

Running of the Weak Mixing Angle

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Jefferson Lab

Electroweak and Beyond the Standard Model Physics at the EIC

INT, WU - Feb 12-16 2024

Outline

- **Definition**
- **Running**
- **Past measurements**
 - **Z-pole measurements**
 - **Low-energy ($Q^2 \ll M_Z^2$) measurements**
- **Potential future measurements**
- **Summary**

Acknowledgement: KK and Ciprian for providing slides and guidance

Weak Mixing angle - fundamental quantity of EW theory



EM force

Infinite-range
Massless mediator
Conserve parity



EW force

Having massive and
massless mediator

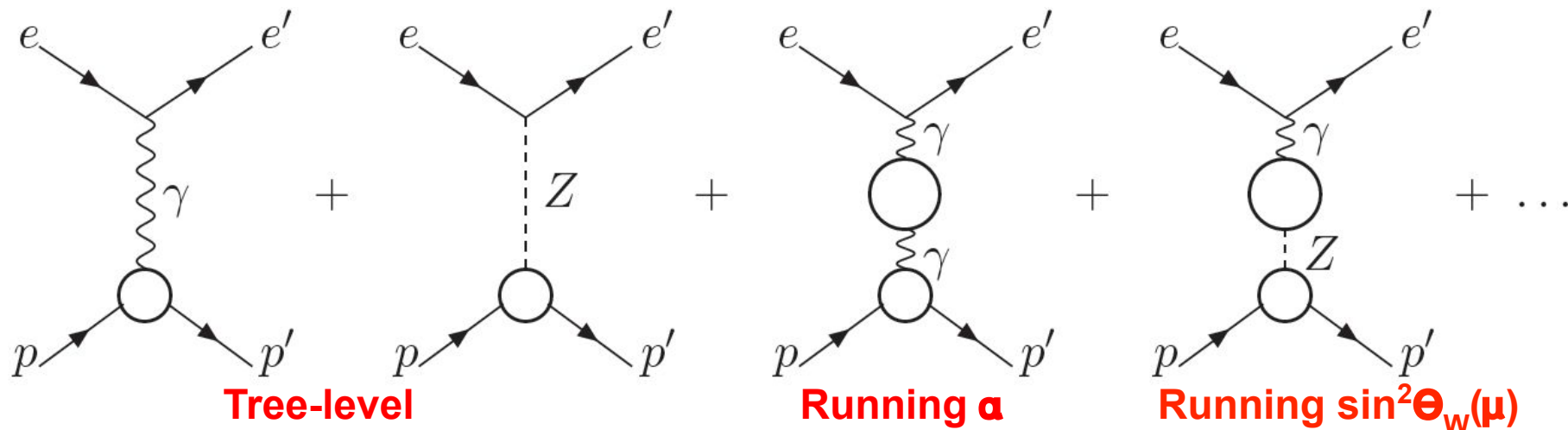


Weak force

Short range
Massive mediator
Violate Parity

$$\sin^2 \theta_w = 1 - (M_W / M_Z)^2 = (e/g)^2$$

Quantum corrections



Universal quantum corrections can be absorbed into a scale dependent - “running” $\sin^2\Theta_W(\mu)$



Schemes of Definition

- On-shell scheme

- promotes Tree-level definition to a renormalized $\sin^2\Theta_W(\mu)$ to all orders in perturbation theory

$$\sin^2\theta_W \rightarrow s_W^2 \equiv 1 - M_W^2/M_Z^2$$

$$M_W = \frac{A_0}{s_W(1-\Delta r)^{1/2}}; M_Z = \frac{M_W}{c_W}$$

$$\Delta r \approx \Delta r_0 - \rho_t / \tan^2\theta_w$$

$$\Delta r_0 = 1 - \alpha / \hat{\alpha}(M_Z)$$

$$\rho_t = 3G_F m_t^2 / 8\sqrt{2}\pi^2$$

- Simple conceptually - relatively large ($\sim 3\%$) correction from ρ_t causes large spurious contributions in higher orders.

Schemes of Definition

- Modified Minimal Subtraction

- Scale dependent scaling - choose $\mu = M_Z$ for many EW processes
- Less sensitive to mt and new physics.

$$\sin^2 \hat{\theta}_W(\mu) \equiv \frac{\hat{g}'^2(\mu)}{\hat{g}^2(\mu) + \hat{g}'^2(\mu)}$$

- Theoretically nice - but unphysical
- Good for GUT running

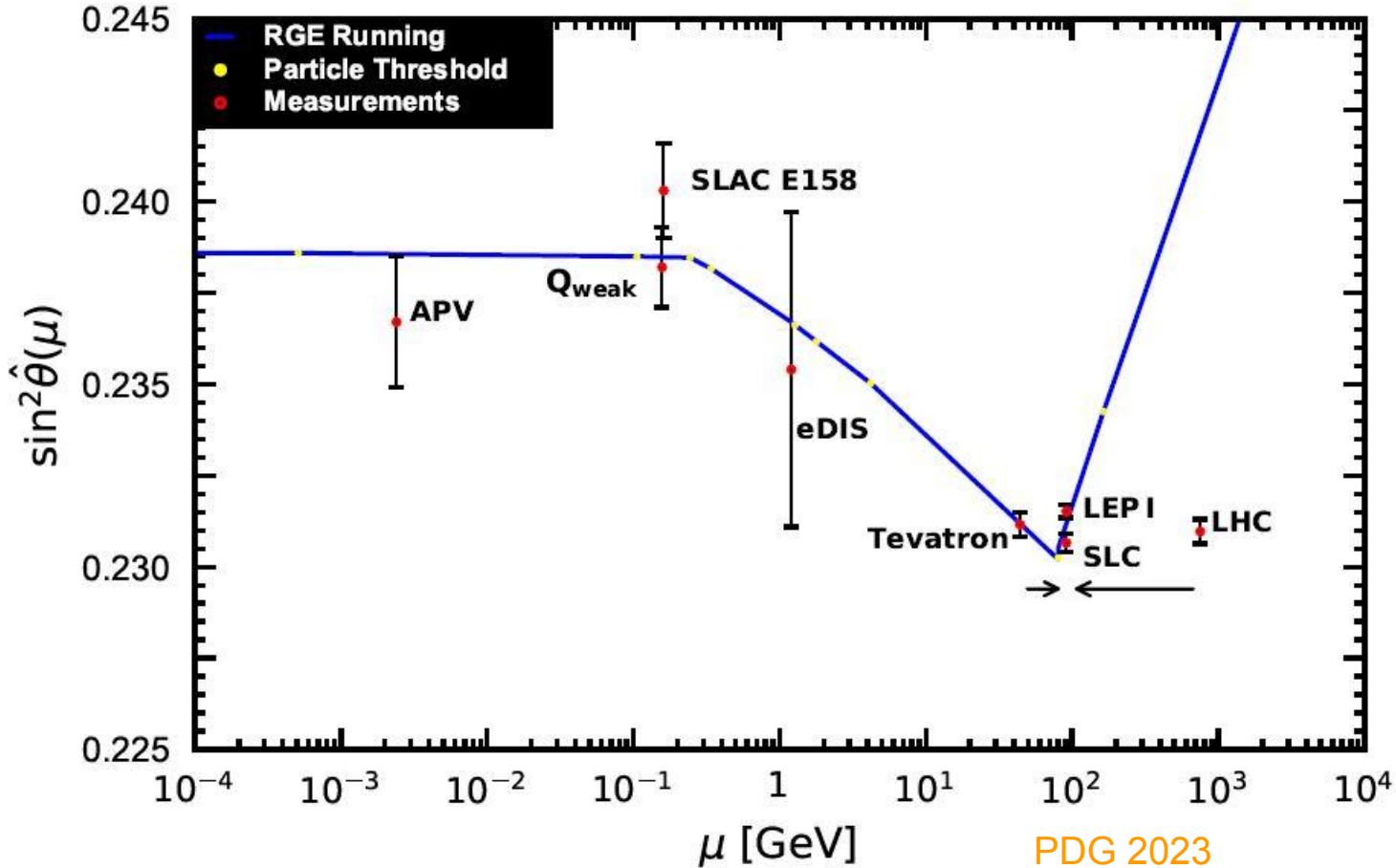
- Effective

- Extensively used at LEP - defined by vector and axial vector couplings at the Z-pole - $Zf\bar{f}$
- Good at Z-pole
- Required to calculate renormalized counterterms for non-Z-pole applications

$$\sin^2 \theta_f^{eff} \equiv \kappa_f(q^2, \mu) \sin^2 \hat{\theta}_W(\mu)$$

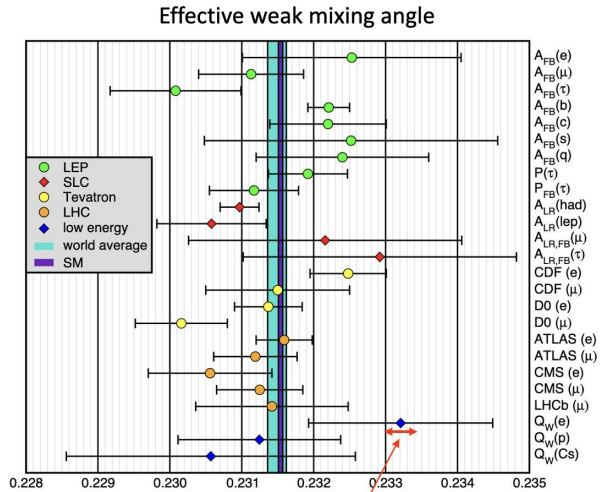
$$\sin^2 \hat{\theta}_W(M_Z) - \sin^2 \theta_f^{eff} = 0.00028$$

Existing Measurements

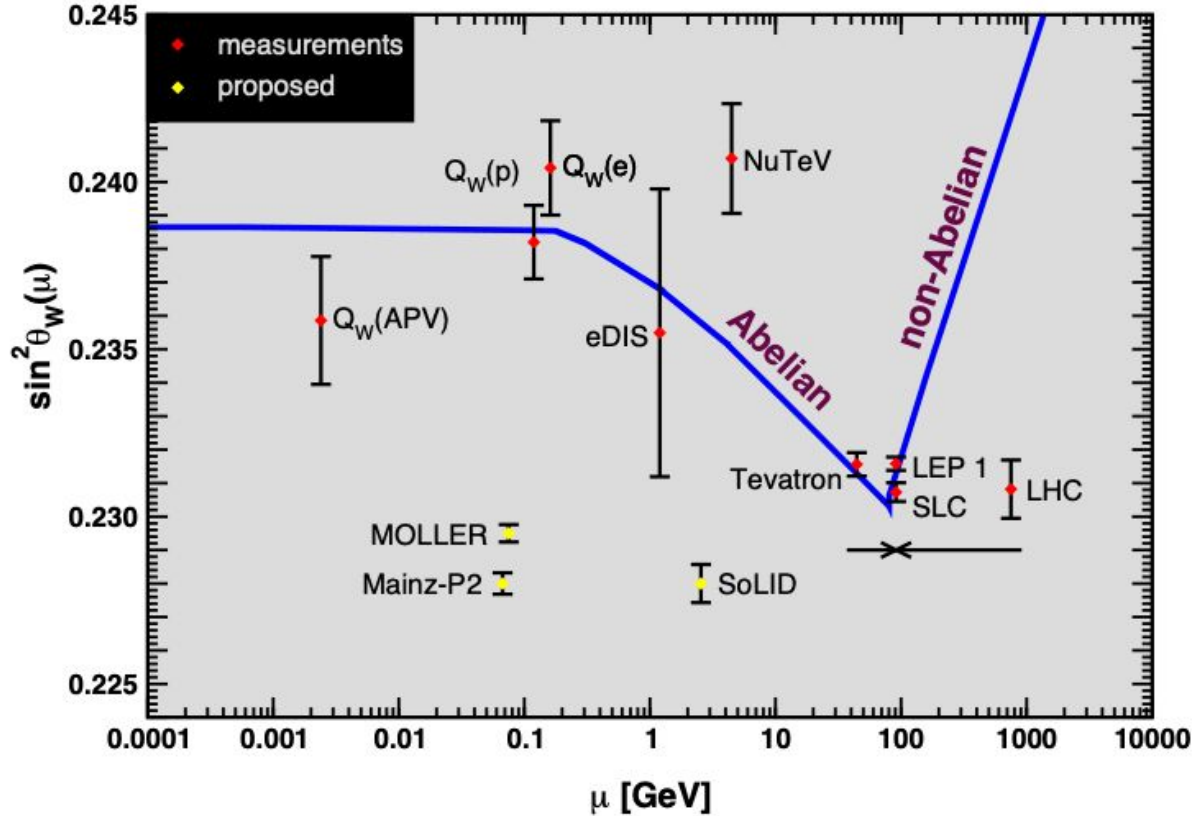


Future Measurements

- Clearly points out the precision of the future experiments: **P2** and **MOLLER** - to the level of Z-pole measurements!

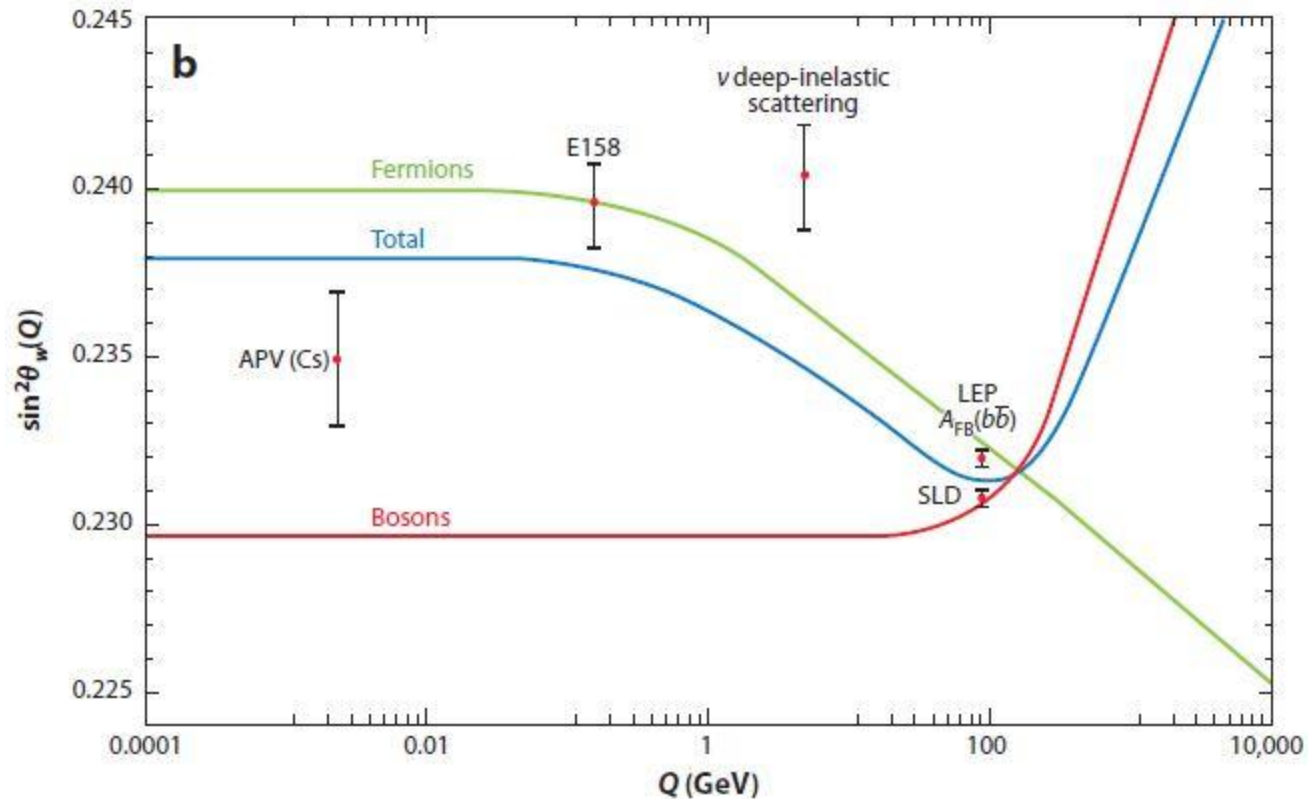


MOLLER expected precision

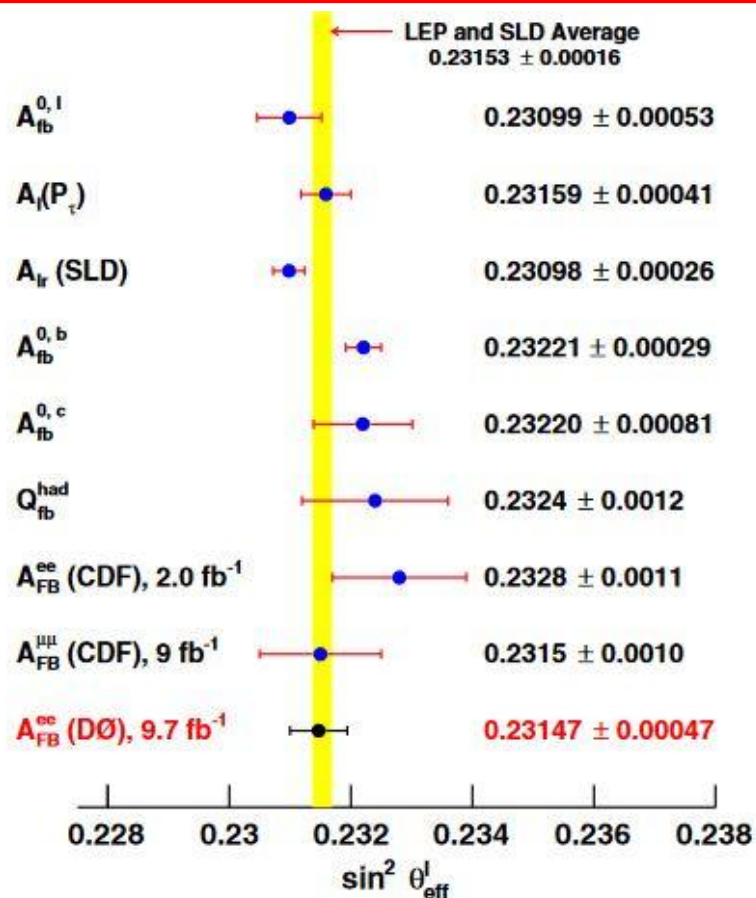


Running - fermionic and bosonic contributions

Annu. Rev. Nucl. Part. Sci. 63 237 (2013)



Z-pole measurements -CERN, SLAC, FermiLab



$$p\bar{p}/e\bar{e} \rightarrow Z \rightarrow q\bar{q}/l\bar{l}$$

Used left-right, forward-backward asymmetry of quark/leptons, polarization state of τ lepton

The two most precision measurements differ by 3.2σ .

PRL 115 041801 (2015)

Low Energy Measurements

$(Q^2 \ll M_Z^2)$

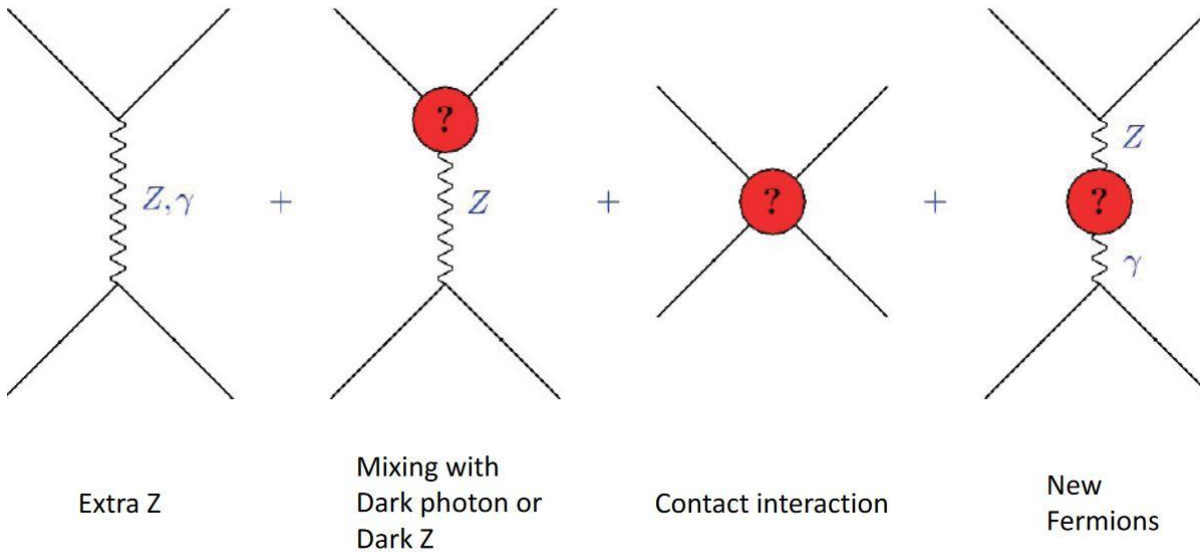
Sensitivity to new physics beyond the Standard Model

Unravelling “New Dynamics” in the Early Universe:

how did nuclear matter form and evolve?

BSM: Symmetry violation with Electrons

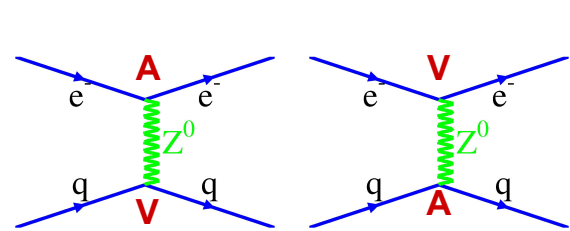
- Lepton number
- Time reversal symmetry
- Charged Lepton Flavor
- **Parity violation with Flavor conservation**



Look for tiny but measurable deviations from precisely calculable predictions from SM process

Observed PV: (SM+BSM) effect

Weak Neutral Current (WNC) Couplings



$$C_{1i} \equiv 2g_A^e g_V^i$$

$$C_{2i} \equiv 2g_V^e g_A^i$$

$$L^{PV} = \frac{G_F}{\sqrt{2}} [\bar{e}\gamma^\mu \gamma_5 e (C_{1u} \bar{u}\gamma_\mu u + C_{1d} \bar{d}\gamma_\mu d) + \bar{e}\gamma^\mu e (C_{2u} \bar{u}\gamma_\mu \gamma_5 u + C_{2d} \bar{d}\gamma_\mu \gamma_5 d)] + C_{ee} (e\gamma^\mu \gamma_5 e \bar{e}\gamma_\mu e)$$

SM relations

| | | |
|----------|--|-----------------|
| C_{1u} | $= -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W$ | ≈ -0.19 |
| C_{1d} | $= \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W$ | ≈ 0.35 |
| C_{2u} | $= -\frac{1}{2} + 2 \sin^2 \theta_W$ | ≈ -0.04 |
| C_{2d} | $= \frac{1}{2} - 2 \sin^2 \theta_W$ | ≈ 0.04 |

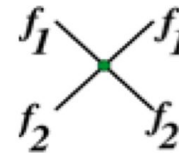
Precision weak-mixing angle measurements: limits on the couplings

$$C_{1q} \propto (g_{RR}^{eq})^2 + (g_{RL}^{eq})^2 - (g_{LR}^{eq})^2 - (g_{LL}^{eq})^2$$

$$C_{2q} \propto (g_{RR}^{eq})^2 - (g_{RL}^{eq})^2 + (g_{LR}^{eq})^2 - (g_{LL}^{eq})^2$$

$$C_{ee} \propto (g_{RR}^{ee})^2 - (g_{LL}^{ee})^2$$

+ New Physics

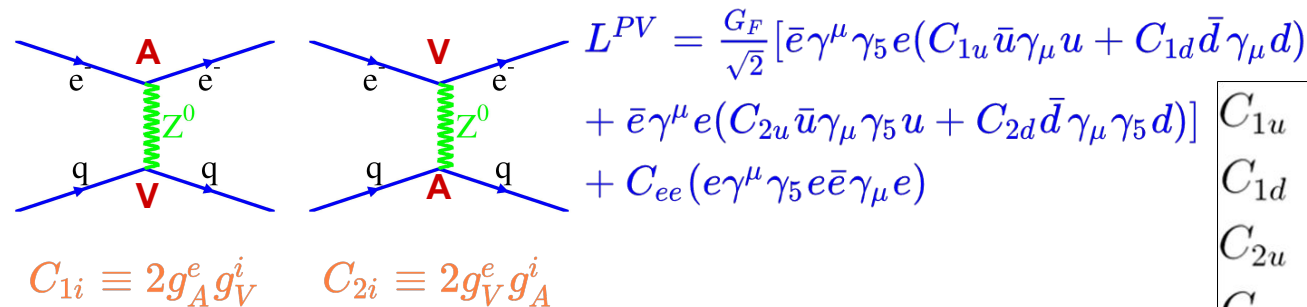


$$L_{eff} = \frac{(g_{ij}^{12})^2}{(1+\delta)\Lambda^2} \sum_{i,j=L,R} \bar{f}_{1i} \gamma_\mu f_{1i} \bar{f}_{2i} \gamma^\mu f_{2j}$$

g - strength of the interaction

Λ - Scale of the new dynamics

Weak Neutral Current (WNC) Couplings



$$\begin{aligned}
 L^{PV} = & \frac{G_F}{\sqrt{2}} [\bar{e}\gamma^\mu \gamma_5 e (C_{1u} \bar{u}\gamma_\mu u + C_{1d} \bar{d}\gamma_\mu d) \\
 & + \bar{e}\gamma^\mu e (C_{2u} \bar{u}\gamma_\mu \gamma_5 u + C_{2d} \bar{d}\gamma_\mu \gamma_5 d)] \\
 & + C_{ee} (e\gamma^\mu \gamma_5 e \bar{e}\gamma_\mu e)
 \end{aligned}$$

| | | | | |
|----------|-----|--|-----------|---------|
| C_{1u} | $=$ | $-\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W$ | \approx | -0.19 |
| C_{1d} | $=$ | $\frac{1}{2} - \frac{2}{3} \sin^2 \theta_W$ | \approx | 0.35 |
| C_{2u} | $=$ | $-\frac{1}{2} + 2 \sin^2 \theta_W$ | \approx | -0.04 |
| C_{2d} | $=$ | $\frac{1}{2} - 2 \sin^2 \theta_W$ | \approx | 0.04 |

$$C_{1q} \propto (g_{RR}^{eq})^2 + (g_{RL}^{eq})^2 - (g_{LR}^{eq})^2 - (g_{LL}^{eq})^2 \longrightarrow \text{Atomic parity violation, PV elastic e-N Scattering}$$

$$C_{2q} \propto (g_{RR}^{eq})^2 - (g_{RL}^{eq})^2 + (g_{LR}^{eq})^2 - (g_{LL}^{eq})^2 \longrightarrow \text{PV deep inelastic scattering}$$

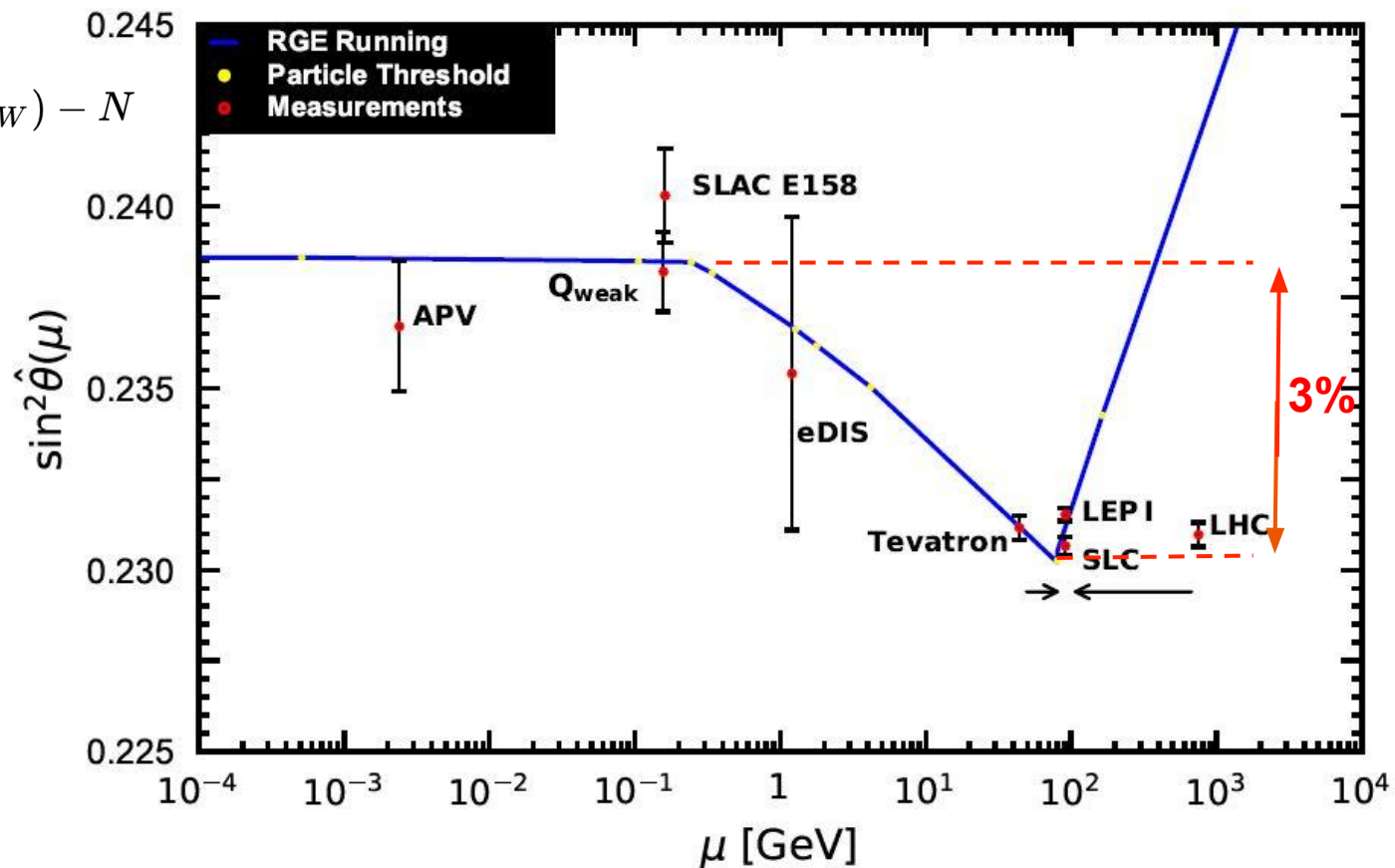
$$C_{ee} \propto (g_{RR}^{ee})^2 - (g_{LL}^{ee})^2 \longrightarrow \text{PV Moller scattering}$$

Why low-energy ($Q^2 \ll M_Z^2$) measurements for the BSM search??

$$Q_W(Z, N) = Z(1 - 4\sin^2\theta_W) - N$$

A 3% shift in $\sin^2\theta_W$ would imply 40% shift of $1-4\sin^2\theta_W$

Reduce the sensitivity of experimental uncertainty to the extracted quantity

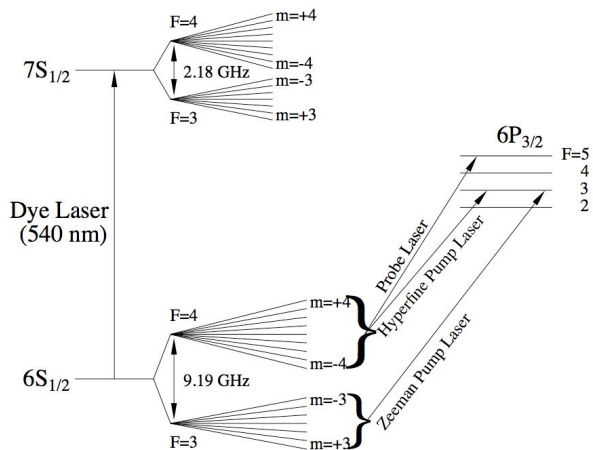


PDG 2023

**Existing Measurements:
Atomic Parity Violation: ^{133}Cs**

Atomic Parity Violation at Q=2.4 MeV

Partial Level Structure of Cs



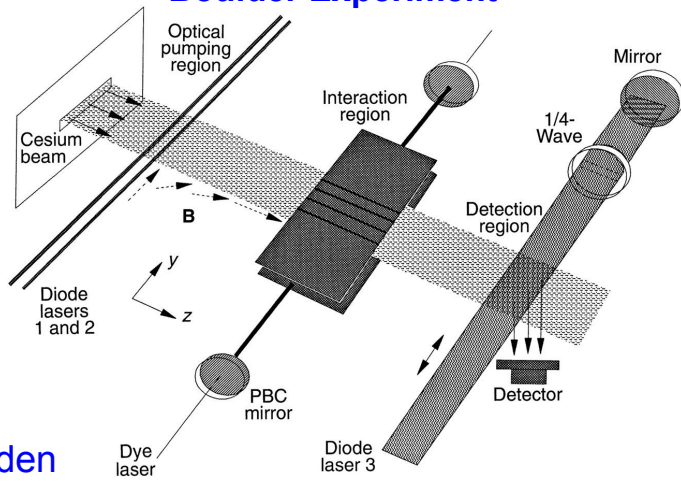
- $6S \rightarrow 7S$ transition in ^{133}Cs is forbidden
- Weak charge - mixes S and P states
- Induced an E1 Stark transitions - measure the modulation of E1-PV interference

$$\text{Im}(E1_{\text{PNC}})/\beta = 1.5935(56) \text{ mV/cm}$$

$$Q_W = \left(\frac{E1_{\text{PNC}}/\beta}{M_{hf}/\beta} \right) \left(\frac{NM_{hf}}{k_{\text{PNC}}} \right)$$

$$Q_W(Z, N) = Z(1 - 4\sin^2\theta_W) - N$$

Boulder Experiment



k_{PNC}

Atomic Theory

$$0.9065(36) \times 10^{-11} e a_0 - 1999$$

$$0.8906(26) \times 10^{-11} e a_0 - 2010$$

$$0.8977(40) \times 10^{-11} e a_0 - 2012$$

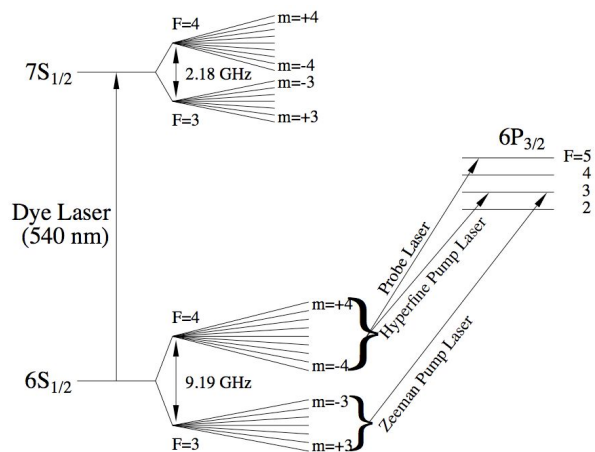
$$\sin^2 \hat{\theta}_W(M_Z) = 0.2283(20)$$

$$\frac{\delta(\sin^2 \hat{\theta}_W)}{\sin^2 \hat{\theta}_W} \sim 0.9\%$$

BSM mass sensitivity 9.9 TeV

Atomic Parity Violation Q=2.4 MeV

Partial Level Structure of Cs



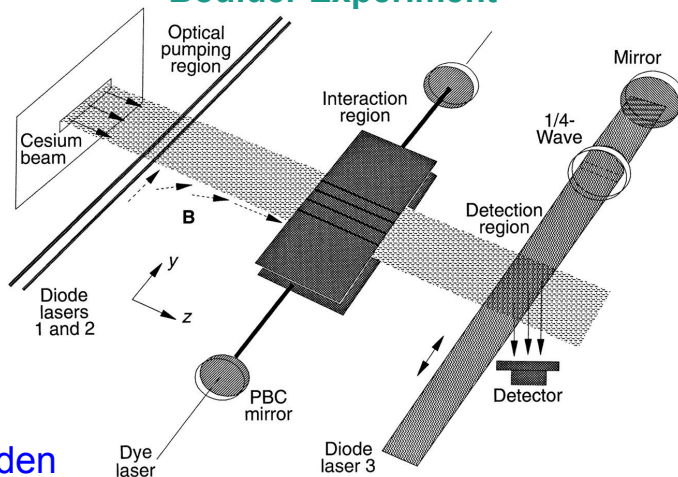
- 6S \rightarrow 7S transition in ^{133}Cs is forbidden
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$$\text{Im}(E1_{PNC})/\beta = 1.5935(56) \text{ mV/cm}$$

$$Q_W = \left(\frac{E1_{PNC}/\beta}{M_{hf}/\beta} \right) \left(\frac{NM_{hf}}{k_{PNC}} \right)$$

$$Q_W(Z, N) = Z(1 - 4\sin^2\theta_W) - N$$

Boulder Experiment



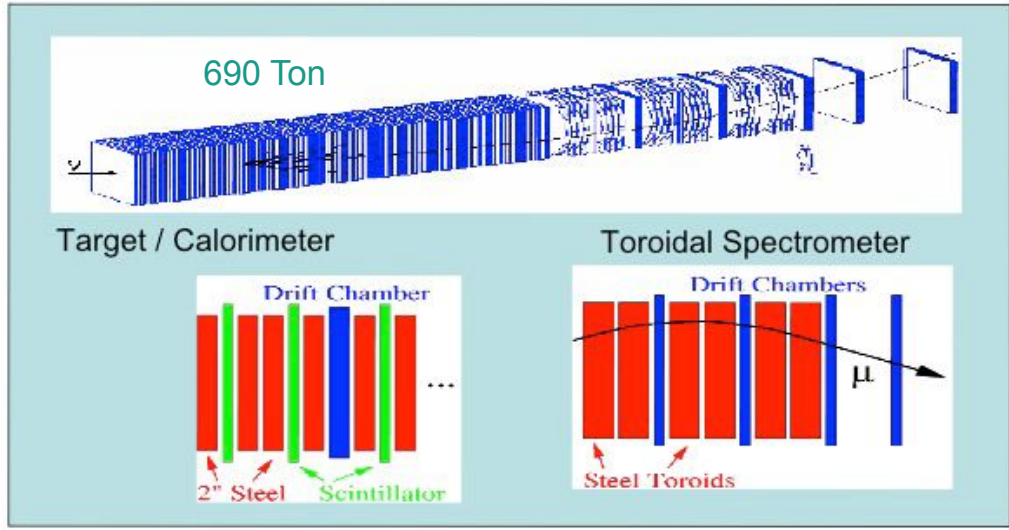
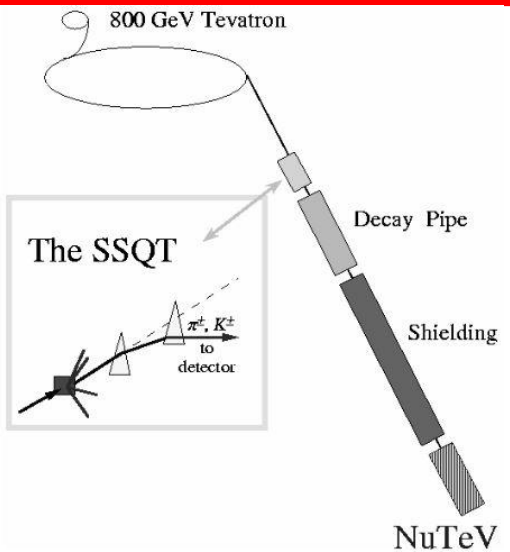
New development

- TRIUMF - Francium
- KVI - Ra+
- PREX/CREX results
- Theory - measurement on isotopic chain

$$\frac{\delta(\sin^2\hat{\theta}_W)}{\sin^2\hat{\theta}_W} \sim 0.9\%$$

BSM mass sensitivity 9.9 TeV

NuTeV@ 4.47 GeV



- 800 GeV p at FNAL produce pi, K from interactions in BeO target;
- Decay of charged pi, K produces neutrinos, antineutrinos;
- Almost pure muon neutrinos;
- Only neutrinos penetrate shielding
- Dipoles select sign of charged meson:
- Determine nu/nubar type

$$R^- = \frac{\sigma_{\nu N}^{NC} - \sigma_{\bar{\nu} N}^{NC}}{\sigma_{\nu N}^{CC} - \sigma_{\bar{\nu} N}^{CC}} \approx \rho^2 \left(\frac{1}{2} - \sin^2 \theta_W \right)$$

$$\sin^2 \theta_W^{(on-shell)} = 0.2277 \pm 0.0013(stat.) \pm 0.0009(syst.)$$

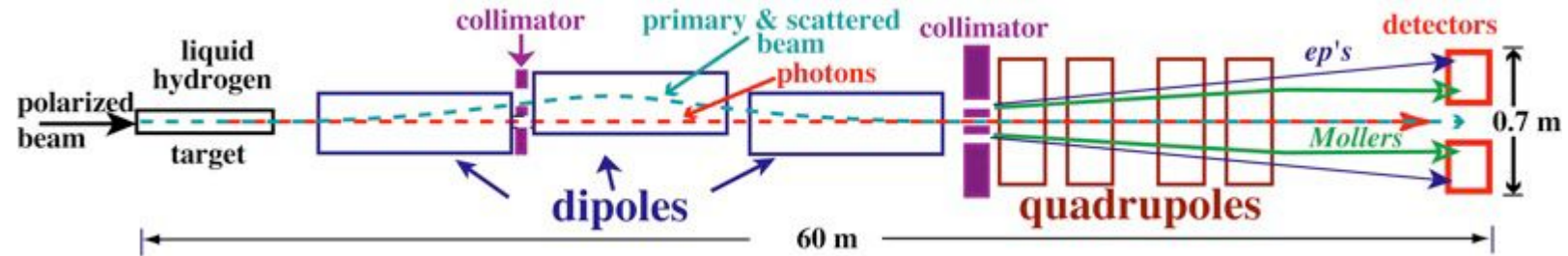
Standard Model prediction is 0.2227 (3σ deviation)

Physics Letters B 693 (2010) 462–466
Charge symmetry violation + s \bar{s}

PRL 88 091802 (2002)

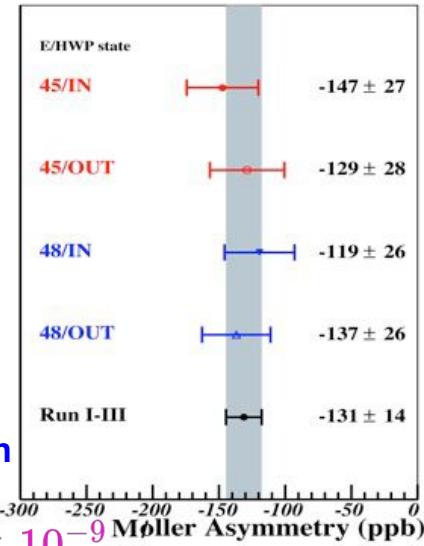
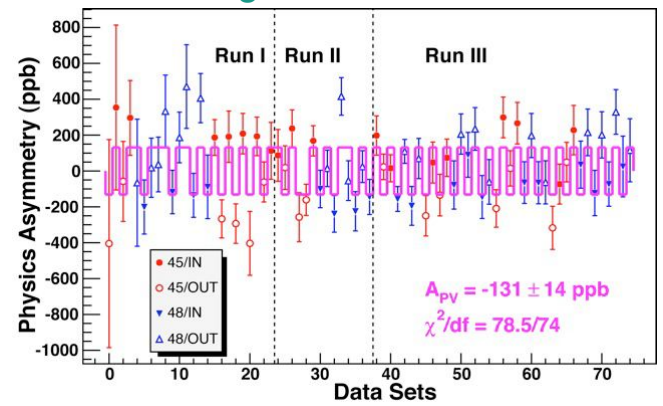
C_{ee}
The purely leptonic interaction

SLAC E158 2002-2003



45/48 GeV Beam
85% long. Polarization

PRL 95 081601 (2005)



Slow reversal: IHWP, (g-2) precession

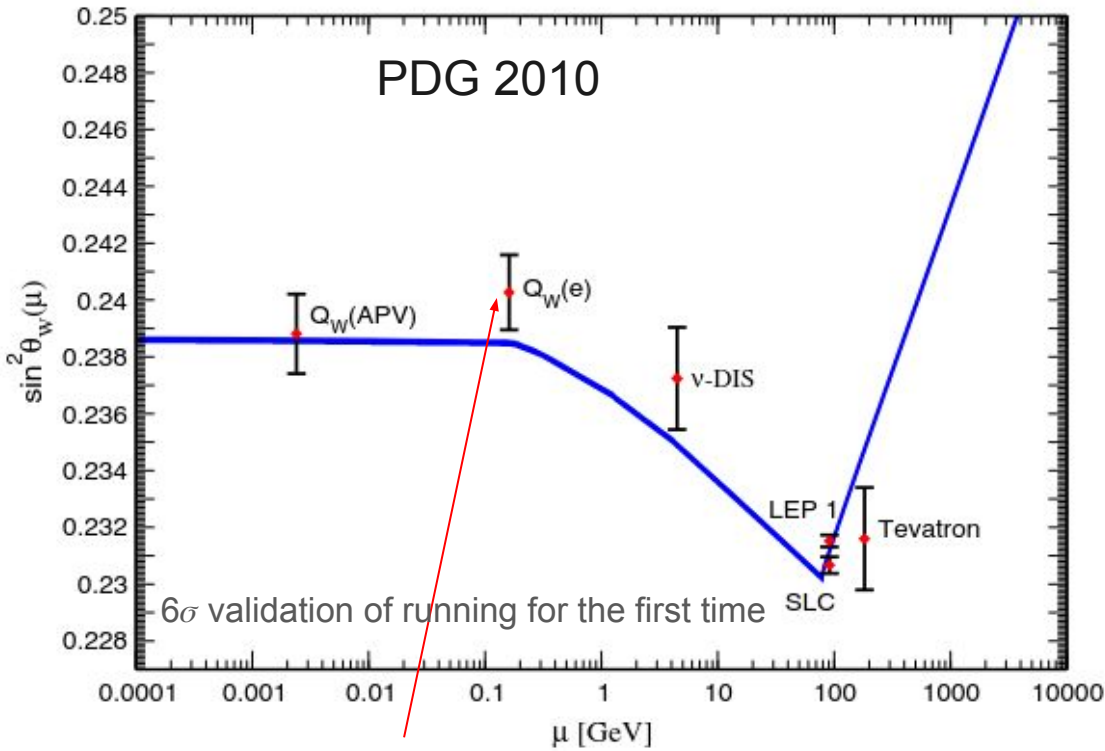
Technical challenges overcome: 10 nm beam position control, Max. beam current limit, Radiation dose, high rates

$$A_{PV} = (131 \pm 14 \pm 10) \times 10^{-9}$$

SLAC E158 -Results @ Q = 161 MeV

$$A_{PV} = (131 \pm 14 \pm 10) \times 10^{-9}$$

$$\sin^2 \hat{\theta}_W(M_Z) = 0.2330 \pm 0.0011(stat) \pm 0.0009(syst.) \pm 0.0006(theo.)$$



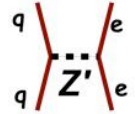
MOLLER: 5x improvement

- Statistics limited
- Theory unct. under control.

$$LEP II \quad \left| \begin{matrix} e & e \\ R & R \\ e & e \end{matrix} \right|^2 + \left| \begin{matrix} e & e \\ L & L \\ e & e \end{matrix} \right|^2$$

17 TeV

Fermilab



0.8

TeV

doubly charged scalar exchange

$$0.01 G_F$$

E158

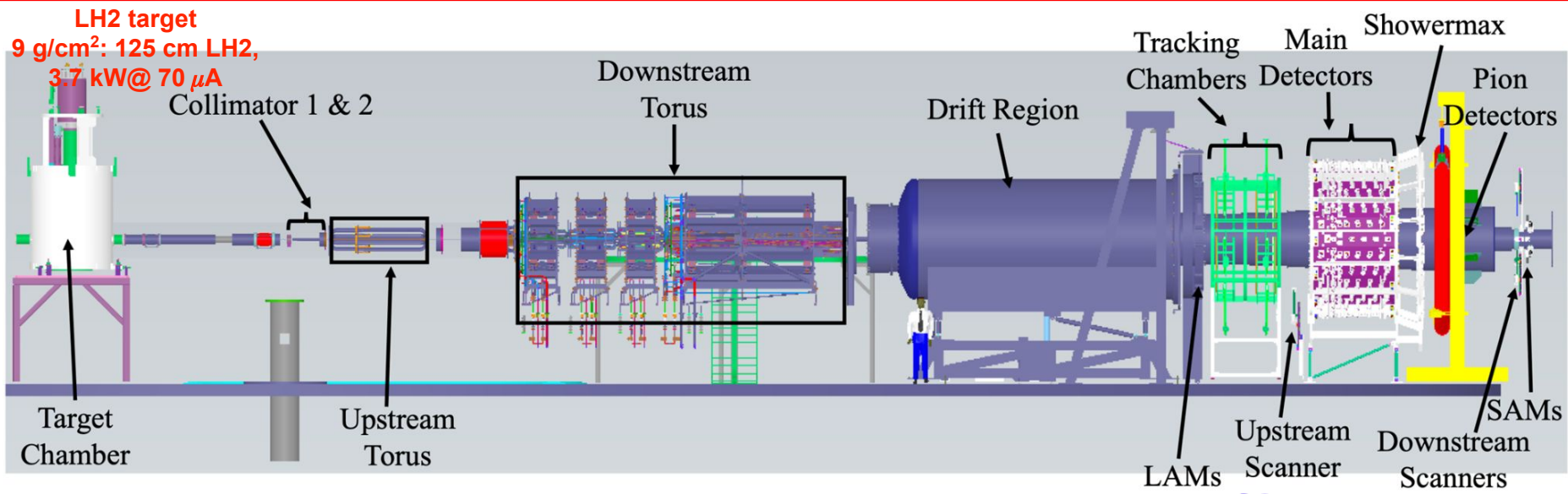
$$\left| \begin{matrix} e & e \\ R & R \\ e & e \end{matrix} \right|^2 - \left| \begin{matrix} e & e \\ L & L \\ e & e \end{matrix} \right|^2$$

16 TeV

1.0 TeV (Z_χ)

MOLLER at JLab

MOLLER at JLab - A Special purpose installation in HallA



- Full Azimuthal acceptance ~ 5 mrad lab frame.
- 134 GHz Electron rate
- 1 nm control of beam centroid on target
- Robust and redundant 0.4% polarization
- Multiple slow reversals: IHWP, Wien filter, spin precession

$$A_{PV} \sim 32 \text{ ppb} \quad \delta(A_{PV}) \sim 0.8 \text{ ppb} \quad \frac{\delta Q_W^e}{Q_W^e} = 2.4\%$$

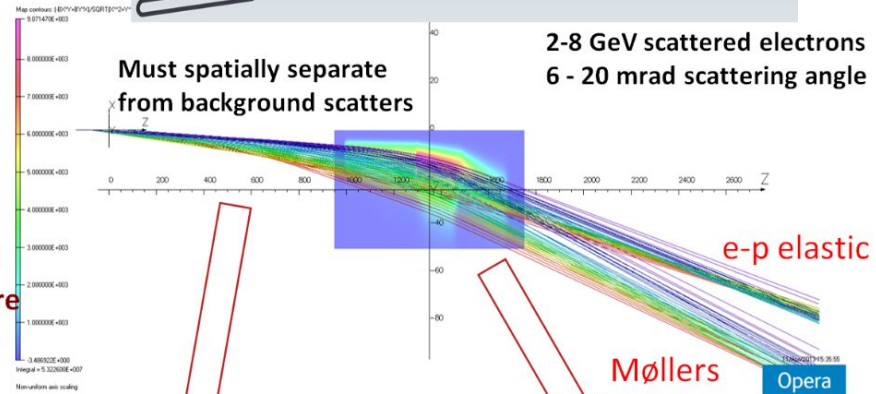
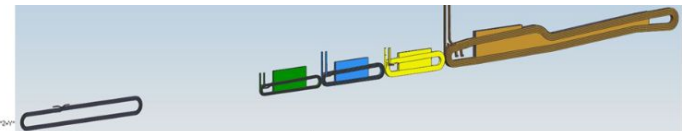
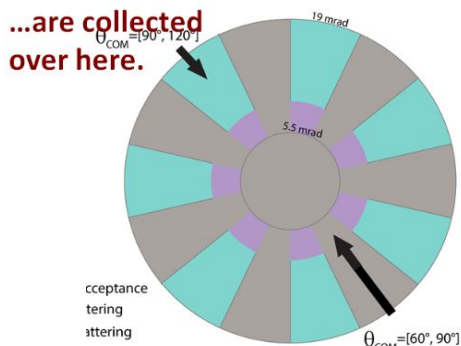
$$\delta(\sin^2 \theta_W) = \pm 0.00023 \text{ (stat.)} \pm 0.00012 \text{ (syst.)}$$

$\sim 0.1\%$ measurement

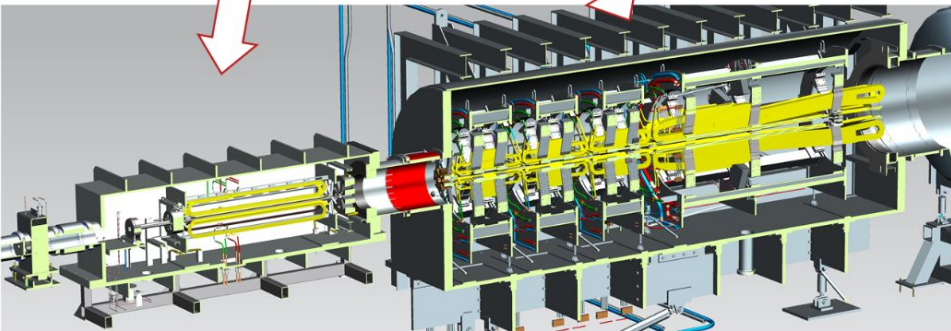
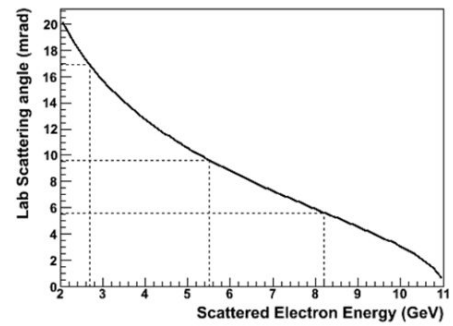
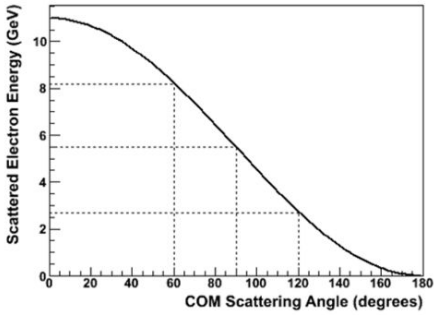
MOLLER measurement is the best among projected sensitivities for new measurements at low Q^2 or colliders over the next decade

Spectrometer Acceptance and Collimation

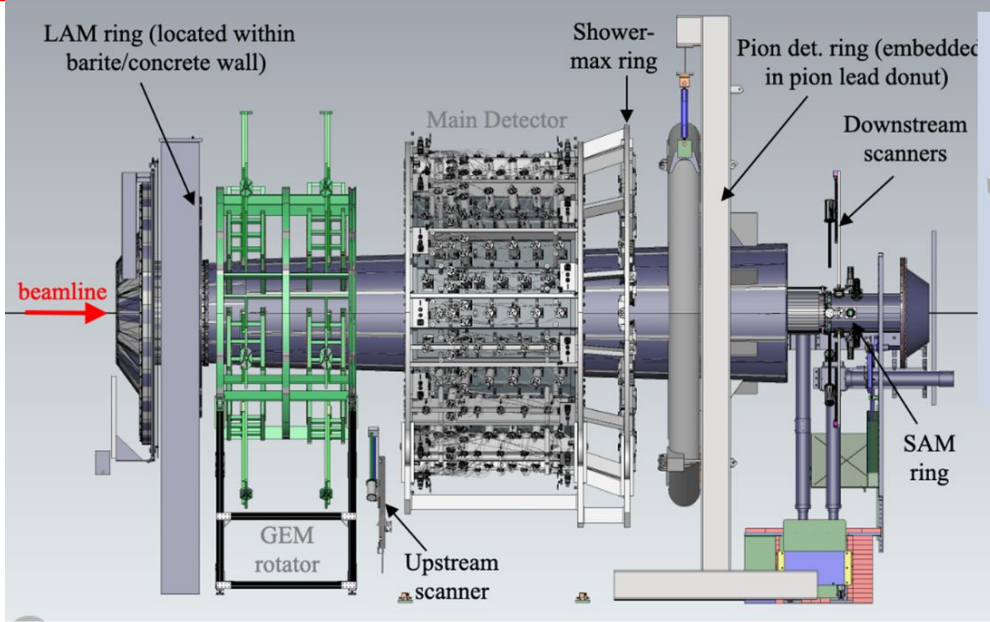
- Accept all Møller scattered electrons in range $\Theta_{CM} = 50^\circ - 130^\circ$
- Exploit identical particle nature for 100% azimuthal acceptance**; needs odd number of coils



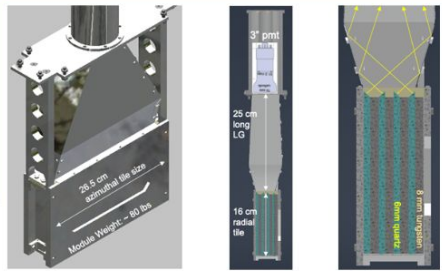
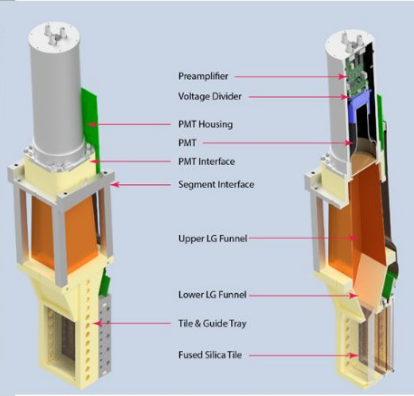
2-8 GeV scattered electrons
6 - 20 mrad scattering angle



MOLLER Detectors



Requirement for Ring 5:
 Detector resolution < 25%
 excess noise < 4%



Integrating (current mode) detectors:
asymmetry measurements of both signal and background, and beam and target monitoring

Tracking (counting mode) detectors:
spectrometer calibration, electron scattering angle distribution, and background measurements

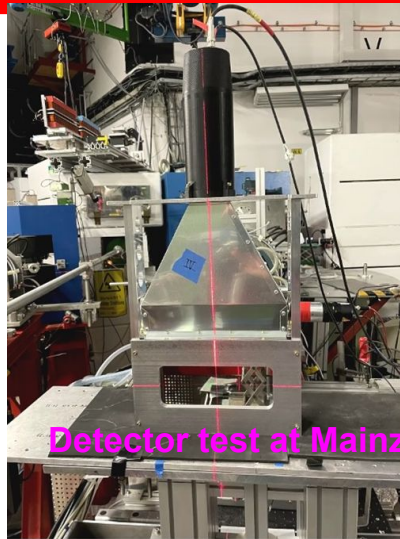
- Gas electron multipliers (GEM) detectors
- “Pion” acrylic Cherenkov detectors

Readout Electronics:

- Integration mode DAQ & trigger
 – Collect & analyze 100% of the helicity windows
- Counting mode DAQ & trigger
 – input rates between 10~kHz and 300~kHz

MOLLER Status - Currently at construction phase

- ~50M\$ MIE by US DOE
- CD-1 granted on Dec-2020
- CD-2/3 review on Oct 2023.
- **Construction: 2024-2025**
- Installation: 2026
- Commissioning: Summer 2026
- **Physics run: thru 2028**



Detector test at Mainz



Prototype Frame for DS Magnet



Pressure test

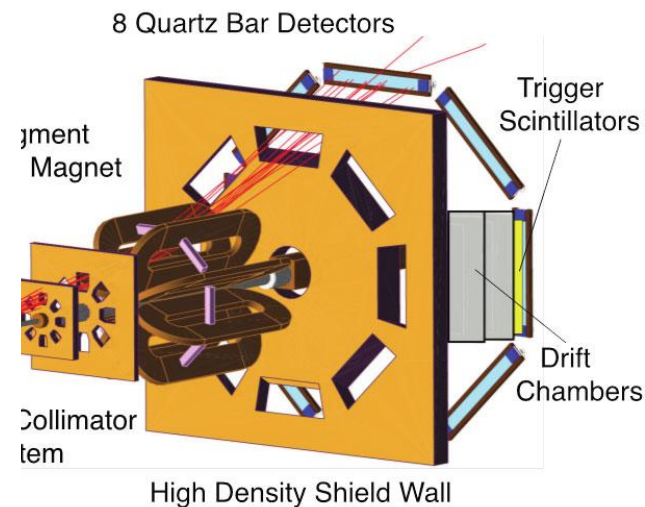
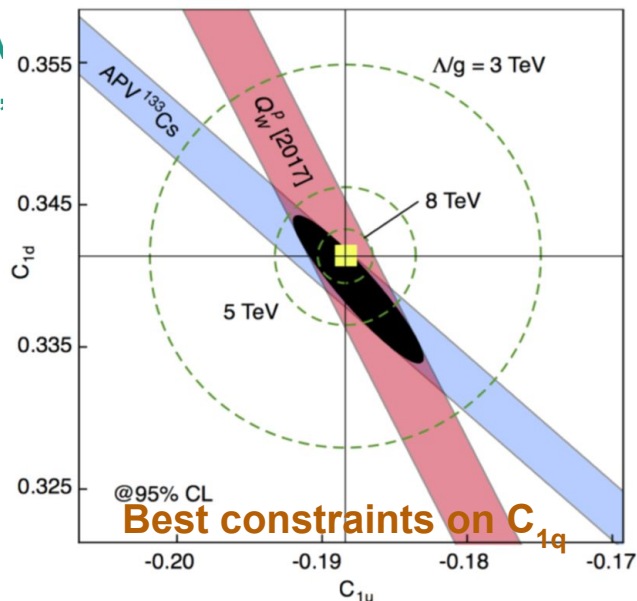
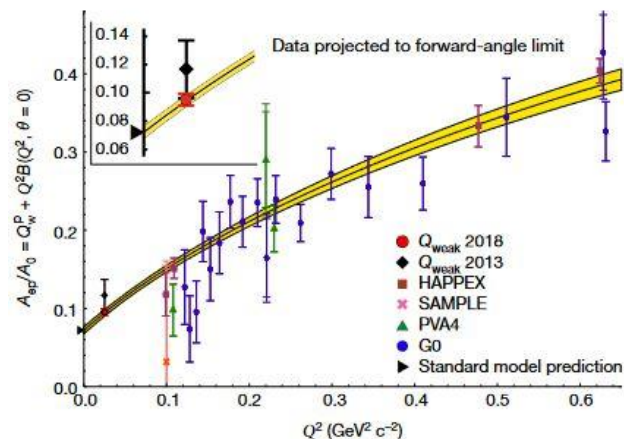


**Qweak:
The axial-vector coupling**

Qweak @ JLab - 4% measurement

$$A_{eP}/A_0 = Q_W^p + Q^2 B(Q^2, \theta)$$

Beam energy = 1.165 GeV, 180 uA
5.8 - 11.6 deg scattered electrons,



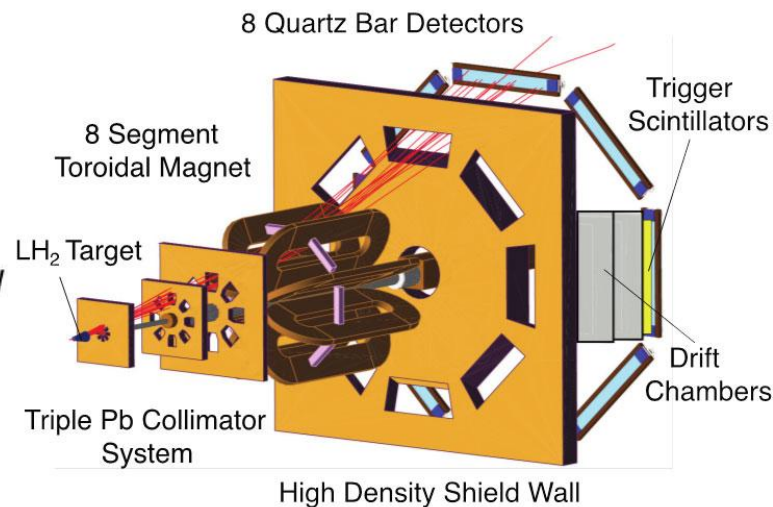
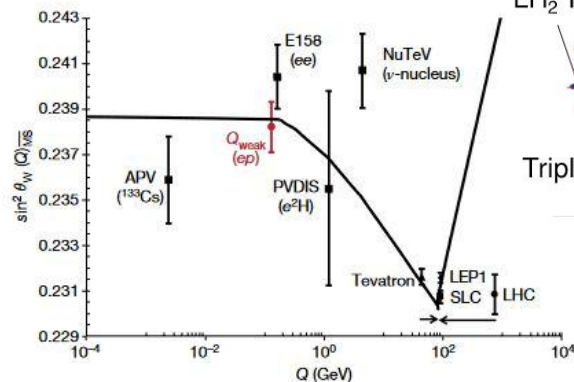
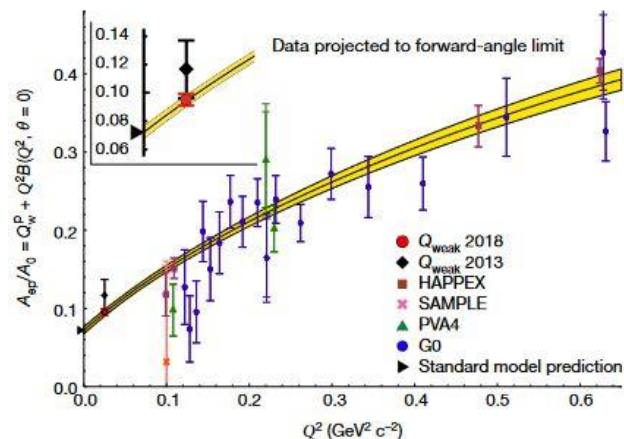
$$A_{eP} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = 226.5 \pm 8.3(\text{stat}) \pm 5.8(\text{syst}) \text{ ppb}$$

$$Q_W^p = -2(2C_{1u} + C_{1d}) = 0.0719 \pm 0.0045$$

Qweak @ JLab - 4% measurement

$$A_{eP}/A_0 = Q_W^p + Q^2 B(Q^2, \theta)$$

Beam energy = 1.165 GeV, 180 uA 35 cm LH2 target (3 kW),
5.8 - 11.6 deg scattered electrons, Q = 158 MeV



$$A_{eP} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = 226.5 \pm 8.3(stat) \pm 5.8(syst) ppb$$

$$Q_W^p = -2(2C_{1u} + C_{1d}) = 0.0719 \pm 0.0045$$

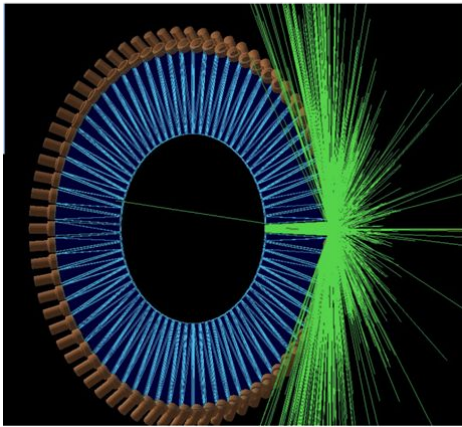
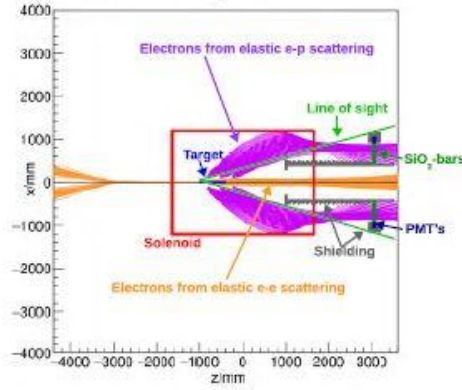
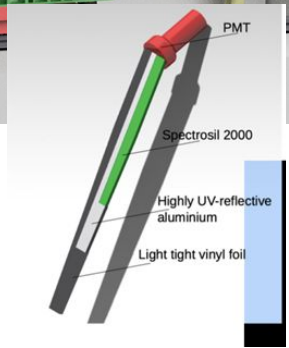
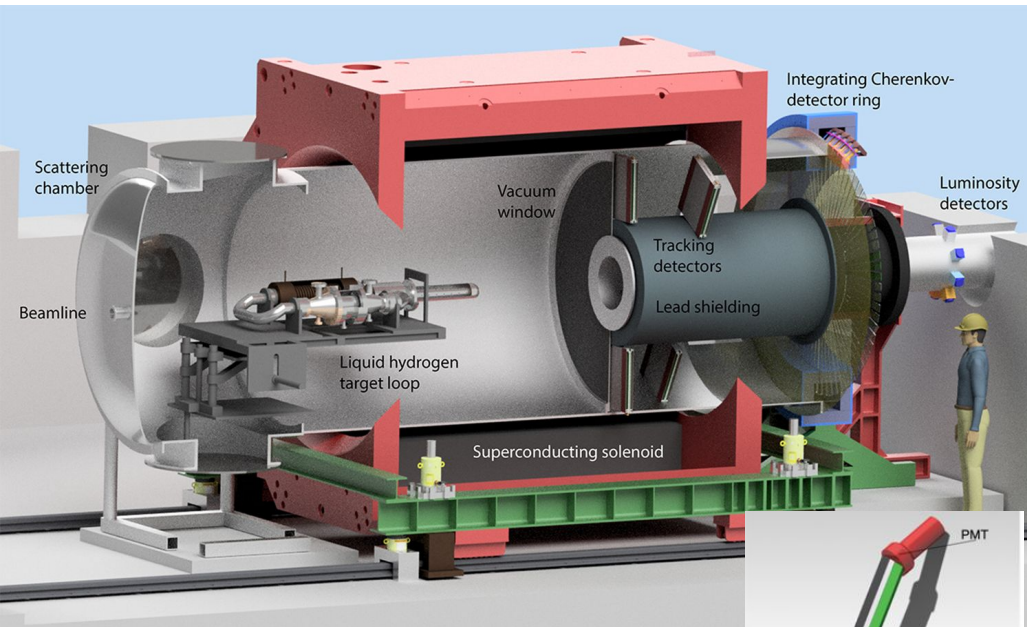
$$\sin^2 \hat{\theta}_W(0) = 0.2383 \pm 0.0011$$



Nature 557 207 (2018)

**P2 at MESA:
3x better Proton weak charge measurement**

P2 at MESA @ Q = 67 MeV



**P2@MESA
hydrogen**

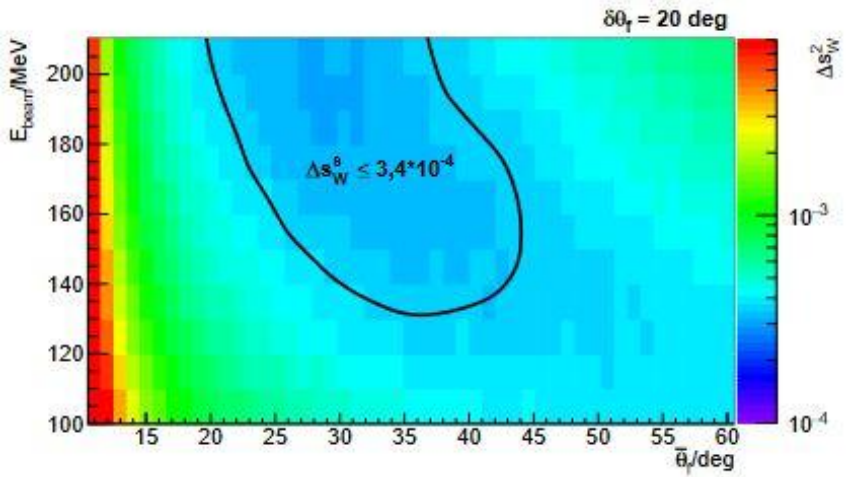
$A_{ep} = -28 \text{ ppb}$

$\Delta A_{ep} = 0.5 \text{ ppb}$
 $\text{ppb} = 1/\sqrt{N}$
 Factor 19
 After 11,000 h

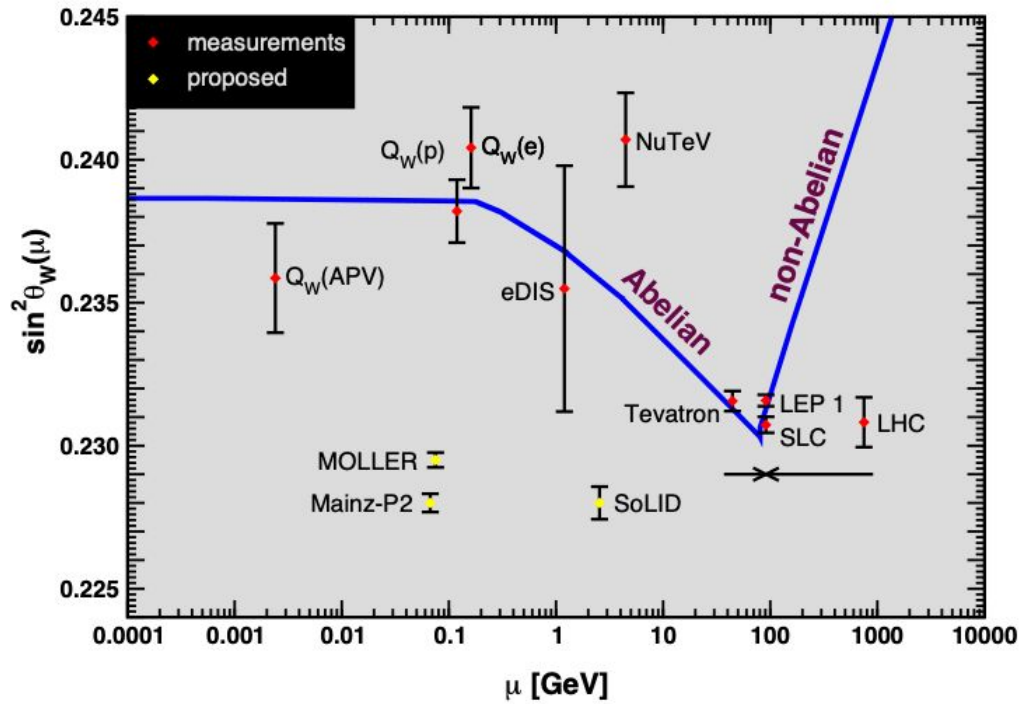
$\Delta A_{ep}/A_{ep} = 1.8 \%$

$\Delta \sin^2 \theta_W / \sin^2 \theta_W = 0.15 \%$

P2 at MESA

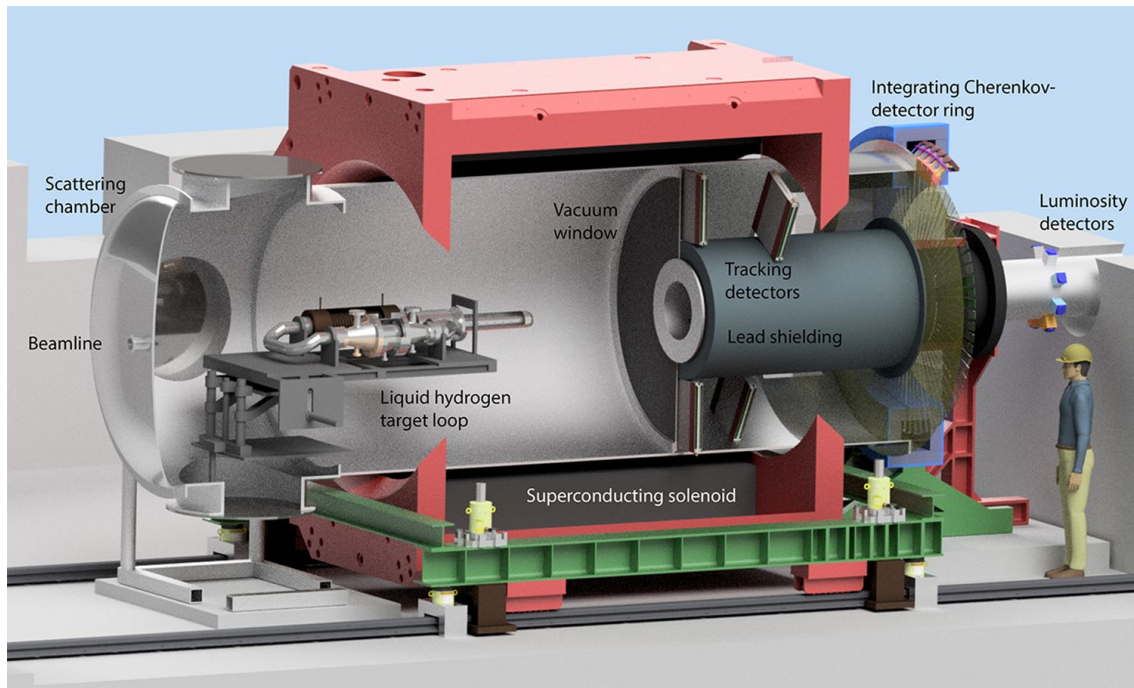


155 MeV - 150 uA beam on 60 cm
 LH2 target - 35 deg central
 scattering angle (Q = 67 MeV) -
 10000h of data taking



Sensitivity test of SM ~ 50 TeV - extendable to 60 TeV

C12 Weak charge measurement at MESA



MIT-Bates C12 Weak measurement ~ 25%

Sensitive to light dark Z-boson

| P2@MESA hydrogen | P2@MESA carbon |
|---|---|
| $A_{ep} = -28 \text{ ppb}$ | $A_{ep} = 416.3 \text{ ppb}$ |
| $\Delta A_{ep} = 0.5 \text{ ppb}$ ppb=1/ \sqrt{N} Factor 19 After 11,000 h | $\Delta A_{ep}^{\text{stat}} = 2.7 \text{ ppb}$ after 300 h $\Delta A_{ep}^{\text{stat}} = 0.9 \text{ ppb}$ after 2500 h |
| $\Delta A_{ep}/A_{ep} = 1.8 \%$ | $\Delta A_{ep}/A_{ep}^{\text{stat}} = 0.6 \%$ (0.2 %) Polarimetry! |
| $\Delta \sin^2 \theta_W / \sin^2 \theta_W = 0.15 \%$ | $\Delta \sin^2 \theta_W / \sin^2 \theta_W = 0.6 \%$ |

EBeam = 150 MeV,
Scatt. Angle = 40 deg.

A Decade-Long Ring PVES Program at MESA!!

- Hydrogen at **forward** angles:
 $A_{PV} \rightarrow Q_W(p) \rightarrow \sin^2\theta_W \rightarrow$ **BSM physics?**

$$\sin^2 \theta_W \approx \frac{1 - Q_W}{4}$$

$$A_{PV} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha_{em}} (Q_W - F(Q^2))$$

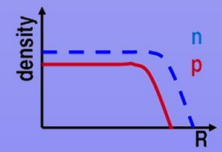
Proton structure - $\ll 1$ at small Q^2

Hadronic structure of proton sizable at not-so-small Q^2

- Hydrogen + Deuterium at **backward** angles:
 $A_{PV} \rightarrow$ **axial FF + strange contribution to magnetic FF**

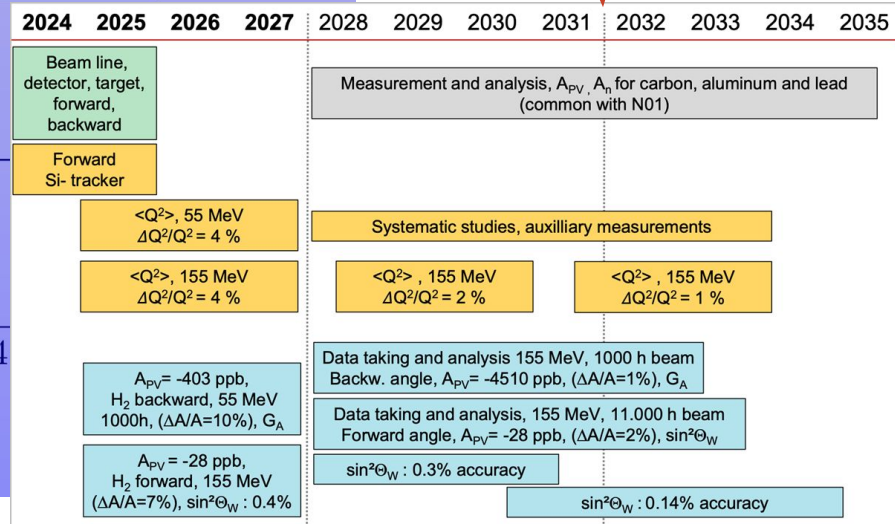
- Carbon:**
 $A_{PV} \rightarrow Q_W(^{12}C) = -24 \sin^2\theta_W$
 Complementary sensitivity to **BSM physics**

- Lead:**
 $A_{PV} \rightarrow F_{weak}(Q^2)$
 \rightarrow **neutron radius**
 \rightarrow **neutron skin thickness**
 related to the
 \rightarrow **symmetry energy - nuclear Equation of State**,
 e.g., \rightarrow **modeling of neutron stars**



$$A_{PV} = \frac{1}{4}$$

Notional Schedule of physics measurement campaign



PVDIS: Measurements of the Vector-Axial couplings

First measurement: E122

PVDIS - Existing Data (e,D) from 6 GeV JLab era

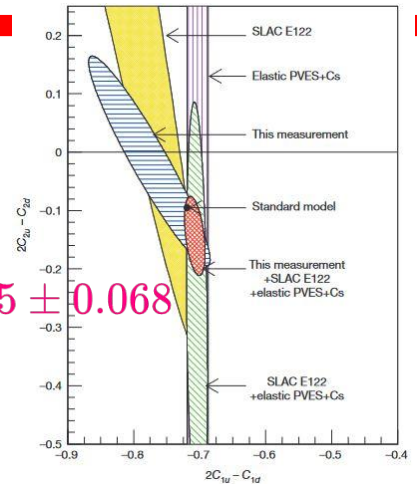
$$A_{PV}(PVDIS) = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L}$$

$$= \frac{G_F Q^2}{4\sqrt{2}\pi\alpha_{EM}} [a_1(x, Q^2)Y_1(x, y, Q^2) + a_3(x, Q^2)Y_3(x, y, Q^2)]$$

$$a_1 = \frac{6}{5}(2C_{1u} - C_{1d})$$

$$a_3 = \frac{6}{5}(2C_{2u} - C_{2d})$$

$$(2C_{2q} - C_{2d})|_{Q^2=0} = -0.145 \pm 0.068$$



At large $y = (E-E')/E$, the A_{PV} is sensitive to C_{2q}

selectively chosen DIS region

$$A_{PV} = -91.1(3.1(\text{stat}), 3.0(\text{sys.})) \times 10^{-6} (4.3\%)$$

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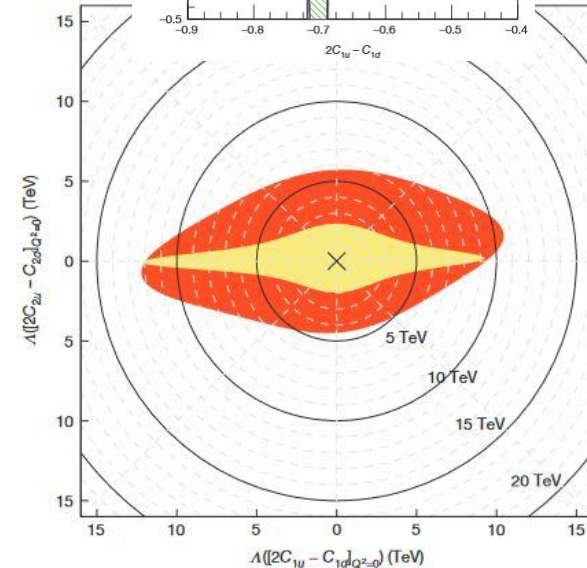
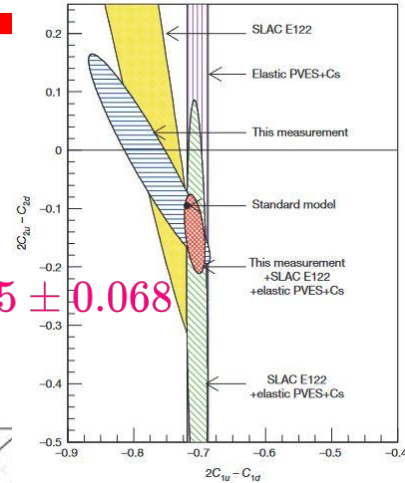
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$$A_{PV} = -91.1(3.1(\text{stat}), 3.0(\text{sys.})) \times 10^{-6} \quad (4.3\%)$$

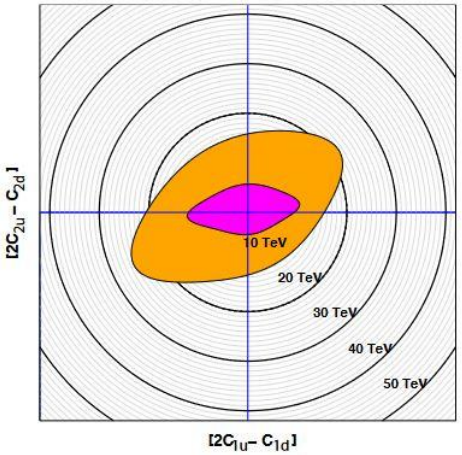
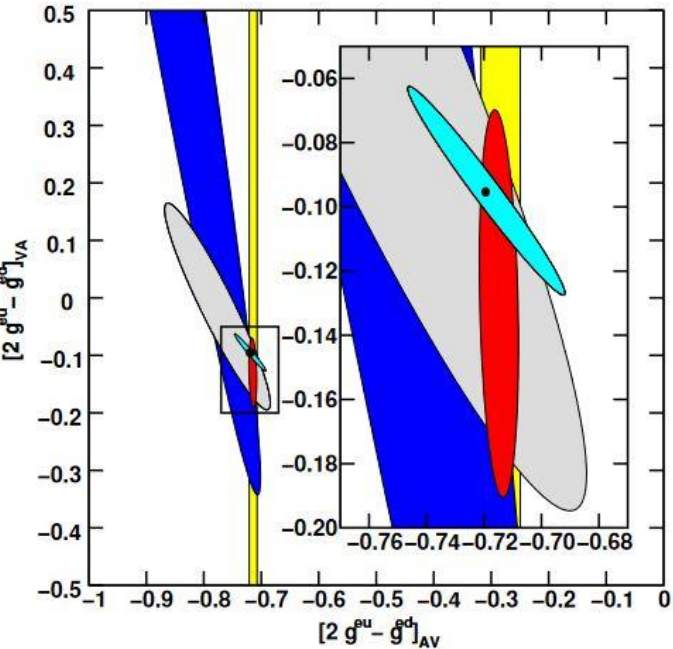
$$\sin^2 \hat{\theta}_w = 0.2299 \pm 0.0043 \quad (1.9\%)$$

Mass scale of new physics ~ 10 TeV!

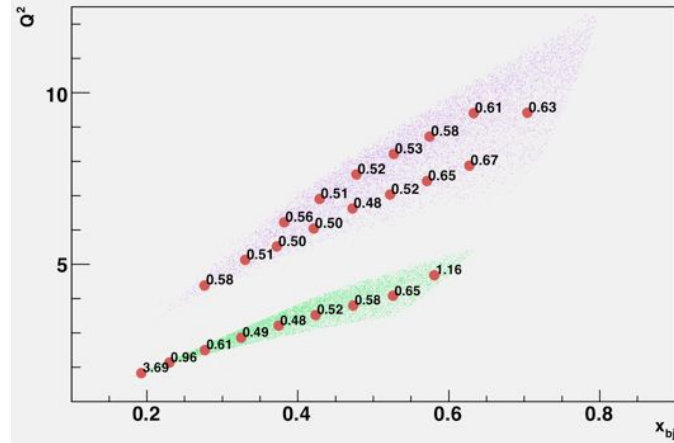
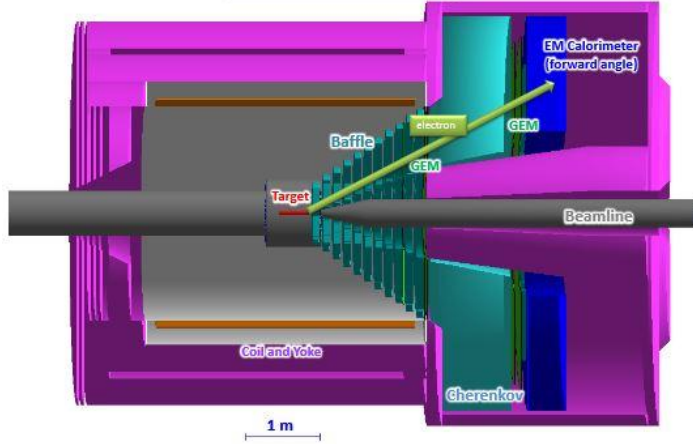


PVDIS @ SoLID: Large Kinematic Coverage

PVDIS @ SoLID

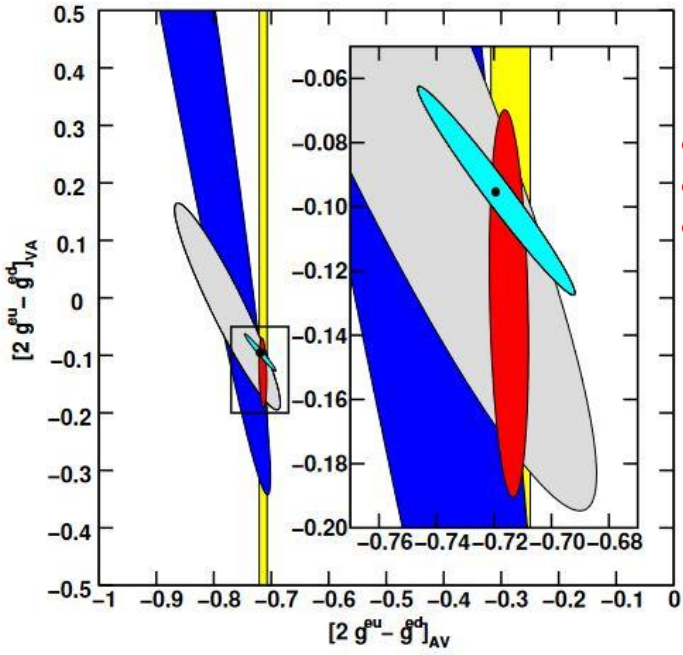
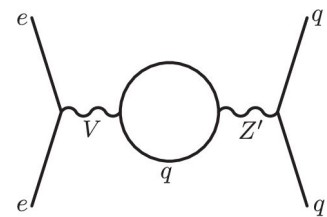


New physics reach of SoLID (with existing data) ~ 20 TeV



PVDIS @ SoLID - Installation will start just after MOLLER.

Leptophobic z'

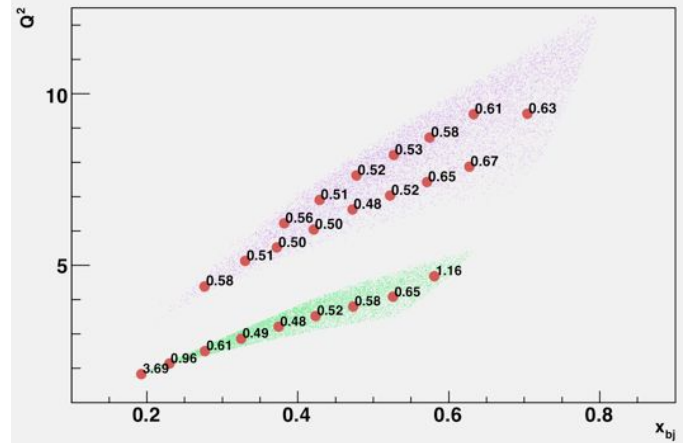
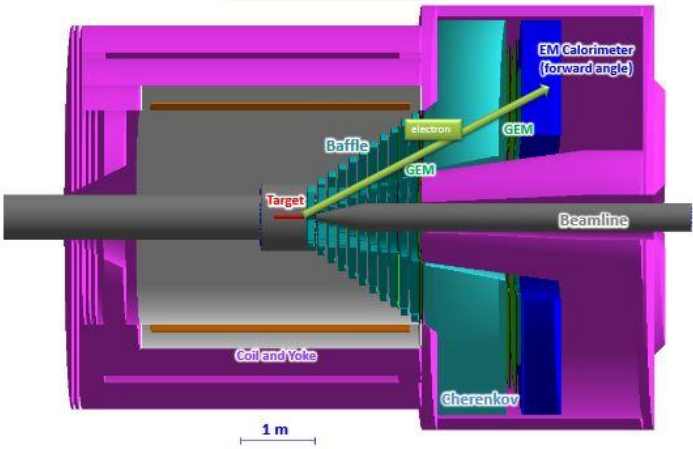


- Virtually all GUT models predict
- LHC reach $\sim 5\text{TeV}$
- Little sensitivity if Z' doesn't couple to leptons

Since e-vertex must be vector, the Z' can't couple to the C_{1q} if there is no electron coupling: can only affect C_{2q} 's

Current limit <100 GeV

SoLID can improve sensitivity: 100-200 GeV range



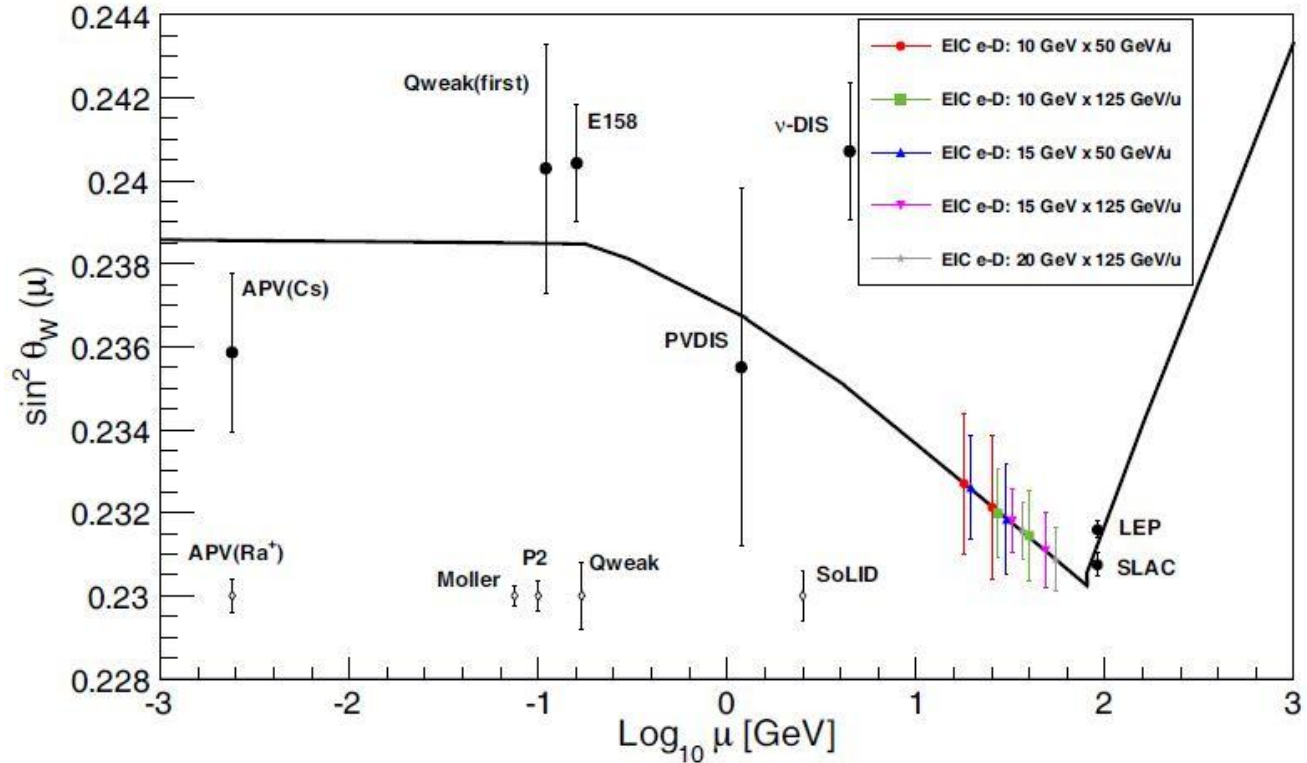
Running of Weak-mixing angle at EIC - PVDIS

- Polarized e on p
 - DIS regime (not like P2)
 - Required precise knowledge of PDFs
- Polarized e on d
 - Isoscalar target - Reduced need for precision PDF input

Zhao, Deshpande, Huang, Kumar, Riordan

-Performed Simulations at EIC

Talk from Michael Nycz



Other possibilities

- Moller scattering at an ILC

- Fixed target Moller scattering - Order of magnitude better than MOLLER.
- Timeline????

- Weak mixing angle at DUNE:

- High neutrino beam intensities
- Relatively smaller uncertainty for neutrino-electron than neutrino-nucleus scattering

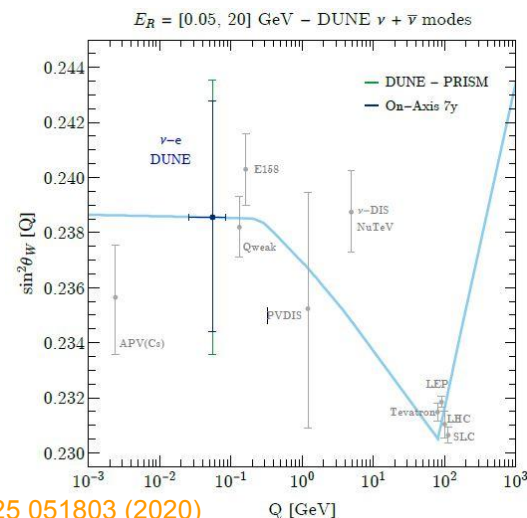
- Challenges:

- Neutrino-electron cross-section is three order smaller than neutrino-nucleus scattering - statistics
- Flux and energy distribution of neutrinos
 - PRISM (near detector) - moves perpendicular to the beam - on- and off- axis measurements

75 ton LAr TPC; 1.2MW proton beam with 7 yrs of data taking -2% measurement of $\sin^2\theta_W$

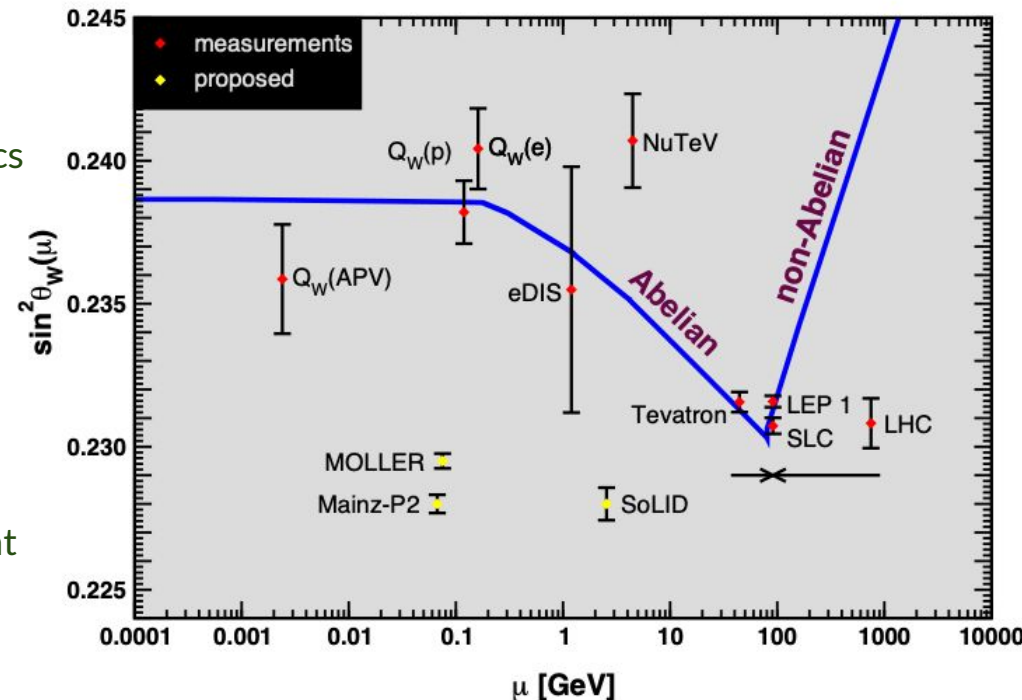
- FEC-ee, CEPC - timeline..

| K K, Snowmass 96 | E158 | LC |
|---------------------------|----------------------|---------------------|
| Energy (GeV) | 48 | 250-500 |
| Intensity/pulse | 4.5×10^{11} | 14×10^{11} |
| Pulse Rate (Hz) | 120 | 120 |
| P_e | 85% | 90% |
| Time (s) | 5×10^6 | 2×10^7 |
| A_{LR} (ppm) | 0.15 | 1-2 |
| δA_{LR} (ppm) | 0.015 | 0.008 |
| $\delta \sin^2(\theta_W)$ | 0.001 | 0.00006-8 |



Summary

- ❖ **Measurements of the Weak Mixing Angle**
 - Central to our understanding of the SM
 - Likely remain central in our search for new physics
- ❖ **A problem involving (both experimentalists and theorists) - Atomic, nuclear, higher-energy, neutrino..**
 - Challenging and exciting future for everyone..
- ❖ **Upcoming facilities, upgrade**
 - Pushing measurements to well below sub-percent levels
 - Reaching to limits where more robust theory calculation required



A remarkably productive research program that will continue to flourish over the next decade