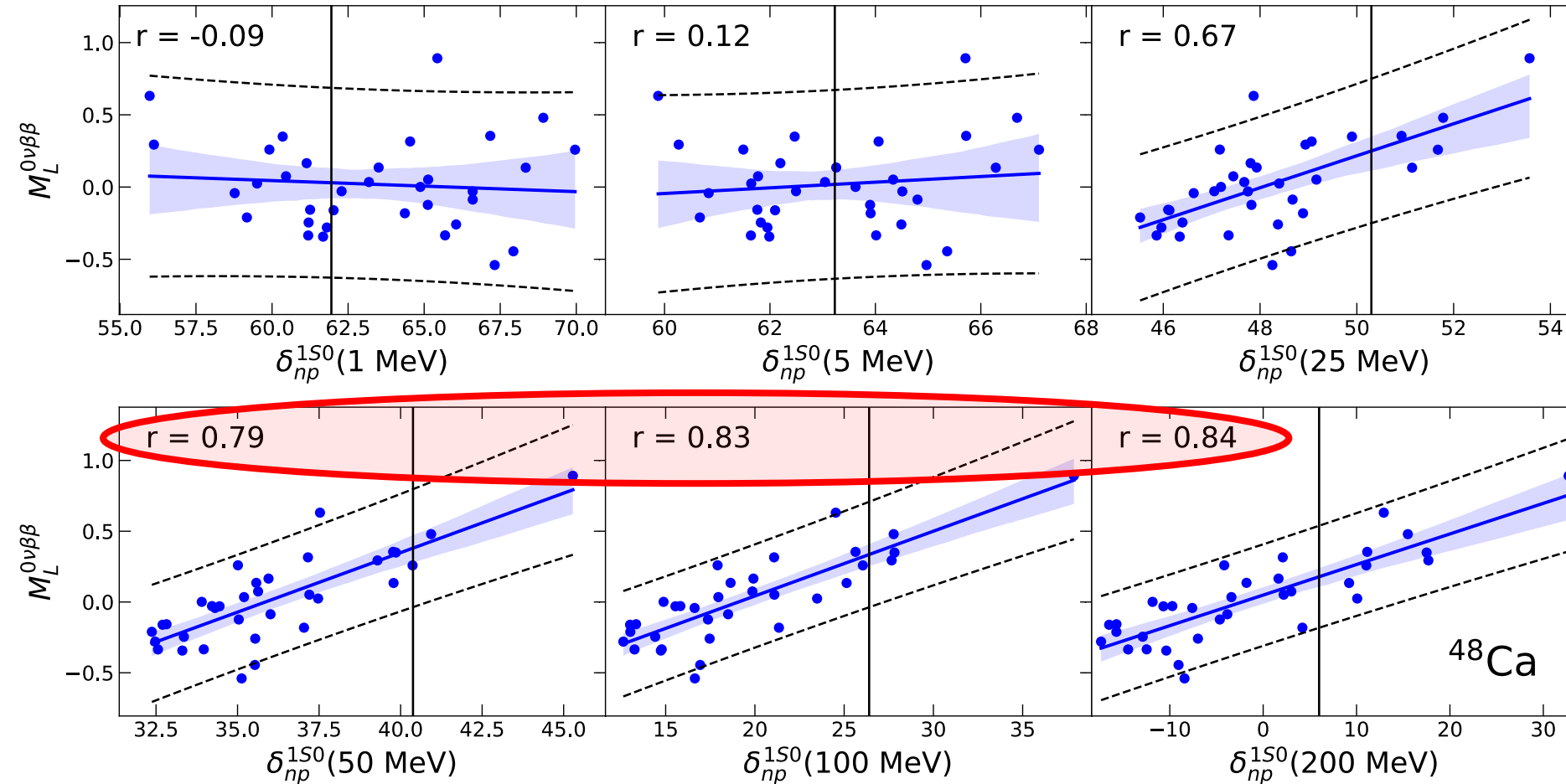
$M_L^{0\nu}$



Highly sensitive to C150 – possible correlation with $^1\text{S}_0$ phase shift (observable!)

Explore correlations with 1S_0 phase shift from 34 non-implausible interactions

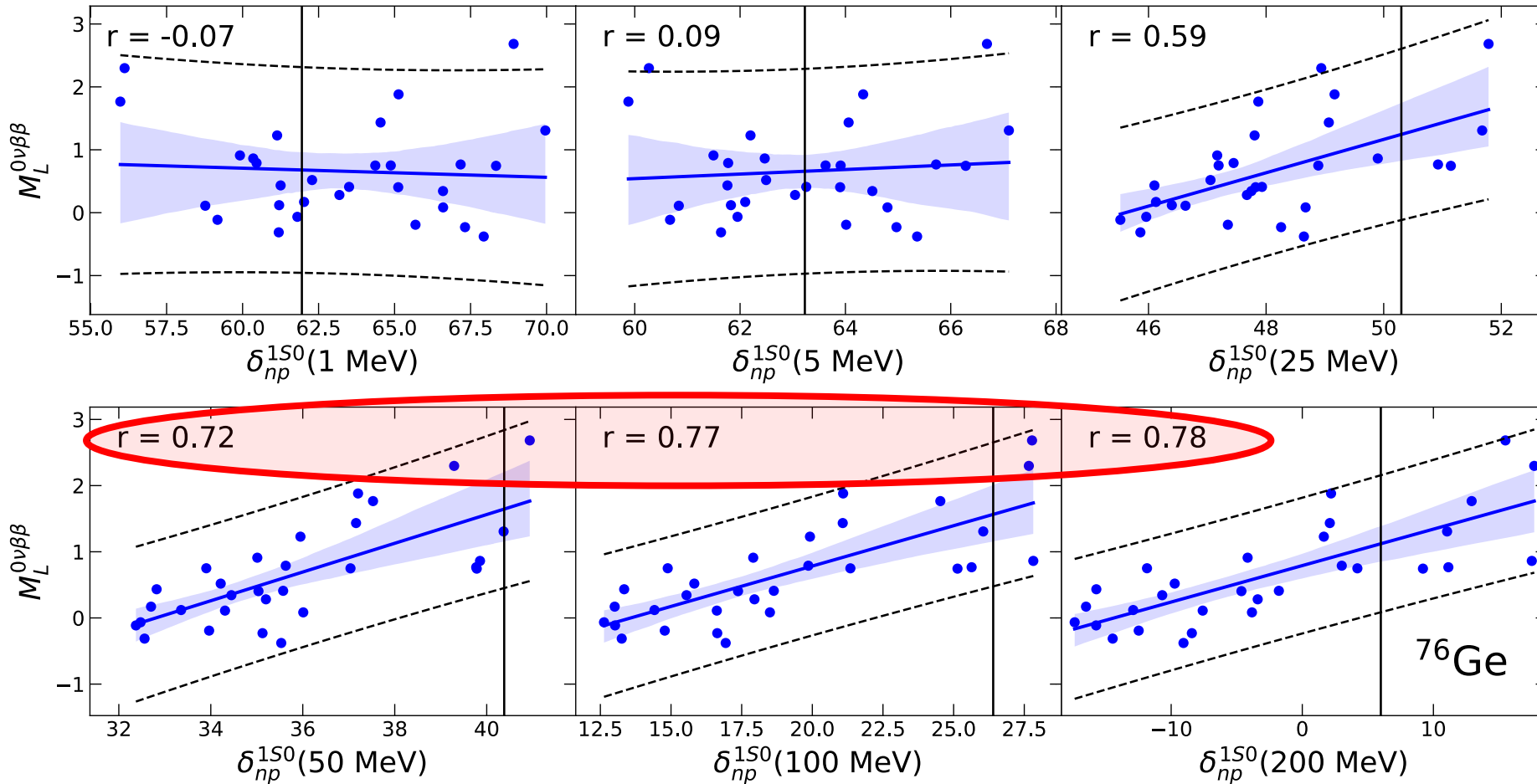
Long-range component in ^{48}Ca



Clear correlation with (measured!) 1S_0 phase shift at high scattering energies

Explore correlations with 1S_0 phase shift from 34 non-implausible interactions

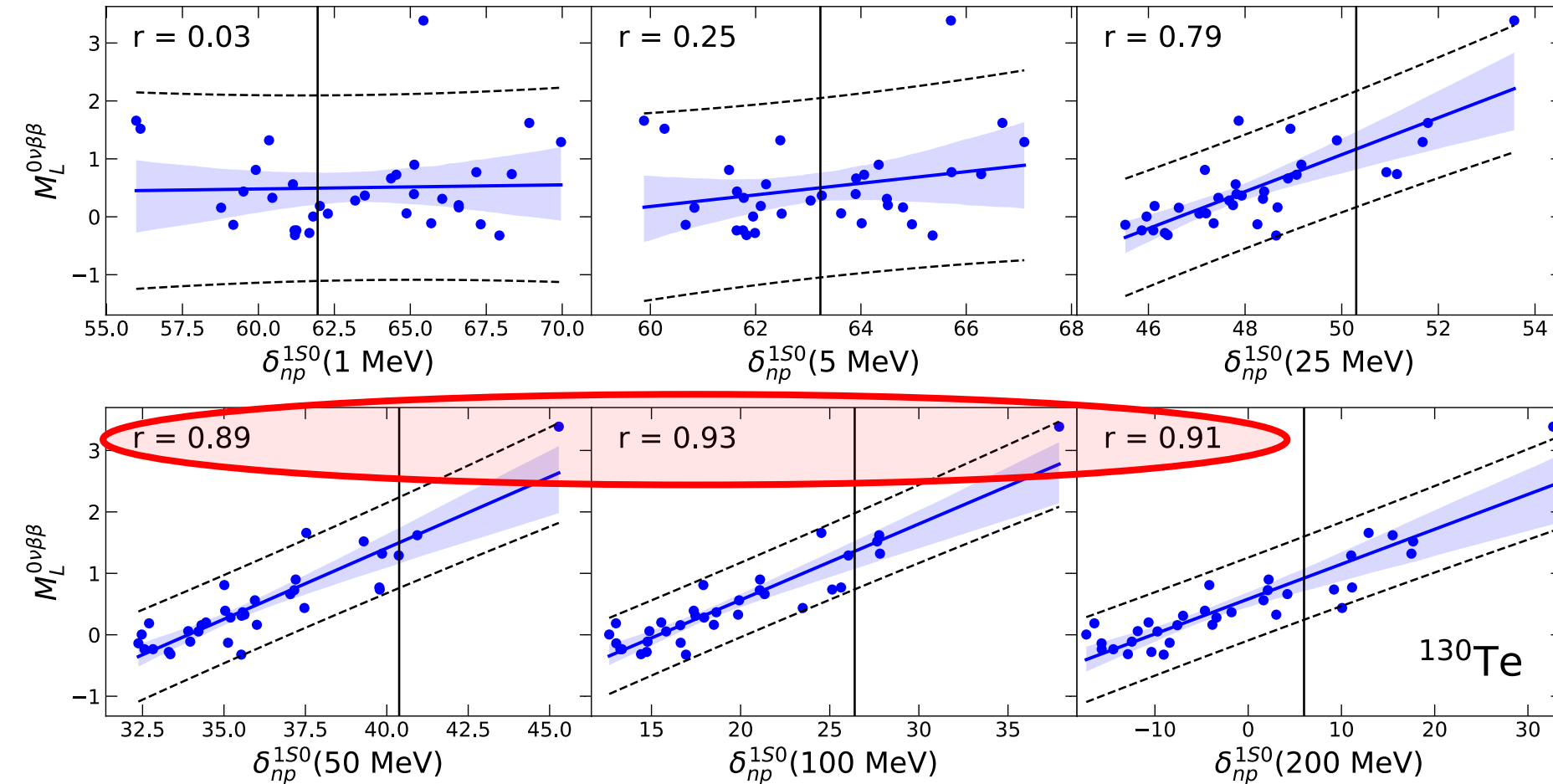
Long-range component in ^{48}Ca , ^{76}Ge



Clear correlation with (measured!) 1S_0 phase shift at high scattering energies

Explore correlations with 1S_0 phase shift from 34 non-implausible interactions

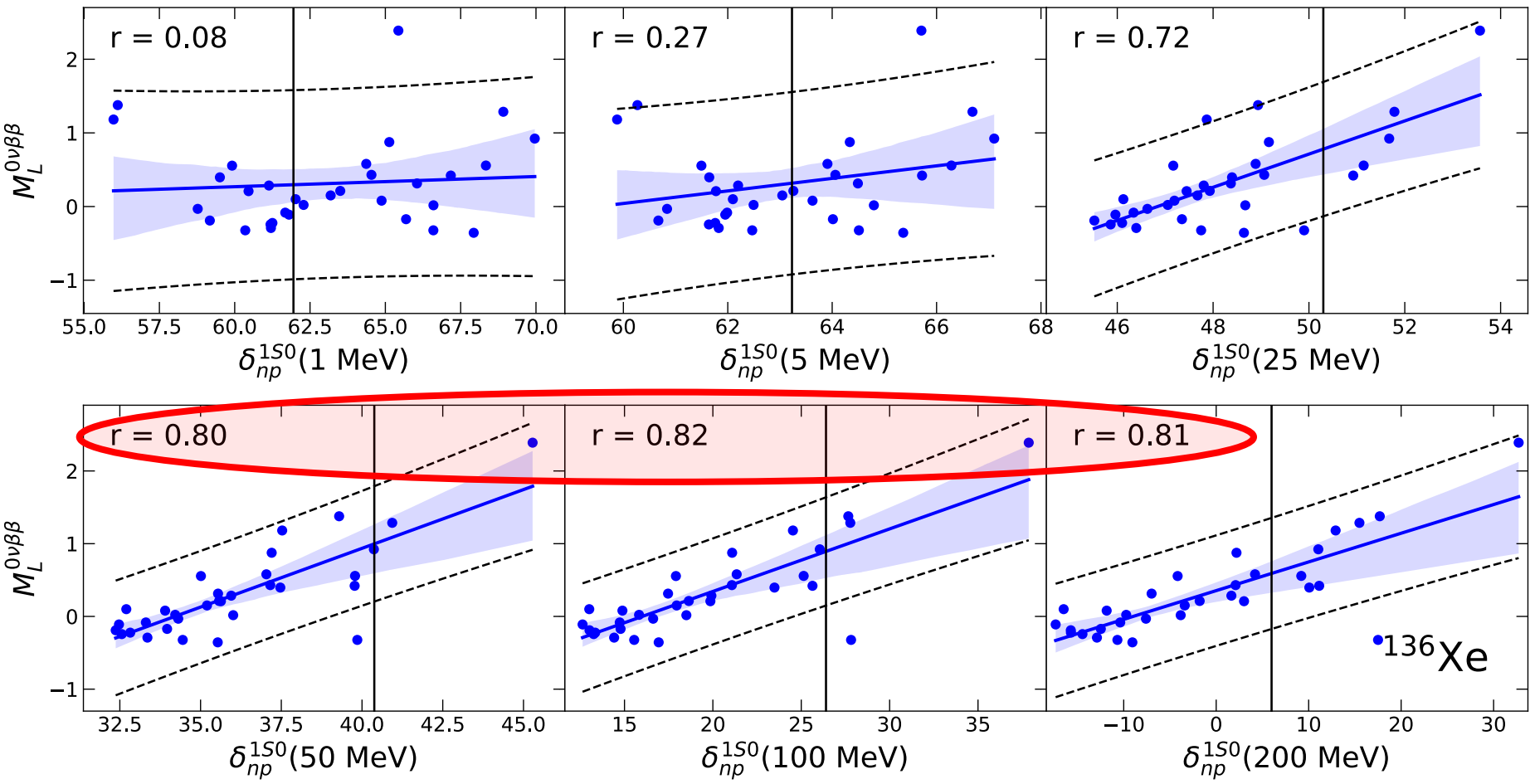
Long-range component in ^{48}Ca , ^{76}Ge , ^{130}Te



Clear correlation with (measured!) 1S_0 phase shift at high scattering energies

Explore correlations with 1S_0 phase shift from 34 non-implausible interactions

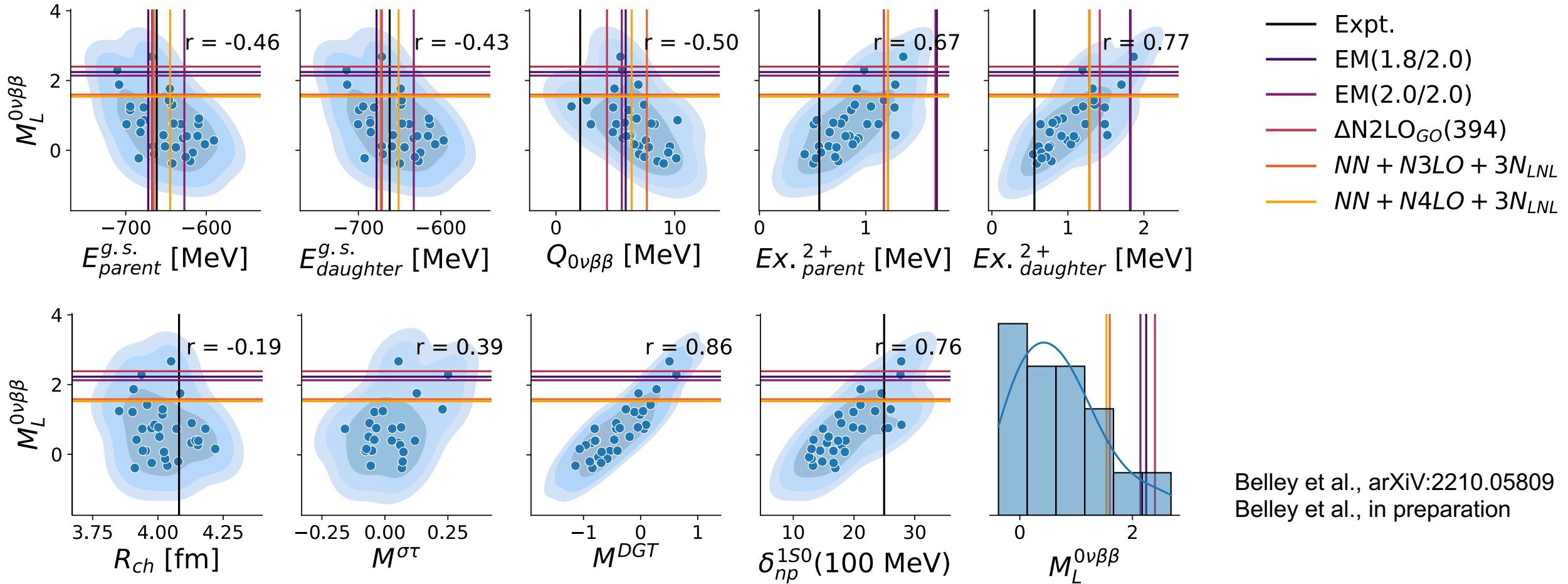
Long-range component in ^{48}Ca , ^{76}Ge , ^{130}Te , ^{136}Xe



Clear correlation with (measured!) 1S_0 phase shift at high scattering energies

Explore correlations with other observables from systematic analysis (34 interactions)

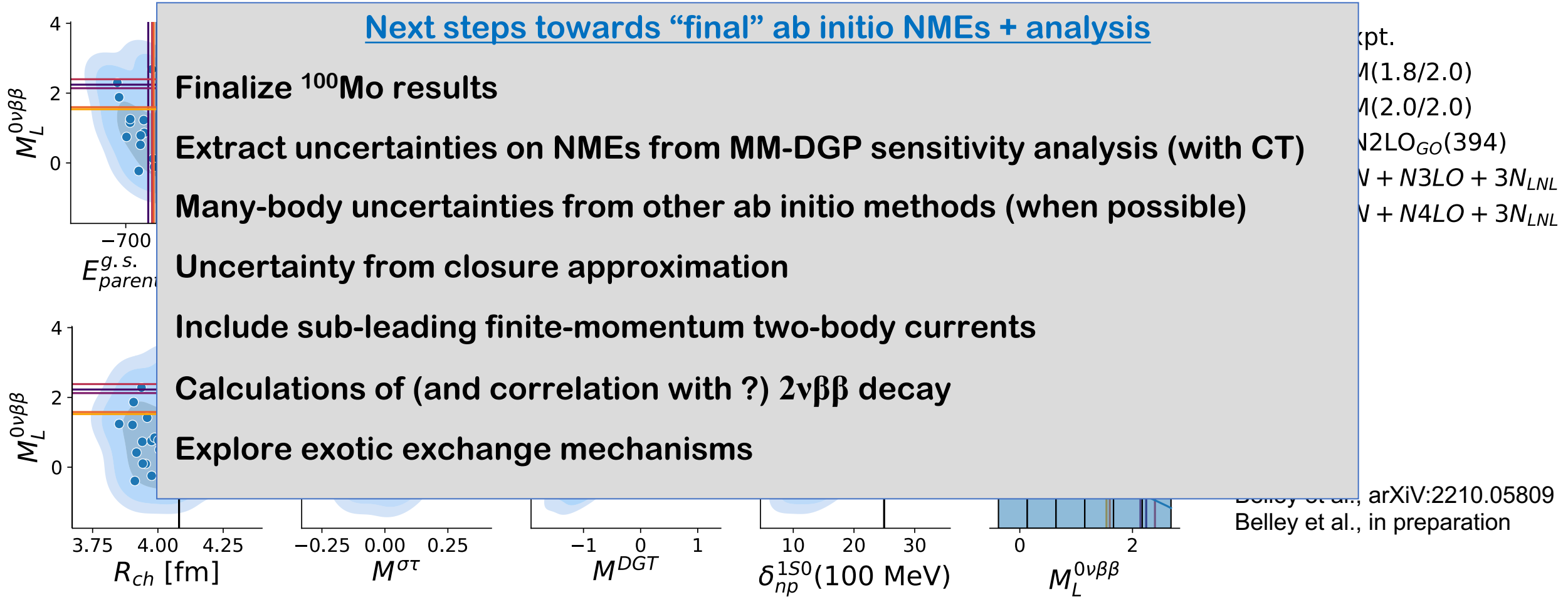
Few clear correlations, except DGT in ^{76}Ge



Now clear correlation with **measured** $^1\text{S}_0$ phase shift!

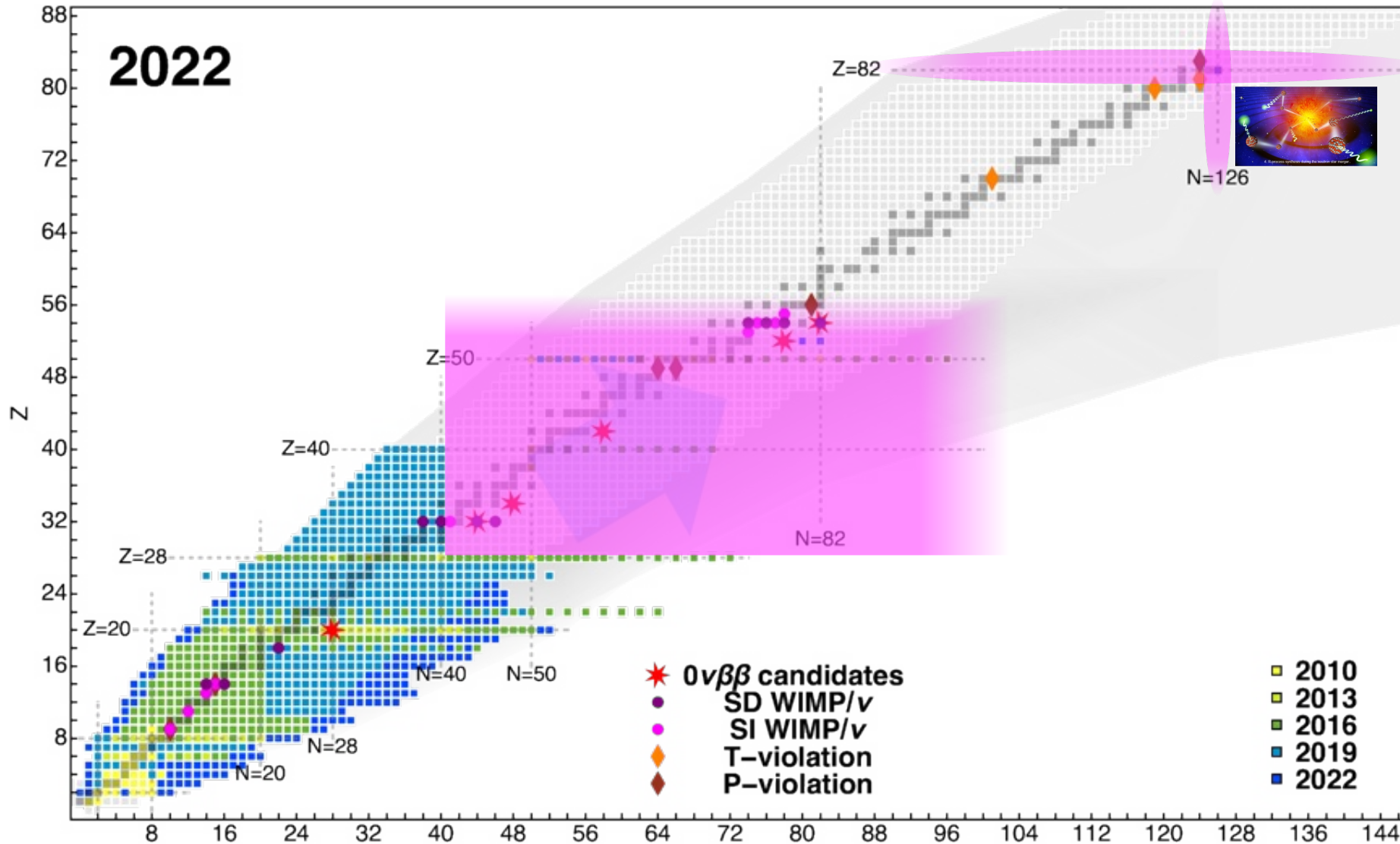
Explore correlations with other observables from systematic analysis (34 interactions)

Few clear correlations, except DGT in ^{76}Ge



Now clear correlation with **measured** 1S_0 phase shift!

Possible to access most nuclei relevant for BSM searches!



Nuclear Structure/Astrophysics

Development of forces and currents

Ab initio to ^{208}Pb : neutron skin, r-process

Dripline predictions to medium-masses

Evolution of magic numbers:

masses, radii, spectra, EM transitions

Multi-shell theory:

Islands of inversion, forbidden decays

Nuclear EOS/Neutron star properties

Atomic systems

T. Miyagi, B. S. Hu, L. Jokiniemi

A. Belley, I. Ginnett, C. G. Payne

M. Bruneault, J. Padua

S. Leutheusser

E. Love

K. Evidence, D. Kush

G. Tenkila, H. Patel, V. Chand

B. Wong, X. Cao

S. R. Stroberg N. Vassh



THE UNIVERSITY OF
BRITISH
COLUMBIA



McGill
UNIVERSITY

Present and Future for Ab Initio Theory

Fundamental Symmetries/BSM Physics

EW operators: GT quenching, muon capture

$0\nu\beta\beta$ decay matrix elements + DGT/ECEC/Dg

WIMP-Nucleus scattering for dark matter detection

Coherent elastic neutrino-nucleus scattering

Superallowed Fermi transitions

Symmetry-violating moments: EDM, anapole...

Work in progress

Higher-order many-body physics: IMSRG(3)

Monte Carlo shell model diagonalization

Extension to superheavy nuclei



A. Schwenk



G. Hagen

T. Papenbrock



J.M. Yao

H. Hergert



M. Martin

K. G. Leach



Massachusetts
Institute of
Technology

R. F. Garcia-Ruiz



UNIVERSITAT DE
BARCELONA

J. Menéndez



THE UNIVERSITY
of NORTH CAROLINA
at CHAPEL HILL

J. Engel



J. W. Holt

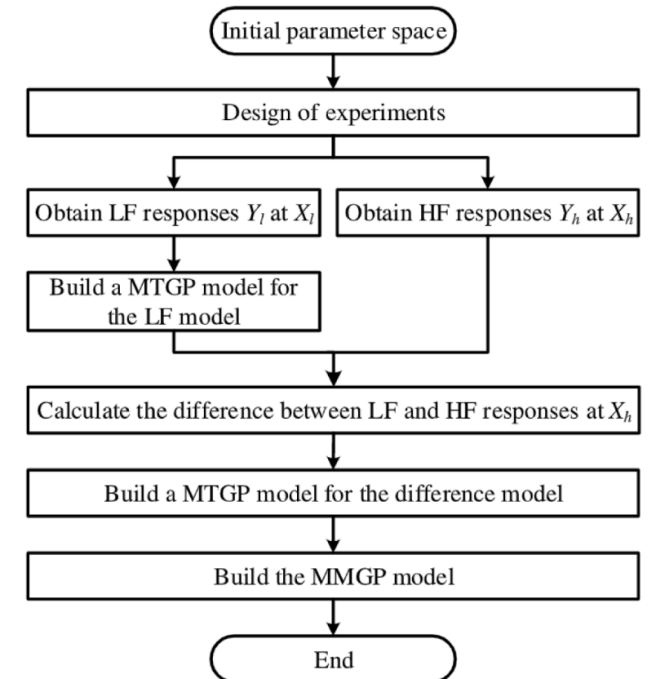
Explore dependence on chiral EFT LECs: requires many samples (as in ^{208}Pb)

Use gaussian processes as an emulator

Multi-Fidelity Gaussian Process: connects few (complicated) high-fidelity data points (eg, full IMSRG) w/ many low-fidelity data points (HF, low e_{max} , etc)

Difference function fit with Gaussian process: predict HF from LF

When relation between LF and HF is complicated, MFGP fails



Explore dependence on chiral EFT LECs: requires many samples (as in ^{208}Pb)

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Multi-Fidelity Gaussian Process: connects few (complicated) high-fidelity data points (eg, full IMSRG) w/ many low-fidelity data points (HF, low e_{max} , etc)

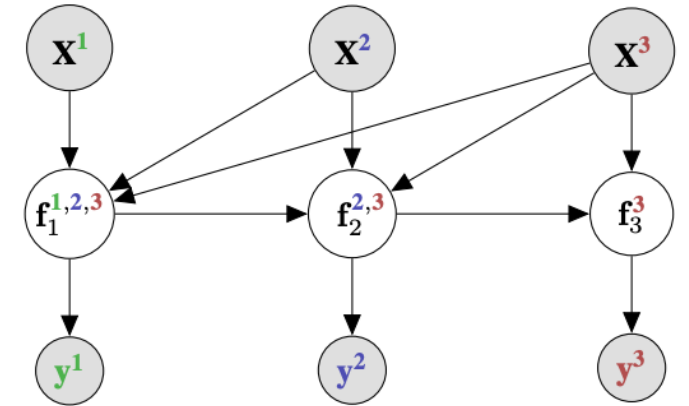
Difference function fit with Gaussian process: predict HF from LF

Deep Gaussian Process: Neural network links multiple GP

Include outputs of previous fidelity as new HF point:
Improves modeling of difference between LF and HF

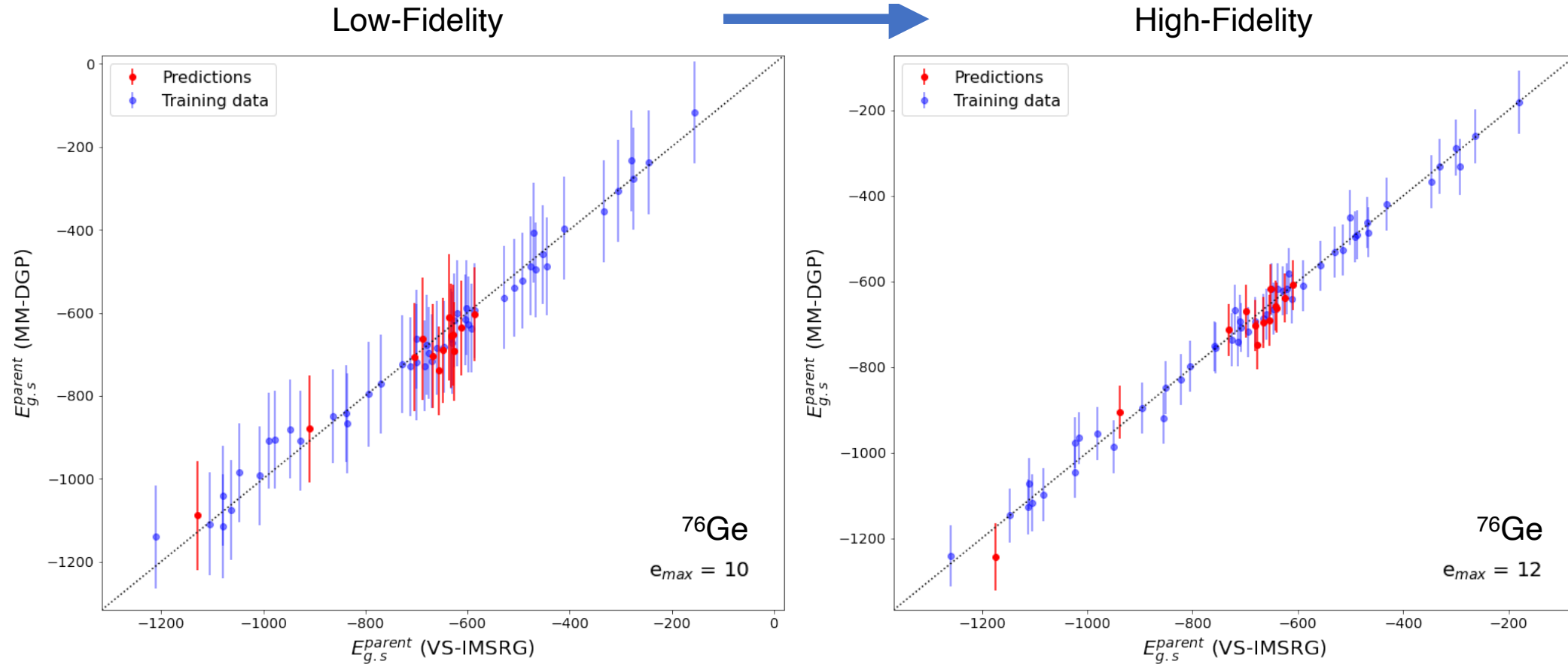
Adapted for multi output:

Multi-Output Multi-Fidelity Deep Gaussian Process (MM-DGP)



Testing MM-DGP: use delta-full chiral EFT at N2LO

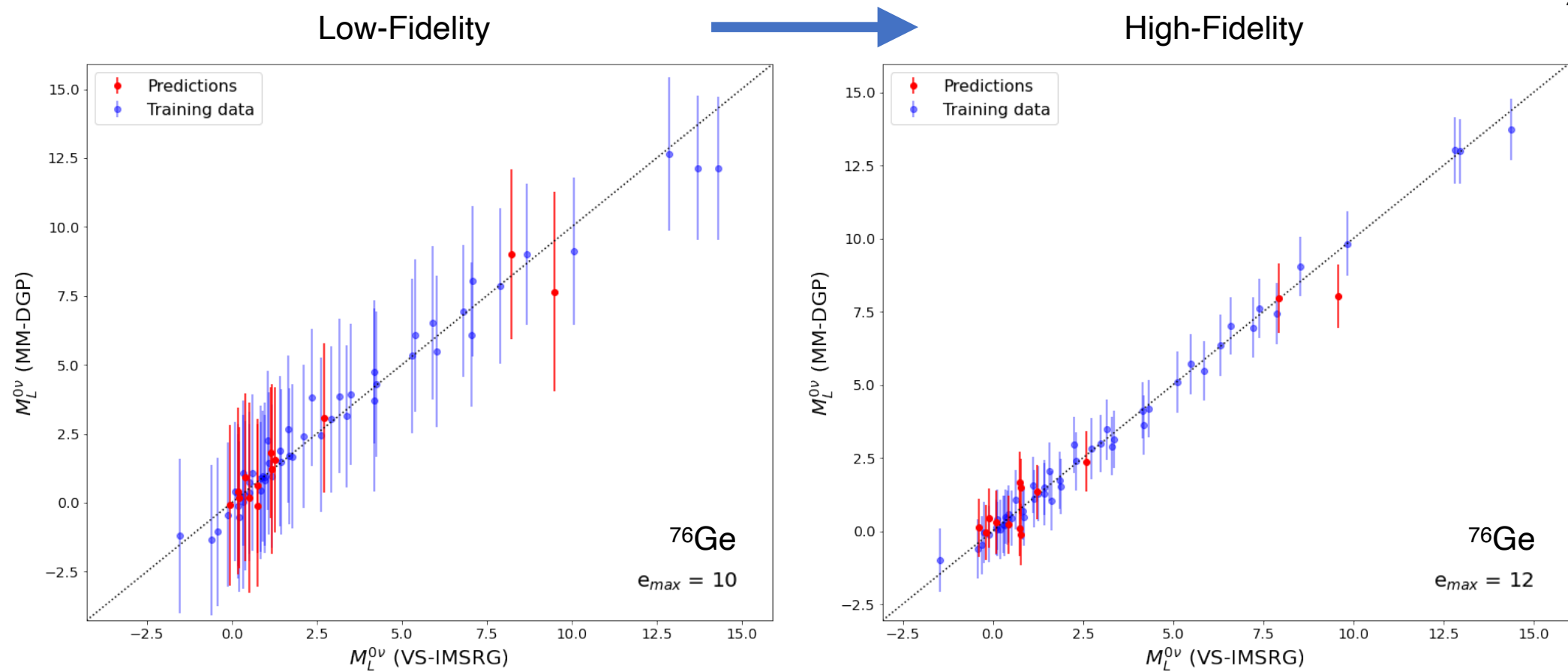
Improved energy predictions with high-fidelity training points



Belley, Pitcher et al. in prep.

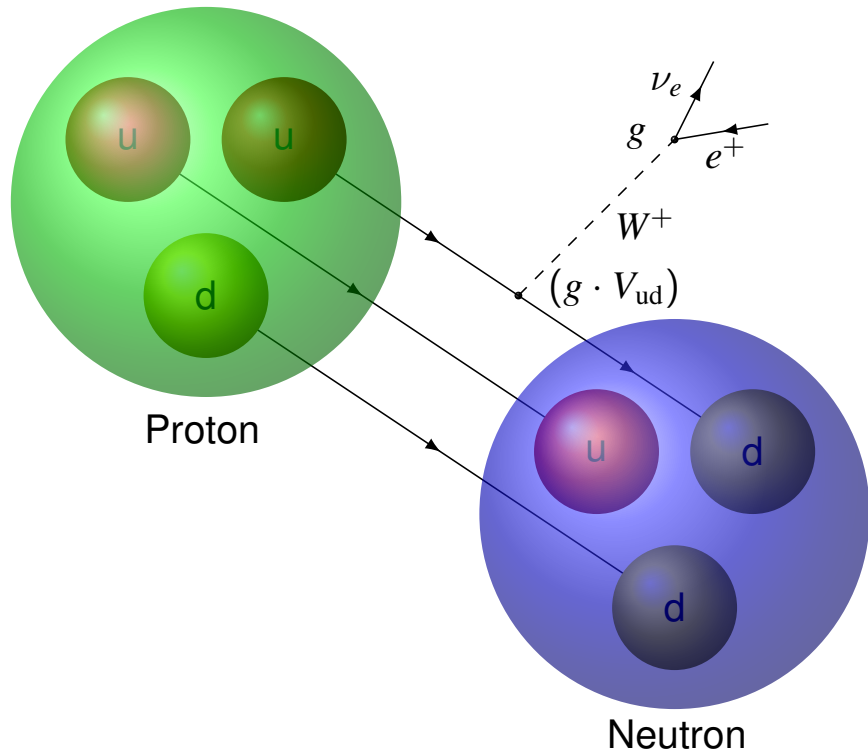
Testing MM-DGP: use delta-full chiral EFT at N2LO

Improved energy predictions with high-fidelity training points



Belley, Pitcher et al. in prep.

Ab Initio Approach to ISB and Superallowed $0^+ \rightarrow 0^+$



Editors' Suggestion

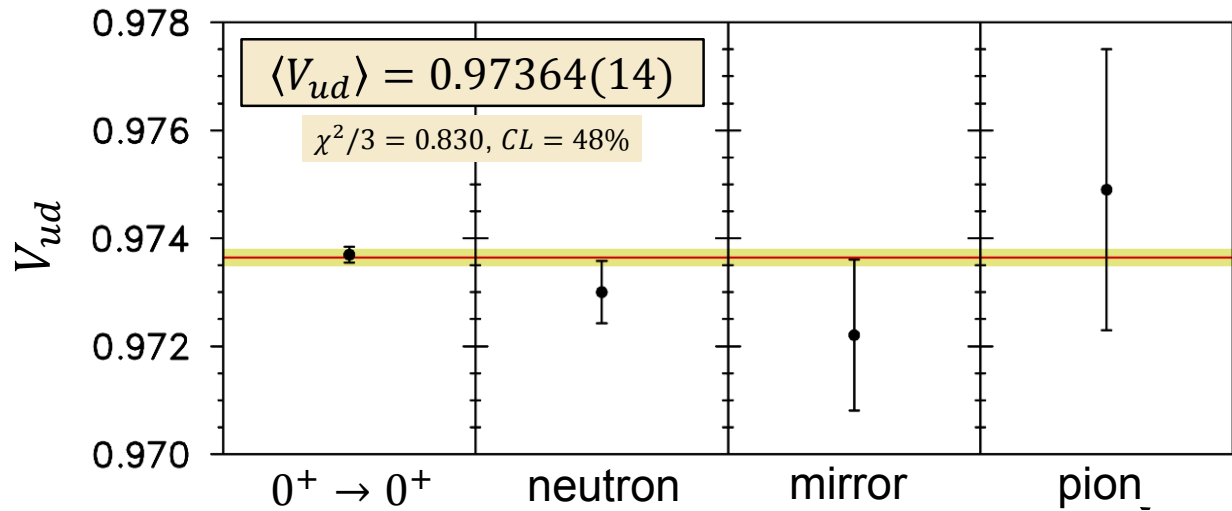
Testing isospin symmetry breaking in *ab initio* nuclear theory

M. S. Martin, S. R. Stroberg, J. D. Holt, and K. G. Leach
Phys. Rev. C **104**, 014324 – Published 30 July 2021

$0^+ \rightarrow 0^+$ transitions: most stringent constraint on V_{ud} from corrected (parameterized) lifetime

$$G_V = G_F V_{ud}, \text{ where } ft = \frac{K}{2G_V^2} \text{ (isospin limit)}$$

$$\mathcal{F}t = ft(1 + \delta'_R[1 - (\delta_C - \delta_{NS})]) = \frac{K/G_F^2}{2V_{ud}^2(1 + \Delta_R^V)}$$

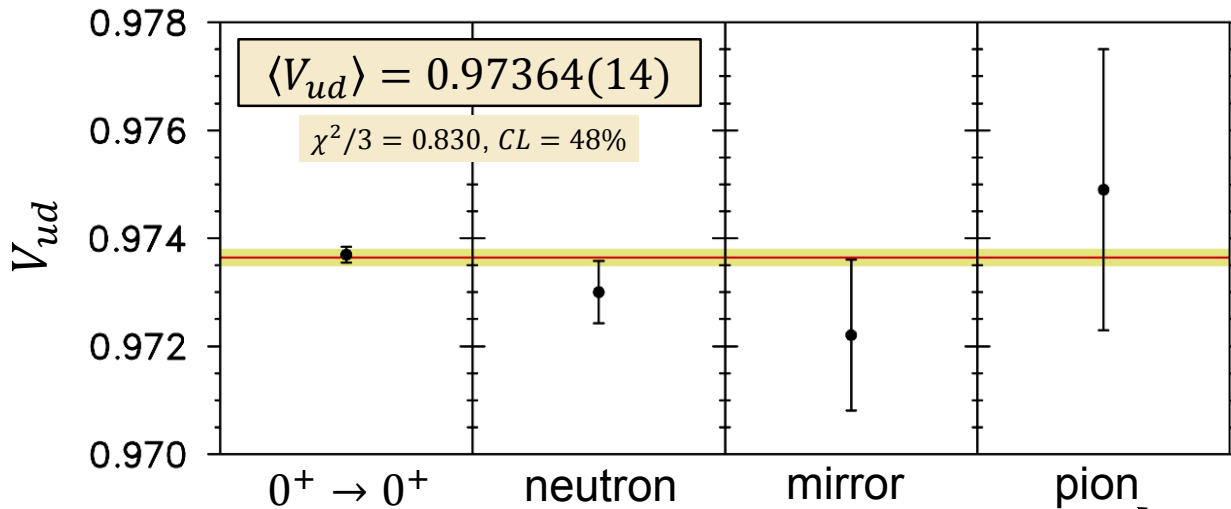


$0^+ \rightarrow 0^+$ transitions: most stringent constraint on V_{ud} from corrected (parameterized) lifetime

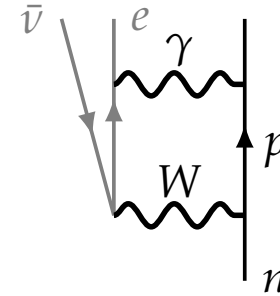
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$$|M_F|^2 = |M_F^0|^2 (1 + \delta_C) \quad \text{Isospin-symmetry breaking}$$

$$\mathcal{F}t = ft(1 + \delta'_R [1 - (\delta_C - \delta_{NS})]) = \frac{K/G_F^2}{2V_{ud}^2 (1 + \Delta_R^V)}$$

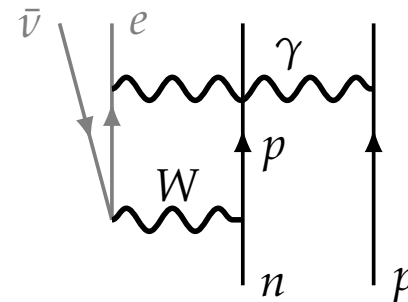


$$\delta'_R \sim$$



Structure-independent radiative correction

$$\delta_{NS} \sim$$

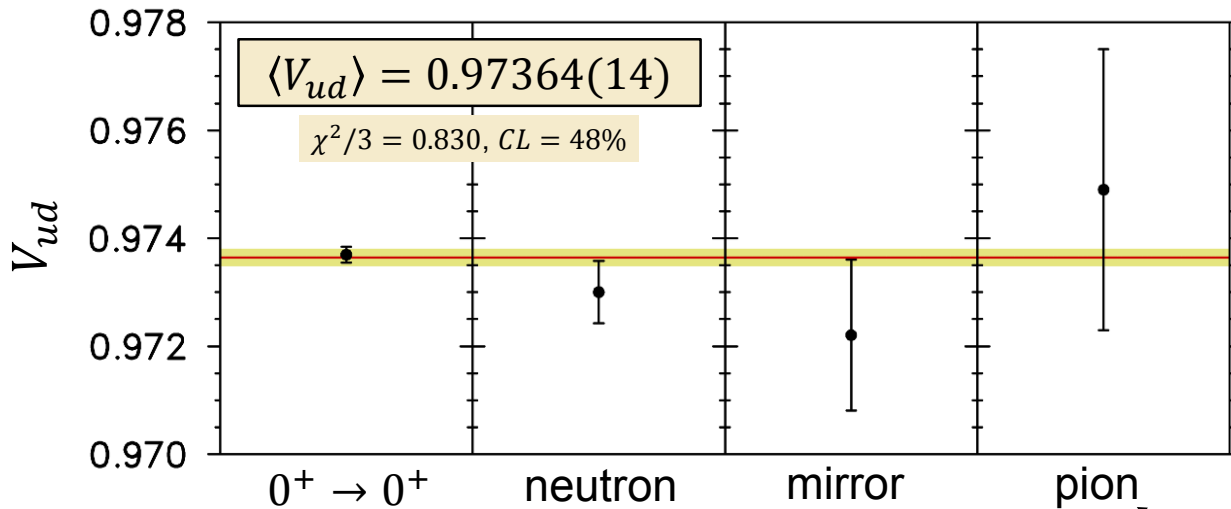


Structure-dependent radiative correction

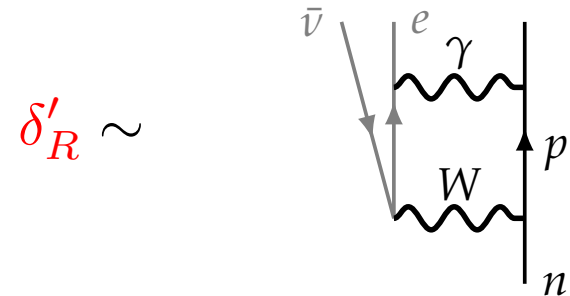
$0^+ \rightarrow 0^+$ transitions: most stringent constraint on V_{ud} from corrected (parameterized) lifetime

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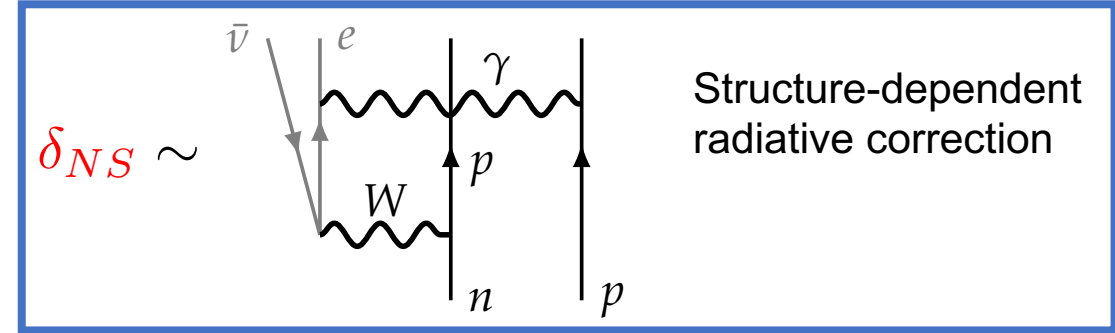
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Structure-independent radiative correction



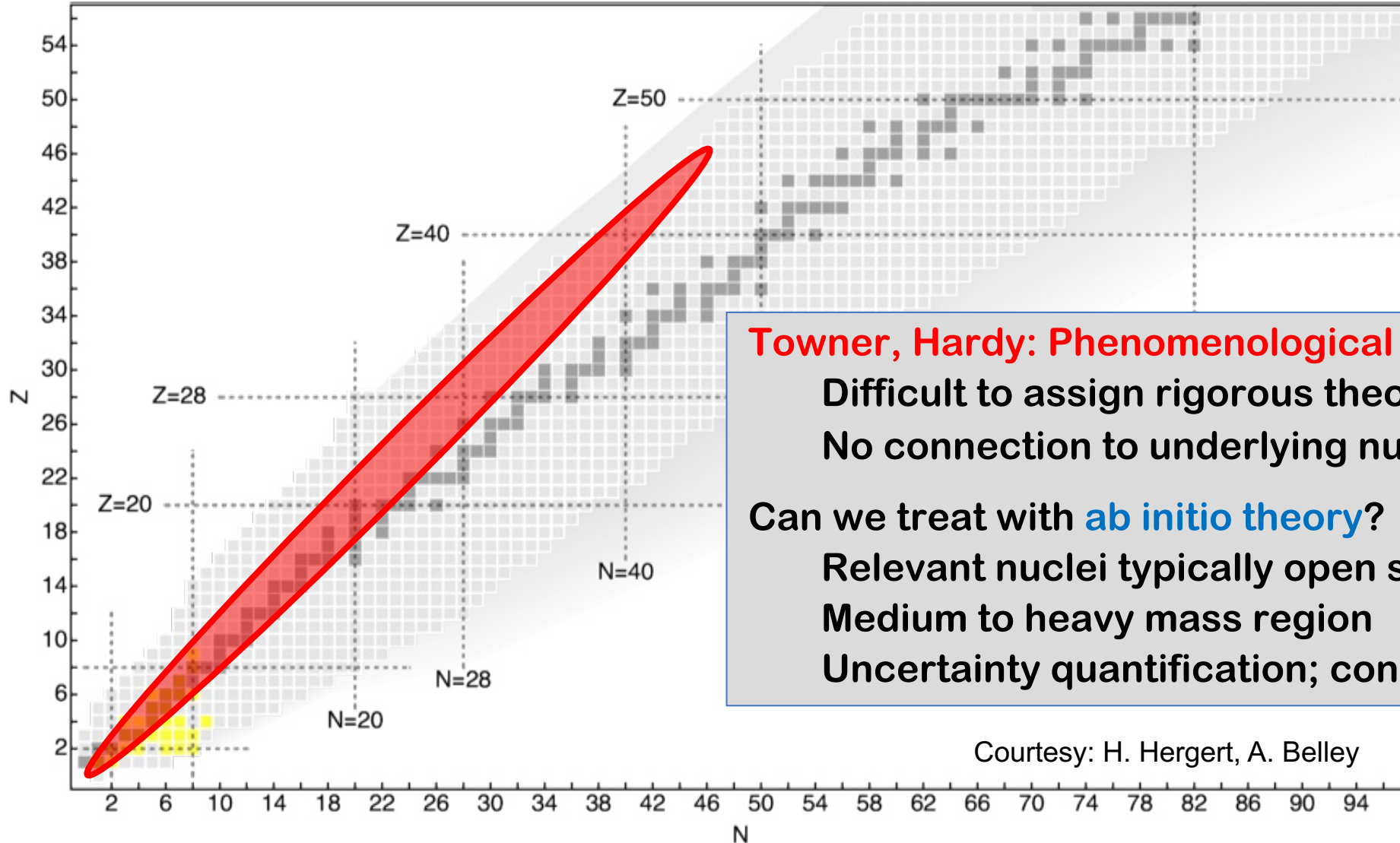
Structure-dependent radiative correction

Nuclear structure theory

Isospin symmetry correction

dominates uncertainty in medium/heavy nuclei (and simple operator to calculate)

2010: Limited capabilities for 3N forces; ^{16}O heaviest



Towner, Hardy: Phenomenological shell model

Difficult to assign rigorous theoretical uncertainties
No connection to underlying nuclear/weak forces

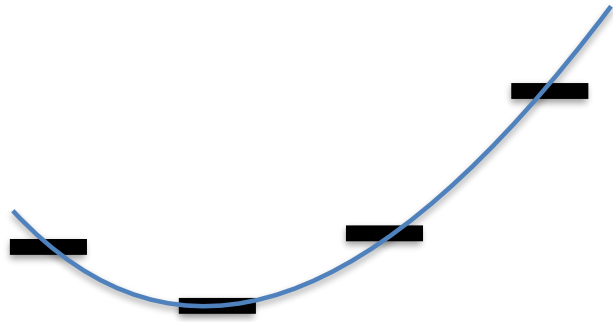
Can we treat with **ab initio theory**?

Relevant nuclei typically open shell
Medium to heavy mass region
Uncertainty quantification; connection to QCD

Courtesy: H. Hergert, A. Belley

Isobaric mass multiplet equation (IMME) relates energies between members of multiplets

$$E(T_z) = a + bT_z + cT_z^2$$

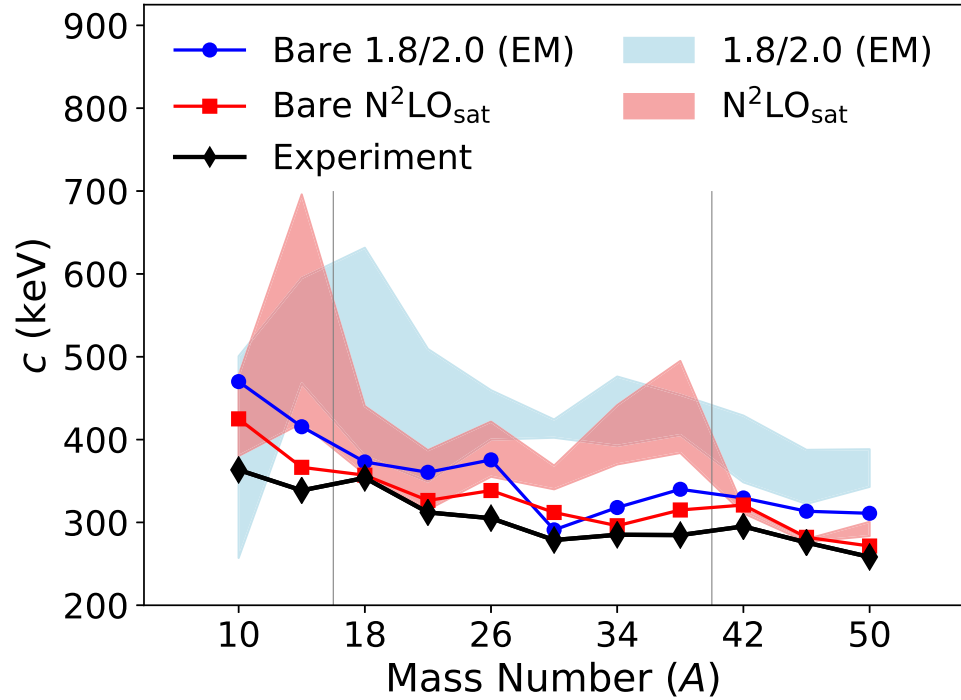
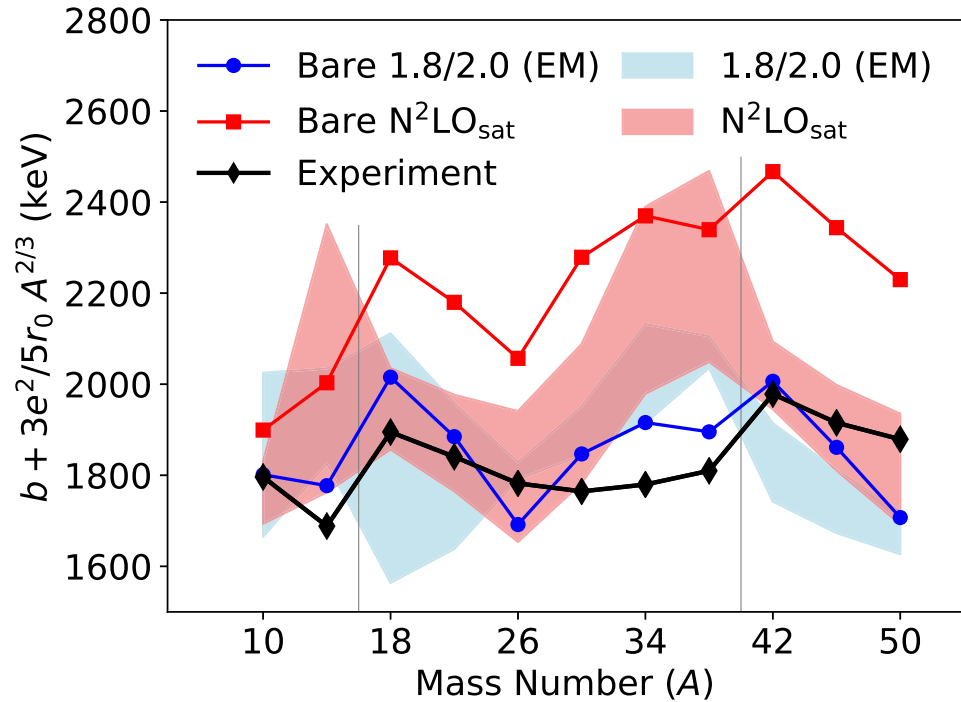


Compare ab initio with experimental determination of IMME coefficients to gauge success

Calculate all nuclei relevant for superallowed transitions; 2 NN+3N forces

Isobaric mass multiplet equation (IMME) relates energies between members of multiplets

$$E(T_z) = a + bT_z + cT_z^2$$



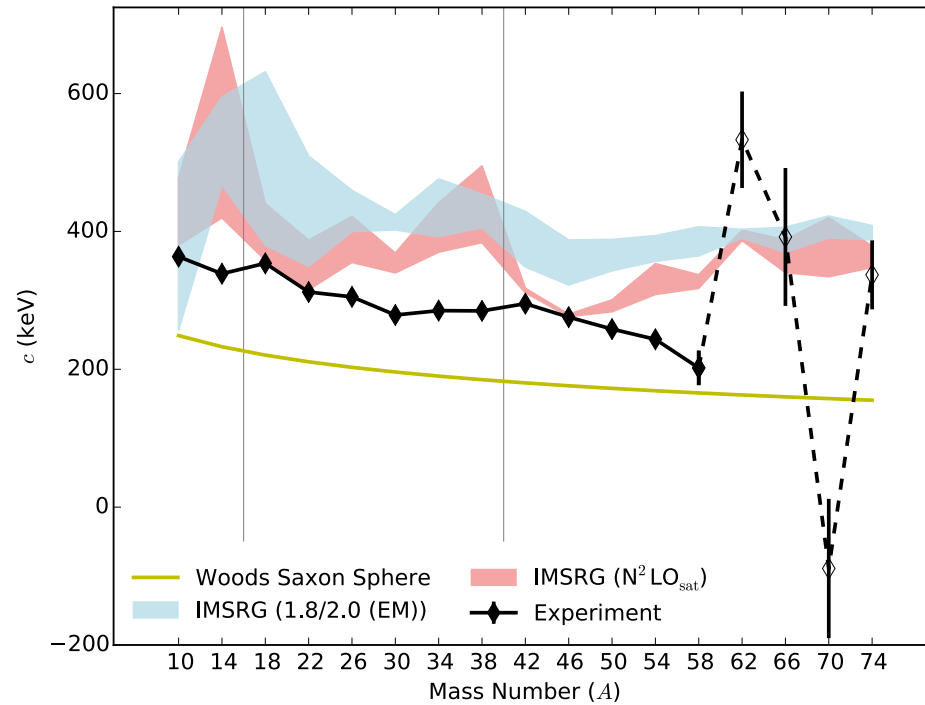
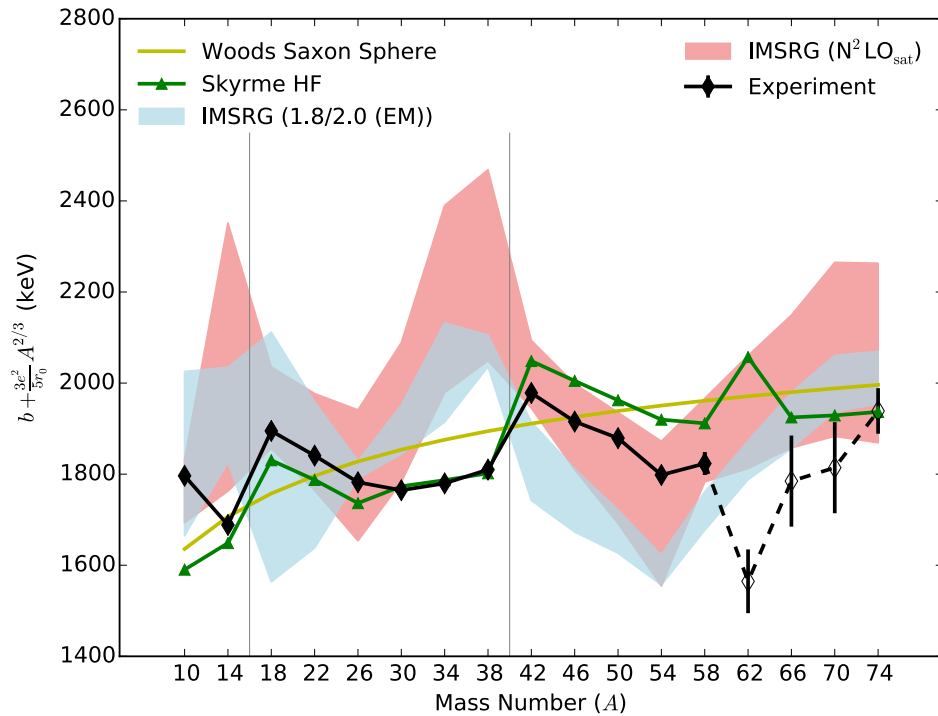
Bands: normal ordering reference dependence

Overall little effect/improvement when applying IMSRG transformation for both b, c

Isobaric mass multiplet equation (IMME) relates energies between members of multiplets

$$E(T_z) = a + bT_z + cT_z^2$$

Compare VS-IMSRG b, c coefficients to HF and results from a uniform charged sphere



Systematics already largely captured (better) by mean field or charged sphere

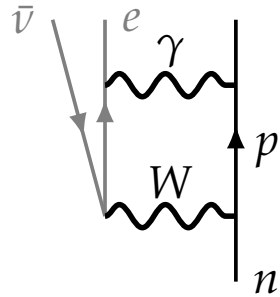
Ambiguous results... turn to superallowed Fermi transitions

$0^+ \rightarrow 0^+$ transitions: most stringent constraint on V_{ud} from corrected (parameterized) lifetime

$$|M_F|^2 = |M_F^0|^2 (1 + \delta_C) \quad \text{Isospin-symmetry breaking}$$

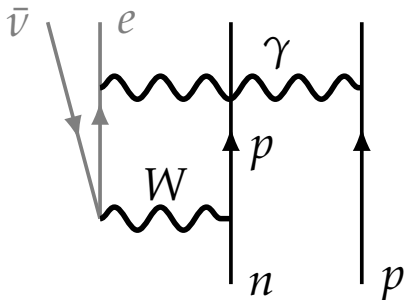
~ Effect of **correlations outside valence space**

$\delta'_R \sim$



Structure-independent radiative correction

$\delta_{NS} \sim$



Structure-dependent radiative correction

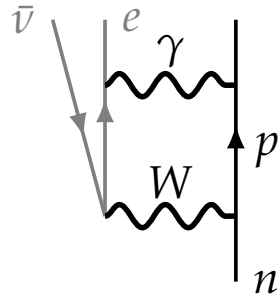
~ Effect of **two-body currents**

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$$|M_F|^2 = |M_F^0|^2 (1 + \delta_C) \quad \text{Isospin-symmetry breaking}$$

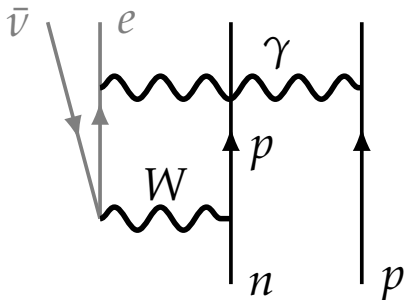
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$\delta'_R \sim$



Structure-independent radiative correction

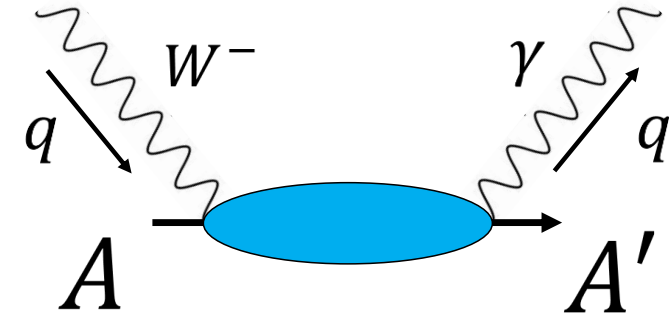
$\delta_{NS} \sim$



Structure-dependent radiative correction

~ Effect of **two-body currents**

Compton amplitude in the NCSM



24

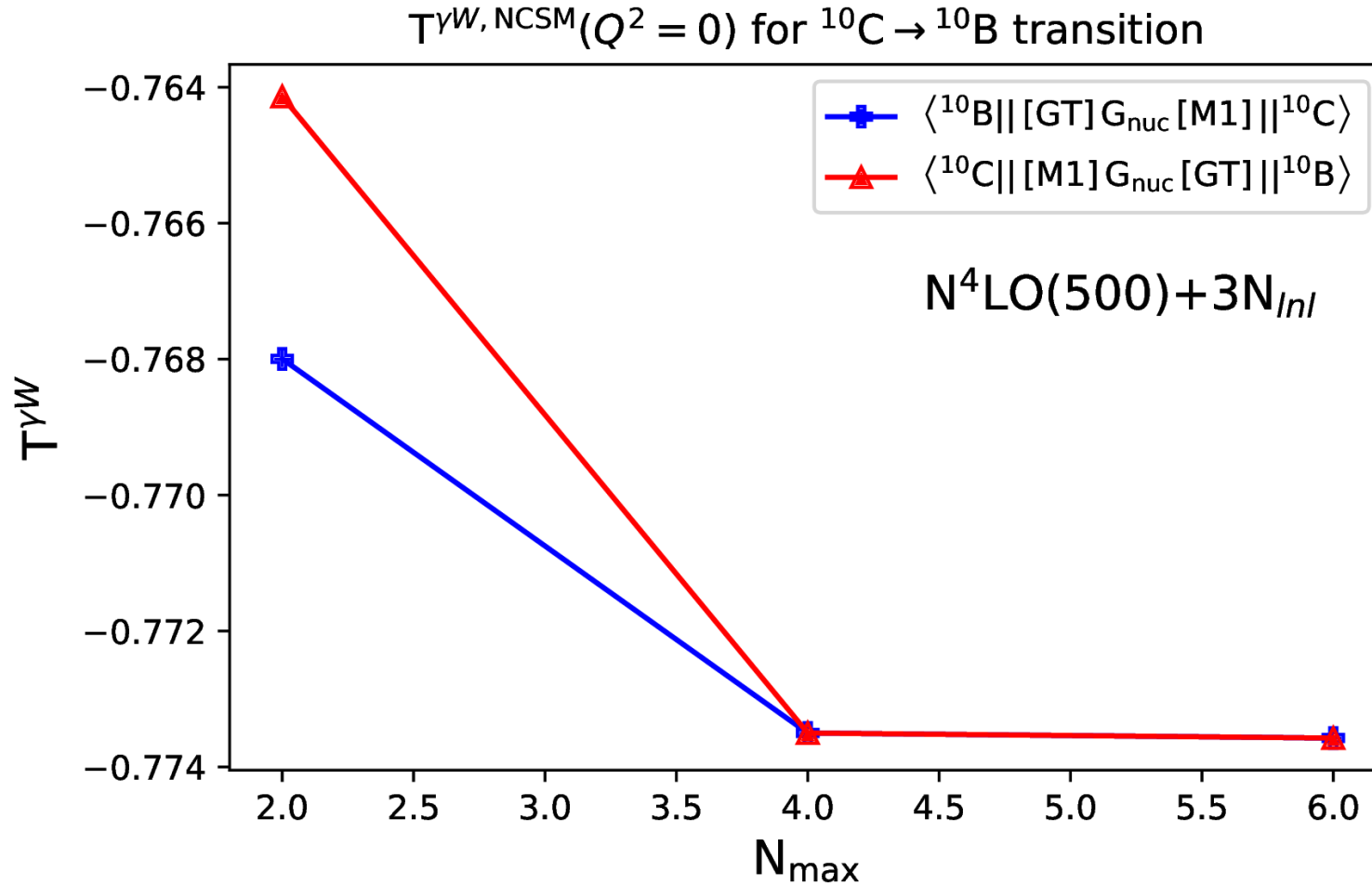
- Nuclear matrix elements for γW -box
 - 1) Express currents in momentum space
 - 2) Multipole expansion of current operators
 - 3) Connect currents to effective one-body operators

$$\begin{aligned}
 T_3(q_0, Q^2) = & -4\pi i \frac{q_0}{q} \sqrt{M_i M_f} \sum_{J=1}^{\infty} (2J + 1) \\
 & \times \langle A\lambda_f J_f M_f | \left[T_{J0}^{mag}(q) \boxed{G(M_f + q_0 + i\epsilon)} T_{J0}^{5,el}(q) + T_{J0}^{el}(q) \boxed{G(M_f + q_0 + i\epsilon)} T_{J0}^{5,mag}(q) \right. \\
 & \left. + T_{J0}^{5,mag}(q) \boxed{G(M_i - q_0 + i\epsilon)} T_{J0}^{el}(q) + T_{J0}^{5,el}(q) \boxed{G(M_i - q_0 + i\epsilon)} T_{J0}^{mag}(q) \right] | A\lambda_i J_i M_i \rangle
 \end{aligned}$$

Lanczos continued fractions method to compute Green's functions!

Comment on many-body convergence

Preliminary



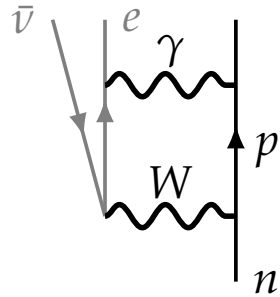
Next step: implement in VS-IMSRG for all superallowed nuclei

$0^+ \rightarrow 0^+$ transitions: most stringent constraint on V_{ud} from corrected (parameterized) lifetime

$$|M_F|^2 = |M_F^0|^2 (1 + \delta_C) \quad \text{Isospin-symmetry breaking}$$

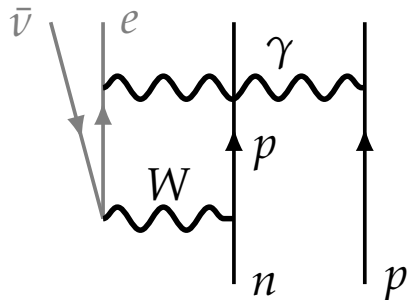
~ Effect of **correlations outside valence space**

$\delta'_R \sim$



Structure-independent radiative correction

$\delta_{NS} \sim$



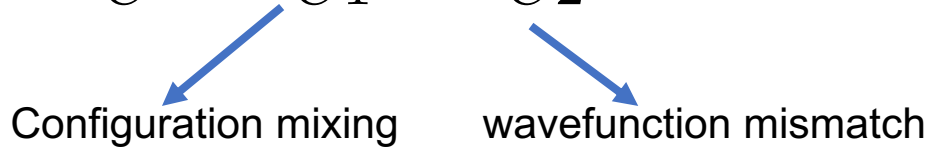
Structure-dependent radiative correction

~ Effect of **two-body currents**

Ab initio calculations of all cases with 1.8/2.0 (EM) interaction

Standard approach (T/H): Split contribution

$$\delta_C = \delta_{C1} + \delta_{C2}$$



 Configuration mixing wavefunction mismatch

Ab initio approach: calculate directly

$$|M_F|^2 = |M_F^0|^2(1 - \delta_C)$$

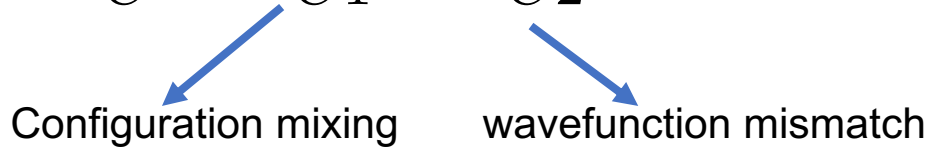
$$\delta_C = 1 - \frac{|M_F|^2}{|M_F^0|^2}$$

$$M_F = \langle \Psi_F || \tau || \Psi_i \rangle$$

Ab initio calculations of all cases with 1.8/2.0 (EM) interaction

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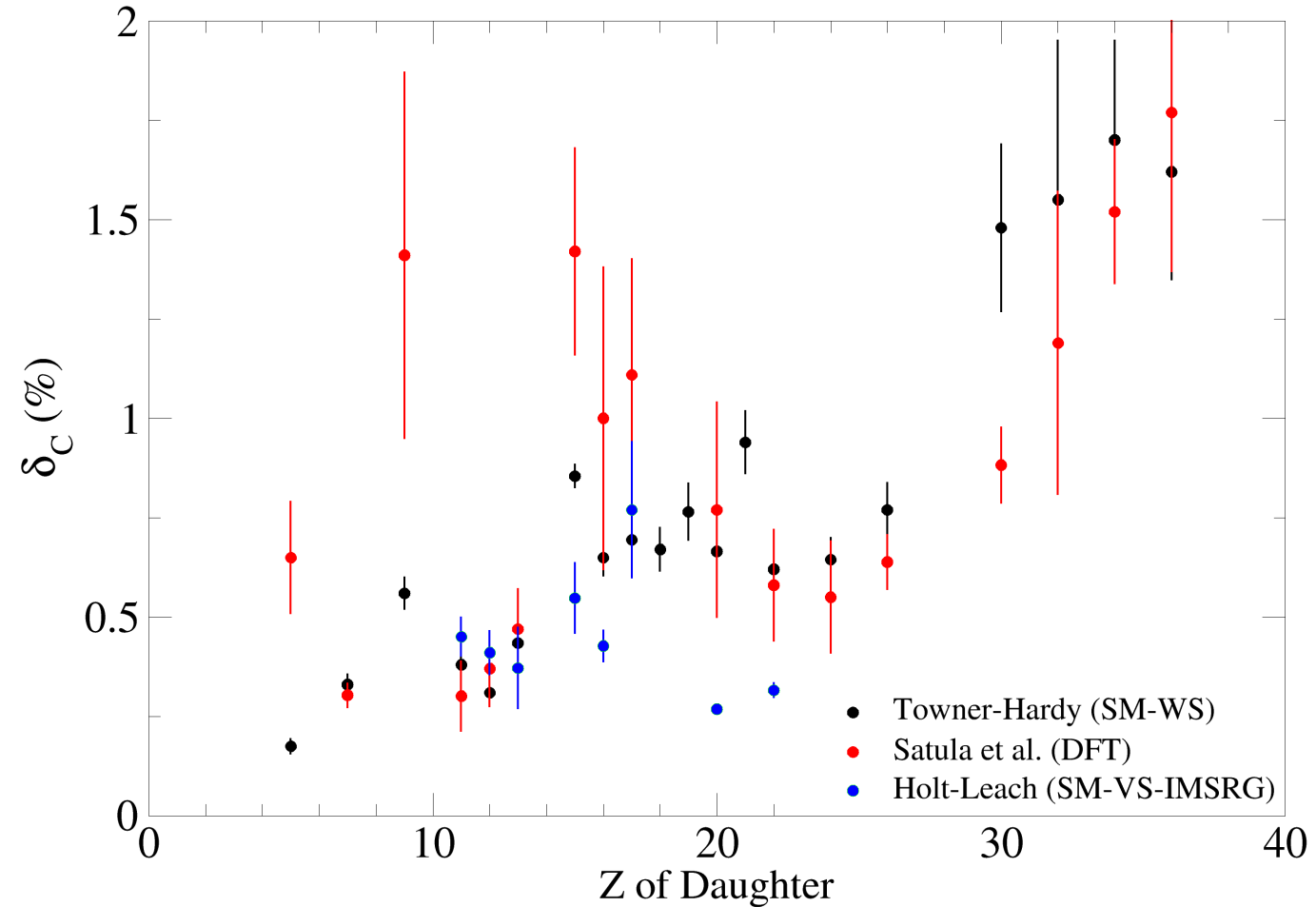


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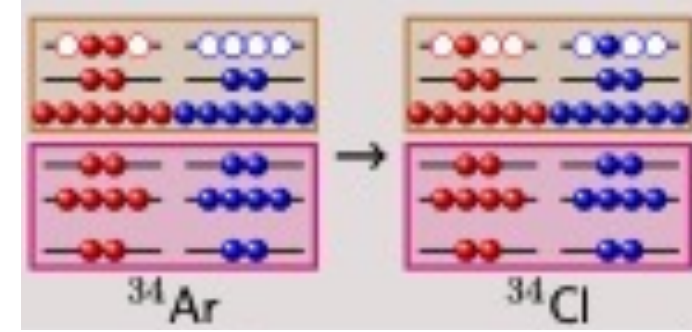
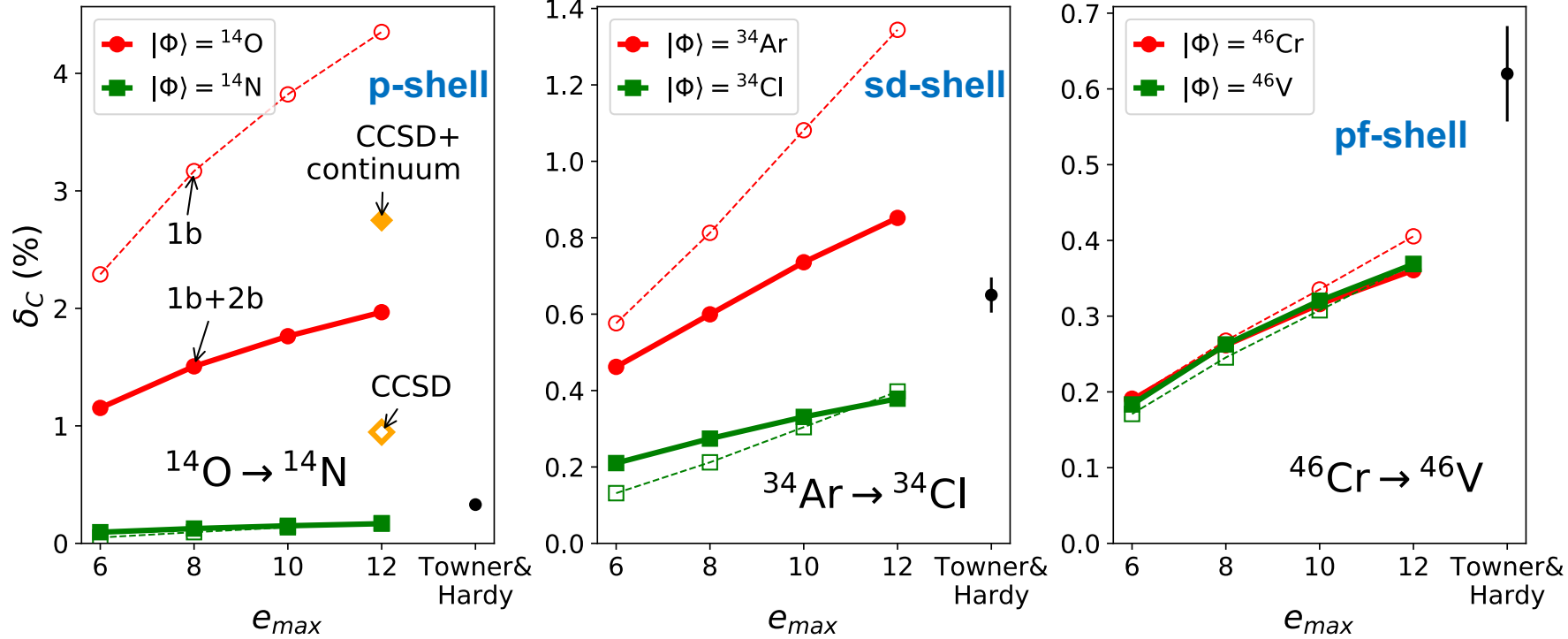
$$M_F = \langle \Psi_F || \tau || \Psi_i \rangle$$



Results comparable to T-H and DFT

Leach, Holt, arXiv:1809.10793

Can we provide rigorous uncertainty estimates?



Significant effect from 1b to 1b+2b

Significant reference-state dependence in some cases; δ_C does not converge with e_{max}

Large effect from CC with continuum indicates generally difficult for ab initio

Natural Orbitals (perturbatively improved) basis:

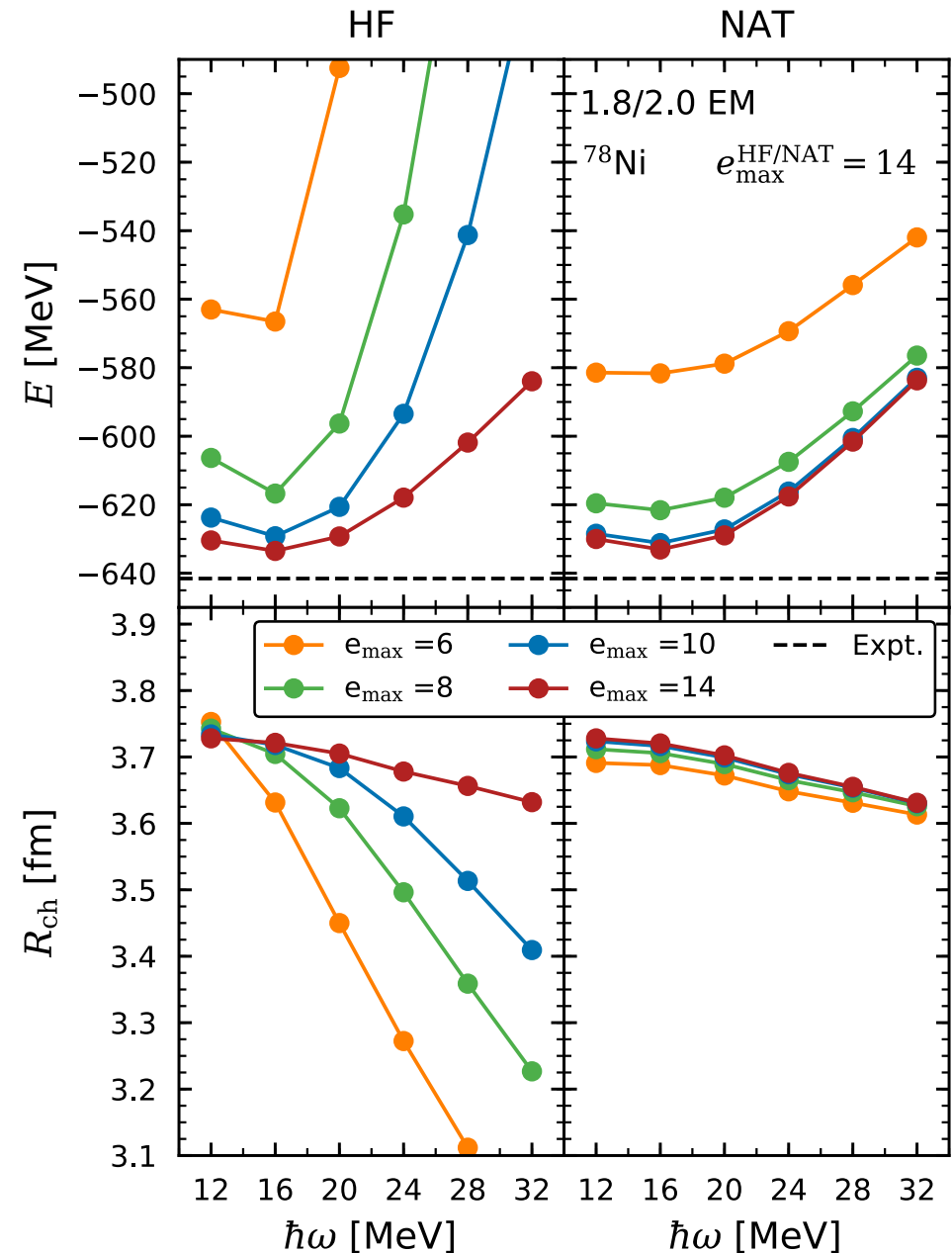
Add *perturbations* caused by interactions between particles to the HF-basis system

$$|\Psi\rangle = |\Phi\rangle + \sum_{n=1}^{\infty} \left(\frac{H_I}{H_0 - E^{(0)}} \right)^n |\Phi\rangle$$

$$E = E^{(0)} + \sum_{n=1}^{\infty} \left\langle \Phi \left| H_I \left(\frac{H_I}{H_0 - E^{(0)}} \right)^n \right| \Phi \right\rangle$$

Dramatic improvement in energies and radii

Can it help with superallowed convergence?

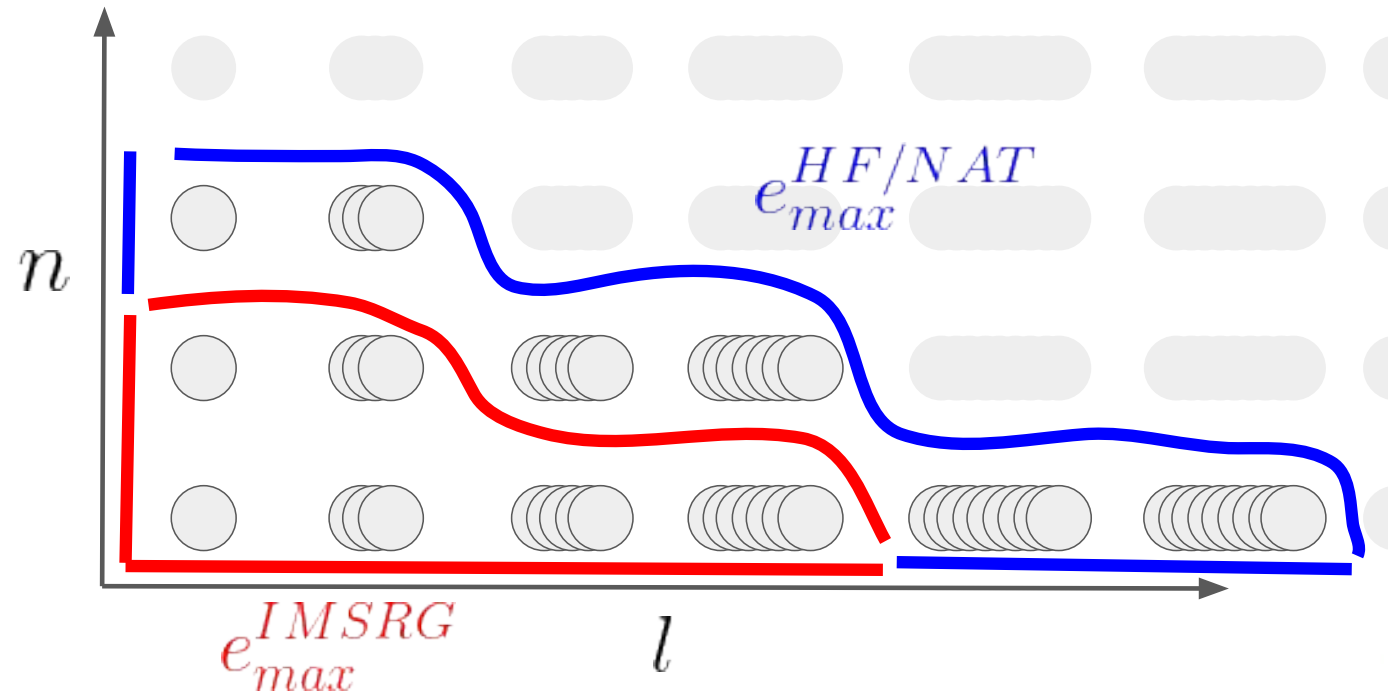


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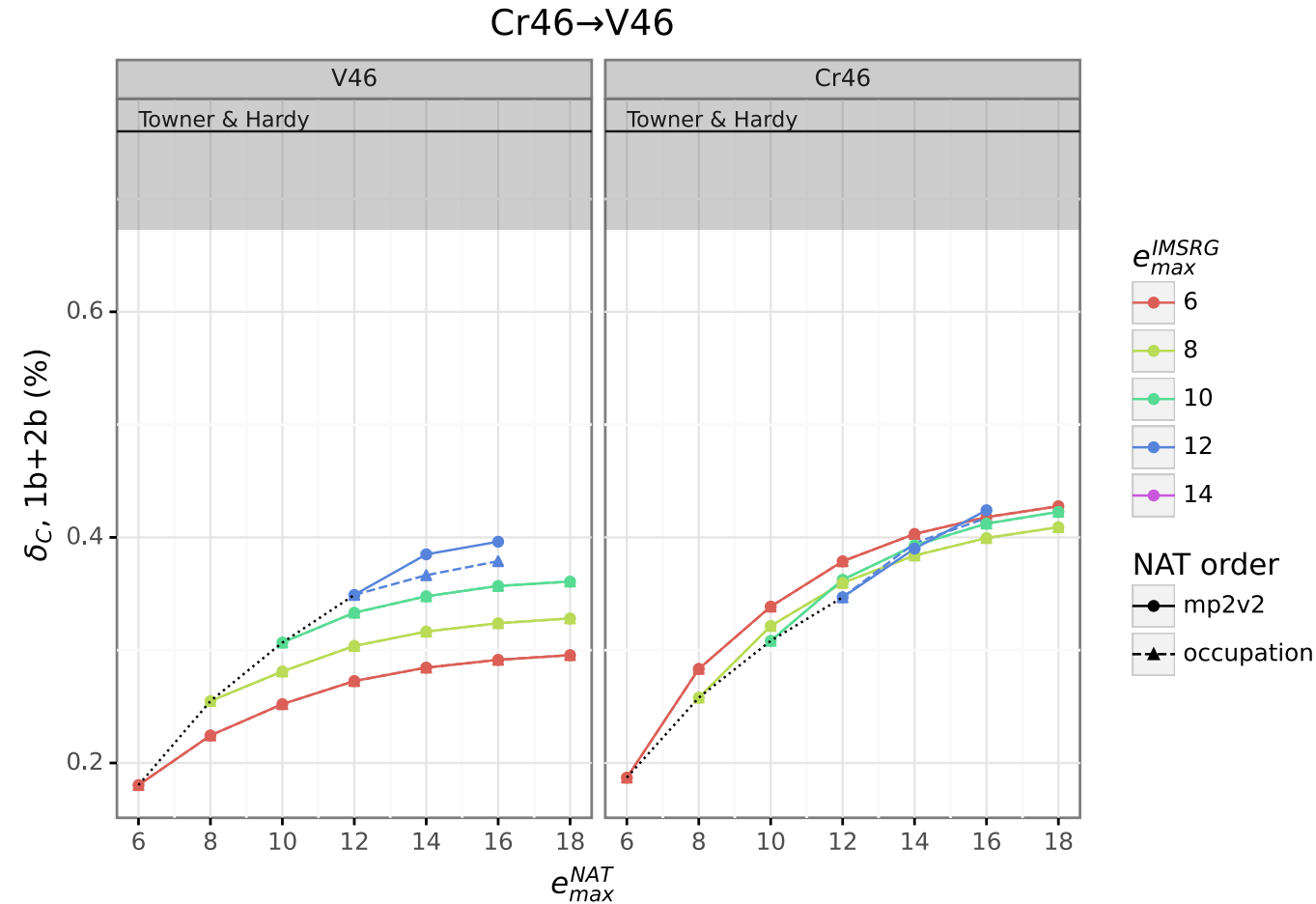
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Natural Orbitals (perturbatively improved) basis:

Medium mass:

consistent results for NAT orbitals chosen
 potentially small reference-state dependence
 still unclear e_{\max} convergence



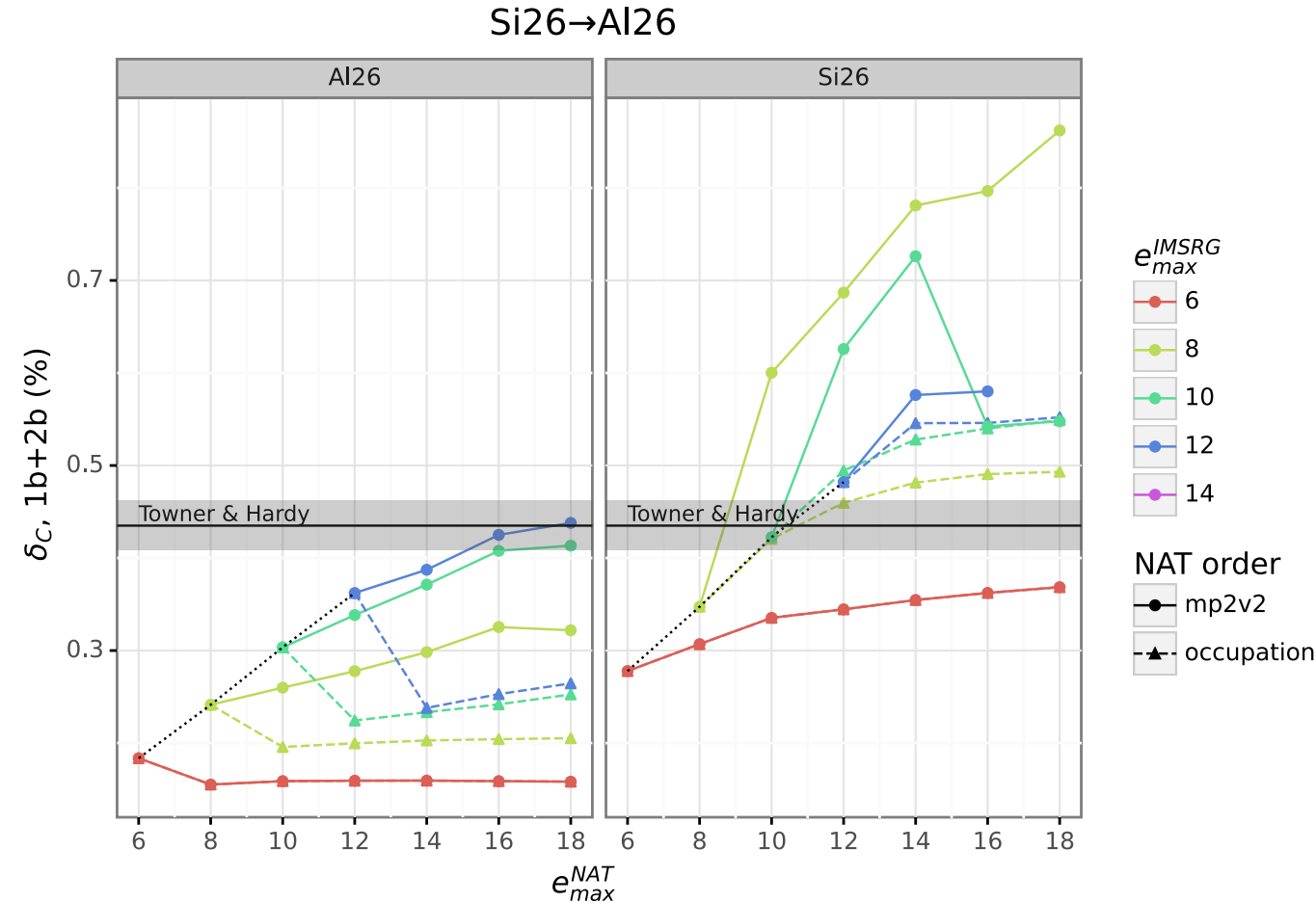
Natural Orbitals (perturbatively improved) basis:

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 still unclear e_{\max} convergence

Lighter systems

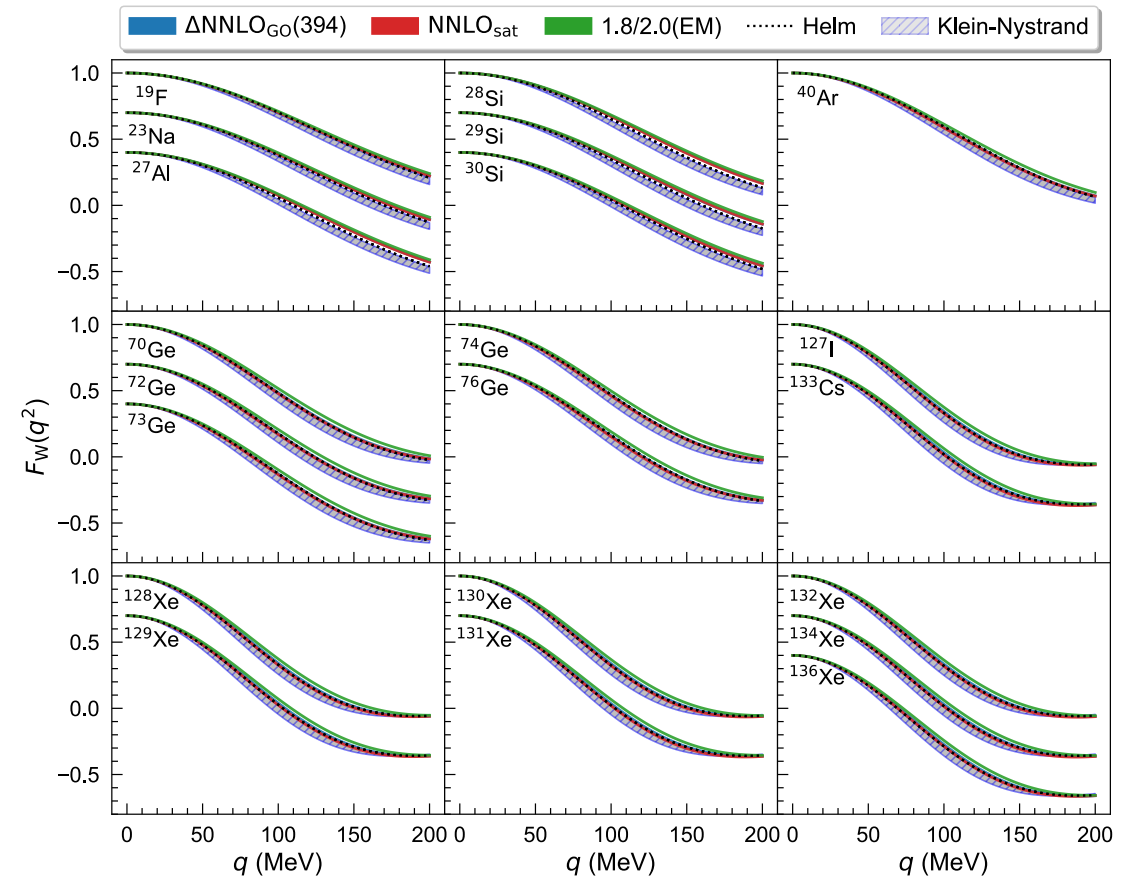
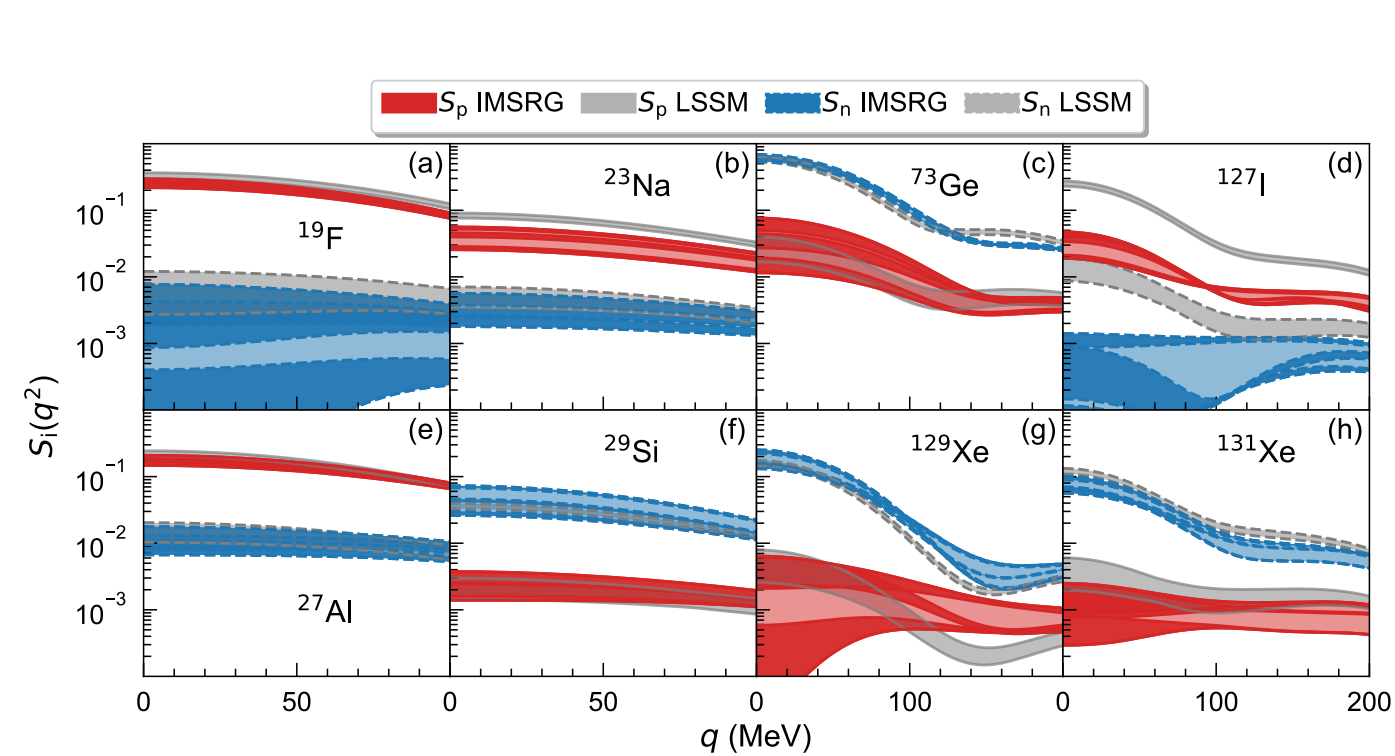
“quirks” in convergence...



Work still in progress...

Use **three** NN+3N chiral interactions with consistent chiral currents

Overall similar to phenomenology at low q , largest discrepancies in ^{127}I



New structure functions for all SD direct-detection candidates