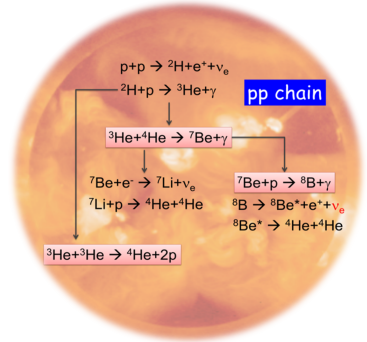


Ab initio calculations of reactions in the solar fusion chain

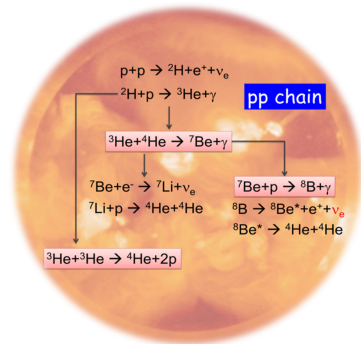
Mack C. Atkinson

Haverford College

${}^3\text{He}(\alpha, \gamma){}^7\text{Be}$ important for solar-model predictions

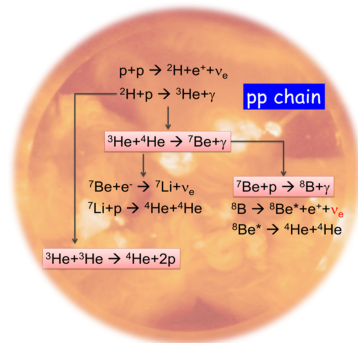
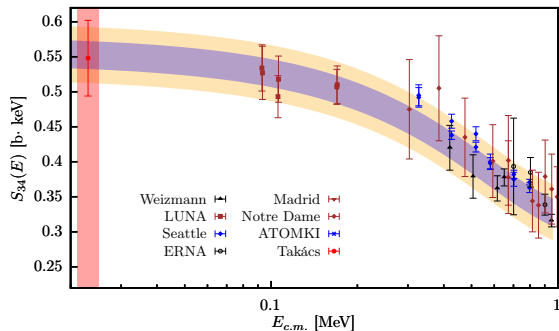


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$$\sigma(E) = \frac{S_{34}(E)}{E} \exp \left\{ -\frac{2\pi Z_1 Z_2 e^2}{\hbar \sqrt{2E/m}} \right\}$$

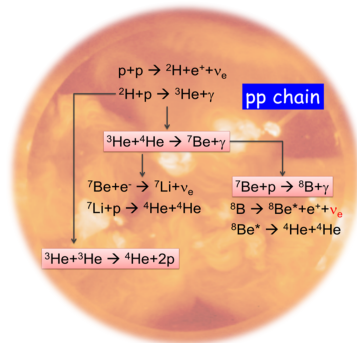
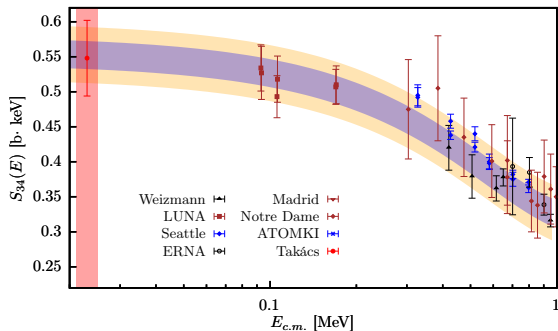
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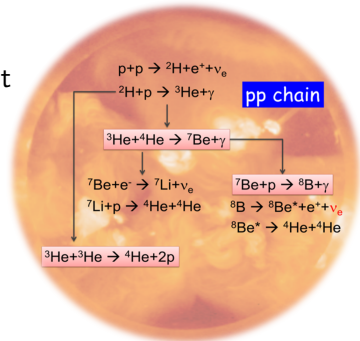
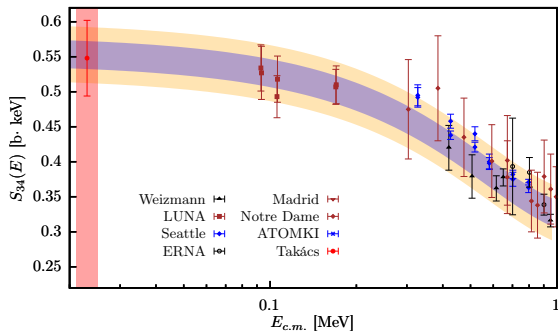
- Reaction rates too low at solar energies in the lab



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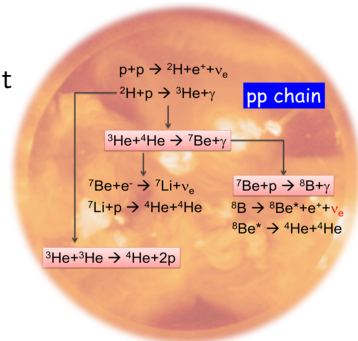
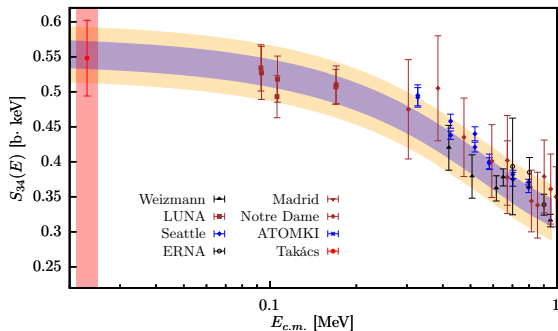
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- Current evaluations depend on both theory and experiment



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$^3\text{He}(\alpha, \gamma)^7\text{Be}$ important for solar-model predictions

- Reaction rates too low at solar energies in the lab
- Current evaluations depend on both theory and experiment
- Ideally, theory will accurately predict $S_{34}(E)$



$$\sigma(E) = \frac{S_{34}(E)}{E} \exp \left\{ -\frac{2\pi Z_1 Z_2 e^2}{\hbar \sqrt{2E/m}} \right\}$$

Goal: Improve the theoretical prediction of $S_{34}(E)$

Current evaluation:

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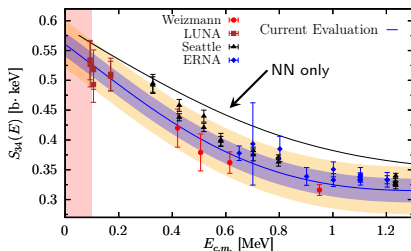
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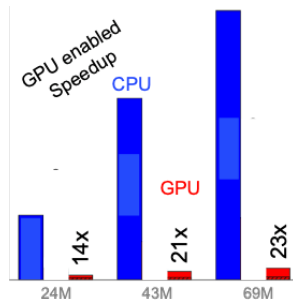
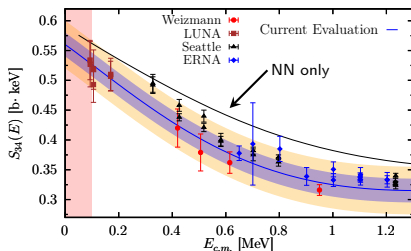


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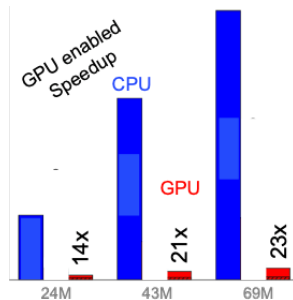
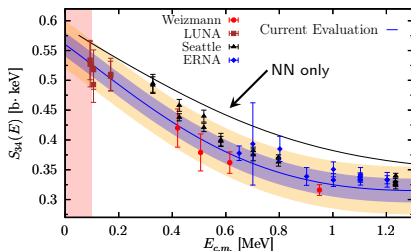


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- GPU speedup $\Rightarrow$ NNN forces are now included

Ab initio reaction theory needed for capture calculations

- Calculate EM transitions from ${}^3\text{He}+\alpha$ scattering state to ${}^7\text{Be}$ bound state

Ab initio reaction theory needed for capture calculations

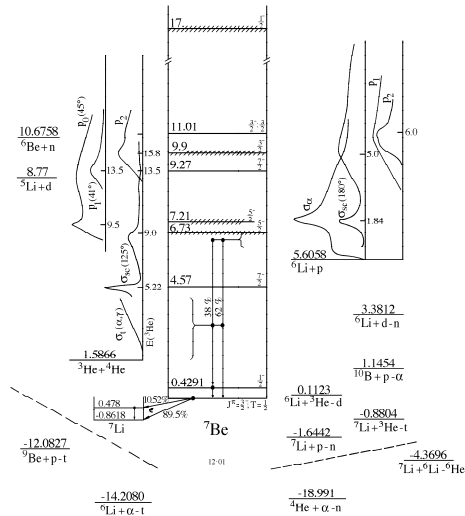
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$$\left\langle \psi_{bs} (^7\text{Be}) \left| \hat{\mathcal{M}}_{\text{EM}} \right| \psi_{sc} (^3\text{He} + \alpha) \right\rangle$$

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 - Only $E1$, $E2$, and $M1$ transitions

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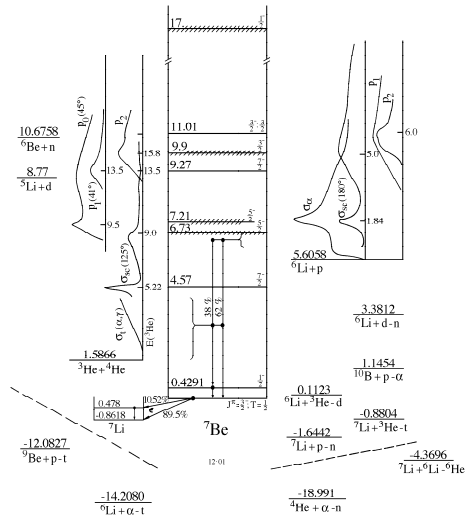


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- Need a method to calculate ψ_{sc} and ψ_{bs} simultaneously



The *ab initio* method: from NCSM to NCSMC

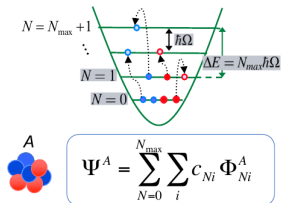
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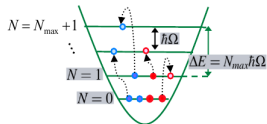
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The *ab initio* method: from NCSM to NCSMC



$$\Psi^A = \sum_{N=0}^{N_{\max}} \sum_i c_{Ni} \Phi_{Ni}^A$$

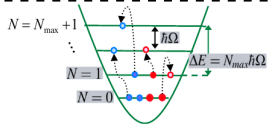
$$\hat{H} = \hat{T} + \hat{V}_{NN} + \hat{V}_{NNN}$$

$$\hat{H} |\Psi^A\rangle = E |\Psi^A\rangle$$

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 $\hbar\Omega$
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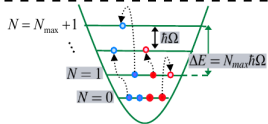
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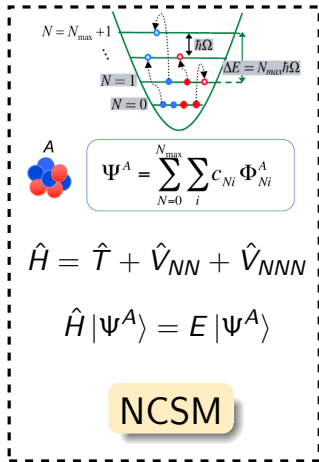
NCSM

$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| \begin{array}{c} (A) \\ \text{cluster} \end{array}, \lambda \right\rangle + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \begin{array}{c} \text{cluster} \\ (A-a) \end{array}, \nu \right\rangle$$

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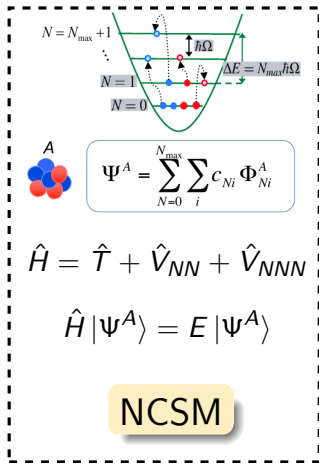
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$\uparrow$
 $|^7\text{Be}\rangle$

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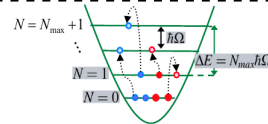
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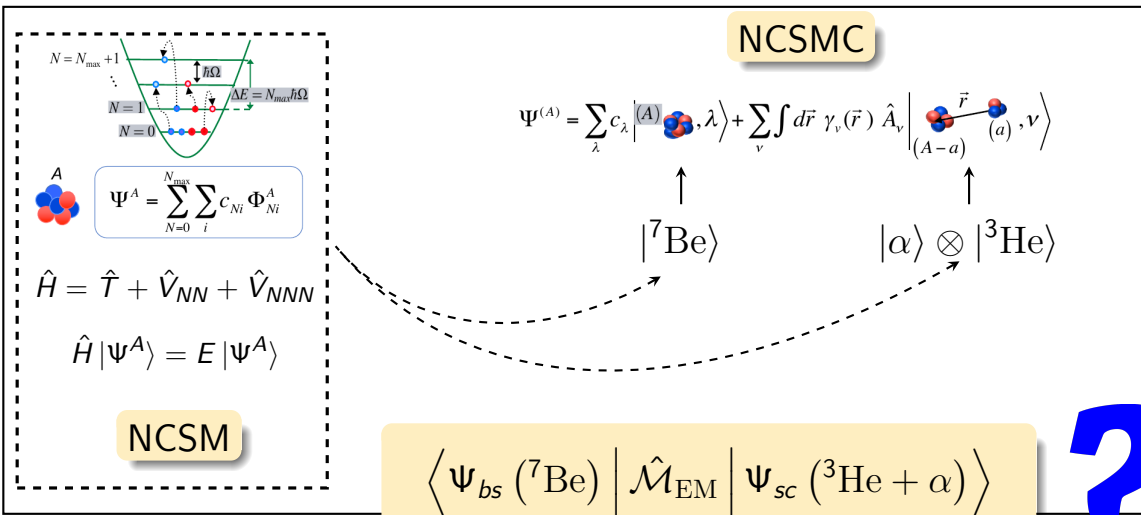
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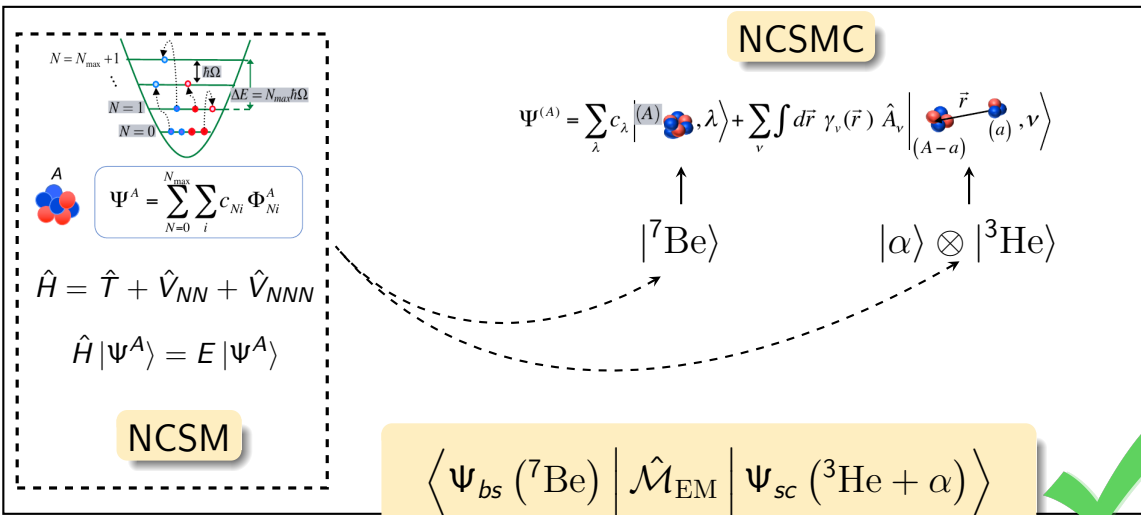
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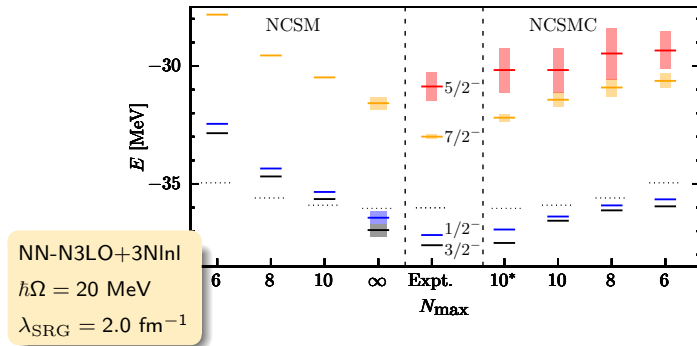
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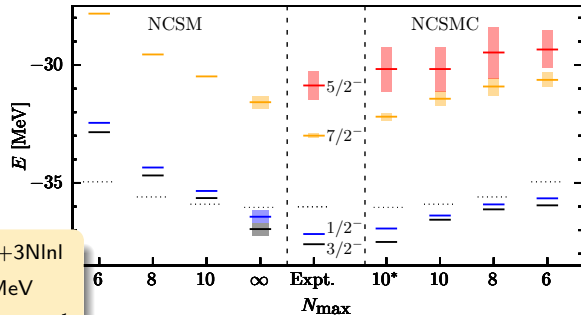
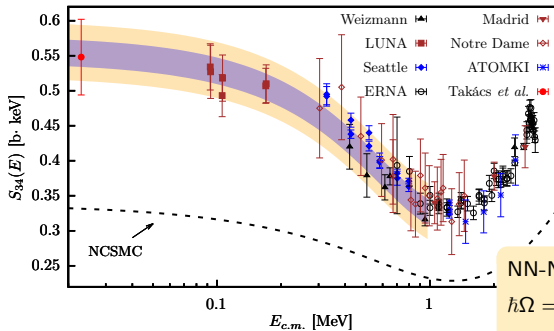
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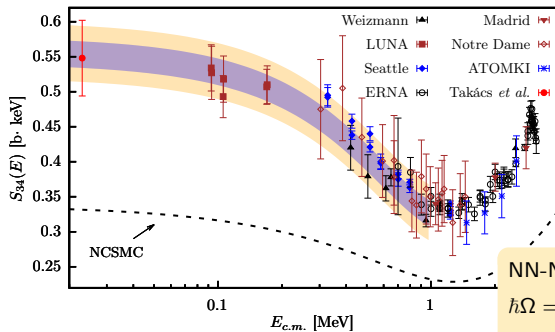
NCSMC Calculation of ${}^3\text{He}+{}^4\text{He}$ well-converged, levels need shifting



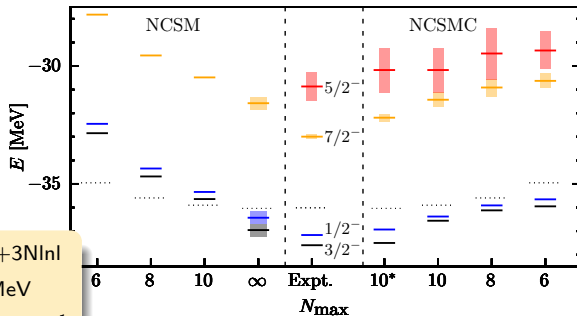
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NN-N3LO+3NInl
 $\hbar\Omega = 20$ MeV
 $\lambda_{\text{SRG}} = 2.0 \text{ fm}^{-1}$



- Capture rate accurate only if Expt. levels reproduced

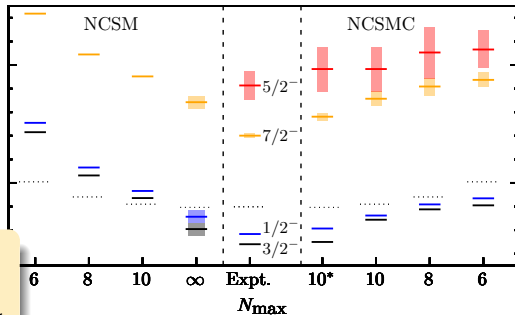
${}^7\text{Be}$	NCSM	NCSMC	Expt.
$E_{3/2^-}$	0.261	-1.05	-1.587
$E_{1/2^-}$	0.563	-0.874	-1.16
$C_{3/2^-}$	-	3.46	-
$C_{1/2^-}$	-	3.44	-
r_{ch}	2.44	2.70	2.647(17)

NCSMC Calculation of ${}^3\text{He}+{}^4\text{He}$ well-converged, levels need shifting

$$\begin{pmatrix} H_{NCSM} & h \\ h & H_{RGM} \end{pmatrix} \begin{pmatrix} \textcircled{C} \\ \textcircled{\gamma} \end{pmatrix} = E \begin{pmatrix} 1_{NCSM} & g \\ g & N_{RGM} \end{pmatrix} \begin{pmatrix} \textcircled{C} \\ \textcircled{\gamma} \end{pmatrix} \quad E \text{ [MeV]}$$

$E_{\lambda}^{NCSM} \delta_{\lambda\lambda'}$ (blue box) $\rightarrow$ H_{NCSM}
 $\langle (A) | H \hat{A}_v | (a) \rangle_{(A-a)}$ (green box) $\rightarrow$ h
 $\delta_{\lambda\lambda'}$ (blue box) $\rightarrow$ 1_{NCSM}
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NN-N3LO+3Nlnl
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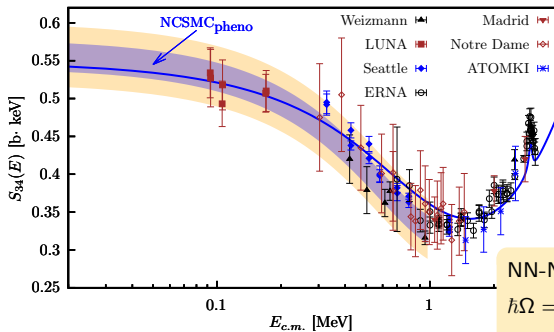


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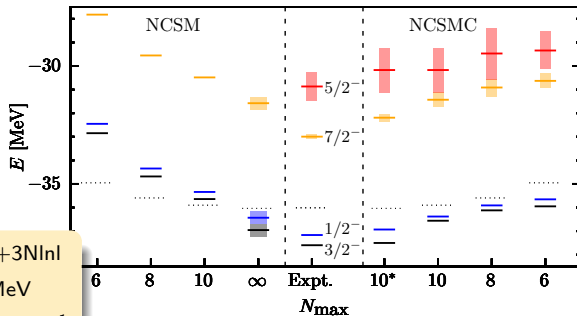
- Capture rate accurate only if Expt. levels reproduced

$$E_{\lambda}^{NCSM} \rightarrow E_{\lambda}^{NCSM} + \epsilon$$

NCSMC Calculation of ${}^3\text{He}+{}^4\text{He}$ well-converged, levels need shifting



NN-N3LO+3NInl
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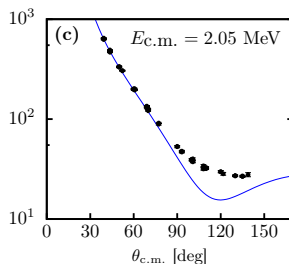
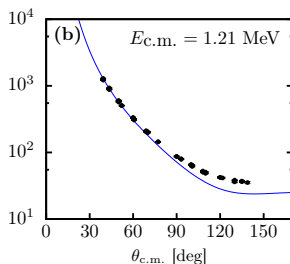
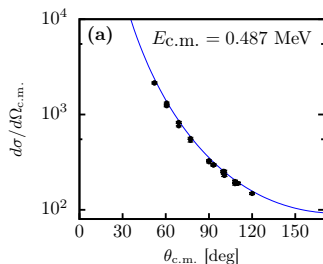
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Now, how about the scattering wave functions?

- Compare to elastic scattering results to further probe ψ_{sc}



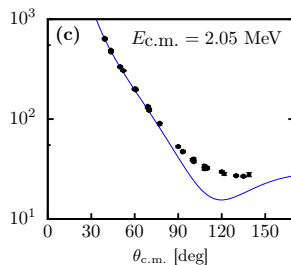
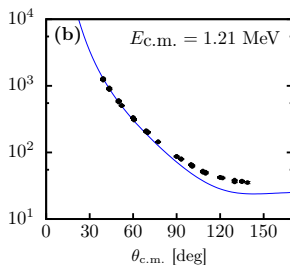
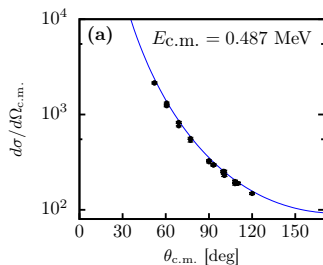
NN-N3LO+3Nlnl

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Now, how about the scattering wave functions?

- Compare to elastic scattering results to further probe ψ_{sc}
- Experiment done at TRIUMF in 2022 $\rightarrow$ lowest E measured to date



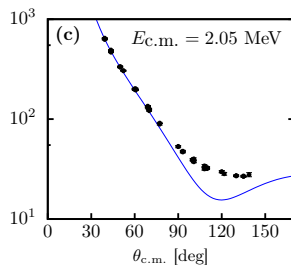
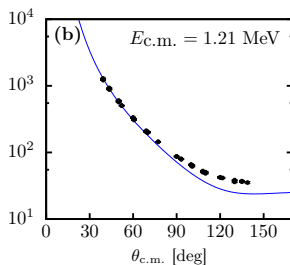
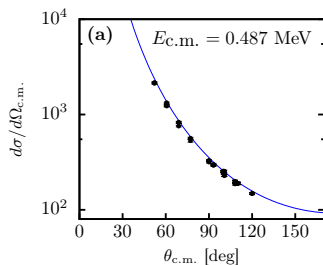
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$\hbar\Omega = 20$ MeV

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Now, how about the scattering wave functions?

- Compare to elastic scattering results to further probe ψ_{sc}
- Experiment done at TRIUMF in 2022 $\rightarrow$ lowest E measured to date



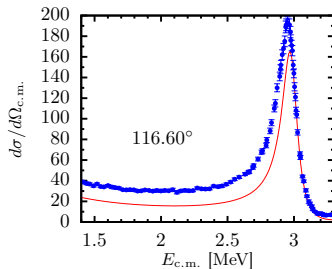
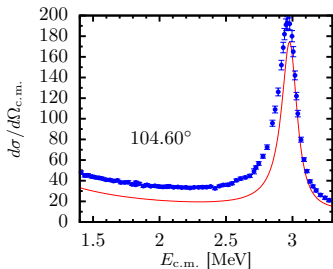
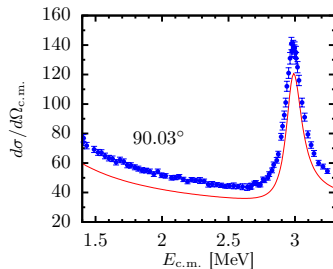
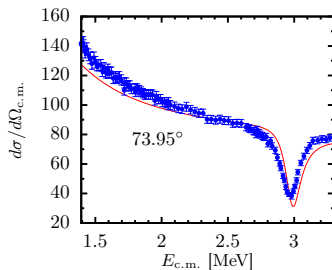
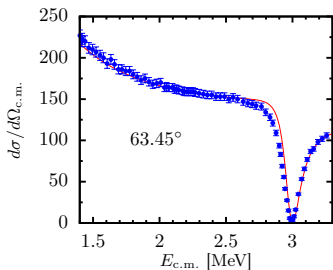
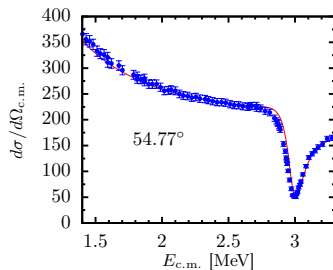
- What is the source of discrepancy at large angles?

NN-N3LO+3Nlnl

$\hbar\Omega = 20$ MeV

$\lambda_{SRG} = 2.0 \text{ fm}^{-1}$

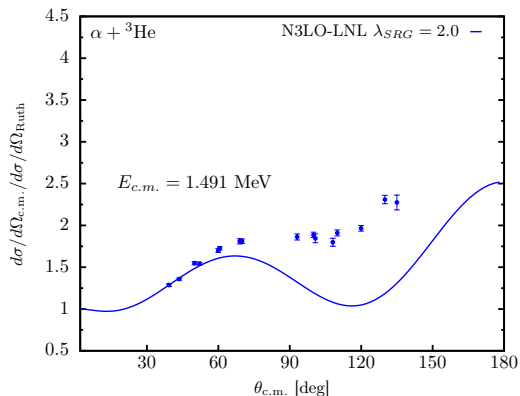
Same large-angle discrepancy when comparing to 1964 Barnard *et al.*



Diagnosing the discrepancy

- Rutherford obscures the fact that a constant shift accounts for the discrepancy

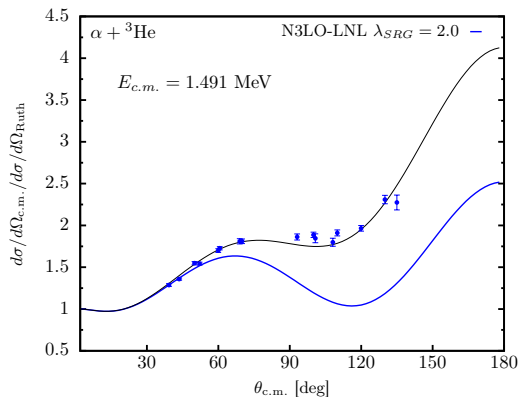
$$\frac{d\sigma}{d\Omega}_{\text{Ruth}} = \left(\frac{Z_1 Z_2 e^2}{8\pi\epsilon_0 m v^2 \sin^2(\frac{\theta}{2})} \right)^2$$



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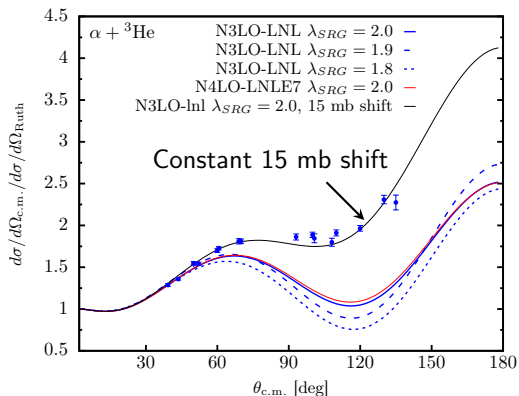


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- Nothing in the NCMSC appears to reproduce the 15 mb shift



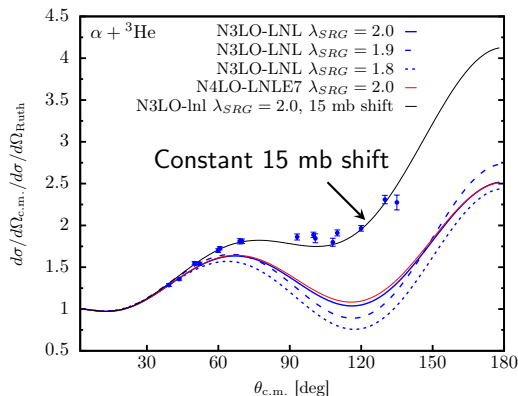
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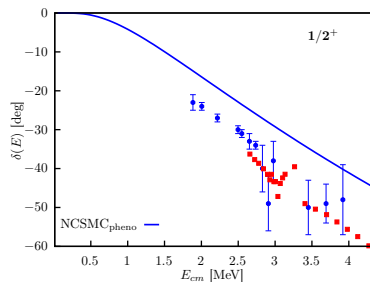
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How can we emulate a constant shift?



The $1/2^+$ channel is responsible for this constant shift, BUT...

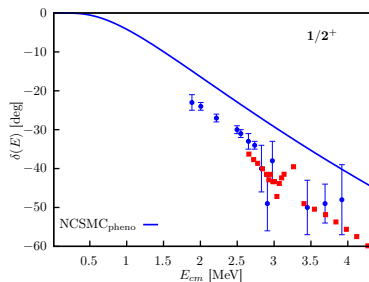
- More repulsion is needed in the $1/2^+$ channel



The $1/2^+$ channel is responsible for this constant shift, BUT...

- More repulsion is needed in the $1/2^+$ channel
- Explicitly add repulsion

$$\mathcal{H}_{\nu\nu'}^{1/2^+}(r, r') \rightarrow \mathcal{H}_{\nu\nu'}^{1/2^+}(r, r') + V(r, r')$$

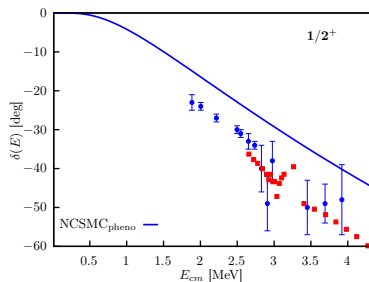


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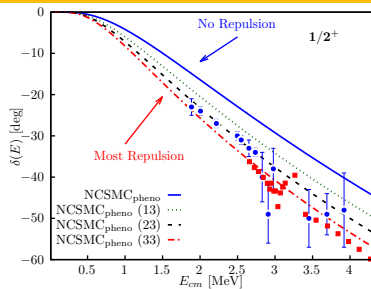


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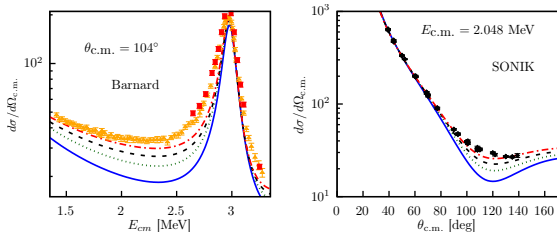
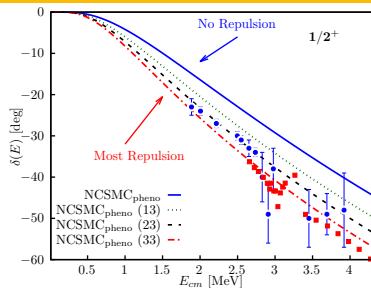


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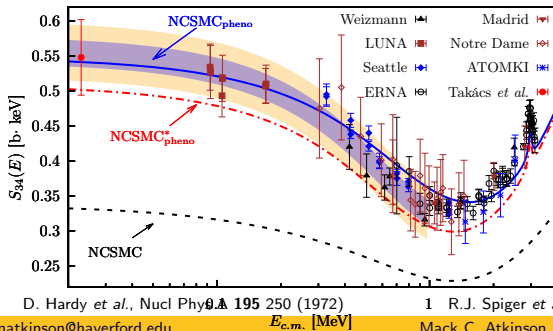
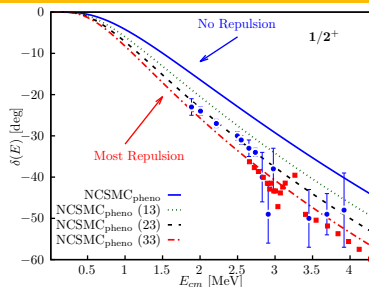


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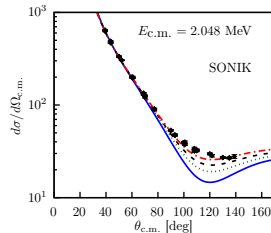
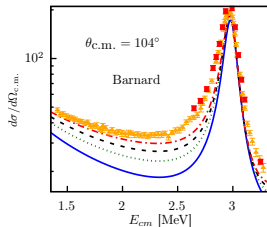
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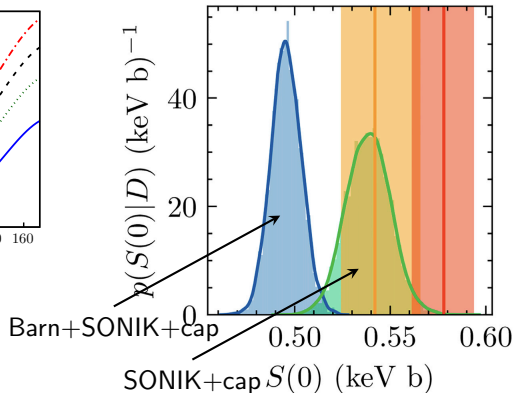
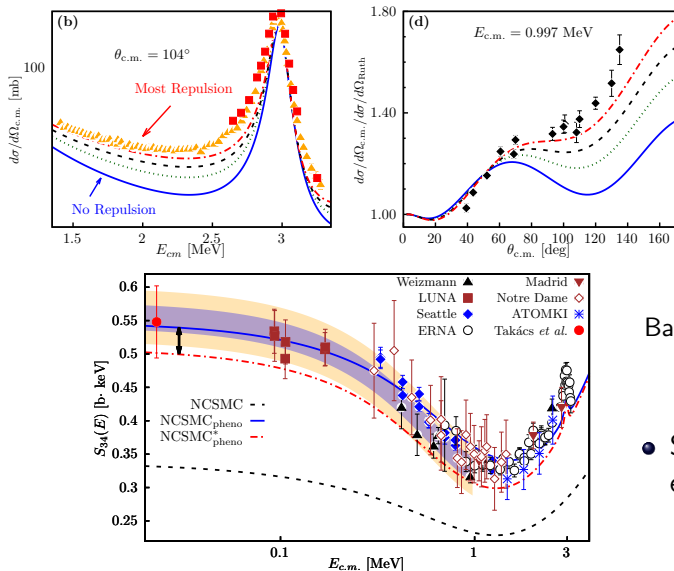
D. Hardy *et al.*, Nucl Phys **A 195** 250 (1972)

1 R.J. Spiger *et al.*, Phys Rev **163** 964 (1967)

M.C. Atkinson *et al.*, PLB **860** 139189 (2025)



Tension in data sets also observed in R matrix analyses

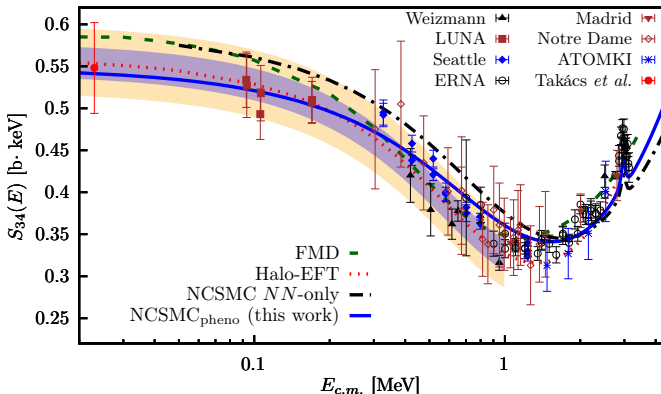


- Simultaneous R matrix fit of capture and elastic scattering

Odell *et al.*, *Front. in Phys.* **10** 888476 (2022)

Data-Informed S factor

- Tension between elastic and capture data dominates the uncertainty



Model	$S_{34}(0)$ [keV b]
NCSMC _{pheno}	0.545 ± 0.001
NCSMC _{pheno} *	0.505
halo EFT [9]	$0.577^{+0.015}_{-0.016}$
halo EFT [10]	$0.558 \pm 0.008(\text{fit}) \pm 0.056(\text{EFT})$
R -matrix [60]	$0.539^{+0.011}_{-0.012}$
SF III [2]	$0.561 \pm 0.018(\text{exp}) \pm 0.022(\text{th})$

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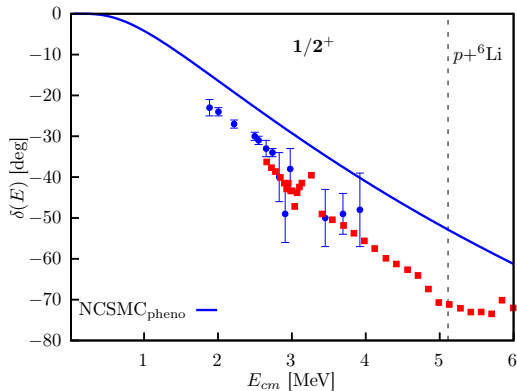
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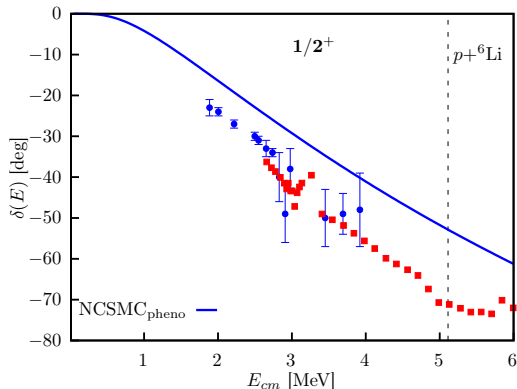
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2 Chiral interaction

- Phase shift shows some dependence on interaction
- Need to compare more interactions



From bound to continuum: $^{11}\text{Be} \rightarrow (p + ^{10}\text{Be}) + \beta + \nu$



Physics Letters B

www.elsevier.com/locate/physletb

$^{11}\text{Be}(\beta p)$, a quasi-free neutron decay?

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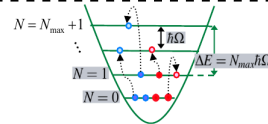
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NCSMC calculation of ^{11}Be and ^{11}B



$$\Psi^A = \sum_{N=0}^{N_{\max}} \sum_i c_{Ni} \Phi_{Ni}^A$$

$$\hat{H} = \hat{T} + \hat{V}_{NN} + \hat{V}_{NNN}$$

$$\hat{H} |\Psi^A\rangle = E |\Psi^A\rangle$$

NCSM

NCSMC

$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| \begin{array}{c} (A) \\ \text{cluster} \end{array}, \lambda \right\rangle + \sum_v \int d\vec{r} \gamma_v(\vec{r}) \hat{A}_v \left| \begin{array}{c} \text{cluster} \\ (A-a) \end{array}, v \right\rangle$$

$\uparrow$
 $|^{11}\text{B}\rangle$

$\uparrow$
 $|p\rangle \otimes |^{10}\text{Be}\rangle$

$\langle \Psi_{sc} (p + ^{10}\text{Be}) | \hat{\mathcal{M}}_{\text{GT}} | \Psi_{bs} (^{11}\text{Be}) \rangle$

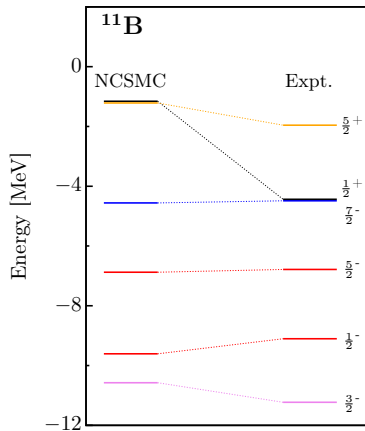


NCSMC Calculation of ^{11}B and ^{11}Be

NN-N4LO(500)+3Nlnl

$\hbar\Omega = 18 \text{ MeV}$, $N_{\text{max}} = 7$

$\lambda_{\text{SRG}} = 1.8 \text{ fm}^{-1}$

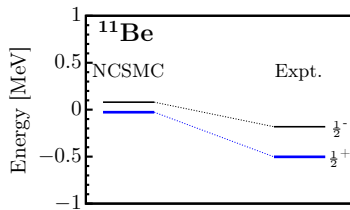
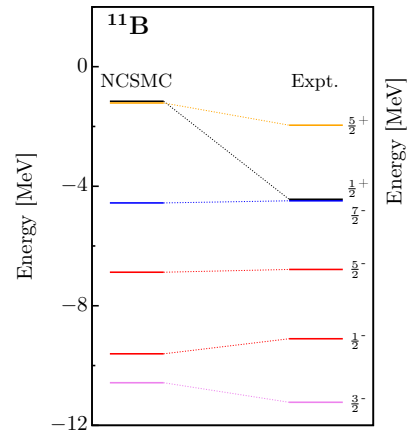


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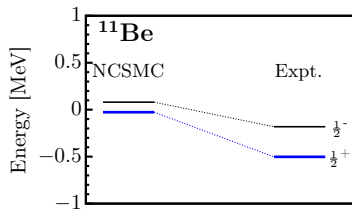
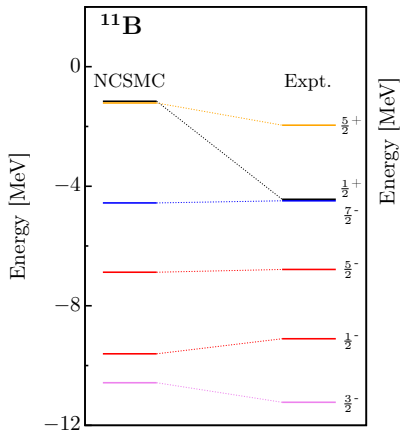
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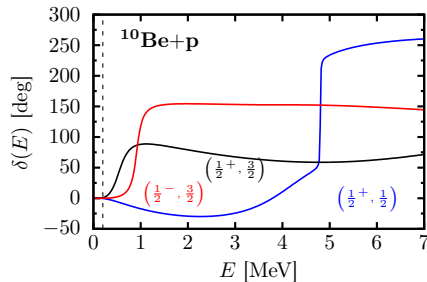
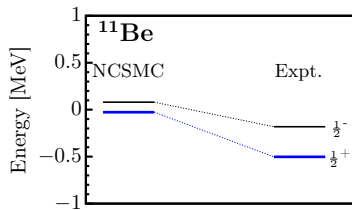
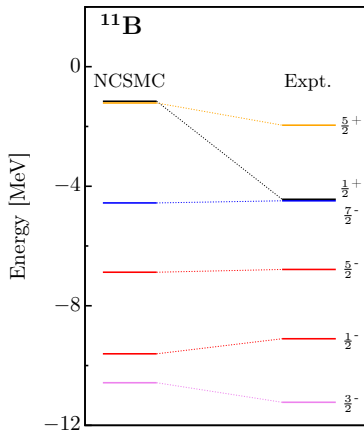
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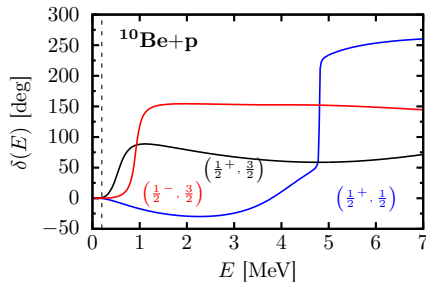
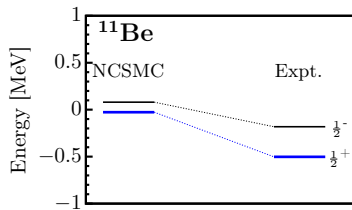
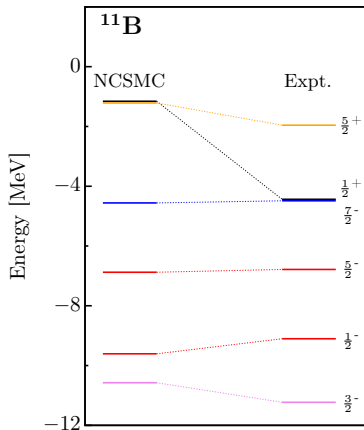
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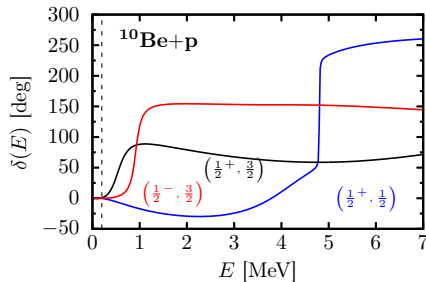
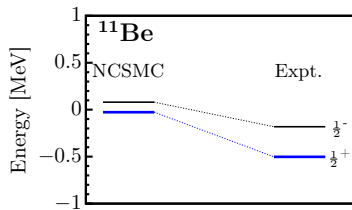
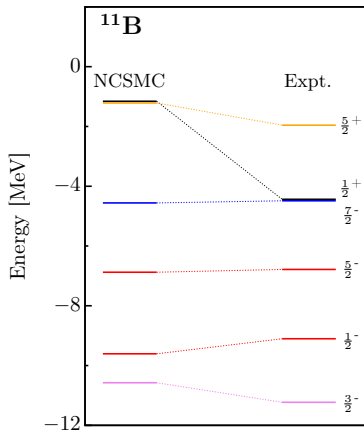
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- Phenomenologically shift levels to calculate β -decay



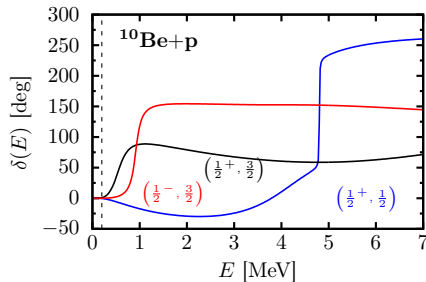
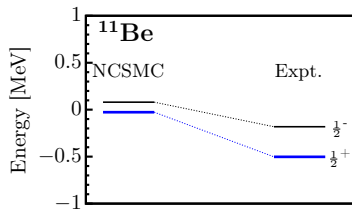
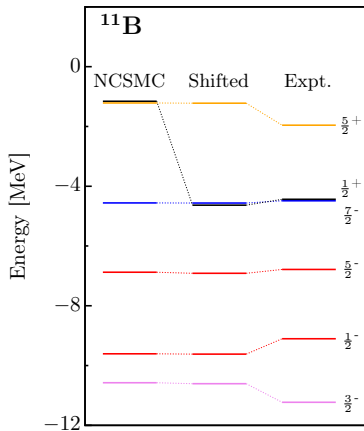
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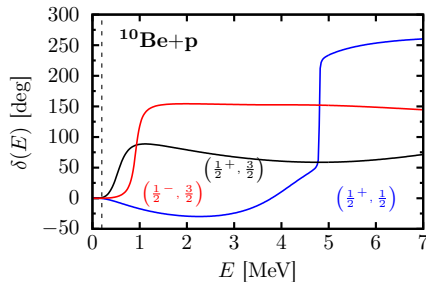
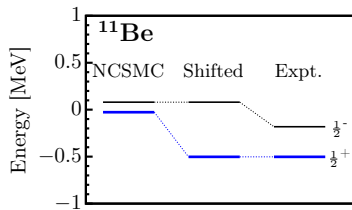
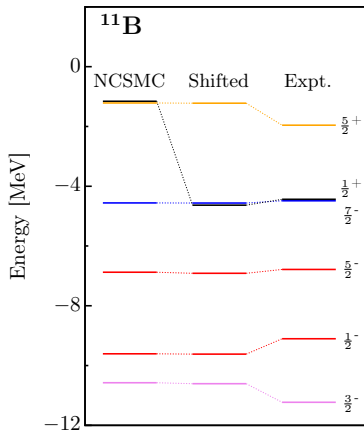
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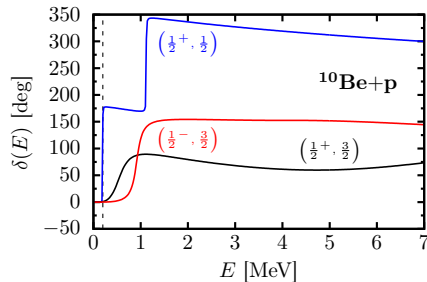
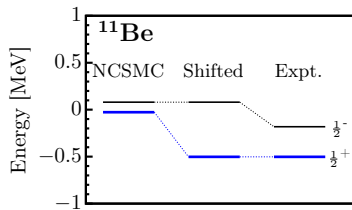
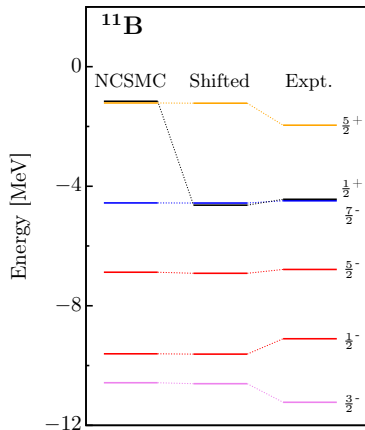
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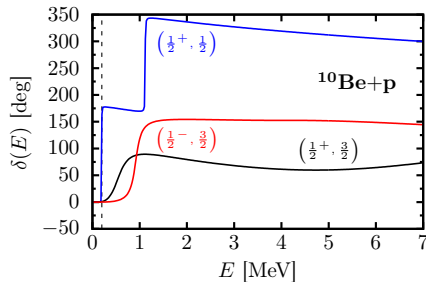
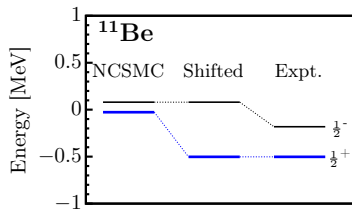
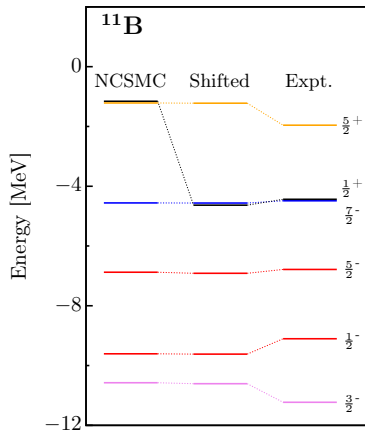
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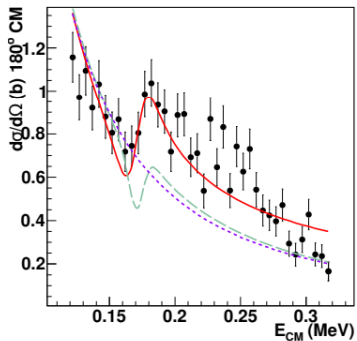


	NCSMC-shifted	Expt.
E [keV]	197	197(20)
Γ [keV]	10	12(5)

M.C. Atkinson *et al.*, PRC **105**, 054316 (2022)

The $1/2^+$ resonance does enhance the branching ratio

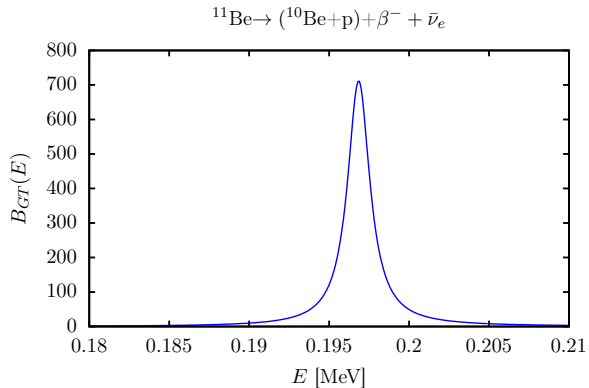
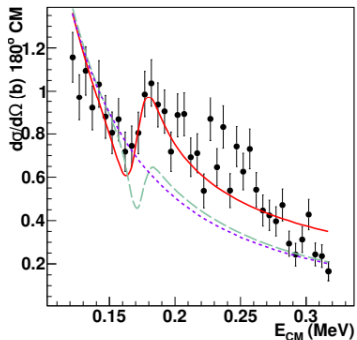
Ayyad *et al.*, PRL **129** 012501 (2022)



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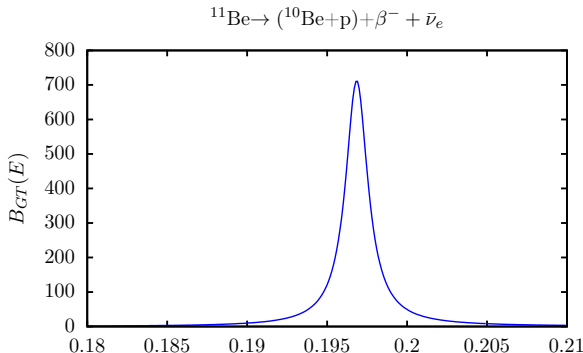
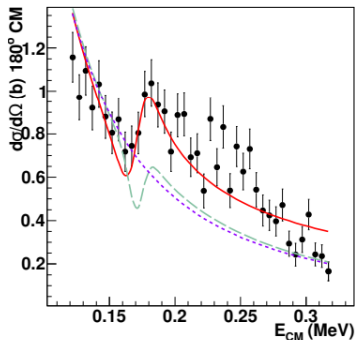
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Ayyad *et al.*, PRL **129** 012501 (2022)



$(1/2^+, 1/2)$	$N_{\max} = 5$		$N_{\max} = 7$		Expt.
	NCSM	NCSMC _{pheno}	NCSM	NCSMC _{pheno}	
$B(\text{GT})$	1.95	0.325	1.39	0.565	$5.5^{8.3}_{3.3}$
b_p	—	7.4×10^{-7}	—	1.3×10^{-6}	$1.3(3) \times 10^{-5}$

M.C. Atkinson *et al.*, PRC **105**, 054316 (2022)

Summary

- *Ab initio* calculation of ${}^3\text{He}(\alpha, \gamma){}^7\text{Be}$ capture reaction using the NCSMC
- NCSMC results with $NN+3N$ quantitatively reproduce data
- Simultaneous analysis of elastic and capture data reveals tension
- Future: Explore lack of repulsion in $1/2^+$ channel
- Future: Include $p+{}^6\text{Li}$ channel

Thanks!



Sofia Quaglioni

(LLNL)

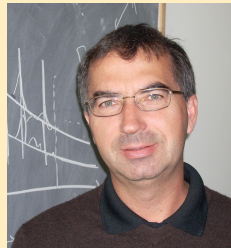


Kostas Kravvaris



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Petr Navratil

(TRIUMF)