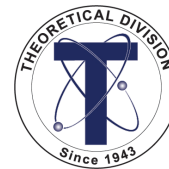


Neutrinoless double beta decay with *light* sterile neutrinos

Kaori Fuyuto

Los Alamos National Laboratory

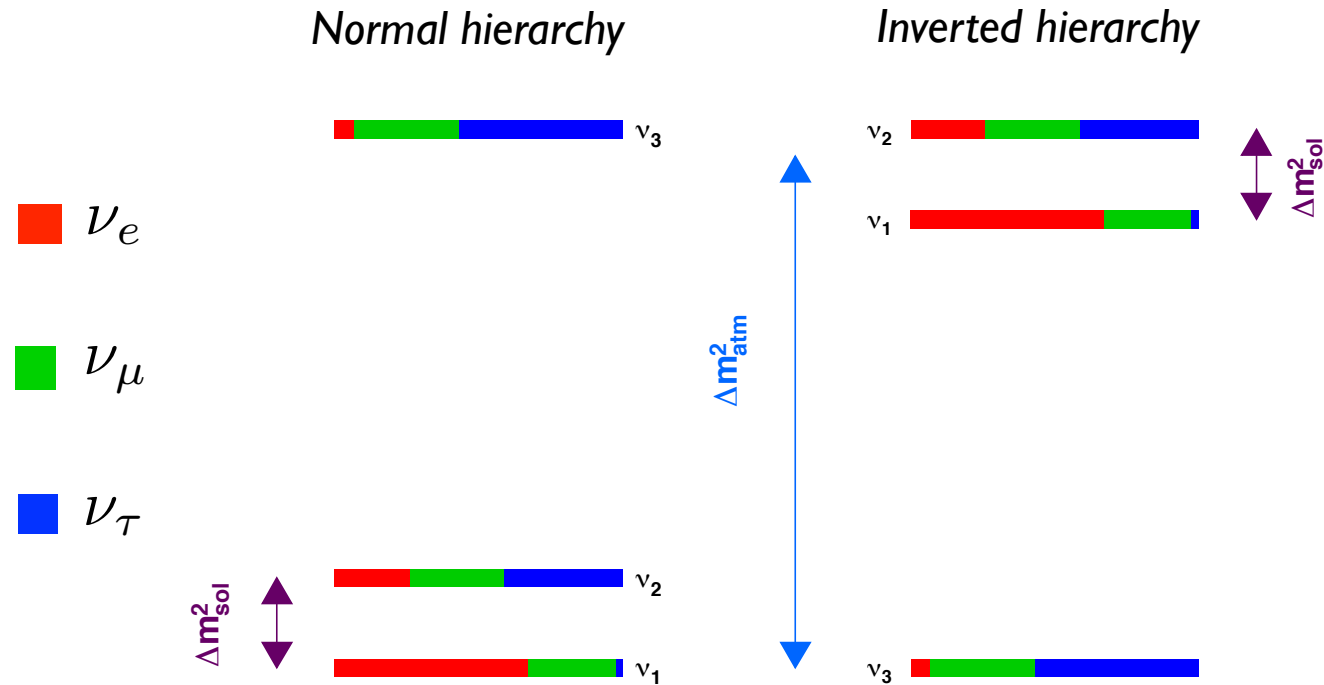


May 12, 2023 at INT

New Physics searches at the precision frontier

W. Dekens, J. de Vries, **KF**, E. Mereghetti, G. Zhou, JHEP06(2020)097

Neutrino mass



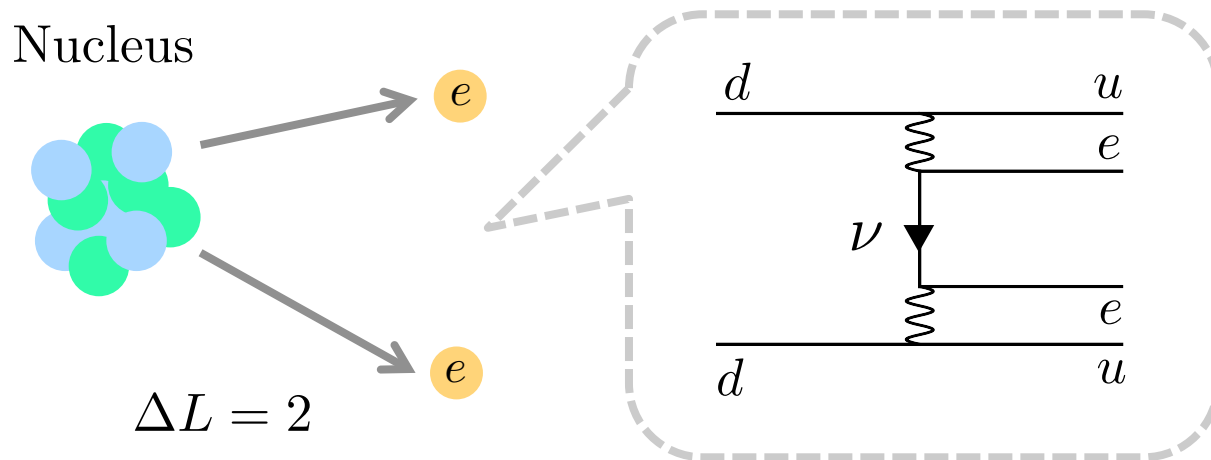
The origin of neutrino masses : Dirac or Majorana?

Neutrinoless Double Beta Decay : $\Delta L = 2$

Neutrinoless Double Beta Decay

Double beta decay without neutrino emission

$$(A, Z) \rightarrow (A, Z + 2) + 2e^{-}$$



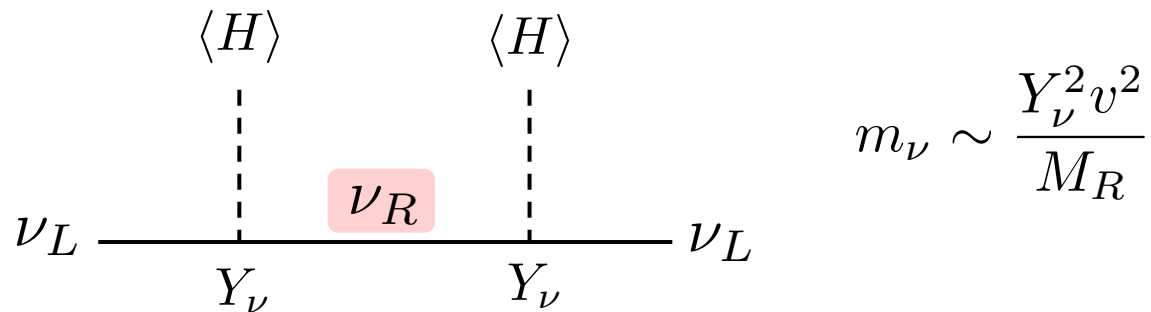
The process can occur if neutrino is a Majorana particle.

$$(\nu = \nu^c)$$

Neutrinoless Double Beta Decay

Right-handed neutrino : ν_R

$$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$$



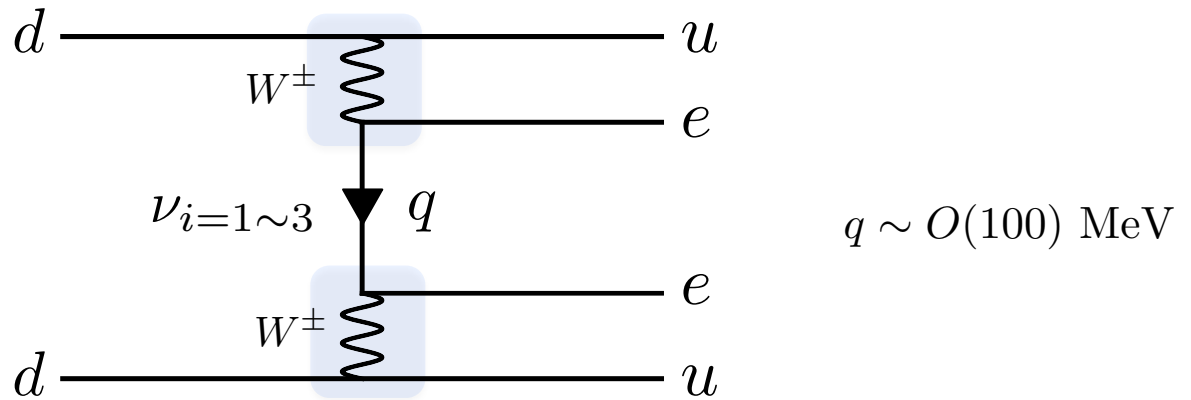
$$\mathcal{L}_{\text{mass}} = -\frac{1}{2} \bar{\nu} m_\nu \nu$$

Majorana mass eigenstate

$$\nu = \nu^c$$

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$

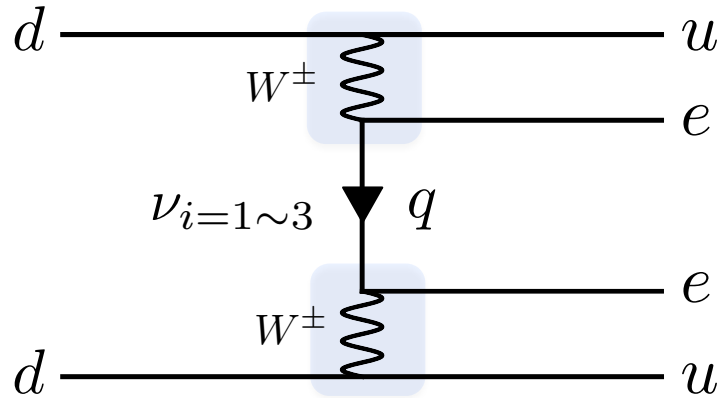


Left-handed vector operator

$$\mathcal{L}^{(6)} = \frac{G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu \quad \Bigg| \quad C_{\text{VLL}}^{(6)} = -2V_{ud}U_{ei}$$

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$



Left-handed vector operator

$$\mathcal{L}^{(6)} = \frac{G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu \quad \Bigg| \quad C_{\text{VLL}}^{(6)} = -2V_{ud}U_{ei}$$

$$\mathcal{A}_{0\nu 2\beta} \sim \sum_{i=1}^3 U_{ei}^2 \frac{m_i}{q^2 + m_i^2} \sim \frac{1}{q^2} \left(\sum_{i=1}^3 U_{ei}^2 m_i \right)$$

O(100) MeV

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$

$$U_{\text{PMNS}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ \cdots & \cdots & \cdots \\ \cdots & \cdots & \cdots \end{pmatrix}$$

[PDG] PRD98, 030001(2018) and update (2019)

$$\sin^2 \theta_{12} = 3.10 \cdot 10^{-1} \quad \sin^2 \theta_{23} = 5.58 \cdot 10^{-1}$$

$$\sin^2 \theta_{13} = 2.241 \cdot 10^{-2} \quad \delta_{\text{Dirac}} = 1.23\pi$$

$$\Delta m_{21}^2 = m_2^2 - m_1^2 = 7.39 \times 10^{-5} \text{ [eV}^2\text{]}$$

$$\Delta m_{31}^2 = m_3^2 - m_1^2 = \pm 2.5 \times 10^{-3} \text{ [eV}^2\text{]}$$

$$\mathcal{A}_{0\nu 2\beta} \sim \sum_{i=1}^3 U_{ei}^2 \frac{m_i}{q^2 + m_i^2} \sim \frac{1}{q^2} \left(\sum_{i=1}^3 U_{ei}^2 m_i \right)$$

$\mathcal{O}(100) \text{ MeV}$
Oscillation data

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$

$$U_{\text{PMNS}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ \cdots & \cdots & \cdots \\ \cdots & \cdots & \cdots \end{pmatrix}$$

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Inverse half-life : $\left(T_{1/2}^{0\nu}\right)^{-1} = g_A^4 G_{0\nu} |\mathcal{A}_{0\nu 2\beta}|^2$

$$g_A = 1.27, G_{0\nu} : \text{Phase space factor}$$

Search for NDBD

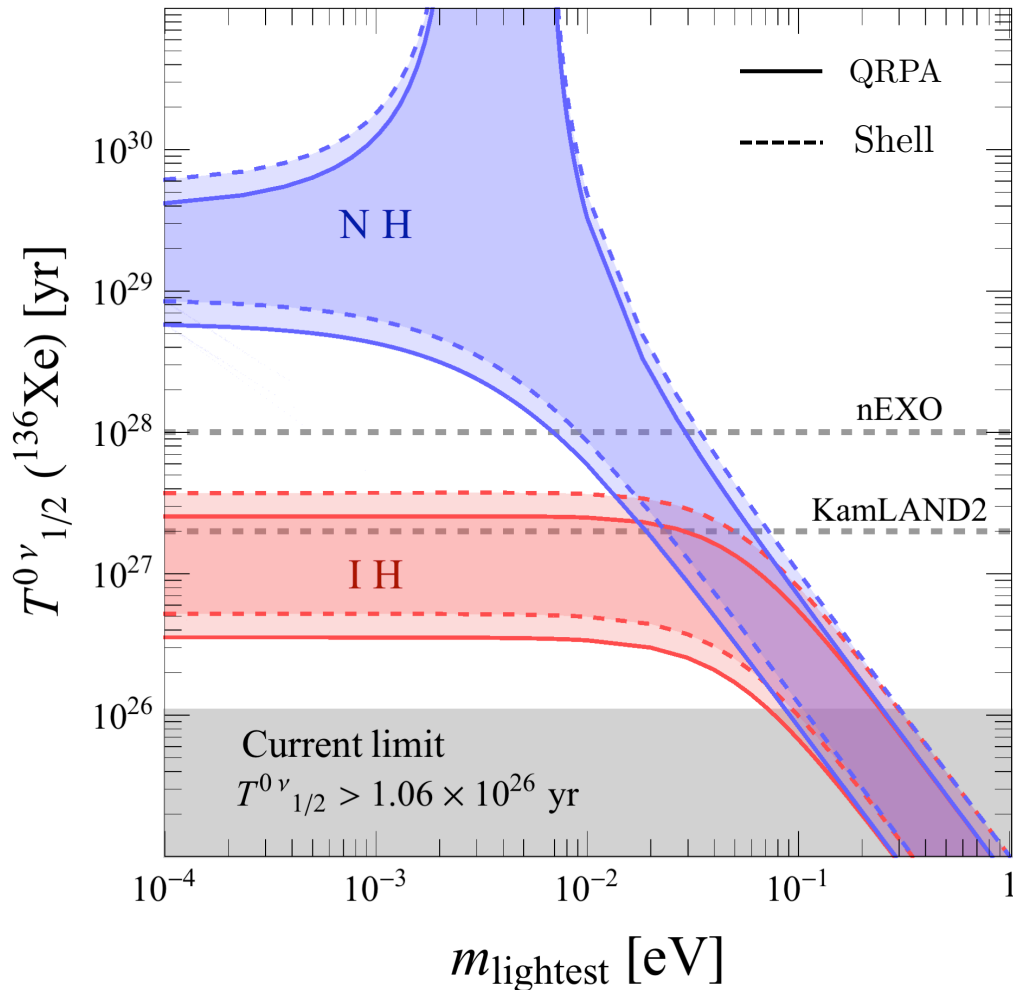
Isotope	Experiment	Current limit ($\times 10^{25}$ yr)		Future sensitivity ($\times 10^{25}$ yr)	
^{48}Ca	ELEGANT-IV	5.8×10^{-3}	[2]	–	
	CANDLES	6.2×10^{-3}	[23]	10^{-2}	[28]
	NEMO-3	2.0×10^{-3}	[9]		
^{76}Ge	MAJORANA DEMONSTRATOR	2.7	[22]	–	
	GERDA	9.0	[24]	–	
	LEGEND	–		10^3	[29]
^{82}Se	CUPID	3.5×10^{-1}	[25]		
	NEMO-3	2.5×10^{-2}	[20]		
	SuperNEMO	–		10	[30]
^{96}Zr	NEMO-3	9.2×10^{-4}	[3]		
^{100}Mo	NEMO-3	1.1×10^{-1}	[8]		
	CUPID-1T	–		9.2×10^2	[37]
	AMoRE	9.5×10^{-3}	[26]	5.0×10	[31]
^{116}Cd	NEMO-3	1.0×10^{-2}	[13]		
^{128}Te	–	1.1×10^{-2}	[1]	–	
^{130}Te	CUORE	3.2	[21]	9.0	[32]
	SNO+	–		1.0×10^2	[33]
^{136}Xe	KamLAND-Zen	10.7	[10]	2.0×10^2	
	EXO-200	3.5	[27]	10^3	[34]
	NEXT	–		2.0×10^2	[35]
	PandaX	–		1.0×10^2	[36]
^{150}Nd	NEMO-3	2.0×10^{-3}	[12]		

$$T_{1/2}^{0\nu} > 2.3 \times 10^{26} \text{ yr}$$

KamLAND-Zen Collaboration
2203.02139

Current limit on half-life

Standard case : 3 light Majorana neutrinos ($M_R \gg v$)



Normal Hierarchy (NH)

$$m_1 < m_2 < m_3$$

Inverted Hierarchy (IH)

$$m_3 < m_1 < m_2$$

$$\sim 10^{27} \text{ yr}$$

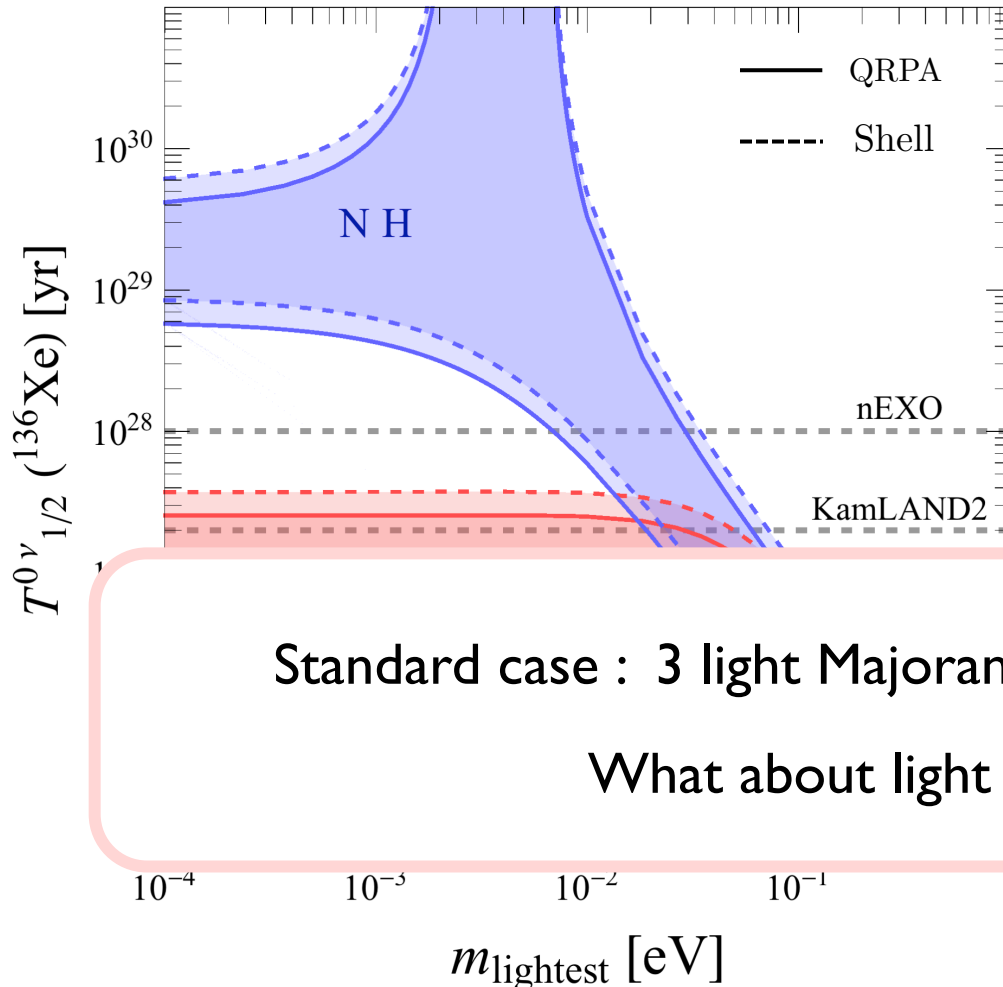
@KamLAND2 – Zen

$$\sim 10^{28} \text{ yr @nEXO}$$

*Future

Current limit on half-life

Standard case : 3 light Majorana neutrinos ($M_R \gg v$)



Normal Hierarchy (NH)

$$m_1 < m_2 < m_3$$

Inverted Hierarchy (IH)

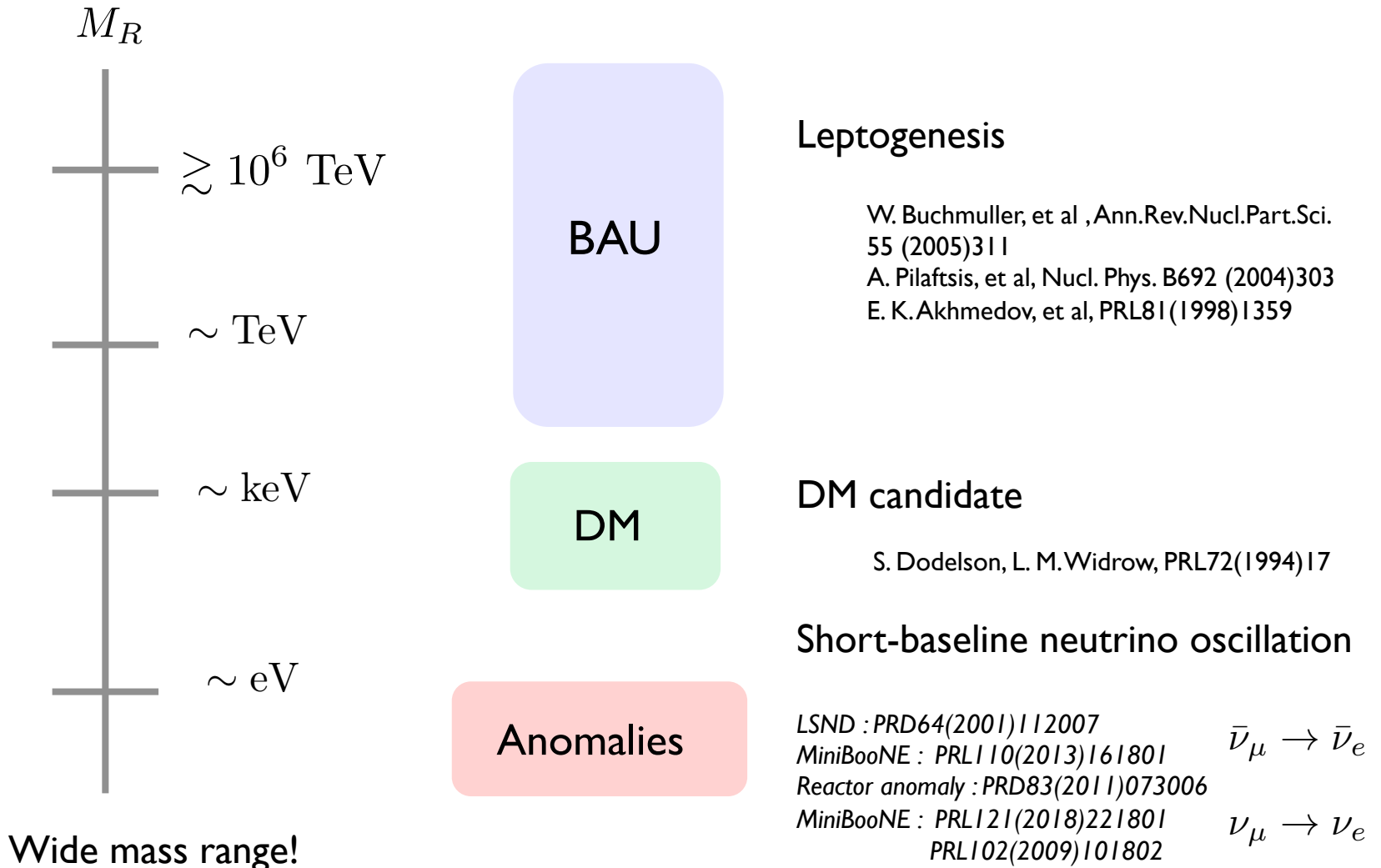
$$m_3 < m_1 < m_2$$

Standard case : 3 light Majorana neutrinos ($M_R \gg v$)

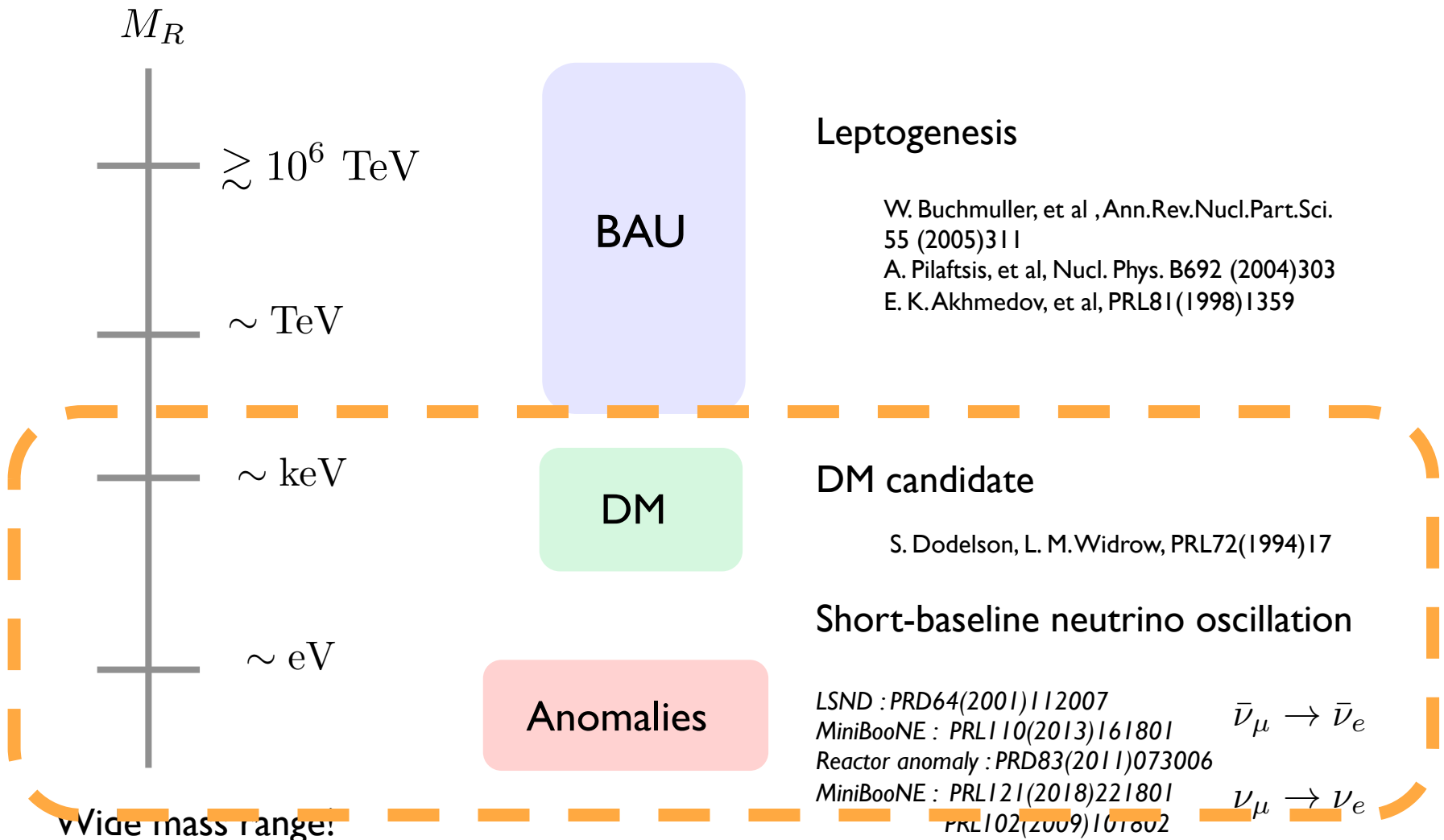
What about light M_R case?

Future

Other phenomenological aspects:



* Need theoretical analysis in light of light sterile neutrinos

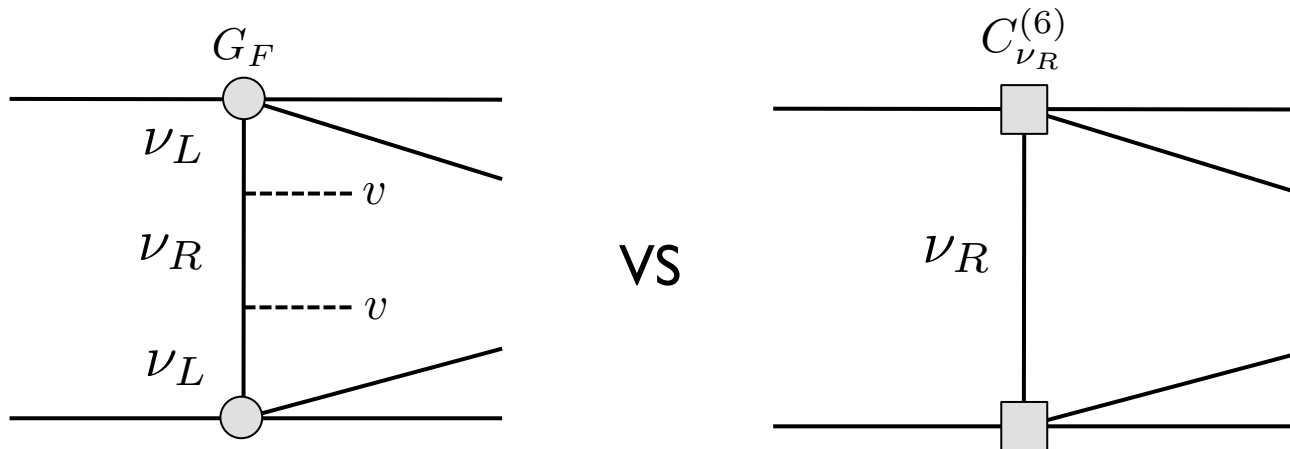


Model-independent analysis in the light ν_R scenario

~ Effective Field Theory

* Non-standard interactions (d = 6)

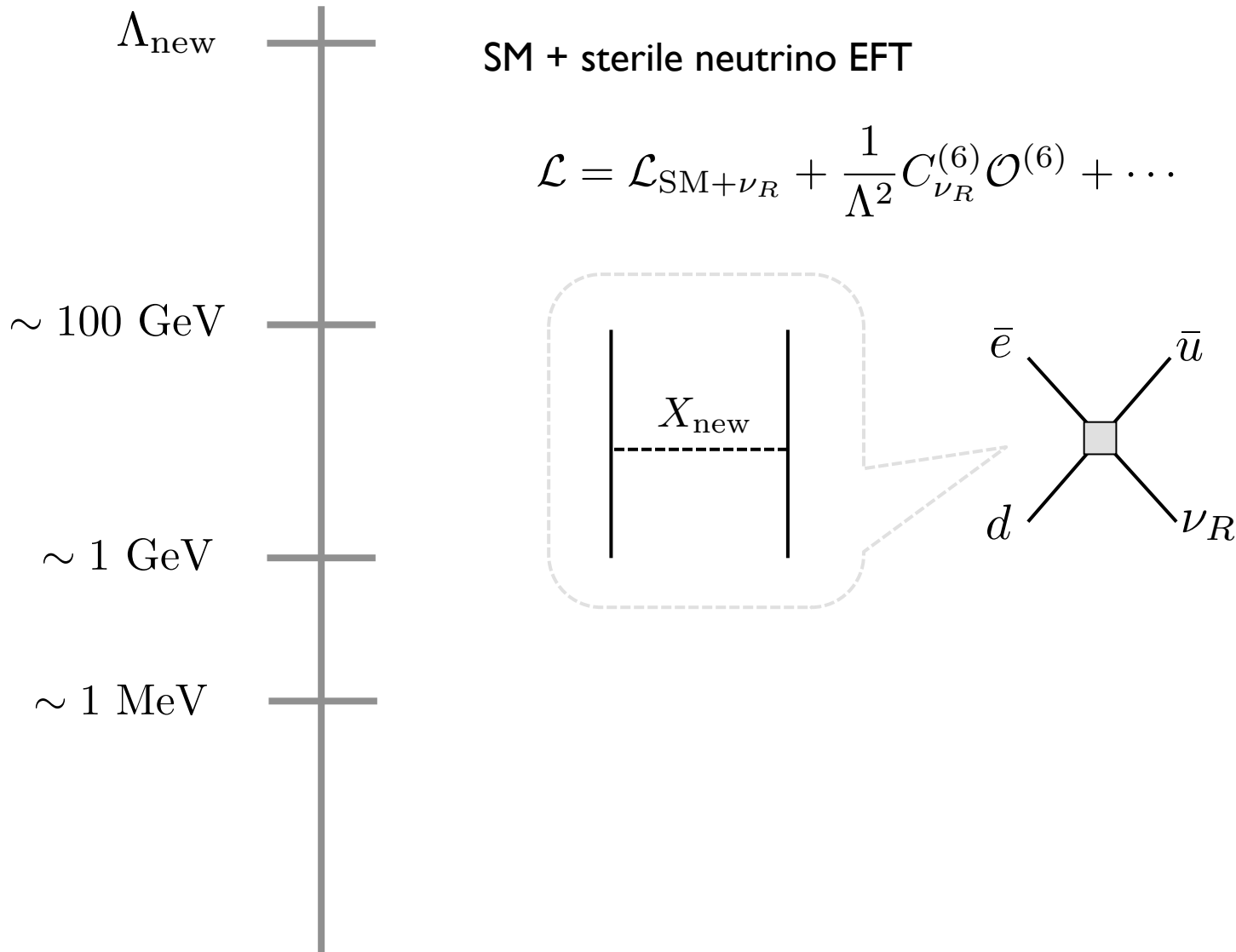
$$\mathcal{L} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)}$$



* Construct interpolation formulas for NMEs and LECs depending on M_R

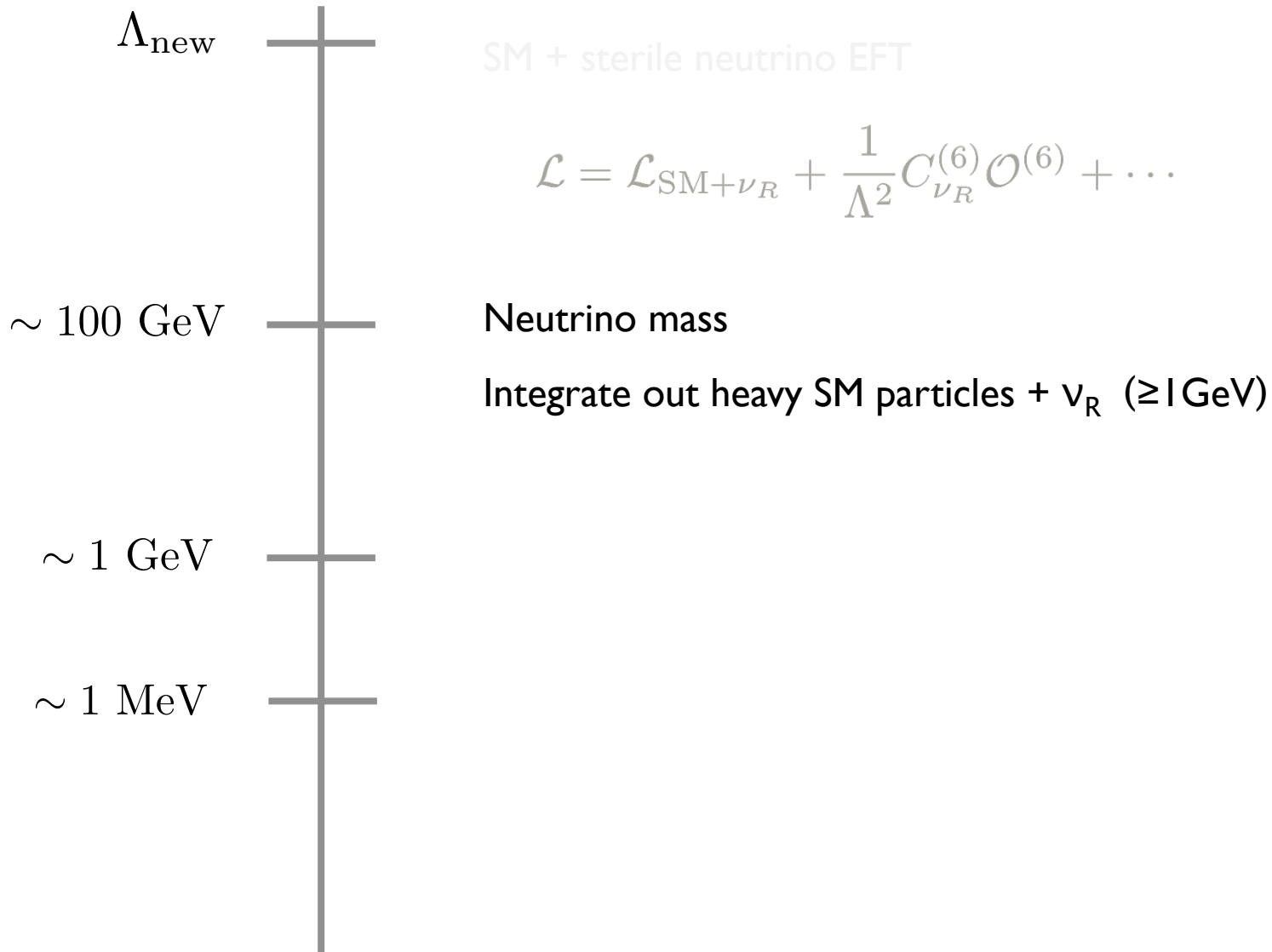
EFT approach

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)
V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 082(2017)
V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 097(2018)



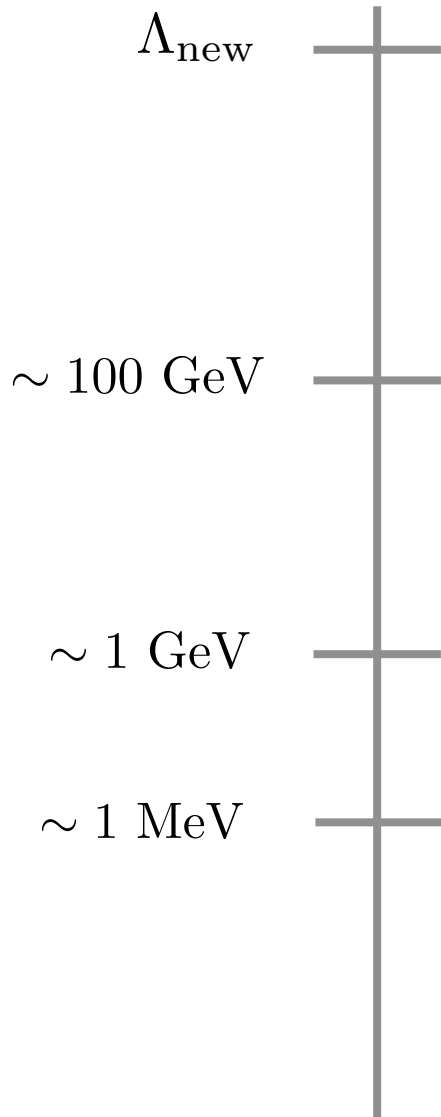
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SM + sterile neutrino EFT

$$\mathcal{L} = \mathcal{L}_{\text{SM}+\nu_R} + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)} + \dots$$

Neutrino mass

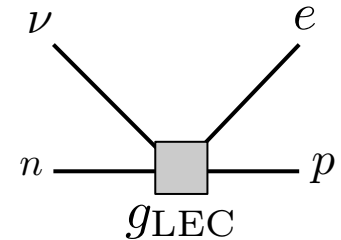
Integrate out heavy SM particles + ν_R ($\geq 1 \text{ GeV}$)

$\sim 1 \text{ GeV}$

Chiral Perturbation Theory

$\sim 1 \text{ MeV}$

“ Inverse half-life ”

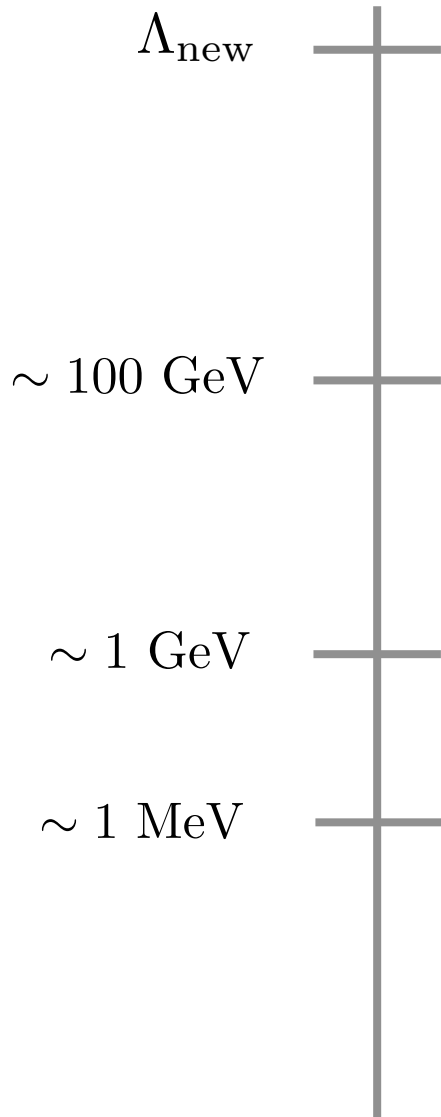


$$\left(T_{1/2}^{0\nu} \right)^{-1} = g_A^4 G_{0\nu} \left| \mathcal{A}_{0\nu 2\beta} \left(g_{\text{LEC}}, C_{\nu_R}^{(6)}, M_{\text{NME}} \right) \right|^2$$

$g_A = 1.27$, $G_{0\nu}$: Phase space factor

EFT approach

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)
 V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 082(2017)
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SM + sterile neutrino EFT

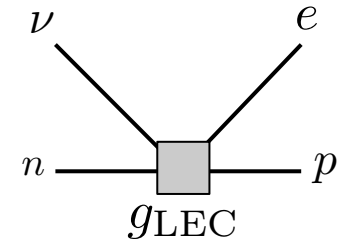
$$\mathcal{L} = \mathcal{L}_{\text{SM}+\nu_R} + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)} + \dots$$

Neutrino mass

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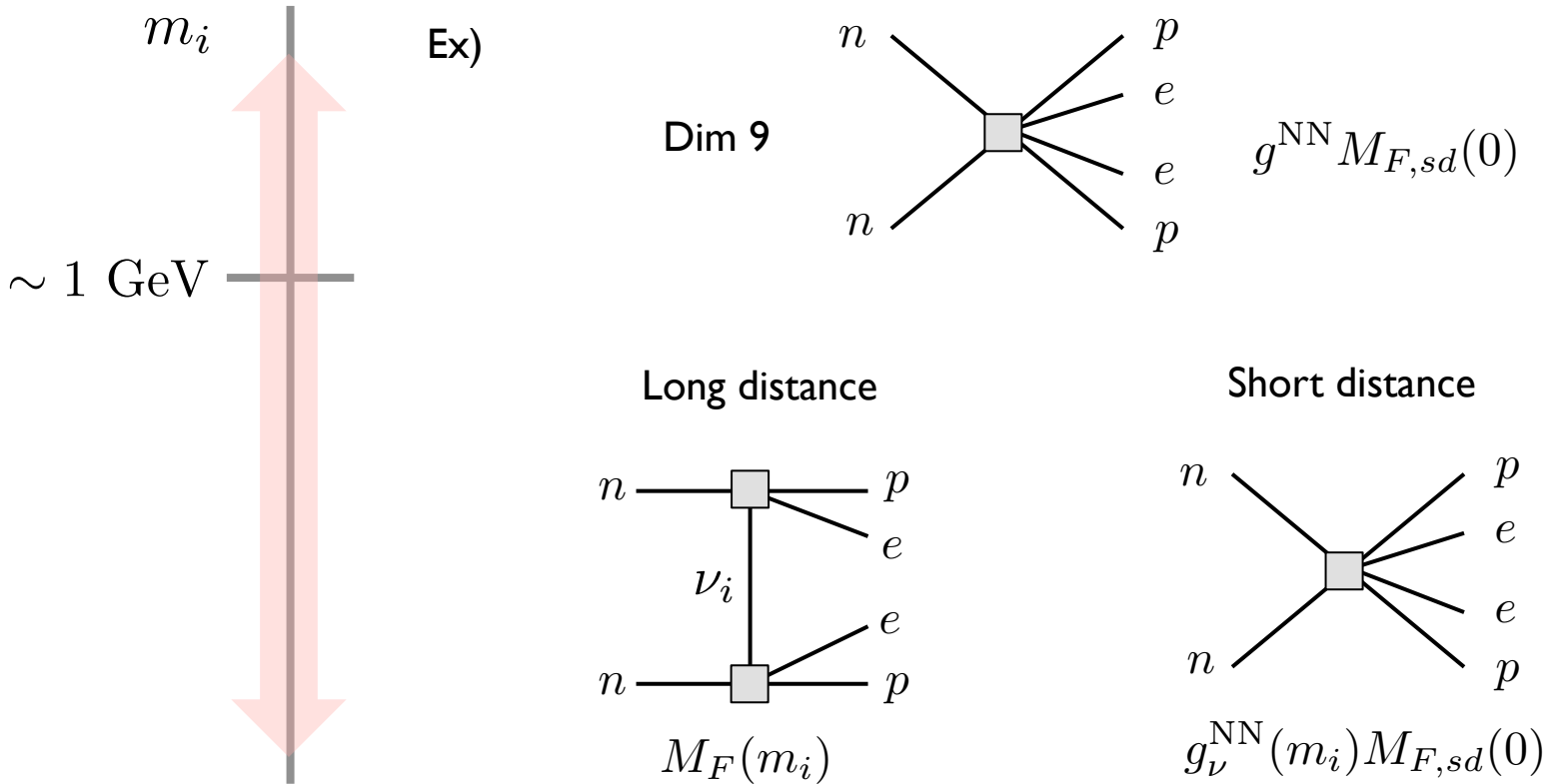
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“Inverse half-life”

$$\left(T_{1/2}^{0\nu}\right)^{-1} = g_A^4 G_{0\nu} \left| \mathcal{A}_{0\nu 2\beta} \left(g_{\text{LEC}}, C_{\nu_R}^{(6)}, M_{\text{NME}} \right) \right|^2$$

“Interpolation formulae”

EFT approach



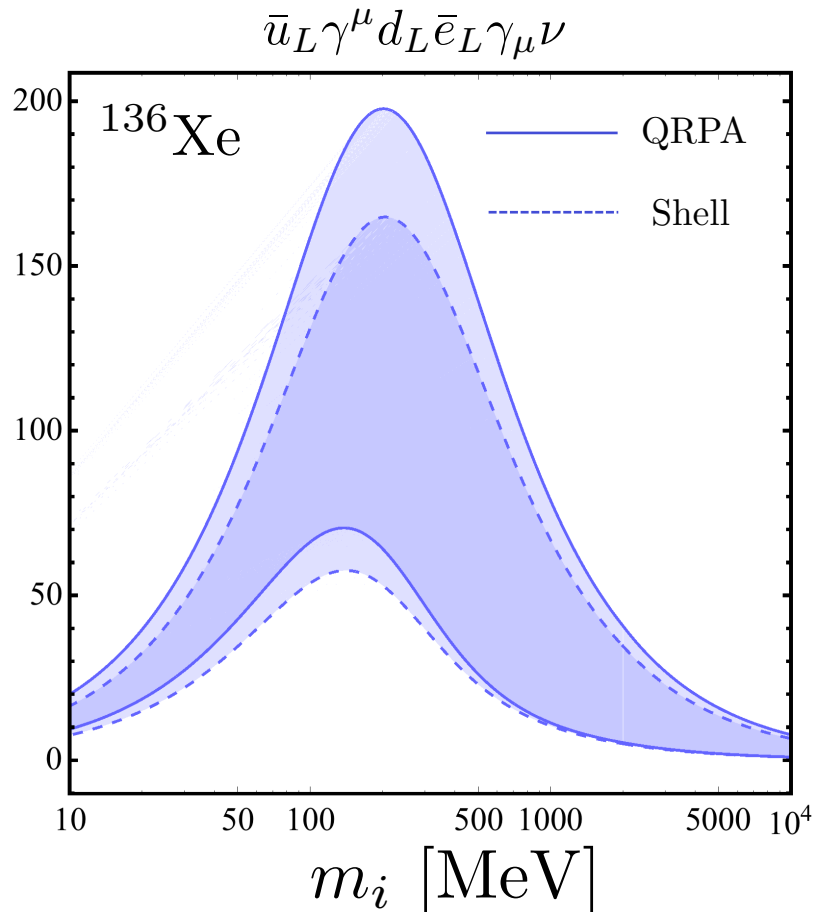
$M_{\text{NME}}(m_i)$: Pade approximation

$$\mathcal{A}_{0\nu 2\beta}(m_i)|_{m_i \gg \text{GeV}} = \mathcal{A}_{0\nu 2\beta}^{(9)}$$

$$\lim_{m_i \rightarrow 0} M_F(m_i) = M_F(0)$$

$$\lim_{m_i \rightarrow \infty} M_F(m_i) = \frac{m_\pi^2}{m_i^2} M_{F,sd}(0)$$

Mass dependence of the amplitude : $|\mathcal{A}_{0\nu 2\beta}(m_i)|_{^{136}\text{Xe}}$



- Two different NMEs
- Peak around $O(100)$ MeV

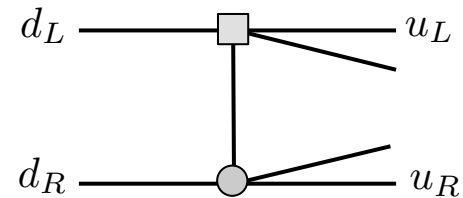
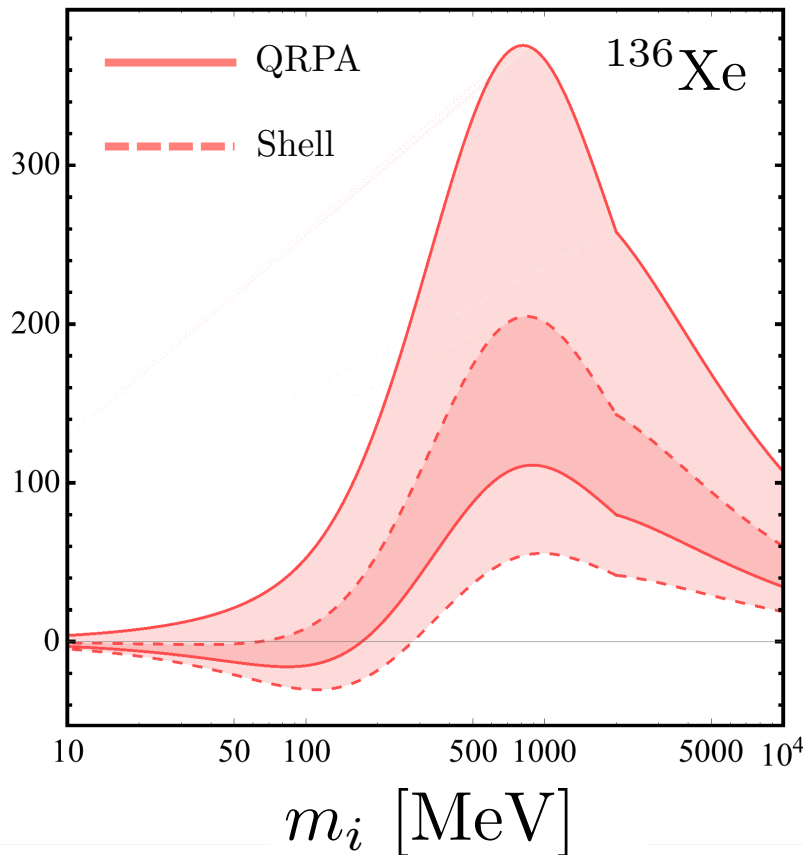
$$\frac{m_i}{q^2 + m_i^2}$$

$O(100)$ MeV

- Similar behavior in literature
J.Barea, et al PRD92(2015)093001
- Large uncertainty in LECs

Mass dependence of the amplitude : $|\mathcal{A}_{0\nu 2\beta}(m_i)|_{^{136}\text{Xe}}$

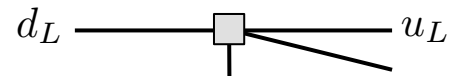
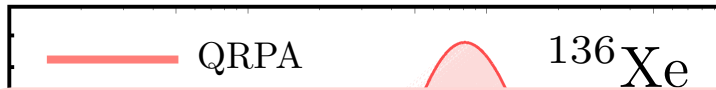
$$(\bar{u}_L \gamma^\mu d_L \times \bar{u}_R \gamma^\mu d_R) \bar{e}_L \gamma_\mu \nu$$



- Peak around $O(1)$ GeV
- * Nontrivial behavior due to LECs
- Not discussed in literature
- Large uncertainty in LECs

Mass dependence of the amplitude : $|\mathcal{A}_{0\nu 2\beta}(m_i)|_{136\text{Xe}}$

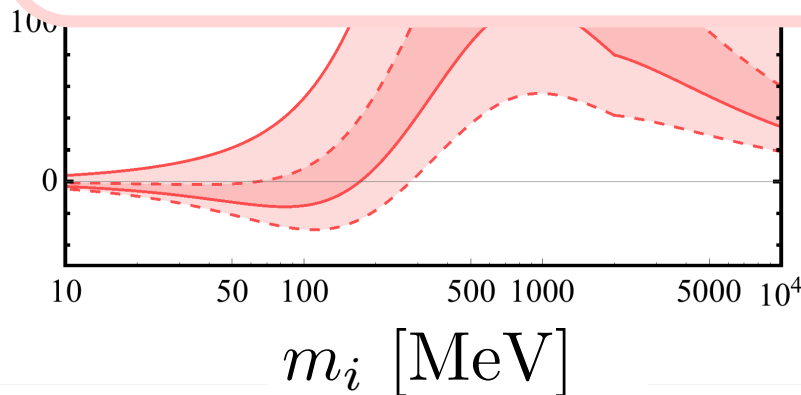
$$(\bar{u}_L \gamma^\mu d_L \times \bar{u}_R \gamma^\mu d_R) \bar{e}_L \gamma_\mu \nu$$



Standard Interactions vs Non-standard Interactions (dim = 6)

* Leptoquark Model

(Normal hierarchy is assumed)



- Not discussed in literature
- Large uncertainty in LECs

LECs

3+1 scenario

One sterile neutrino : m_4

$$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$$

* Standard interactions

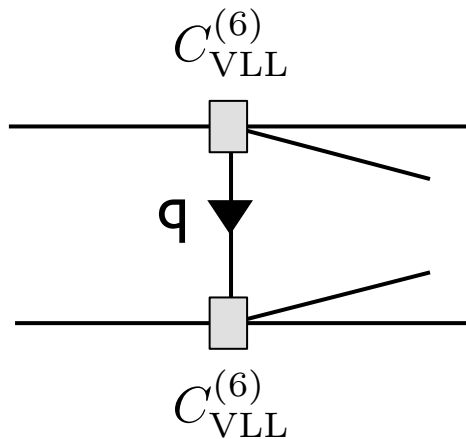
Mass matrix : $(M_\nu)_{i4,4i} \neq 0$

$$M_\nu = \begin{pmatrix} 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ M_D^* & M_D^* & M_D^* & M_R \end{pmatrix} \begin{matrix} \text{Yukawa} \\ \text{Majorana} \end{matrix}$$

3+1 scenario

One sterile neutrino : m_4

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu_i \quad C_{\text{VLL}}^{(6)} = -2V_{ud} U_{ei}$$



$$q \sim O(100)\text{MeV}$$

For $q^2 \gg m_i^2$

$$\sim \frac{m_i}{q^2} U_{ei}^2 \left(1 + \frac{m_i^2}{q^2} + \dots \right)$$

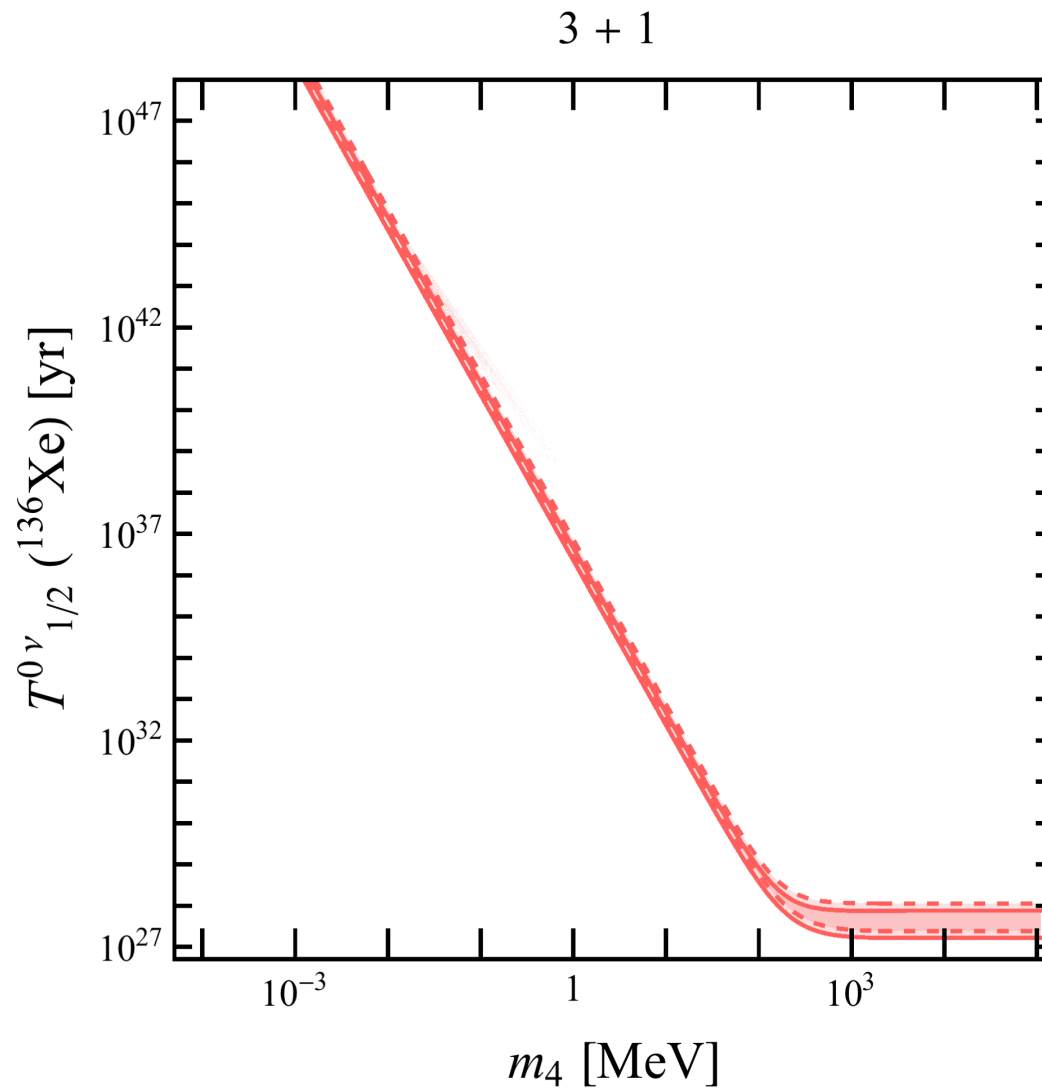


LO vanishes

$$m_i U_{ei}^2 = (M_\nu)_{11} = 0$$

* Cancellation of LO contribution in light-mass region

m_4 vs Half-life (^{136}Xe)



3+1 Standard case : The half-life is well above experimental reach.

3+1 Leptoquark

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 87, 075004 (2013)

I. Dorsner, S. Fajfer, A. Greljo, J. F. Kamenik and N. Kosnik, Phys. Rept. 641, 1 (2016)

26

Leptoquark (LQ) couples to the SM quark and lepton

+ one sterile neutrino

3+1 Leptoquark

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 87, 075004 (2013)

I. Dorsner, S. Fajfer, A. Greljo, J. F. Kamenik and N. Kosnik, Phys. Rept. 641, 1 (2016)

27

Leptoquark (LQ) couples to the SM **quark** and **lepton**

+ **one sterile neutrino**

Scalar LQ : $\tilde{R}(\mathbf{3}, \mathbf{2}, 1/6)$

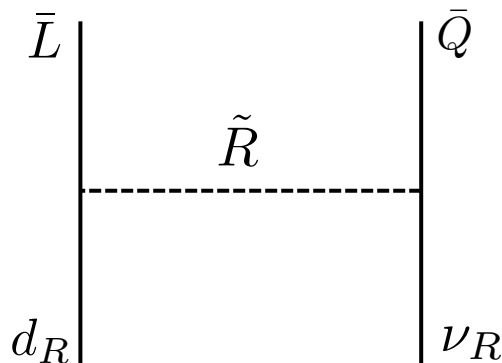
$$\mathcal{L}_{\text{LQ}} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$

Leptoquark (LQ) couples to the SM **quark** and **lepton**

+ **one sterile neutrino**

Scalar LQ : $\tilde{R} (\mathbf{3}, \mathbf{2}, 1/6)$

$$\mathcal{L}_{\text{LQ}} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$



Gauge-invariant dim6 operator:

$$\mathcal{L}_{\nu_R}^{(6)} = C_{LdQ\nu}^{(6)} (\bar{L} d_R) \epsilon (\bar{Q} \nu_R)$$

$$C_{LdQ\nu}^{(6)} = \frac{1}{m_{\text{LQ}}^2} y^{\overline{LR}} y^{RL*}$$

3+1 Leptoquark

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 87, 075004 (2013)

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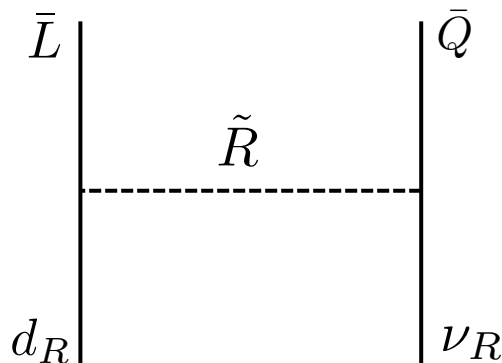
29

Leptoquark (LQ) couples to the SM quark and lepton

+ one sterile neutrino

Scalar LQ : $\tilde{R} (\mathbf{3}, \mathbf{2}, 1/6)$

$$\mathcal{L}_{\text{LQ}} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$



LQ parameters :

$$m_{\text{LQ}} = 10 \text{ TeV} \quad y^{\overline{LR}} y^{RL*} = 1.0$$

Scalar and tensor operators show up below EW scale:

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \left[\bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu_i + \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_L \sigma_{\mu\nu} C_{\text{TRR}}^{(6)} \nu_i \right]$$

$$C_{\text{SRR}}^{(6)} = 4C_{\text{TRR}}^{(6)} = \frac{v^2}{2} C_{LdQ\nu}^{(6)} U_{4i}^* \quad i = 1 \sim 4$$

Scalar and tensor operators show up below EW scale:

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \left[\bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu_i + \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_L \sigma_{\mu\nu} C_{\text{TRR}}^{(6)} \nu_i \right]$$

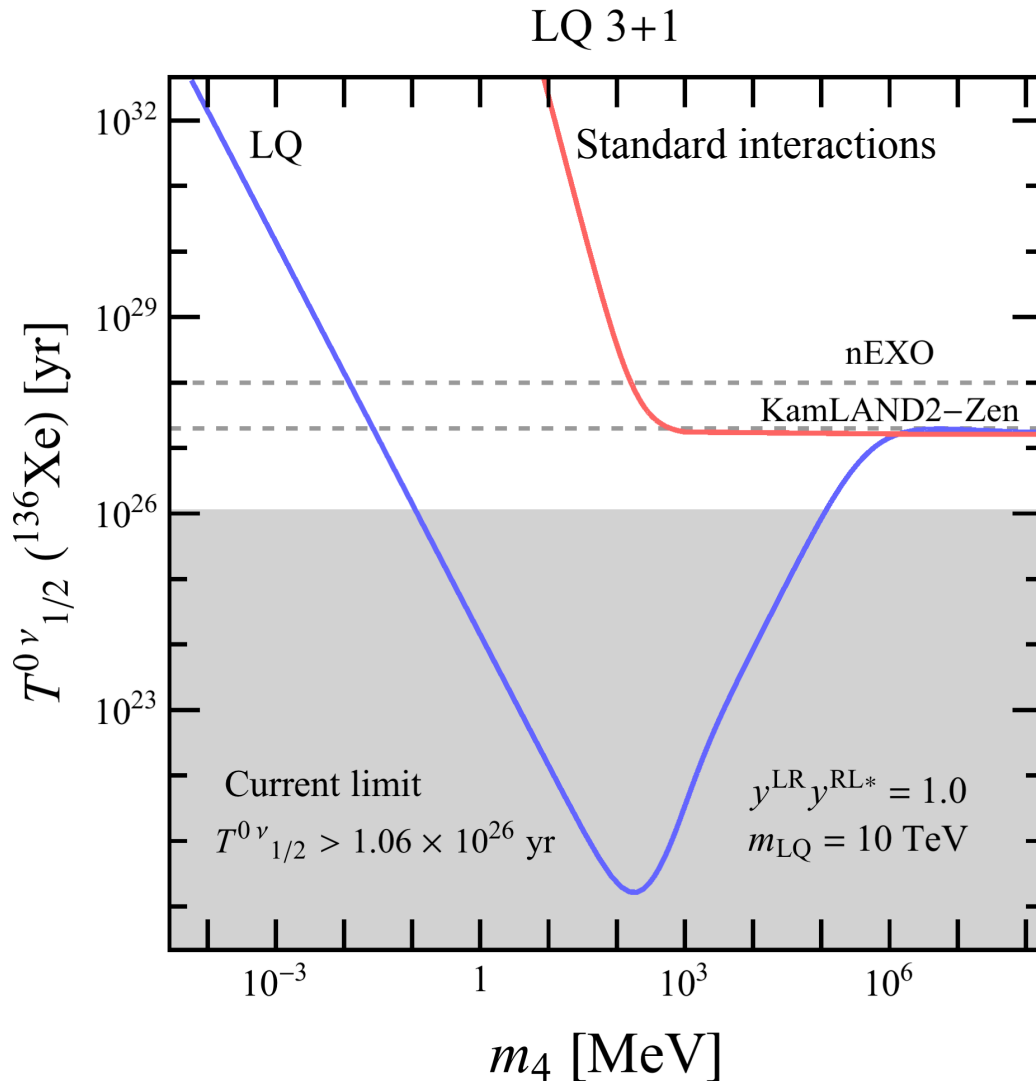
$$C_{\text{SRR}}^{(6)} = 4C_{\text{TRR}}^{(6)} = \frac{v^2}{2} C_{LdQ\nu}^{(6)} U_{4i}^* \quad i = 1 \sim 4$$

$$+ \frac{2G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu$$



Induced by
standard interaction
(No LQ interaction)

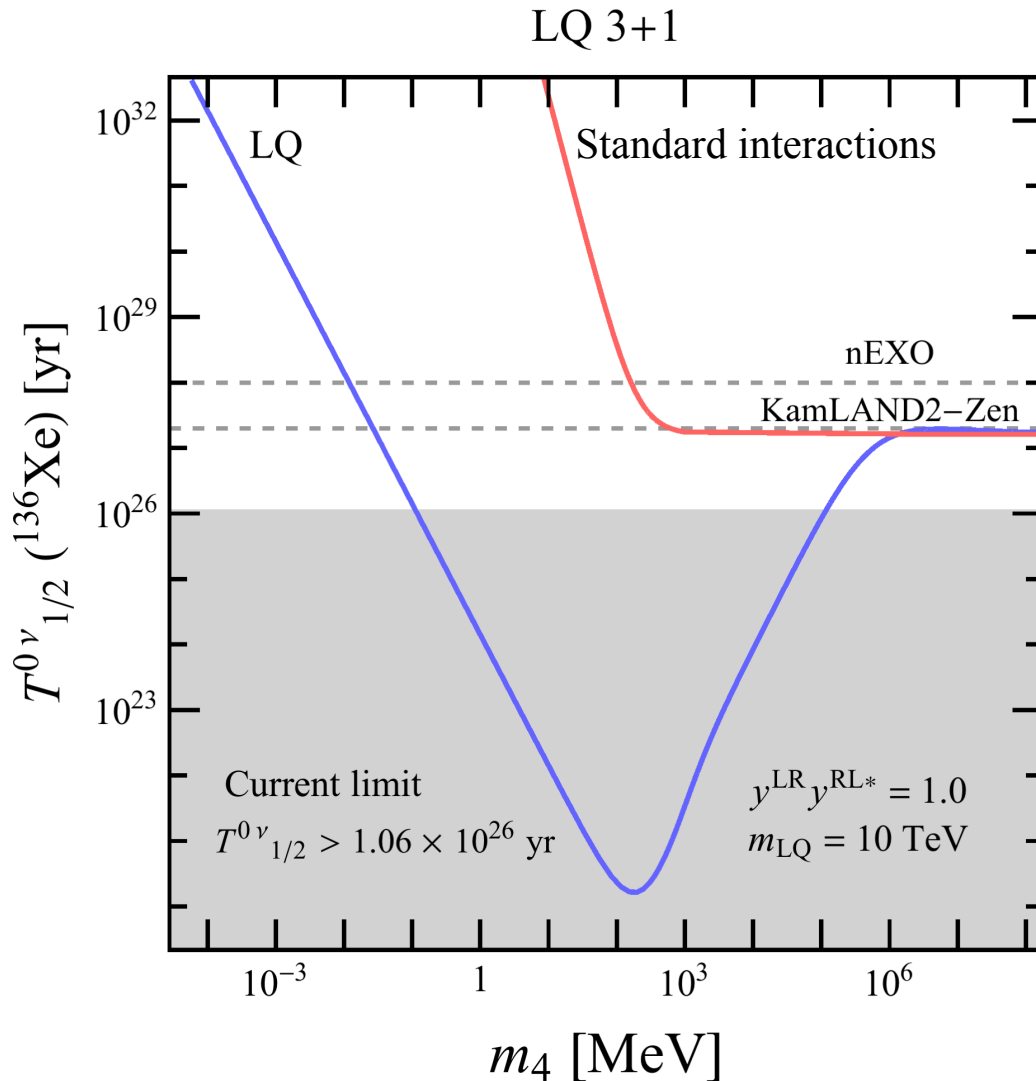
$$C_{\text{VLL}}^{(6)} = -2V_{ud} U_{ij} \quad i = 1 \sim 3, j = 1 \sim 4$$



Blue : LQ interaction

Pink : No LQ interaction
 (vector contribution)

* LQ interactions dominate
 over standard contributions.

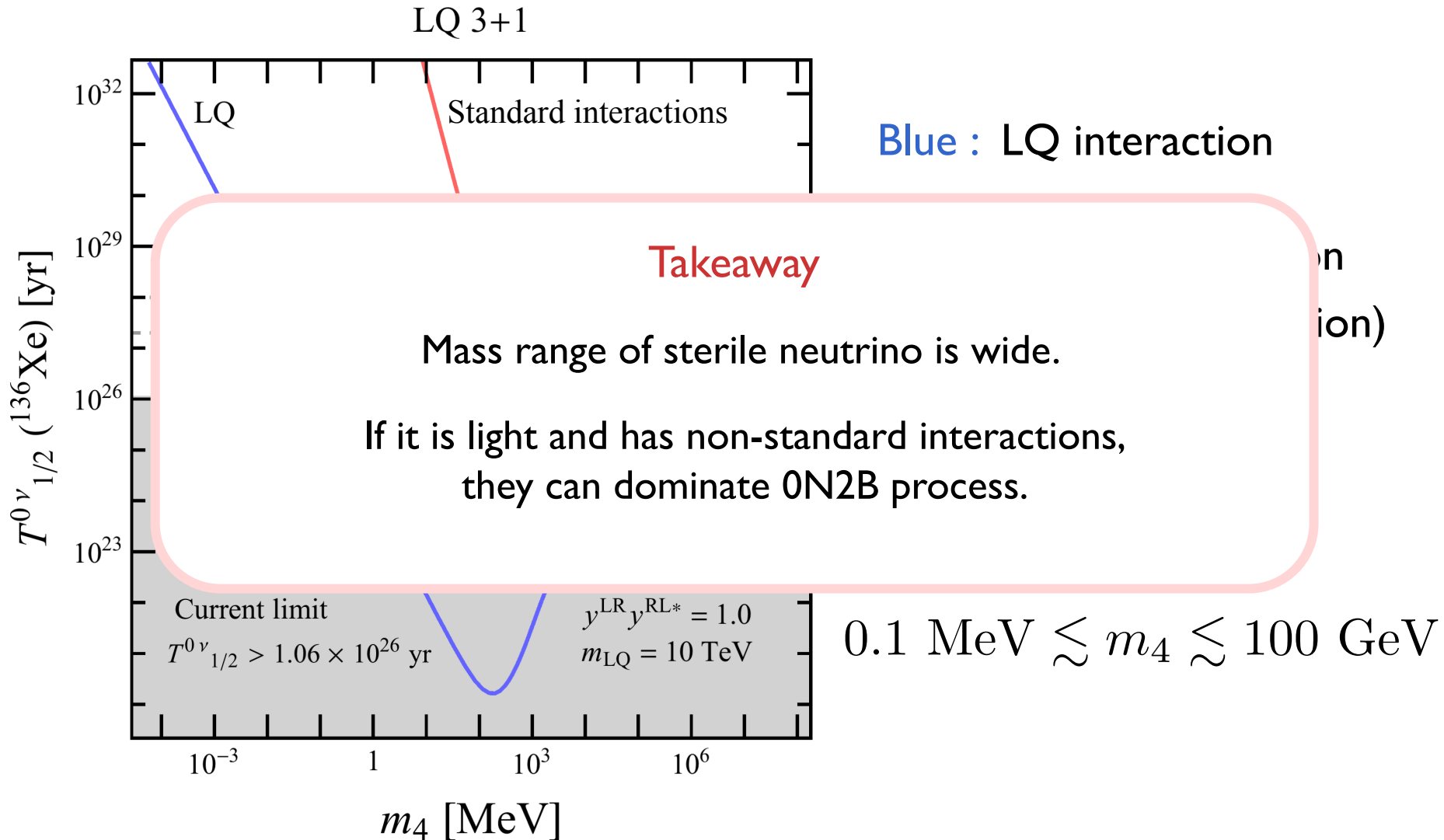


Blue : LQ interaction

Pink : No LQ interaction
(vector contribution)

Ruled out

$$0.1 \text{ MeV} \lesssim m_4 \lesssim 100 \text{ GeV}$$



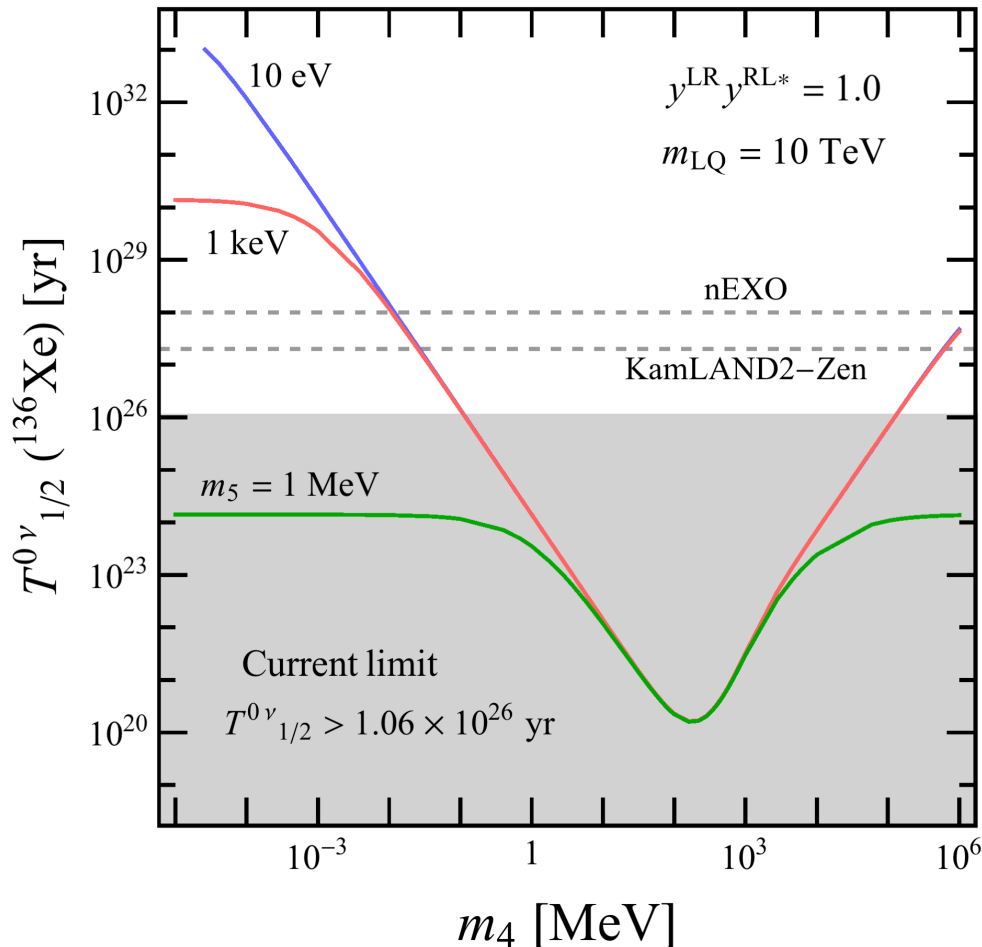
3+2 leptoquark

Two sterile neutrinos : m_4 and m_5

Oscillation parameters [PDG]PRD98, 030001(2018) and update (2019)

NH	$\Delta m_{21}^2 = 7.39 \times 10^{-5} \text{ [eV}^2\text{]}$	$\Delta m_{32}^2 = 2.5 \times 10^{-3} \text{ [eV}^2\text{]}$
	$\sin^2 \theta_{12} = 3.1 \times 10^{-1}$	$\sin^2 \theta_{13} = 2.241 \times 10^{-2}$
	$\sin^2 \theta_{23} = 5.58 \times 10^{-1}$	$\delta_{\text{Dirac}} = 1.23\pi$
IH	$\Delta m_{21}^2 = 7.39 \times 10^{-5} \text{ [eV}^2\text{]}$	$\Delta m_{32}^2 = -2.5 \times 10^{-3} \text{ [eV}^2\text{]}$
	$\sin^2 \theta_{12} = 3.1 \times 10^{-1}$	$\sin^2 \theta_{13} = 2.261 \times 10^{-2}$
	$\sin^2 \theta_{23} = 5.63 \times 10^{-1}$	$\delta_{\text{Dirac}} = 1.58\pi$
[3 + 2]	$\theta_{45} = \pi/8$	$m_{4,5} : \text{ free parameters}$
	$\gamma_{45} = 0.5$	Majorana phases = 0

LQ 3 + 2 : NH



Three choices of m_5 :

Blue : $m_5 = 10 \text{ eV}$

Pink : $m_5 = 1 \text{ keV}$

Green : $m_5 = 1 \text{ MeV}$

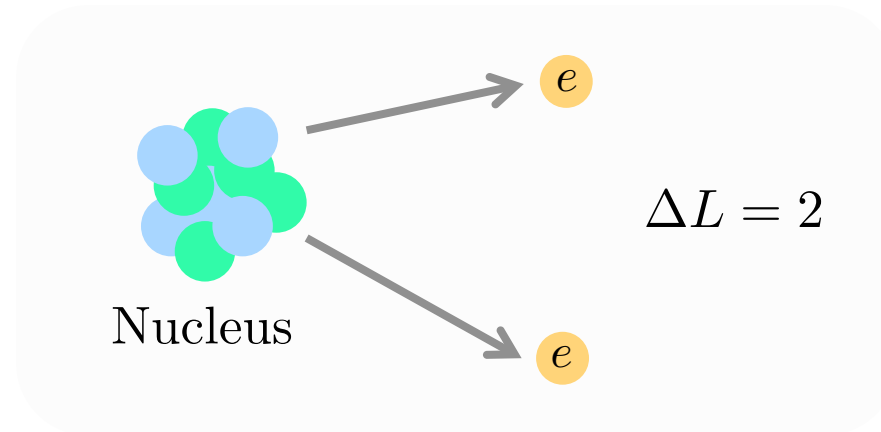
For the two light cases,

$0.1 \text{ MeV} \lesssim m_4 \lesssim 100 \text{ GeV}$

excluded.

Conclusion

★ Search for $0\nu 2\beta$ is a probe of Majorana mass.



Our study : Model-independent analysis with light ν_R

- Possible to analyze NDBD in any mass spectrum with interpolation formulae
- Non-standard interactions can dominate
- ✓ Applicable to phenomena involved in light sterile neutrinos (e.g., DM phenomenology and the BAU)