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DI PAVIA



Funded by JSA travel fund award



Possible new insights into strong PV in the nucleon's structure from DIS measurements

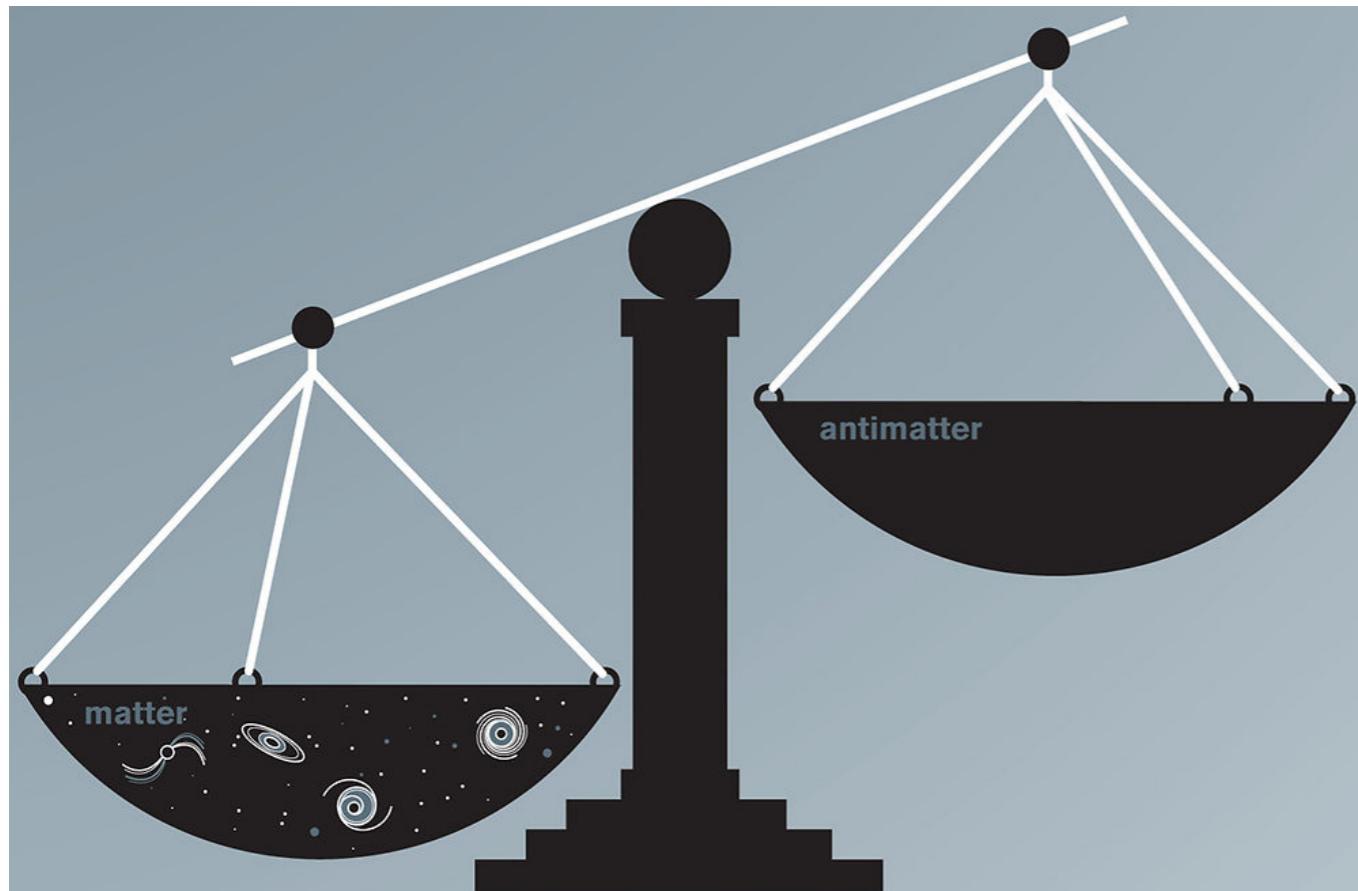
Matteo Cerutti

Electroweak and Beyond the Standard Model Physics at the EIC

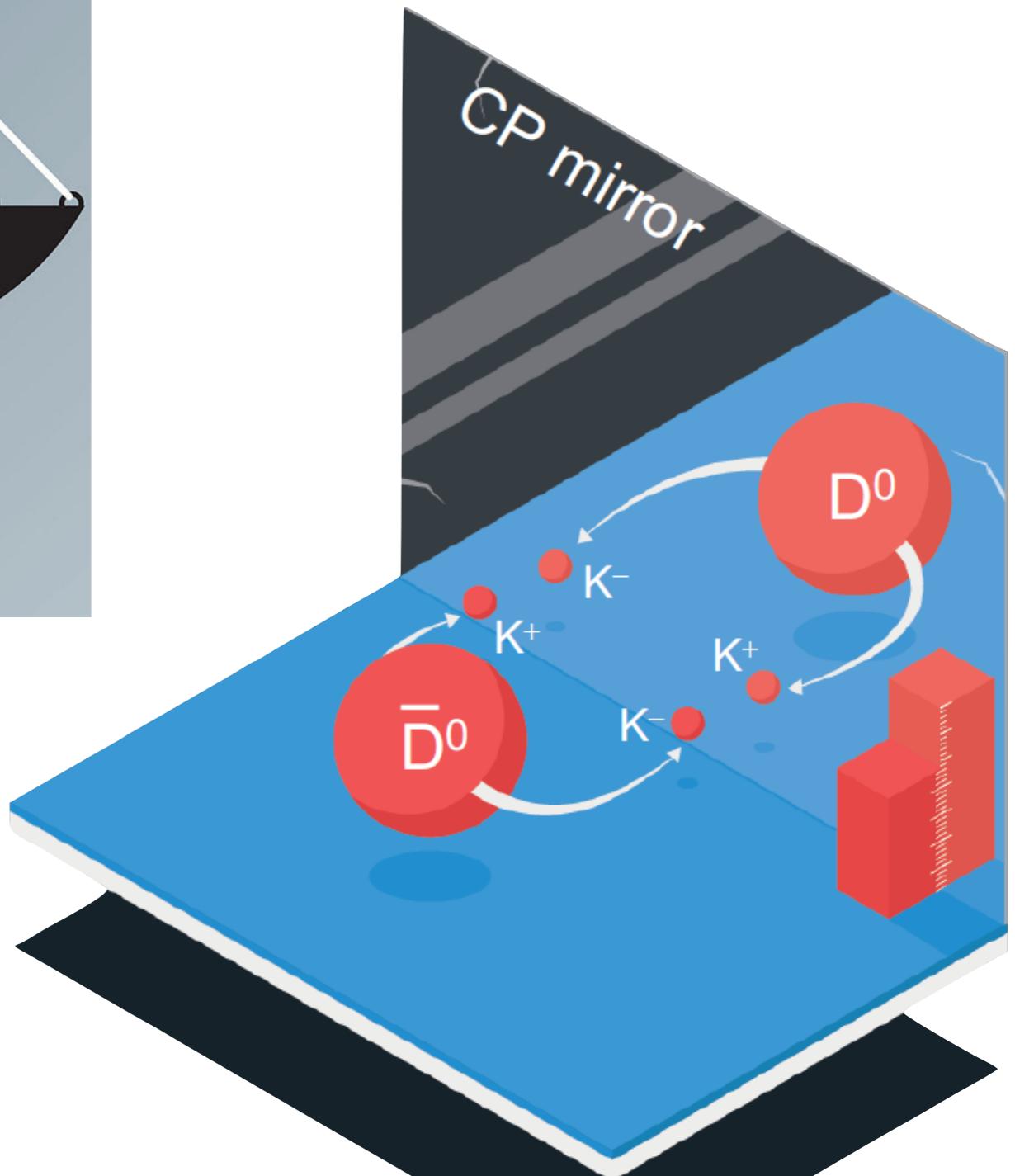
Bacchetta, Cerutti, Radici, Zheng, PLB 849 (2024), arXiv: 2306.04704



Motivations



Investigation of the
“Strong CP problem”



Motivations

EW sector

CP violation is included

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Weak CP

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CP violation is included

too small...



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QCD sector



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Strong CP



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Strong CP

$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$



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QCD sector

Strong CP

$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$

θ -term

SMEFT operators



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QCD sector

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$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$

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SMEFT operators



Nucleon electric dipole moment



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QCD sector

Strong CP

$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$

θ -term

SMEFT operators



Nucleon electric dipole moment

never measured...



Motivations

P-symmetry

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QCD sector

QCD Lagrangian is assumed to be invariant under parity transformations

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*Are there any effects of QCD
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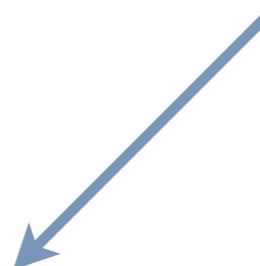
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Terms from EW sector

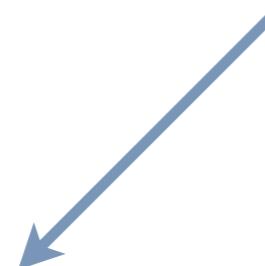
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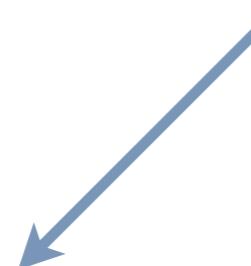
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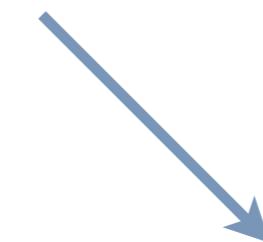
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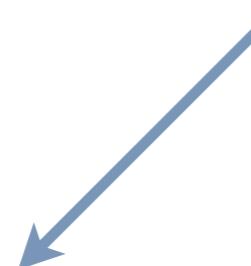
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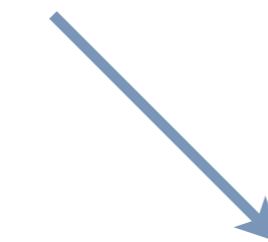
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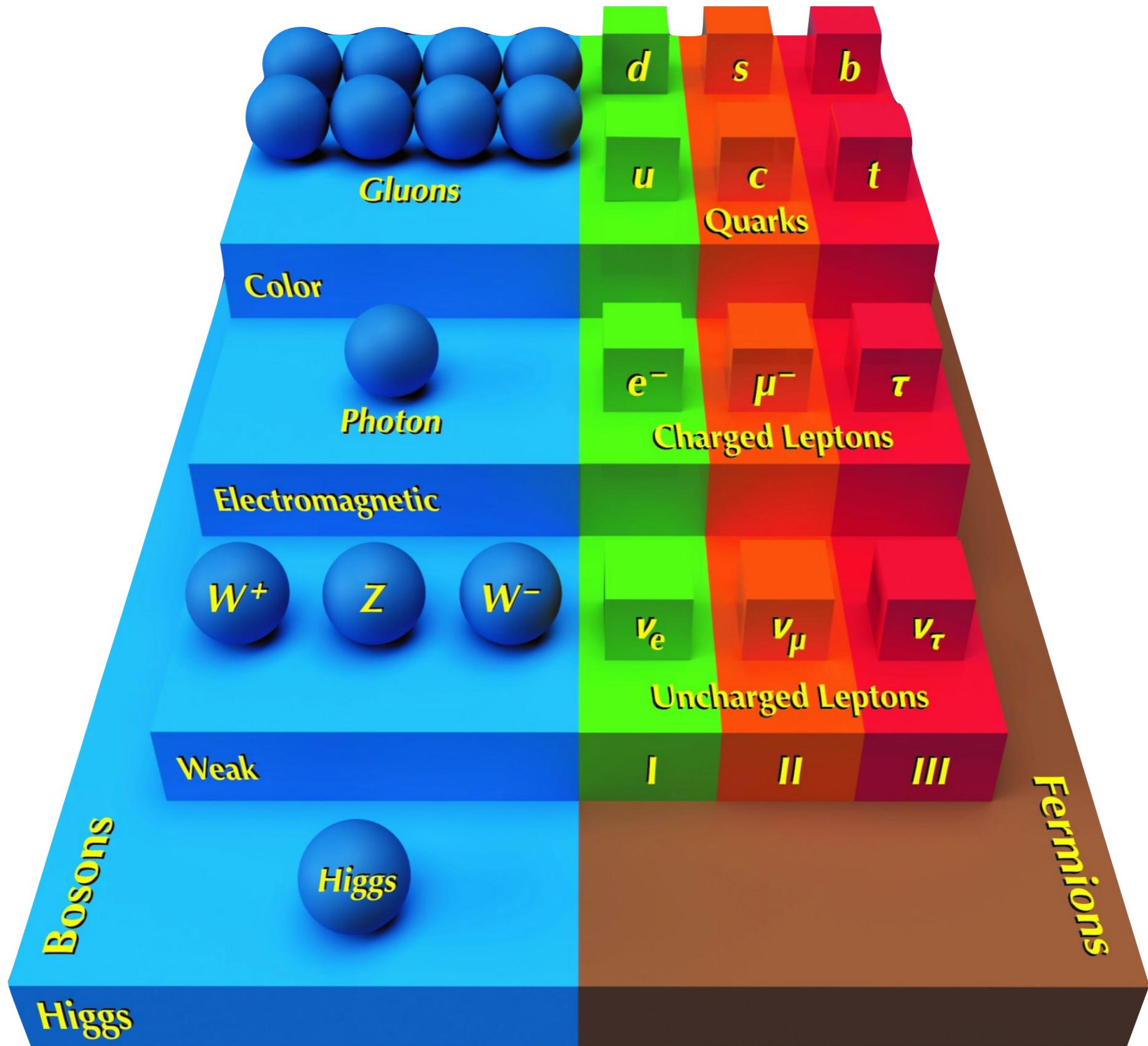
Weak P-violation



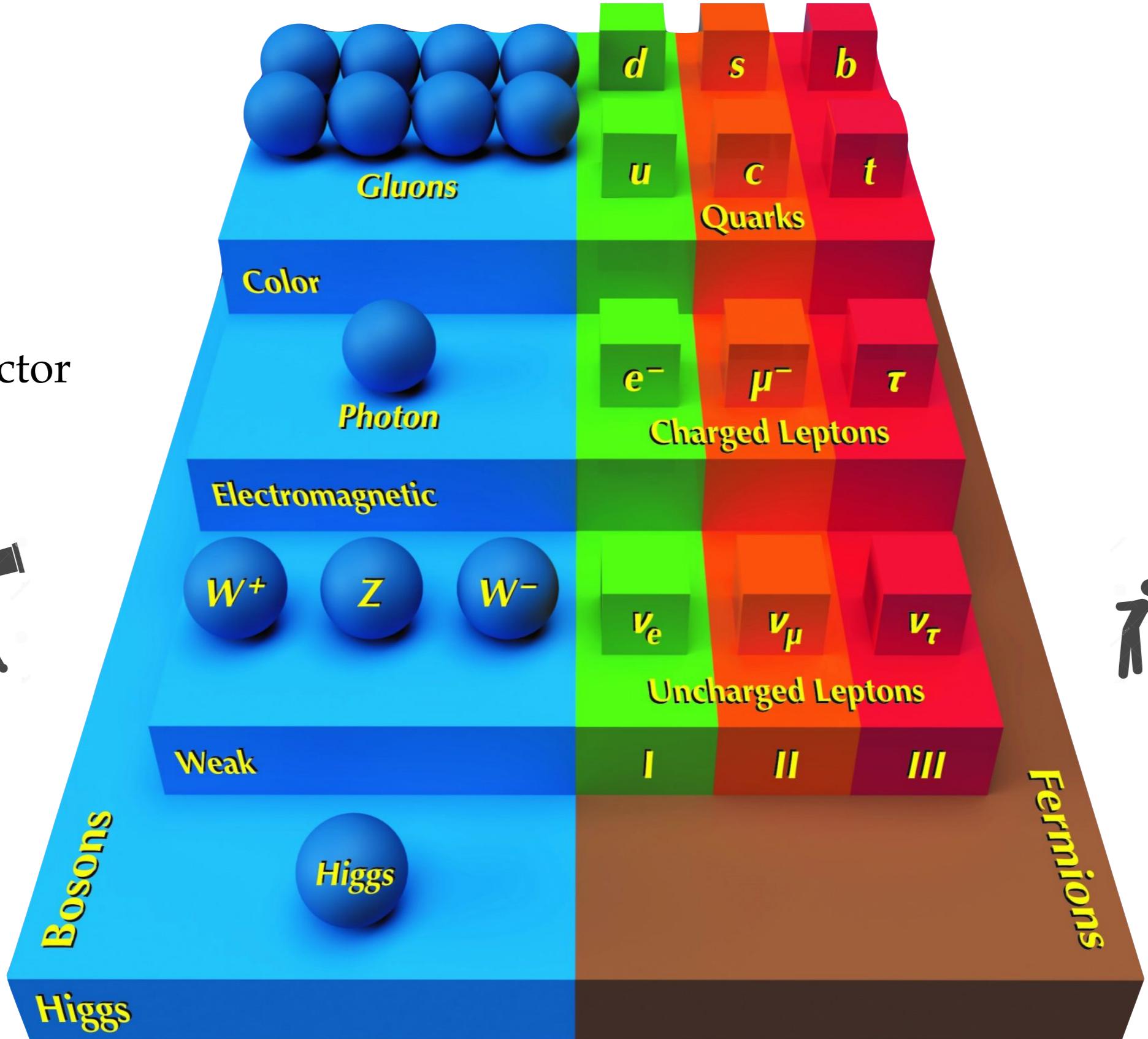
Terms from QCD sector

Strong P-violation

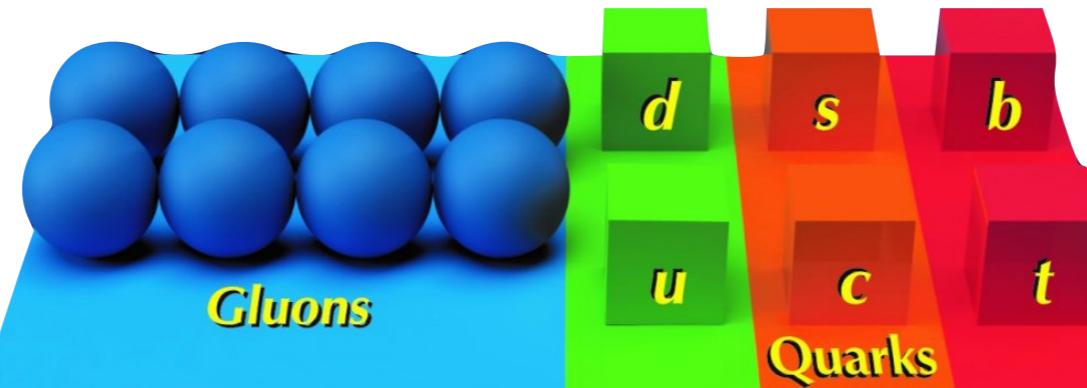




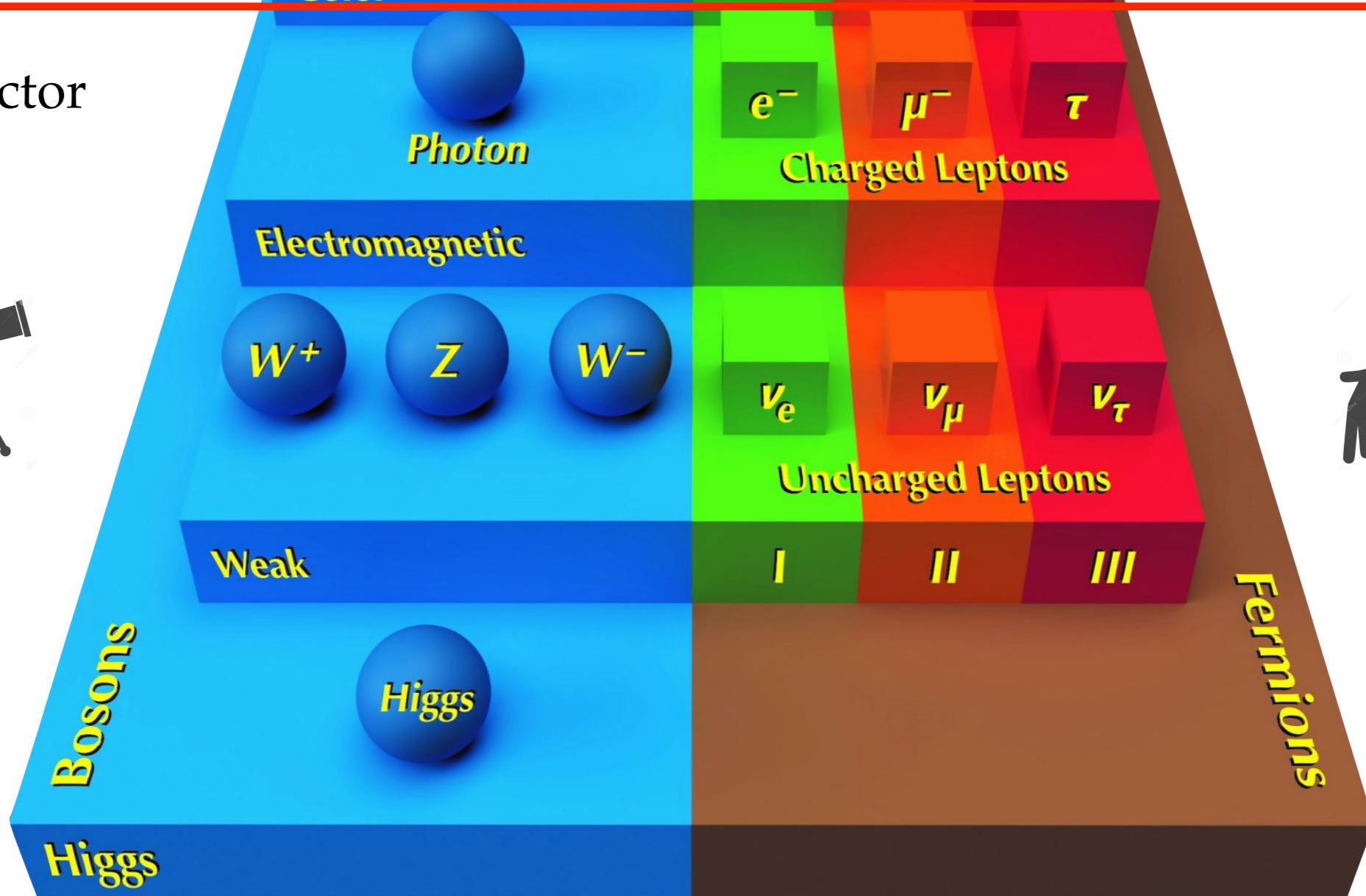
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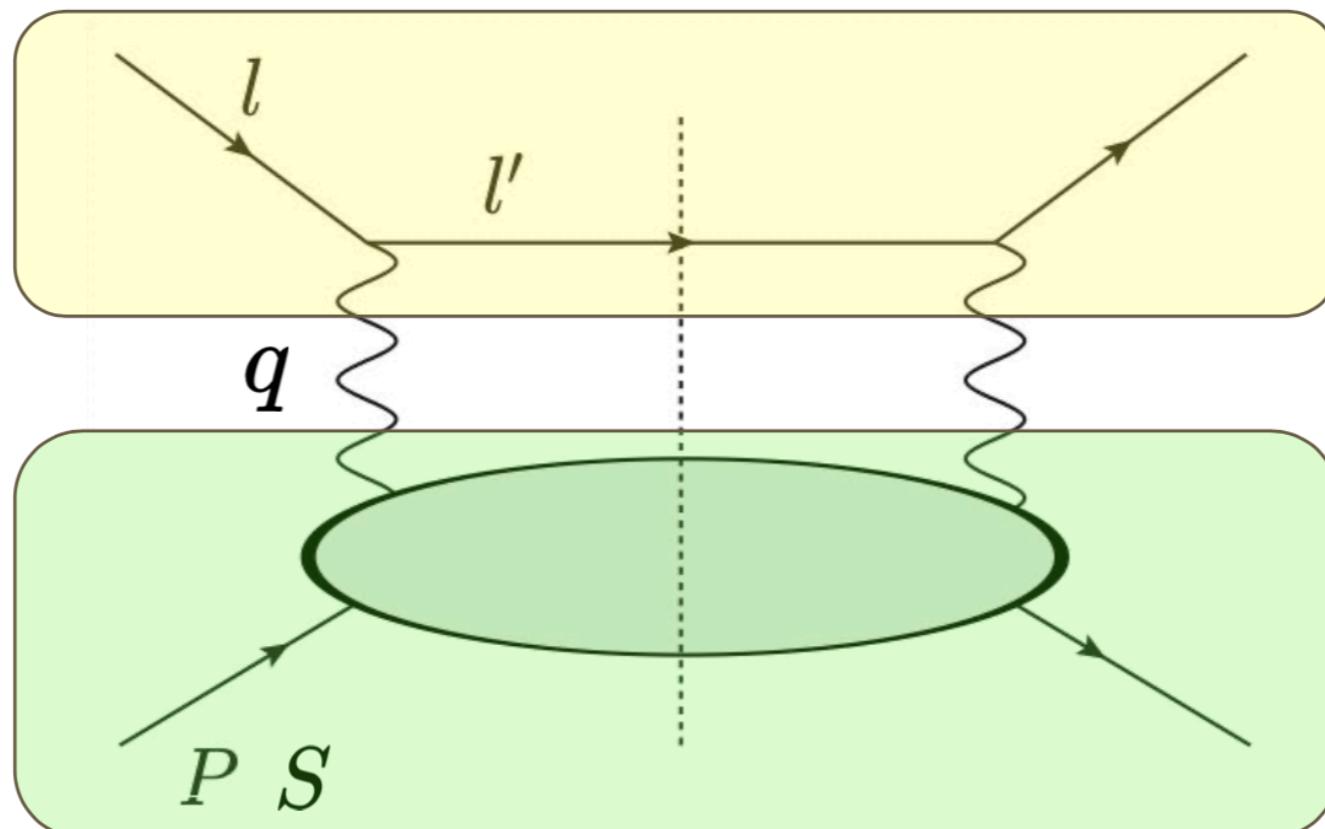


Which implications could the
presence of strong P-violation cause
to inclusive DIS?

DIS Cross Section

$$\frac{d^3\sigma}{dx_B dy d\phi_S} = \frac{\alpha^2 y}{2 Q^4} [L_{\mu\nu}(l, l', \lambda_e)] [2 M W^{\mu\nu}(q, P, S)]$$

Leptonic tensor - QED
(completely
calculable)



Hadronic tensor - QCD
(NOT completely
calculable)

J. Collins, "Foundation of Perturbative QCD"

DIS Cross Section

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$$\eta^\gamma = 1 \quad \eta^{\gamma Z} = \left(\frac{G_F M_Z^2}{2\sqrt{2}\pi\alpha} \right) \frac{Q^2}{Q^2 + M_Z^2} \quad \eta^Z = (\eta^{\gamma Z})^2$$

Hadronic Tensor (unpolarized)

$$2MW_{\mu\nu}(q, P) = \sum_X \int \frac{d^3 P_X}{2E_X} \delta^4(P + q - P_X) \langle P | J_\mu^\dagger(0) | P_X \rangle \langle P_X | J_\nu(0) | P \rangle$$

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Dominant contribution on the Light-Cone

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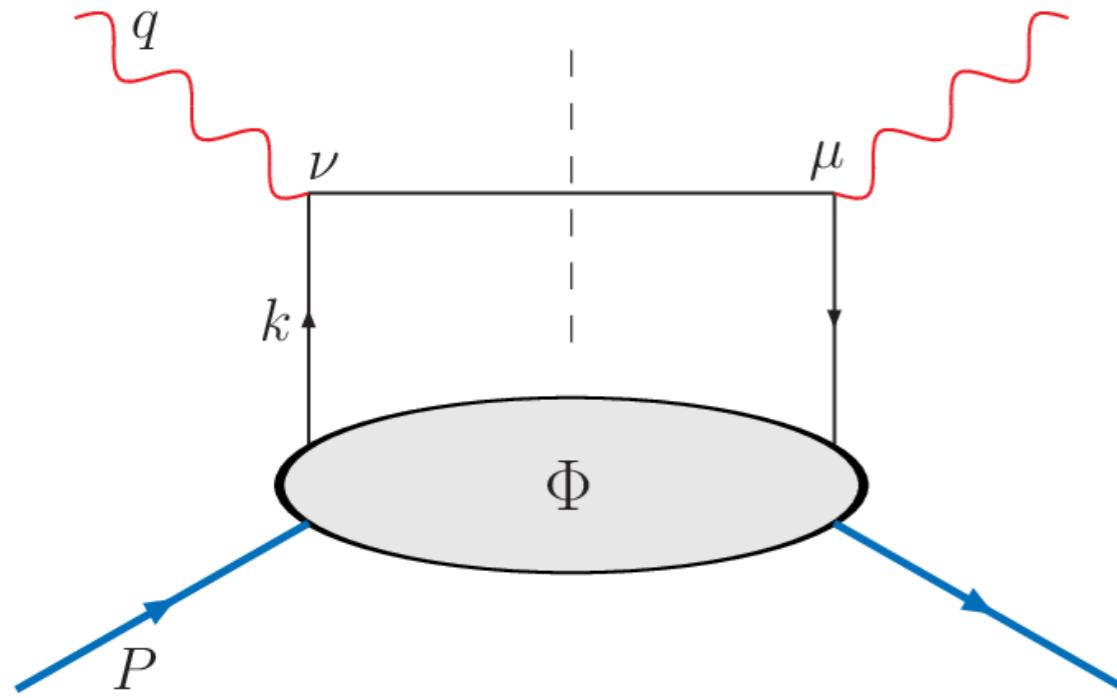
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Dominant contribution on the Light-Cone

$$2MW^{\mu\nu}(q, P, S) = \sum_q e_q^2 \frac{1}{2} \text{Tr} [\Phi(q, P, S) \Gamma^\mu \gamma^+ \Gamma^\nu]$$

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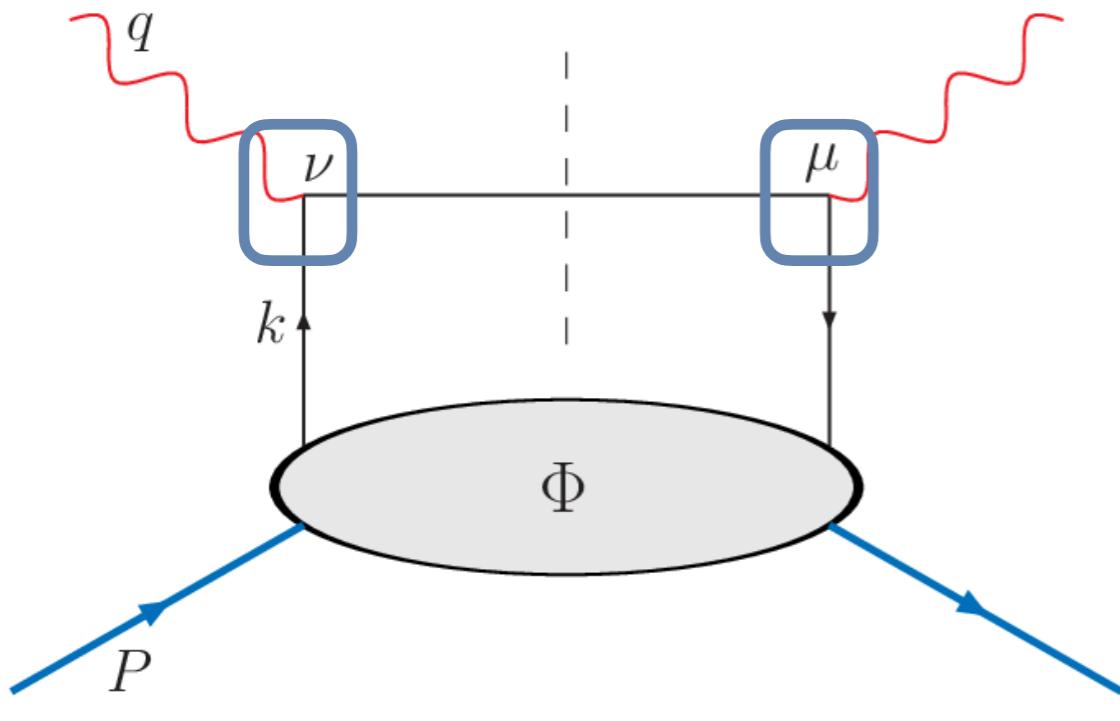
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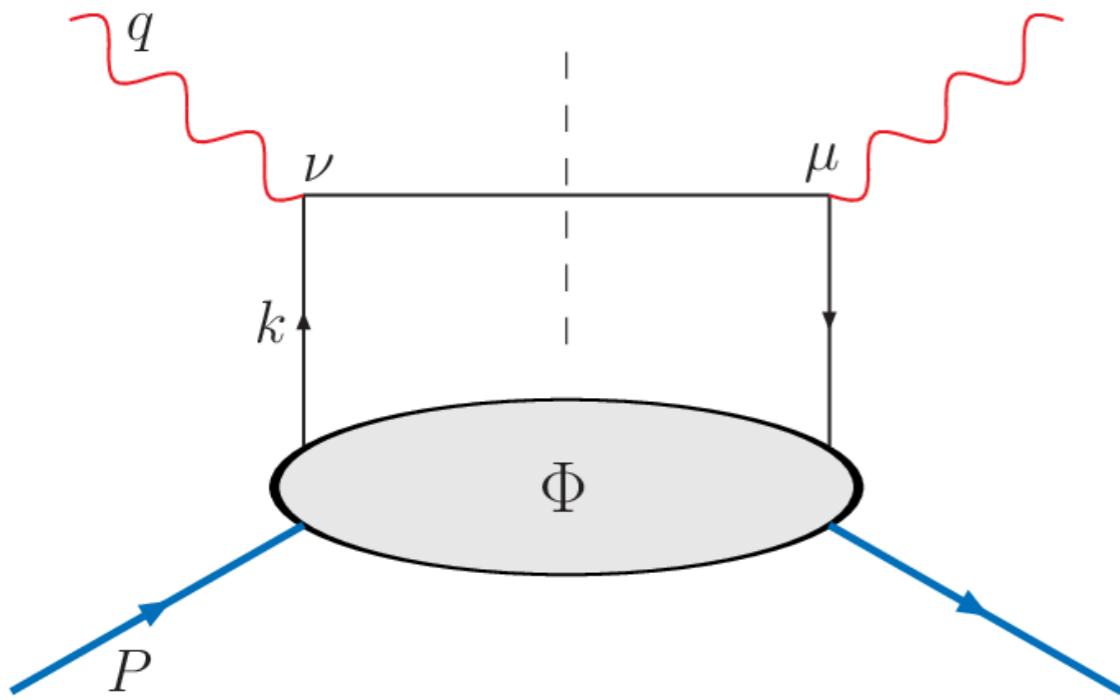


Vertices of the interactions

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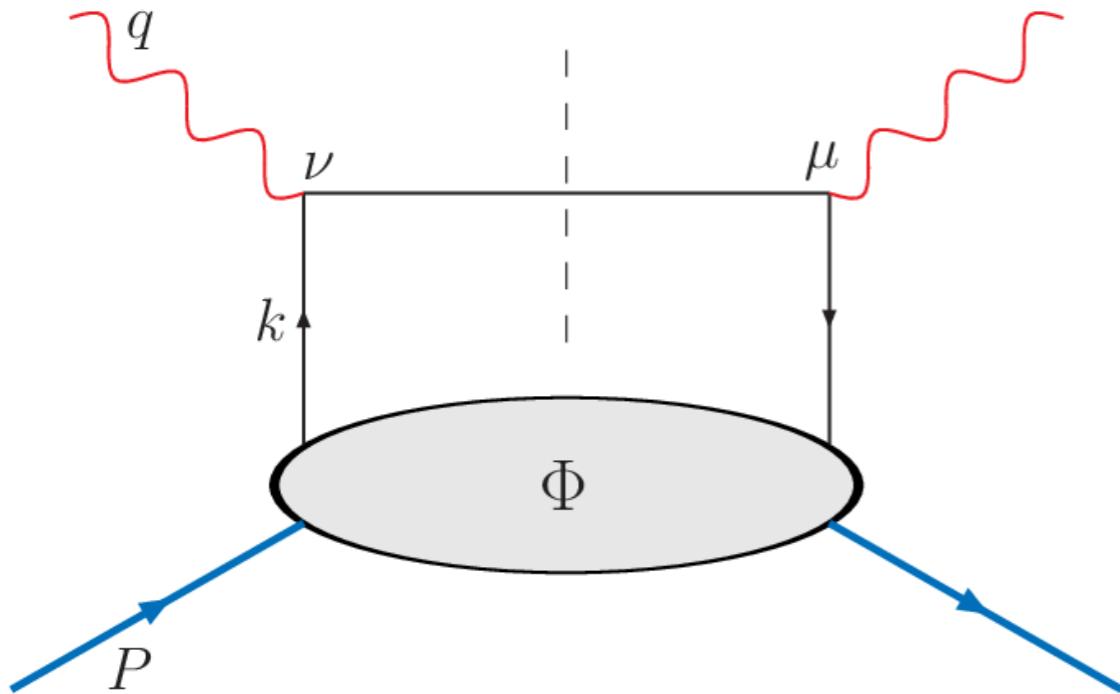


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Correlation distribution function

Hadronic Tensor (unpolarized)



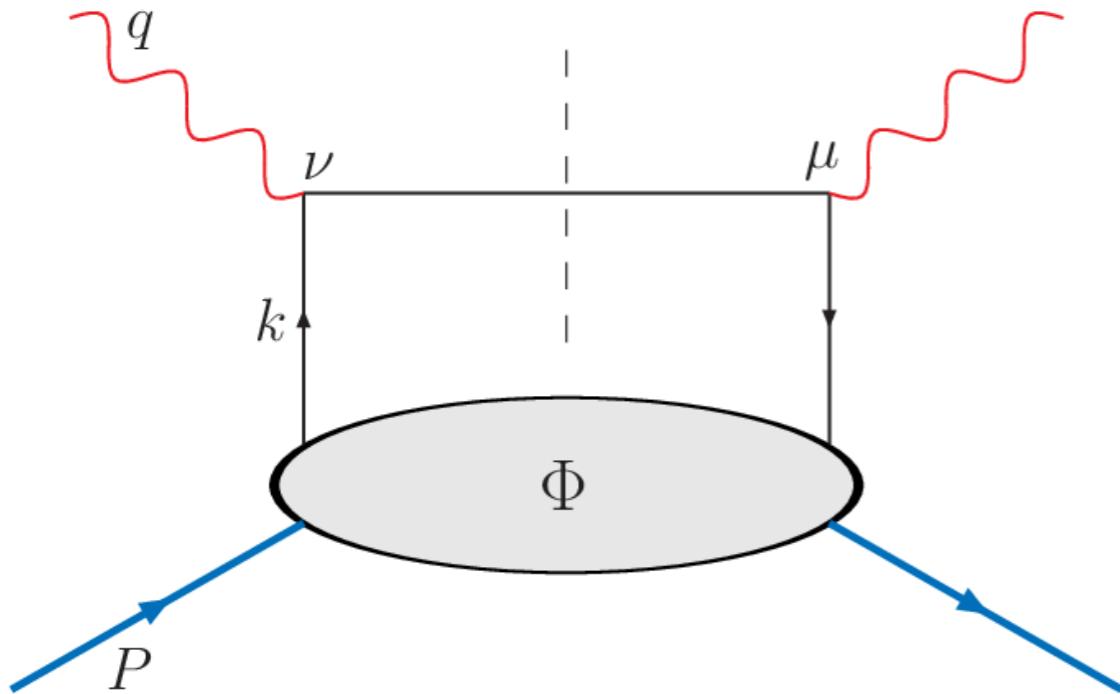
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Decomposition in partonic densities

Partonic Correlator (unpolarized)

Integrated correlator

$$\Phi_{ij}(x_B) = \int \frac{d\xi^-}{2\pi} e^{ik \cdot \xi} \langle P | \bar{\psi}_j(0) \psi_i(\xi) | P \rangle_{\xi^+ = \xi_T = 0}$$

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Leading twist contributions

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$$\Phi(x) = \Phi_{\text{PE}}(x) + \Phi_{\text{PV}}(x)$$

5 — DIS in collinear framework

Quark Polarization

Nucleon Pol.

	U	L	T
U	$f_1(x)$		
L		$g_1(x)$	
T			$h_1(x)$

5 — DIS in collinear framework

PDFs occurring in DIS processes

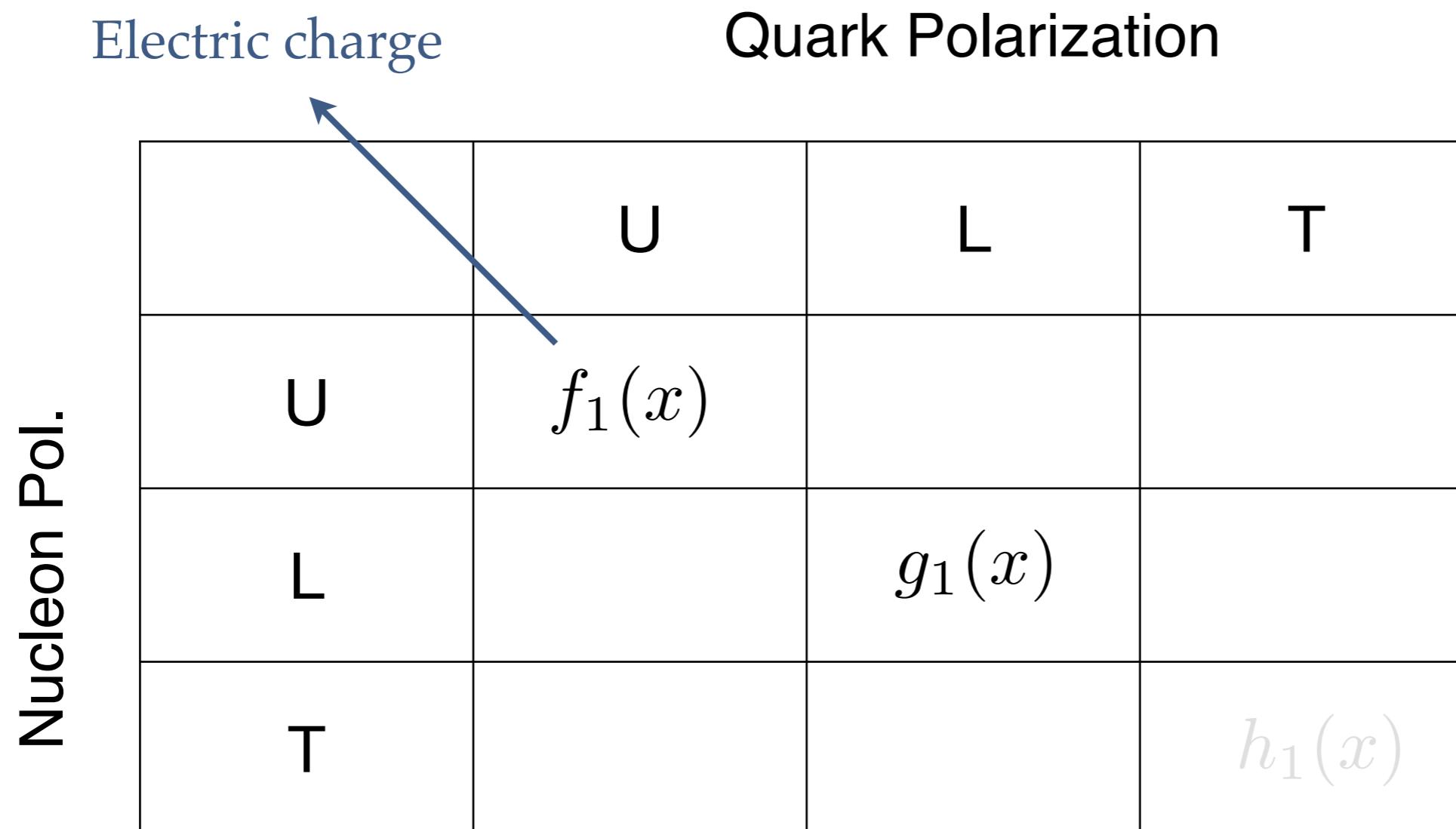
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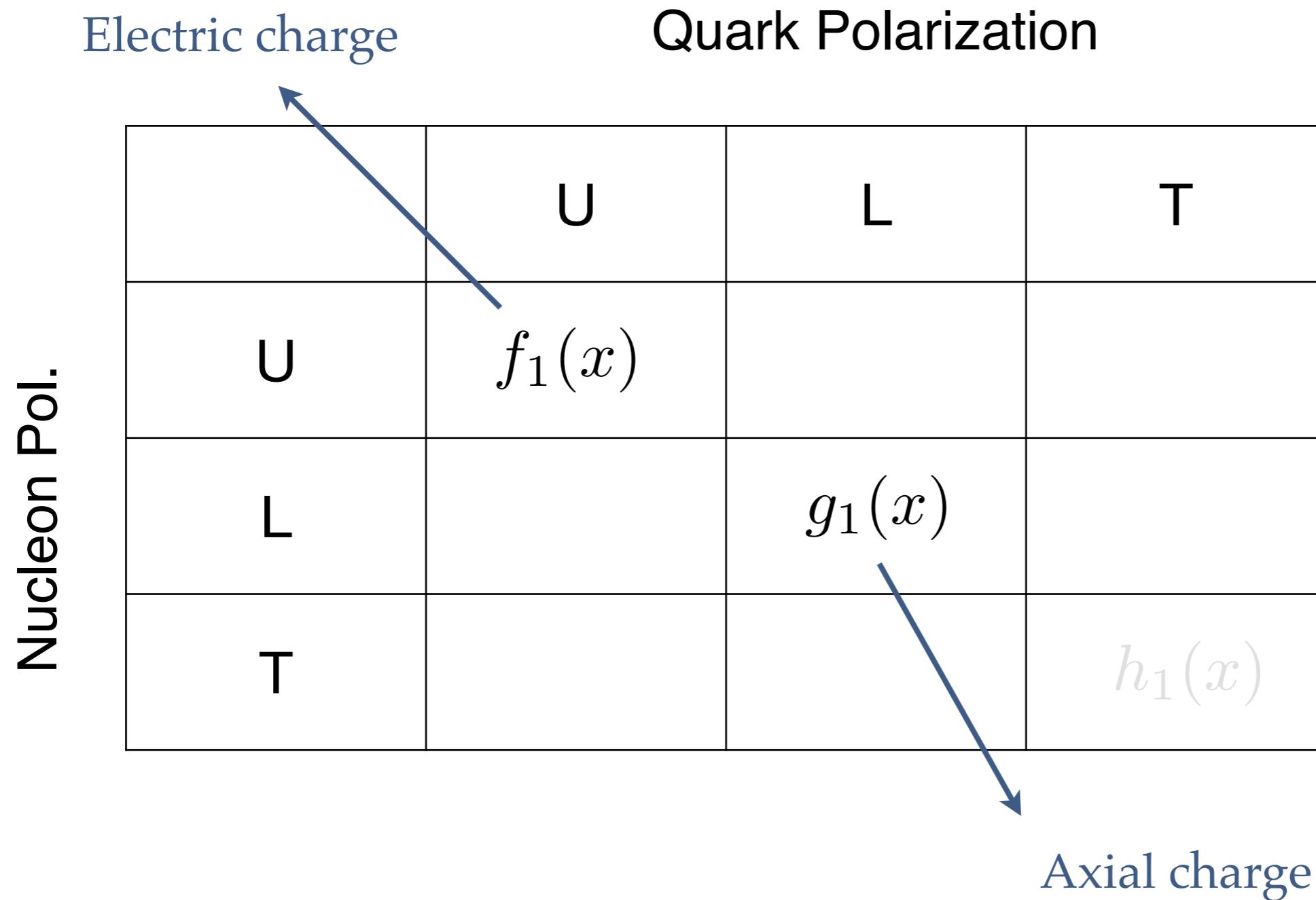
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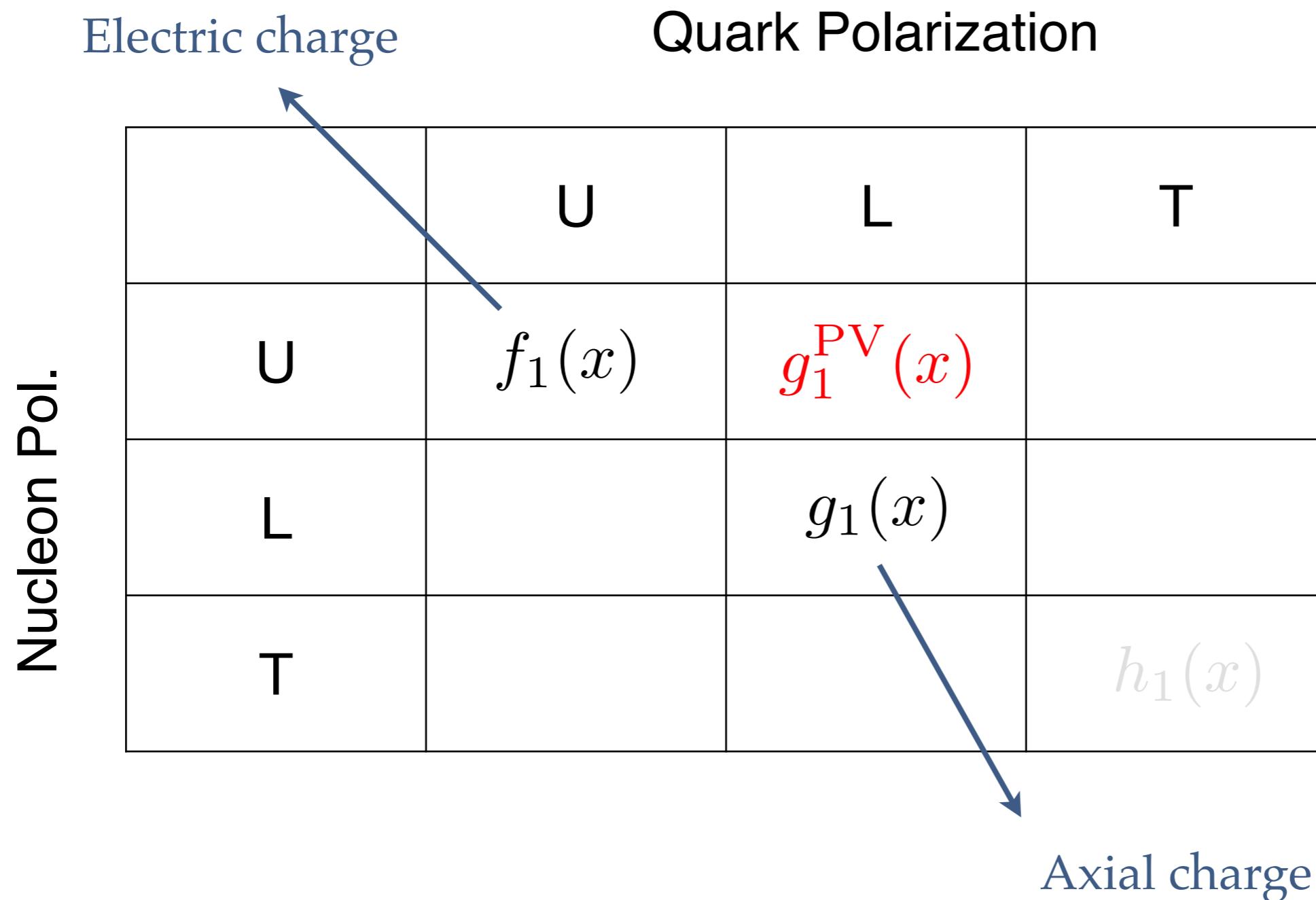
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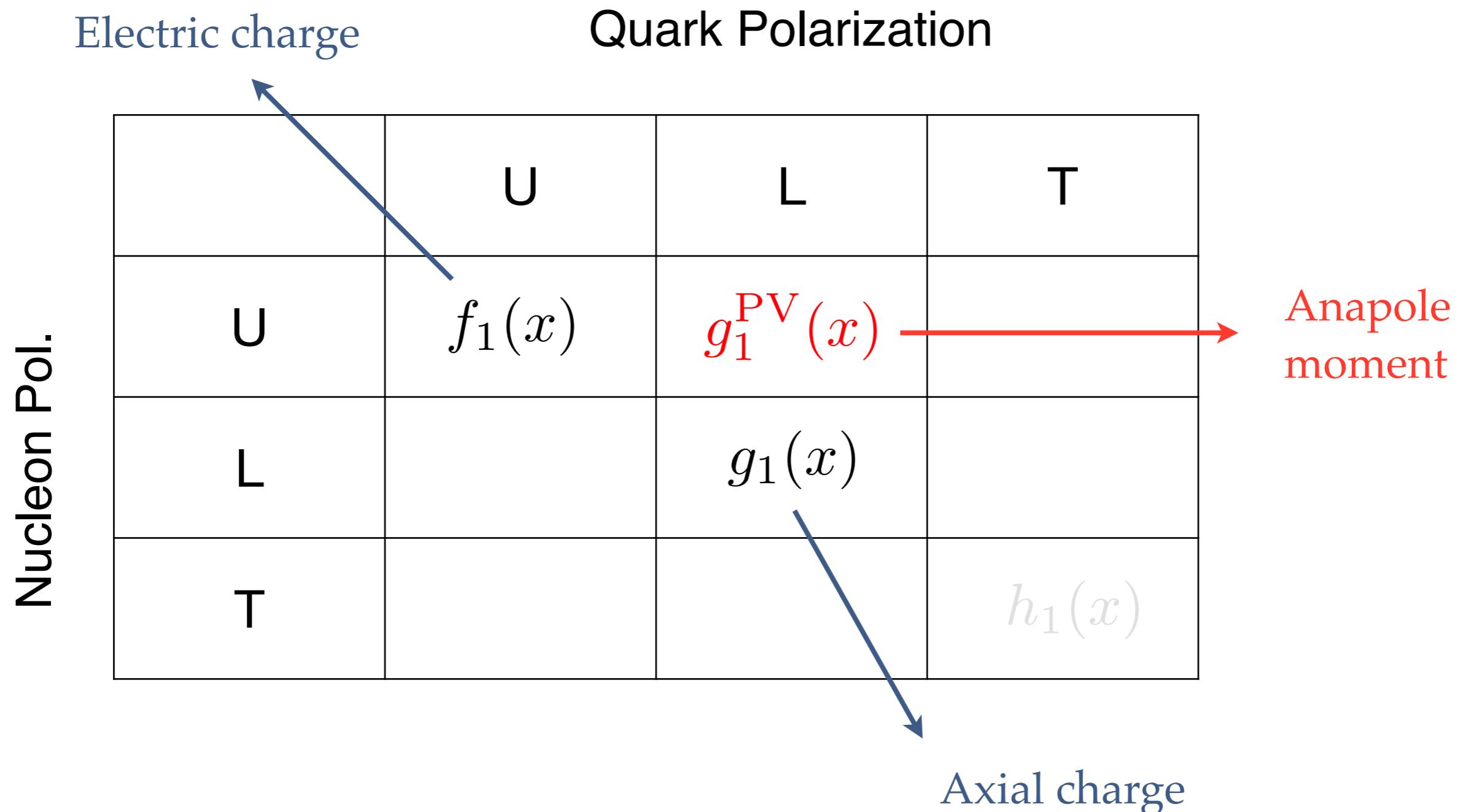
5 – DIS in collinear framework

PDFs occurring in DIS processes **with P violation**



5 – DIS in collinear framework

PDFs occurring in DIS processes **with P violation**



Neutral-Current DIS

$$\frac{d\sigma^\pm}{dxdy} = \frac{2\pi\alpha^2}{xyQ^2} \left[\left(Y_+ + \gamma^2 y^2/2 \right) (F_{2UU} + \lambda F_{2LU}^\pm) - y^2 (F_{L,UU} + \lambda F_{L,LU}^\pm) - \frac{Y_-}{\sqrt{1+\gamma^2}} (xF_{3UU}^\pm + \lambda xF_{3LU}) \right]$$

$$\frac{d\sigma^\pm}{dxdy} = \frac{2\pi\alpha^2}{xyQ^2} [Y_+ F_2^\pm - y^2 F_L^\pm \mp Y_- x F_3^\pm]$$

Particle Data Group, Tanabashi, et al., PRD 98 (2018)

Focus: structure function $xF_3(x, Q^2)$

$$xF_{3LU}(x, Q^2) = xF_3^{(\gamma)} - g_V^e \eta_{\gamma Z} xF_3^{(\gamma Z)} + (g_V^{e2} + g_A^{e2}) \eta_Z xF_3^{(Z)}$$

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$$xF_3^{(\gamma)}(x, Q^2) = 0$$

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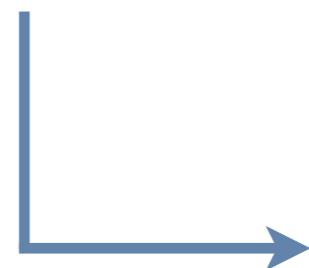
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Additional contributions
due to the new PV parton
distribution

$$x\Delta F_3^{(\gamma)}(x, Q^2) = - \sum_q e_q^2 x g_1^{\text{PV}(q+\bar{q})}$$

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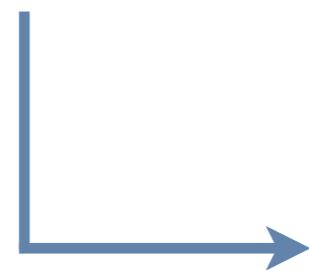
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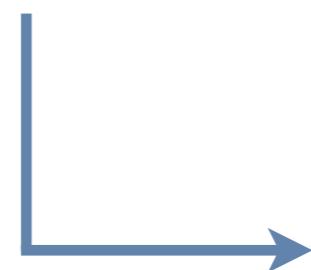
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**MAIN INNOVATION
OF PV-HYPOTESIS**



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$$x\Delta F_3^{(\gamma Z)}(x, Q^2) = - \sum_q 2e_q g_V^q x g_1^{\text{PV}(q+\bar{q})}$$

$$x\Delta F_3^{(Z)}(x, Q^2) = - \sum_q (g_V^{q2} + g_A^{q2}) x g_1^{\text{PV}(q+\bar{q})}$$

Neutral-Current DIS

$$\frac{d\sigma^\pm}{dxdy} = \frac{2\pi\alpha^2}{xyQ^2} \left[\left(Y_+ + \gamma^2 y^2/2 \right) (F_{2UU} + \lambda F_{2LU}^\pm) - y^2 (F_{L,UU} + \lambda F_{L,LU}^\pm) - \frac{Y_-}{\sqrt{1+\gamma^2}} (xF_{3UU}^\pm + \lambda xF_{3LU}) \right]$$

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Standard DIS structure functions

Neutral-Current DIS

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Standard DIS structure functions

$$\begin{aligned} F_{2UU}(x, Q^2) &= F_2^{(\gamma)} - g_V^e \eta_{\gamma Z} F_2^{(\gamma Z)} + (g_V^e)^2 + (g_A^e)^2 \eta_Z F_2^{(Z)}, \\ F_{2LU}^\pm(x, Q^2) &= \mp g_A^e \eta_{\gamma Z} F_2^{(\gamma Z)} \pm 2g_V^e g_A^e \eta_Z F_2^{(Z)}, \\ xF_{3UU}^\pm(x, Q^2) &= \mp g_A^e \eta_{\gamma Z} xF_3^{(\gamma Z)} \pm 2g_V^e g_A^e \eta_Z xF_3^{(Z)}, \\ xF_{3LU}(x, Q^2) &= xF_3^{(\gamma)} - g_V^e \eta_{\gamma Z} xF_3^{(\gamma Z)} + (g_V^e)^2 + (g_A^e)^2 \eta_Z xF_3^{(Z)}, \end{aligned}$$

Phenomenology

Experimental information

PVDIS Asymmetry

$$A_{\text{PV}} \equiv \frac{d\sigma(\lambda = 1) - d\sigma(\lambda = -1)}{d\sigma(\lambda = 1) + d\sigma(\lambda = -1)}$$

PVDIS Collaboration, *Nature* 506 (2014)
D. Wang et al., Phys.Rev.C 91 (2015)

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Contribution of g_1^{PV} in each of
the structure functions due to
 γZ and Z channels

Available experimental data sets

HERA dataset
(Run I + II combined)

H1 Collaboration, Eur. Phys. J. C 78 (2018)

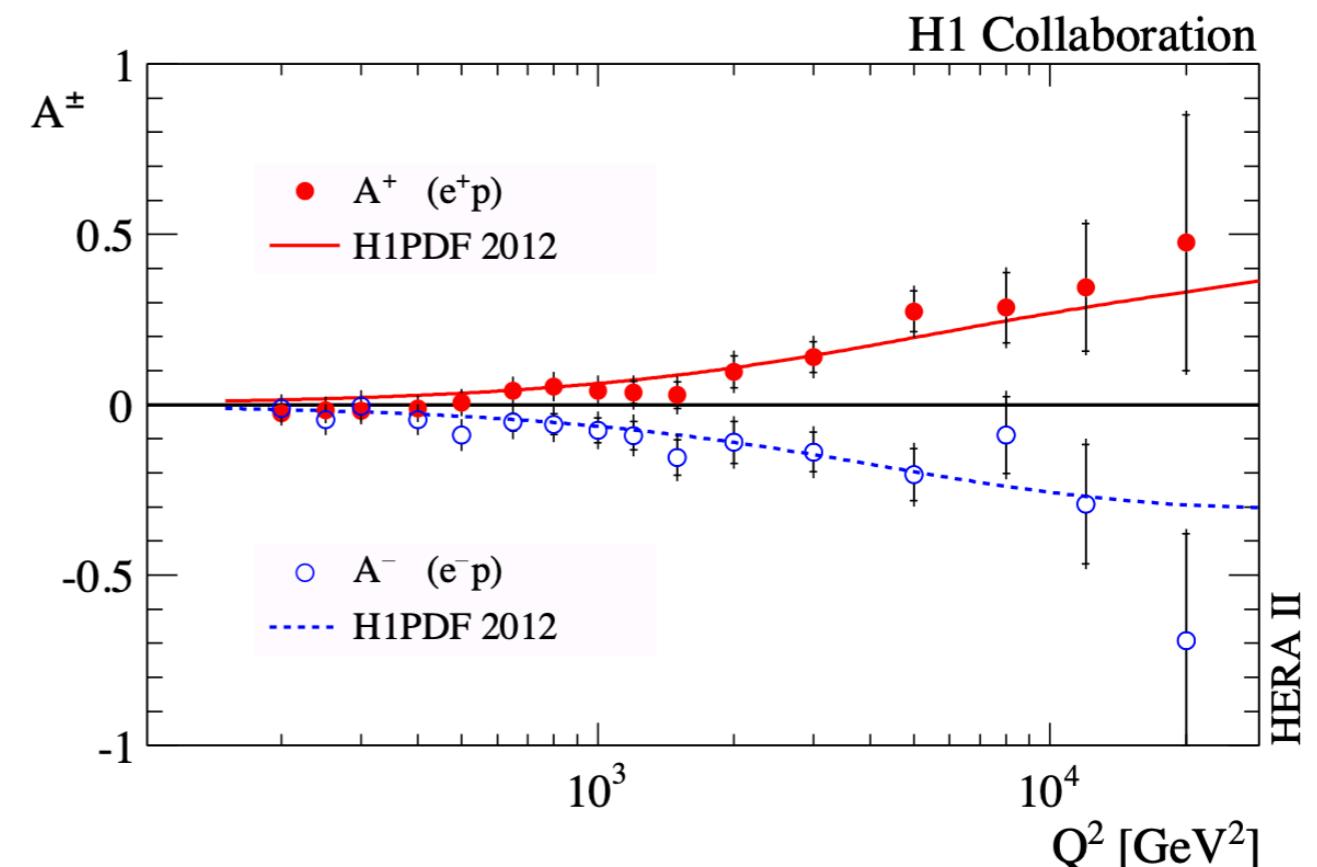
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e⁺ asymmetry: 136 data

e⁻ asymmetry: 138 data



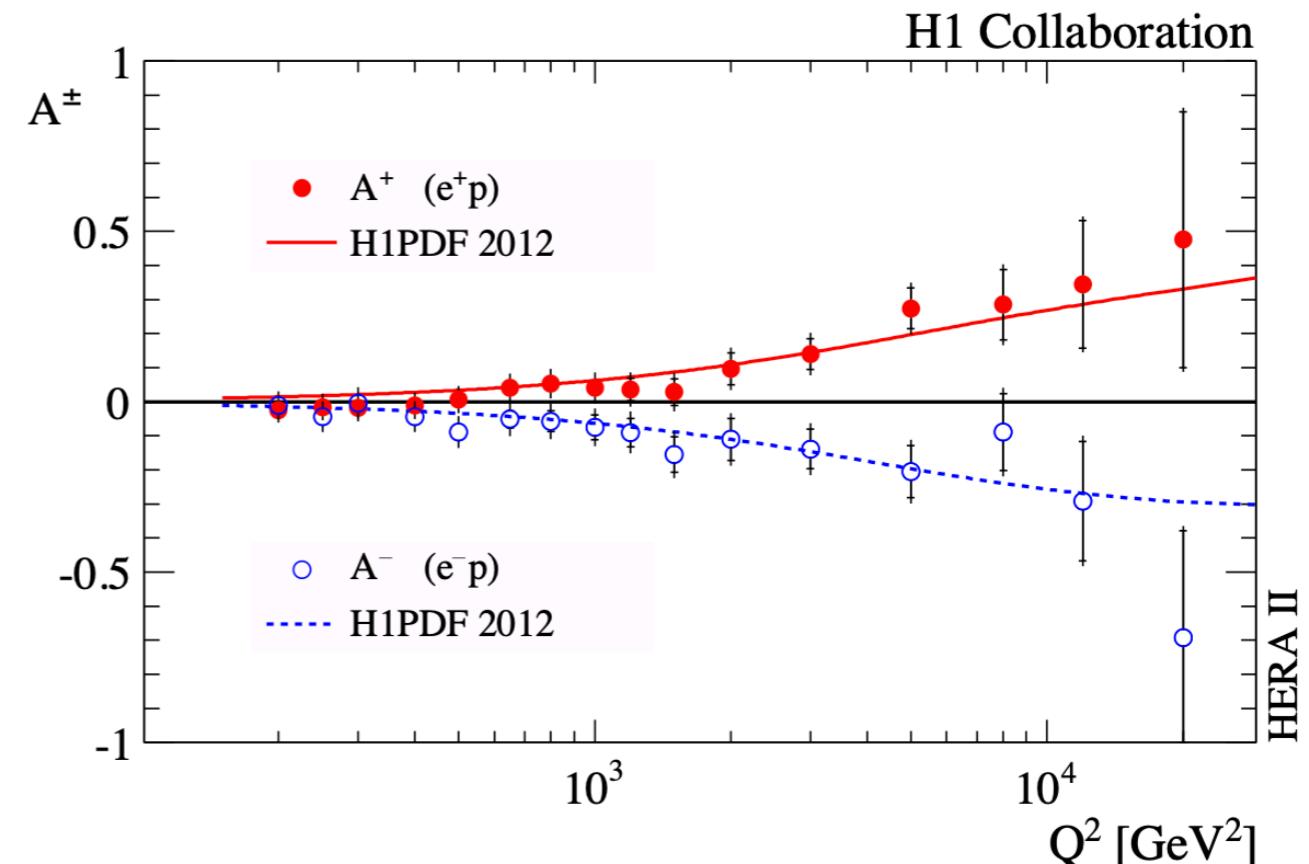
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JLab6 PVDIS dataset

PVDIS Collaboration, *Nature* 506 (2014)

D. Wang et al., *Phys.Rev.C* 91 (2015)

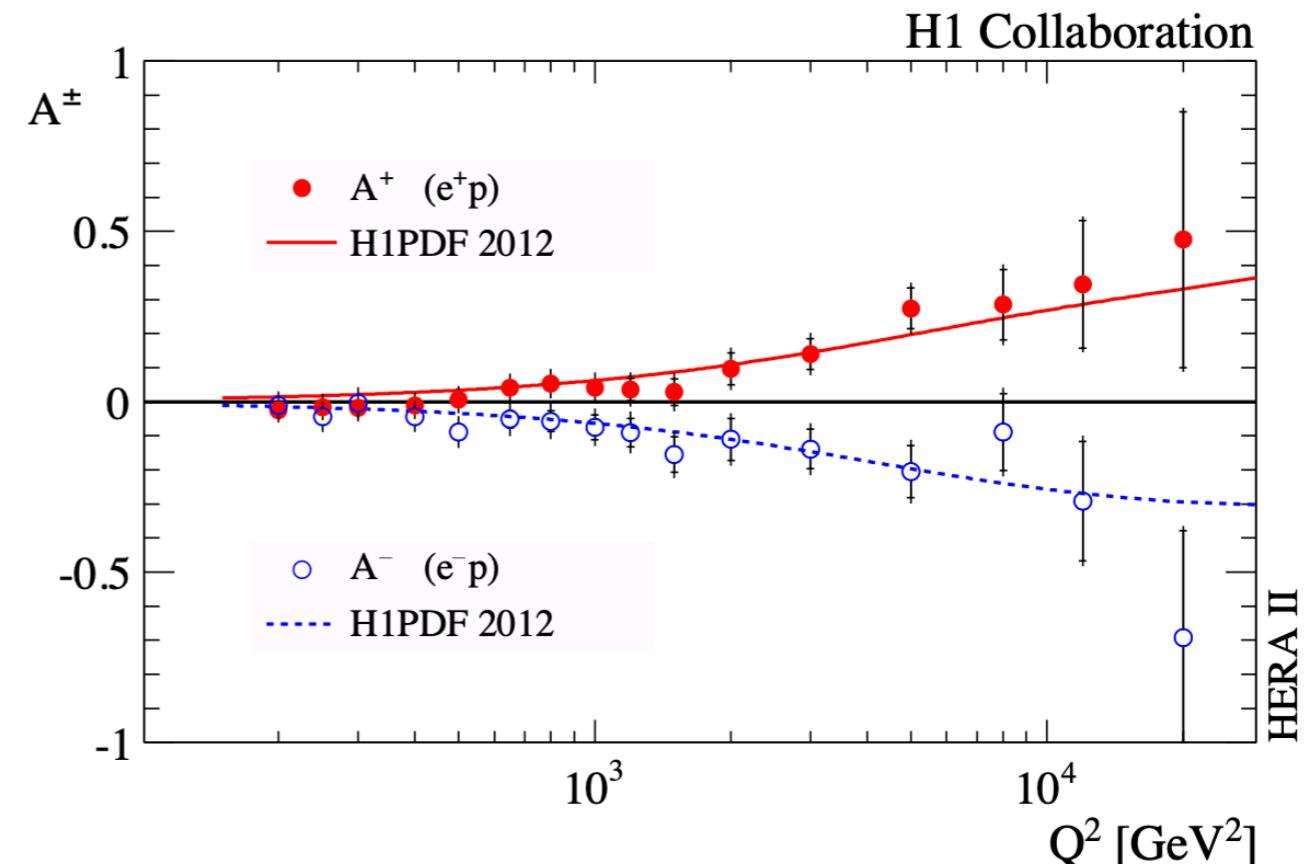
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D. Wang et al., Phys.Rev.C 91 (2015)

e⁻ asymmetry: 2 data

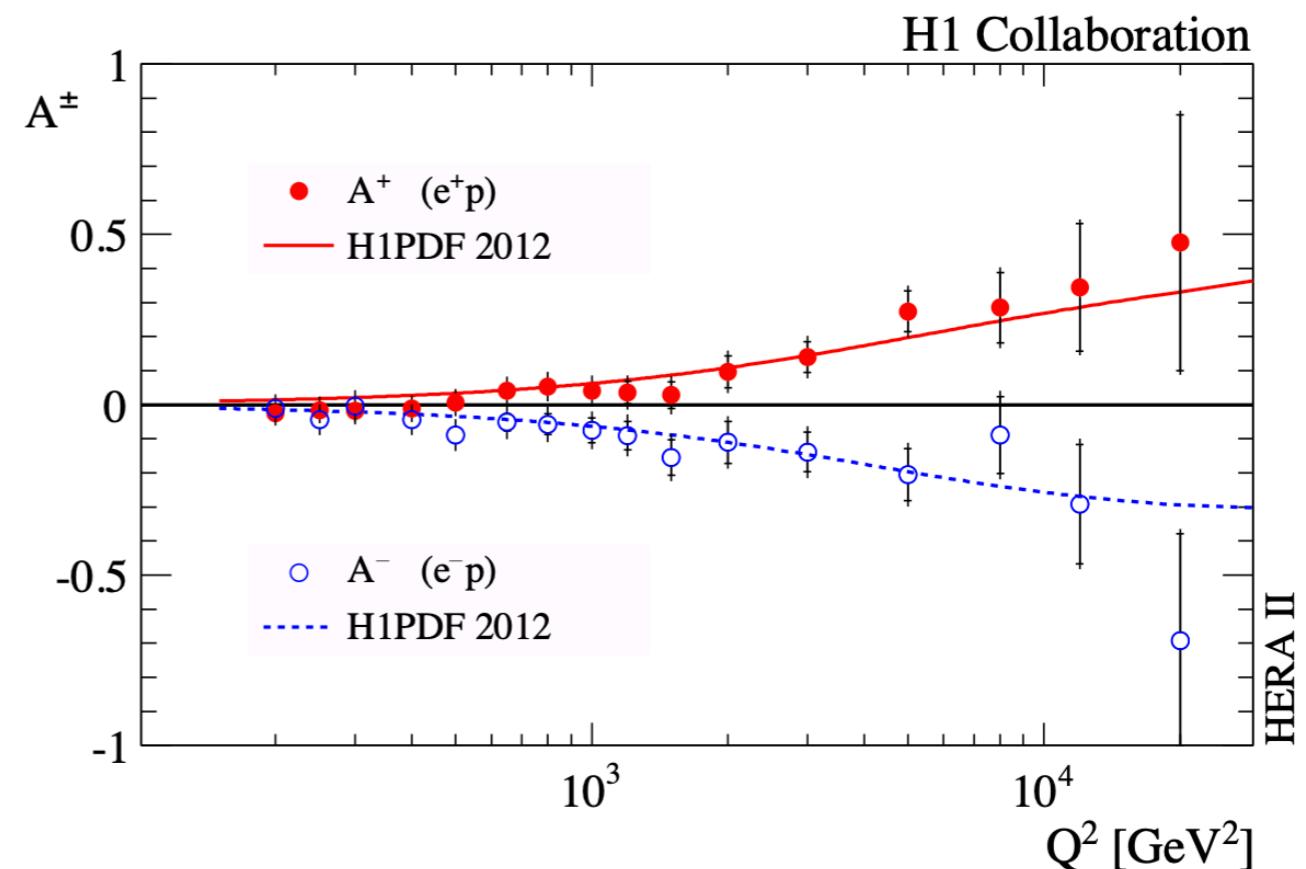
Available experimental data sets

HERA dataset (Run I + II combined)

H1 Collaboration, Eur. Phys. J. C 78 (2018)

e^+ **asymmetry: 136 data**

e^- **asymmetry: 138 data**



JLab6 PVDIS dataset

PVDIS Collaboration, *Nature* 506 (2014)
D. Wang et al., Phys.Rev.C 91 (2015)

e^- **asymmetry: 2 data**

SLAC-E122 dataset

C.Y. Prescott et al., Phys. Lett. B (1979)

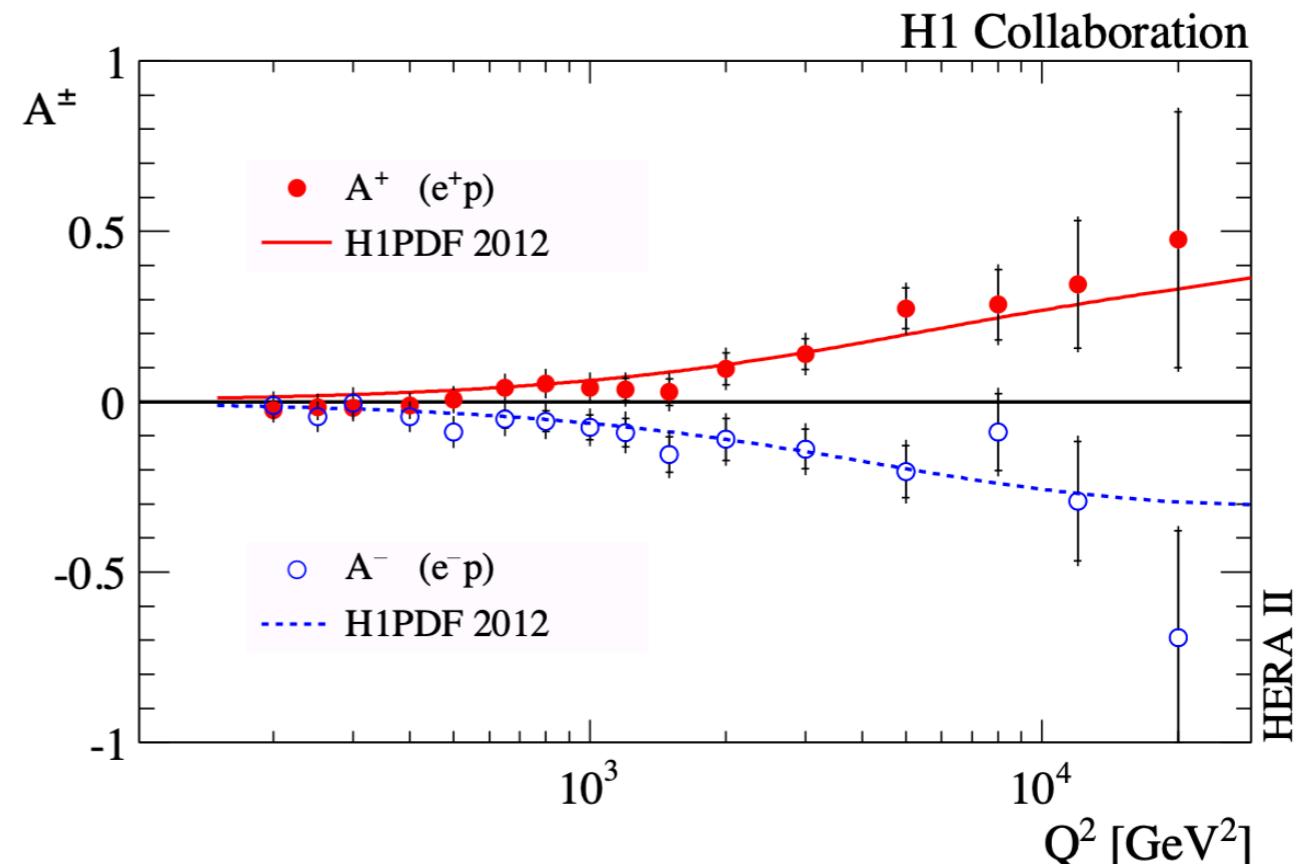
Available experimental data sets

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JLab6 PVDIS dataset

PVDIS Collaboration, *Nature* 506 (2014)
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C.Y. Prescott et al., Phys. Lett. B (1979)

e⁻ asymmetry: 2 data

e⁻ asymmetry: 11 data

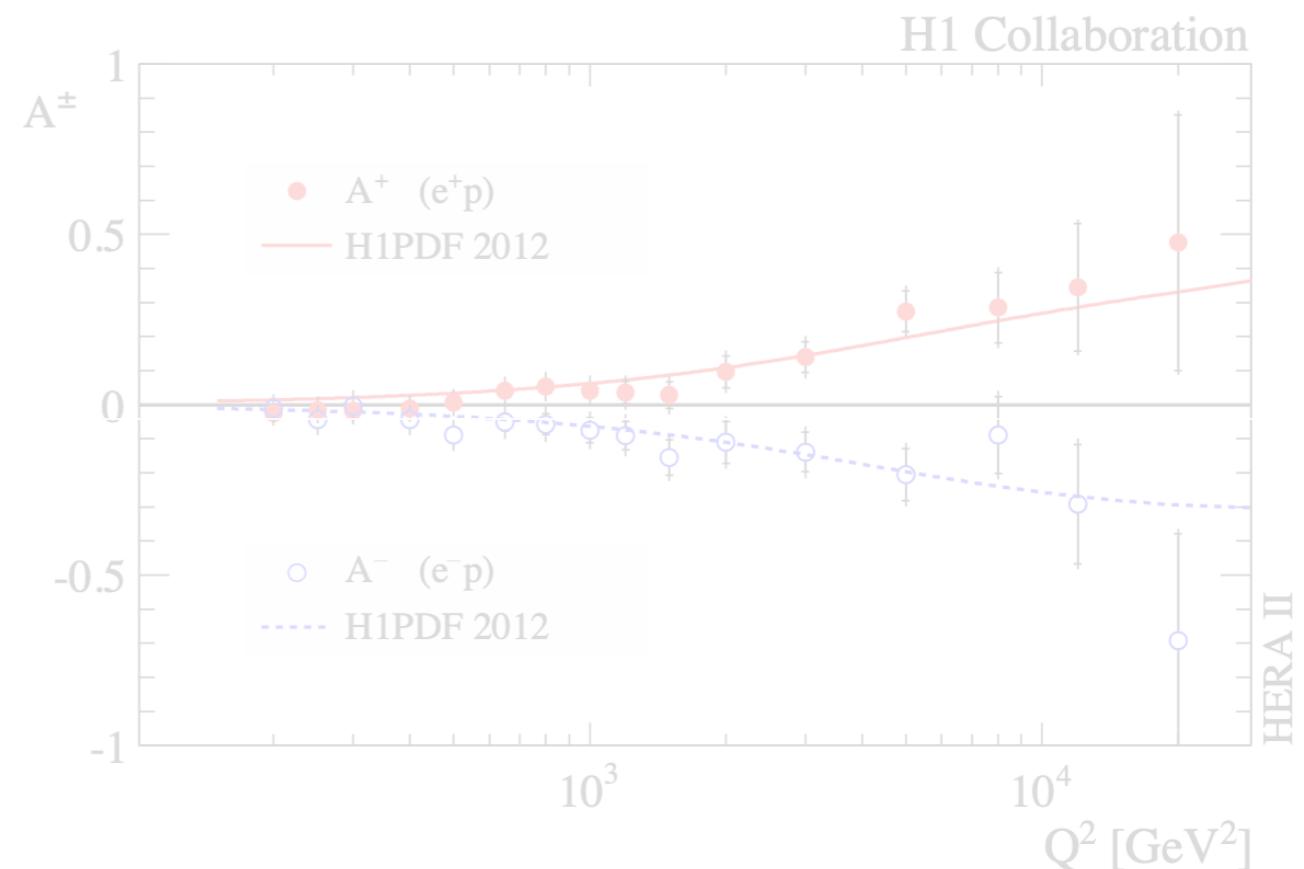
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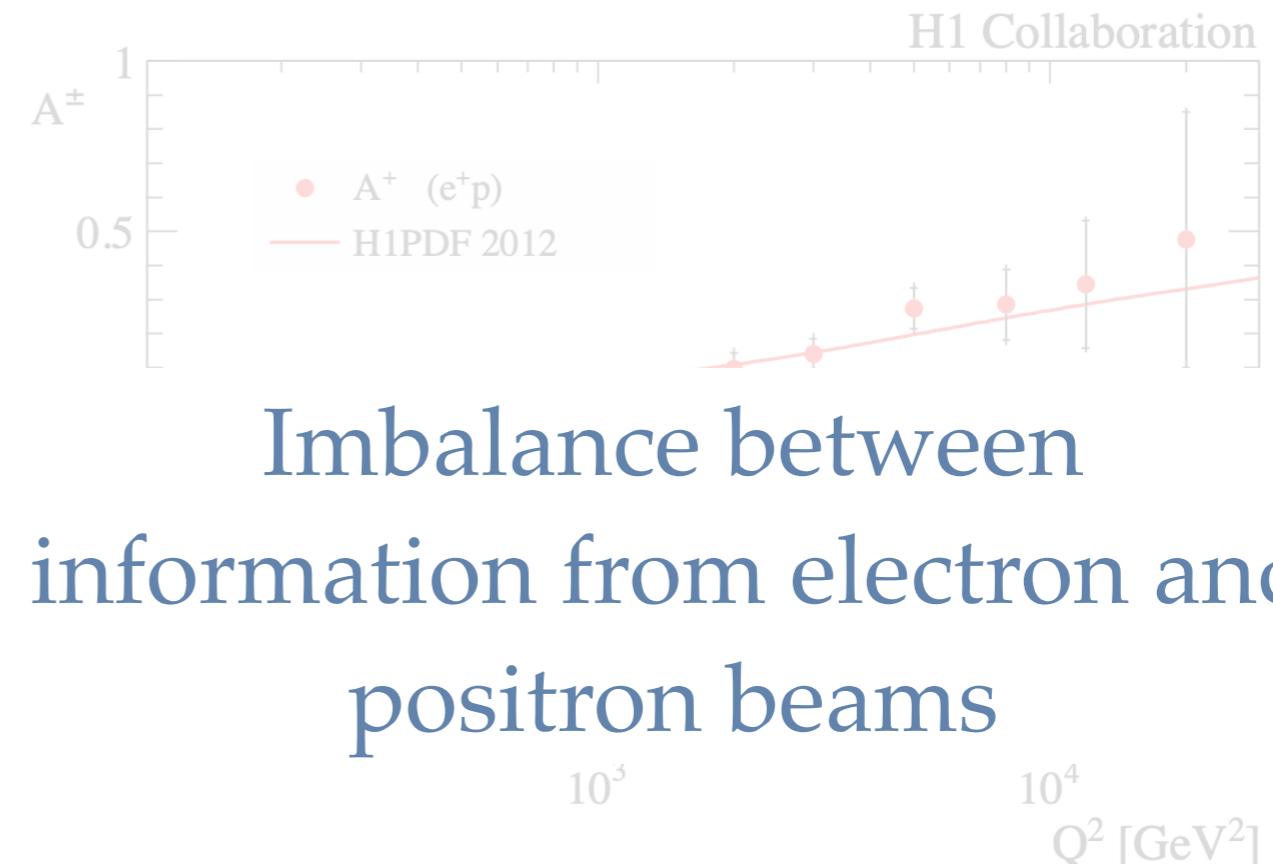
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PVDIS Collaboration, *Nature* 506 (2014)
D. Wang et al., *Phys.Rev.C* 91 (2015)

SLAC-E122 dataset

C.Y. Prescott et al., *Phys. Lett. B* (1979)



Imbalance between
information from electron and
positron beams

e⁻ asymmetry: 2 data

e⁻ asymmetry: 11 data

Experimental data: energy range

HERA dataset

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$$Q^2 \in (200, 30000) \text{ GeV}^2$$

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$$Q^2 \gg M_N^2$$

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$$Q^2 \in (0.9, 1.9) \text{ GeV}^2$$

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$$C_{1u} = 2g_A^e g_V^u = 2 \left(-\frac{1}{2} \right) \left(\frac{1}{2} - \frac{4}{3} \sin^2 \theta_W \right)$$

$$C_{2u} = 2g_V^e g_A^u = 2 \left(-\frac{1}{2} + 2 \sin^2 \theta_W \right) \left(\frac{1}{2} \right)$$

$$C_{1d} = 2g_A^e g_V^d = 2 \left(-\frac{1}{2} \right) \left(-\frac{1}{2} + \frac{2}{3} \sin^2 \theta_W \right)$$

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$$C_{1u}^{\text{SM}} = -0.1887 - 0.0011 \times \frac{2}{3} \ln(\langle Q^2 \rangle / 0.14 \text{ GeV}^2)$$

$$C_{1d}^{\text{SM}} = 0.3419 - 0.0011 \times \frac{-1}{3} \ln(\langle Q^2 \rangle / 0.14 \text{ GeV}^2)$$

$$C_{2u}^{\text{SM}} = -0.0351 - 0.0009 \ln(\langle Q^2 \rangle / 0.078 \text{ GeV}^2)$$

$$C_{2d}^{\text{SM}} = 0.0248 + 0.0007 \ln(\langle Q^2 \rangle / 0.021 \text{ GeV}^2)$$

Parameterization of $g_1^{PV}(x, Q^2)$

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PV parton density comes from the structure

$$\gamma^5 \gamma^\mu$$

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$$\gamma^5 \gamma^\mu \longrightarrow \textcolor{red}{\text{Same evolution as helicity PDF } g_1(x, Q^2)}$$

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$$\begin{array}{ccc} \gamma^5 \gamma^\mu & \xrightarrow{\hspace{2cm}} & \text{Same evolution as helicity PDF } g_1(x, Q^2) \\ & \xrightarrow{\hspace{2cm}} & \text{C-odd} \end{array}$$

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1 parameter to be fitted

Error propagation in the analysis

PDF set for

Error propagation in the analysis

PDF set for

$$f_1(x, Q^2)$$

NNPDF4.0

Ball et al. (NNPDF), EPJ C 82 (2022)

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100 MC replicas of unpolarized PDF

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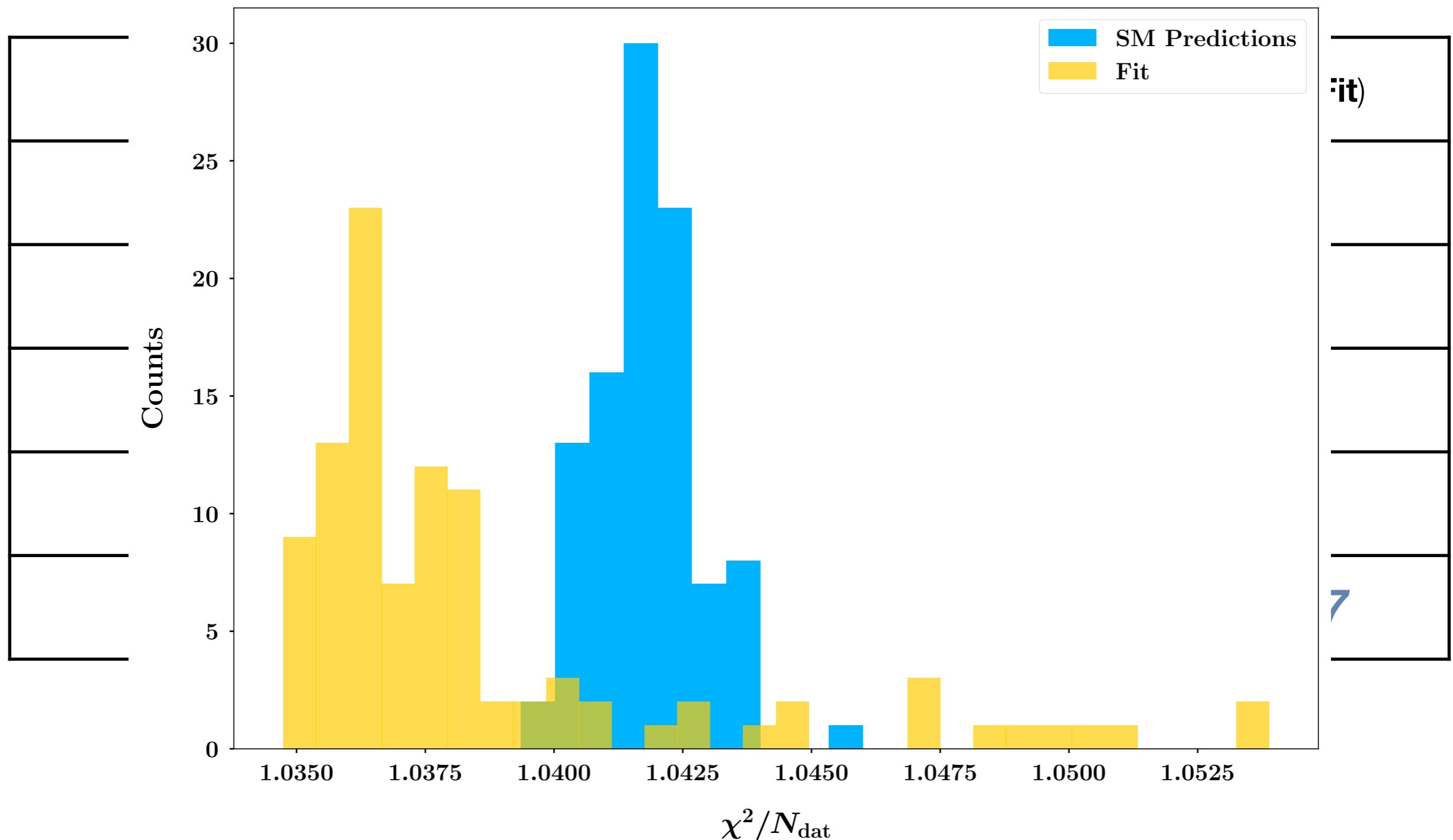
100 MC replicas experimental data

Statistical distribution of
100 values of parameter α

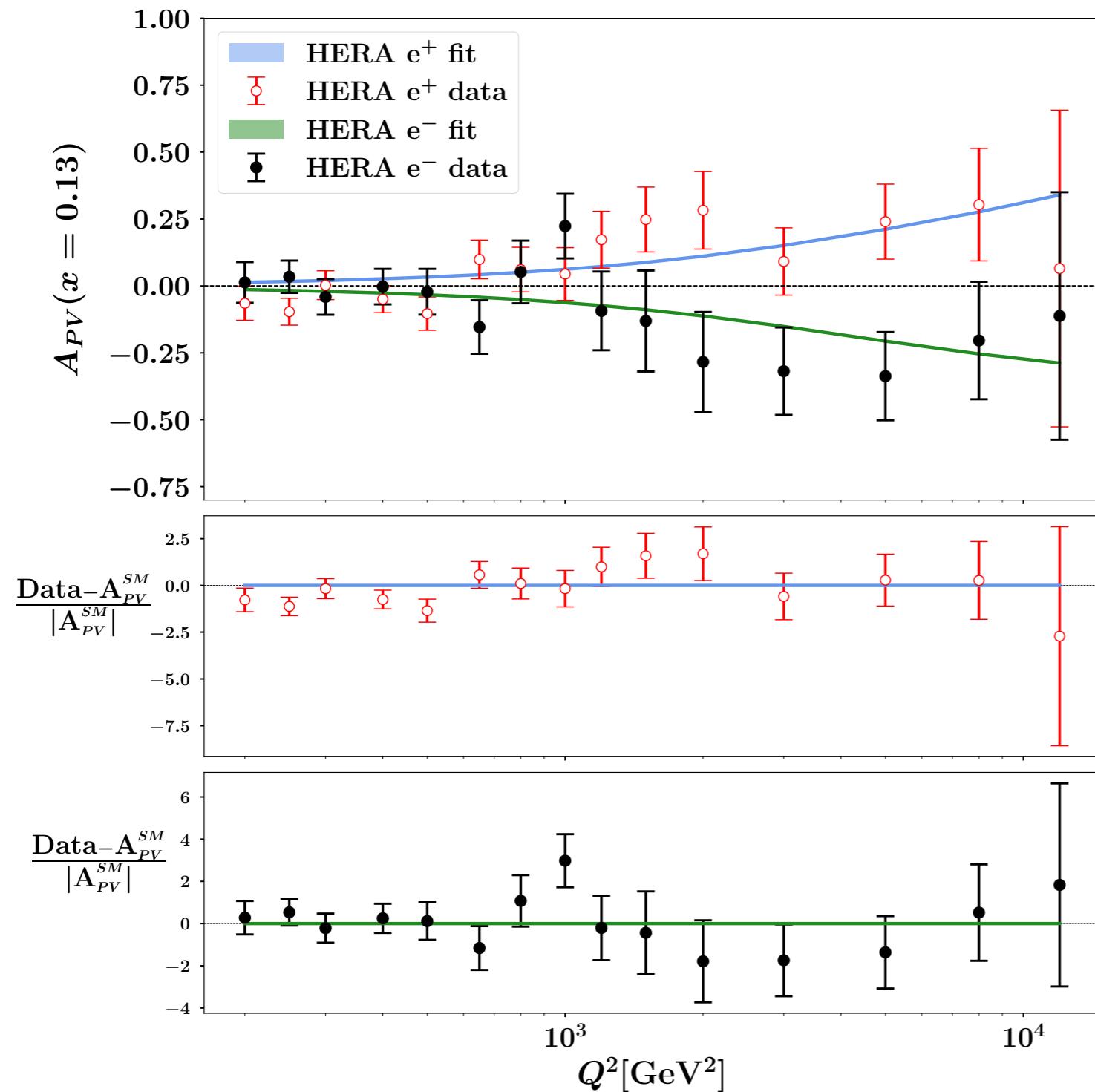
Results of the fit

	N of points	χ^2/N_{data} (SM)	χ^2/N_{data} (Fit)
HERA e^+	136	1.12	1.12
HERA e^-	138	0.98	0.98
JLab6	2	0.67	0.42
SLAC-E122	11	0.97	0.94
TOTAL	287	1.042	1.037

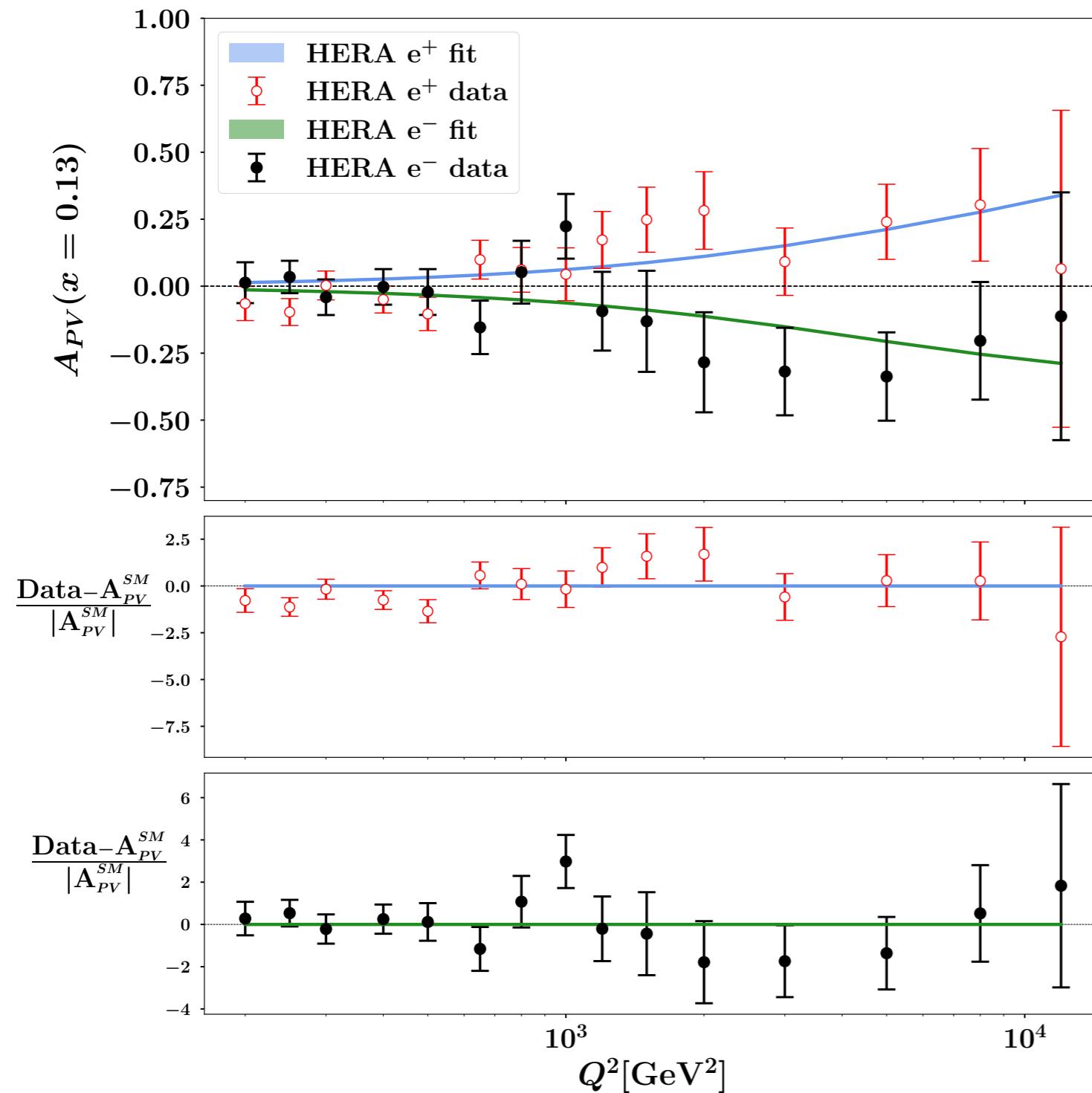
Results of the fit



Results of the fit: data vs theory

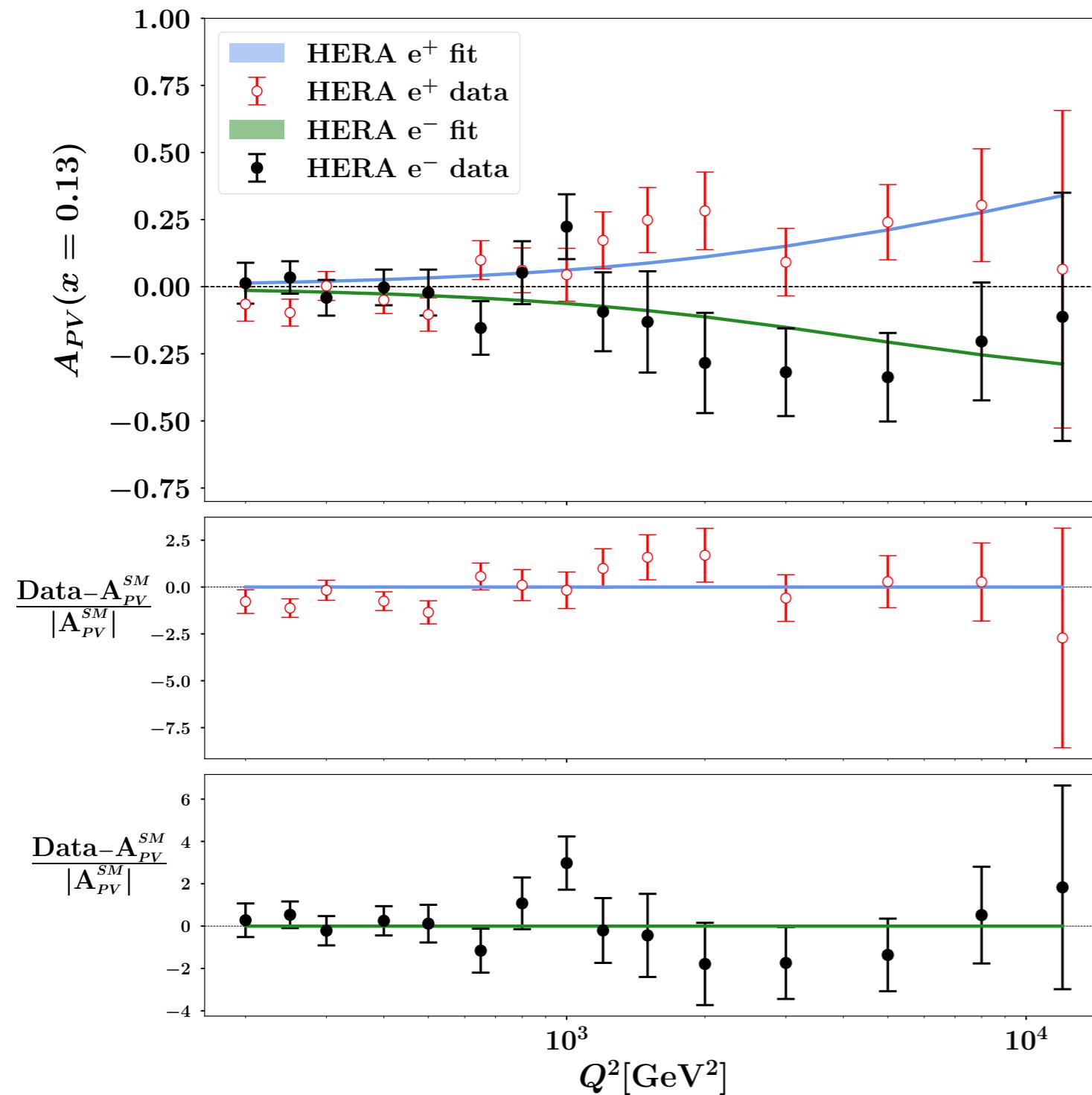


Results of the fit: data vs theory



Very small uncertainties in the predictions because the fit is dominated by data with smaller errors

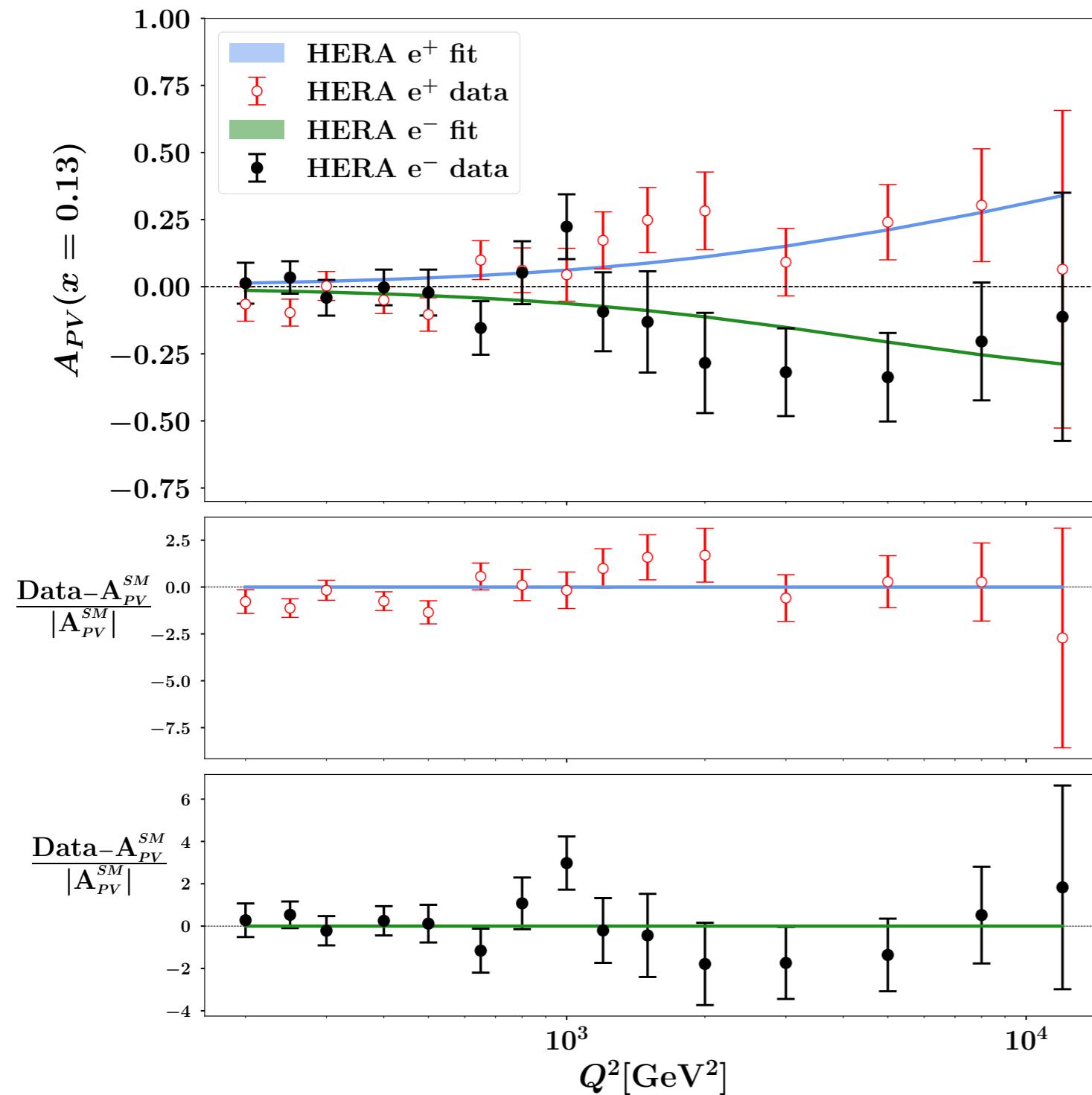
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There's room for a better description for positron asymmetry at low- Q

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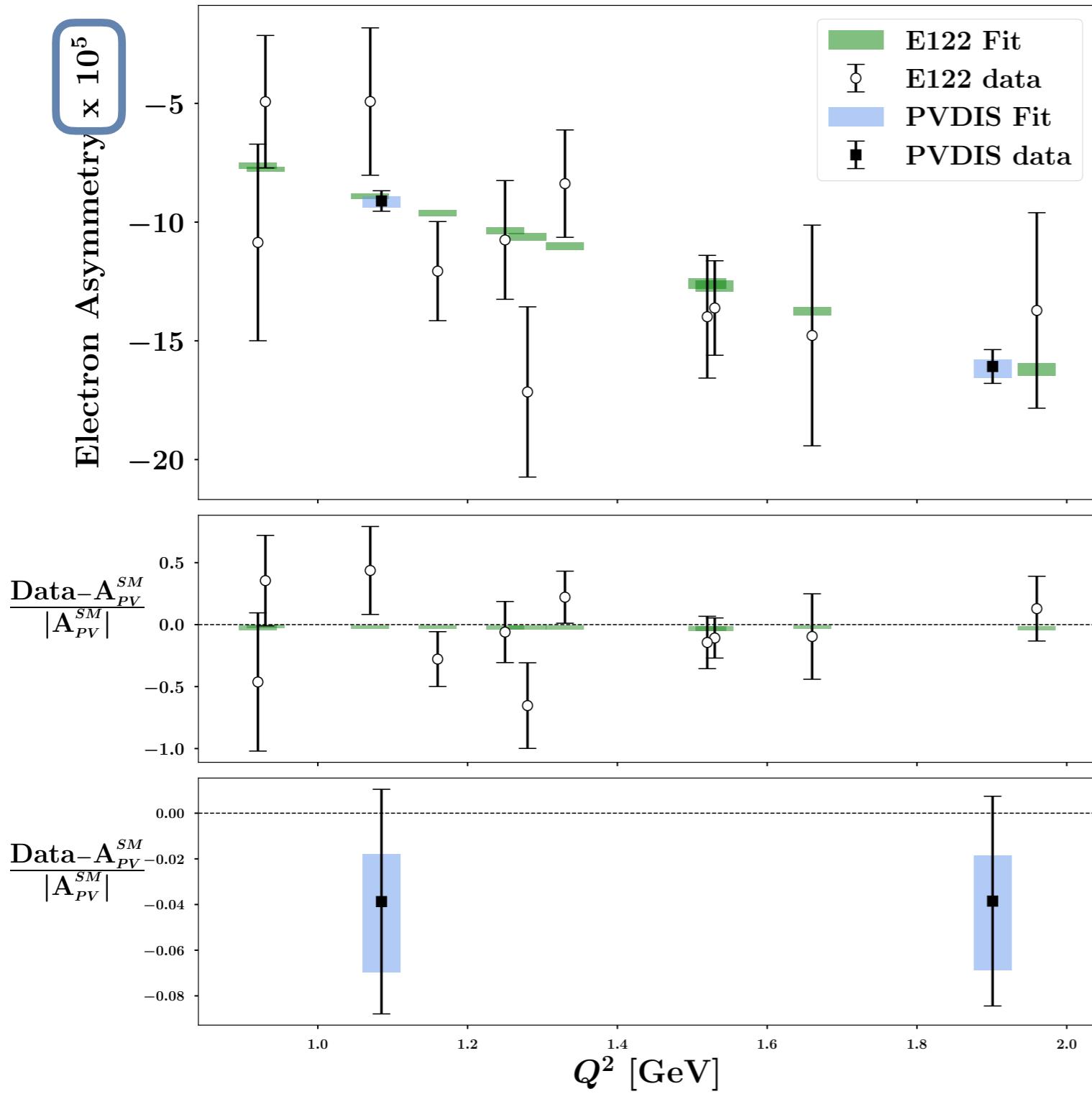


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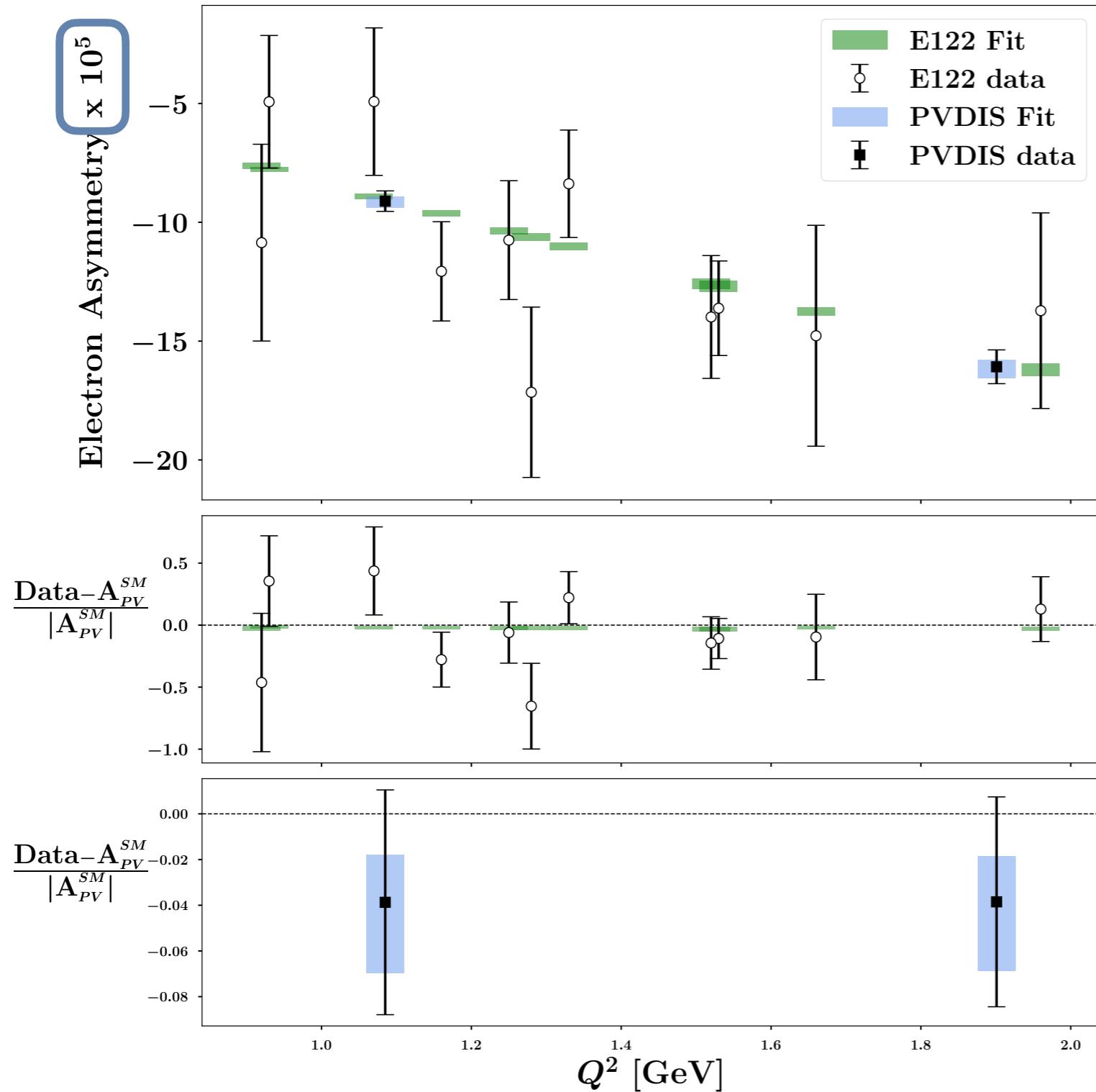
There's room for a better description for positron asymmetry at low- Q

Agreement for electron asymmetry, but too large errors at low- Q

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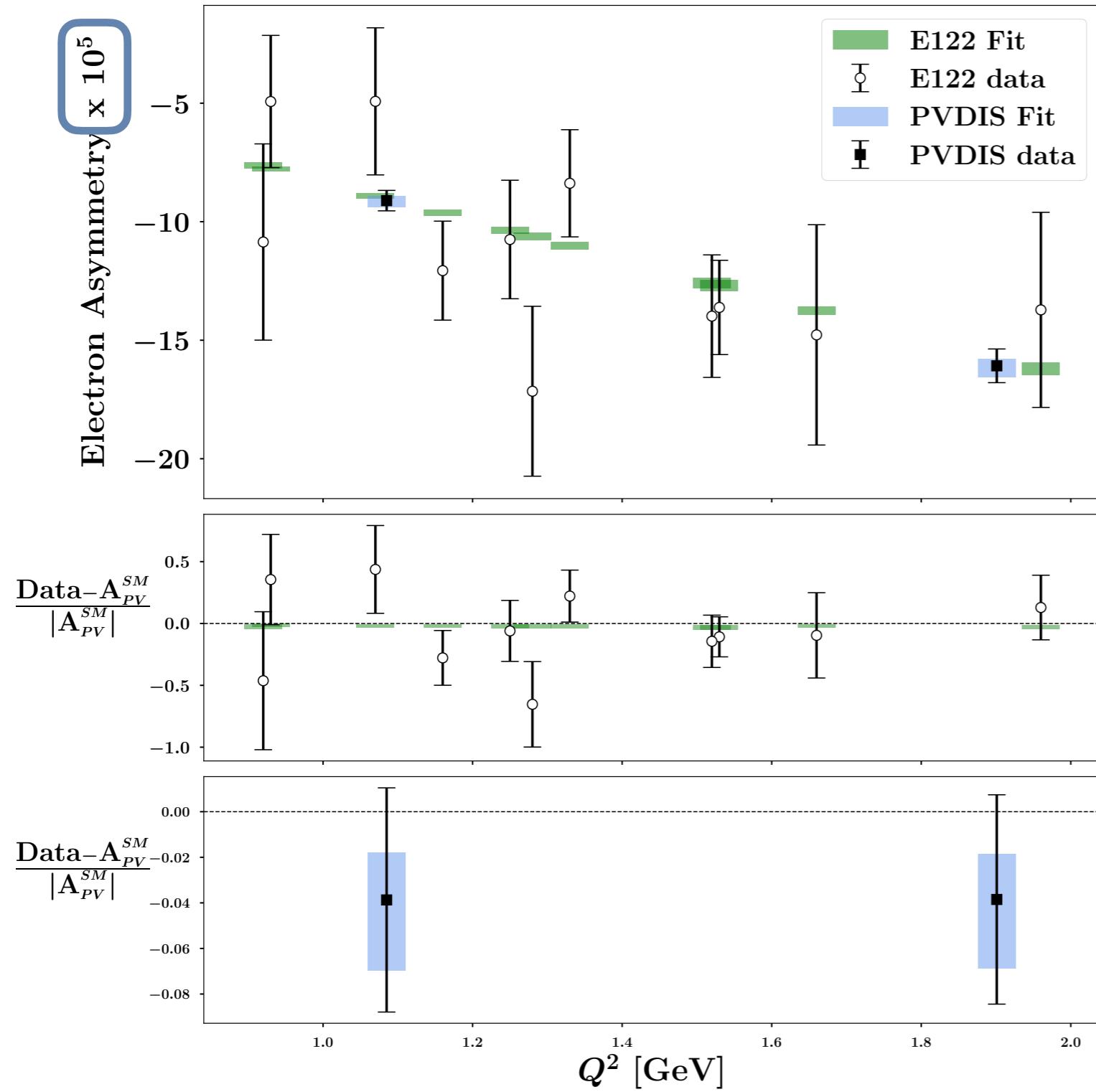


Results of the fit: data vs theory



Sizeable improvement of the fit
w.r.t. SM predictions

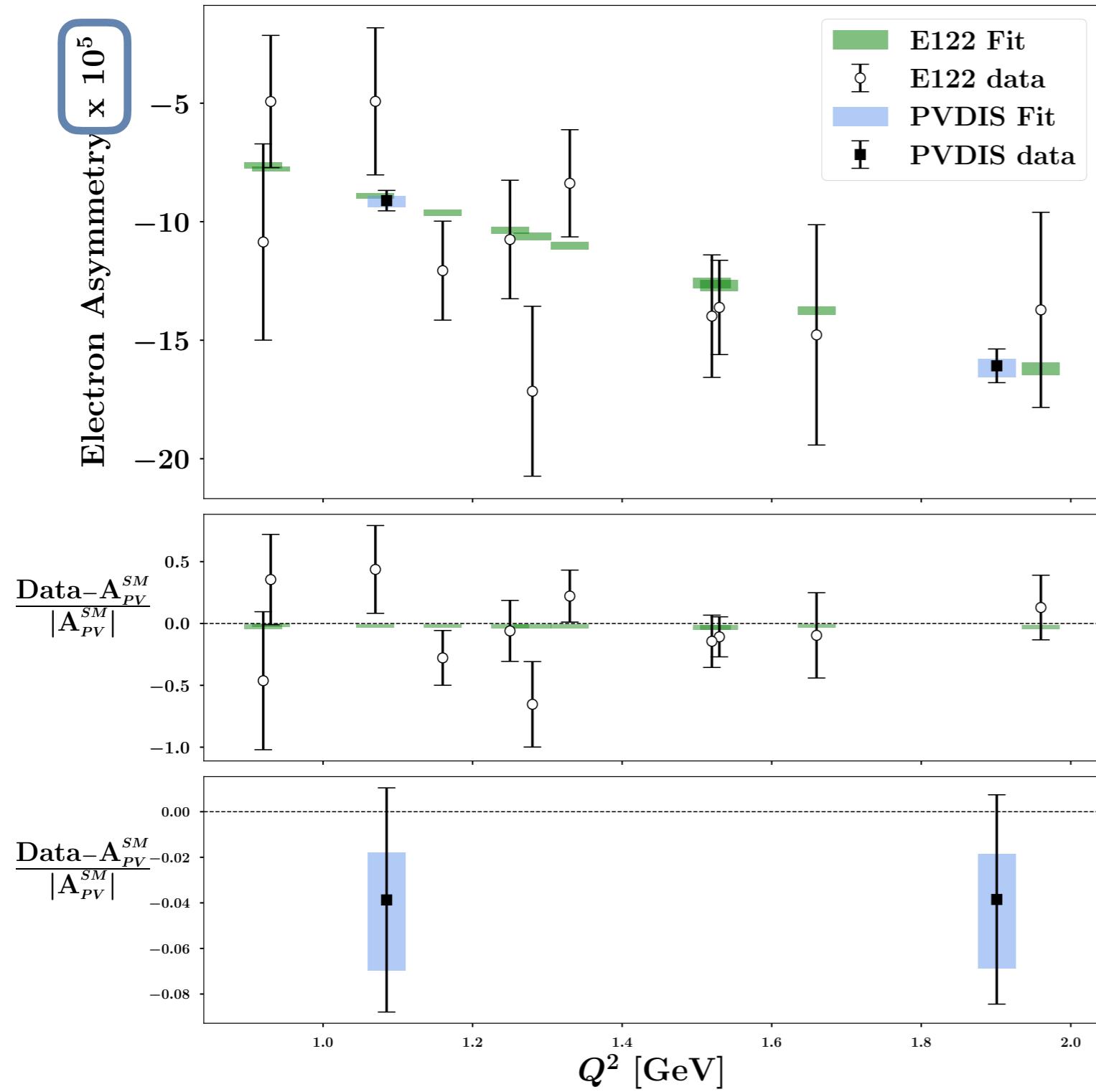
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Old dataset with still quite large
experimental errors ($> 20\%$)

Results of the fit: data vs theory



Sizeable improvement of the fit
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Old dataset with still quite large
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Data points which actually
drive the fit due to very small
experimental errors ($\sim \%$)

Results: size of the strong PV effect

$$g_1^{\text{PV}}(x) = \alpha g_1(x)$$

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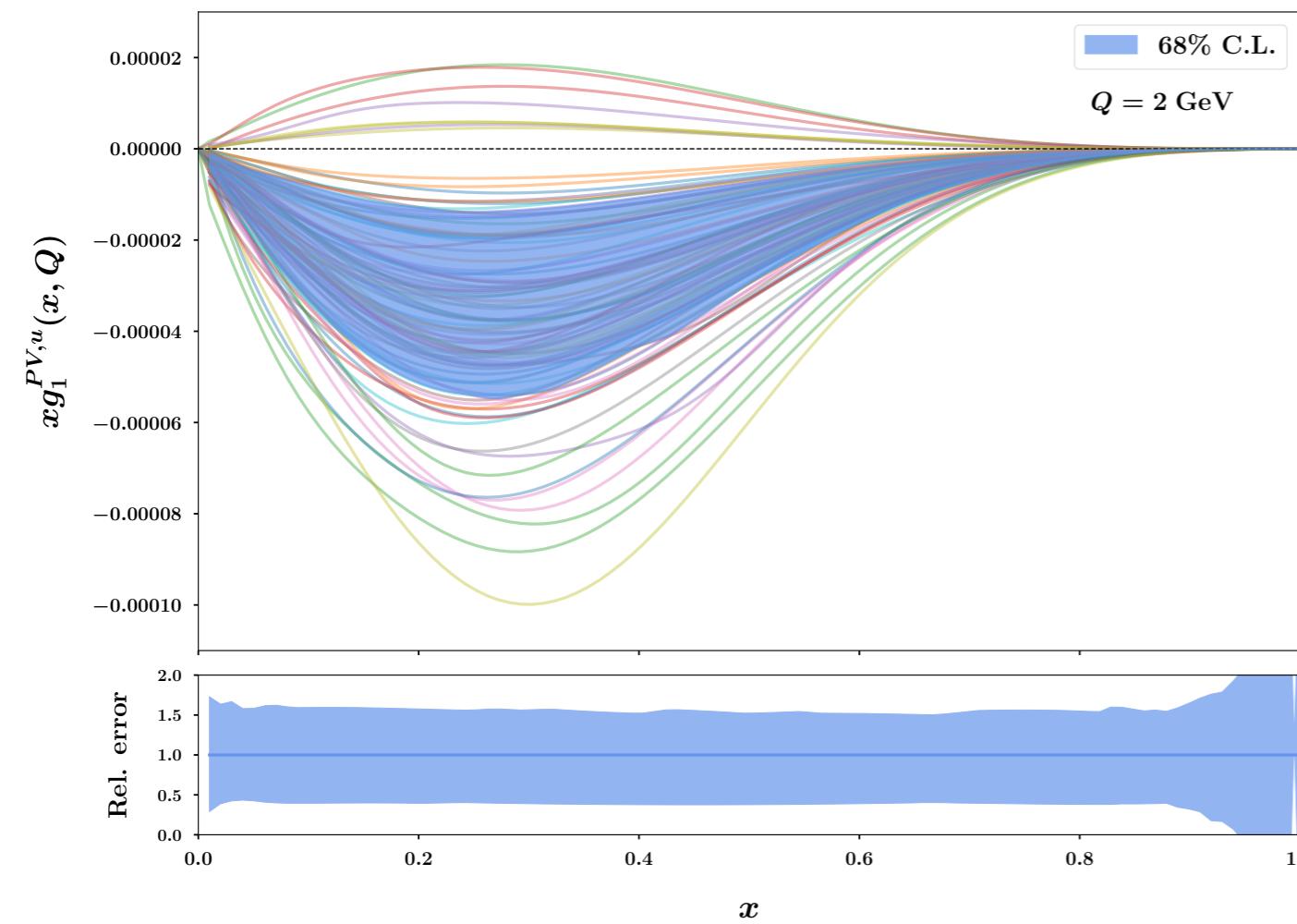
$$g_1^{\text{PV}}(x) = \alpha g_1(x)$$

$$\alpha = (-1.01 \pm 0.66) \cdot 10^{-4}$$

Results: size of the strong PV effect

$$g_1^{\text{PV}}(x) = \alpha g_1(x)$$

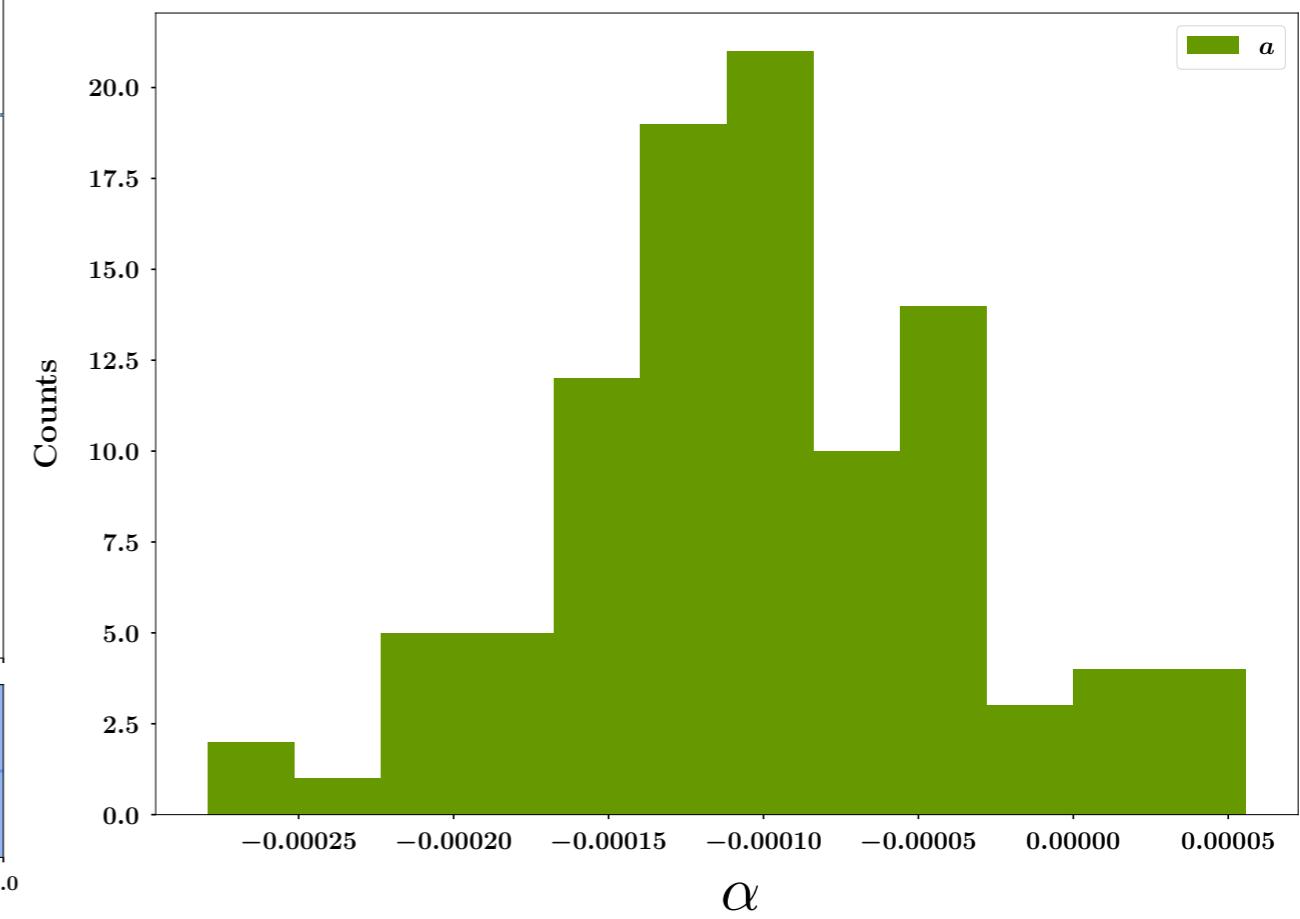
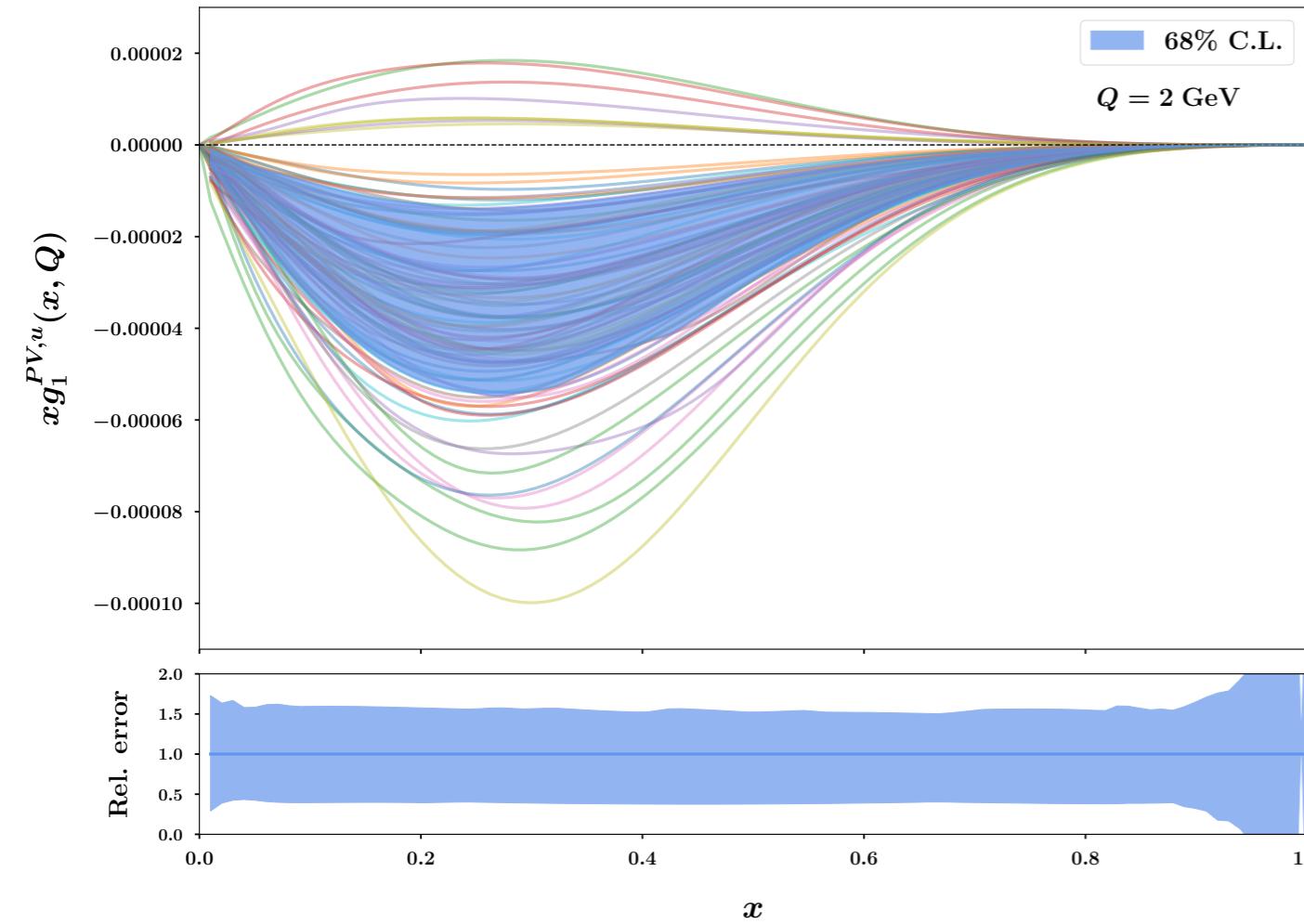
$$\alpha = (-1.01 \pm 0.66) \cdot 10^{-4}$$



Results: size of the strong PV effect

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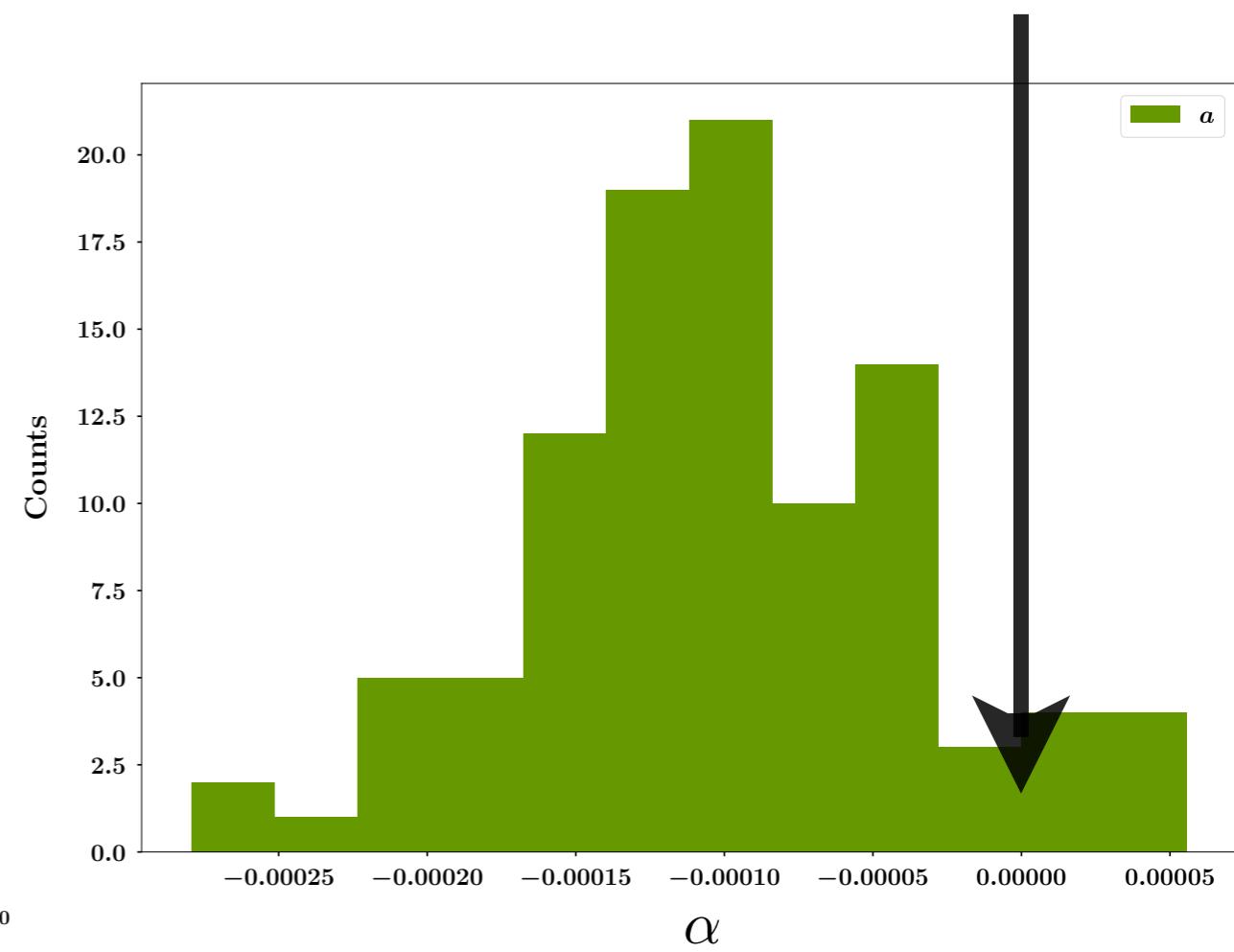
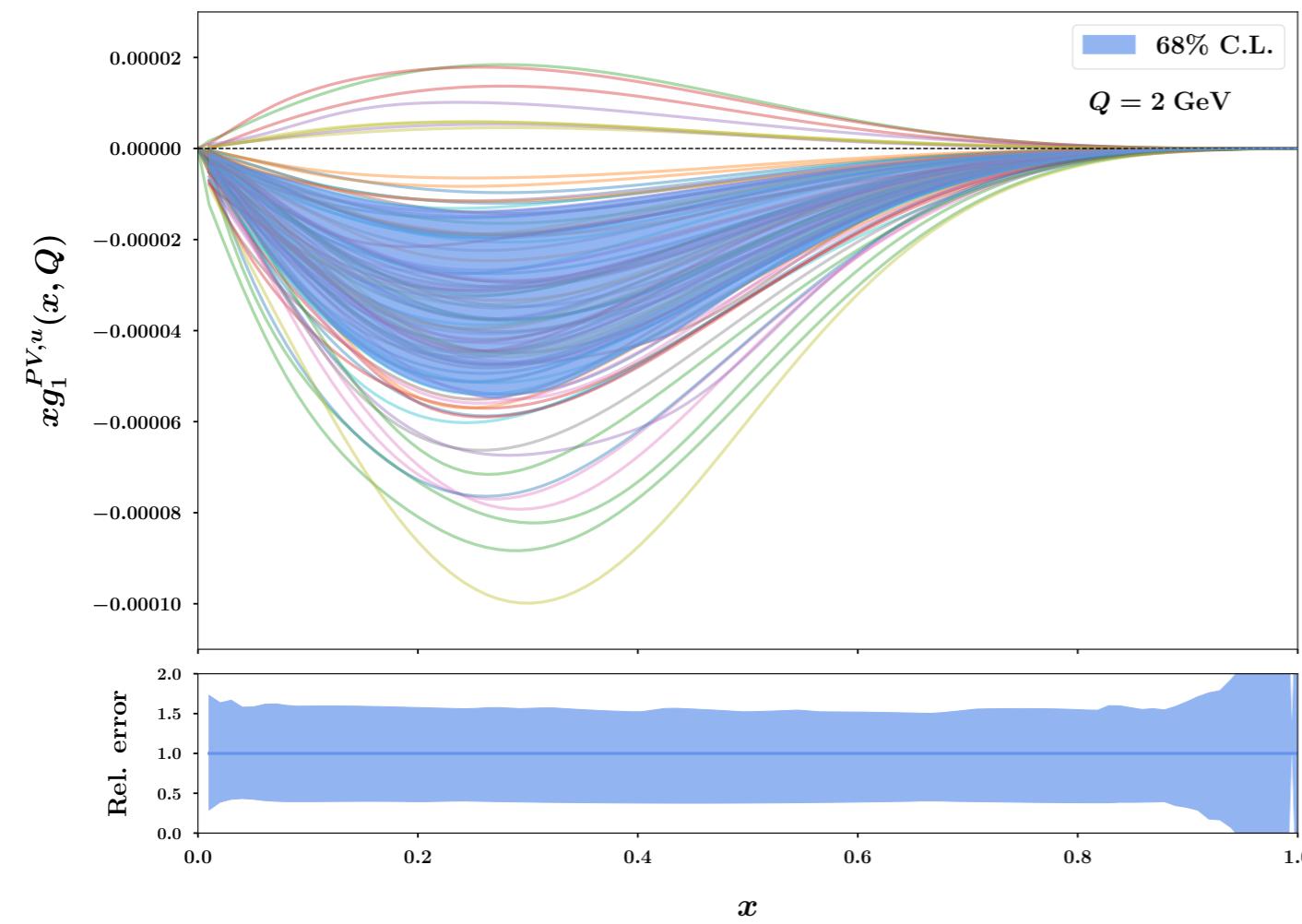


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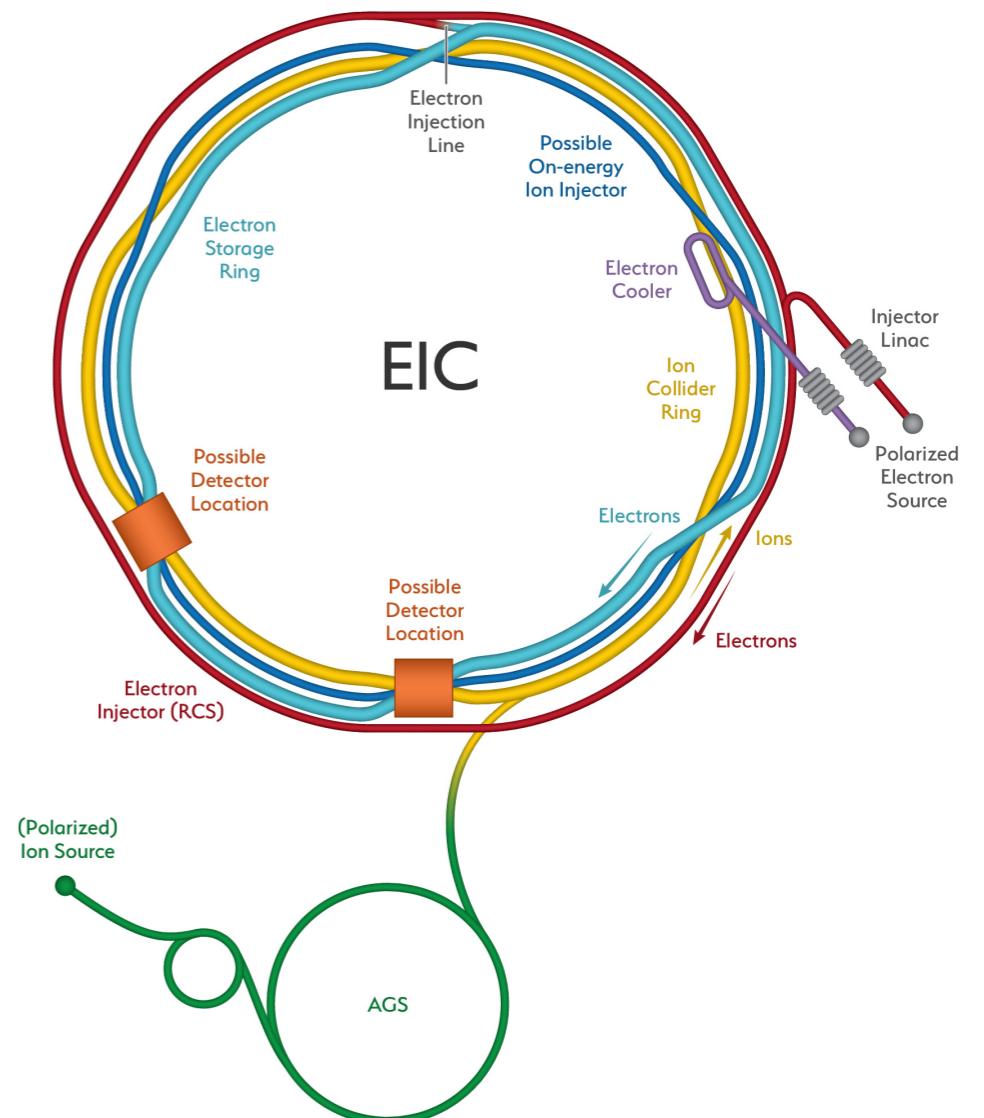
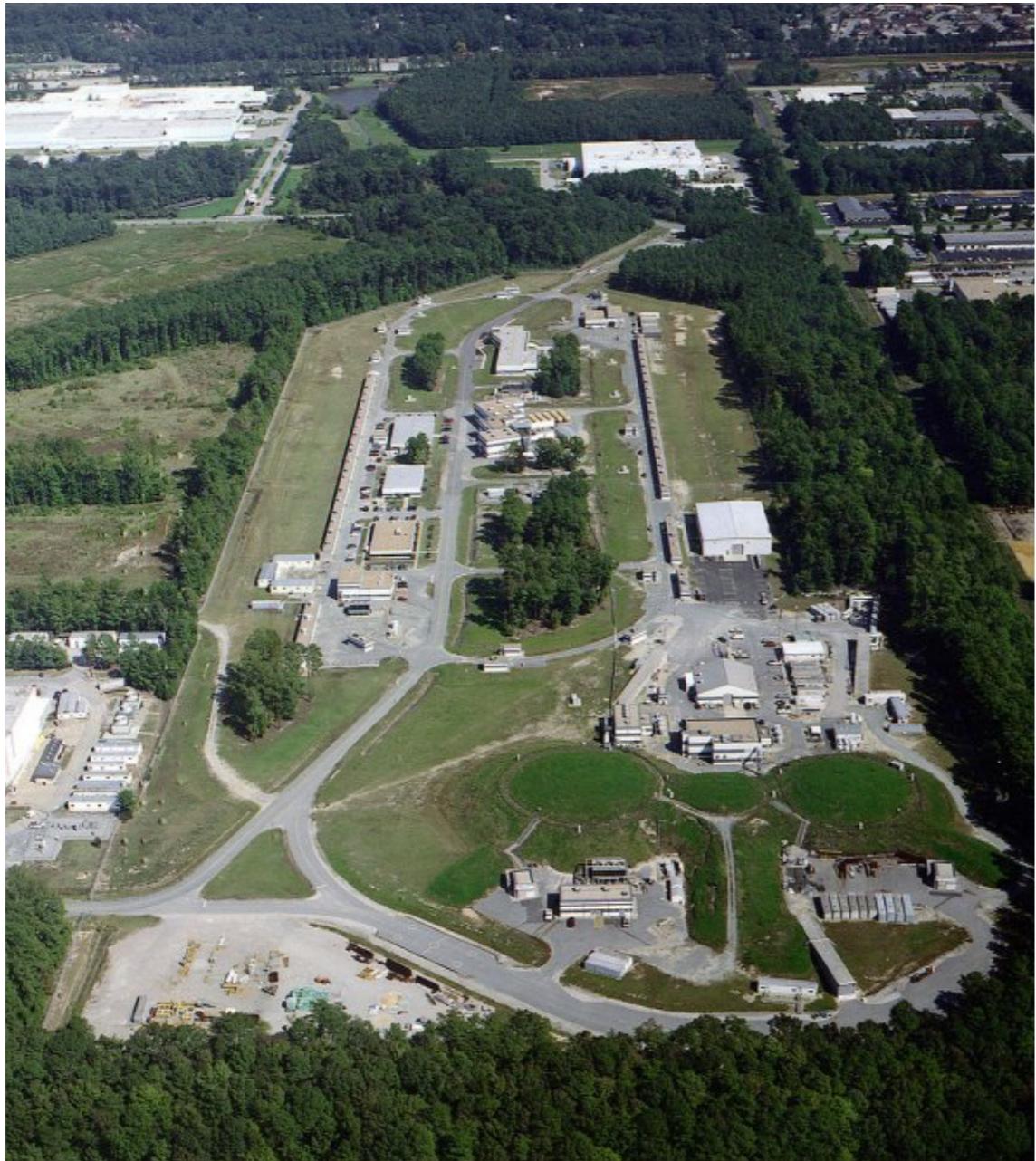
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$$\alpha = 0$$



Future facilities



Impact of future data

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JLab 12 GeV — SoLID detector

Wood, Bennet, Cho, et al., Science 275 (1997)

Souder, Reimer, Zheng, JLab Experiment E12-10-007 (2022 update)

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SoLID (d)

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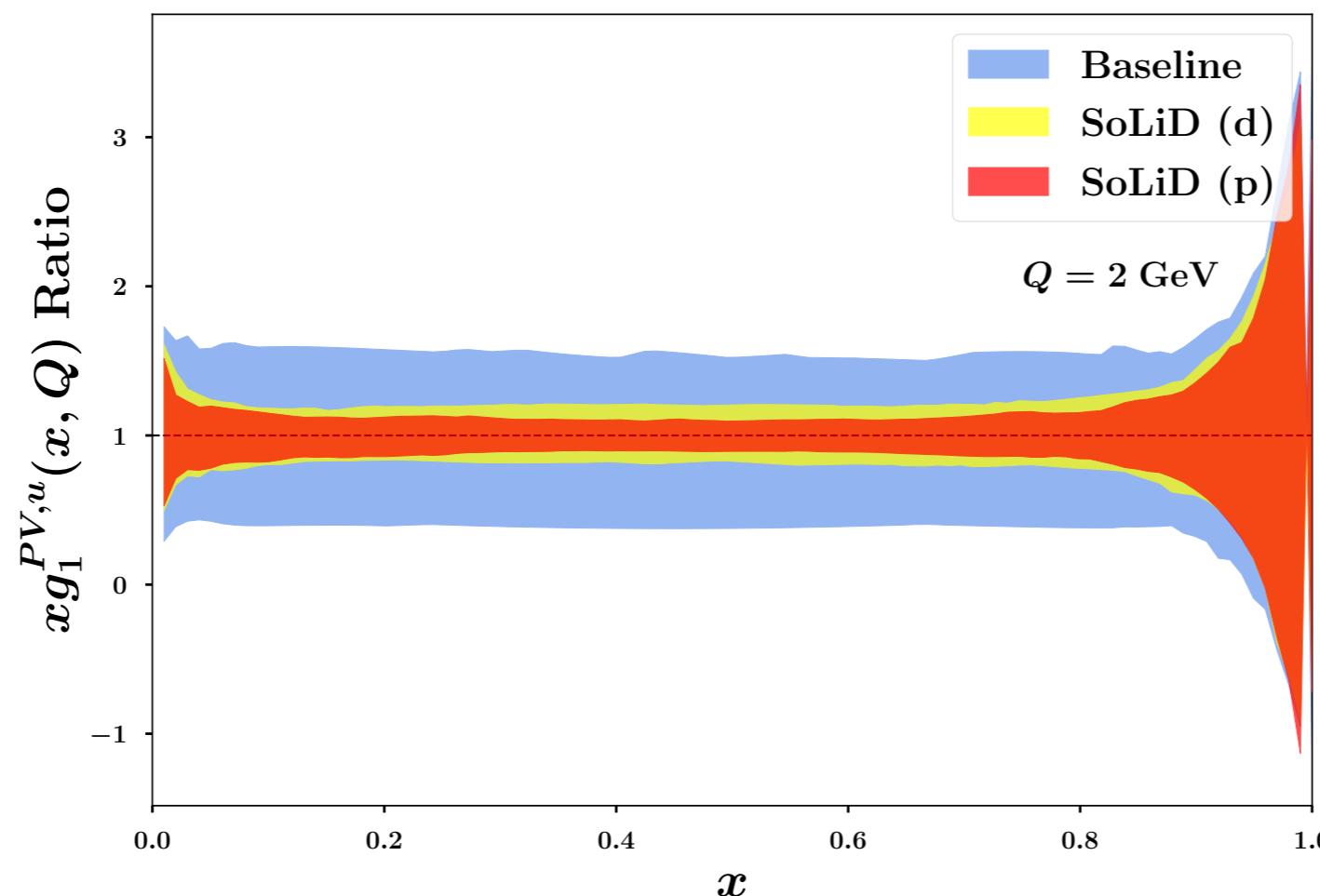
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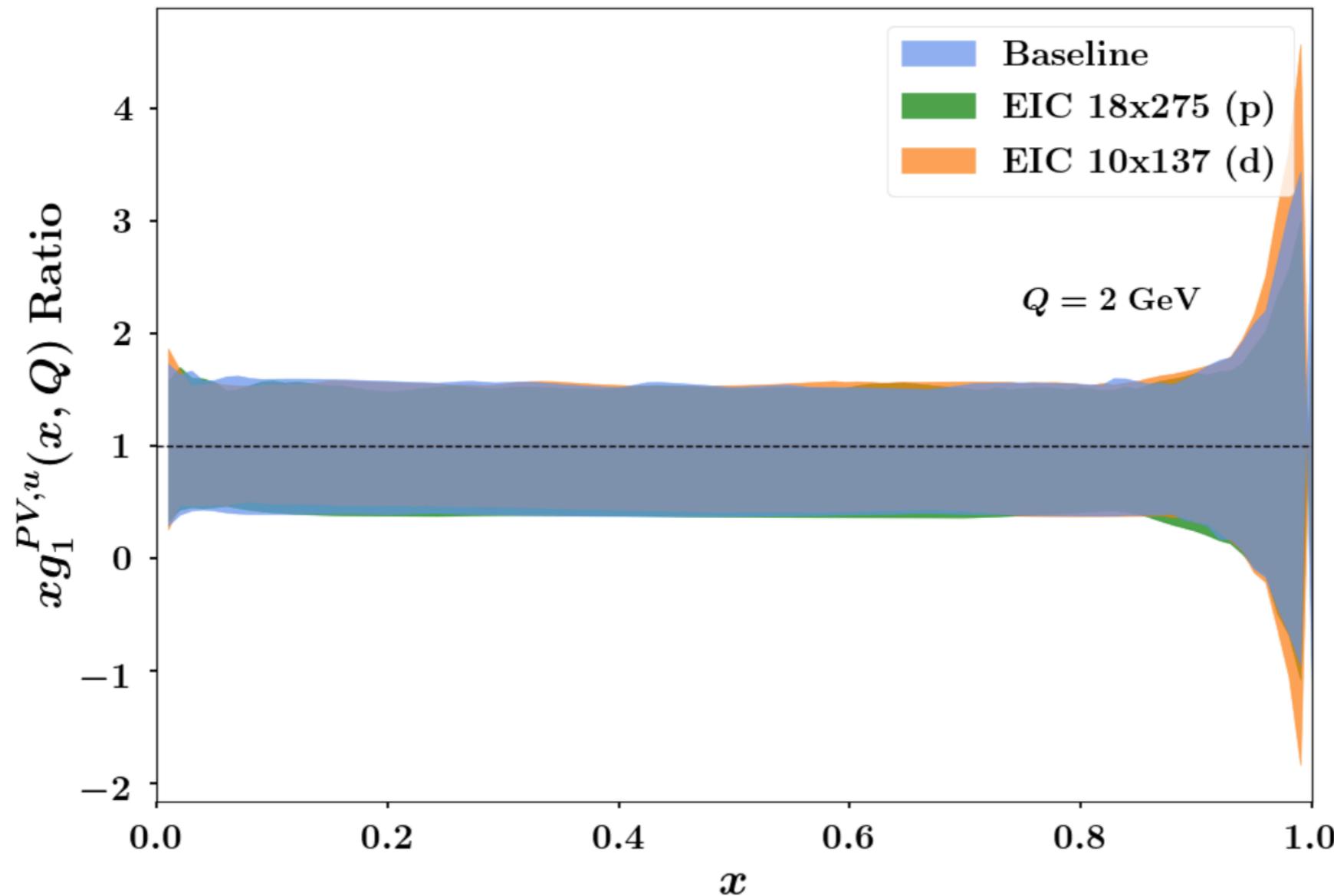
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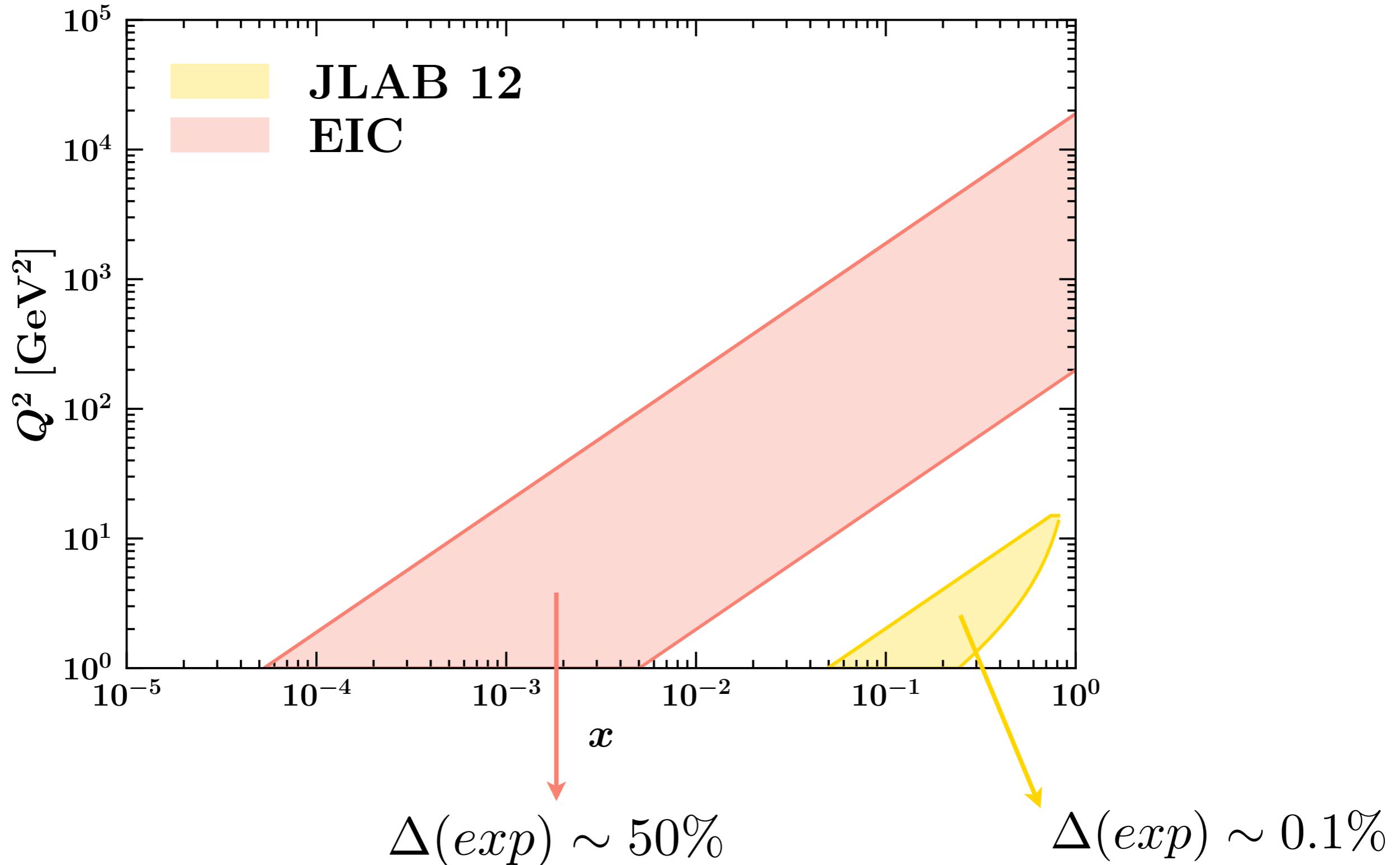
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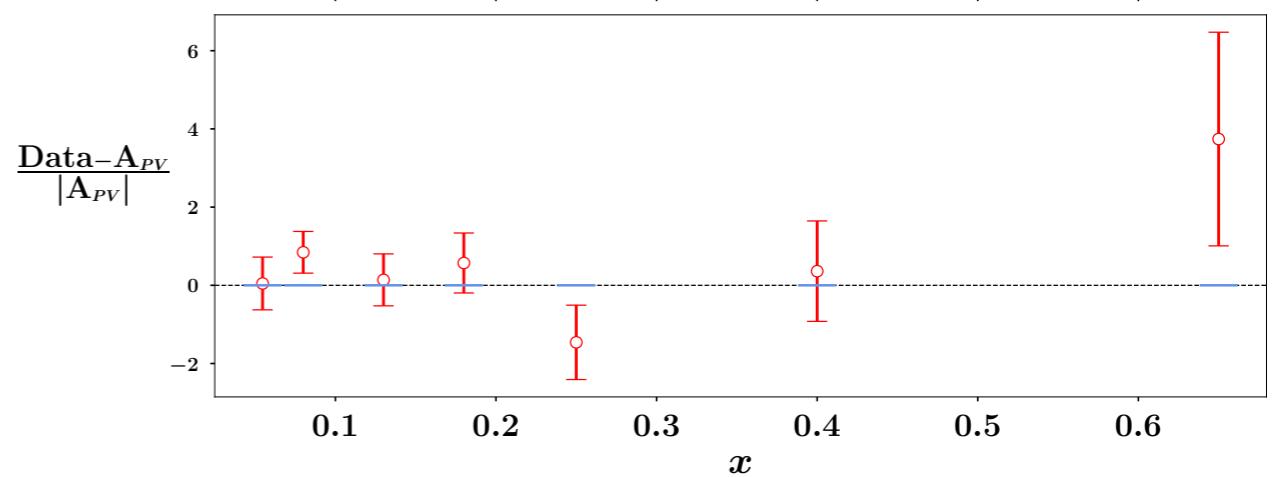
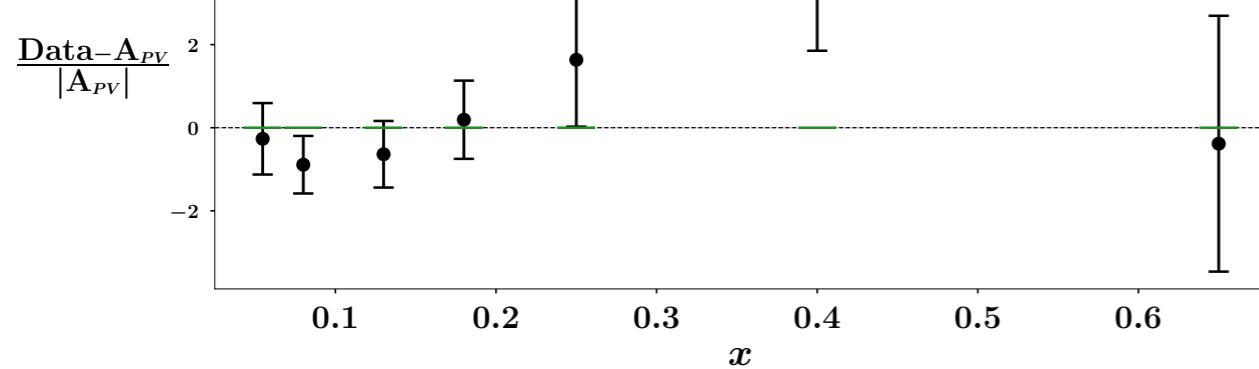
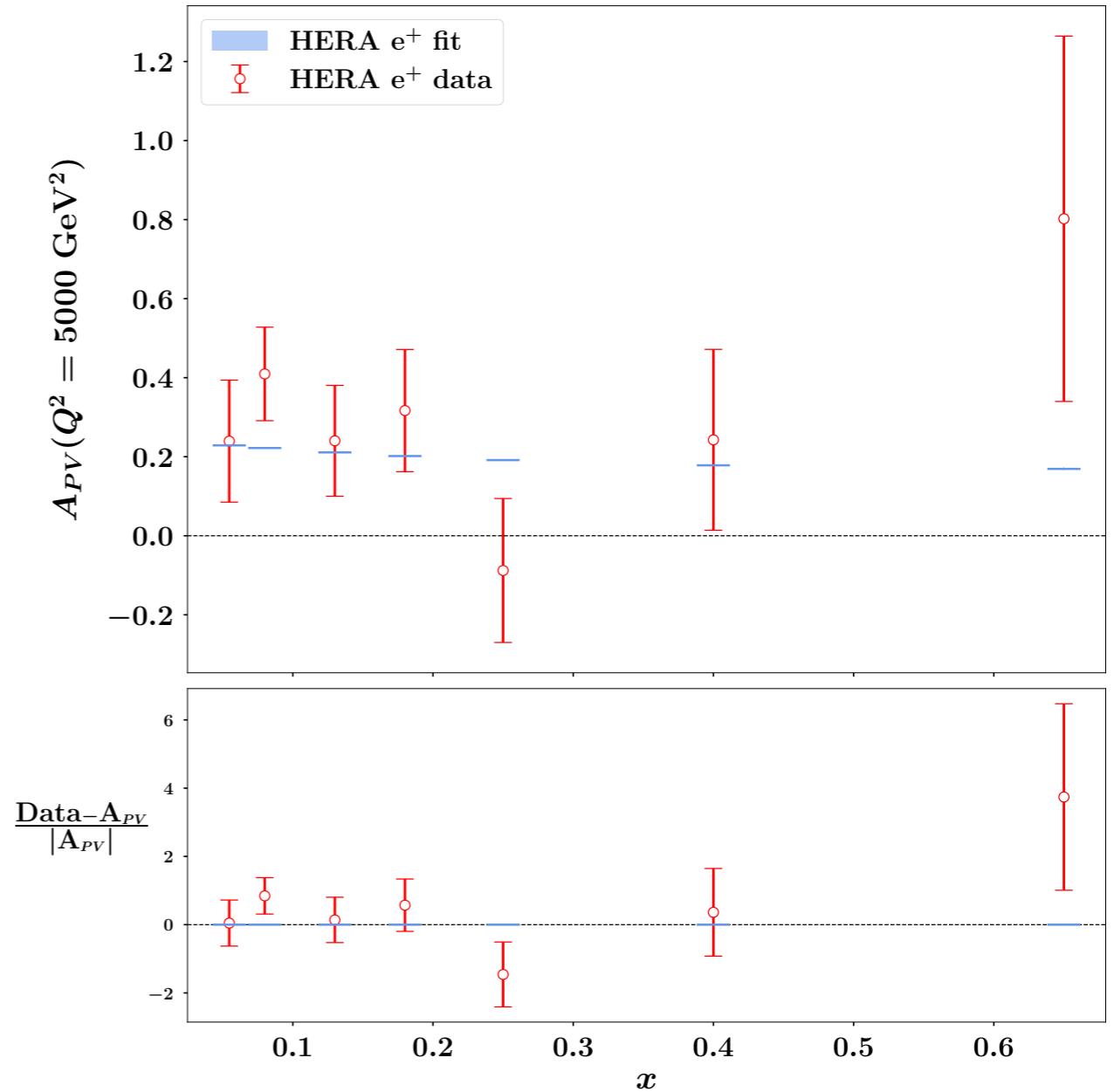
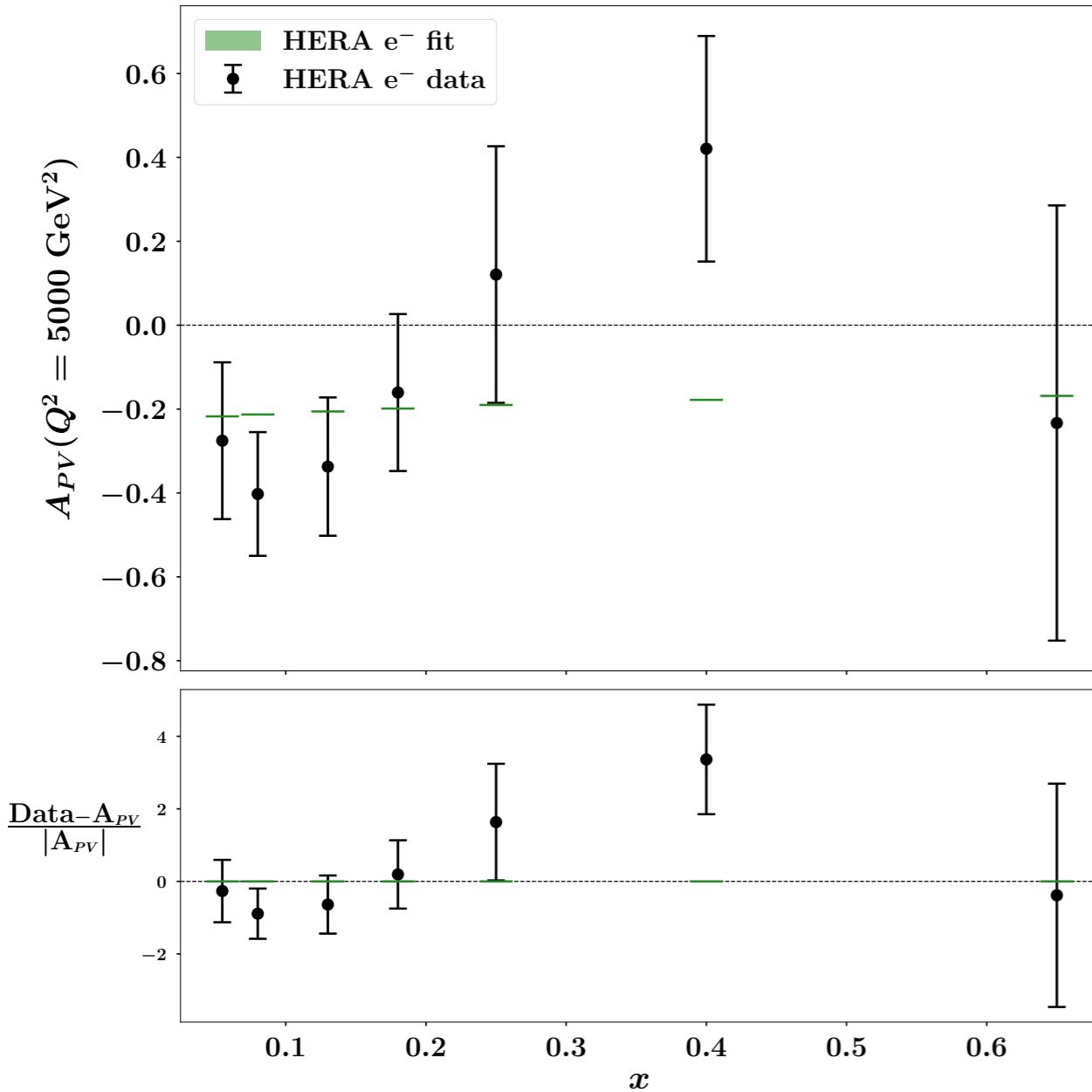


Step forward: dependence on x

- New model of the PV parton distribution

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Step forward: a new CP-odd PDF

- Further investigations on a new P-odd, CP-odd distribution function arising when considering the polarisation of the target

$$\begin{aligned}\Phi^q(x, Q^2) = & \left\{ f_1^q(x, Q^2) + g_1^{\text{PV}q}(x, Q^2)\gamma_5 \right. \\ & + S_L \left(g_1^q(x, Q^2)\gamma_5 + f_{1L}^{\text{PV}q}(x, Q^2) \right) \\ & \left. - S_T \left(h_1^q(x, Q^2)\gamma_5 - e_{1T}^{\text{PV}q}(x, Q^2) \right) \right\} \frac{\eta_+}{2}\end{aligned}$$

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$$\Delta x_B g_5(x_B, Q^2) \approx \Delta x_B g_5^{(\gamma)}(x_B, Q^2) = \frac{1}{2} \sum_q e_q^2 x_B f_{1L}^{\text{PV}(q-\bar{q})}$$

PDFs in DIS processes

Quark Polarization

	U	L	T
U	$f_1(x)$		
L		$g_1(x)$	
T			$h_1(x)$

PDFs in DIS processes

with P violation

Quark Polarization

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Electric dipole moment

Summary

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Summary

- The strong P- violation can give origin to a new structure function in DIS cross section for one-photon exchange
- A fit of present experimental data is compatible with a non-zero contribution from a new strong PV parton density
- To better assess the presence (or not) of this PV effect we need very precise experimental data
- Improvements in the theoretical framework of our analysis are surely needed to obtain more and more accurate results