

# Heavy flavor and quarkonium production in pp collisions

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# Overview

- 1 Introduction
  - Quarkonium
  - Polarization
  - Results

- 2 Discussions

- 3 Conclusion and Future

# Scope of Heavy Flavor Production

- focus on charm and bottom production
- hadrons include mesons ( $D$ ,  $B$ ), baryons, onia ( $\psi$  and  $\Upsilon$ )
- produced through QCD/QED processes
- in  $hh$ ,  $\gamma\gamma$ , and  $e^+e^-$  collisions

	2.4 MeV 2/3 u up	1.27 GeV 2/3 c charm	173.2 GeV 2/3 t top	0 1 $\gamma$ photon
Quarks	4.8 MeV -1/3 d down	104 MeV -1/3 s strange	4.2 GeV -1/3 b bottom	0 0 1 g gluon
	+2.2 MeV 0 1/2 e electron neutrino	+0.17 MeV 0 1/2 $\nu_\mu$ muon neutrino	+1.777 MeV 0 1/2 $\nu_\tau$ tau neutrino	0 1 1 Z weak force
Leptons	0.511 MeV -1 1/2 e electron	105.7 MeV -1 1/2 $\mu$ muon	1.777 GeV -1 1/2 $\tau$ tau	80.4 GeV +1 1 W weak force
				Bosons (Forces)

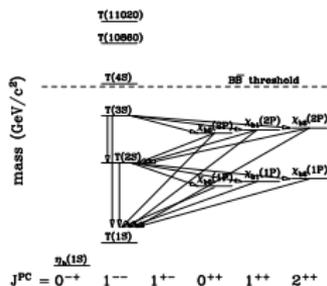
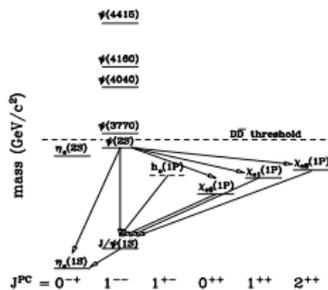
## Color Evaporation Model (CEM) for total charm cross section

$$\sigma = \sum_{i,j=q,\bar{q},g} \int dx_1 dx_2 f_i^P(x_1, \mu_F) f_j^P(x_2, \mu_F) \hat{\sigma}_{ij},$$

In PRC.87.014908, an attempt to reduce the uncertainty on the total charm cross section,

- $m_c$  was fixed at  $1.27 \pm 0.09$  GeV ( $\overline{\text{MS}}$  scheme)
- $\mu_F/m_c = 2.1_{-0.85}^{+2.55}$  and  $\mu_R/m_c = 1.6_{-0.12}^{+0.11}$

# Quarkonium production



CEM [Fritzsch 77; Halzen 77; Glück, Owens, Reya 78; Gavai *et al.* 95; Schuler, Vogt 95]

$$\sigma = F_Q \sum_{i,j=q,\bar{q},g} \int_{4m_c^2}^{4m_H^2} dM \int dx_1 dx_2 f_i^P(x_1, \mu_F) f_j^P(x_2, \mu_F) \hat{\sigma}_{ij},$$

- $m_c = 1.27 \pm 0.09$  GeV,  $\mu_F/m_T = 2.1_{-0.85}^{+2.55}$ , and  $\mu_R/m_T = 1.6_{-0.12}^{+0.11}$
- where  $m_T = \sqrt{m_c^2 + p_T^2}$ ,  $p_T^2 = 0.5(p_{Tc}^2 + p_{T\bar{c}}^2)$

# Quarkonium Production Models

## Improved CEM (ICEM) [Ma, Vogt 16]

$$\sigma = F_Q \sum_{i,j} \int_{M_\psi}^{2m_H} dM \int dx_i dx_j f_i(x_i, \mu_F) f_j(x_j, \mu_F) d\hat{\sigma}_{ij \rightarrow c\bar{c} + \chi}(p_{c\bar{c}}, \mu_R) \Big|_{p_{c\bar{c}} = \frac{m}{M_\psi} p_\psi},$$

where  $M_\psi$  is the mass of the charmonium state,  $\psi$ .

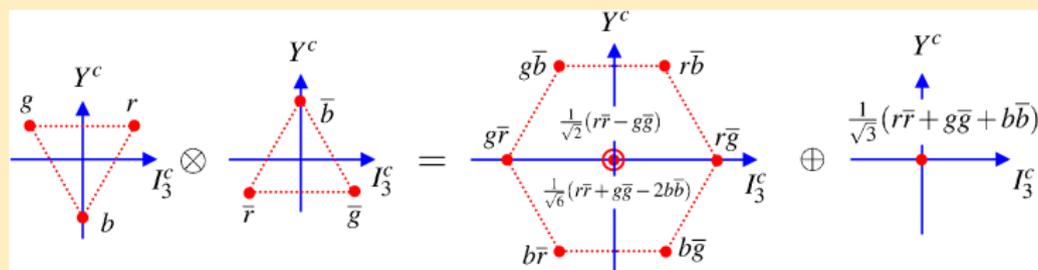
- first new advance in the basic CEM model since 1990s
- able to describe relative production of  $\psi(2S)$  to  $J/\psi$ , where the ratio is flat in the traditional CEM
- distinction between the momentum of the  $c\bar{c}$  pair and that of charmonium so that the  $p_T$  spectra will be softer and thus may explain the high  $p_T$  data better
- employed to calculate production and polarization of all S states, and relative production of  $\chi$  states

# Quarkonium Production Models

## Color Singlet Model (CSM) [Berger, Jones 81; Baier, Rückl 81, Schuler 94, Lansberg 11]

- constrains the production of  $Q\bar{Q}$  to the color singlet state only
- the produced  $Q\bar{Q}$  pair does not change its color and spin between production and hadronization

$$d\sigma[Q + X] = \sum_{i,j} \int dx_i dx_j f_i(x_i, \mu_F) f_j(x_j, \mu_F) d\hat{\sigma}_{i+j \rightarrow (Q\bar{Q})+X}(\mu_R, \mu_F) \times |R(0)|^2.$$

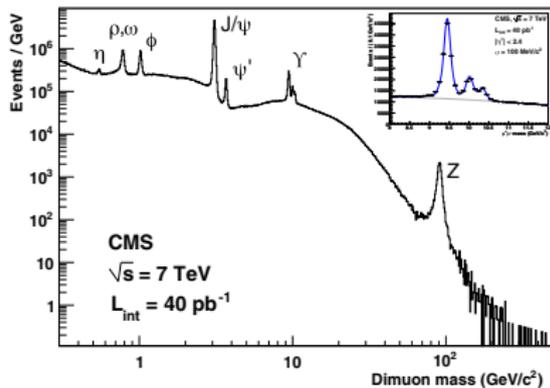
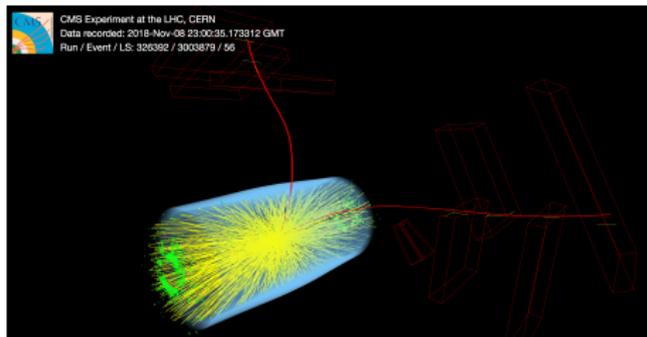


# Quarkonium Production Models

## Non Relativistic QCD (NRQCD) [Bodwin, Braaten, Lepage 95]

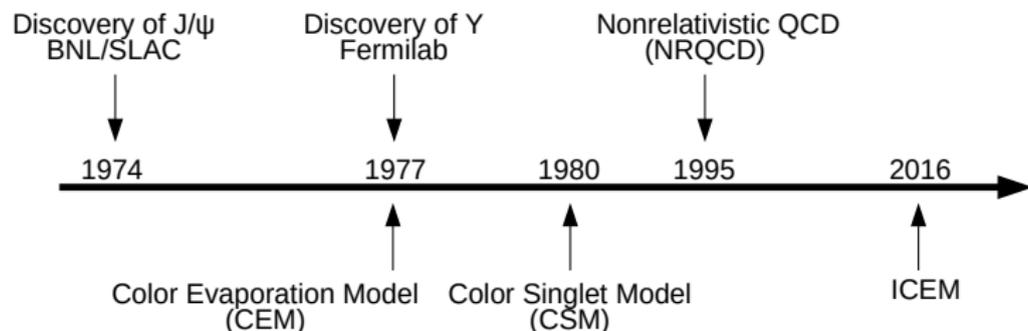
- an Effective Field Theory where production is described as an expansion in powers of  $\alpha_s$  and the heavy quark velocity,  $v/c$
- At each order, the production is further factorized into perturbative Short Distance Coefficients and non-perturbative Long Distance Matrix Elements (LDMEs); e.g. for  $J/\psi$ ,  $\sigma_{J/\psi} = \sum_n \sigma_{c\bar{c}[n]} \langle \mathcal{O}^{J/\psi}[n] \rangle$
- $\sigma_{c\bar{c}[n]}$  are cross sections in a particular color and spin state  $n$  calculated by perturbative QCD
- including  $^3S_1^{[1]}$  (singlet), and  $^3P_J^{[8]}$ ,  $^3S_1^{[8]}$  and  $^1S_0^{[8]}$  (octets)
- $\langle \mathcal{O}^{J/\psi}[n] \rangle$  are the LDMEs that describe the conversion of  $c\bar{c}[n]$  state into final state  $J/\psi$ , assuming that the hadronization does not change the momentum
- LDMEs are conjectured to be universal and the mixing of LDMEs are determined by fitting to data

# Models are tested against the data



- S states ( $J^{PC} = 1^{--}$ ) decay to  $\ell^+\ell^-$ , so they can be observed as peaks in dilepton mass spectra
- $\chi(nP)$  states ( $J^{PC} = J^{++}$ ) can be reconstructed by matching an S state with a low momentum photon
- $\eta_c$  and  $\eta_b$  states ( $J^{PC} = 0^{-+}$ ) decay hadronically

# Discovery and Production Models



## Color Evaporation Model [Fritzsch 77; Halzen 77; Glück, Owens, Reya 78]

- spins and colors are averaged

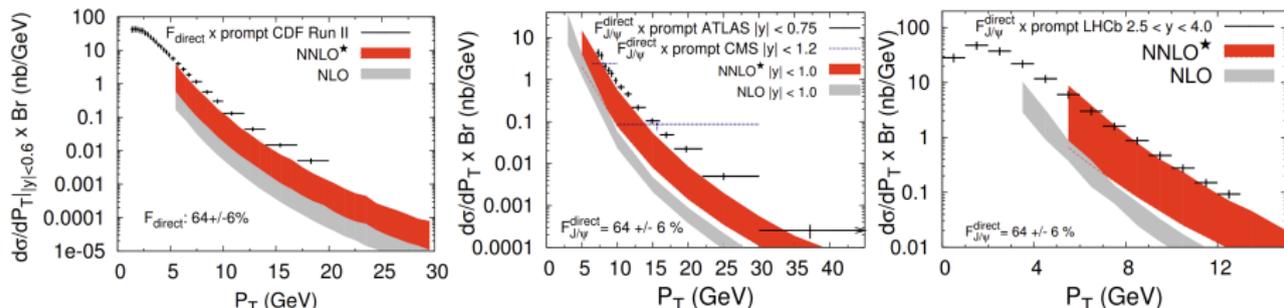
## Color Singlet Model [Berger, Jones 81; Baier, Rückl 81, Schuler 94, Lansberg 11]

- only color singlet contribution is considered

## Nonrelativistic QCD (NRQCD) [Bodwin, Braaten, Lepage 95]

- separate all spin and color states

# Highlights in the CSM

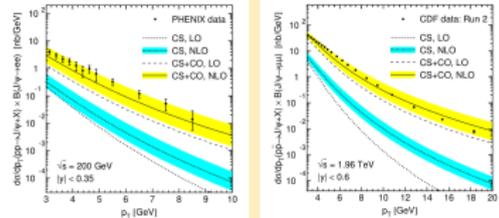


- LO and NLO calculations underestimate the Tevatron  $p_T$  distributions
- Recent advancements in CSM show that by adding real-emission contribution at NNLO, CSM can describe the distributions<sup>[1]</sup> (NNLO\*)

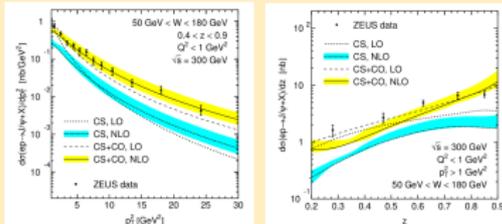
<sup>1</sup>J.P. Lansberg, J. Phys. G **38**, 124110 (2011).

# Highlights in NRQCD - A global fit of LDMEs<sup>[2]</sup>

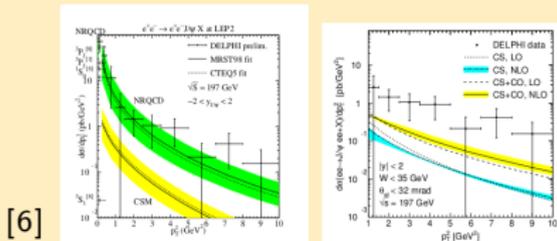
## $hh$ ( $p_T > 3$ GeV)



## $\gamma p$ ( $p_T > 3$ GeV)

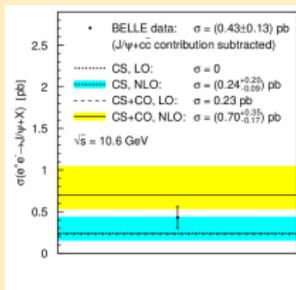


## $\gamma\gamma$ (Right: $p_T > 1$ GeV)



[6]

## $e^+e^-$



<sup>2</sup>M. Butenschön and B. A. Kniehl, Nucl. Phys. Proc. Suppl. **222-224**, 151 (2012).

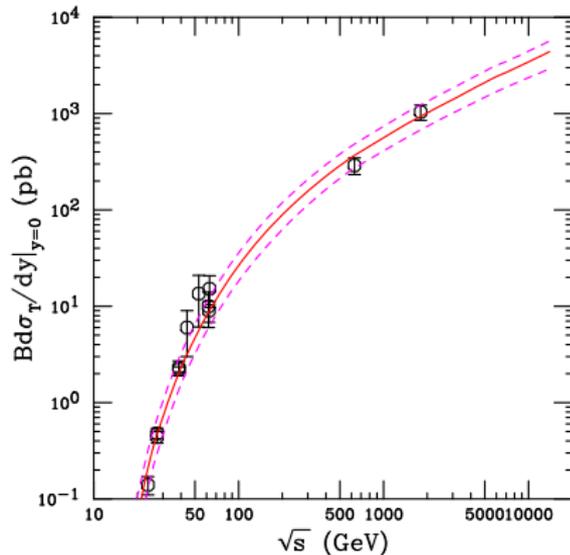
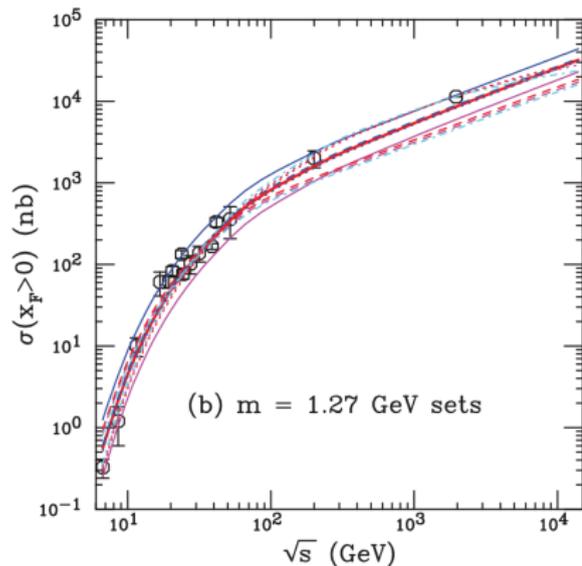
<sup>3</sup>M. Klasen et. al, DESY 01-202.

# Results in the CEM<sup>[4]</sup>

- one fitting factor ( $F_Q$ ) for each quarkonium state ( $Q$ )
- great consistency with experimental results over large range of  $\sqrt{s}$

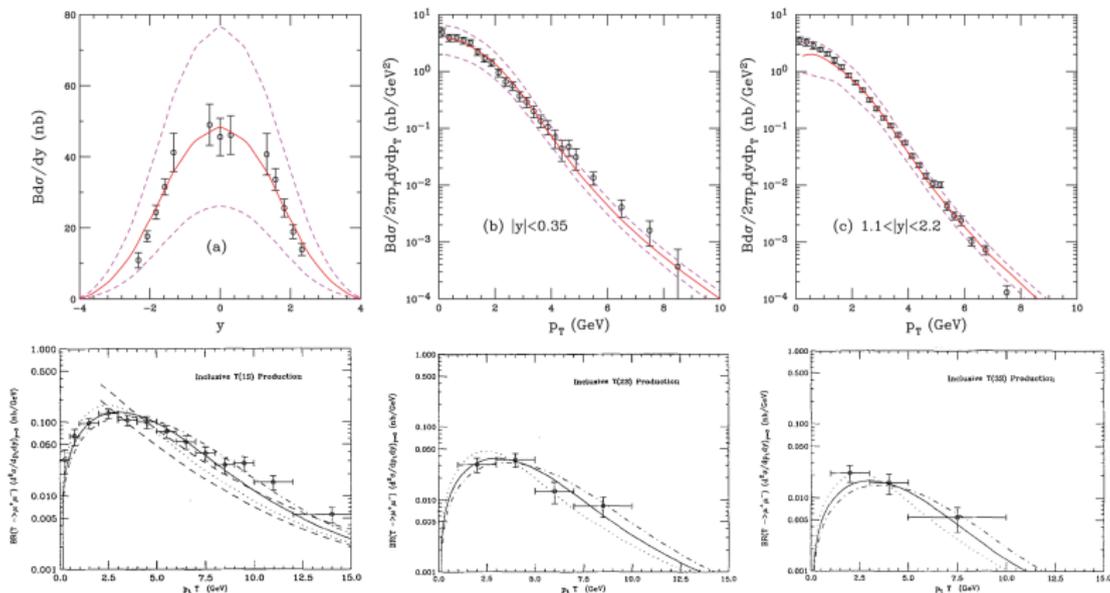
$J/\psi$

$\sum \Upsilon$ 's



<sup>4</sup>R. E. Nelson, R. Vogt and A. D. Frawley, Phys. Rev. C **87**, 014908 (2013).

# Results in the CEM<sup>[5,6]</sup>



- overall less rigorous, but accurate predictions

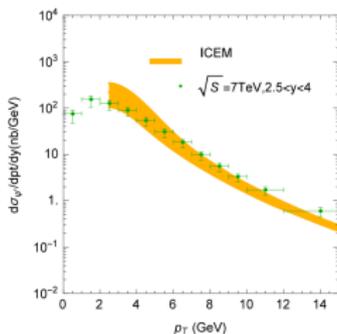
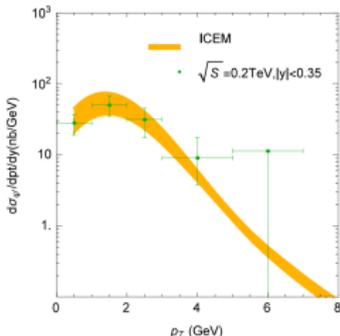
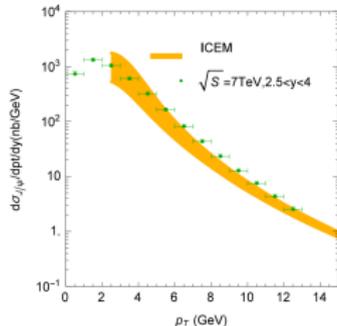
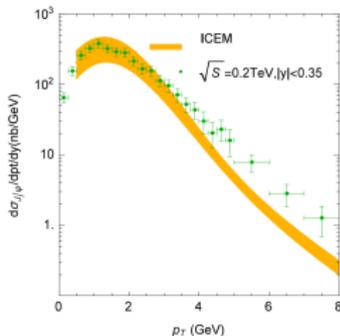
- no advances in the basic model since 1990s

<sup>5</sup>R. E. Nelson, R. Vogt and A. D. Frawley, Phys. Rev. C **87**, 014908 (2013).

<sup>6</sup>G. A. Schuler and R. Vogt, Phys. Lett. B **387**, 181 (1996).

# Results in the ICEM

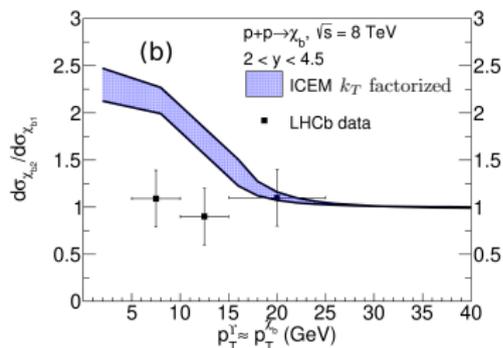
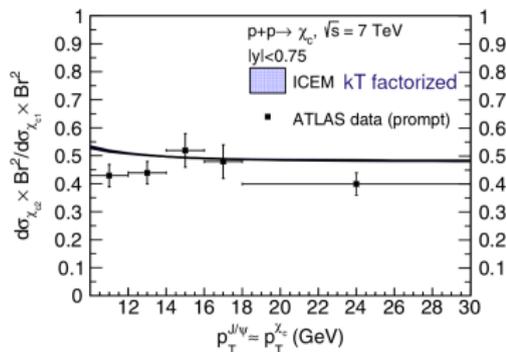
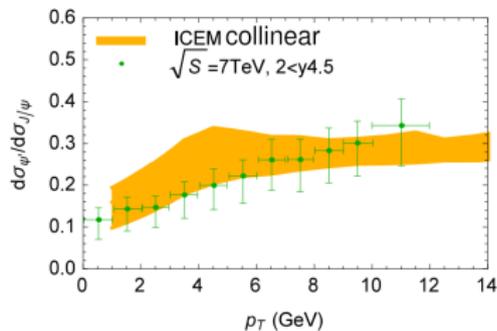
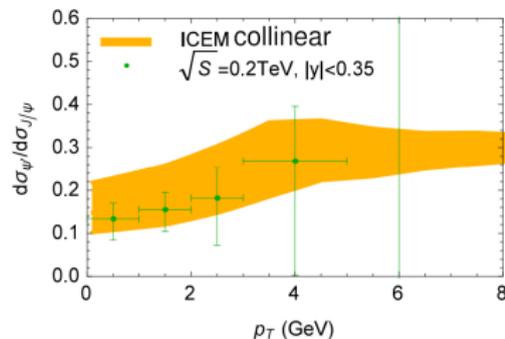
$$\frac{d\sigma_\psi(P)}{dp_T} = F_\psi \int_{M_\psi}^{2M_D} dM \frac{M}{M_\psi} \frac{d\sigma_{c\bar{c}}(M, P')}{dM dp'_T} \boxed{p'_T = (M/M_\psi) p_T}$$



Ma and Vogt, PRD 94, 114029 (2016).

- explicit charmonium mass dependence  $\rightarrow$  the ratio of cross sections is no longer  $p_T$ -independent
- distinction between the momentum of the  $c\bar{c}$  pair and that of charmonium  $\rightarrow p_T$  spectra will be softer and thus may explain the high  $p_T$  data better

# Relative production in the ICEM<sup>[7,8]</sup>



<sup>7</sup>Y. Q. Ma and R. Vogt, Phys. Rev. D **94**, 114029 (2016).

<sup>8</sup>V. Cheung and R. Vogt, Phys. Rev. D **98**, 114029 (2018) and **99**, 034007 (2019).

# Tests of Models

- CEM and NRQCD remain the most commonly used models today.
- They can predict yields and relative production of different quarkonium states.
- What about the relative production of different spin projection states of the same quarkonium state? → Polarization

## (I)CEM

- Less rigorous
- Fewer fit parameters
- Applied extensively to only hadroproduction (so far)

## NRQCD

- More rigorous
- More fit parameters
- Applied to all collision systems

# Polarization and Angular Distribution

$$|\psi\rangle = a_{-1} |J_z = -1\rangle + a_0 |J_z = 0\rangle + a_{+1} |J_z = +1\rangle, \quad \sum |a_{J_z}|^2 = 1$$

$$\lambda_\vartheta = \frac{1-3|a_0|^2}{1+|a_0|^2}, \quad \lambda_\varphi = \frac{2\text{Re}[a_{+1}a_{-1}^*]}{1+|a_0|^2}, \quad \lambda_{\vartheta\varphi} = \frac{\sqrt{2}\text{Re}[a_0^*(a_{+1}-a_{-1})]}{1+|a_0|^2}$$

$$\frac{d\sigma}{d\Omega} \propto \frac{1}{3 + \lambda_\vartheta} \left[ 1 + \lambda_\vartheta \cos^2 \vartheta + \lambda_\varphi \sin^2 \vartheta \cos(2\varphi) + \lambda_{\vartheta\varphi} \sin(2\vartheta) \cos \varphi \right]$$

- For a single elementary process, the polarized-to-total cross section can be calculated as  $a_{J_z}$ 's. Combinations of  $a_{J_z}$ 's gives different angular distributions.
- However, there is no combination that would give  $\lambda_\vartheta = \lambda_\varphi = \lambda_{\vartheta\varphi} = 0$ .
- An unpolarized production can only be described by a mixture of sub-processes or randomization modeling.



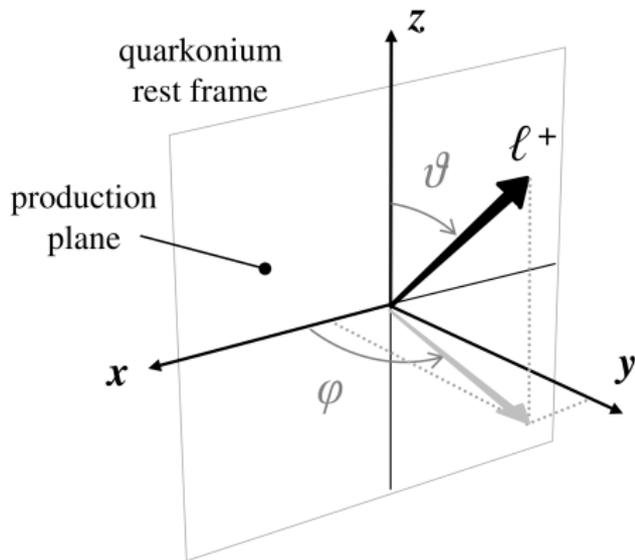
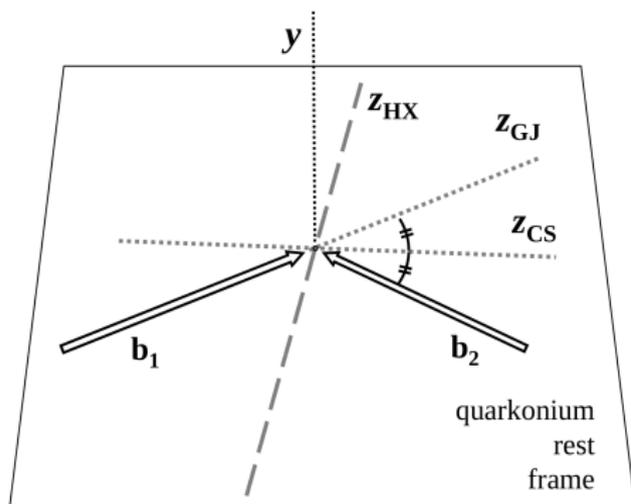
Pietro Faccioli, QWG

2010.

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# Polarization Measurement

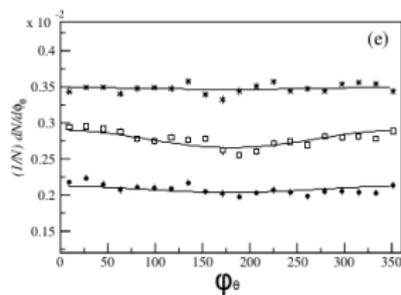
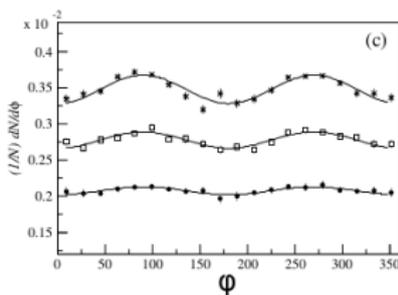
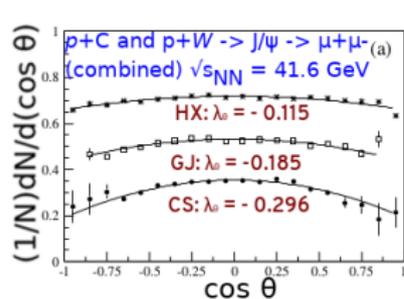


- There are three commonly used choices for the  $z$ -axis, namely  $z_{HX}$  (helicity),  $z_{CS}$  (Collins-Soper), and  $z_{GJ}$  (Gottfried-Jackson)
- $\vartheta$  is defined as the angle between the  $z$ -axis and the direction of travel for the  $\ell^+$  in the quarkonium rest frame

# Extracting Polarization

$$\frac{d\sigma}{d\Omega} \propto \frac{1}{3 + \lambda_{\vartheta}} [1 + \lambda_{\vartheta} \cos^2 \vartheta + \lambda_{\varphi} \sin^2 \vartheta \cos(2\varphi) + \lambda_{\vartheta\varphi} \sin(2\vartheta) \cos \varphi]$$

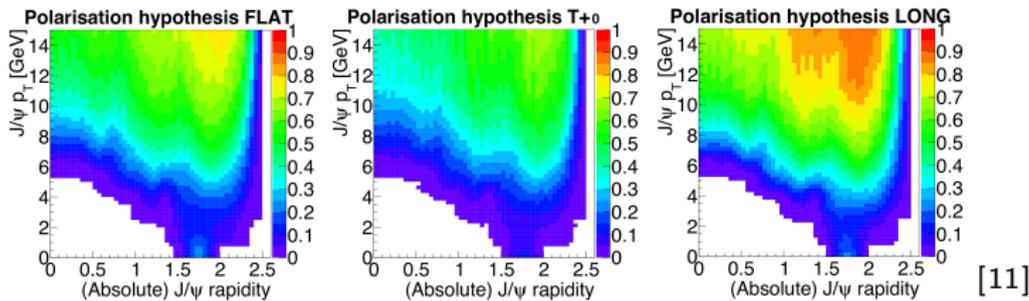
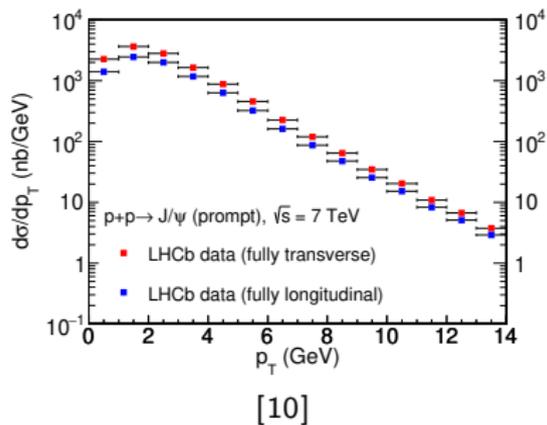
- Polarization parameters can be obtained by fitting the angular spectra as a function of  $\vartheta$  and  $\varphi$
- One can write  $\varphi_{\vartheta} = \varphi - \frac{\pi}{2} \mp \frac{\pi}{4}$  for  $\cos \vartheta \lesseqgtr 0$ , then<sup>[9]</sup>
- $\frac{d\sigma}{d\varphi_{\vartheta}} \propto 1 + \frac{\sqrt{2}\lambda_{\vartheta\varphi}}{3 + \lambda_{\vartheta}} \cos \varphi_{\vartheta}$



<sup>9</sup>I. Abt *et al.* (HERA-B Collaboration), *Eur. Phys. J. C* **60**, 517 (2009).

# Importance of Polarization

- Polarization predictions are strong tests of production models
- Detector acceptance depends on polarization hypothesis
- Understanding polarization helps narrow systematic uncertainties

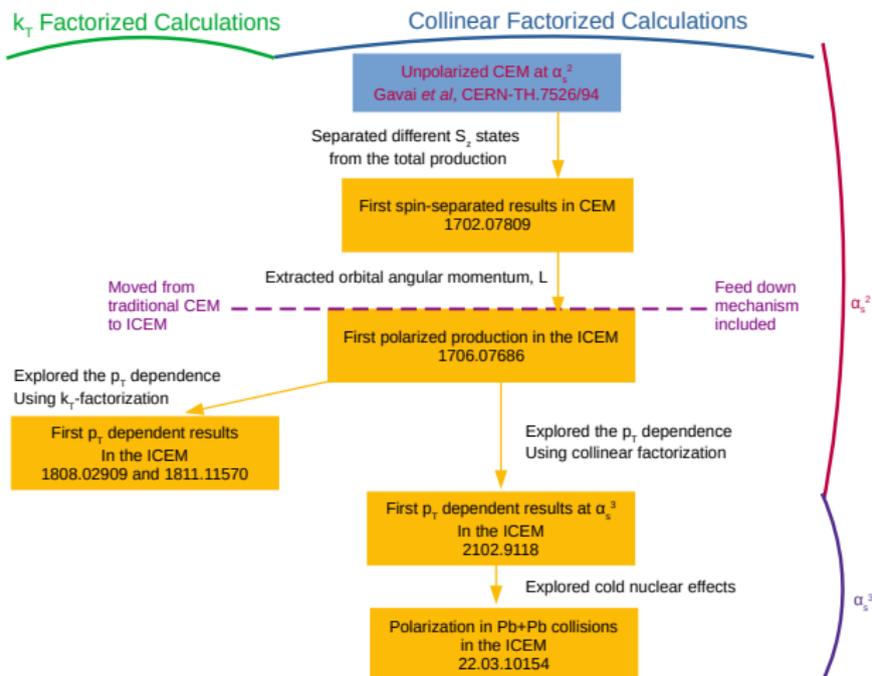


<sup>10</sup>R. Aaij *et al.* (LHCb Collaboration), *Eur. Phys. J. C* **71**, 1645 (2011).

<sup>11</sup>G. Aad *et al.* (ATLAS Collaboration), *Nucl. Phys. B* **850**, 387 (2011).

# Polarized Production in the CEM and ICEM

- No polarization calculations made in the CEM family before 2017.
- It is worth revisiting back the CEM to calculate polarized results
- VC and Ramona Vogt made a few calculations using the (I)CEM.



## How we started at $\mathcal{O}(\alpha_s^2)$

In terms of the Dirac spinors  $u$  and  $v$ , the individual amplitudes at leading order are

$$\begin{aligned}\mathcal{A}_{qq} &= \frac{g_s^2}{\hat{s}} [\bar{u}(p') \gamma_\mu v(p)] [\bar{v}(k) \gamma^\mu u(k')] , \\ \mathcal{A}_{gg,s} &= -\frac{g_s^2}{\hat{s}} \left\{ -2k' \cdot \epsilon(k) [\bar{u}(p') \not{\epsilon}(k') v(p)] \right. \\ &\quad + 2k \cdot \epsilon(k') [\bar{u}(p') \not{\epsilon}(k) v(p)] \\ &\quad \left. + \epsilon(k) \cdot \epsilon(k') [\bar{u}(p') (\not{k}' - \not{k}) v(p)] \right\} , \\ \mathcal{A}_{gg,t} &= -\frac{g_s^2}{\hat{t} - M^2} \bar{u}(p') \not{\epsilon}(k') (\not{k} - \not{p} + M) \not{\epsilon}(k) v(p) , \\ \mathcal{A}_{gg,u} &= -\frac{g_s^2}{\hat{u} - M^2} \bar{u}(p') \not{\epsilon}(k) (\not{k}' - \not{p} + M) \not{\epsilon}(k') v(p) ,\end{aligned}$$

- $\mathcal{A}$ 's are separated according to the  $|S, S_z\rangle$  of the final state
- Orbital Angular Momentum is extracted before squaring the amplitudes

# Orbital Angular Momentum

To extract the projection on a state with orbital-angular-momentum quantum number  $L$ , we determine the corresponding Legendre component  $\mathcal{A}_L$  in the amplitudes by

$$\begin{aligned}\mathcal{A}_{L=0} &= \frac{1}{2} \int_{-1}^1 dx \mathcal{A}(x = \cos \theta) , \\ \mathcal{A}_{L=1} &= \frac{3}{2} \int_{-1}^1 dx x \mathcal{A}(x = \cos \theta) .\end{aligned}$$

$L = 2$  amplitudes are not needed for S and  $\chi$  states production.

# Feed Down Production<sup>12</sup>

CEM polarization calculations assume two pions are emitted from an S state feed down and a photon is emitted from a P state feed down.

$$R_{J/\psi}^{J_z=0} = \sum_{\psi, J_z} c_\psi S_\psi^{J_z} R_\psi^{J_z}, R_{\Upsilon(1S)}^{J_z=0} = \sum_{\Upsilon, J_z} c_\Upsilon S_\Upsilon^{J_z} R_\Upsilon^{J_z},$$

Q	$M_Q$ (GeV)	$c_Q$	$S_Q^{J_z=0}$	$S_Q^{J_z=\pm 1}$
$J/\psi$	3.10	0.62	1	0
$\psi(2S)$	3.69	0.08	1	0
$\chi_{c1}(1P)$	3.51	0.16	0	1/2
$\chi_{c2}(1P)$	3.56	0.14	2/3	1/2
$\Upsilon(1S)$	9.46	0.52	1	0
$\Upsilon(2S)$	10.0	0.1	1	0
$\Upsilon(3S)$	10.4	0.02	1	0
$\chi_{b1}(1P)$	9.89	0.13	0	1/2
$\chi_{b2}(1P)$	9.91	0.13	2/3	1/2
$\chi_{b1}(2P)$	10.3	0.05	0	1/2
$\chi_{b2}(2P)$	10.3	0.05	2/3	1/2

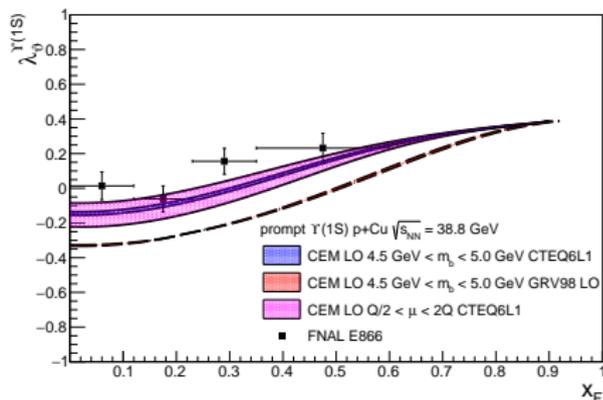
<sup>12</sup>S. Digal, P. Petreczky, and H. Satz, Phys. Rev. D **64**, 094015 (2001).

# Comparing $x_F$ Dependence with Fixed-Target Data<sup>13</sup>

CEM polarization calculation using collinear factorization:

$$J^P = 1^- \text{ (S states)}$$

$$\lambda_{\vartheta} = \frac{1 - 3R^{J_z=0}}{1 + R^{J_z=0}}$$



$x_F$  ( $x_1 - x_2$ ) Dependence (EPS09 for Cu PDFs)

- longitudinally polarized at small  $|x_F|$  and transversely polarized at large  $|x_F|$
- prediction is consistent with the  $\sim 0$  polarization for  $\Upsilon(1S)$

<sup>13</sup>C. N. Brown *et al.* (NuSea Collaboration), Phys. Rev. Lett. **86**, 2529 (2001).

## Calculation at $\mathcal{O}(\alpha_s^2)$ using $k_T$ -factorization

In our calculations using  $k_T$ -factorization, we compute the scattering amplitudes  $\mathcal{A}(\mathcal{R}\mathcal{R} \rightarrow Q\bar{Q})$ :

$$\begin{aligned}\mathcal{A}(\mathcal{R}\mathcal{R} \rightarrow Q\bar{Q}) &= \epsilon(k)^\mu \epsilon(k')^\nu \mathcal{A}_{\mu\nu}(gg \rightarrow Q\bar{Q}), \\ \epsilon(k)^\mu &= \left(0, \frac{\vec{k}_T}{|k_T|}, 0\right),\end{aligned}$$

$\mathcal{A}$ 's are separated according to the  $|S, S_z\rangle$  of the final state. We then determine the corresponding Legendre component  $\mathcal{A}_L$  in the amplitudes by

$$\begin{aligned}\mathcal{A}_{L=0} &= \frac{1}{2} \int_{-1}^1 dx \mathcal{A}(x = \cos\theta), \\ \mathcal{A}_{L=1} &= \frac{3}{2} \int_{-1}^1 dx x \mathcal{A}(x = \cos\theta).\end{aligned}$$

$L = 2$  amplitudes are not needed for S and  $\chi$  states production. Only  $\mathcal{A}_{gg}$ 's are used in the  $k_T$ -factorization approach

# Production in $k_T$ -factorized ICEM

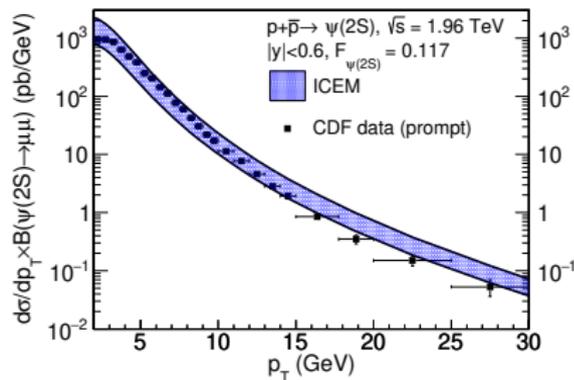
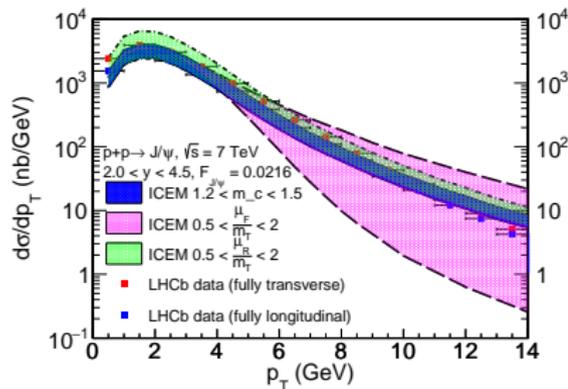
## Production cross section

$$\begin{aligned}\sigma &= F_Q \int_{M_Q^2}^{4m_H^2} d\hat{s} \int dx_1 \int dx_2 \int dk_{1T}^2 \int dk_{2T}^2 \int \frac{d\phi_1}{2\pi} \int \frac{d\phi_2}{2\pi} \\ &\times \Phi_1(x_1, k_{1T}, Q_1) \Phi_2(x_2, k_{2T}, Q_2) \hat{\sigma}(\mathcal{R} + \mathcal{R} \rightarrow Q\bar{Q}) \\ &\times \delta(\hat{s} - x_1 x_2 s + |\vec{k}_{1T} + \vec{k}_{2T}|^2)\end{aligned}$$

## Parameters used

- We used JH-2013<sup>[5]</sup> unintegrated (transverse-momentum-dependent) PDF set for  $\Phi(x, k_T, Q)$
- factorization scale set at  $Q = m_T$
- $1.27 < m_c < 1.50$  GeV,  $4.5 < m_b < 5.0$  GeV
- $\frac{1}{2} < \frac{\mu_r}{m_T} < 2$

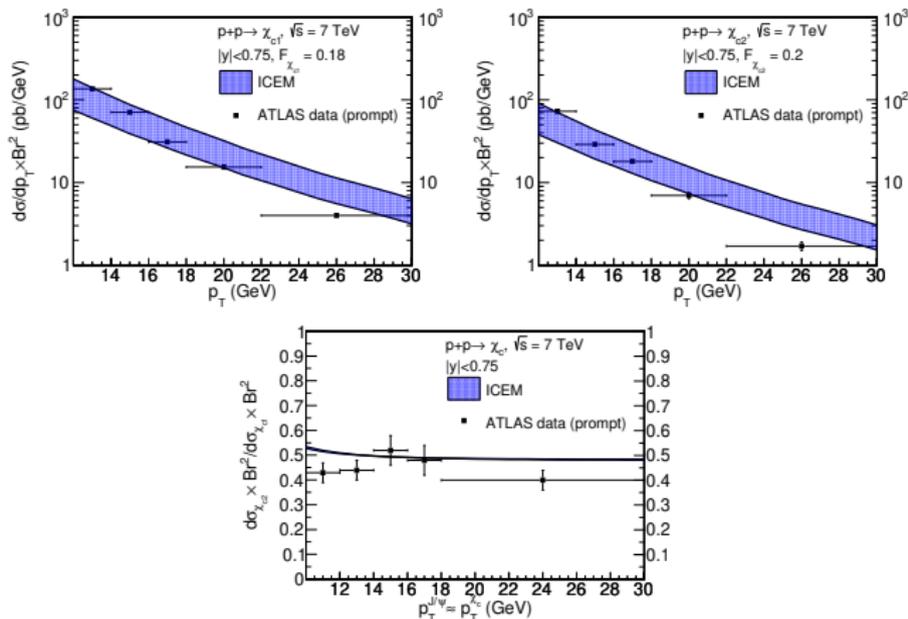
# Charmonium production in $k_T$ -factorized ICEM<sup>[14]</sup>



- We obtained  $F_{J/\psi}$  while assuming a constant direct-to-inclusive ratio of 0.62 for  $J/\psi$ .
- We also compare our directly produced  $\psi(2S)$  to the prompt production of  $\psi(2S)$  to obtain  $F_{\psi(2S)}$ .
- The ICEM with  $k_T$ -factorization is able to describe the yield, but having a strong dependence on factorization scale at high  $p_T$ .

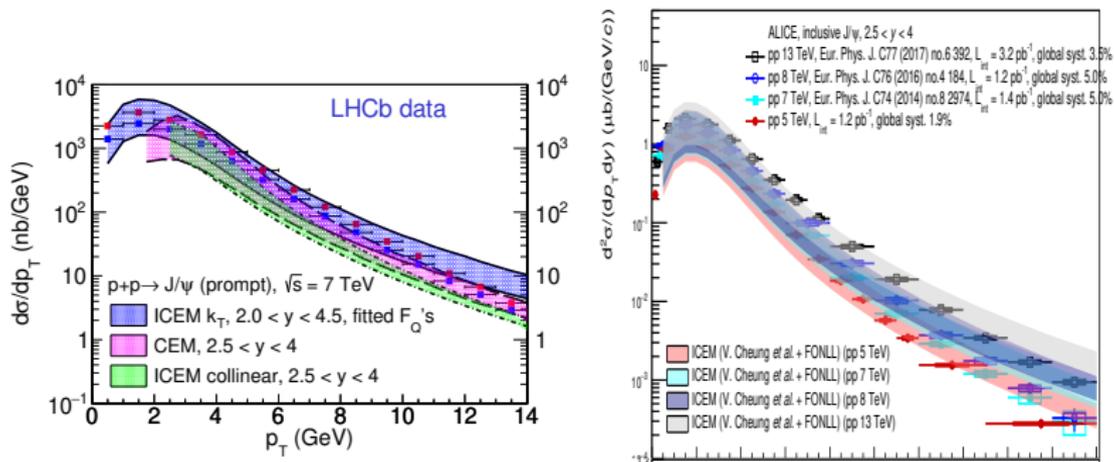
<sup>14</sup>V. Cheung and R. Vogt, Phys. Rev. D **98**, 114029 (2018) and **99**, 034007 (2019).

# $\chi_c$ production in $k_T$ -factorized ICEM<sup>[14]</sup>



- We also compare our results to  $\chi_c$  production at ATLAS to obtain the  $F_Q$ 's as well.
- We found the relative production is stable at high  $p_T$ . This is consistent with the data.

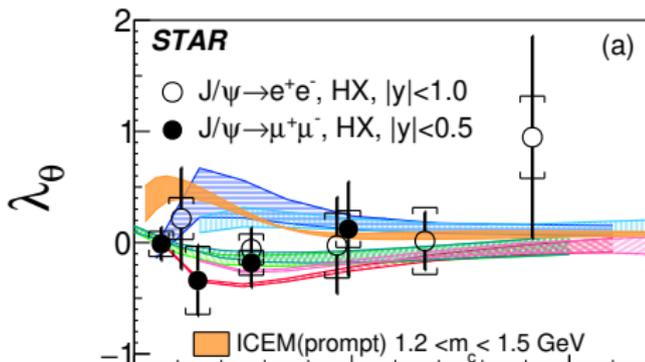
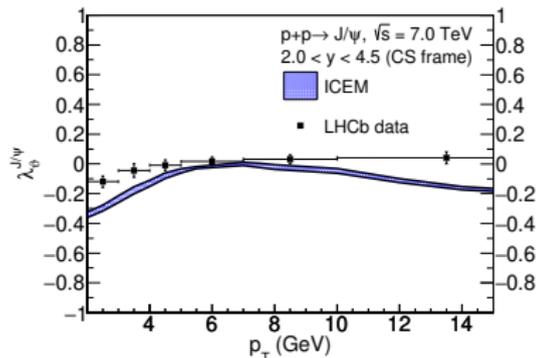
# Prompt and inclusive $J/\psi$ in $k_T$ -factorized ICEM<sup>[14]</sup>



- With all the  $F_Q$ 's fitted for all S states and P states, the prompt  $J/\psi$  yield can be calculated.
- The  $k_T$ -factorized ICEM agrees with previous collinear (I)CEM calculations.
- When B feed-down is also added using FONLL, we found agreement with inclusive  $J/\psi$  production in a large range of beam energies.

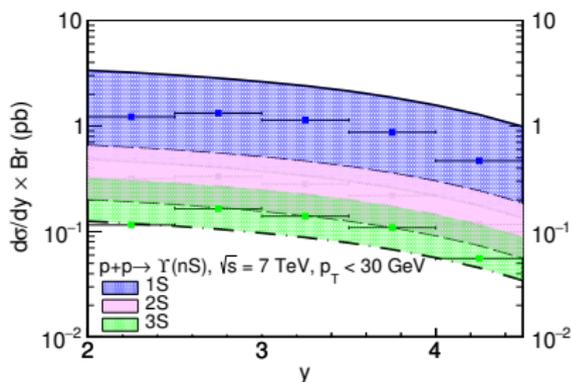
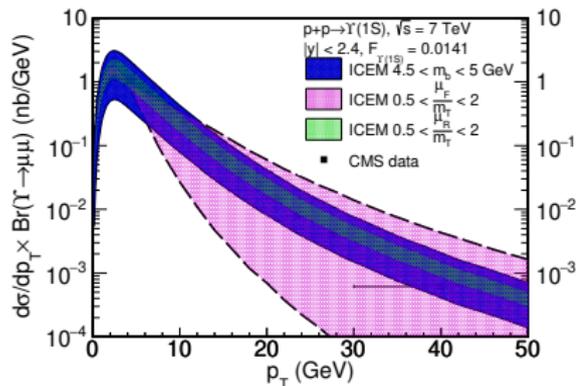
# $J/\psi$ polarization in $k_T$ -factorized ICEM<sup>[14]</sup>

Polarization is independent of  $F_Q$  and scales, mass is the only uncertainty



- We found the prompt production of  $J/\psi$  is slightly longitudinally polarized in the CS frame.
- Slightly transversely polarized in the HX frame.
- Agreement with polarization data is frame-dependent at low  $p_T$ .

# $\Upsilon$ production in $k_T$ -factorized ICEM<sup>[14]</sup>



- The  $p_T$ -distributions for  $\Upsilon$  production also have a strong dependence on factorization scale at high  $p_T$ .
- When the factorization scale is set at  $m_T$ , both  $p_T$  and  $y$  distributions are described.

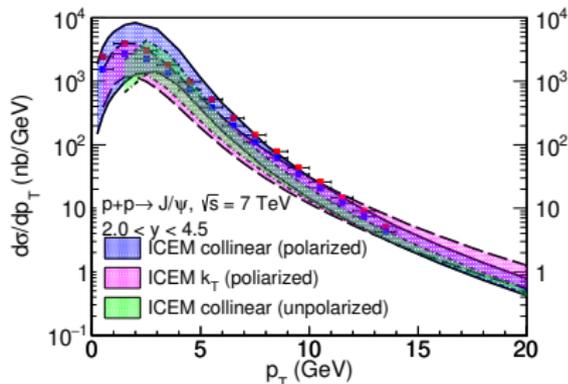
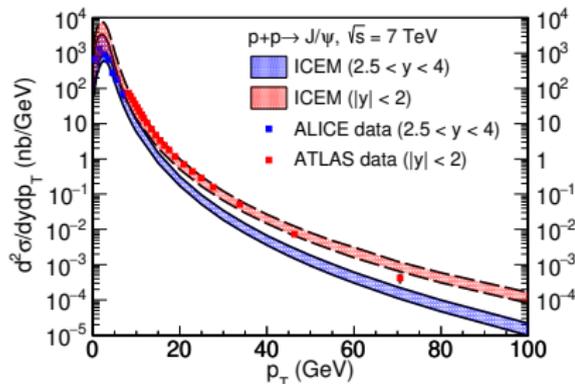
## Production distribution

$$\frac{d^2\sigma}{dp_T dy} = F_Q \sum_{i,j=\{q,\bar{q},g\}} \int_{M_Q}^{2m_H} dM_\psi \int d\hat{s} dx_1 dx_2 f_{i/p}(x_1, \mu^2) f_{j/p}(x_2, \mu^2) d\hat{\sigma}_{ij \rightarrow c\bar{c}+X},$$

- We consider all 16 diagrams from  $gg \rightarrow c\bar{c}g$ , 5(+5) from  $gq(\bar{q}) \rightarrow c\bar{c} q(\bar{q})$ , and 5 from  $q\bar{q} \rightarrow c\bar{c}g$  with the projection operator applied at the diagram level.
- The  $c\bar{c}$  produced are the proto- $J/\psi$  before hadronization.
- We used the CT14 PDFs in our calculations.
- $k_T$ -smearing is applied to the initial state partons to provide better description at low  $p_T$
- First  $p_T$ -dependent polarization results using collinear factorization
- $1.18 < m_c < 1.36$  GeV,  $\mu_F/m_T = 2.1_{-0.85}^{+2.55}$ ,  $\mu_R/m_T = 1.6_{-0.12}^{+0.11}$
- same set of variations used in MV (2016) and NVF [PRC **87**, 014908 (2013)]

<sup>15</sup>V. Cheung and R. Vogt, PRD **104**, 094026(2021).

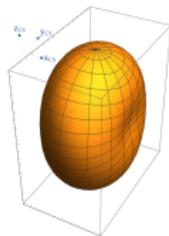
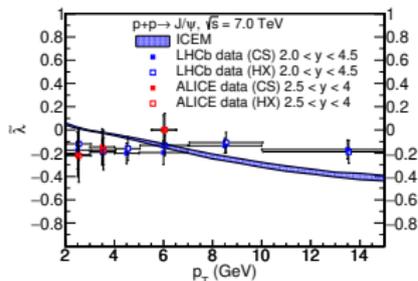
# Collinear ICEM Unpolarized Cross Sections<sup>[15]</sup>



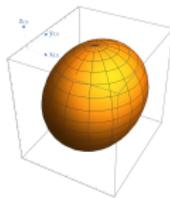
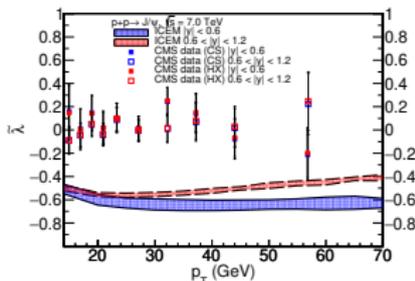
- a small kick of  $\langle k_T^2 \rangle \sim 1 \text{ GeV}^2$  given to each initial state parton.
- The uncertainty band<sup>[5]</sup> is constructed by varying the charm quark mass, factorization scale, and renormalization scale.
- We find agreement with the  $p_T$ -distribution measured by the LHCb<sup>[16]</sup>.
- We also find agreement with the unpolarized ICEM calculations [MV (2016)].

<sup>16</sup>R. Aaij *et al.* (LHCb Collaboration), *Eur. Phys. J. C* **73**, 2631 (2013).

# Invariant Polarization Parameter in Collinear ICEM<sup>[16]</sup>



ICEM ( $p_T = 12 \text{ GeV}$ )



LHCb data ( $10 < p_T < 15 \text{ GeV}$ )

- The frame-invariant polarization parameter  $\tilde{\lambda} = \frac{\lambda_\theta + 3\lambda_\varphi}{1 - \lambda_\varphi}$
- Comparing the frame-invariant polarization parameter removes frame-induced kinematic dependencies
- We find agreement with the invariant polarization at LHCb<sup>[6]</sup>, but discrepancy between high  $p_T$  data at CMS<sup>[7]</sup>.

# $J/\psi$ production in Pb+Pb collisions

## How different is $J/\psi$ in Pb+Pb compared to in $p + p$ collisions

- Suppression
  - ▶ higher mass states suppressed first
  - ▶ color singlets and color octets could have different suppression rates
- Regeneration from uncorrelated  $c\bar{c}$  pairs
  - ▶ at low  $p_T$  and particularly at midrapidity

## What $J/\psi$ polarization in Pb+Pb collisions can teach us

- If hadronization is a fast process, then polarization should not be significantly different than in  $p + p$
- If it takes longer, then the polarization can be different as color singlets and octets have different polarization

## What we can do in ICEM (now)?

- Cold Nuclear Matter Effects
  - ▶  $k_T$ -broadening
  - ▶ nPDFs

# Polarization in Pb+Pb using the ICEM Approach

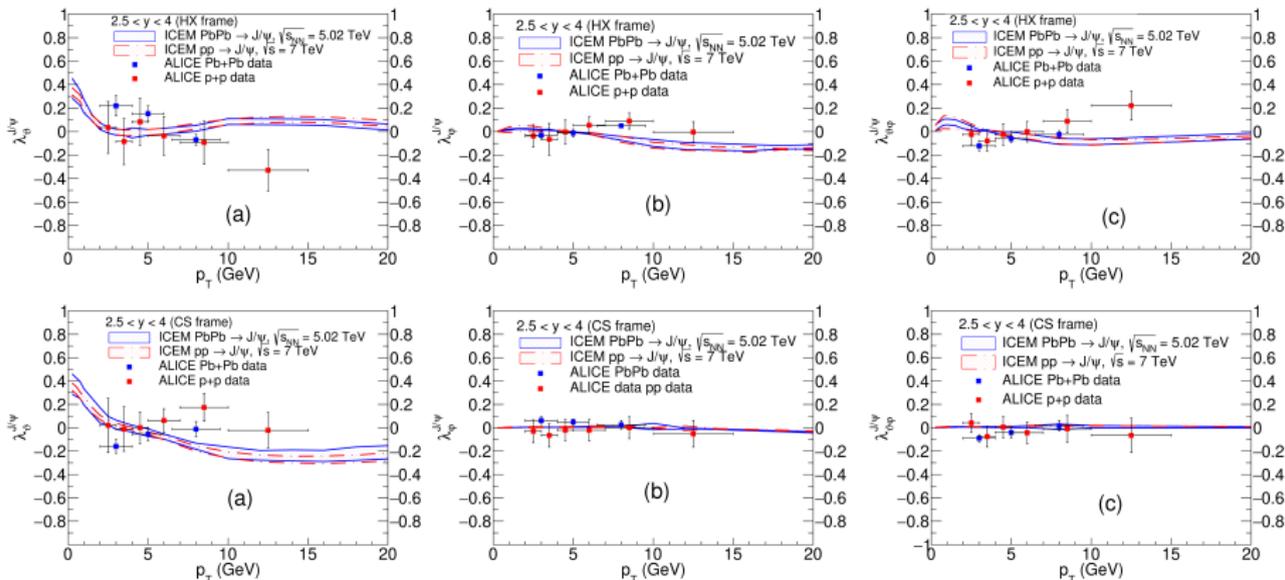
PRC.105.055202 (2022).

## Production distribution

$$\frac{d^2\sigma}{dp_T dy} = F_Q \sum_{i,j=\{q,\bar{q},g\}} \int_{M_Q}^{2m_H} dM_\psi \int d\hat{s} dx_1 dx_2 f_{i/A}(x_1, \mu^2) f_{j/A}(x_2, \mu^2) d\hat{\sigma}_{ij \rightarrow c\bar{c}+X},$$

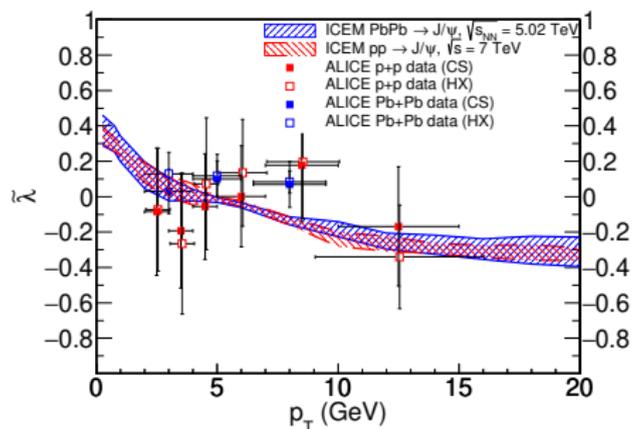
- We consider all diagrams that produces  $c\bar{c}$  with a parton.
- The  $c\bar{c}$  produced are the proto- $J/\psi$  before hadronization.
- We used the CT14 PDFs and EPPS16 nuclear modifications in our calculations.
- $k_T$ -smearing (gaussian) is applied to the initial state partons to provide better description at low  $p_T$ .
- $\langle k_T^2 \rangle = 1 + (1/12) \ln(\sqrt{s}/20 \text{ GeV})$
- An additional kick of  $0.41 \text{ GeV}^2$  is added to partons from Pb nuclei.
- $1.18 < m_c < 1.36 \text{ GeV}$ ,  $\mu_F/m_T = 2.1_{-0.85}^{+2.55}$ ,  $\mu_R/m_T = 1.6_{-0.12}^{+0.11}$
- same set of variations used in MV [2016] and NVF [PRC **87**, 014908 (2013)]

# Polarization in Pb+Pb compared to $p+p$



- Note that there is a 40% difference in collision energy per nucleon.
- No significant differences between the  $p + p$  and Pb+Pb.
- Choosing another shadowing set will not change the polarization.
- Similar lack of system and energy dependence is also expected from CGC+NRQCD approach (PRD 104, 034004)

# Invariant Polarization



- The polarization parameters shown on the previous slide ( $\lambda_\theta, \lambda_\varphi, \lambda_{\theta\varphi}$ ) depend on the frame.
- It is possible to construct an invariant polarization parameter because the angular distribution is rotationally invariant:
- $$\tilde{\lambda} = \frac{\lambda_\theta + 3\lambda_\varphi}{1 - \lambda_\varphi}$$
- It is possible to remove the frame-induced kinematic dependences when comparing theoretical predictions to data by comparing  $\tilde{\lambda}$ .

## Lack of system and energy dependence in ICEM polarization

- Polarization parameters depend on the ratio of the polarized cross sections
- The numerator and denominator of the polarization parameters are affected similarly
- Although yields can be very different, polarization parameters are similar.

## There are effects that are not modeled

- No feed down are included, but data in this region are unable to tell the effect of potential loss of feed down due to large uncertainties
- Hot effects such as regeneration are neglected, but regeneration is concentrated at low  $p_T$  and more important at midrapidity than at forward rapidity.
- Suppression by comovers is neglected.

## What the experimental results are showing

- The polarization in these two systems is consistent within uncertainties
- Feed down from excited states does not strongly affect the prompt  $J/\psi$  polarization

## Possible further investigations

- Polarization of regenerated quarkonium states
- Centrality dependence of polarization
  - ▶ preliminary results from ALICE: no dependence
  - ▶ PoS HardProbes2020, 095 (2021)
- Extending the Pb+Pb polarization data to  $p_T > 10$  GeV where regeneration is no longer important
- $\psi(2S)$  polarization as an independent check
  - ▶ much more difficult due to strong suppression

# Photoproduction in ICEM at $\mathcal{O}(\alpha\alpha_s^2)$ <sup>[17]</sup>

## Production distribution

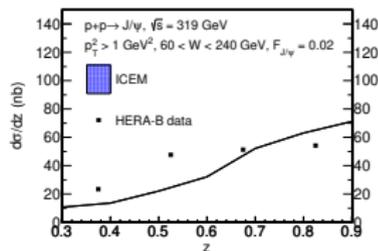
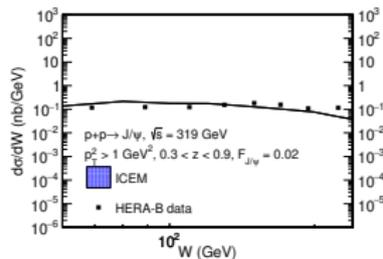
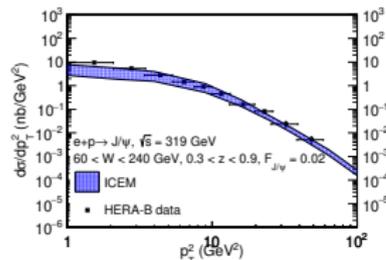
$$\frac{d^2\sigma}{dp_T^2 dW^2 dz} = F_Q \sum_{j=\{q,\bar{q},g\}} \int_{M_Q}^{2m_H} dM_\psi \int dy dx_2 f_{\gamma/e}(y, Q^2) f_{j/p}(x_2, \mu^2) d\hat{\sigma}_{\gamma j \rightarrow c\bar{c}+X},$$

- Currently all 8 diagrams from  $\gamma g \rightarrow c\bar{c}$  channel are included
- The  $c\bar{c}$  produced are the proto- $J/\psi$  before hadronization.
- We used the CT14 PDFs and Weizsacker-Williams approximation in our calculations.
- $k_T$ -smearing is applied to the hadronic initial state partons
- First photoproduction results in the ICEM
- $1.18 < m_c < 1.36$  GeV,  $\mu_F/m_T = 2.1_{-0.85}^{+2.55}$ ,  $\mu_R/m_T = 1.6_{-0.12}^{+0.11}$
- Preliminary results are compared to low  $Q^2$  measurements

<sup>17</sup>V. Cheung and R. Vogt, in progress.

# Photoproduction Results in ICEM<sup>[17]</sup>

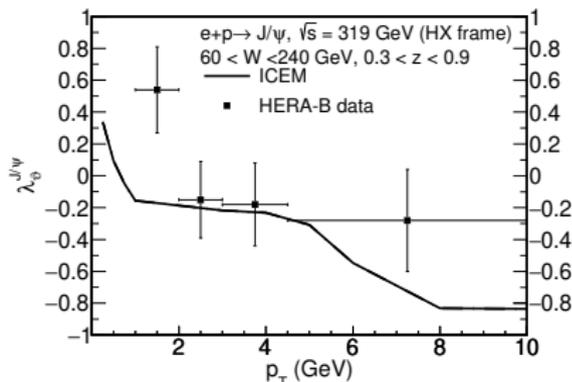
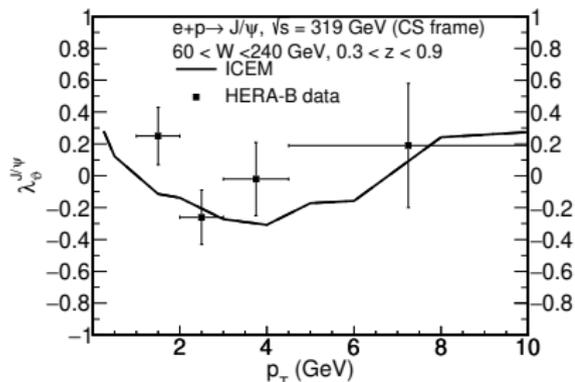
$$W^2 = (q + p)^2, \quad z = (p_\psi \cdot p)/(q \cdot p)$$



- Our preliminary results find agreement with the  $p_T$  and  $W$  distribution at HERA<sup>[18]</sup>,
- and fair agreement with the  $z$  distribution.
- The fit parameter in the model,  $F_Q$ , is about 2%, consistent with previous CEM results in hadroproduction.

<sup>18</sup>F. D. Aaron *et al.* (H1 Collaboration), *Eur. Phys. J. C* **68**, 401-420 (2010).

# Photoproduction Results in ICEM<sup>[17]</sup>



- In the CS frame, the polarization is slightly transverse at low  $p_T$ , then slightly longitudinal at moderate  $p_T$ , and becomes slightly transverse again as  $p_T$  grows.
- In the HX frame, the polarization is transverse at low  $p_T$ , then becomes longitudinal as  $p_T$  grows.
- These trends from our preliminary results are consistent with the HERA-B data<sup>[18]</sup>

# Conclusion and Future

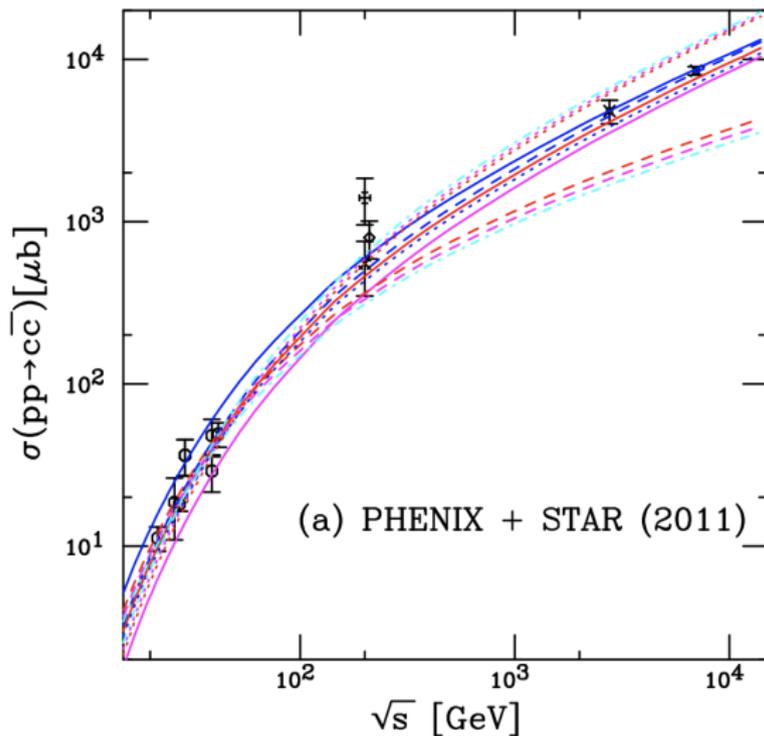
## In this talk, I

- showed recent attempts to describe quarkonium production using the (I)CEM
- showed expansions of our approach beyond  $p + p$  collisions

## We are working on

- including effects from feed down production.
- production in  $ep$  via photo-production.
- photo-production in CGC+NRQCD and CGC+ICEM.

# Backup Slides



## How $|J, J_z\rangle$ states are formed

Two helicity combinations that result in  $S_z = 0$  are added and normalized to give contribution to the spin triplet state ( $S = 1$ ). We calculate the amplitudes for  $J = 0, 1, 2$ :

$$\mathcal{A}_{J=1, J_z=\pm 1} = \mathcal{A}_{L=0, L_z=0; S=1, S_z=\pm 1}, (\text{S States})$$

$$\mathcal{A}_{J=1, J_z=0} = \mathcal{A}_{L=0, L_z=0; S=1, S_z=0}, (\text{S States})$$

$$\mathcal{A}_{J=0, J_z=0} = -\sqrt{\frac{1}{3}} \mathcal{A}_{L=1, L_z=0; S=1, S_z=0}, (\chi_0 \text{ States})$$

$$\mathcal{A}_{J=1, J_z=\pm 1} = \mp \frac{1}{\sqrt{2}} \mathcal{A}_{L=1, L_z=0; S=1, S_z=\pm 1}, (\chi_1 \text{ States})$$

$$\mathcal{A}_{J=1, J_z=0} = 0, (\chi_1 \text{ States})$$

$$\mathcal{A}_{J=2, J_z=\pm 2} = 0, (\chi_2 \text{ States})$$

$$\mathcal{A}_{J=2, J_z=\pm 1} = \frac{1}{\sqrt{2}} \mathcal{A}_{L=1, L_z=0; S=1, S_z=\pm 1}, (\chi_2 \text{ States})$$

$$\mathcal{A}_{J=2, J_z=0} = \sqrt{\frac{2}{3}} \mathcal{A}_{L=1, L_z=0; S=1, S_z=0}, (\chi_2 \text{ States})$$

# Production formula in collinear CEM at $\mathcal{O}(\alpha_s^2)$

## CEM using collinear factorization approach

$$\sigma = F_Q \sum_{i,j} \int_{M_Q^2}^{4m_H^2} d\hat{s} \int dx_1 dx_2 f_{i/p}(x_1, \mu^2) f_{j/p}(x_2, \mu^2) \hat{\sigma}_{ij}(\hat{s}) \delta(\hat{s} - x_1 x_2 s),$$

- Convolved with the CTEQ6L1 parton distribution functions (PDFs)
- $\alpha_s$  is calculated at one-loop level
- We took the factorization and renormalization scales to be  $\mu^2 = \hat{s}$
- $1.27 < m_c < 1.50$  GeV,  $4.5 < m_b < 5.0$  GeV
- Assumed that the polarization is unchanged by the transition from the parton level to the hadron level

# Presenting Polarization

- The tendency for quarkonium states of spin  $J$  to be in a particular  $|J, J_z\rangle$  state is known as polarization
- For S state ( $J = 1$ ) quarkonium, if  $J_z = 0$ , then it is longitudinally polarized
- If  $J_z = \pm 1$ , then it is transversely polarized
- It is typical to represent the polarization in terms of the polarization parameter,  $\lambda_\theta$ , which ranges from -1 to +1
- For the S states,  $\lambda_\theta = -1$  refers to pure longitudinal production while  $\lambda_\theta = +1$  refers to pure transverse production

$$J^P = 1^- \text{ (S states)}^{[19]}$$

$$\lambda_\theta = \frac{\sigma^{J_z=+1} + \sigma^{J_z=-1} - 2\sigma^{J_z=0}}{\sigma^{J_z=+1} + \sigma^{J_z=-1} + 2\sigma^{J_z=+0}}$$

<sup>19</sup>P. Faccioli, C. Lourenco, J. Seixas, and H. K. Wohri, Eur. Phys. J. C **69**, 657 (2010).

# Presenting Polarization

- For the  $\chi_1$  ( $J = 1$ ) and  $\chi_2$  ( $J = 2$ ) states, the polarization parameter is defined as the polarization parameter of the product  $J/\psi$  or  $\Upsilon(nS)$  if production comes purely from  $\chi$  state feed down
- $\chi_c \rightarrow J/\psi + \gamma$ ,  $\chi_b \rightarrow \Upsilon(nS) + \gamma$

$$J^P = 1^+ (\chi_1 \text{ P states})^{[20]}$$

$$\lambda_\theta = \frac{2\sigma^{J_z=0} - \sigma^{J_z=+1} - \sigma^{J_z=-1}}{2\sigma^{J_z=0} + 3\sigma^{J_z=+1} + 3\sigma^{J_z=-1}}$$

$$J^P = 2^+ (\chi_2 \text{ P states})^{[20]}$$

$$\lambda_\theta = \frac{-6\sigma^{J_z=0} - 3\sigma^{J_z=+1} + 6\sigma^{J_z=+2} - 3\sigma^{J_z=-1} + 6\sigma^{J_z=-2}}{10\sigma^{J_z=0} + 9\sigma^{J_z=+1} + 6\sigma^{J_z=+2} + 9\sigma^{J_z=-1} + 6\sigma^{J_z=-2}}$$

<sup>20</sup>P. Faccioli *et al.*, Phys. Lett. B **773**, 476 (2017).

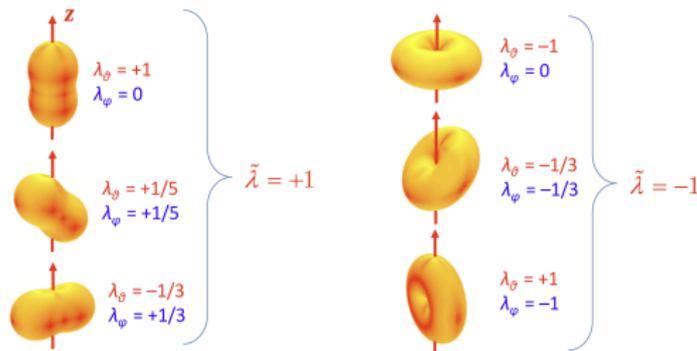
# Visualizing invariant polarization

Azimuthal anisotropy<sup>[19]</sup>

$$\lambda_\phi = \frac{2\text{Re}[a_{+1}a_{-1}^*]}{\mathcal{N} + a_0^2}$$

Frame invariant parameter<sup>[19]</sup>

$$\tilde{\lambda} = \frac{\lambda_\theta - 3\lambda_\phi}{1 - \lambda_\phi}$$



- Calculating invariant  $\tilde{\lambda}$  removes frame-induced kinematic dependencies

# Polarization Puzzle<sup>[21]</sup>

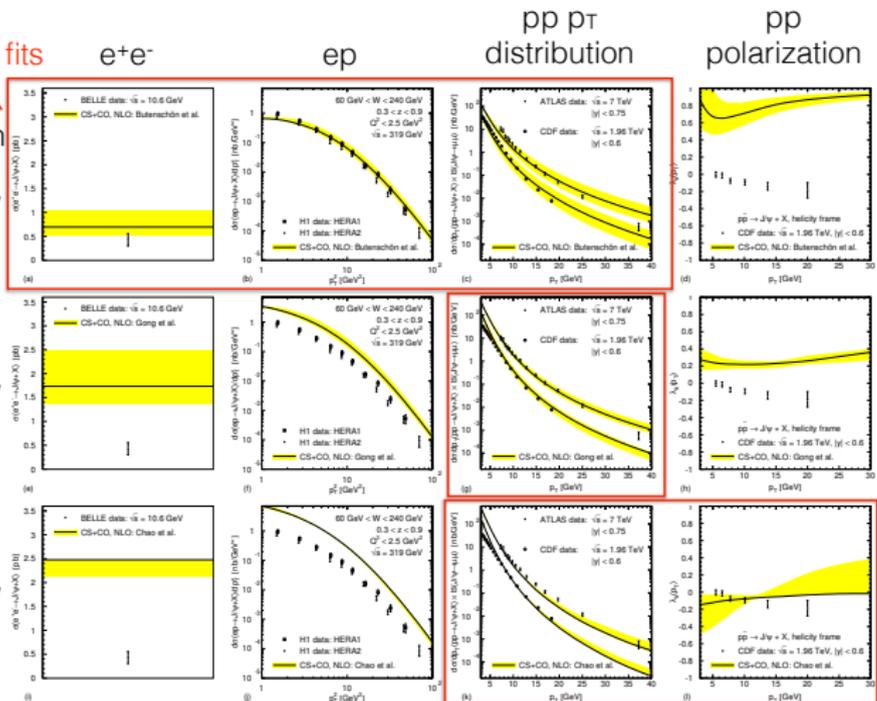
Difficult to describe both the yields and polarizations simultaneously within a given approach (e.g. NRQCD)

Included in fits

Butenschön  
& Kniehl  
 $p_T > 3 \text{ GeV}$

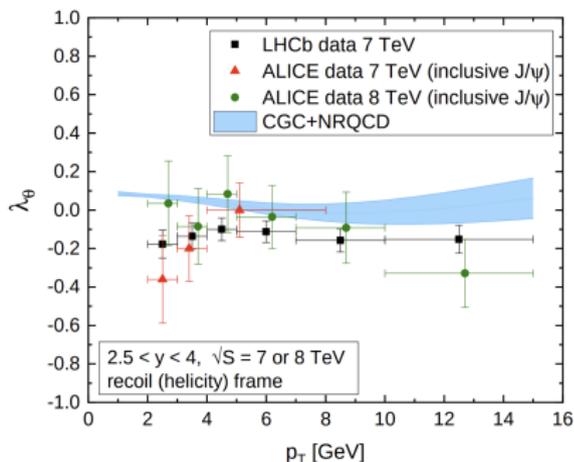
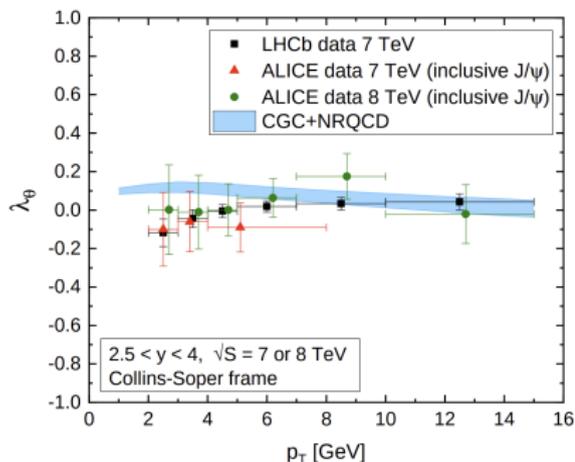
Gong et al.  
 $p_T > 5 \text{ GeV}$

Chao et al.  
 $p_T > 7 \text{ GeV}$



<sup>21</sup>N. Brambilla et al., Eur. Phys. J. C **74**, 2981 (2014)

- is a solution to the polarization puzzle where gluon distribution is calculated using CGC and the conversion of  $Q\bar{Q}$  is described by NRQCD formulation
- able to describe all polarization parameters for  $p_T < 15$  GeV



<sup>22</sup>Y. Q. Ma, T. Stebel, R. Venugopalan, JHEP12 (2018) 057.