

# Jet substructure in heavy-ion collisions with energy correlators

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IGFAE, Universidade de Santiago de Compostela

Probing QCD at High Energy and Density with Jets  
INT, Seattle, USA  
October 16th, 2023

C. Andres, FD, R. K. Elayavalli, J. Holguin, C. Marquet, I. Moutl, [arXiv:2209.11236](https://arxiv.org/abs/2209.11236)

C. Andres, FD, J. Holguin, C. Marquet, I. Moutl, [arXiv:2303.03413](https://arxiv.org/abs/2303.03413)

C. Andres, FD, J. Holguin, C. Marquet, I. Moutl, [arXiv:2307.15110](https://arxiv.org/abs/2307.15110)



**IGFAE**

Instituto Galego de Física de Altas Enerxías

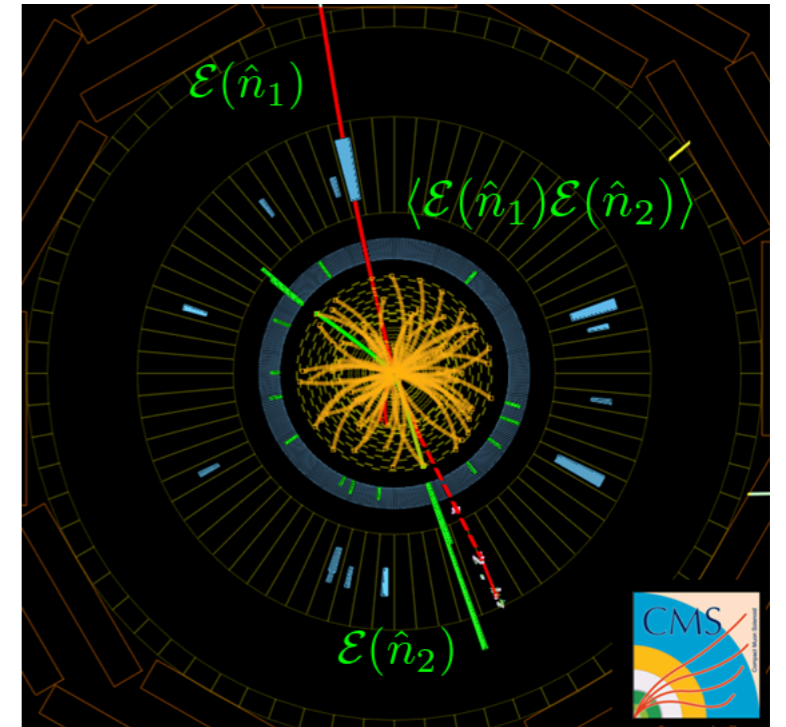
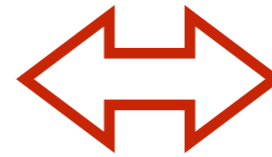
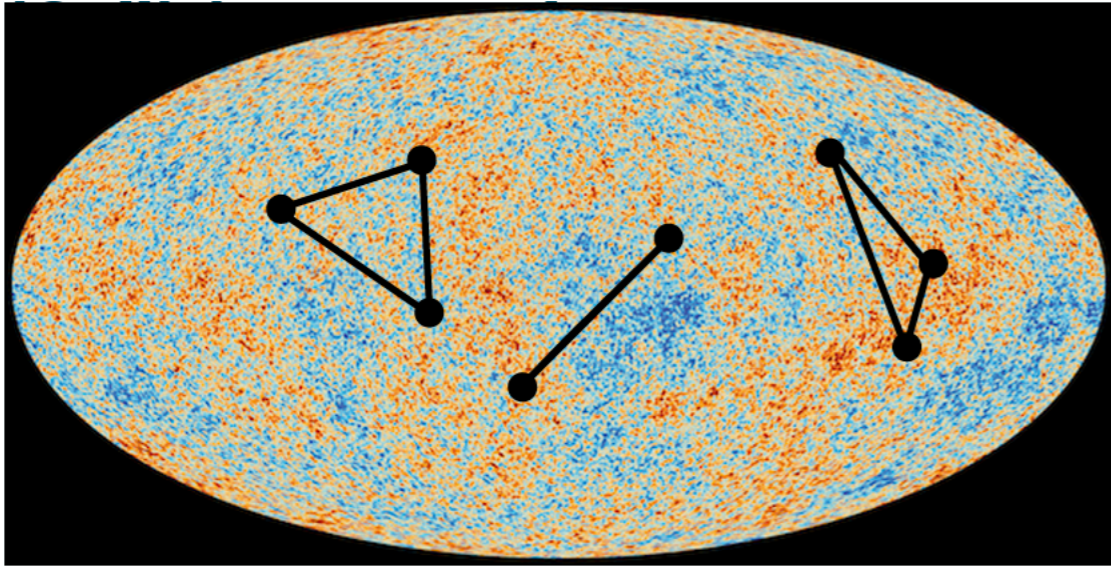


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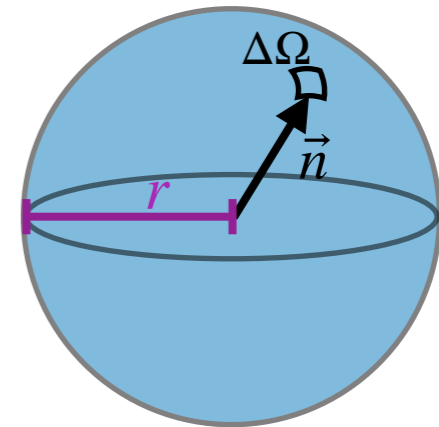
# Energy flux operators



- Correlations of asymptotic energy flux provide valuable information about the underlying theory

$$\mathcal{E}(\vec{n}) = \lim_{r \rightarrow \infty} \int_0^\infty dt r^2 n^i T_{0i}(t, r\vec{n})$$

$$\mathcal{E}(\vec{n})|X\rangle = \sum_a E_a \delta^{(2)}(\Omega_{\vec{p}_a} - \Omega_{\vec{n}}) |X\rangle$$



# Energy correlators

- 2-point function

$$\frac{\langle \mathcal{E}^n(\vec{n}_1) \mathcal{E}^n(\vec{n}_2) \rangle}{Q^{2n}} = \frac{1}{\sigma} \sum_{ij} \int \frac{d\sigma_{ij}}{d\vec{n}_i d\vec{n}_j} \frac{E_i^n E_j^n}{Q^{2n}} \delta^{(2)}(\vec{n}_i - \vec{n}_1) \delta^{(2)}(\vec{n}_j - \vec{n}_2)$$

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Hard scale of the process

- Due to rotational symmetry, the only relevant variable is the opening angle

$$\frac{d\Sigma^{(n)}}{d\theta} = \int d\vec{n}_{1,2} \frac{\langle \mathcal{E}^n(\vec{n}_1) \mathcal{E}^n(\vec{n}_2) \rangle}{Q^{2n}} \delta(\vec{n}_2 \cdot \vec{n}_1 - \cos \theta)$$

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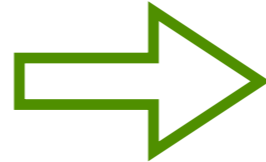
- Can be expressed as a weighted average of the double-inclusive cross-section

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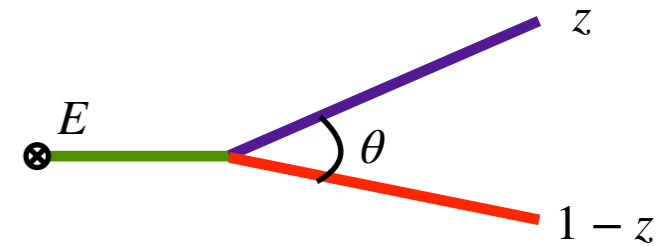
# Energy correlators in vacuum

- At leading order

$$\frac{d\sigma_{qg}^{\text{vac}}}{d\theta dz} = \frac{\alpha_s C_F \sigma}{\pi} \frac{1 + (1 - z)^2}{z \theta}$$



$$\frac{d\Sigma^{(1)}}{d\theta} \sim \frac{1}{\theta}$$

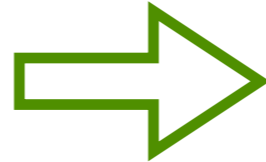




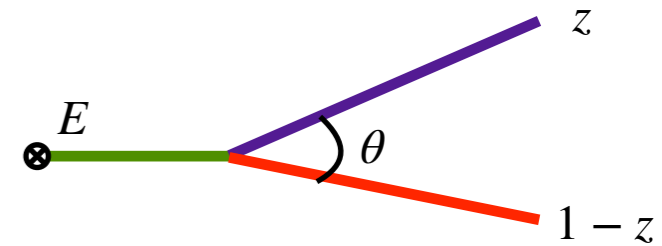
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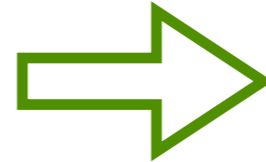


- For jets we are interested in the collinear (or OPE) limit

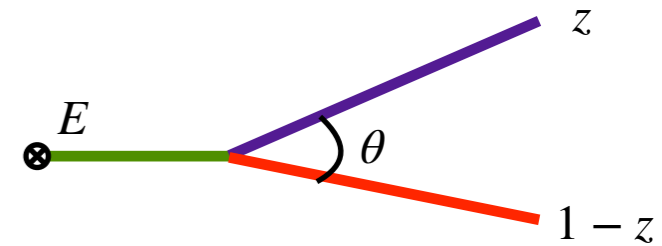
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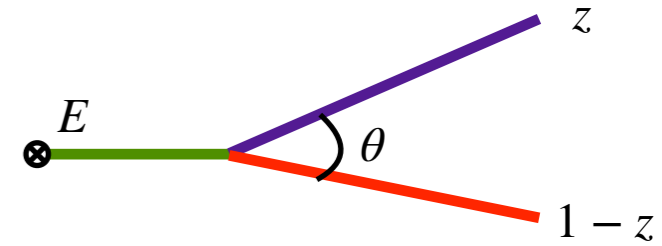


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$$\mathcal{O}(x)\mathcal{O}(y) \xrightarrow{x \rightarrow y} \sum_i |x - y|^{\gamma_i} c_i \mathcal{O}_i$$

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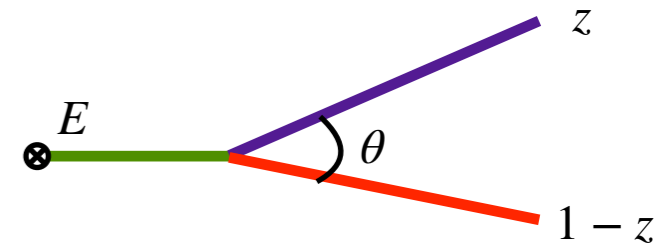
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Light-ray OPE

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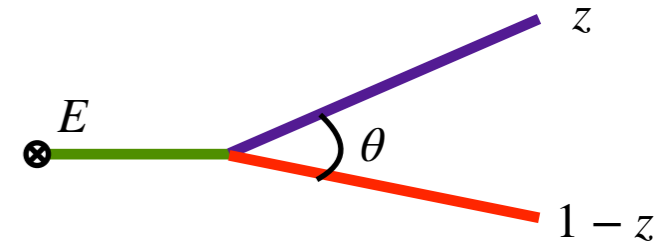
In a CFT:

$$\frac{d\Sigma^{(1)}}{d\theta} \sim \frac{1}{\theta^{1-\gamma(3)}}$$

$\gamma(3)$  is the twist-2 spin-3  
QCD anomalous dimension

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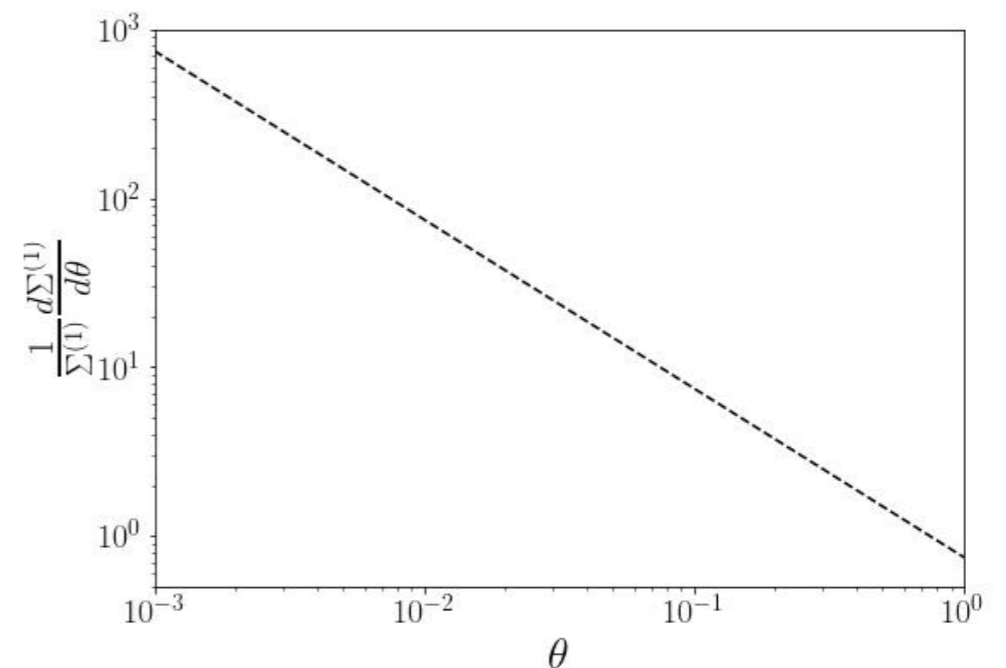
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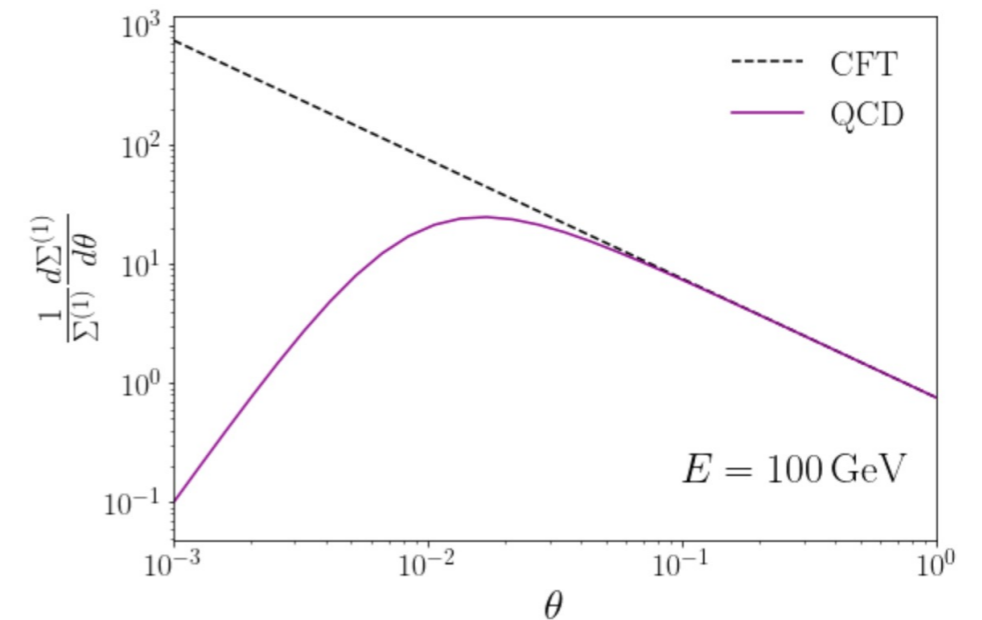
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# Energy correlators in vacuum

P. T. Komiske, I. Moutt, J. Thaler, H. X. Zhu [2201.07800](#)

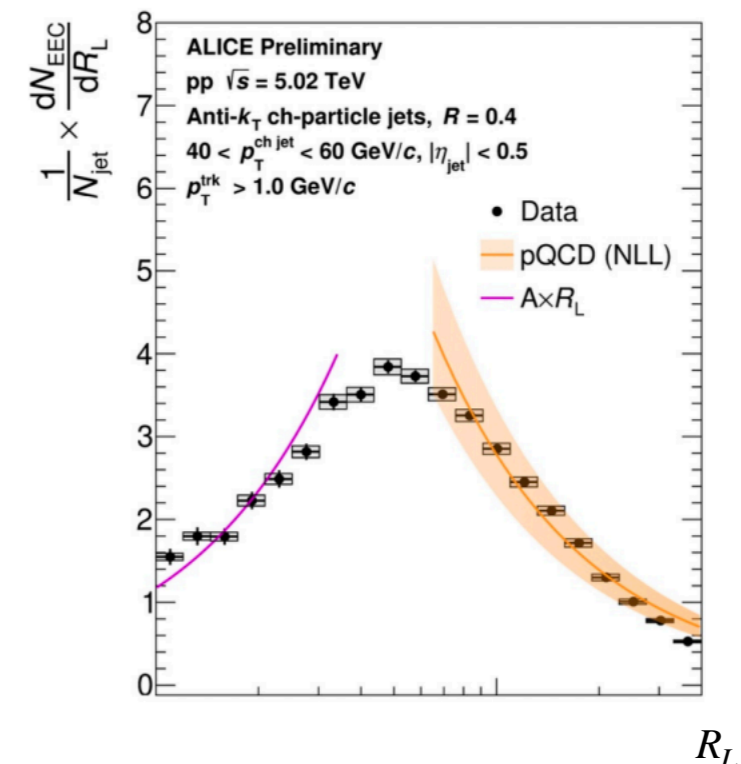
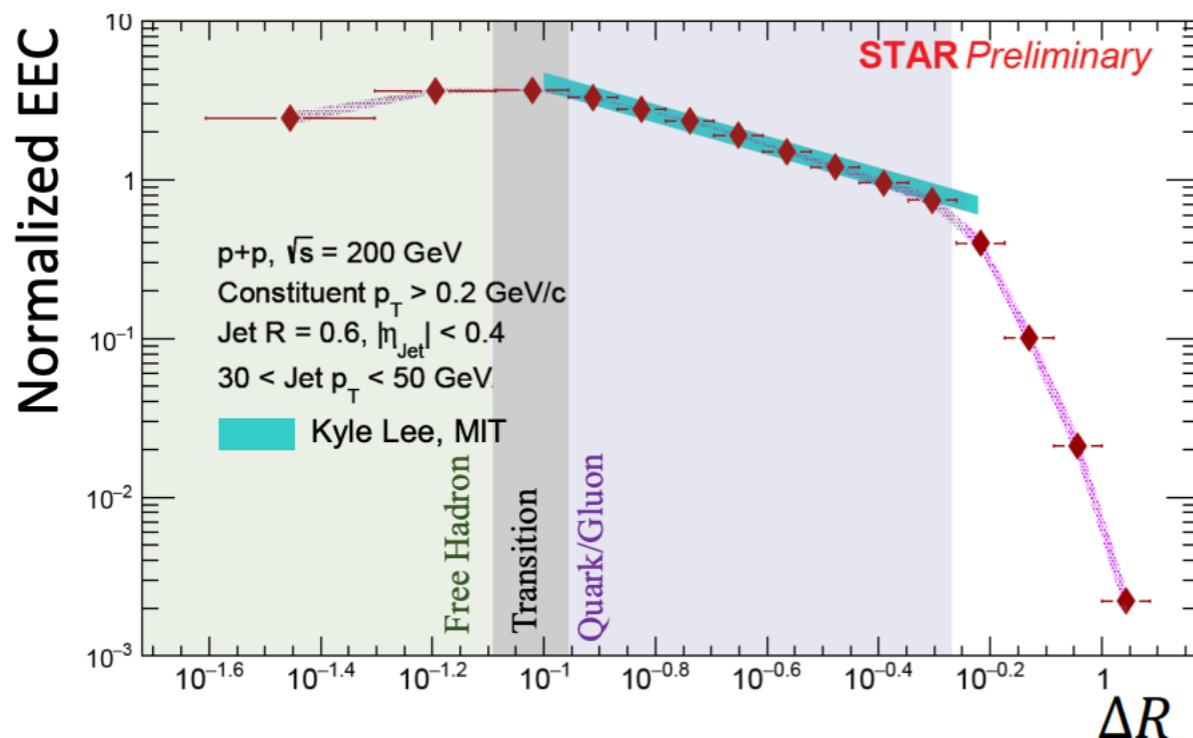
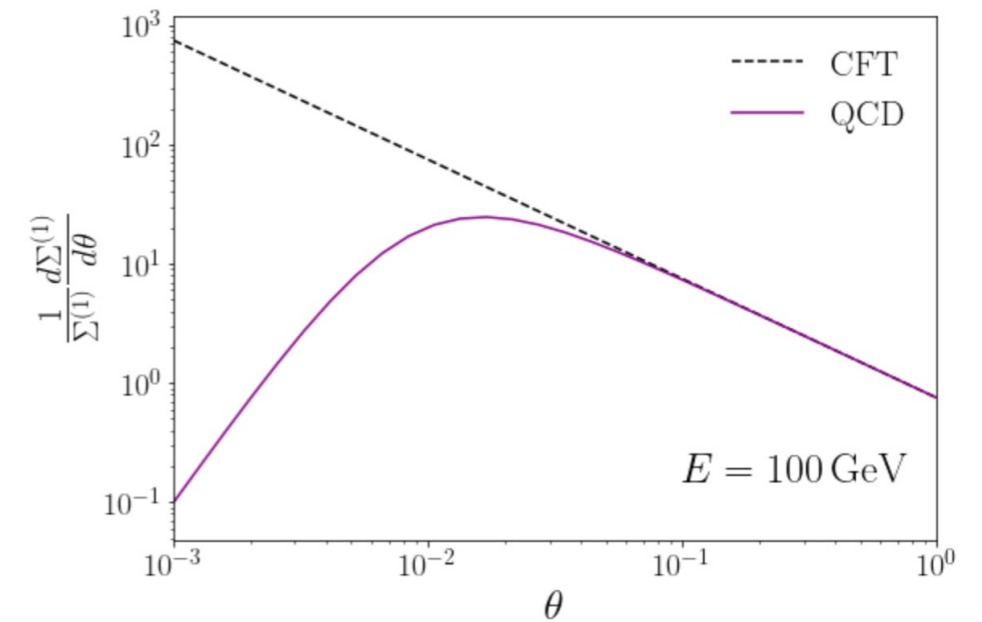
- QCD is not conformal
- Confinement scale brakes power law behavior at angles below  $\Lambda_{\text{QCD}}/E$ 
  - ✦ Small angles correspond to large times, where hadronization is dominant
  - ✦ Larger angles correspond to early times



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# EECs from massive jets

- Dead-cone effect: radiation from heavy quarks is suppressed at small angles

$$\frac{d\sigma_M^{\text{vac}}}{d\theta dz} \sim \frac{\theta^3}{\left(\theta^2 + \frac{\theta_0^2}{1-z}\right)^2} \frac{d\sigma^{\text{vac}}}{d\theta dz}$$

Dead-cone angle!

$$\theta_0 = \frac{M}{E}$$



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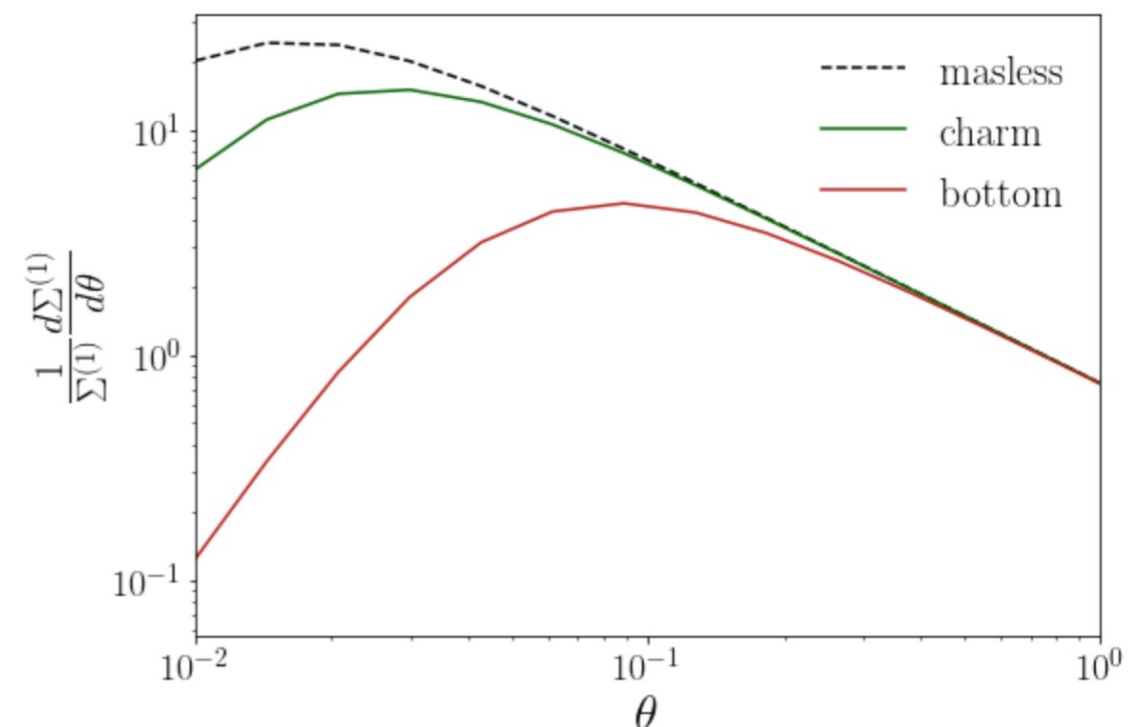
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Dead-cone angle!

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- Deviation from power-law behavior occurs at the dead-cone angle in the perturbative regime
- In the massless case, the transition to the non-perturbative regime can be modeled by putting a gluon mass



# Energy correlators in HIC

- pp baseline understood to a very high degree of accuracy in the perturbative regime
- Less sensitive to soft physics than other observables, better for higher powers of the energy weighting
- Being an inclusive observable, it is insensitive to large logs from soft divergences
- No need for de-clustering

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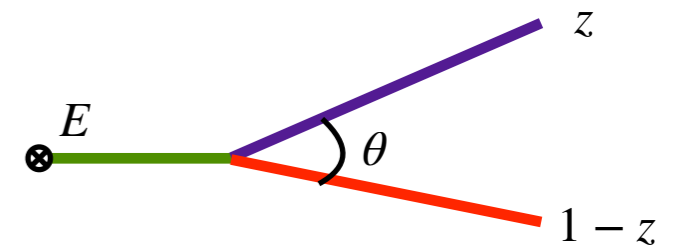
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Allows us to isolate the modification of the hard splittings

# Contribution from the QGP

- For simplicity, we consider a quark initiated jet where the initial energy is known ( $\gamma/Z$ -jet)
- Energy loss effects are subleading

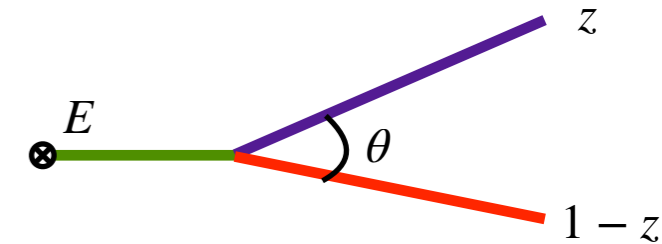
$$\frac{d\Sigma^{(n)}}{d\theta} = \frac{1}{\sigma_{qg}} \int dz \left( \frac{d\sigma_{qg}^{\text{vac}}}{d\theta dz} + \frac{d\sigma_{qg}^{\text{med}}}{d\theta dz} \right) z^n (1-z)^n + \mathcal{O}\left(\frac{\mu_s}{E}\right)$$



- The presence of the medium is not expected to affect the non-perturbative regime at very small angles, given that it corresponds to late emissions occurring outside of the medium

Evaluation of in-medium splittings must go beyond the soft limit  $z \rightarrow 0$

# Evaluation of in-medium splittings



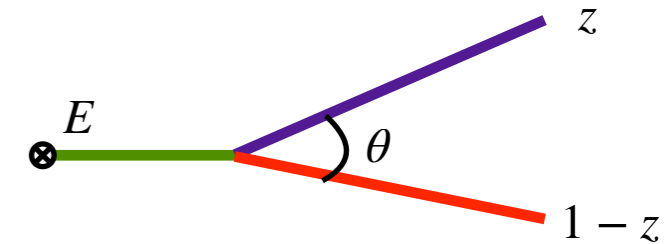
- Most calculations of medium modifications and MCs restricted to the soft limit
- Only recently, there have been some advances in the full calculation of medium-modified splittings  
[Isaksen, Tywoniuk 2303.12119](#)
- Two available approximations:
  - ♦ Opacity expansion ( $N = 1$ )
    - ★ Unitarity problems can lead to negative cross sections
    - ★ Recursive formulas to generate all orders (not yet implemented numerically)
  - ♦ Semi-hard approximation
    - ★ Resums multiple scatterings in the eikonal approximation through Wilson lines in straight-line trajectories
    - ★ Assumes semi-hard splittings ( $z$  not too small)
    - ★ Neglects effects coming from broadening of transverse momenta of produced particles

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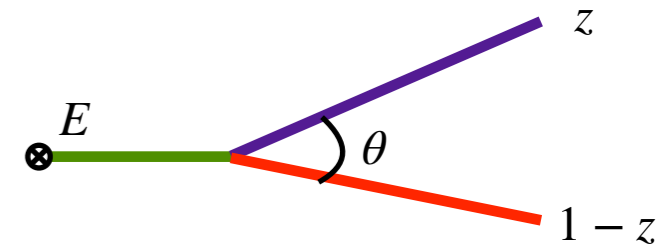
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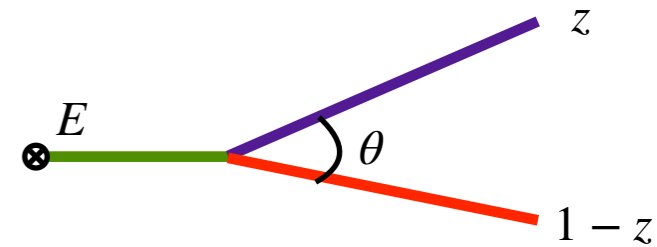
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- For a static medium of length  $L$  within the harmonic approximation with jet quenching parameter  $\hat{q}$  one can read off the relevant scales directly from the formulas





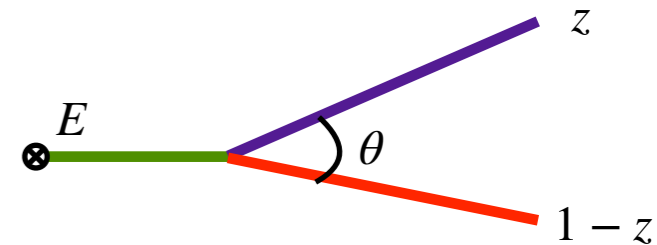
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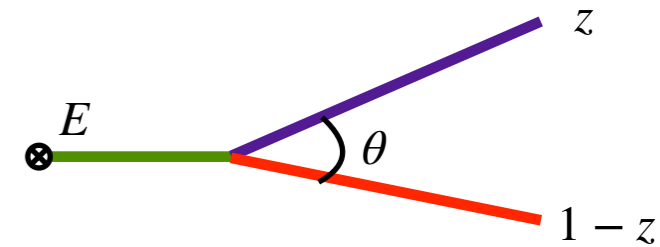
$$t_f = \frac{2}{z(1-z)E\theta^2}$$



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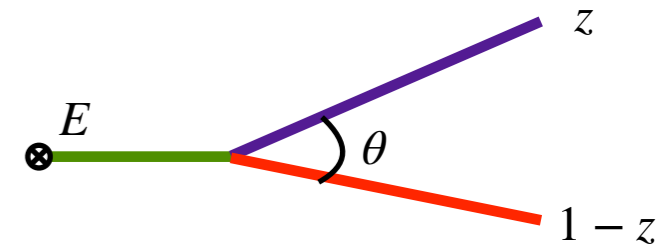
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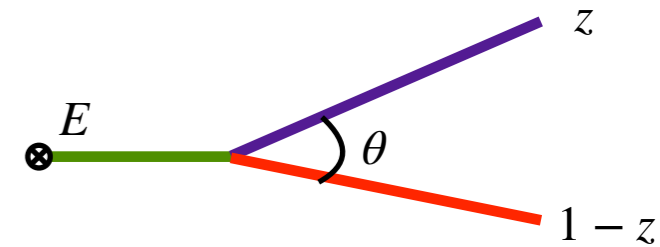
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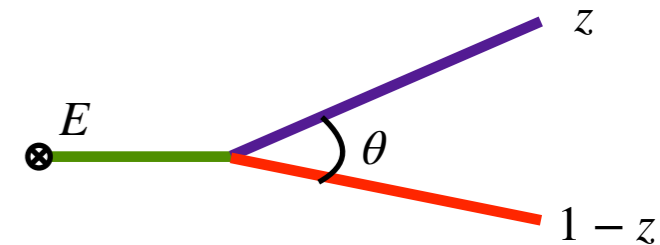
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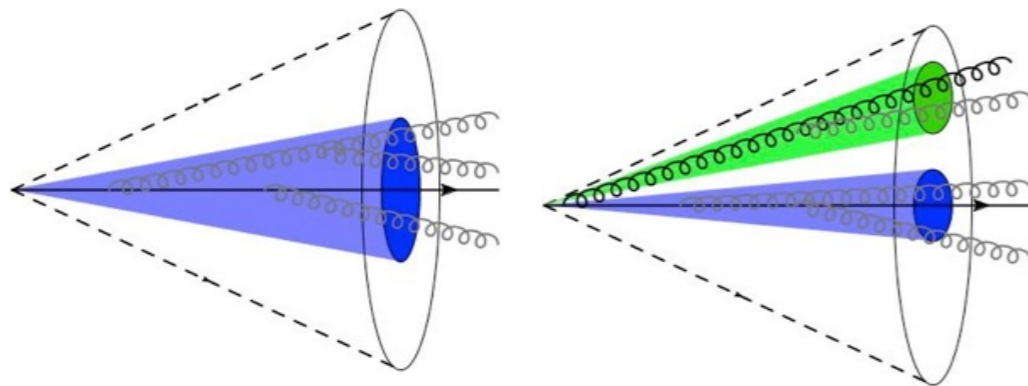
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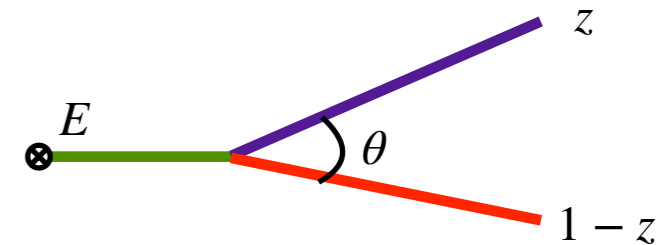
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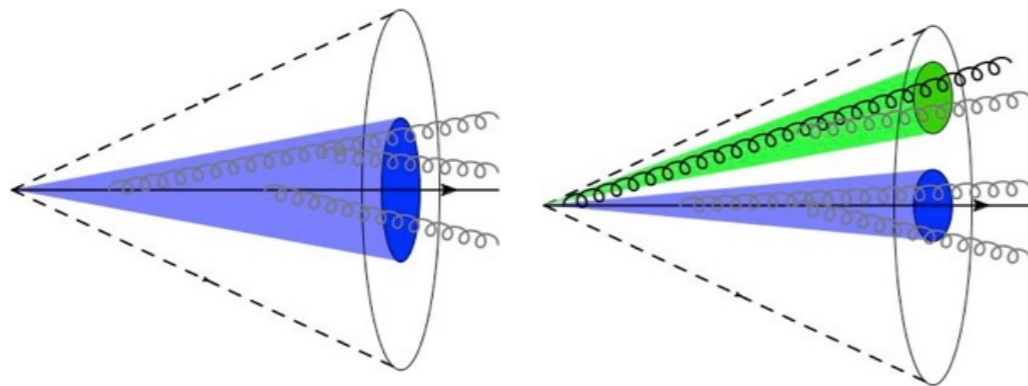
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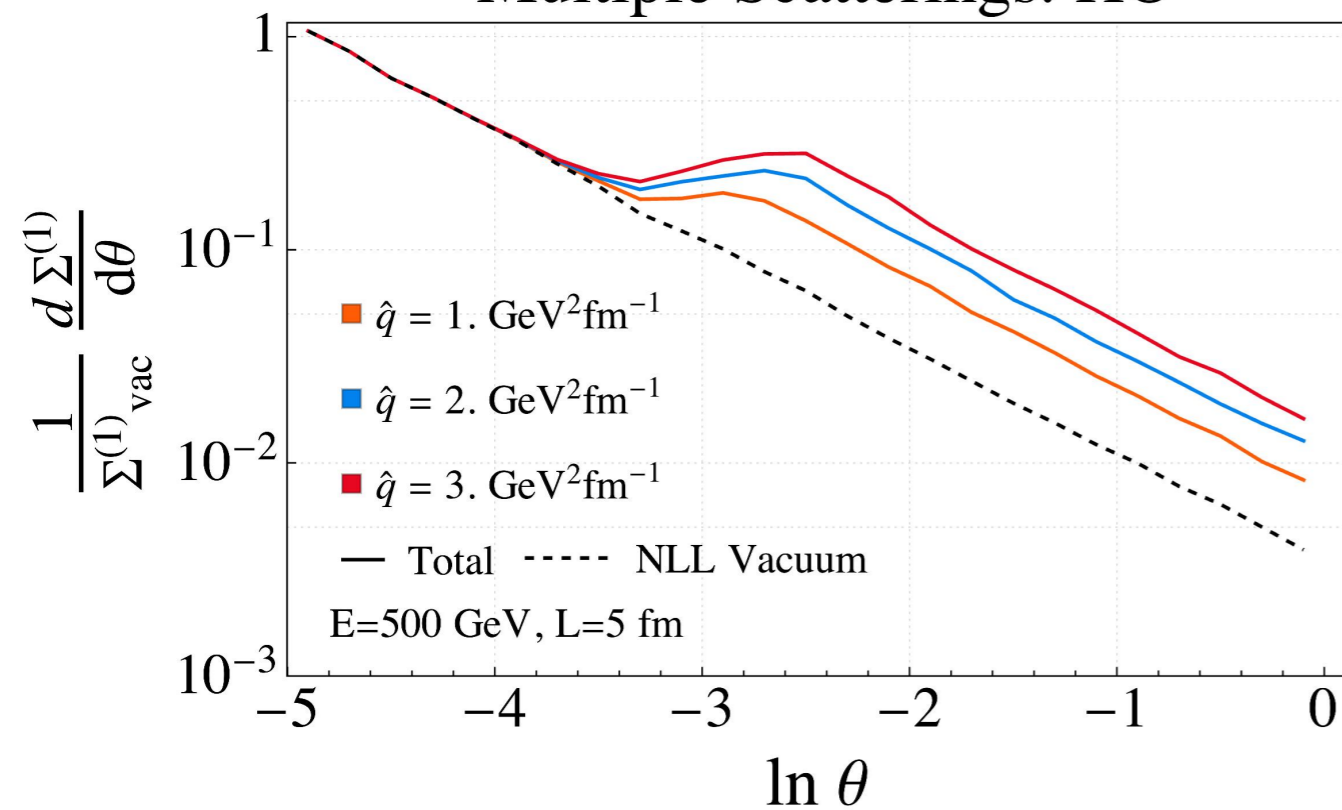
If  $\theta_L > \theta_c$  then  $\theta_c$  becomes irrelevant

# Results HO

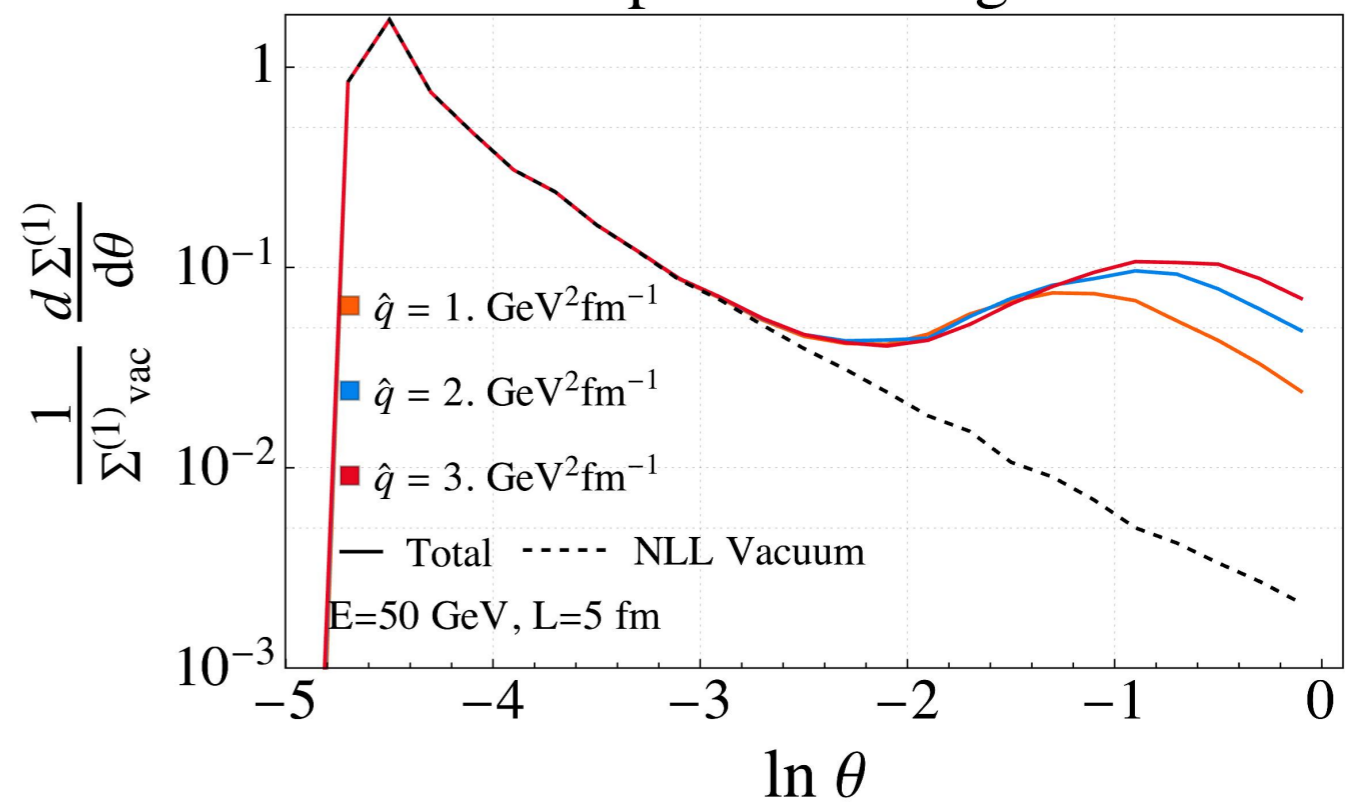
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Two-Point Energy Correlator  
Multiple Scatterings: HO



Two-Point Energy Correlator  
Multiple Scatterings: HO



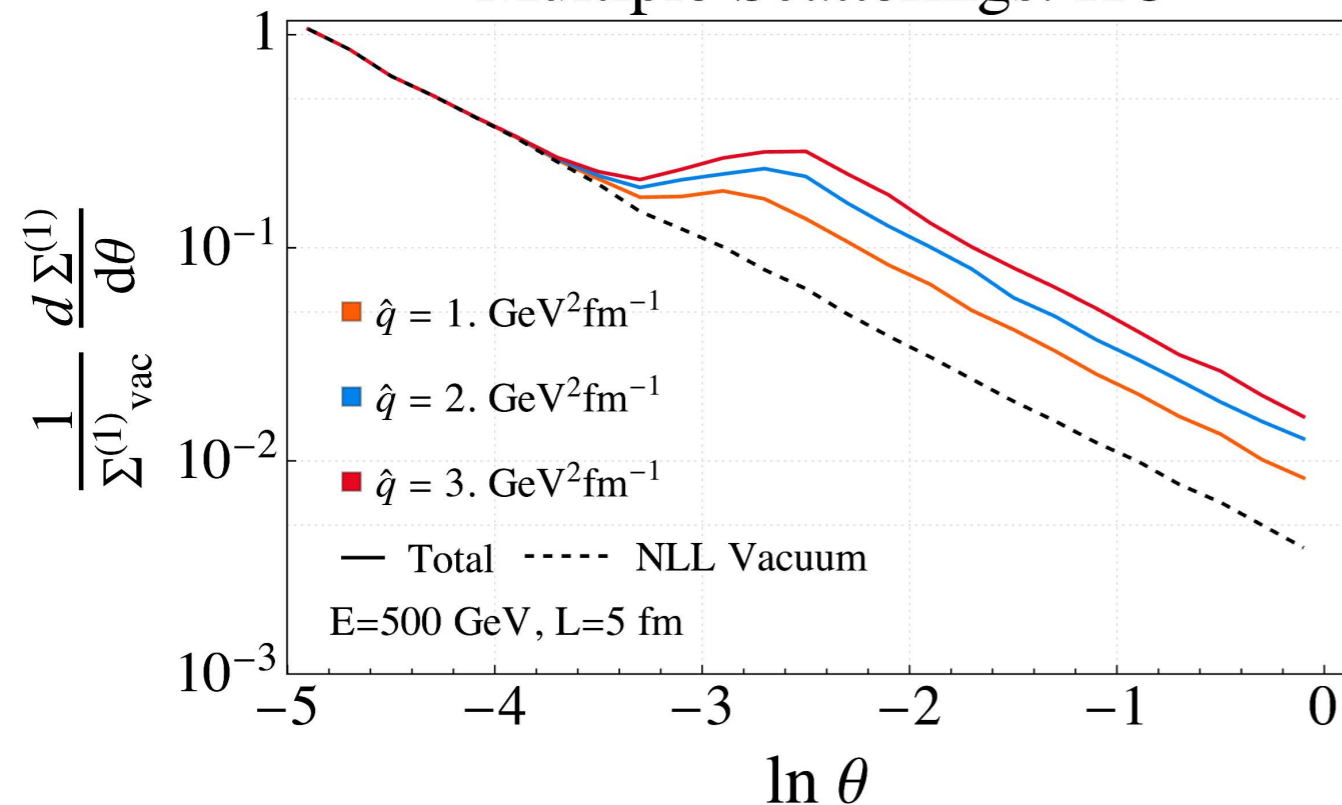
C. Andres, FD, R. K. Elayavalli, J. Holguin, C. Marquet, I. Moutl, [arXiv:2209.11236](https://arxiv.org/abs/2209.11236)  
 C. Andres, FD, J. Holguin, C. Marquet, I. Moutl, [arXiv:2303.03413](https://arxiv.org/abs/2303.03413)

# Results HO

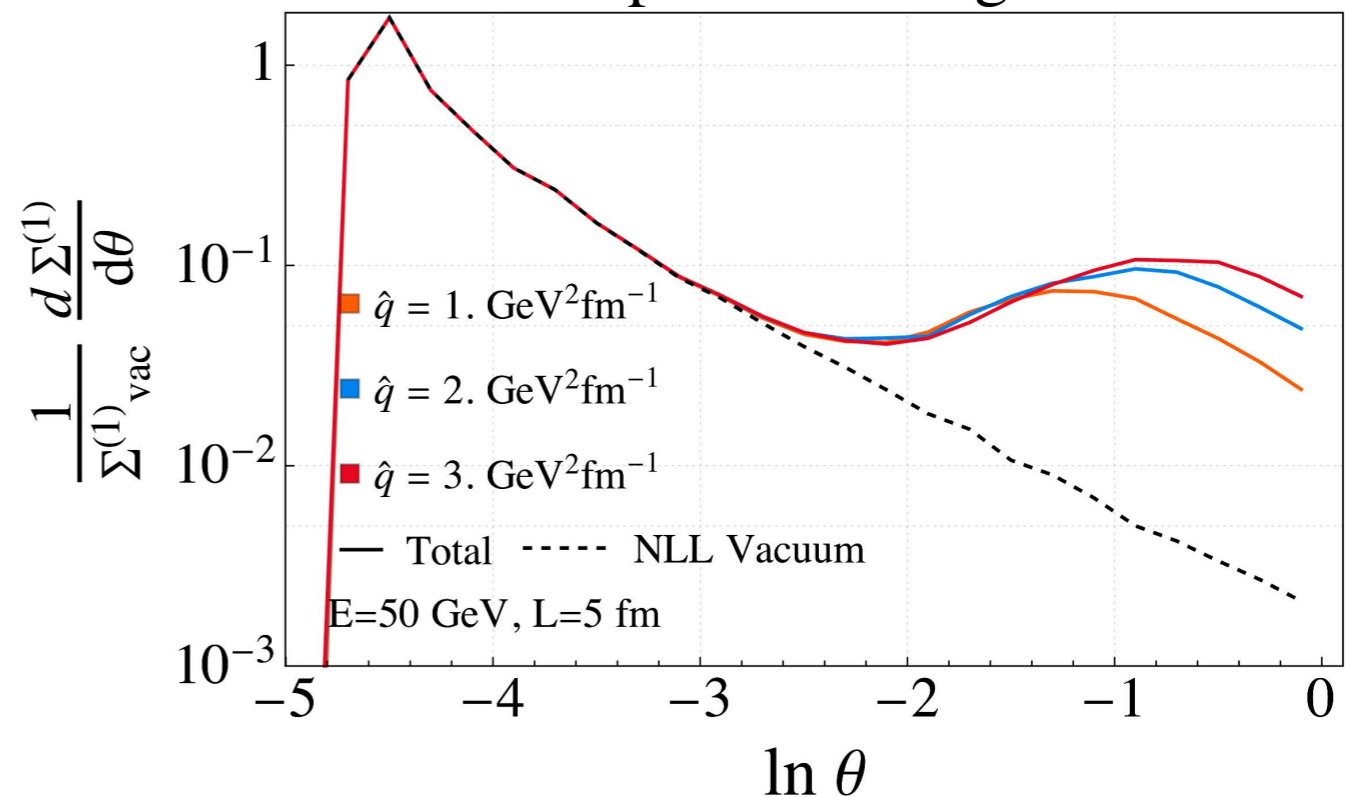
$$\theta_c > \theta_L$$

$$\theta_c < \theta_L$$

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Multiple Scatterings: HO



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- No enhancement at small angles as expected

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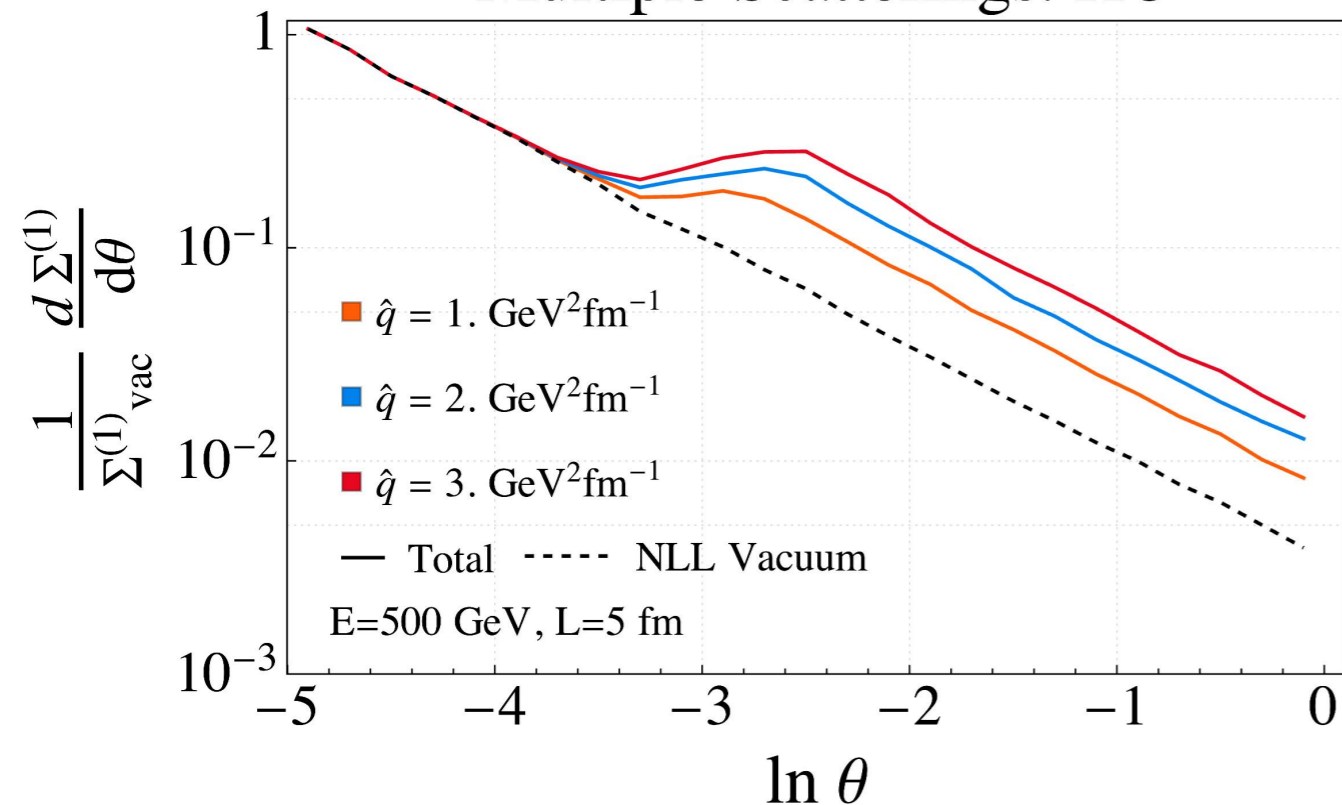


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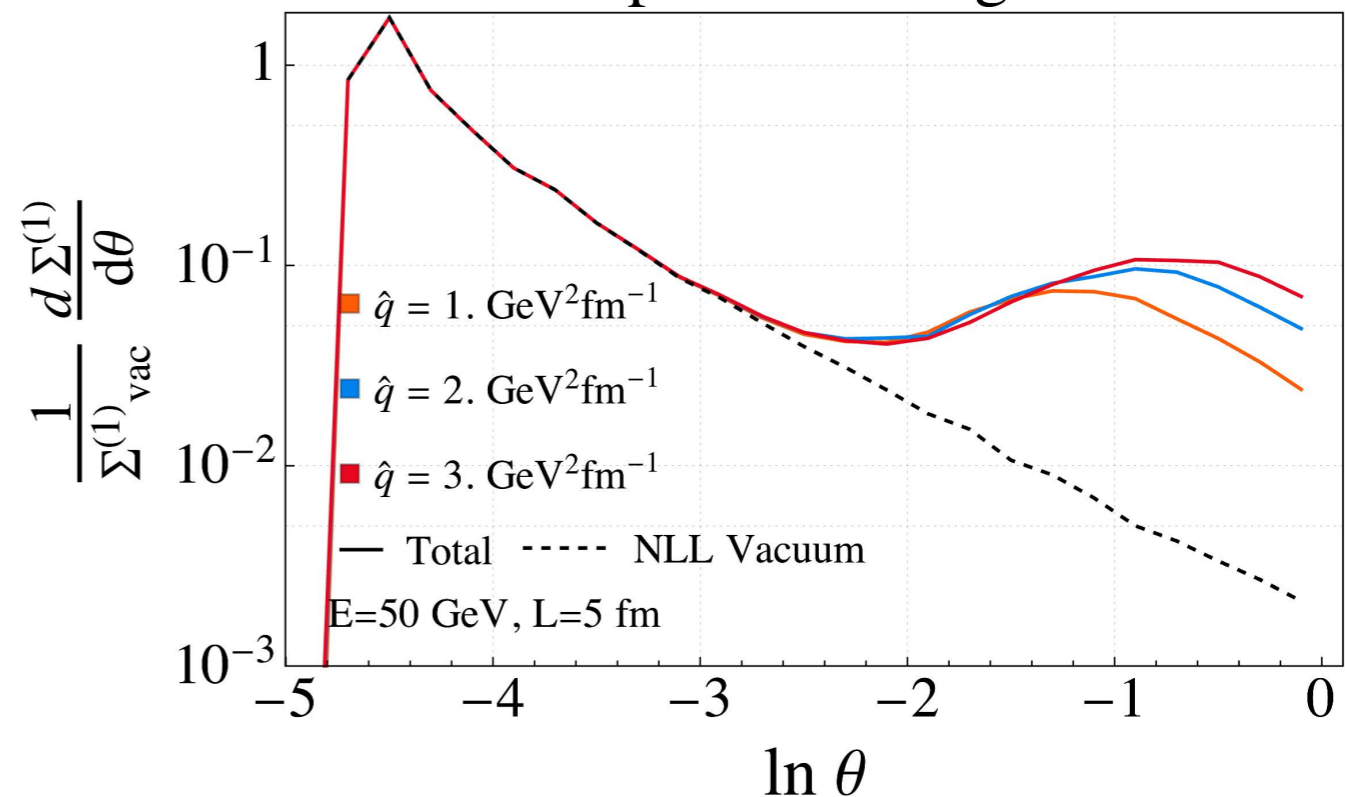
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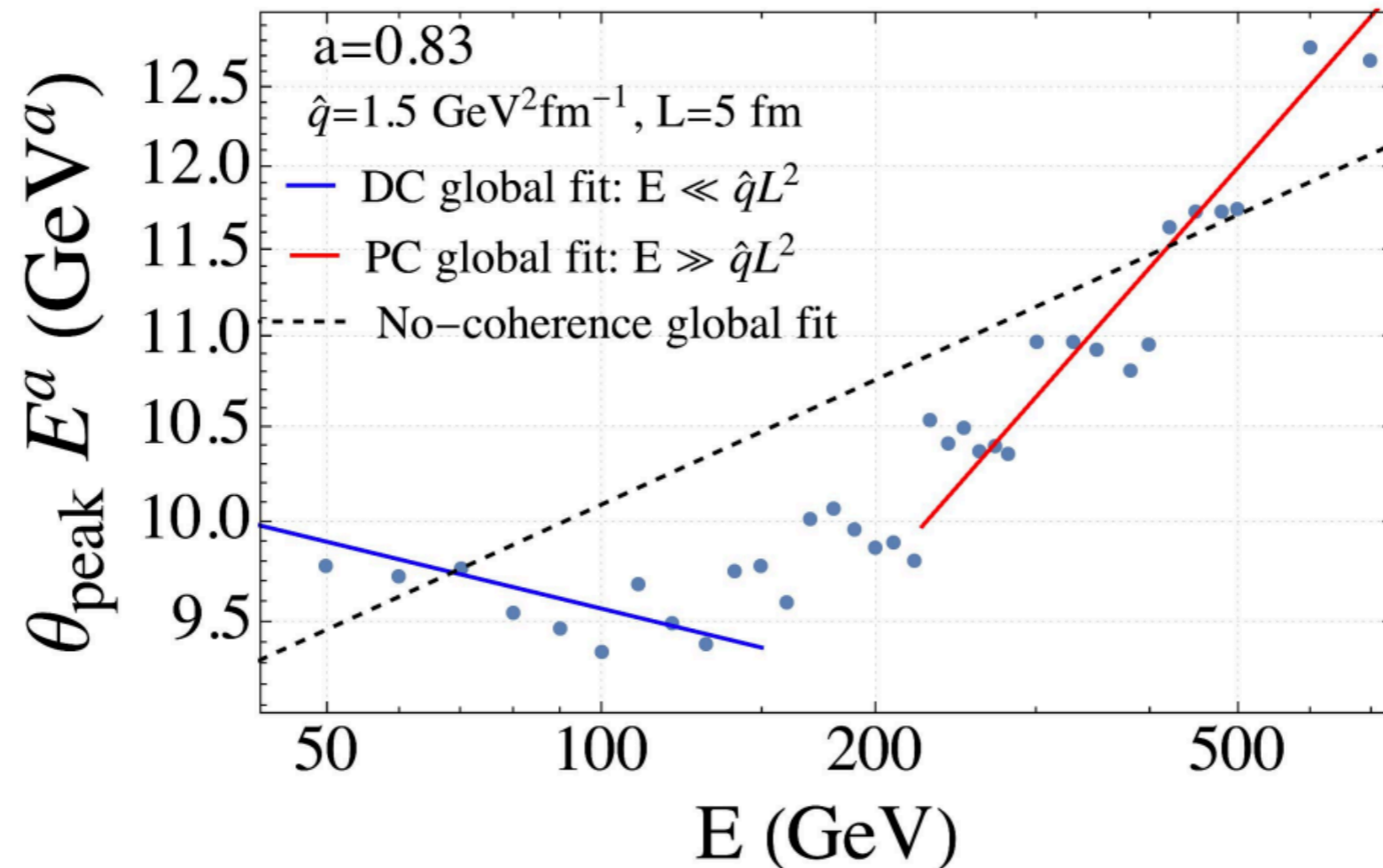


- No enhancement at small angles as expected
- Varying  $\hat{q}$  has different effects in the two regions

C. Andres, FD, R. K. Elayavalli, J. Holguin, C. Marquet, I. Moult, [arXiv:2209.11236](https://arxiv.org/abs/2209.11236)

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# Coherence transition

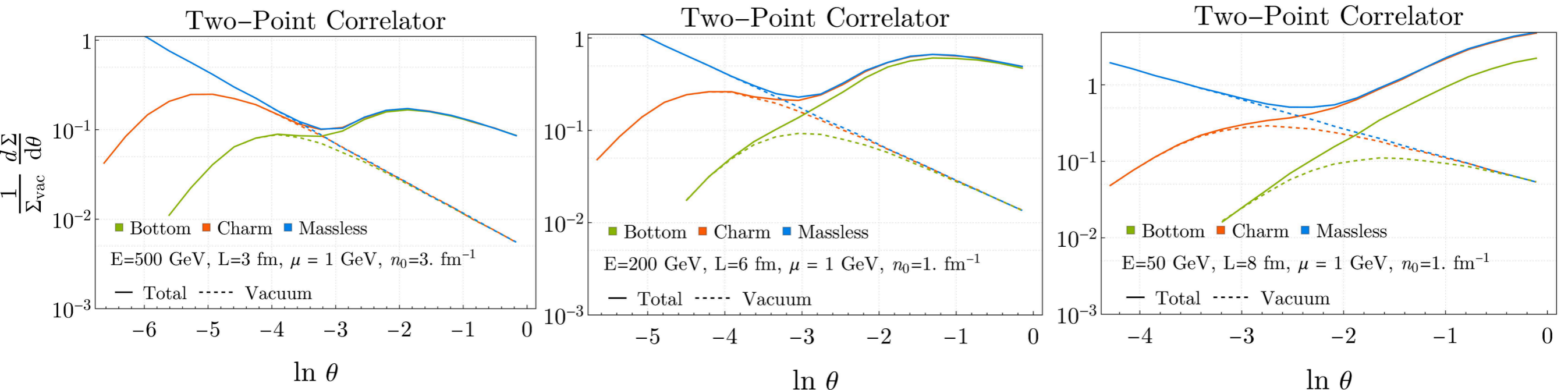


- Extracted the peak angle  $\theta_{\text{peak}}$  for 332 sets of parameters with  $E \in [50, 700]$  GeV,  $L \in [0.2, 10]$  fm,  $\hat{q} \in [1, 3]$  GeV<sup>2</sup>/fm
- Performed separate fits in the two different regions for the scaling behavior of the peak angle with respect to the 3 parameters

C. Andres, FD, R. K. Elayavalli, J. Holguin, C. Marquet, I. Mout, [arXiv:2209.11236](https://arxiv.org/abs/2209.11236)  
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# Massive EEC in HIC

Including mass in medium-induced calculations is straightforward



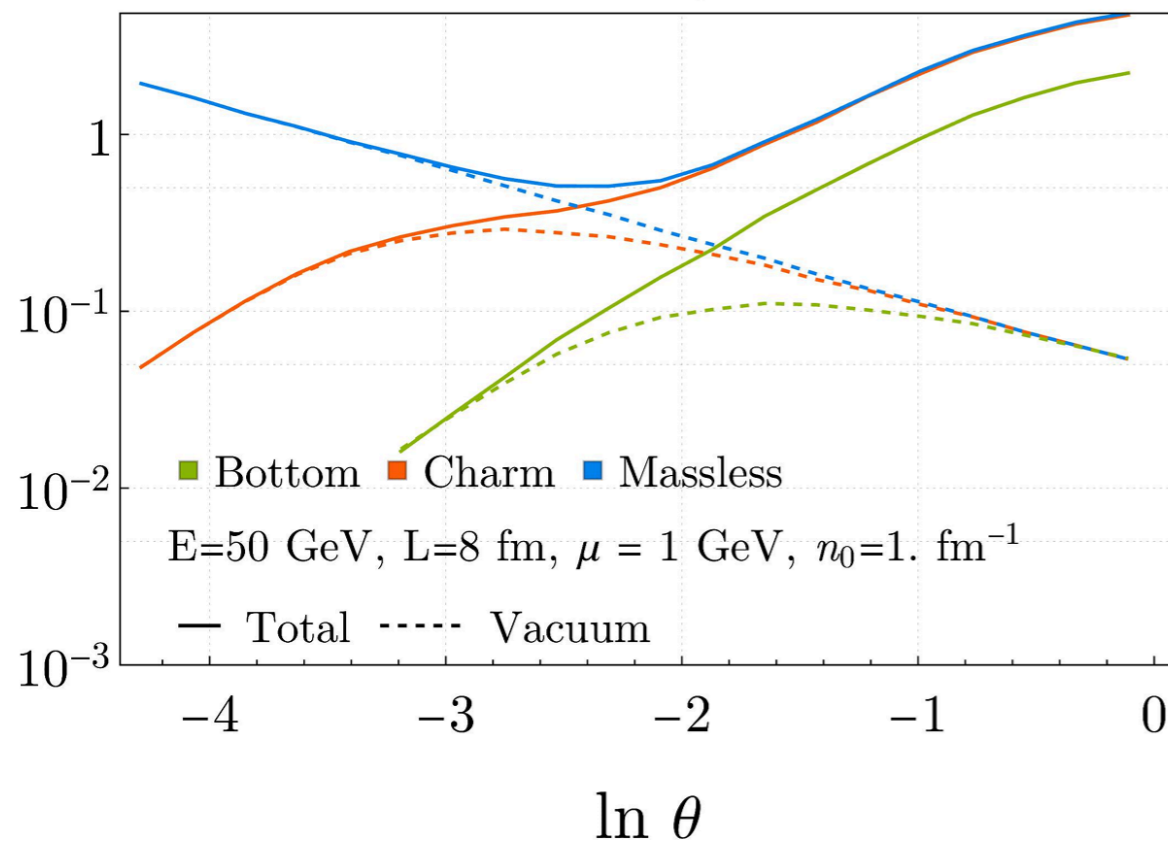
- Dead-cone is filled for lower energy jets
- When dead-cone is filled the mass changes also the large angle behavior

C. Andres, FD, J. Holguin, C. Marquet, I. Moulton, arXiv:2307.15110

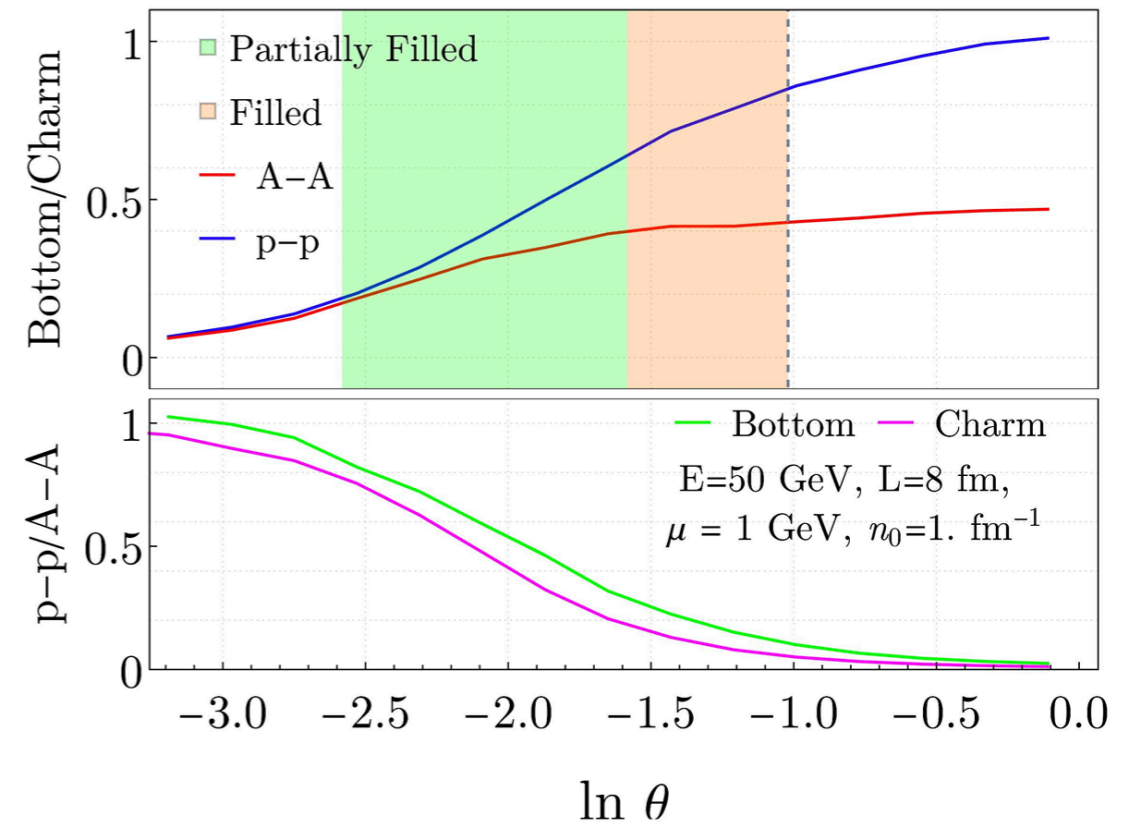
# Massive EEC in HIC

- Experimentally, the cleanest observable would be the b/c ratio

Two-Point Correlator



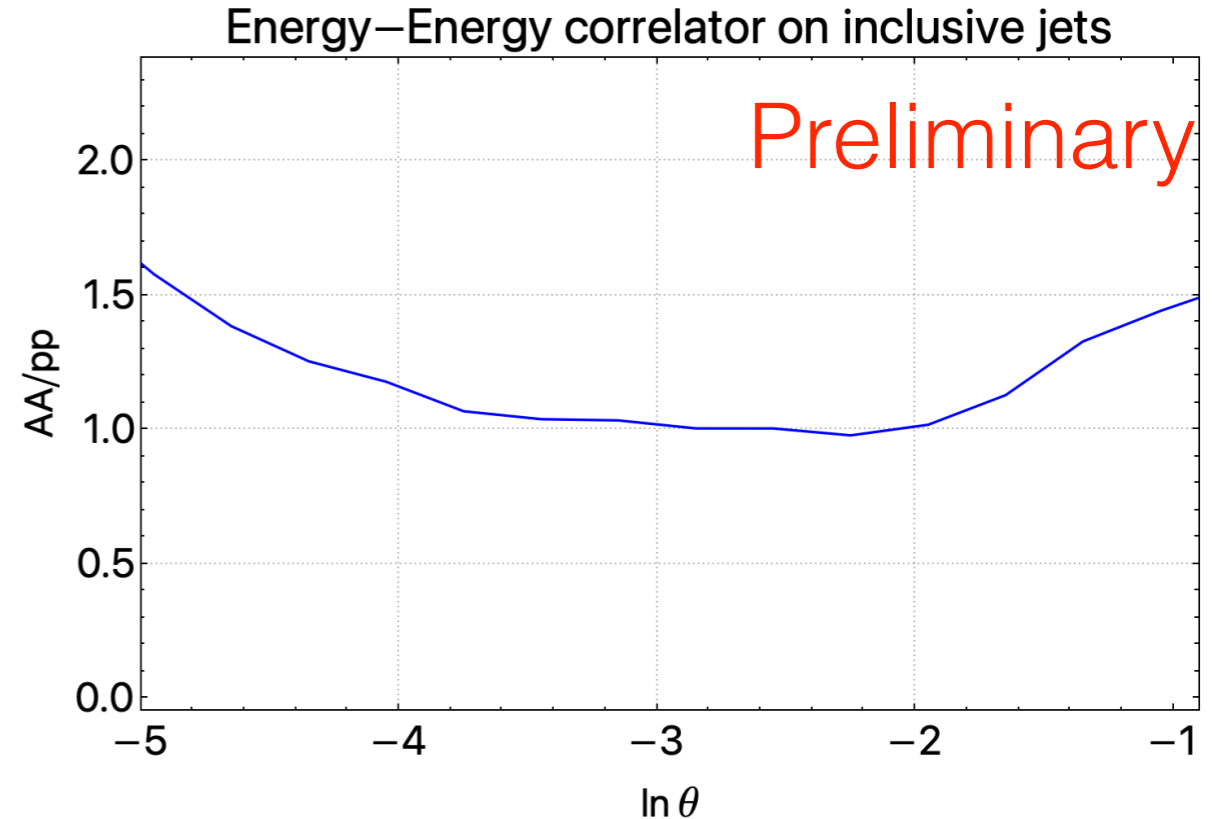
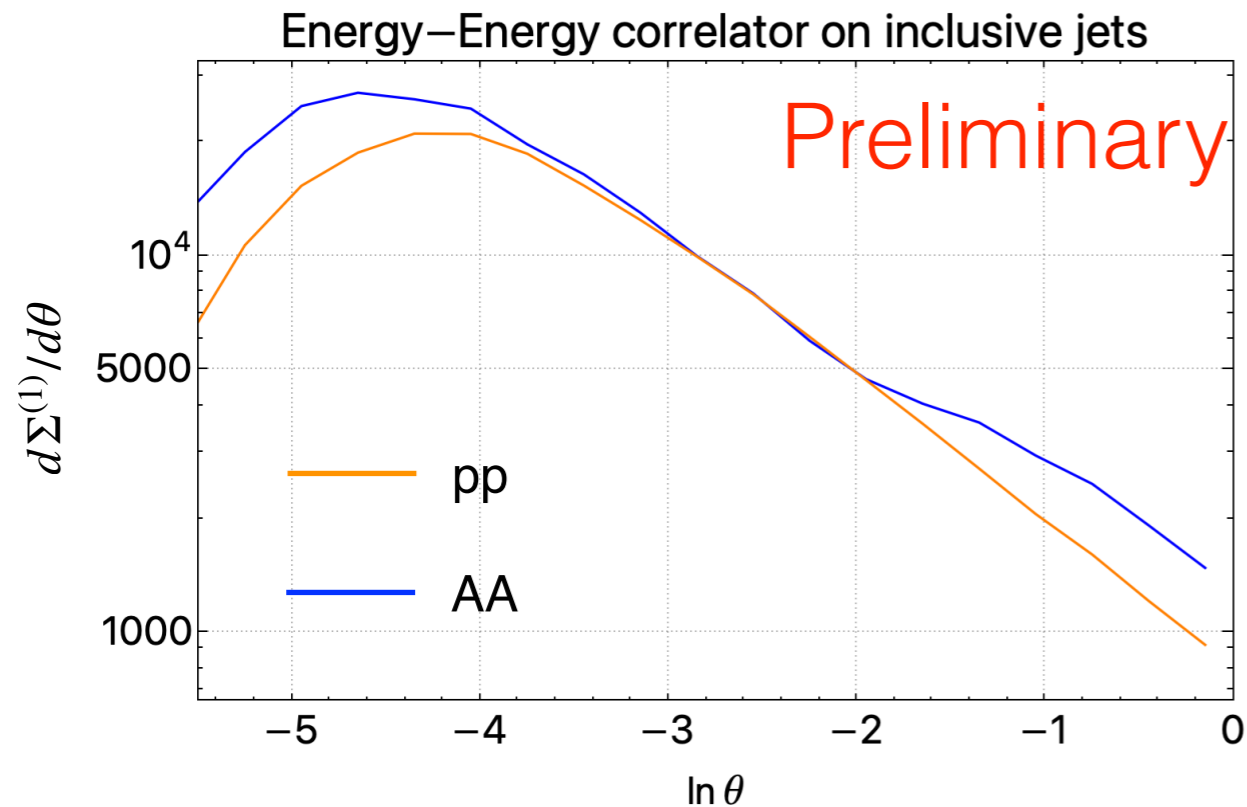
Two-Point Correlator



C. Andres, FD, J. Holguin, C. Marquet, I. Moulton, arXiv:2307.15110

# EECs for inclusive jets

- First measurements will be performed for inclusive jets
- In this case we do not know the energy of the initial parton and therefore energy loss becomes important
- HI-jets have a higher initial energy than pp-jets and therefore the transition to NP regime happens at smaller angles



# Outlook

- Calculations of medium-modified splittings can be vastly improved:
  - ✦ Go beyond the brick setup and include medium expansion
  - ✦ Calculate corrections which account for transverse momentum broadening
- Additional angular structure due to inherent anisotropy  
[J. Barata, G. Milhano, A. Sadofyev, arXiv:2308.01294](#)
- Better understanding of the role of energy loss
- Studies of how the background affects the EECs and what is the effect of increasing the power of the energy weights
- Medium response (see Xin-Nian's talk)  
[Z. Yang, Y. He, I. Moulton, X.-N. Wang, arXiv:2310.01500](#)

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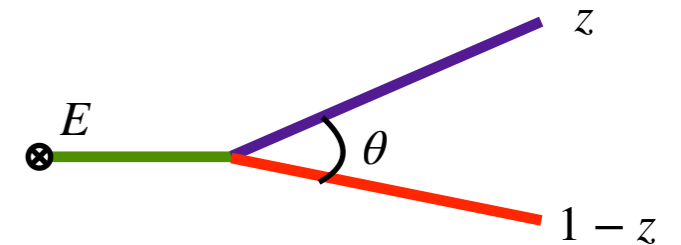
# Conclusions

- Energy correlators provide a powerful tool for understanding jets in HIC
  - ✦ Experimentally accessible
  - ✦ Can be calculated perturbatively thanks to insensitivity to soft physics and uncorrelated background
  - ✦ No need for de-clustering
  - ✦ Vacuum baseline well understood to a high degree of accuracy
- Characteristic features of the calculation for in-medium splittings are clearly imprinted in the observables



Thank you!

# Energy correlators



- For a quark jet at leading order in the splittings,  $Q = E$  the energy of the jet

$$\frac{d\Sigma^{(n)}}{d\theta} = \frac{1}{\sigma_{qg}} \int dz \frac{d\sigma_{qg}}{d\theta dz} z^n (1-z)^n + \mathcal{O}\left(\frac{\mu_s}{E}\right)$$

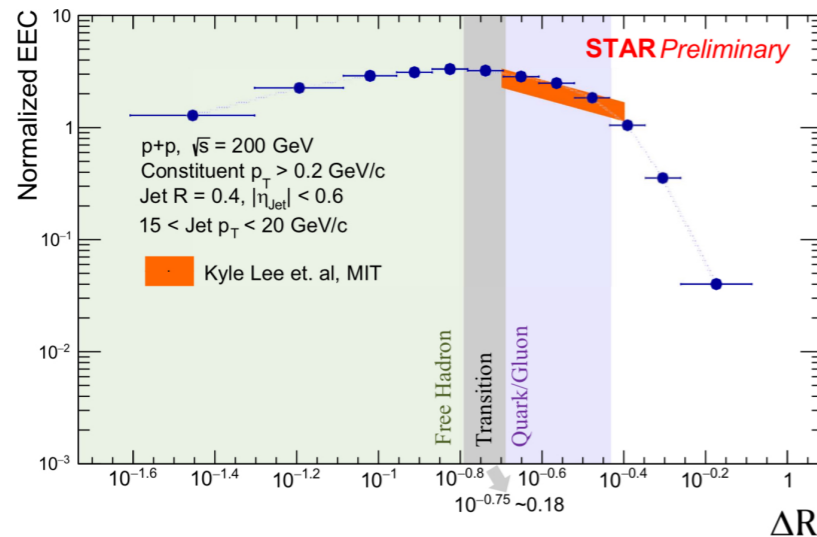
$\mu_s$  a softer scale over which the cross section is inclusive

- $qq$  and  $gg$  contributions are higher order
- Additional energy loss ( $E_q + E_g \neq E$ ) is also subleading

$$z = \frac{E_g}{E}$$

# Energy correlators in vacuum

- New measurements announced at HP2023!

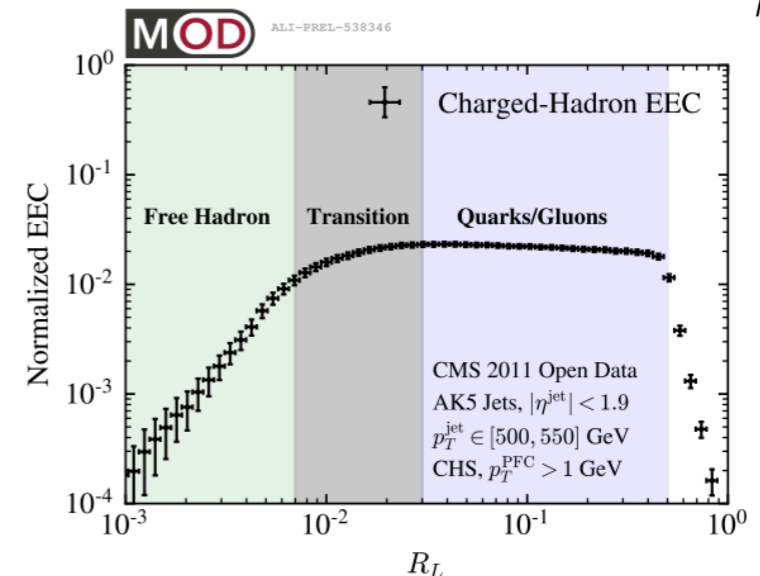


See R. Cruz-Torres's Talk Tue. 17:30

See A. Tamis's Talk Wed. 11:30

- Analyses done by theorists with CMS open data showing sensitivity to hadronization transition

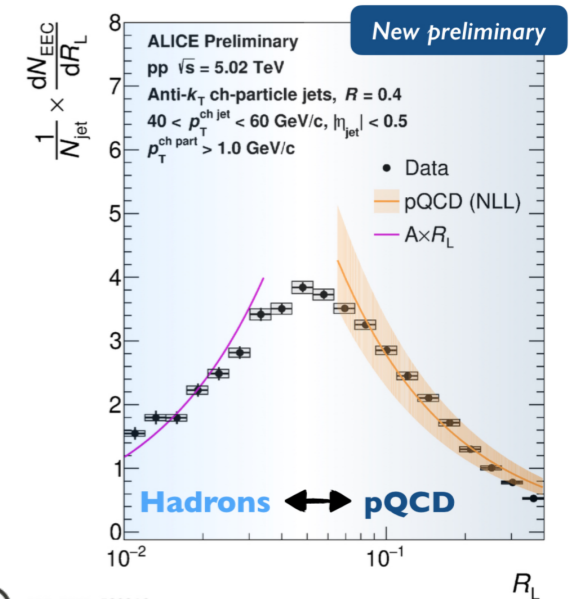
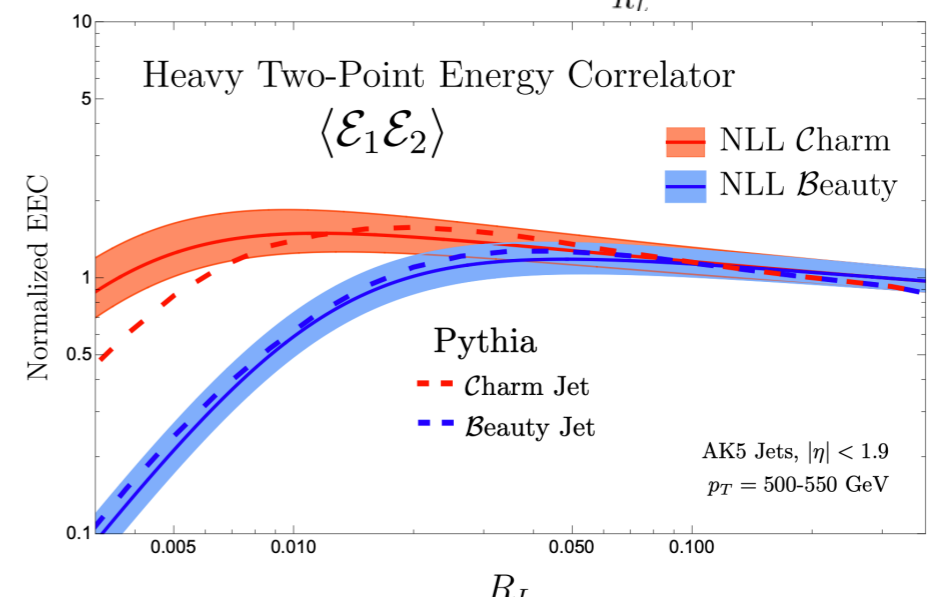
P. T. Komiske, I. Moutl, J. Thaler, H. X. Zhu [2201.07800](#)



- Dead cone for massive quarks

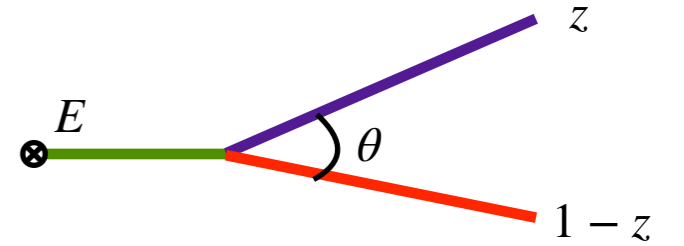
E. Craft, K. Lee, B. Meçai, I. Moutl [2210.09311](#)

See J. Holguin's Talk Wed. 11:50



# Energy correlators in HIC

$$\frac{d\Sigma^{(n)}}{d\theta} = \frac{1}{\sigma_{qg}} \int dz \frac{d\sigma_{qg}}{d\theta dz} z^n (1-z)^n + \mathcal{O}\left(\frac{\mu_s}{E}\right)$$



- We factor out the vacuum cross section and define the modification factor  $F_{\text{med}}$

$$\frac{d\sigma_{qg}}{d\theta dz} = (1 + F_{\text{med}}(z, \theta)) \frac{d\sigma_{qg}^{\text{vac}}}{d\theta dz} \quad F_{\text{med}}(z, \theta) \xrightarrow{\theta < \theta_L} 0$$

- We do not expect medium modification at small angles, thus vacuum collinear resummation should still be valid

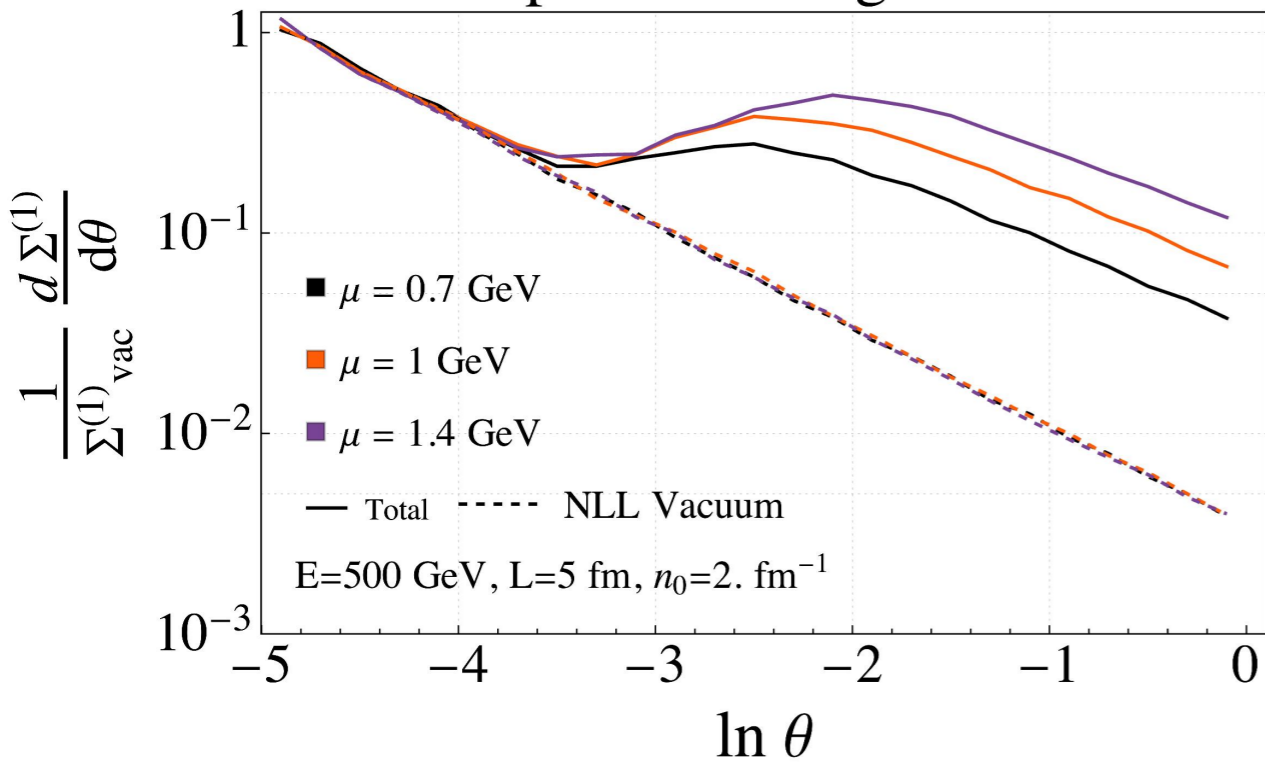
$$\frac{d\Sigma^{(n)}}{d\theta} = \frac{1}{\sigma_{qg}} \int dz \left( g^{(n)}(\theta, \alpha_s) + F_{\text{med}}(z, \theta) \right) \frac{d\sigma_{qg}^{\text{vac}}}{d\theta dz} z^n (1-z)^n \left( 1 + \mathcal{O}\left(\frac{\mu_s}{E}\right) \right) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{\theta Q}\right)$$

$$g^{(1)} = \theta^{\gamma(3)} + \mathcal{O}(\theta)$$

# Results with Yukawa interaction

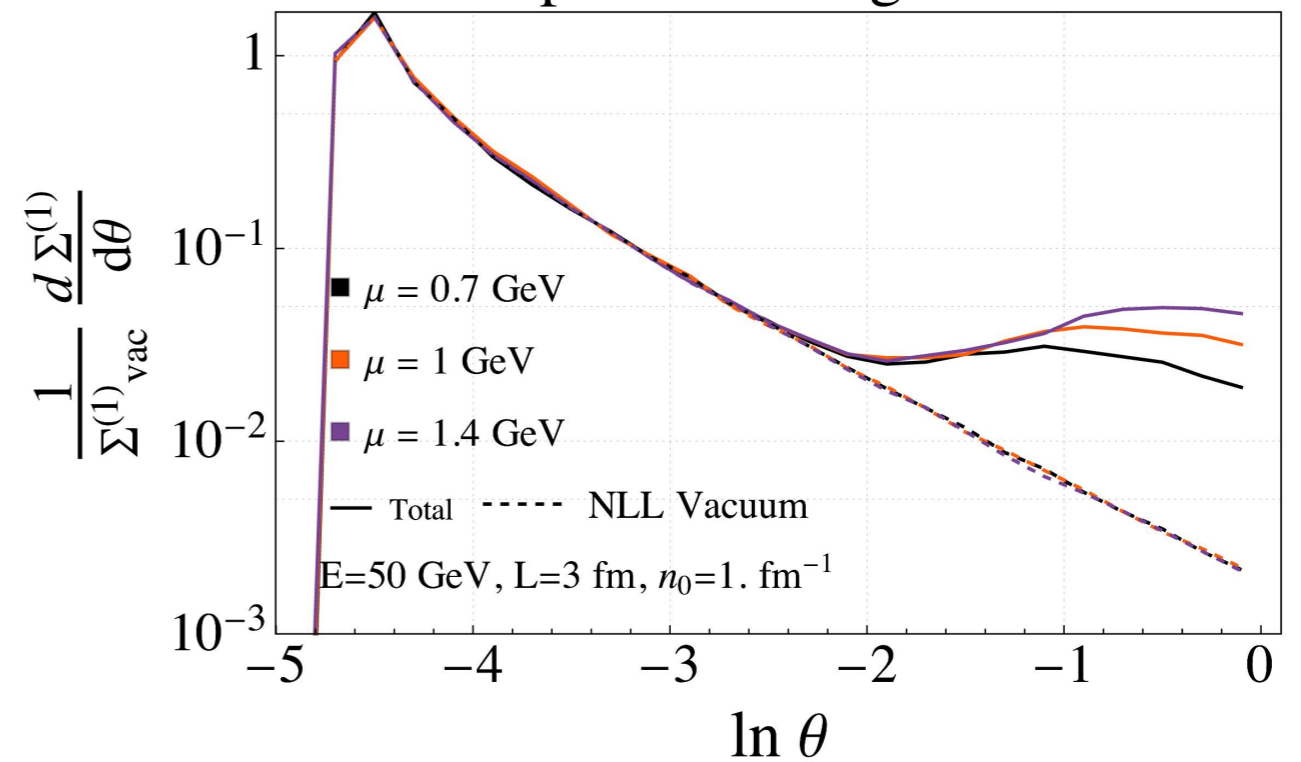
$$\theta_c > \theta_L$$

Two-Point Energy Correlator  
Multiple Scatterings: Yukawa



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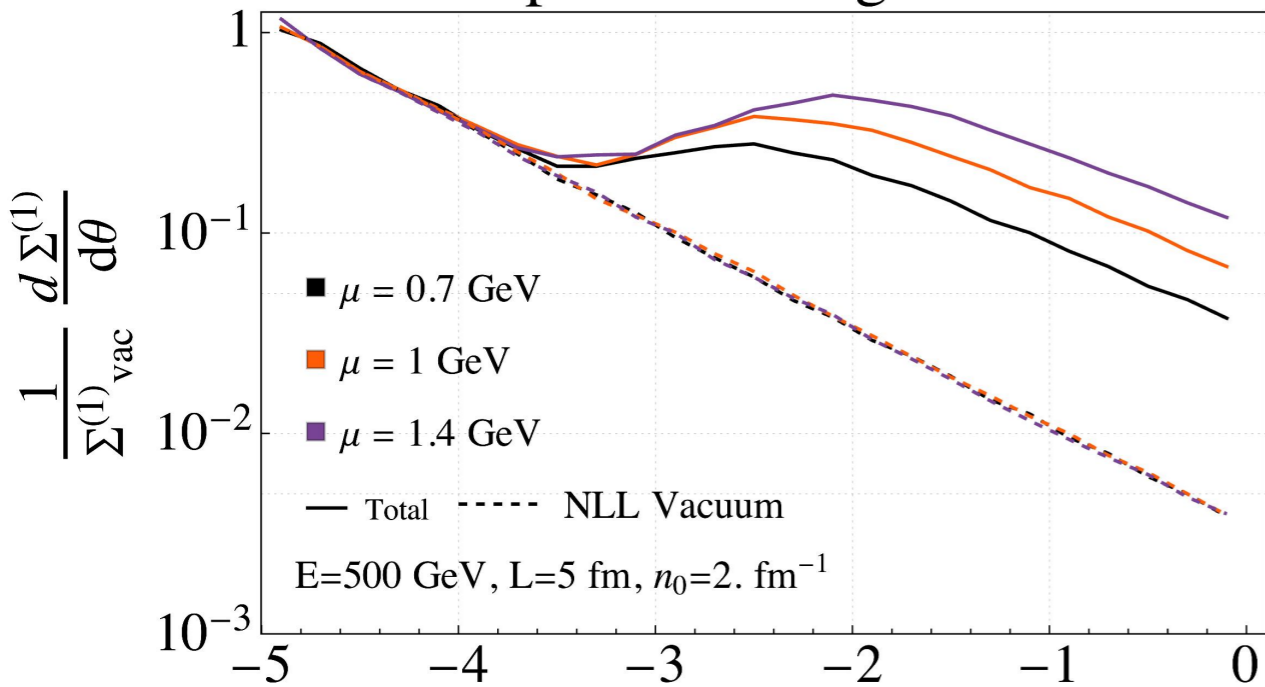
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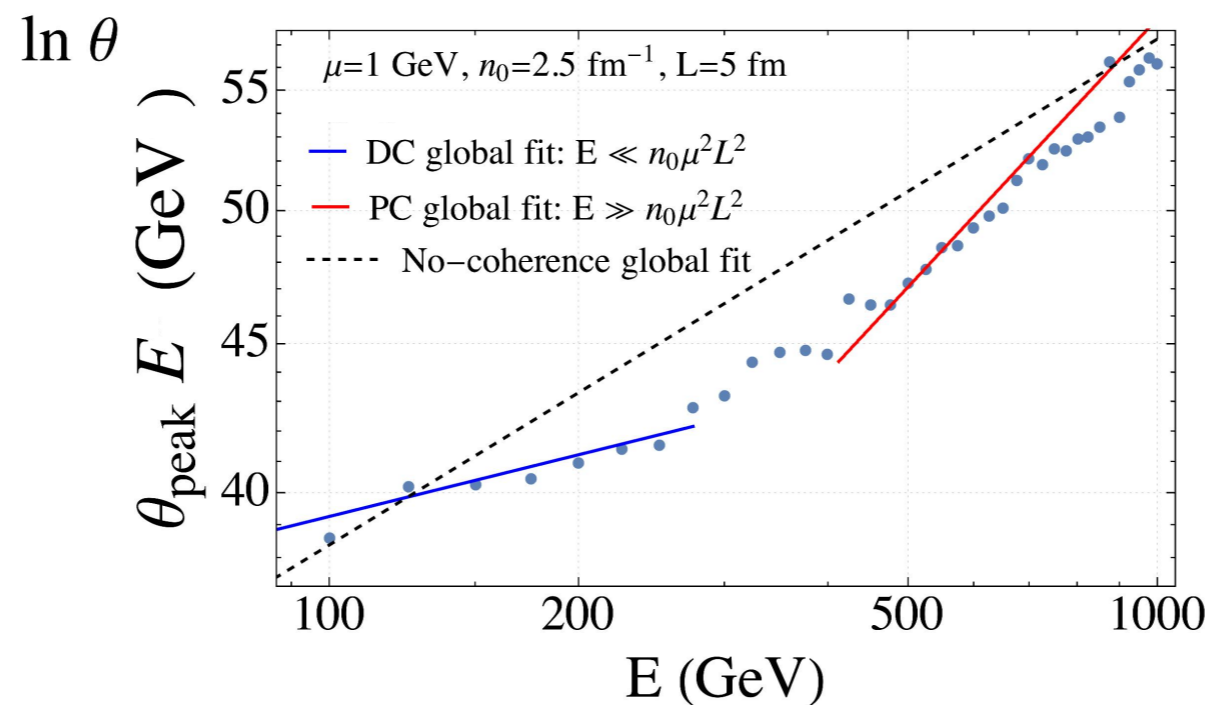
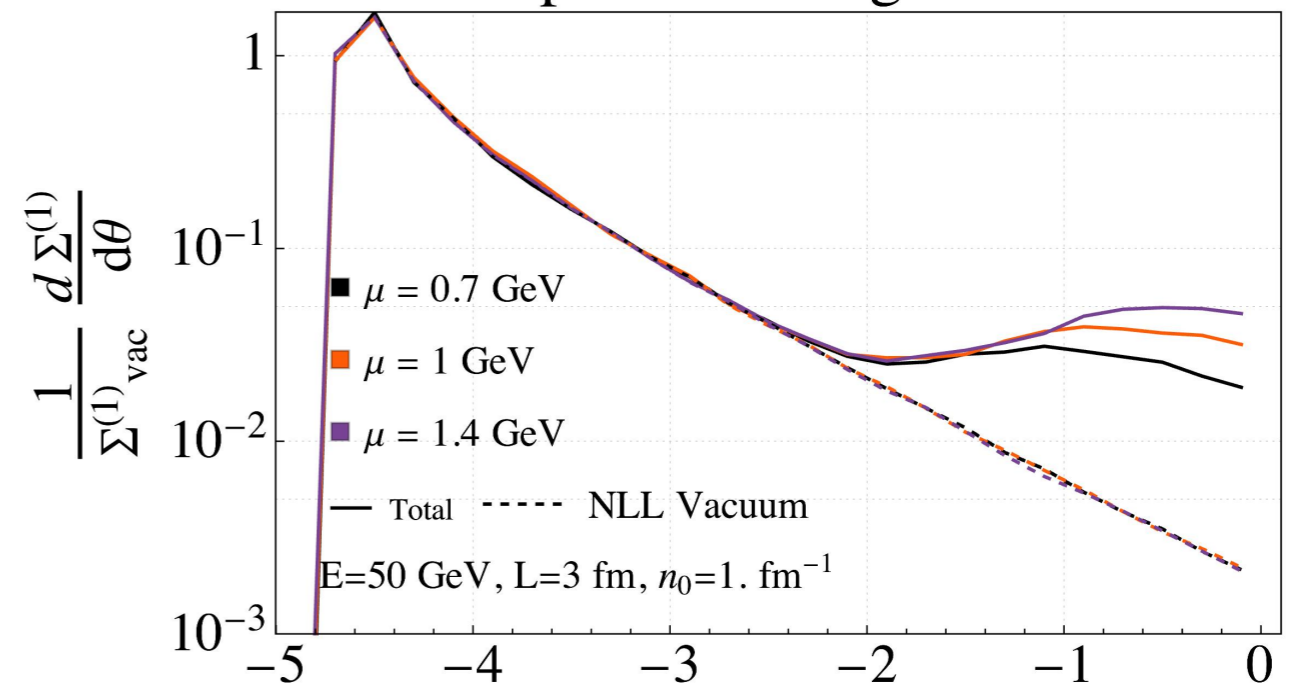
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Two-Point Energy Correlator  
Multiple Scatterings: Yukawa



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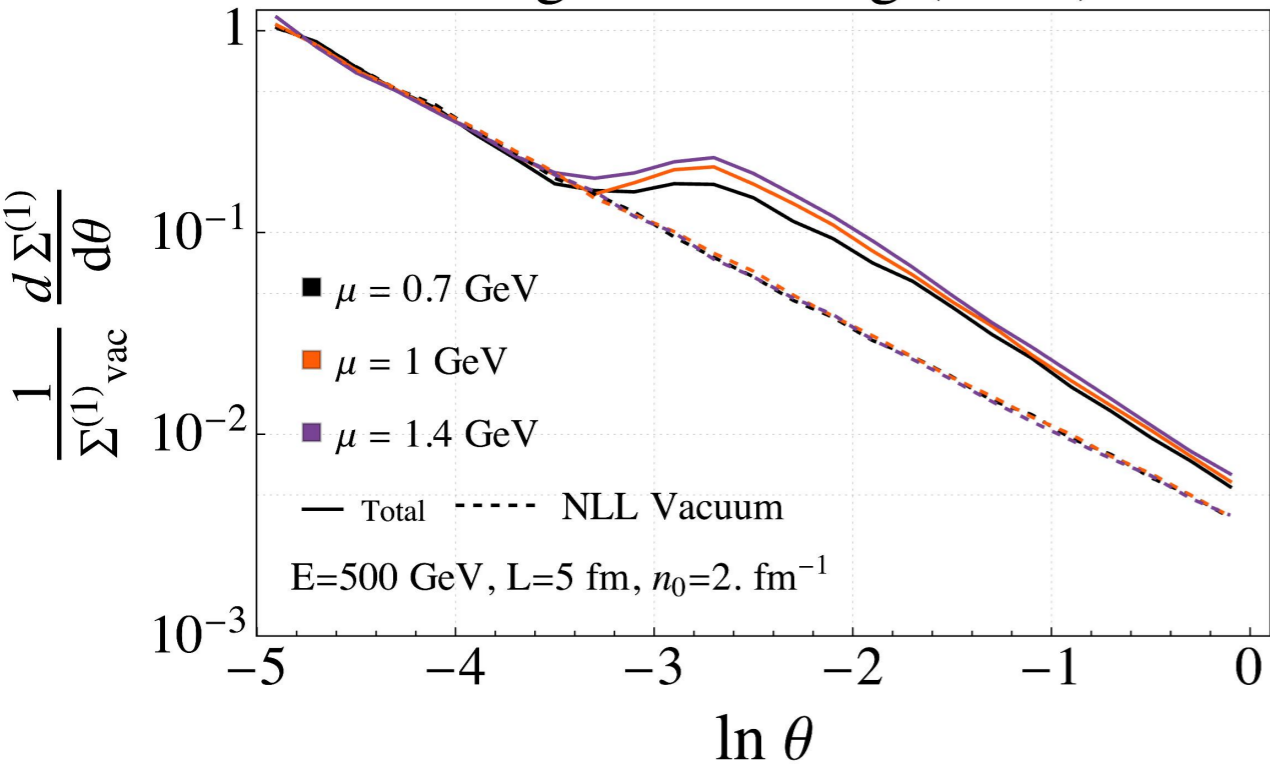
Two-Point Energy Correlator  
Multiple Scatterings: Yukawa



# Results with single scattering (GLV)

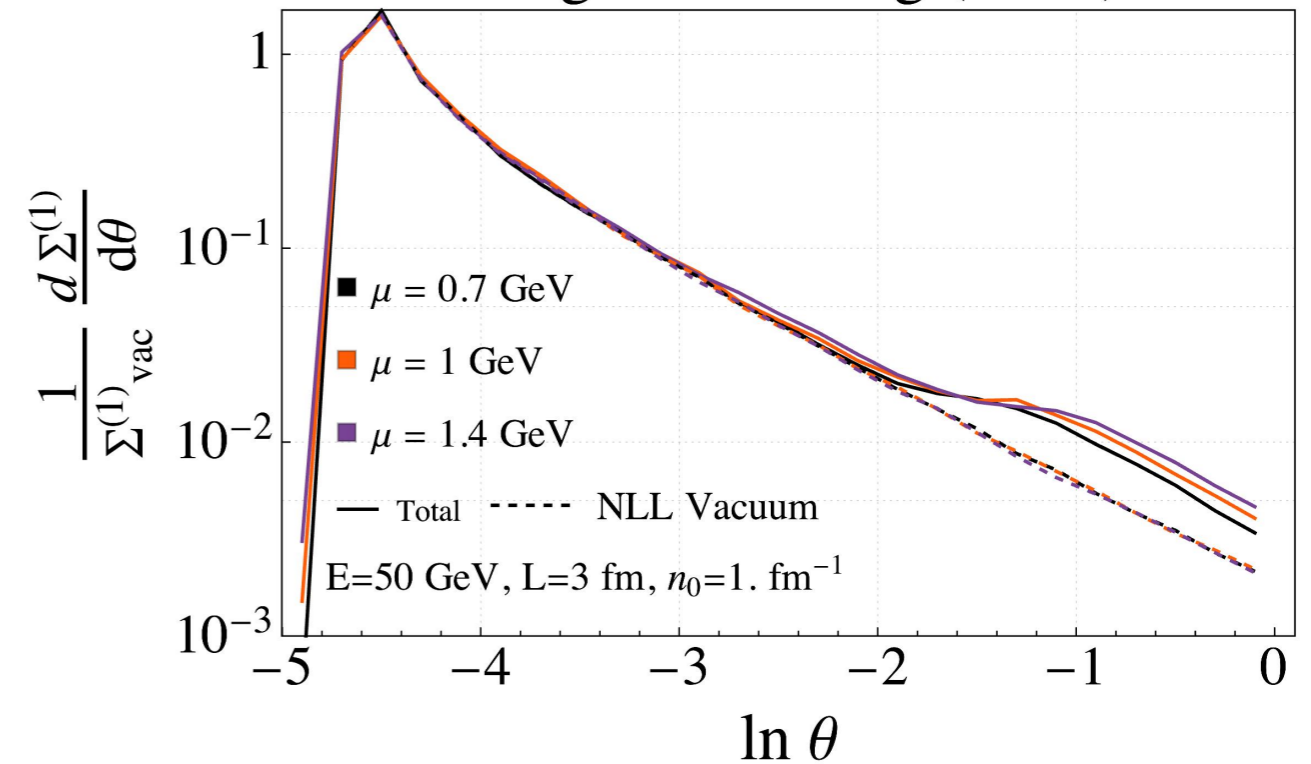
$$\theta_c > \theta_L$$

Two-Point Energy Correlator  
Single Scattering (GLV)



$$\theta_c < \theta_L$$

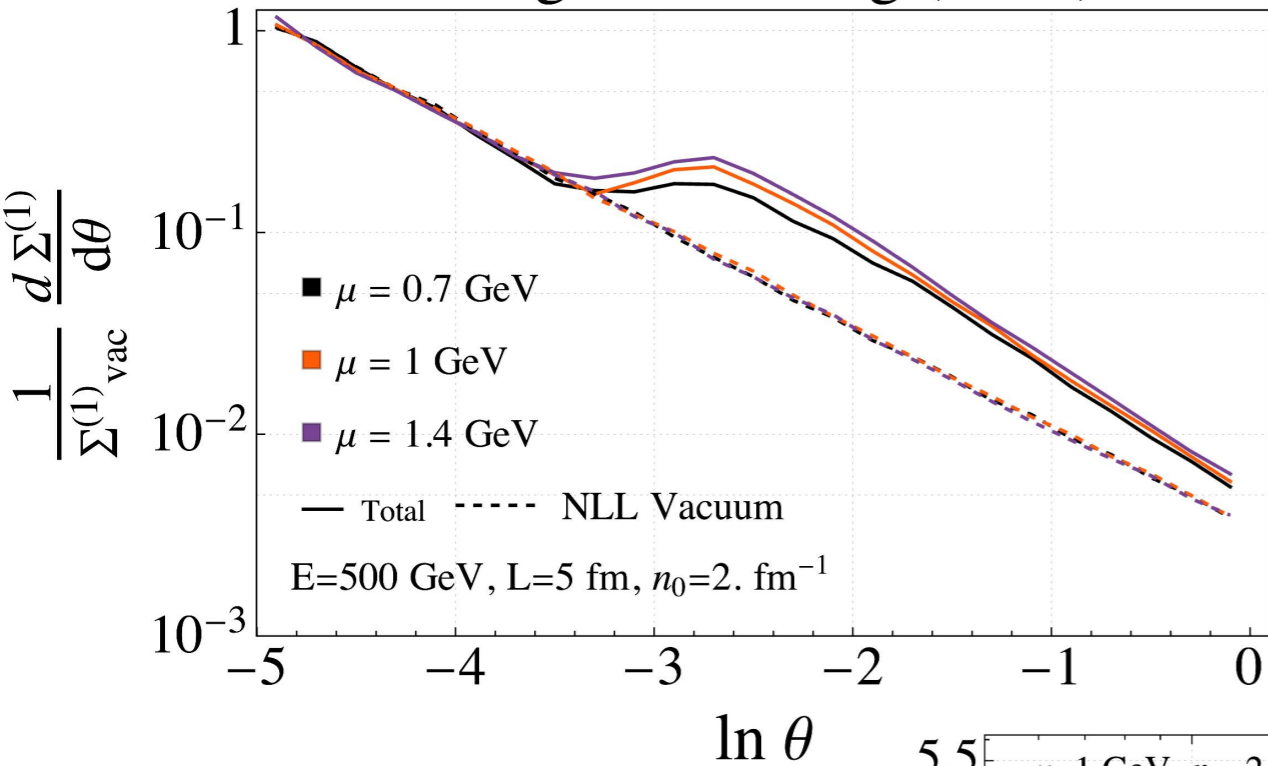
Two-Point Energy Correlator  
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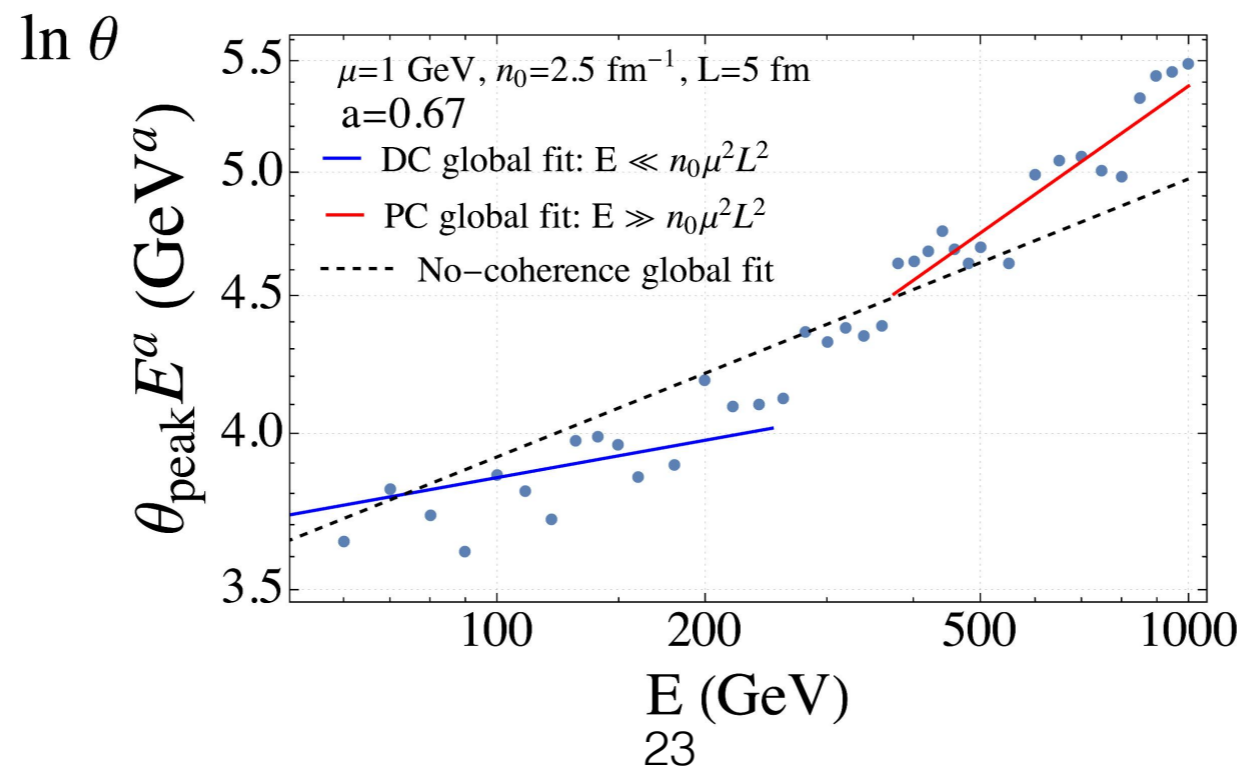
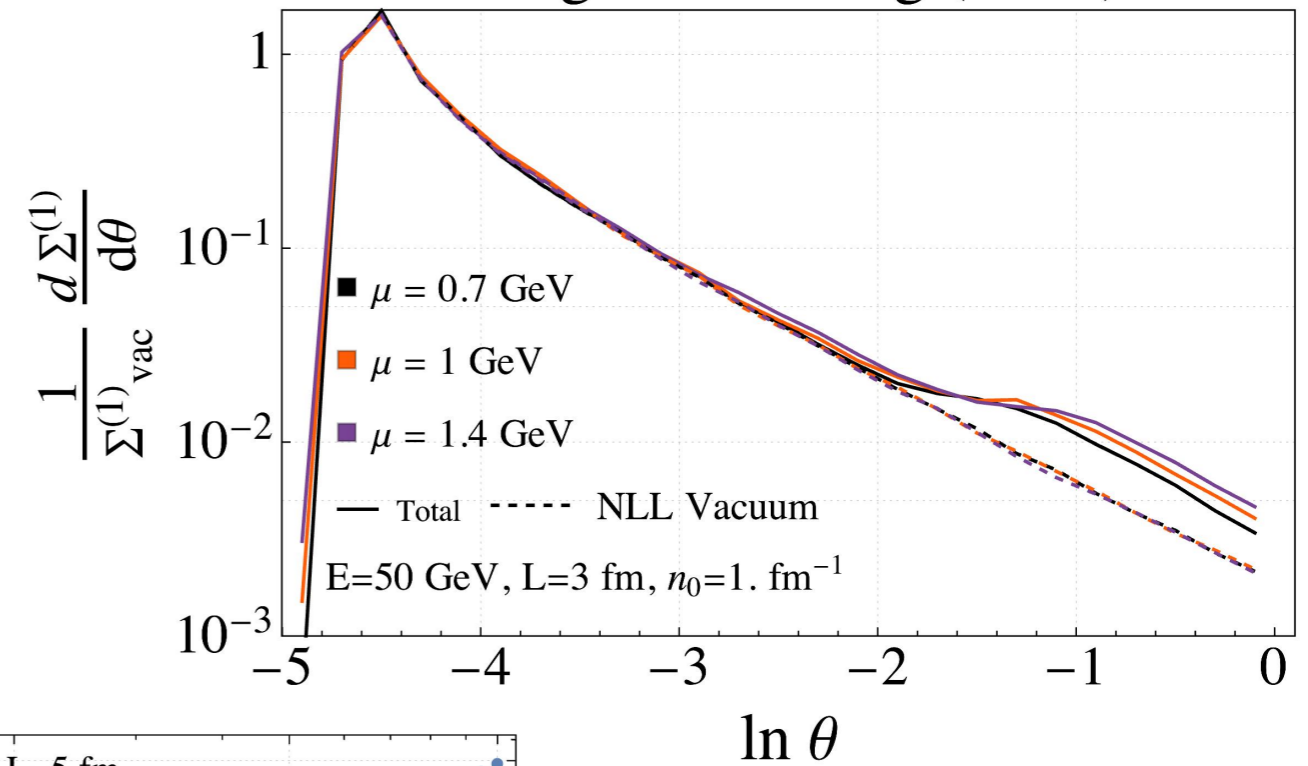
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Two-Point Energy Correlator  
Single Scattering (GLV)



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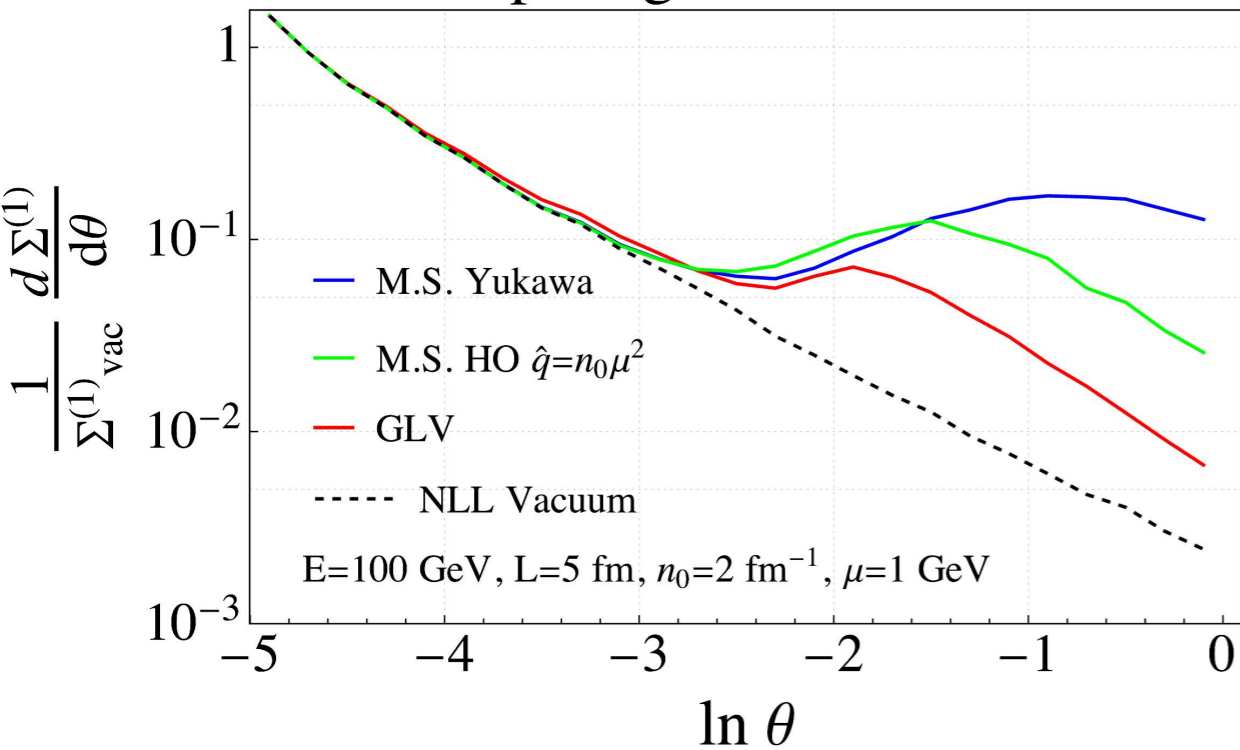
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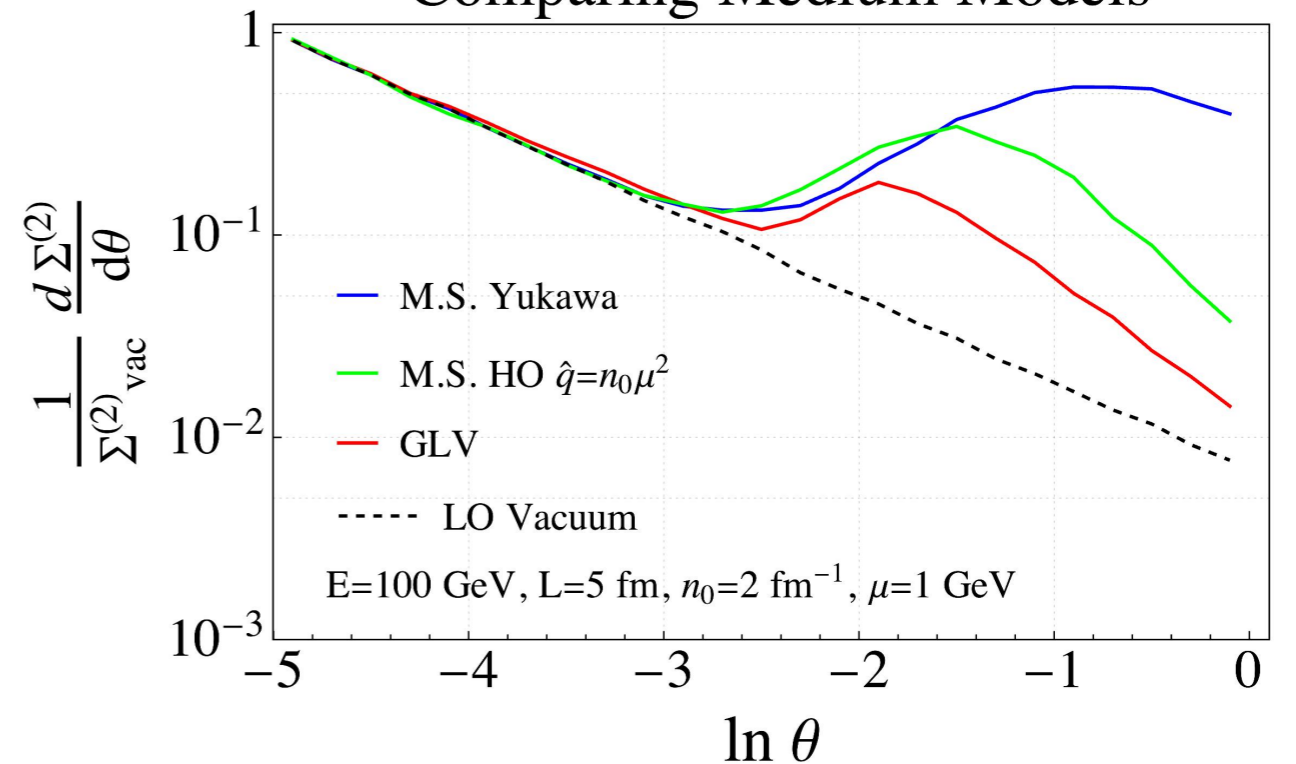


# Higher energy power

Two-Point Energy Correlator  
Comparing Medium Models



Two-Point Energy<sup>2</sup> Correlator  
Comparing Medium Models



# Tilted Wilson lines

FD, Milhano, Salgado, Tywoniuk, Vila [1907.03653](#)  
Isaksen, Tywoniuk [2107.02542](#)

- Use high-energy limit of propagators: vacuum propagator times a Wilson line in the classical trajectory

$$\mathcal{G}_R(t_2, \mathbf{p}_2; t_1, \mathbf{p}_1; \omega) \rightarrow (2\pi)^2 \delta^{(2)}(\mathbf{p}_2 - \mathbf{p}_1) e^{-i \frac{p_2^2}{2\omega} (t_2 - t_1)} V_R(t_2, t_1; [\mathbf{n}t])$$

- Calculate averages of Wilson lines in the large- $N_c$  limit (calculations also available for finite  $N_c$ ). All averages can be expressed in terms of fundamental dipoles and quadrupoles

$$\frac{1}{N_c} \left\langle \text{Tr } V_1 V_2^\dagger \right\rangle = S_{12} \qquad \frac{1}{N_c} \left\langle \text{Tr } V_1 V_2^\dagger V_2 V_1^\dagger \right\rangle = Q$$

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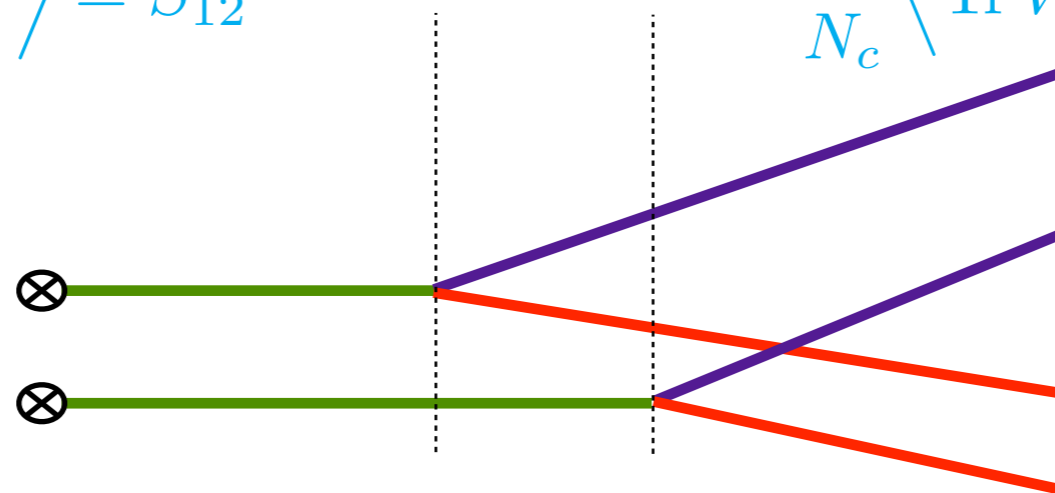
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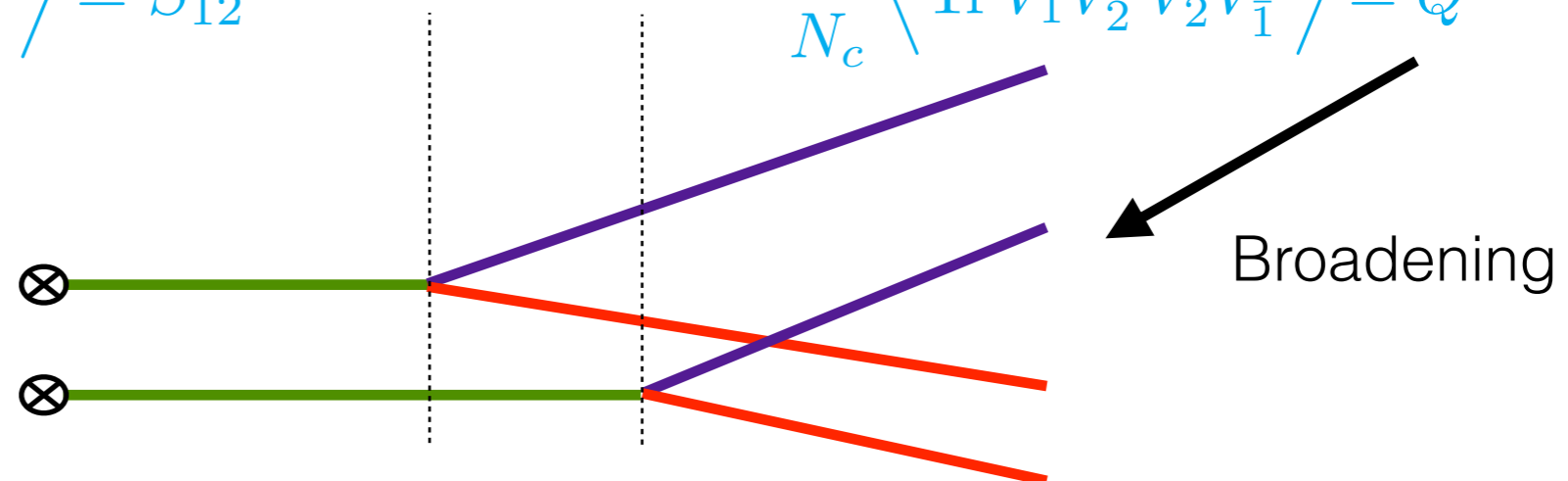
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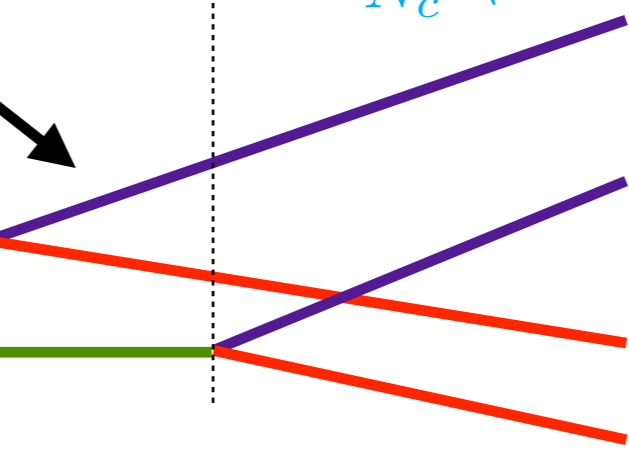
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Dynamics of emission process



Broadening

# EECs and color coherence

Transition from Decoherent to Partially Coherent Quenching

