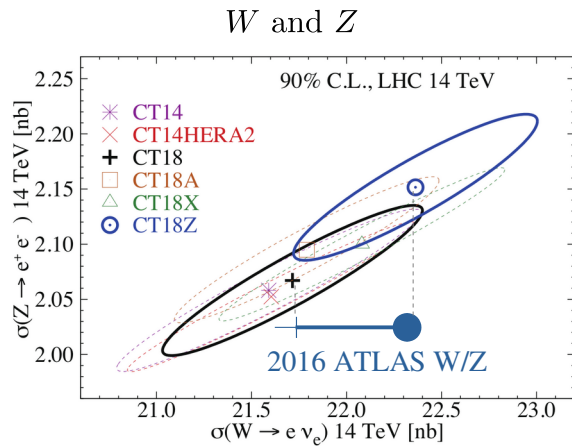
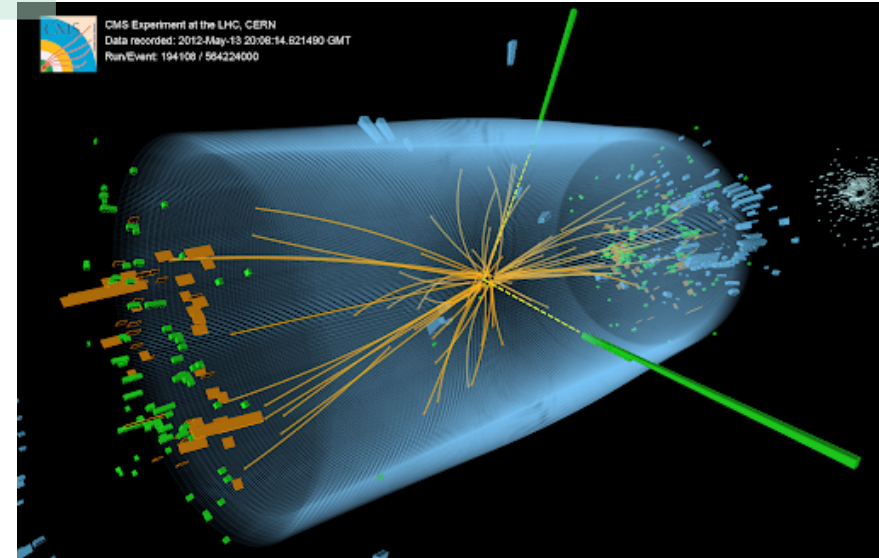
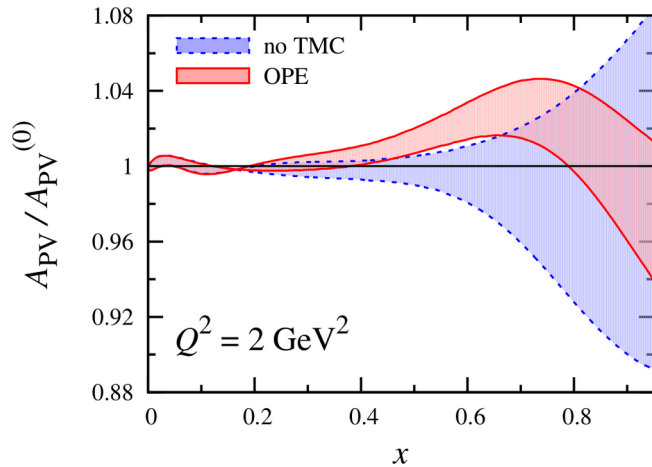


PDF implications and potential of PVDIS at JLab

Tim Hobbs – Fermilab, IIT

30th June 2022



i PVDIS and PDF uncertainties, flavor dependence

1: precision BSM searches limited by (incomplete) proton structure info

- many standard-candle HEP measurements PDF-limited
... including very high x ...
- taming PDF dependence: knowledge of hard-to-access phase-space regions
- PDF studies central to NP QCD at JLab12, maps of hadron structure

2: closely related: flavor separation generally needs numerous expts

- controlling PDF uncertainties requires knowledge of flavor dependence
- complementary measurements/analyses for d/u , \bar{d}/\bar{u} , s , \dots

highlight through: i general status of HEP PDFs; ii flavor dependence issues

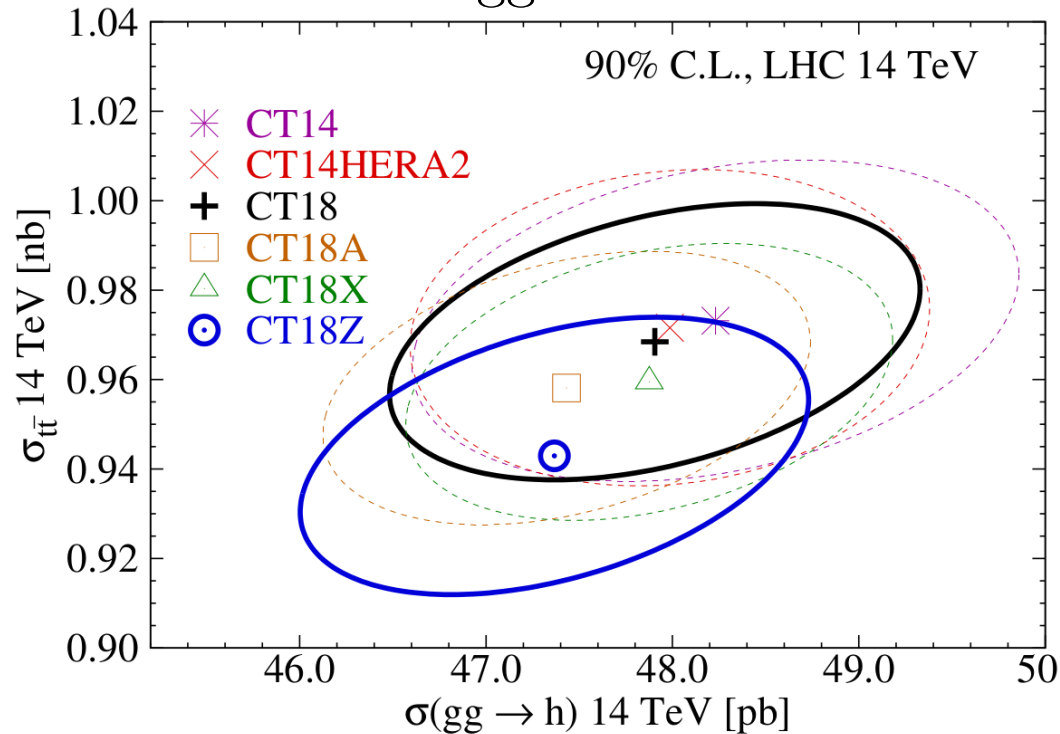
iii conclusion(s): implications for EW physics and PVDIS

SM theory predictions from global analyses

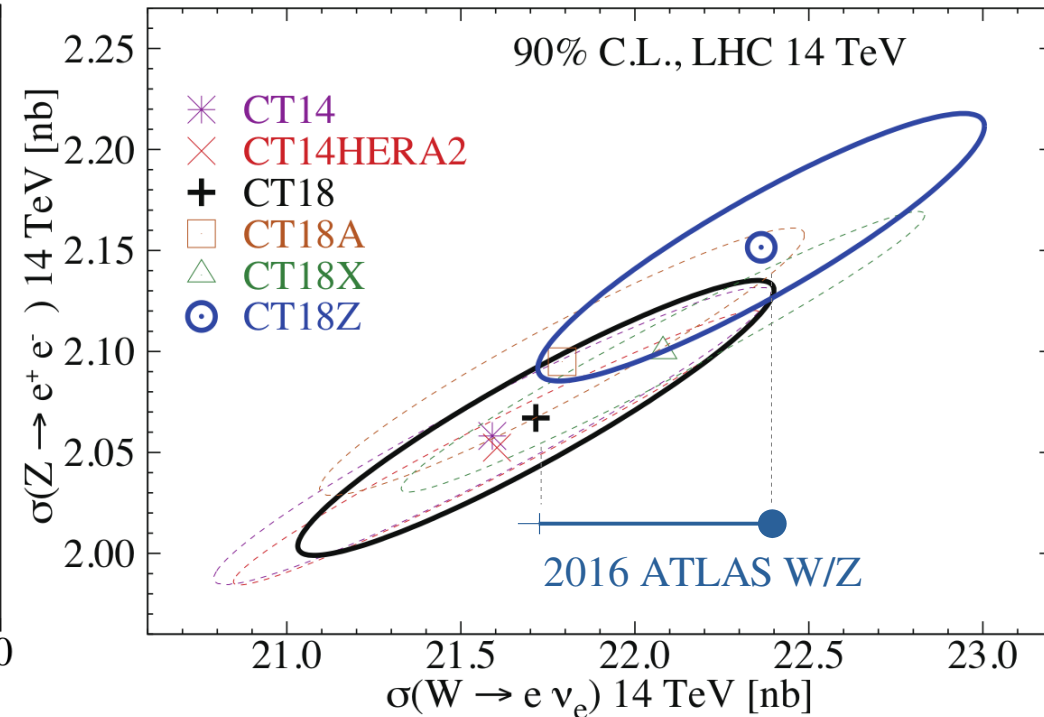
- from NNLO analyses, state-of-the-art predictions for fundamental LHC observables \rightarrow *e.g.*, **total cross sections at 14 TeV**

CT18 NNLO, PRD 103 (2021) 1

Higgs and $t\bar{t}$



W and Z



Higgs, NNLO QCD: iHixs v1.3

$$\mu_R = \mu_F = m_t; m_{W,Z}; m_H$$

NNLO QCD: Vrap v0.9

$t\bar{t}$, NNLO+NNLL: Top++ v2.0

- significant PDF-driven uncertainties; also, systematic effects: W cross sections sensitive to inclusion of 2016 7 TeV ATLAS inclusive W/Z data

i high-interest SM quantities are precision-limited by PDFs

→ these include σ_H , $\sin^2 \theta_W$, m_W , ...

ATLAS, 1701.07240

for example:

Channel	$m_{W^+} - m_{W^-}$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$W \rightarrow e\nu$	-29.7	17.5	0.0	4.9	0.9	5.4	0.5	0.0	24.1	30.7
$W \rightarrow \mu\nu$	-28.6	16.3	11.7	0.0	1.1	5.0	0.4	0.0	26.0	33.2
Combined	-29.2	12.8	3.3	4.1	1.0	4.5	0.4	0.0	23.9	28.0

→ the PDF uncertainty can be a/the dominant uncertainty!

→ frontier efforts at the HL-LHC aim for (sub)percent precision

→ **large cross-cutting effort spanning theory/expt to improve**

- heightened theory accuracy (HO, power corrections)
- novel measurements (JLab12, EIC, LHC, νA)
- generator development

PDFs critical to next-generation precision

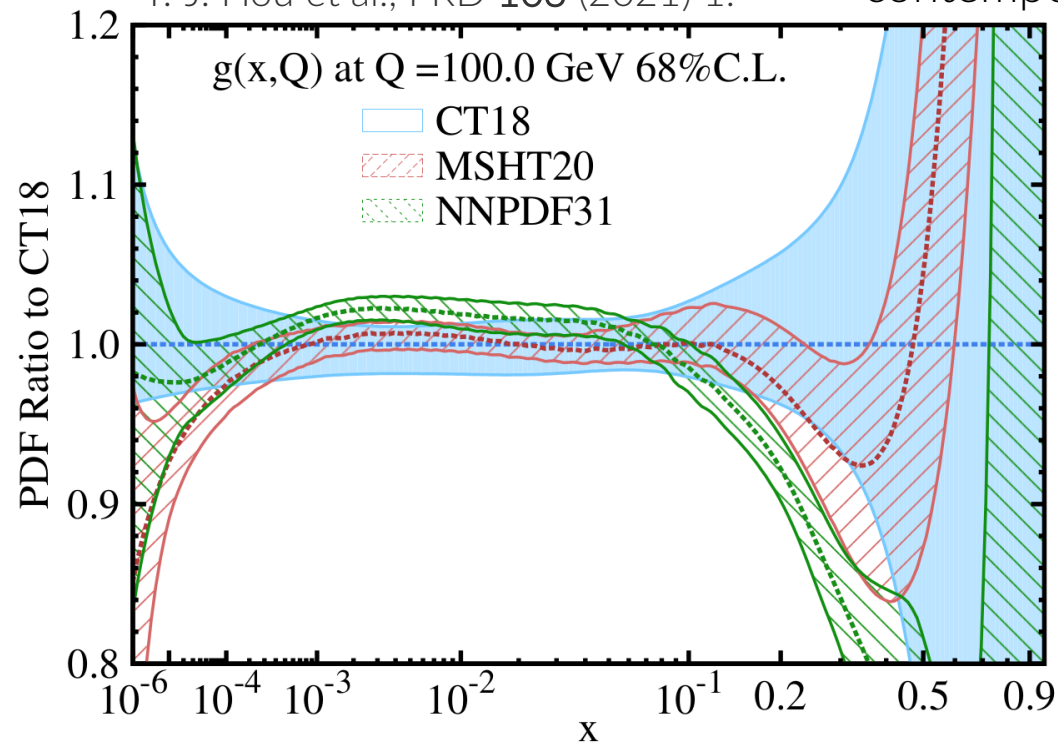
Snowmass21, Amoroso et al.: [2203.13923](#)

→ driven by marriage of latest theory, high-energy hadronic data

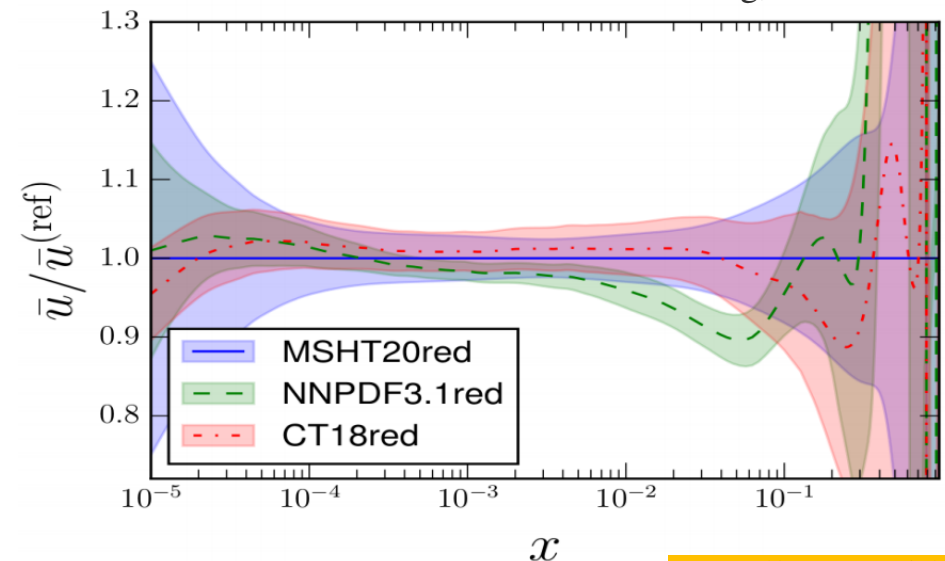
$$\sigma(AB \rightarrow W/Z+X) = \sum_n \alpha_s^n \sum_{a,b} \int dx_a dx_b f_{a/A}(x_a, \mu^2) \hat{\sigma}_{ab \rightarrow W/Z+X}^{(n)}(\hat{s}, \mu^2) f_{b/B}(x_b, \mu^2)$$

T.-J. Hou et al., PRD 103 (2021) 1.

contemporary NNLO QCD fits



PDF4LHC21 benchmarking, [2203.05506](#)



see talk, T. Cridge

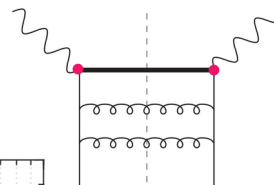
- periodic benchmarking (PDF4LHC21) valuable to cross-check treatment of data

→ seek methodological independence in identifying data-driven PDF features

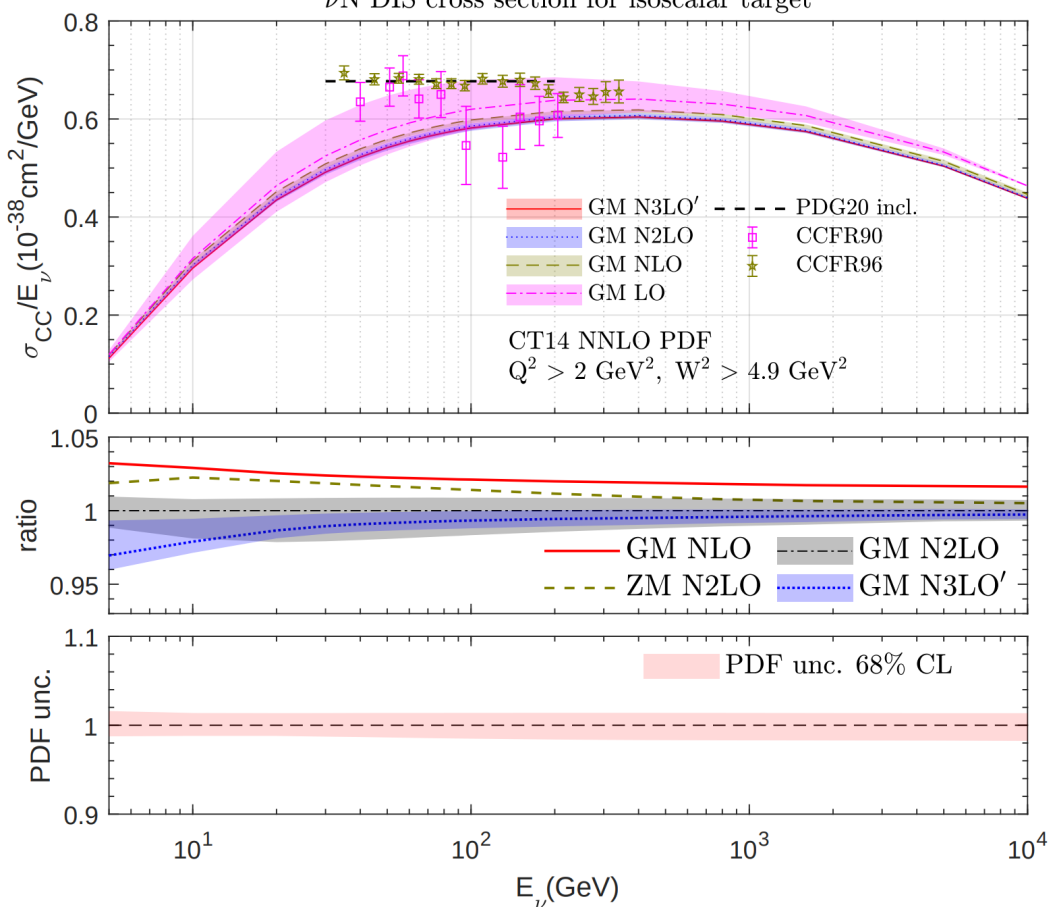
- future analyses will witness an interplay between pQCD & other dynamics
- NNLO+ necessary to stabilize scale uncertainties; especially over wide scales

charge-current DIS

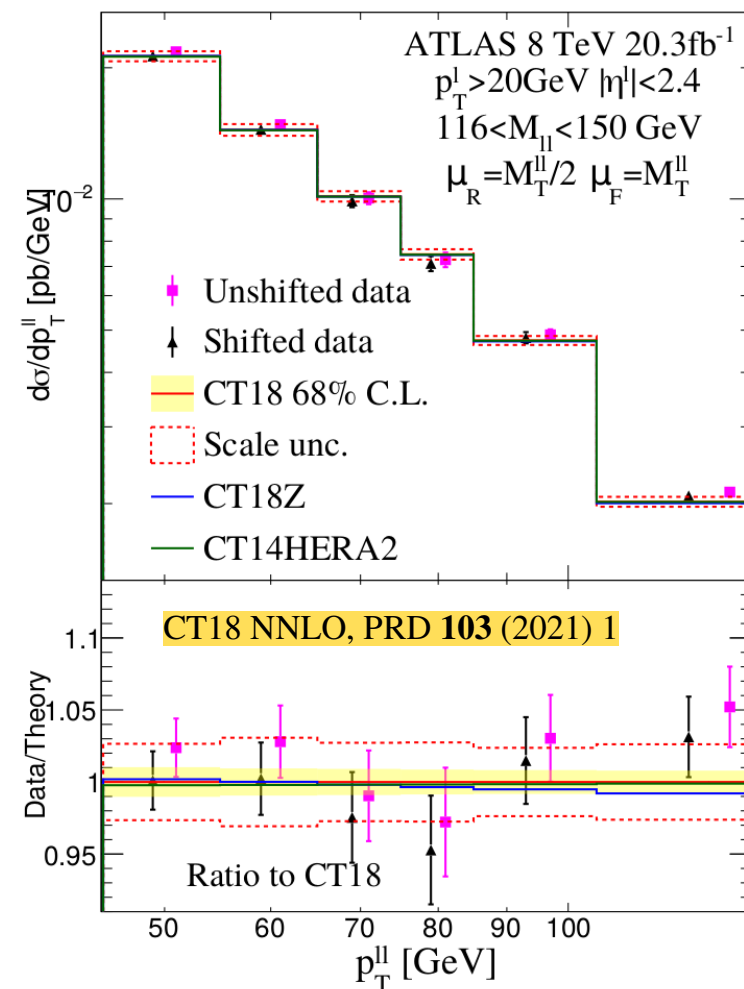
Gao, TJH, Nadolsky, Sun, Yuan: PRD105 (2022) 1, L011503



νN DIS cross section for isoscalar target



NNLO scale variations at LHC



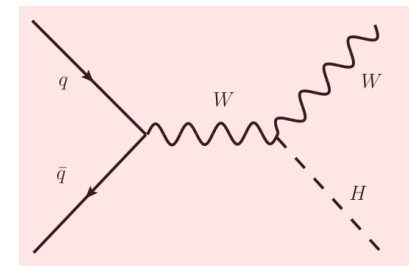
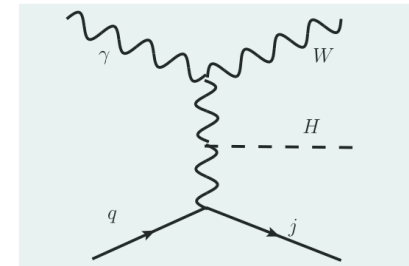
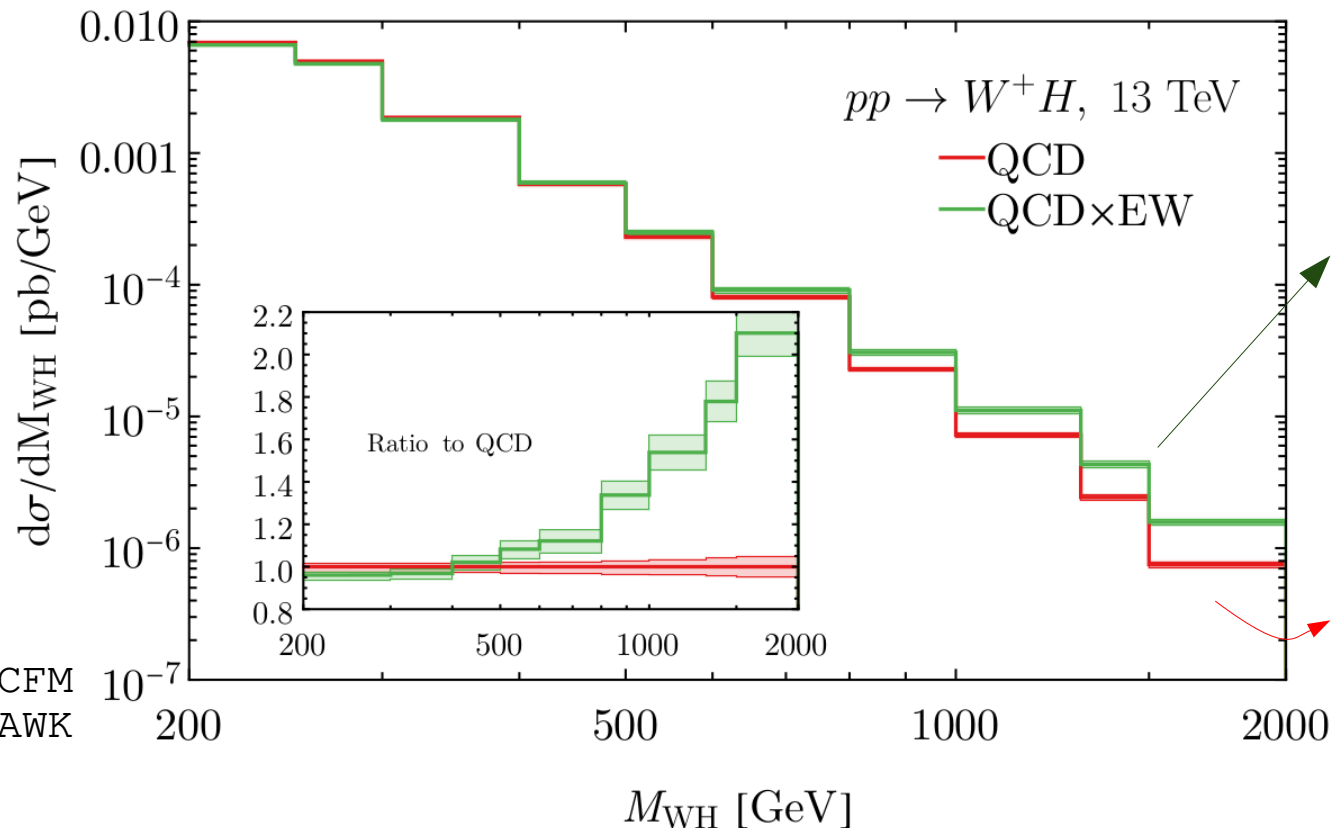
\rightarrow essential to assess PDF dependence in parallel with HO corrections (beyond LO QPM)

electroweak (EW) corrections also vital

- at $\mathcal{O}(\alpha_s^2)$ accuracy, EW corrections and explicit $\gamma(x, \mu^2)$ needed

Xie, TJH, Hou, Schmidt, Yan, Yuan: PRD105 (2022) 5, 054006

- important for high-energy LHC processes: *e.g.*, 13 TeV W+H production



- TeV-scale NLO EW corrections dominated (60%) by single-photon (PDF) contributions

→ requires **delicate** treatment along with QCD perturbative effects

i necessary for electroweak precision: photon PDF

- at $\mathcal{O}(\alpha_s^2)$ accuracy, EW corrections and explicit $\gamma(x, \mu^2)$ needed

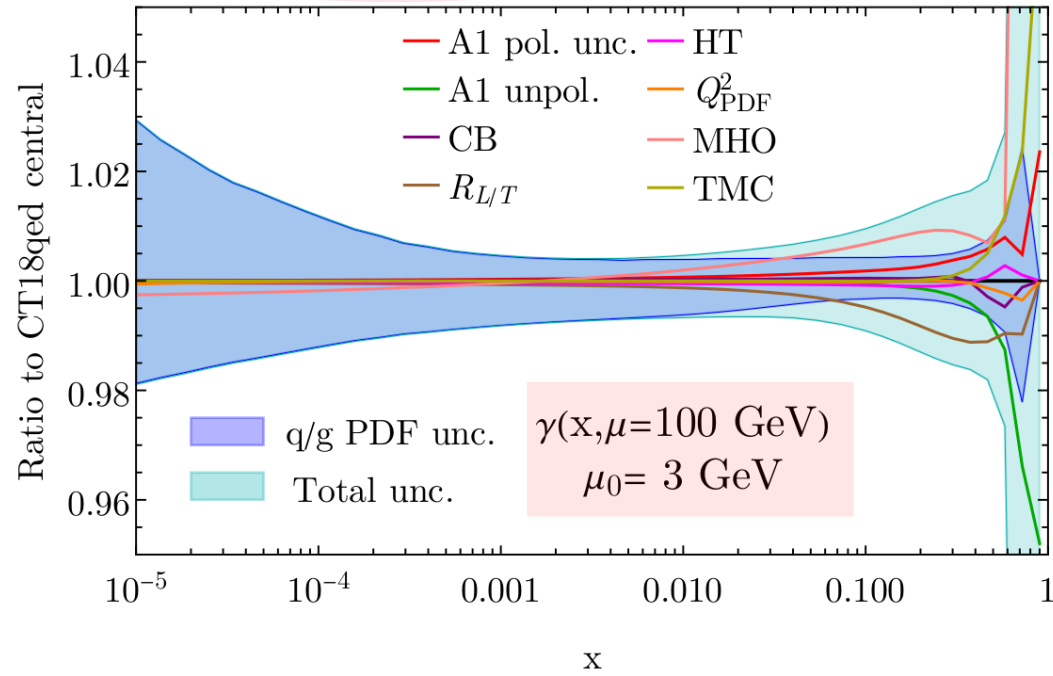
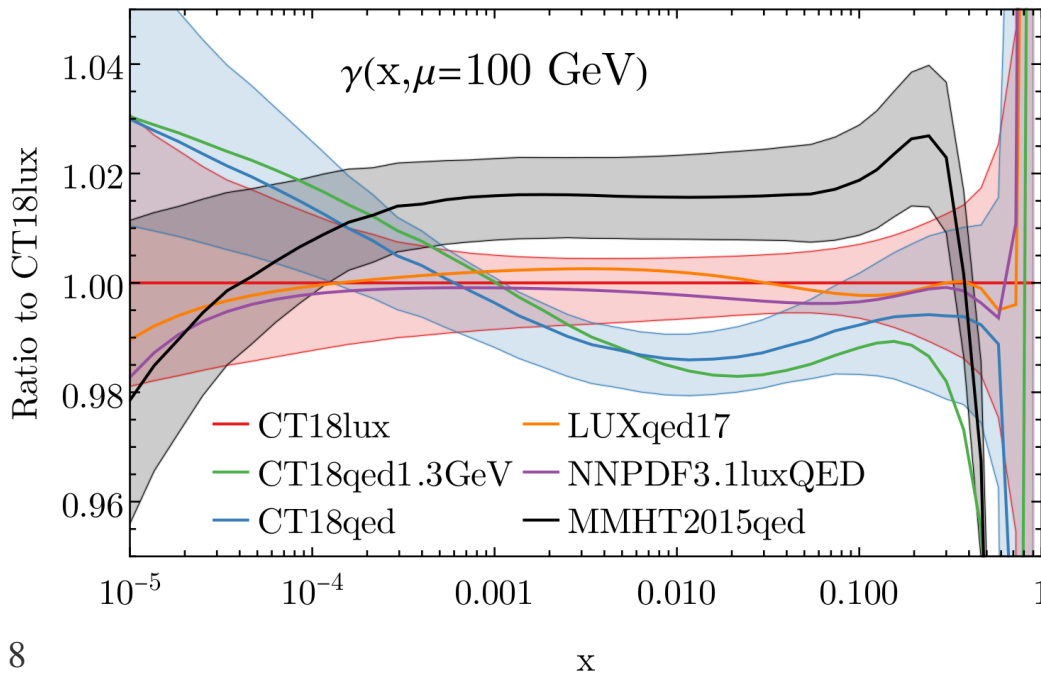
Xie, TJH, Hou, Schmidt, Yan, Yuan: PRD105 (2022) 5, 054006

- following CT14QED, CT18QED now interfaces LUX formalism

$$x\gamma(x, \mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_x^1 \frac{z}{z} \left\{ \int_{\frac{x^2 m_p^2}{1-z}}^{\frac{\mu^2}{1-z}} \frac{Q^2}{Q^2} \alpha_{\text{ph}}^2(-Q^2) \left[\left(zp_{\gamma q}(z) + \frac{2x^2 m_p^2}{Q^2} \right) F_2(x/z, Q^2) - z^2 F_L(x/z, Q^2) \right] - \alpha^2(\mu^2) z^2 F_2(x/z, \mu^2) \right\} + \mathcal{O}(\alpha^2, \alpha\alpha_s)$$

- depends on nonperturbative inputs [kinematical cuts alone can't avoid this]

[i.e., large- x physics...]

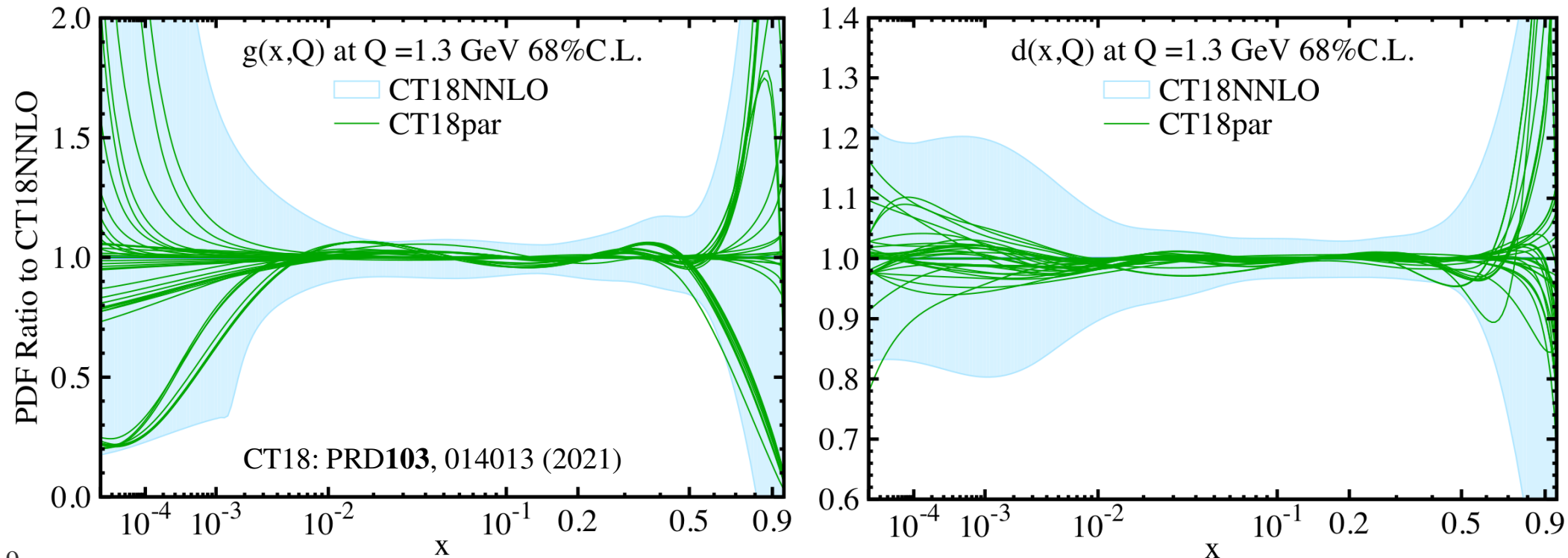


i

parametrization uncertainty: nonperturbative fitting forms

- initial PDFs still not generally calculable through rigorous QCD at $Q = Q_0 = m_c$ (to the needed precision...)
 - subject to complex nonperturbative dynamics
 - practice agnosticism w.r.t. initial parametrization
(some guidance from QCD, QCD-inspired models)
 - explore model uncertainty with many forms

parametrization uncertainties largest in extrapolated regions



ii

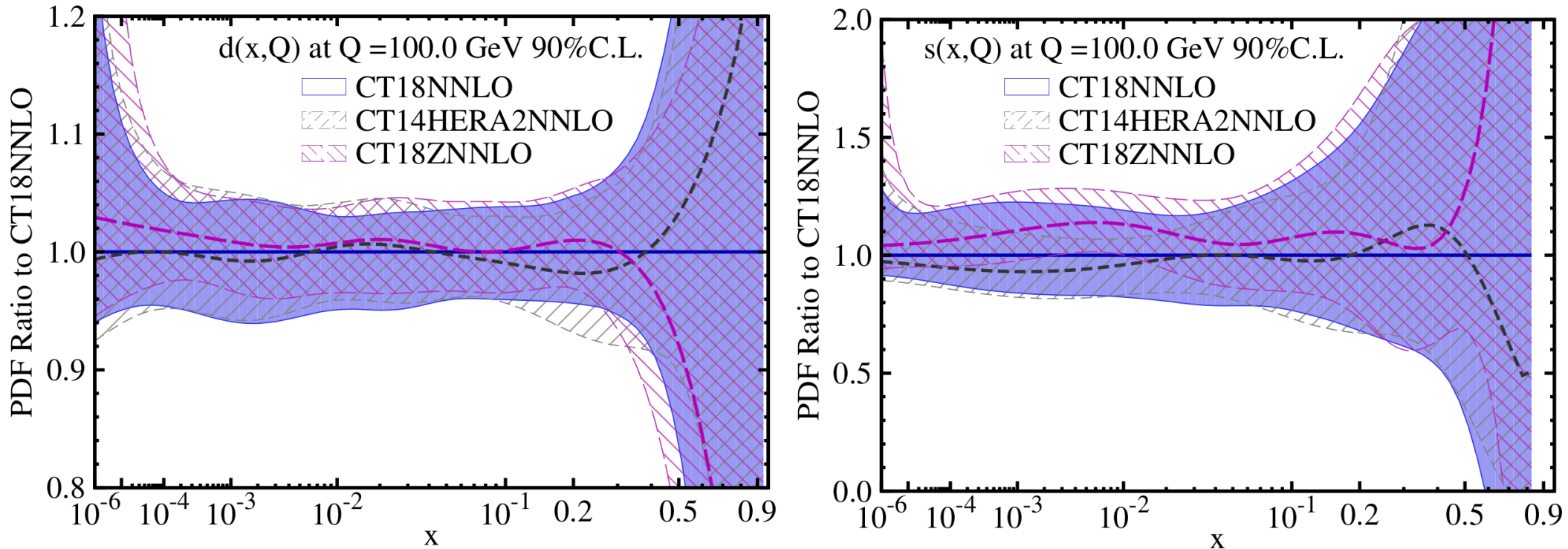
high- x PDFs remain dominated by large uncertainties

- much of the JLab12 (PVDIS) sensitivity probes high- x (low- W , Q) PDFs
- PDF (Hessian) uncertainties enlarge dramatically in high- x limit

→ limited data

→ extrapolation

→ data tensions

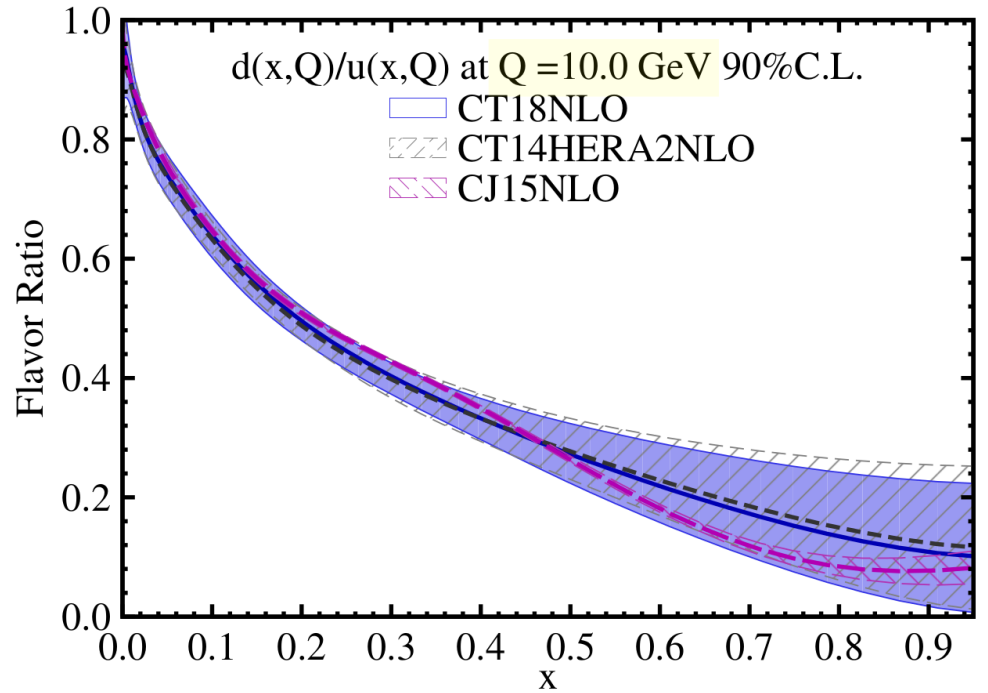
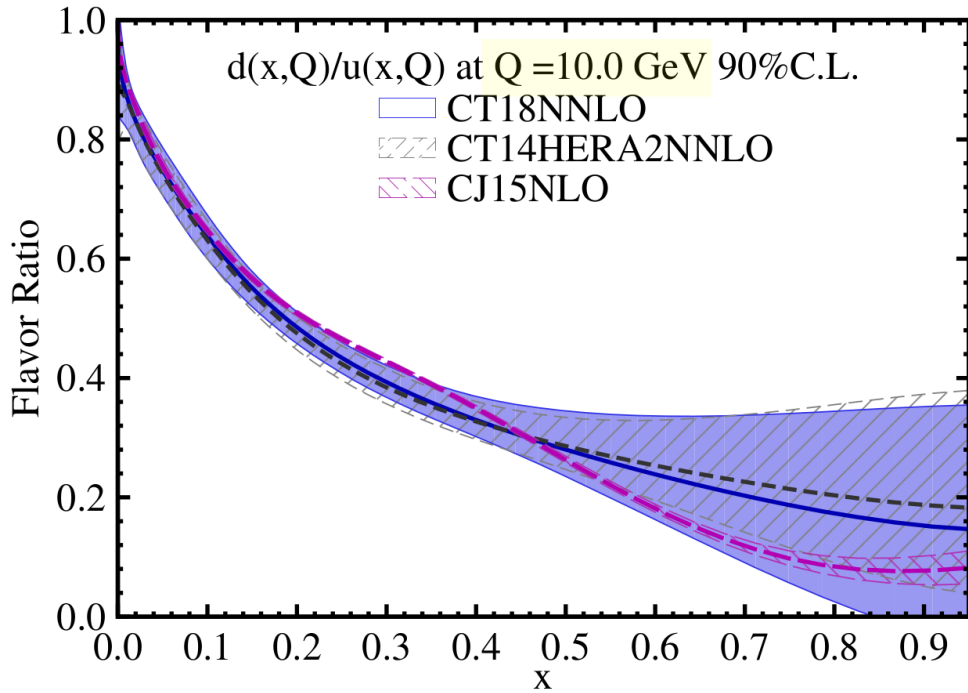


- flavor separation also challenging; parsing quark sea: various precision data

→ PVDIS γ -Z interference further complements standard data sets

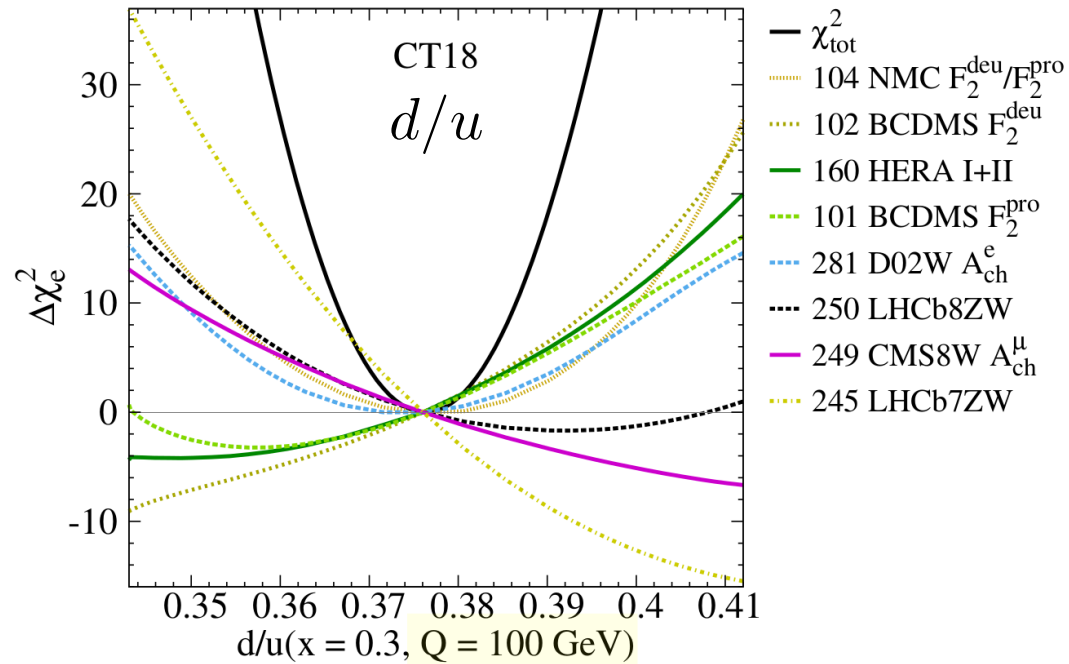
ii

perturbative order (α_s), interplay of data sets relevant for high- x d/u



[see talk: C. Keppel]

- NNLO vs. NLO theory accuracy influences extrapolation region behavior
- competing pulls of fitted data at high- x also restrict precision; e.g.,
 - BCDMS, F_2^d
 - LHCb, W/Z 7 TeV



ii light-nuclear corrections: **flavor dependence**, high- x PDFs

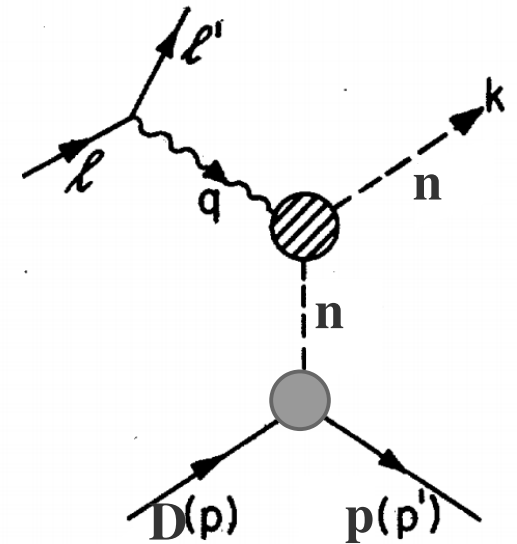
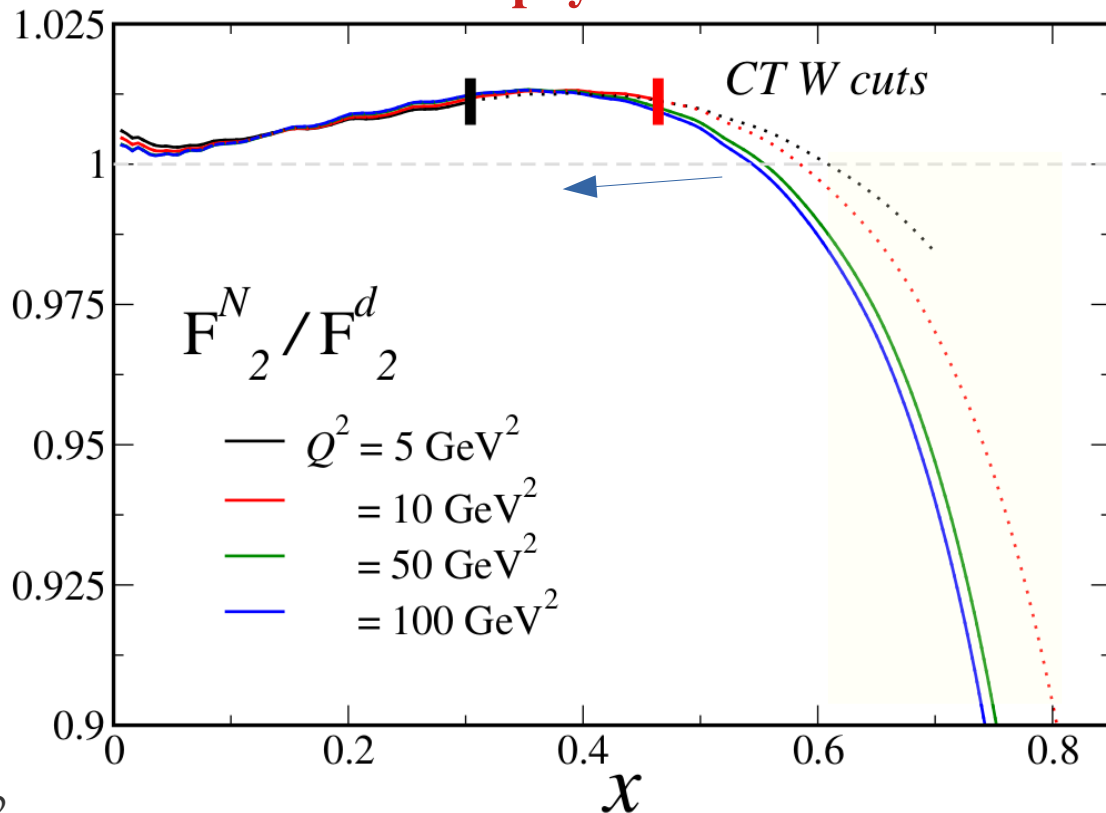
- d -PDF information from deuteron scattering; nuclear corrections relevant

$$f^d(x, Q^2) = \int \frac{dz}{z} \int dp_N^2 \mathcal{S}^{N/d}(z, p_N^2) \tilde{f}^N(x/z, p_N^2, Q^2)$$

CJ-CT: Accardi, TJH, Jing, Nadolsky: EPJC81 (2021) 7, 603

- corrections are generally ~percent-level, but can become larger, especially at high x

isoscalar-to-physical deuteron



- impacts LHC observables; necessary for high precision

ii

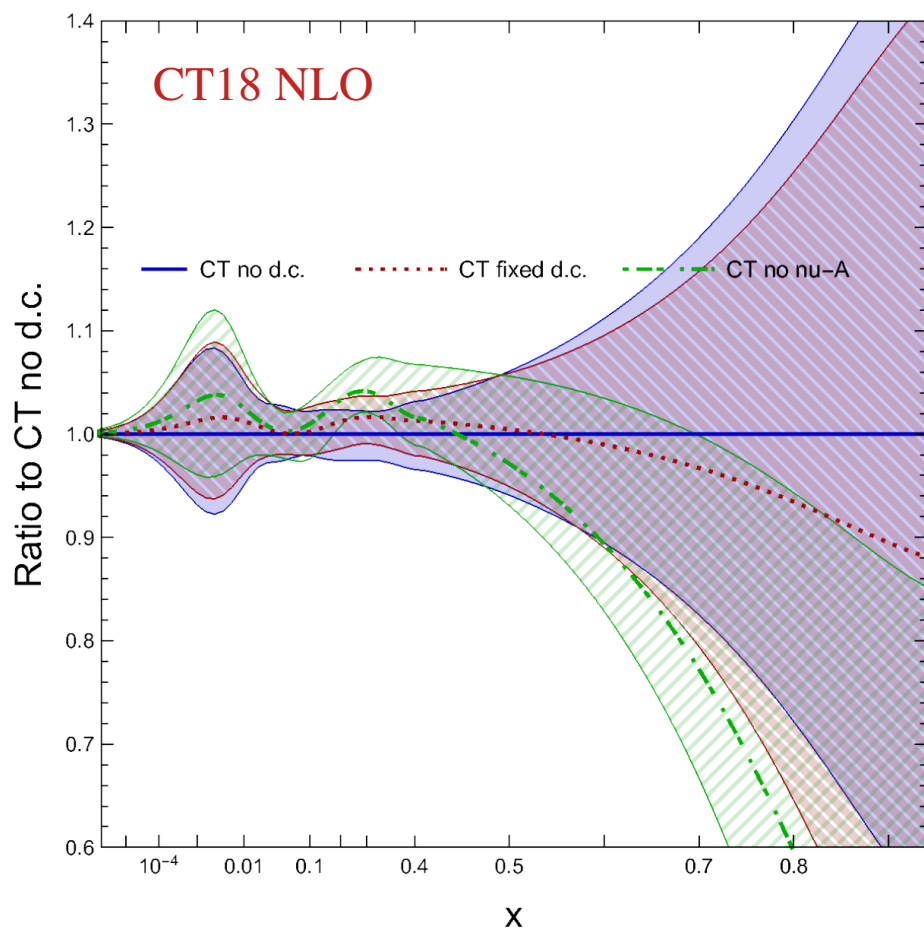
nuclear modifications of increasing importance with greater PDF precision

- example: nuclear effects in deuteron influence d -quark PDF ($x \geq 0.1$)

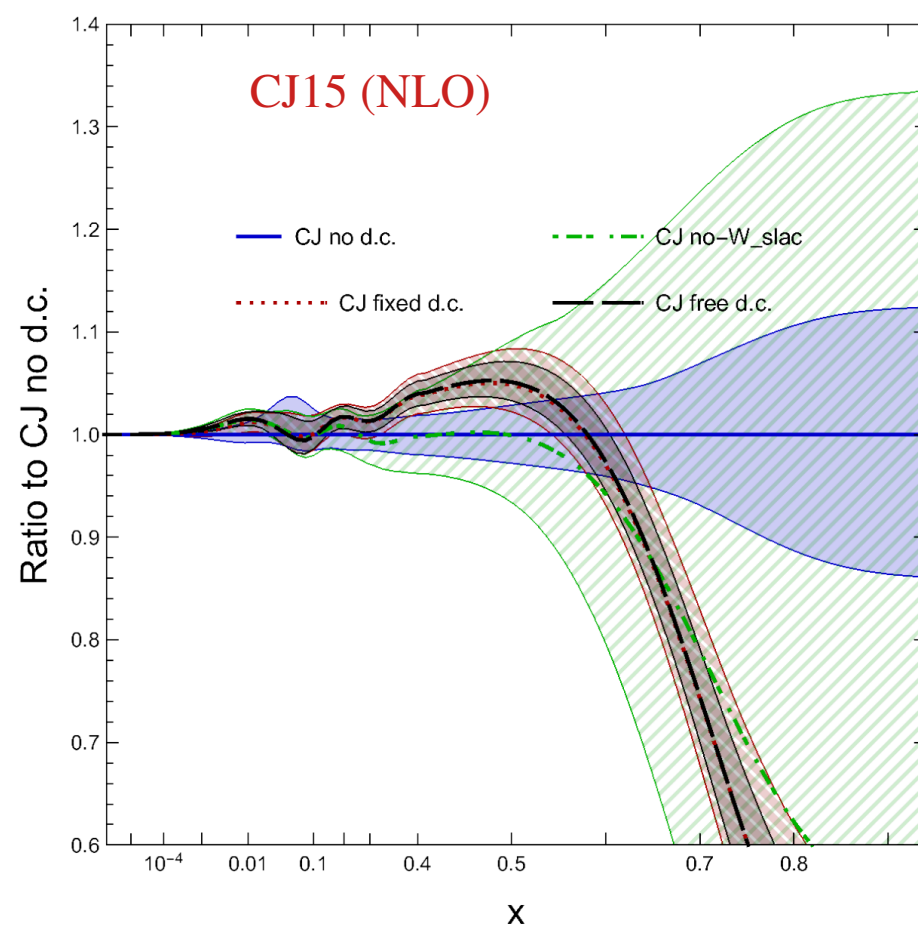
CJ-CT: Accardi, TJH, Jing, Nadolsky: EPJC81 (2021) 7, 603

- comparative study: additional effects at lower- x ; gluon impacts (from flavor correlations)

$d(x,Q)/u(x,Q)$ at $Q=2.0$ GeV, $T^2 = 10$



$d(x,Q)/u(x,Q)$ at $Q=2.0$ GeV, $T^2 = 10$



- subtle interplay with **nuclear corrections** in large- A targets

→ demands more attention in future (free nucleon) PDF analyses

[will revisit]

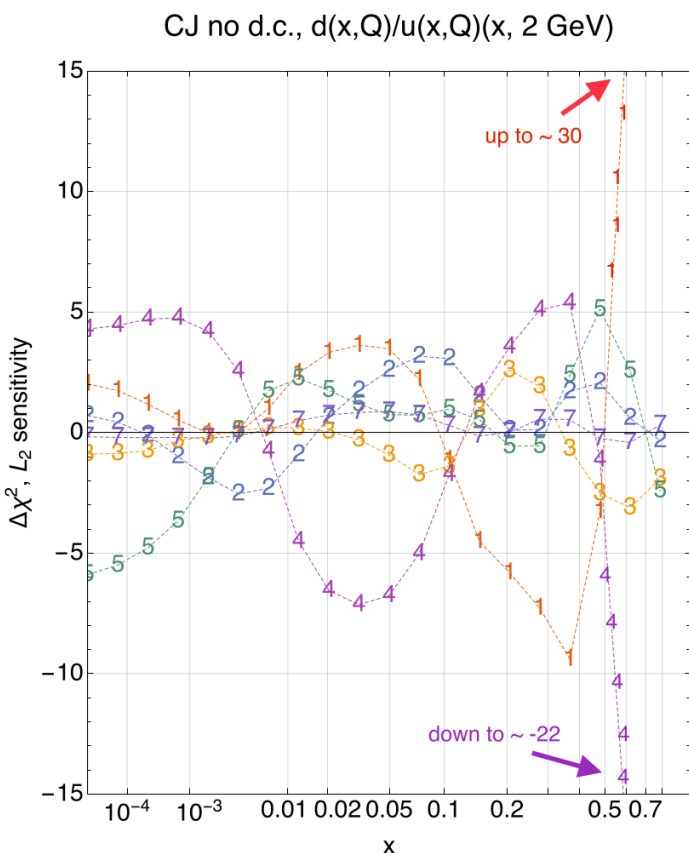
pulls of fitted data on d/u influenced by deuteron corrections

- L_2 sensitivity: quickly assess $\Delta\chi^2$ from upward shift of PDFs by 1σ uncertainty

→ useful for apples-apples comparisons, especially among Hessian fits

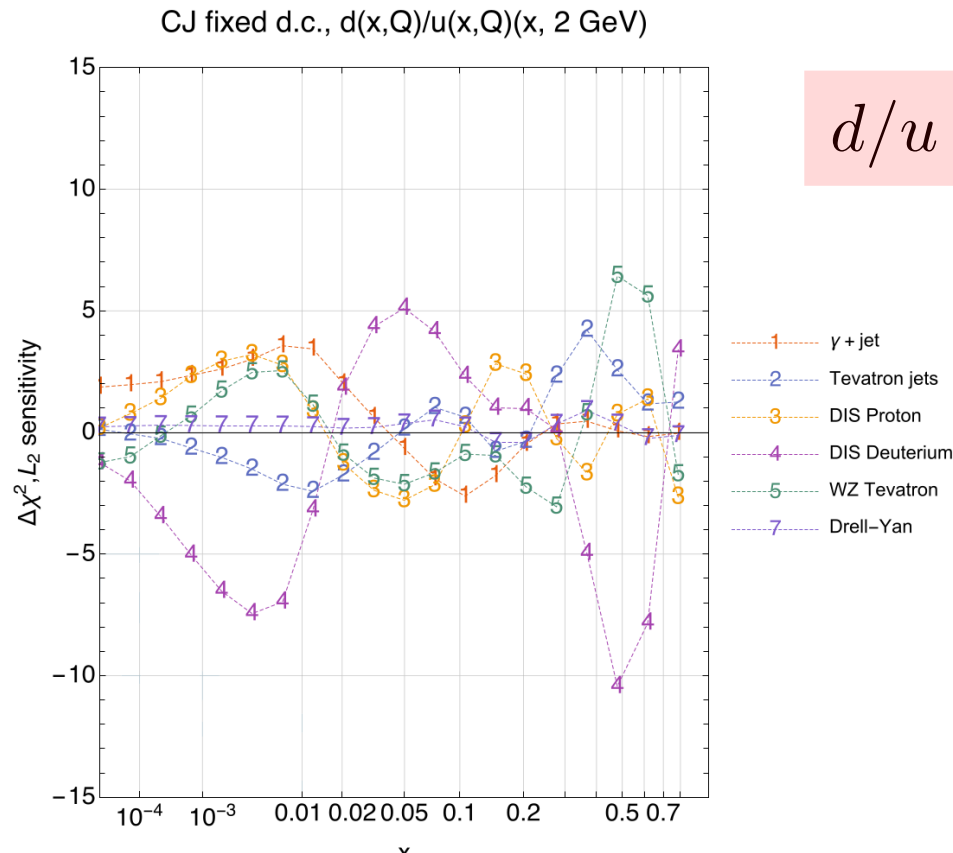
<https://ct.hepforge.org/PDFs/ct18/figures/L2Sensitivity/>

CJ-CT: Accardi, TJH, Jing, Nadolsky: EPJC81 (2021) 7, 603



— 1 γ + jet
— 2 Tevatron jets
— 3 DIS Proton
— 4 DIS Deuterium
— 5 WZ Tevatron
— 7 Drell-Yan

↑ data prefer smaller
↓ (larger) PDF at given x

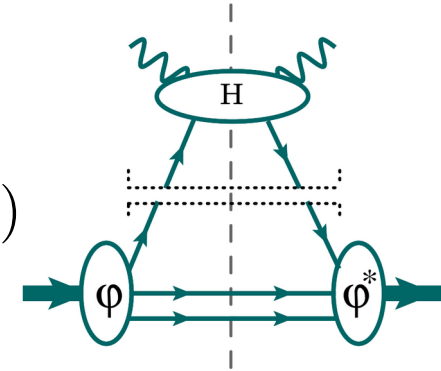


- in CJ fits *without* deuteron correction (left), large tensions at high x : γ -jet [1] vs. DIS-deuterium [4] data; especially at $x > 0.5$

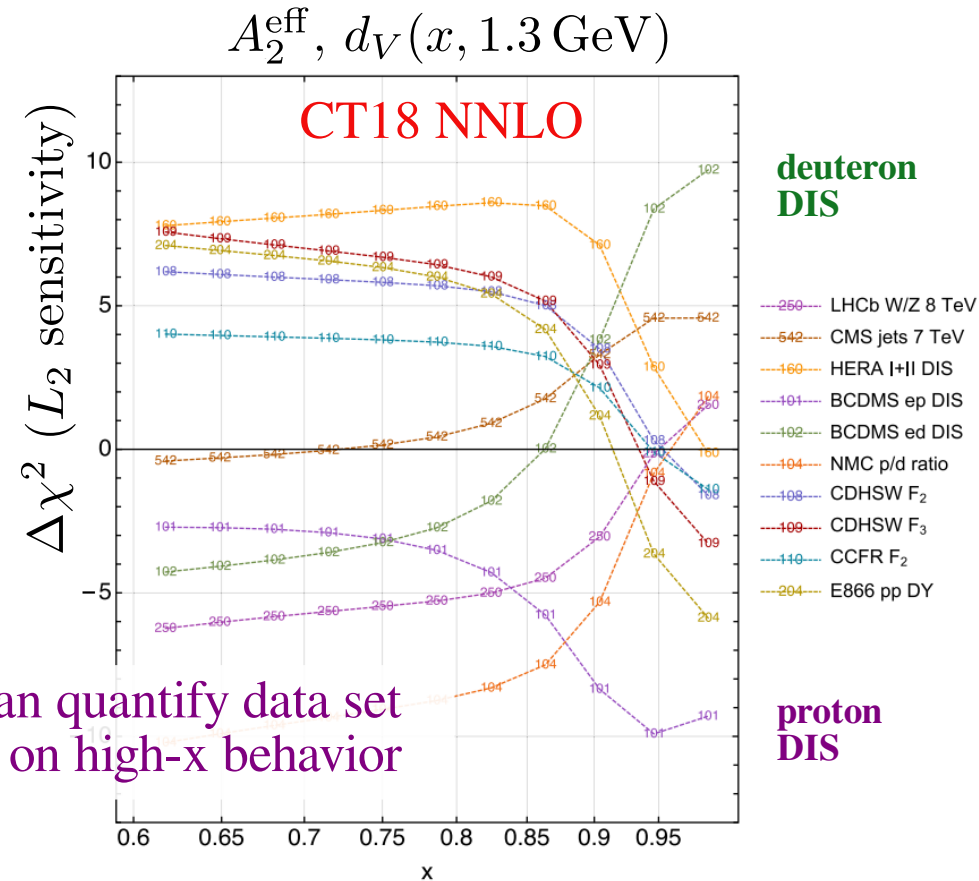
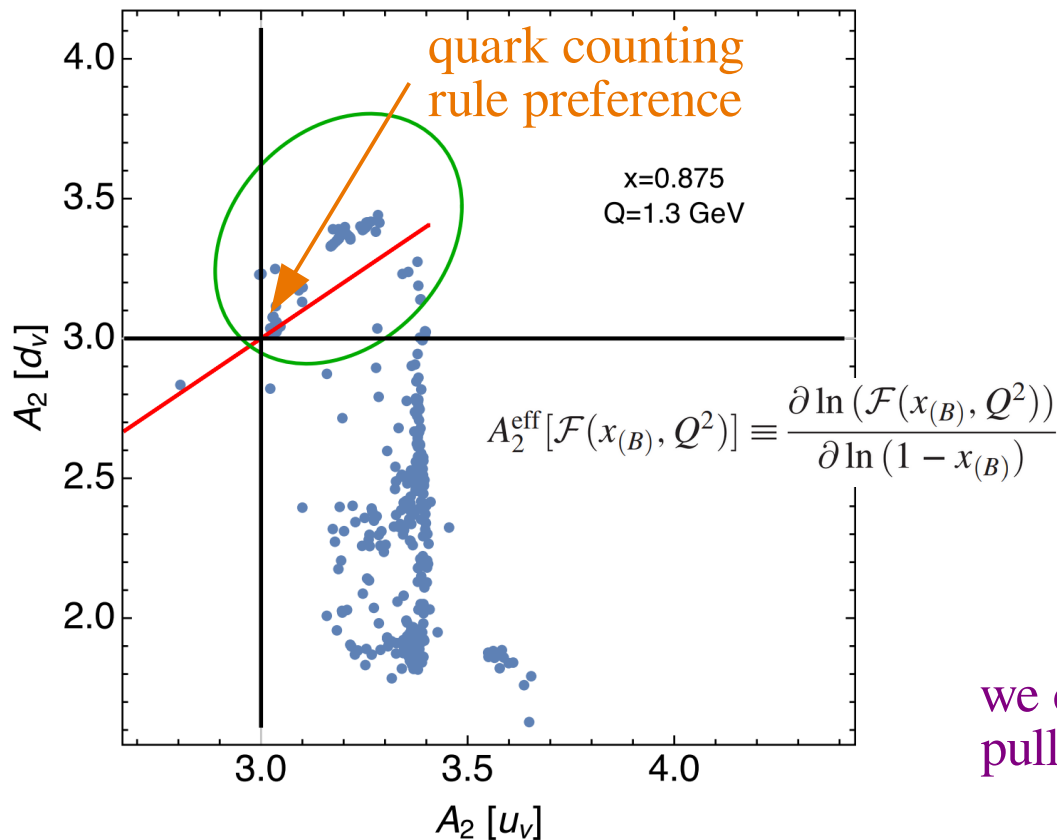
→ with fixed correction (right), tensions relieved significantly

extracting high- x dependence in PDF fits

- high- x PDFs, ratios [e.g., d/u] connected to details of proton WF
- behavior at $x \rightarrow 1$ an important nonpert. discriminator
- CT18, parametrize $f_{a/A}(x, Q_0^2) = x^{A_{1,a}} (1-x)^{A_{2,a}} \times \Phi_a(x)$



Courtoy and Nadolsky, PRD**103**, 054029 (2021)



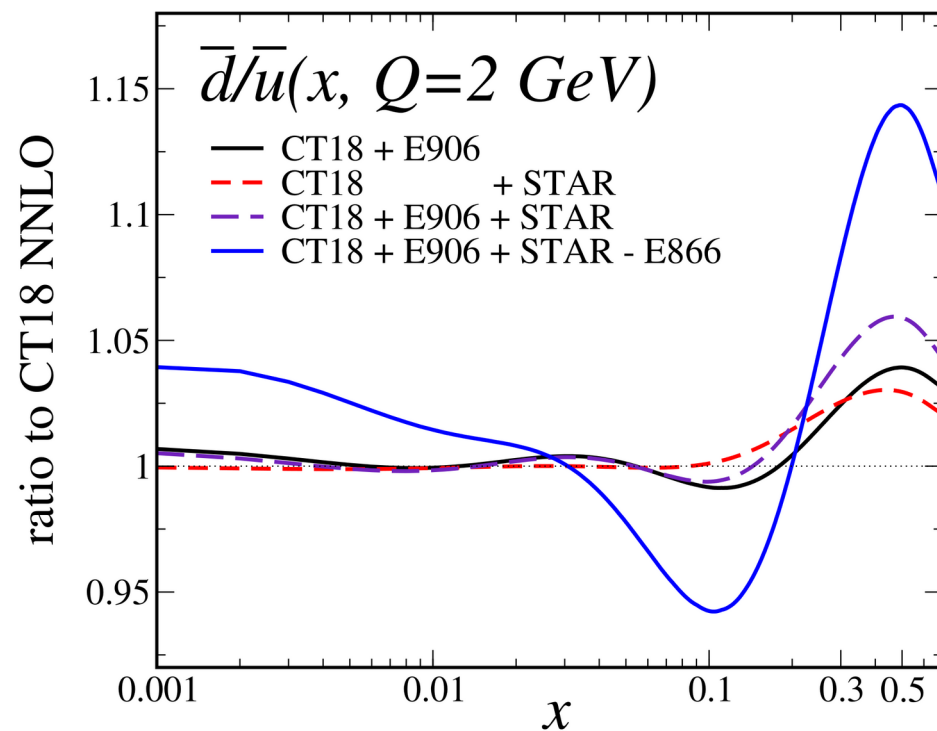
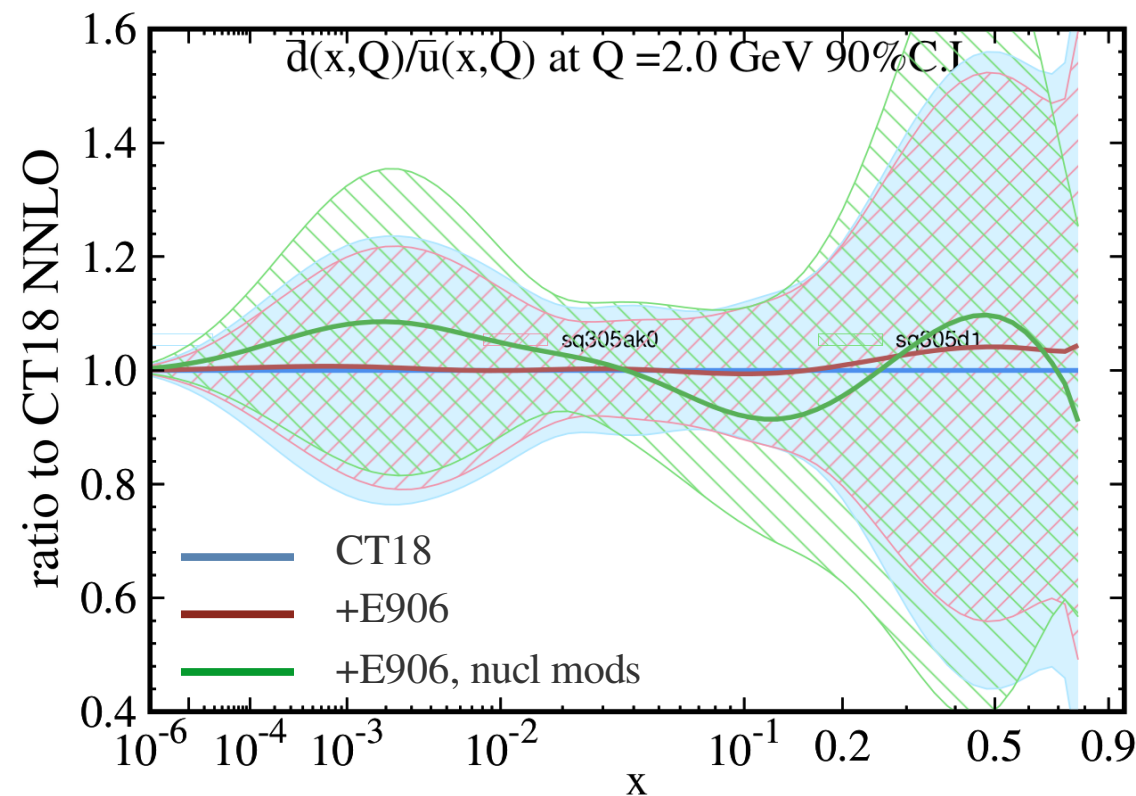
we can quantify data set pulls on high- x behavior

ii

high- x sea-quark asymmetries: SeaQuest (E906) and STAR Drell-Yan data

- potential overlap between PVDIS and PDF sensitivities of other high- x expts $\bar{d} > \bar{u}$
- recently-released SeaQuest data have **moderate sensitivity** to high- x

[see talk: A. Tadepalli]

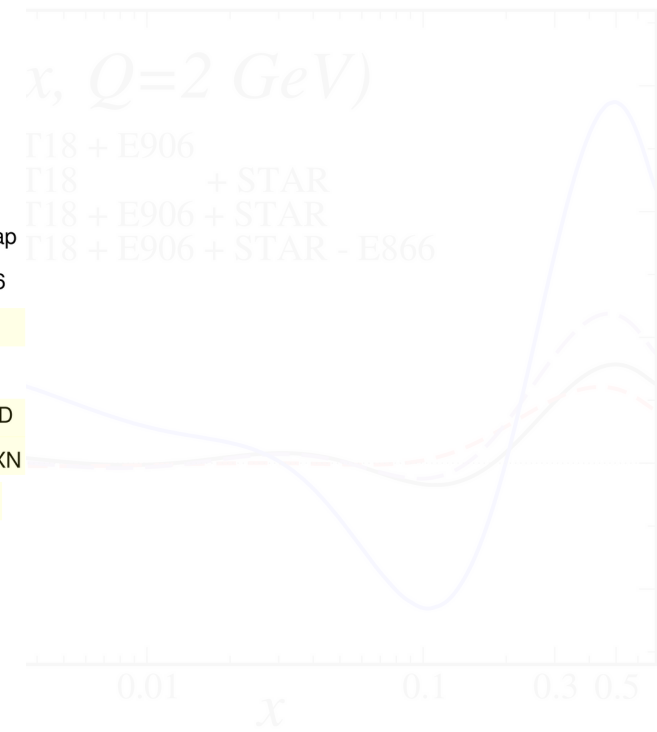
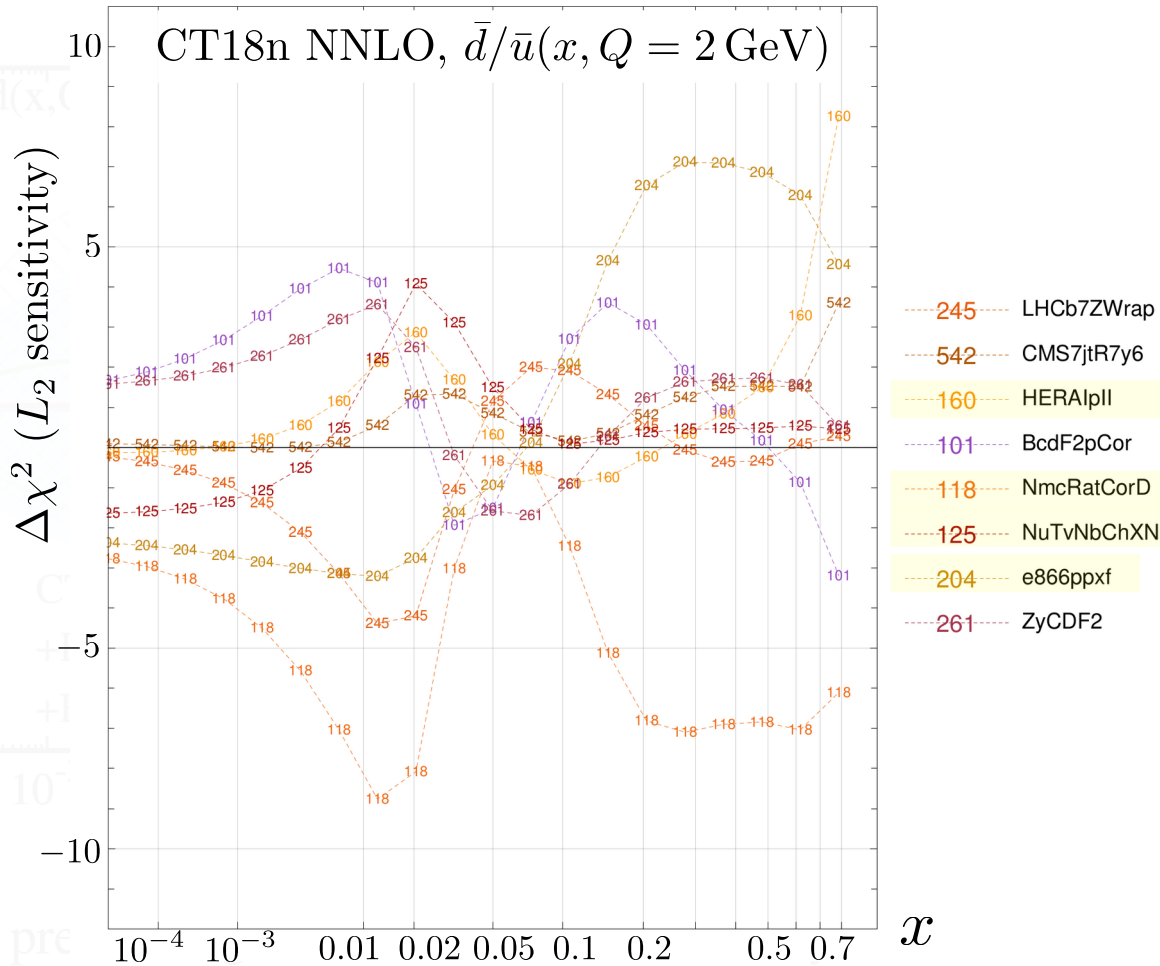


- SeaQuest prefers larger \bar{d}/\bar{u} at $x > 0.2$; may *somewhat* reduce strange-PDF uncertainty
- interplays: treatment of nucl. data (left); inclusion of STAR W -prod., E866 expts. (right)
 - E906, STAR constructively enhance \bar{d}/\bar{u} ; removing E866 augments this effect

ii

high- x sea-quark asymmetries: SeaQuest (E906) and STAR Drell-Yan data

- potential overlap between PVDIS and PDF sensitivities of other high- x expts $\bar{d} > \bar{u}$
- L_2 sensitivities: excluding E866, minimal tensions between E906, other sets
- recently-released SeaQuest data have moderate sensitivity to high- x



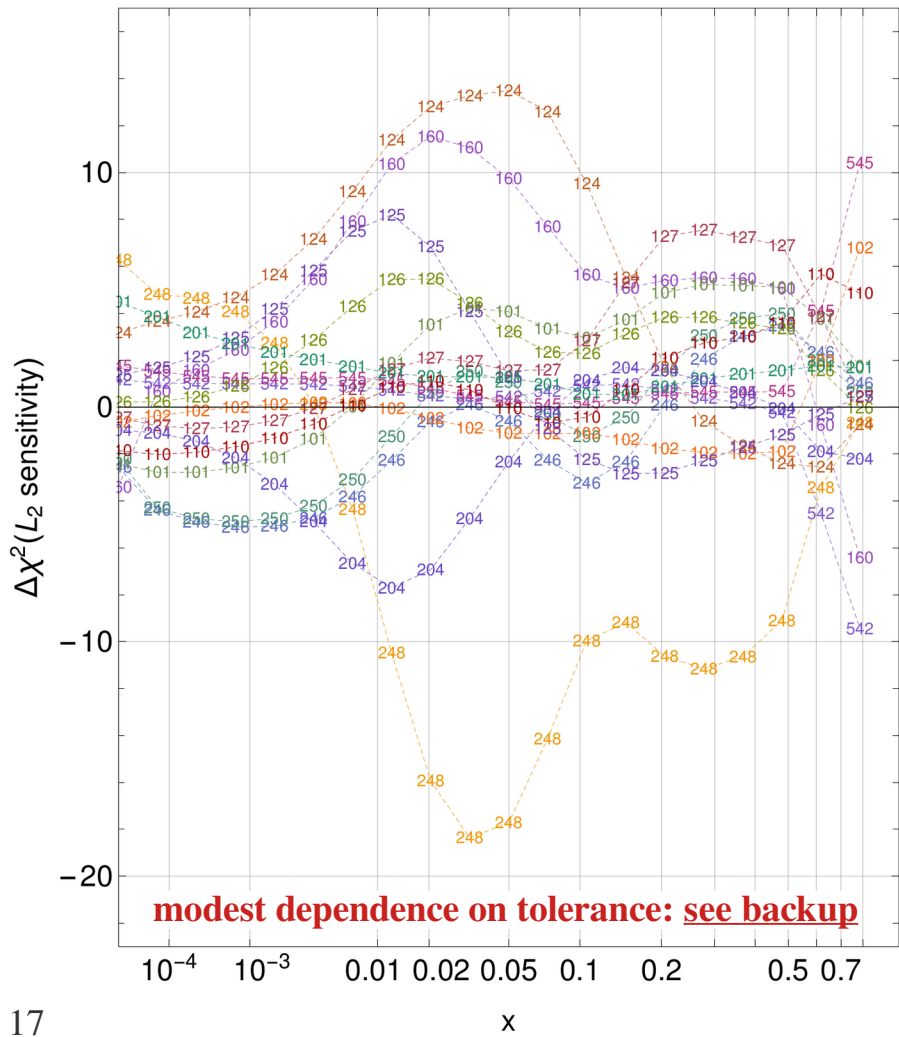
- SeaQuest pre
- interplays: treatment of nucl. data (left); inclusion of STAR W -prod., E866 expts. (right)
- forthcoming study: exploration of PDF pulls in post-E906 fits...
 - E906 + STAR constructively enhance \bar{d}/\bar{u} ; removing E866 augments this effect

ii

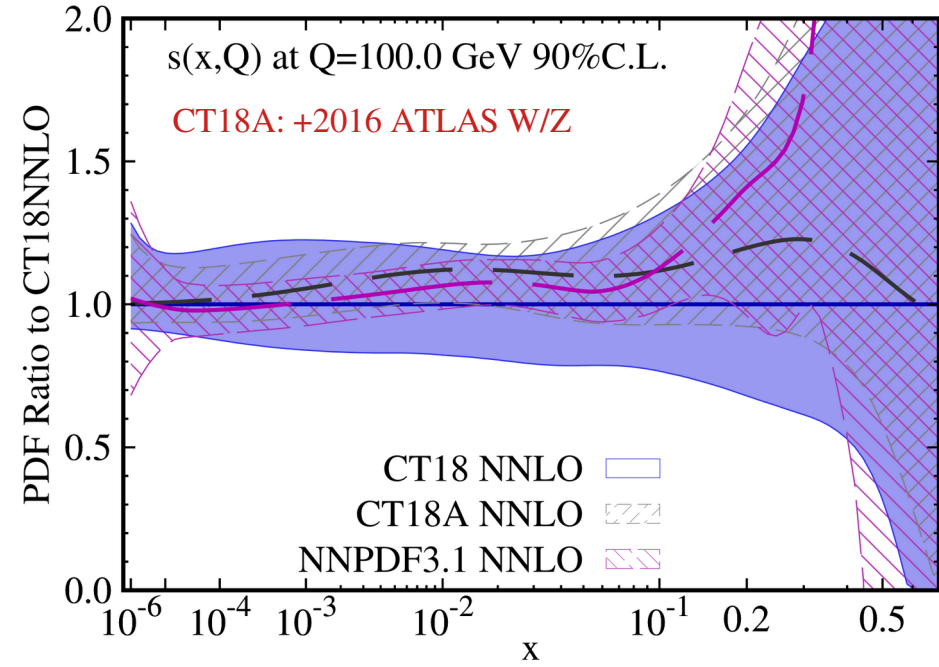
nucleon strangeness from neutrino and Drell-Yan data

- strangeness PDF, breaking of flavor SU(3) remain highly uncertain
- CT18: indications of tension between neutrino (need nuclear corrections), precise LHC W/Z data

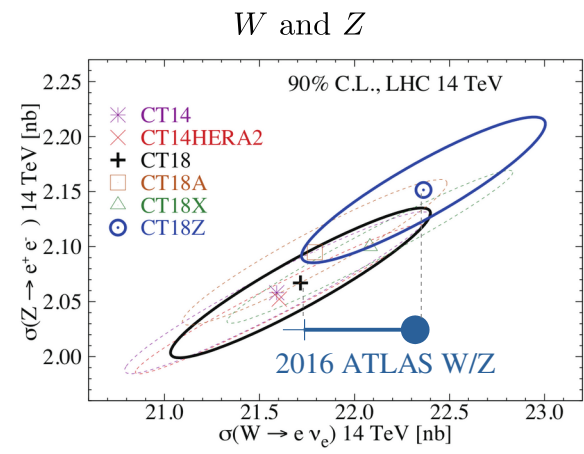
CT18Z NNLO, $s(x, 2 \text{ GeV})$



- 246--- LHCb8Zeer
 - 248--- ATL7ZW.xF
 - 250--- LHCb8WZ
 - 542--- CMS7jtR7y6T
 - 545--- CMS8jtR7T
 - 160--- HERAIpII
 - 101--- BcdF2pCor
 - 102--- BcdF2dCor
 - 110--- ccfrr2.mi
 - 124--- NuTvNuChXN
 - 125--- NuTvNbChXN
 - 126--- CcfrNuChXN
 - 127--- CcfrNbChXN
 - 201--- e605
 - 204--- e866ppxf
- νA



→ again, consequential for EW sector HEP measurements

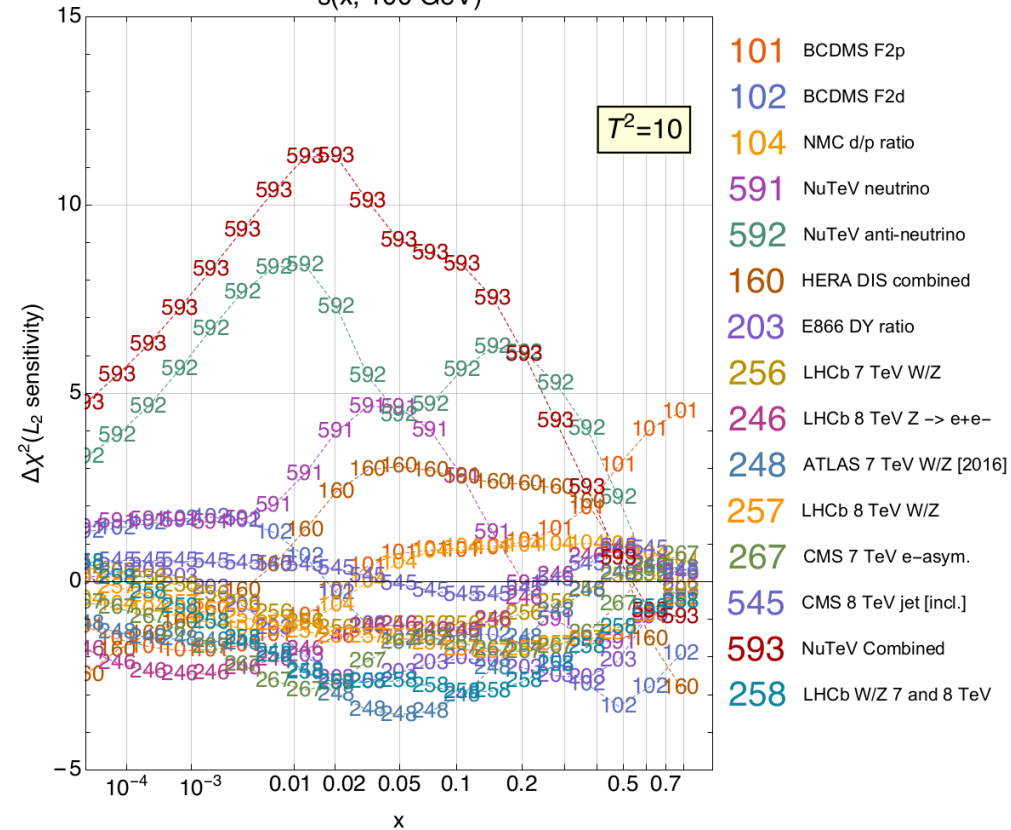
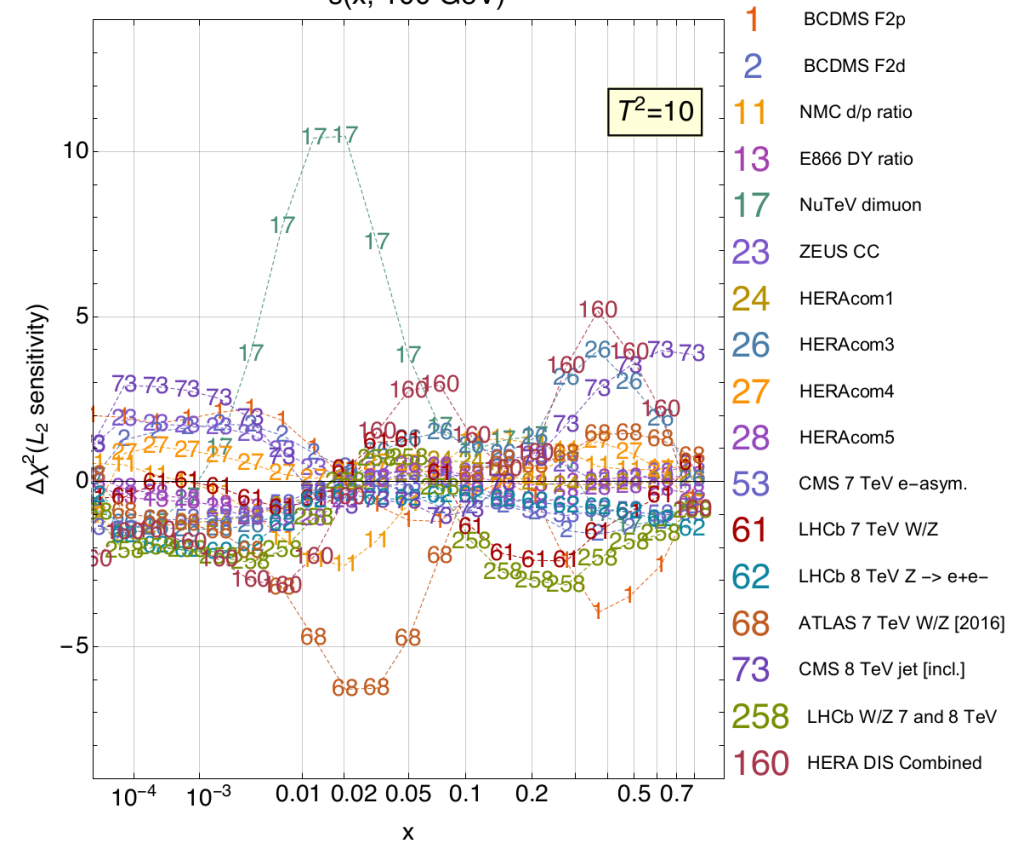


[again, see talk: T. Cridge]

- explored in PDF4LHC21 benchmarking studies, especially for *reduced* PDF fits

PDF4LHC21 benchmarking: 2203.05506, App. D

(common tolerance, theory choices)

MSHT20 reduced NNLO
s(x, 100 GeV)CT18 reduced NNLO
s(x, 100 GeV)

- dominant experiments exert qualitatively similar pulls on strangeness in CT, MSHT

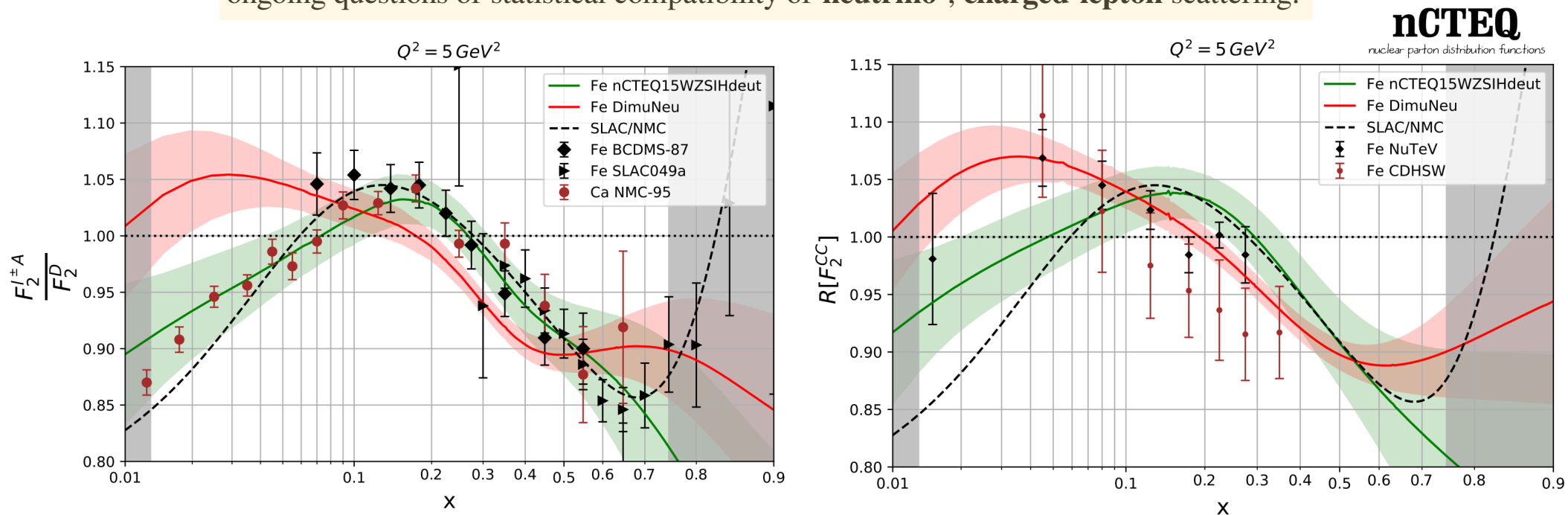
NuTeV neutrino scattering; 2016 ATLAS W/Z; HERA combined DIS data; ...

heavy-nuclear effects relevant for proton structure studies

- beyond few-body systems, CT, other analyses use heavy-nuclei for flavor separation
- requires knowledge of nuclear corrections; these directly fitted by nPDF analyses
 - better control over x , A dependence can benefit nucleon PDF extractions

[see talk: B. Ramson]

ongoing questions of statistical compatibility of **neutrino-**, **charged-lepton** scattering:



Muzakka, Duwentäster, TJH et al., 2204.13157

- more systematic studies of interdependence of nucleon, nuclear analyses needed
 - high- x PVDIS from proton, nuclei helpful to building this picture

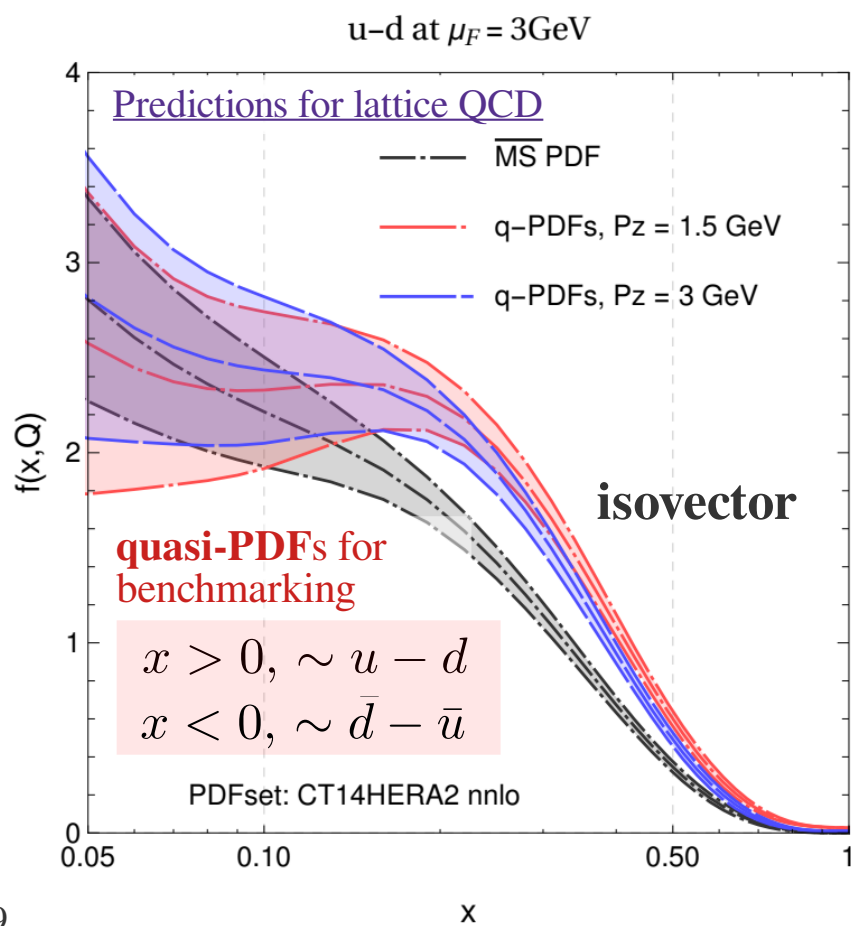
nonperturbative theory developments: lattice QCD inputs

- recent years: progress in *ab initio* hadron-structure calculations from LQCD
 - quasi-PDFs, pseudo-PDFs, quasi-TMDs, ...

there are be important synergies between PDF fitting and lattice QCD

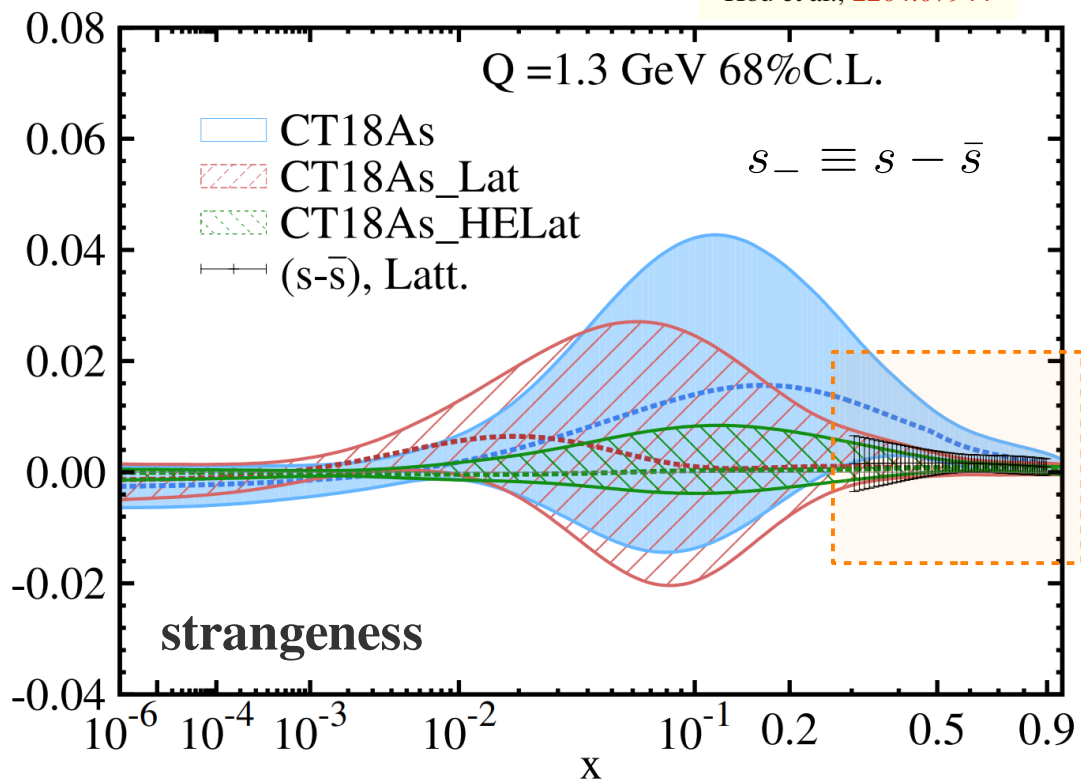
[overlaps with PVDIS]

TJH, Wang, Nadolsky, Olness, PRD100 (2019) 9, 094040

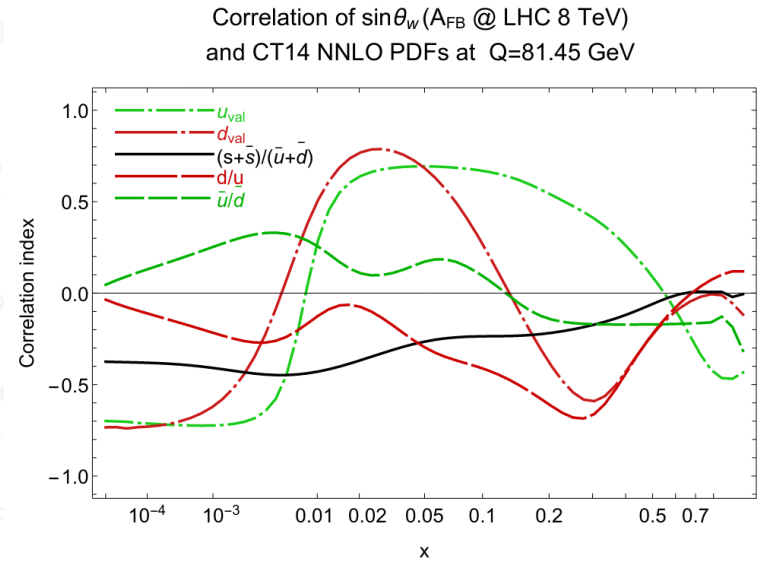


- lattice data can potentially inform high- x behavior of quark sea

Hou et al., 2204.07944



- have illustrated: PDF flavor dependence, including high x , is an HEP frontier



- array of (non)overlapping experiments with sensitivity
- PVDIS, JLab12 should have unique flavor access

- BUT: HEP-focused PDF analyses typically exclude very low Q^2 , high x
(in CT, standard cut of $W > 3.5$ GeV, $Q > 2$ GeV...)

- future impact studies, though challenging, may be helpful
- meanwhile, a few observations

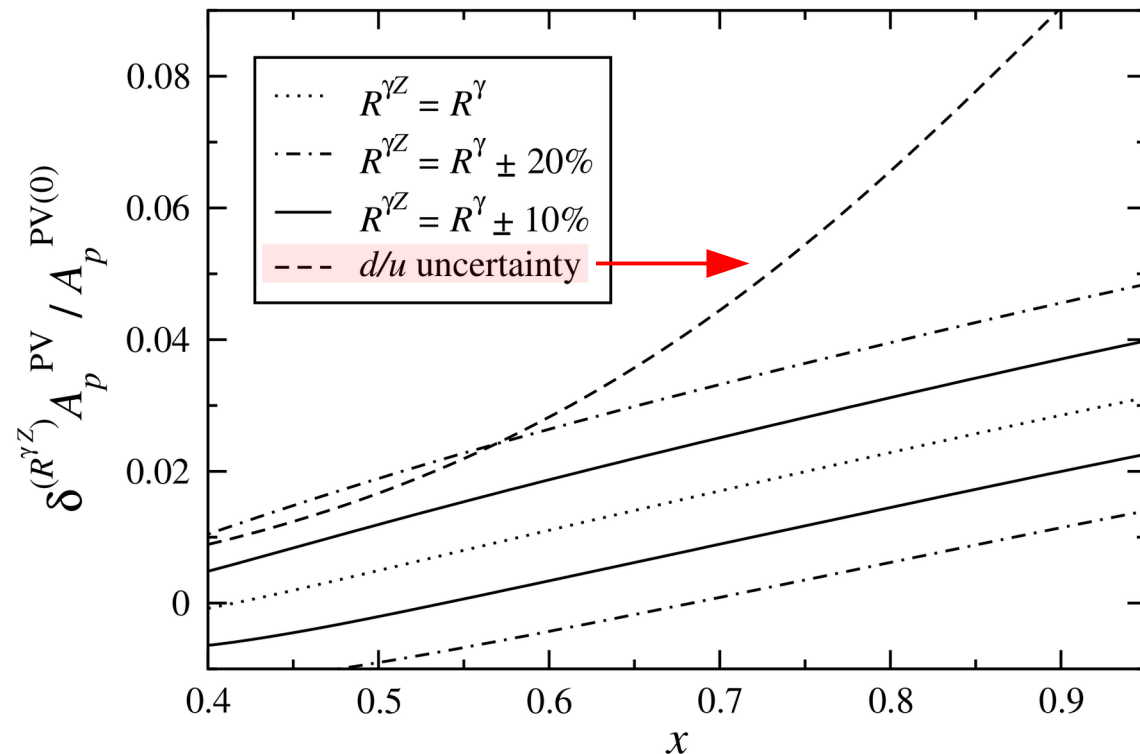
→ γ -Z interference accesses unique flavor currents in nucleon

$$A^{\text{PV}} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) \left[g_A^e Y_1 \frac{F_1^{\gamma Z}}{F_1^\gamma} + \frac{g_V^e}{2} Y_3 \frac{F_3^{\gamma Z}}{F_1^\gamma} \right] \quad A^{\text{PV}} \text{ potentially subject to finite-}Q^2 \text{ corrections}$$

$$Y_1 = \frac{1 + (1-y)^2 - y^2(1-r^2/(1+R^{\gamma Z})) - xyM/E}{1 + (1-y)^2 - y^2(1-r^2/(1+R^\gamma)) - xyM/E} \left(\frac{1+R^{\gamma Z}}{1+R^\gamma} \right) \quad R = \sigma_L/\sigma_T \neq 1$$

(= 1, Callan-Gross)

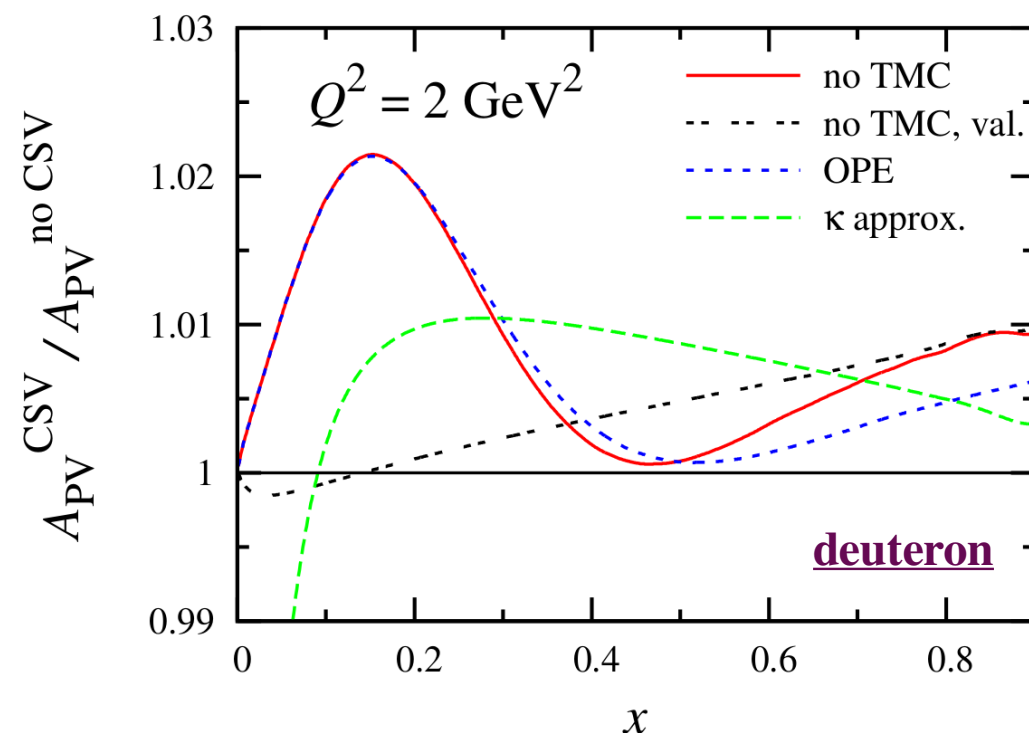
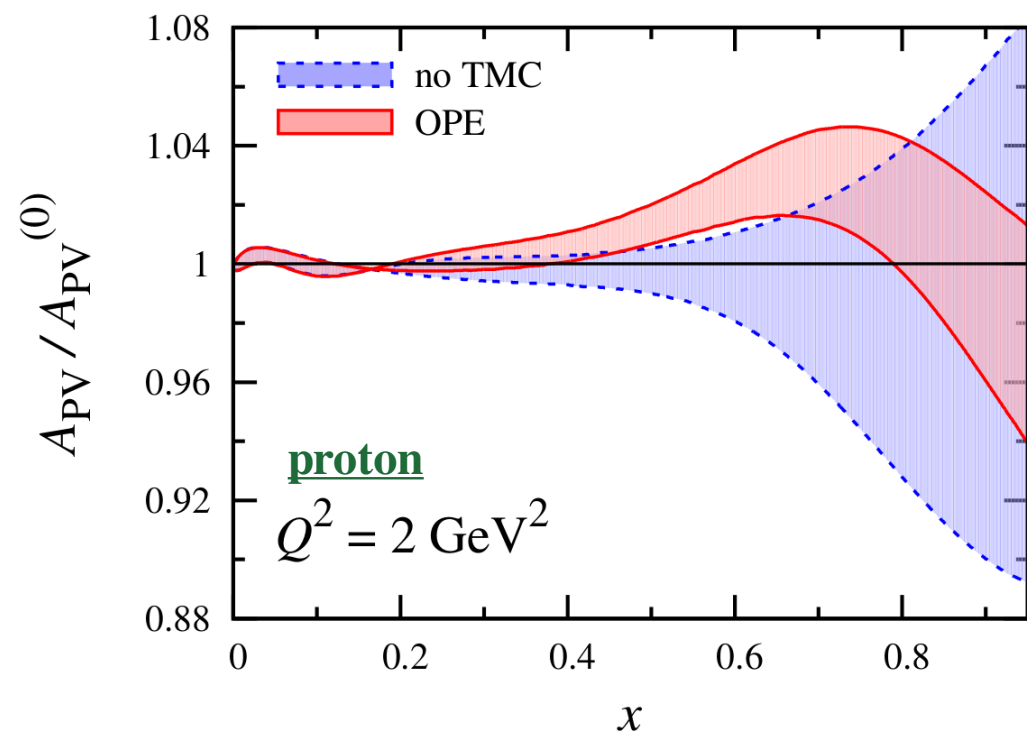
- in principle, could complicate PDF sensitivity of PV asymmetry
- effectively, proxy for various low- Q^2 corrections which must be investigated/controlled
- substantial theory, phenomenological progress over intervening years



Brady, Accardi, TJH, and Melnitchouk, PRD84, 074008 (2011)

- at lowest Q^2 , TMCs (and HTs) can represent multi-percent **proton** A^{PV} corrections

→ as precision effect, ~comparable to deuteron corrections shown earlier



- TMC prescription dependence mild; deuteron A^{PV} (mostly) insulated from effects

→ BSM, SMEFT analyses based on deuteron have much weaker PDF dependence

[see talk: K. Simsek]

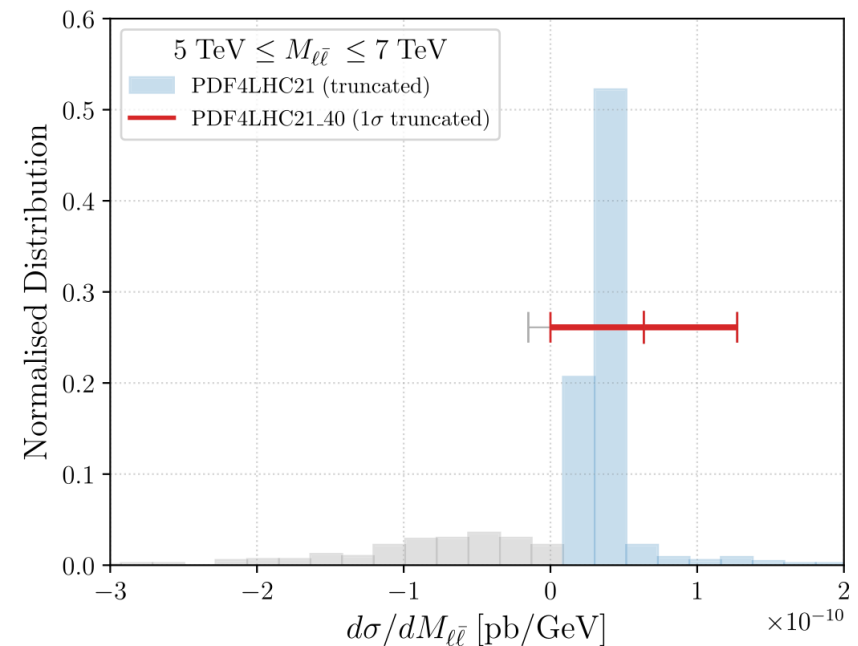
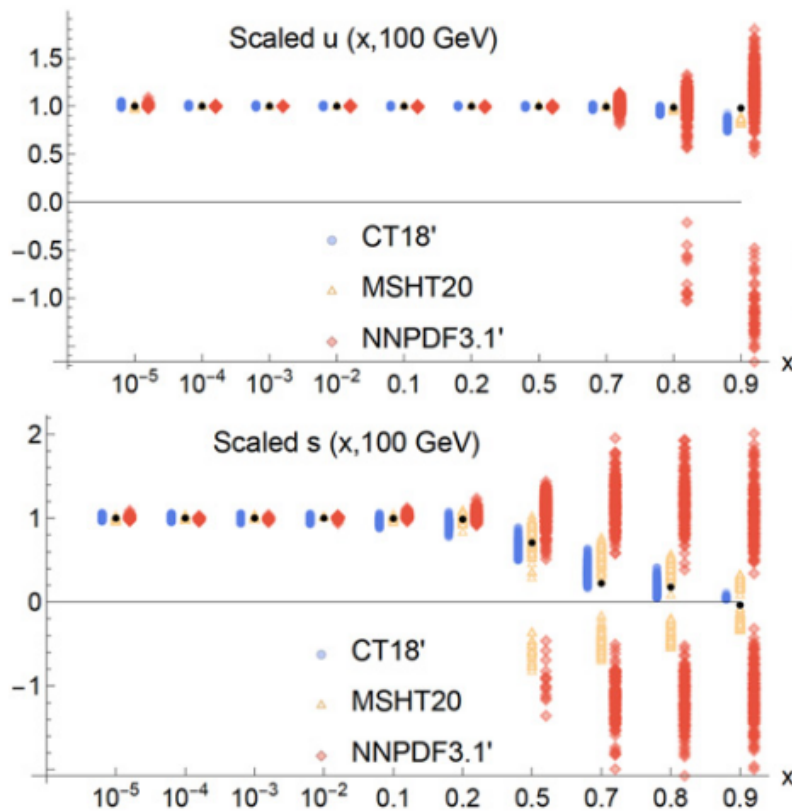
→ A^{PV} deuteron more sensitive to charge-symmetry violation (complement EIC)

→ TMCs more relevant for CSV; consequential for $\gamma(x)$, CT EW phenomenology

- MC sampling of high- x PDFs can sometimes produce irregularities

→ *e.g.*, positive-definiteness not always guaranteed for $x \rightarrow 1$

→ can produce subtle but non-negligible phenomenological consequences:



- high- x PVDIS data: perhaps explore PDF uncertainties with representative sampling

→ discriminating power

conclusions

- HEP analyses increasingly confront problem of taming high- x uncertainties
 - limit to EW precision, sensitivity of BSM tests
 - closely related to challenge of flavor separation
- QCD analysis progress: mix of theory corrections, pheno considerations
[higher-order QCD, EW; light, heavy nuclear effects; power-suppressed corrections; ...]
.....
- PVDIS, EW measurements at JLab12 hold intriguing possibilities
 - significant PDF (proton), BSM/EW (deuteron) sensitivity
 - extending HEP fits past kinematical cuts nontrivial but may be worthwhile

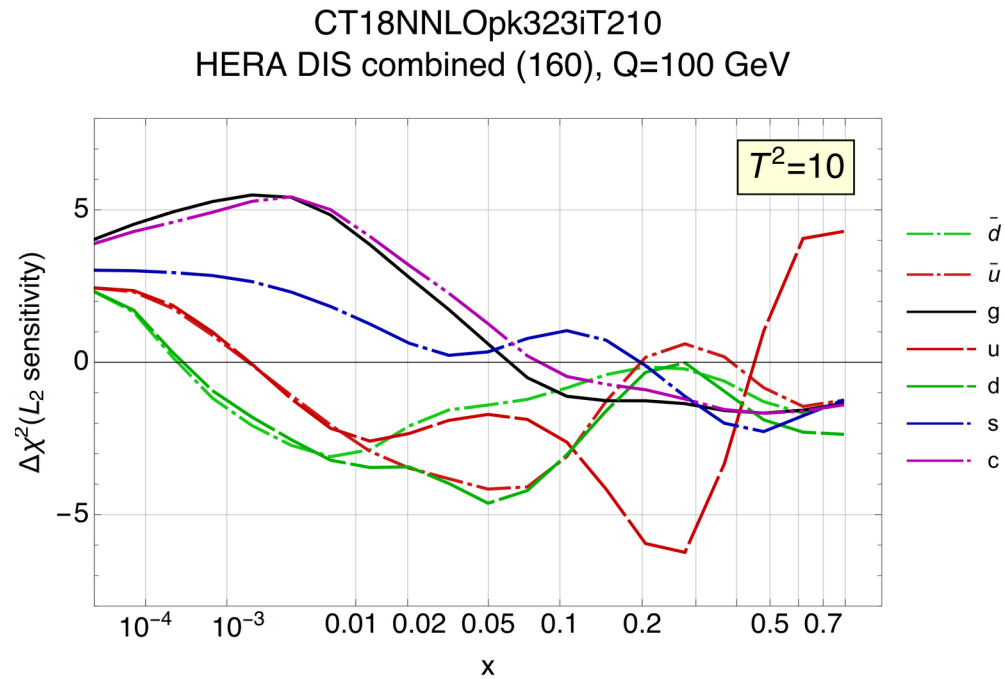
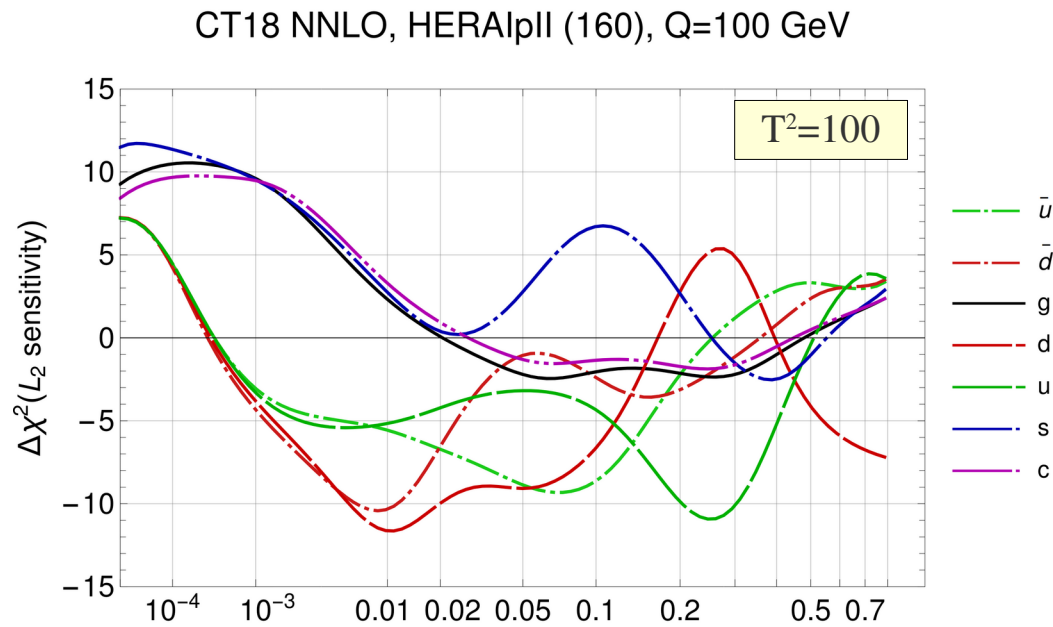
meanwhile, could play valuable benchmarking role

 - clear complementarity to EIC (both PV and positron) measurements

—— supplementary material ——

strangeness (and other) PDF pulls have modest tolerance dependence

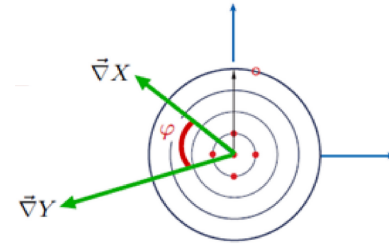
CT & MSHT groups, in preparation.



quantifying PDF preferences of fitted data: **the L_2 method**

$S_{f,L_2}(E)$: fast approximation of the Lagrange Multiplier scan of χ_E^2 along direction of $f_a(x_i, Q_q)$.

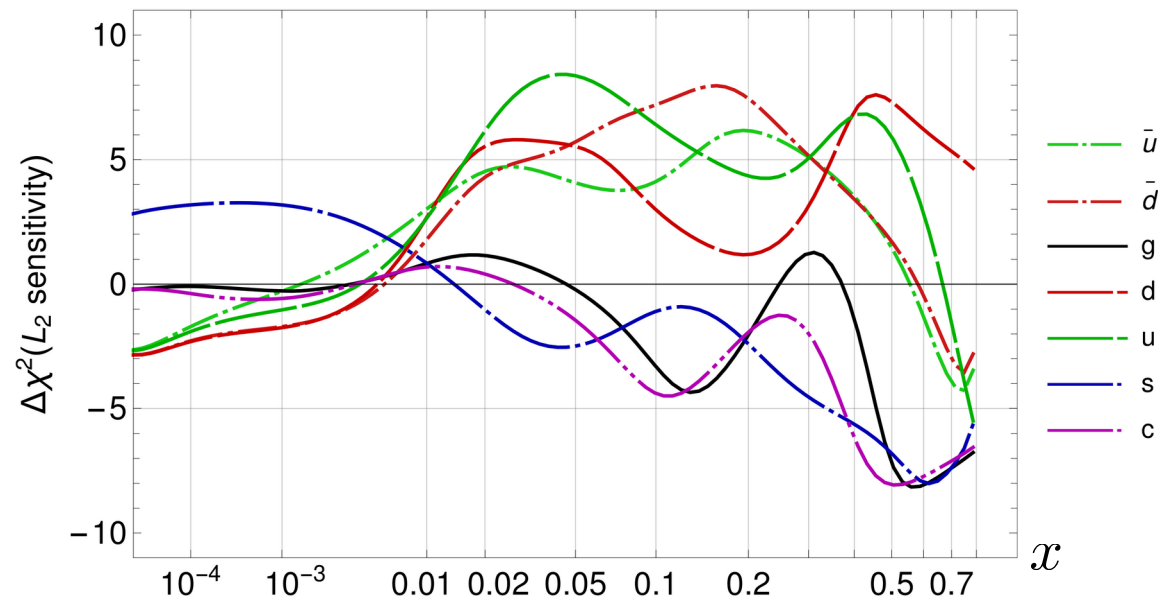
→ estimated $\Delta\chi_E^2$ for experiment E when $f_a(x_i, Q_i)$ increases by its +68% c.l. PDF uncertainty



$$Y = \chi_E^2 \quad X = f_a(x_i, Q_i) \quad S_{f,L_2} \equiv \Delta Y(\vec{z}_{m,X}) = \vec{\nabla} Y \cdot \vec{z}_{m,X}$$

$$= \vec{\nabla} Y \cdot \frac{\vec{\nabla} X}{|\vec{\nabla} X|} = \Delta Y \cos \varphi$$

CT18 NNLO, BcdF2dCor (102), Q=2 GeV



→ extension of L_1 sensitivity (PDFSense) method used to explore

- HEP data pulls for CT18
Phys.Rev.D 103 (2021) 1, 014013
- PDF-Lattice sensitivities
Phys.Rev.D 100 (2019) 9, 094040
- EIC potential
EIC YR, arXiv: 2103.05419

flavor structure only from inclusive data is challenging!

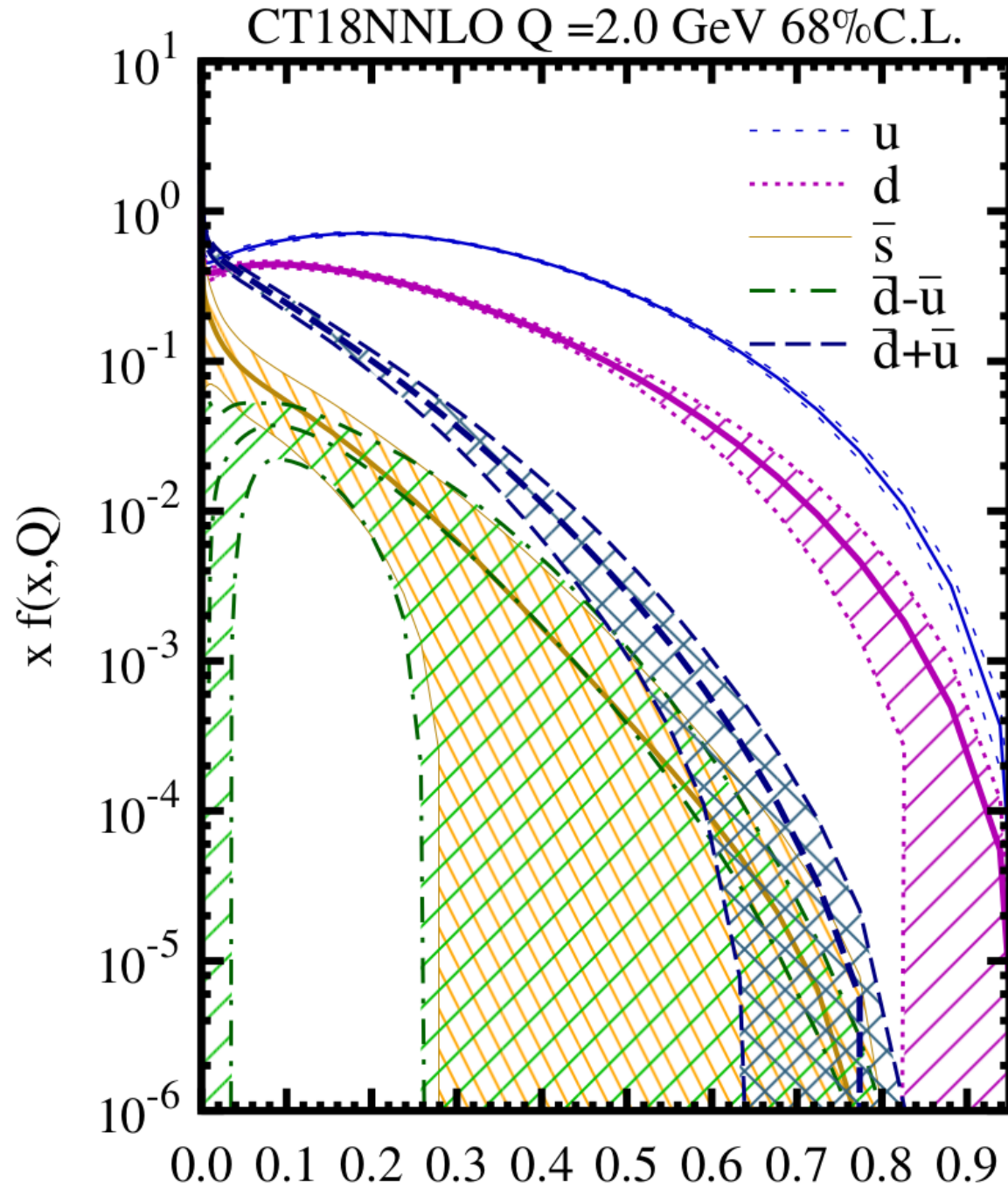


Figure: S. Dulat

note PDFs' different orders-of-mag.!

NC DIS: sensitivity to d -type quarks $\frac{1}{4}$ that of u -type

$$\sigma \propto \frac{4}{9}(u_+ + c_+) + \frac{1}{9}(d_+ + s_+ + b_+)$$

CC DIS: lower accuracy (1/10 lumi.)

→ u -quark dominates

→ d -quark $\frac{1}{2}$ of u , but harder to access in NC DIS (above)

→ $\bar{d} + \bar{u} \sim$ few percent of u

→ for $x \sim 0.1$,
 $s \approx \bar{s} \approx \bar{d} - \bar{u} < 0.1(\bar{d} + \bar{u})$

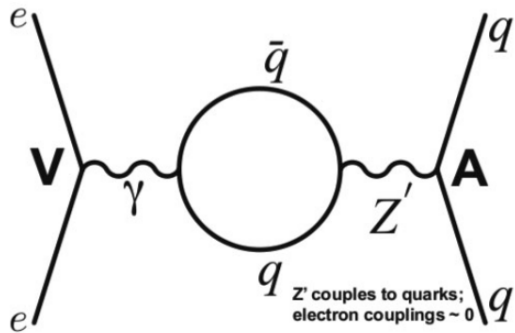
→ at $x > 0.5$, no separation for $\bar{u}, \bar{d}, \bar{s}$

the electroweak sector and **New Physics** searches at EIC

- if measured to sufficient precision, the quark-level electroweak couplings may be sensitive to an extended EW sector, e.g., Z'

$$\mathcal{L}^{\text{PV}} = \frac{G_F}{\sqrt{2}} \left[\bar{e} \gamma^\mu \gamma_5 e \left(C_{1u} \bar{u} \gamma_\mu u + C_{1d} \bar{d} \gamma_\mu d \right) + \bar{e} \gamma^\mu e \left(C_{2u} \bar{u} \gamma_\mu \gamma_5 u + C_{2d} \bar{d} \gamma_\mu \gamma_5 d \right) \right]$$

$$C_{1u} = -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W$$



- a unique strength of an EIC is its combination of very high precision and **beam polarization**, which allows the observation of **parity-violating helicity asymmetries**:

$$A^{\text{PV}} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \quad (\text{R/L : } e^- \text{ beam helicities})$$

selects γ - Z interference diagrams!

TJH and Melnitchouk, PRD77, 114023 (2008).

$$A^{\text{PV}} = - \left(\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) (Y_1 a_1 + Y_3 a_3)$$

$$a_1 = \frac{2 \sum_q e_q C_{1q} (q + \bar{q})}{\sum_q e_q^2 (q + \bar{q})}$$

$$a_3 = \frac{2 \sum_q e_q C_{2q} (q - \bar{q})}{\sum_q e_q^2 (q + \bar{q})}$$

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$$C_{1u} = -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W$$

→ with sufficient precision, an EIC (which will be statistics-limited in these measurements) can extract $\sin^2 \theta_W$

- this measurement is potentially sensitive to the TeV-scale in a complementary fashion to energy-frontier searches!

TJH and Melnitchouk, PRD77, 114023 (2008).

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N.B.: extractions are dependent upon knowledge of the PDFs