

# J/ $\psi$ production in pp and Heavy Ion Collisions

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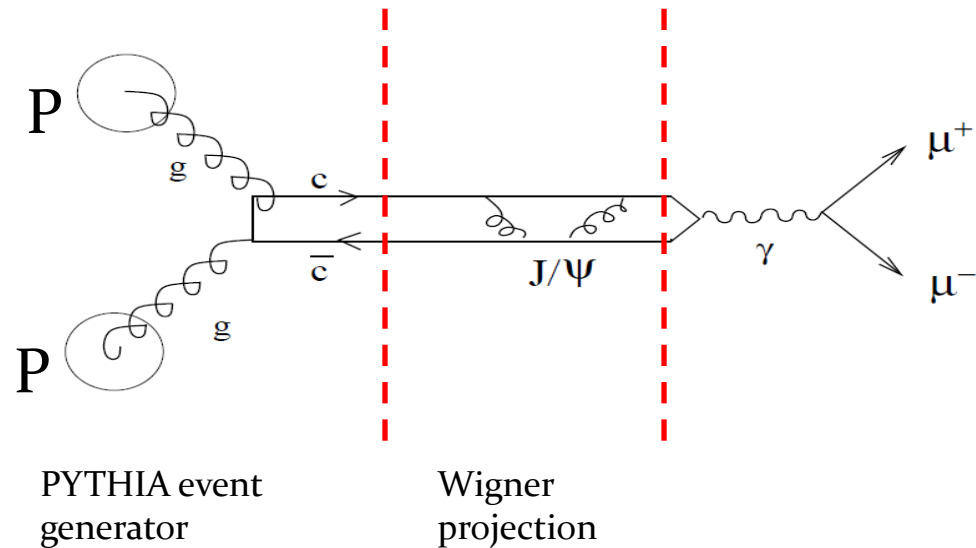
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# $J/\psi$ production in $p+p$ collisions

How to describe a composite object if perturbative QCD deals only with quarks and gluons

Need for **non perturbative** information/ assumptions.

Our approach: Wigner density formalism (as successful at lower energies)



# Wigner Density Formalism

Interaction depends on relative coordinates only,  $\rightarrow$  plane wave of CM

Starting point: Wave function (w.f.) of the relative motion of state  $i$ :  $|\Phi_i\rangle$

w.f  $\rightarrow$  density matrix  $|\Phi_i\rangle\langle\Phi_i|$

Fourier transform of density matrix in relative coord.  $\rightarrow$  Wigner density of  $|\Phi_i\rangle$   
(close to classical phase space density)

$$\Phi_i^W(\mathbf{r}, \mathbf{p}) = \int d^3y e^{i\mathbf{p}\cdot\mathbf{y}} \langle \mathbf{r} - \frac{1}{2}\mathbf{y} | \Phi_i \rangle \langle \Phi_i | \mathbf{r} + \frac{1}{2}\mathbf{y} \rangle .$$

$$\mathbf{R} = \frac{\mathbf{r}_1 + \mathbf{r}_2}{2}, \quad \mathbf{r} = \mathbf{r}_1 - \mathbf{r}_2,$$

$$\mathbf{P} = \mathbf{p}_1 + \mathbf{p}_2, \quad \mathbf{p} = \frac{\mathbf{p}_1 - \mathbf{p}_2}{2}.$$

$$n_i(\mathbf{R}, \mathbf{P}) = \int d^3r d^3p \Phi_i^W(\mathbf{r}, \mathbf{p}) n^{(2)}(\mathbf{r}_1, \mathbf{p}_1, \mathbf{r}_2, \mathbf{p}_2)$$

$n^{(2)}(\mathbf{r}_1, \mathbf{p}_1, \mathbf{r}_2, \mathbf{p}_2)$  two body cbar density matrix

pp: In momentum space given by PYTHIA (Innsbruck tune)

In coordinate space  $\sim r^2 \exp\left(-\frac{r^2}{2\delta^2}\right) \delta^2 = \langle r^2 \rangle / 3 = 4/(3m_c^2)$

# Wigner Density Formalism

If there are  $N$  c cbar pairs in the system the phase space density of states  $|\Phi_i\rangle$

$$n_i(\mathbf{R}, \mathbf{P}) = \sum \int \frac{d^3r d^3p}{(2\pi)^3} \Phi_i^W(\mathbf{r}, \mathbf{p}) \prod_j \int \frac{d^3r_j d^3p_j}{(2\pi)^3} n^{(N)}(\mathbf{r}_1, \mathbf{p}_1, \mathbf{r}_2, \mathbf{p}_2, \dots, \mathbf{r}_N, \mathbf{p}_N) \quad (5)$$

Sum over all possible c cbar pairs after integration of the relative coordinates  
Integration over all  $N-2$  left particles.

Multiplicity of  $|\Phi_i\rangle$

$$P_i = \int \frac{d^3R d^3P}{(2\pi)^3} n_i(\mathbf{R}, \mathbf{P})$$

Momentum distribution

$$\frac{dP_i}{d^3P} = \int \frac{d^3R}{(2\pi)^3} n_i(\mathbf{R}, \mathbf{P})$$

# Wigner Density Formalism

The Wigner density of the state  $|\Phi_i\rangle$  is different for S and P states

We choose the simplest possible parametrization

$$\Phi_S^W(\mathbf{r}, \mathbf{p}) = 8 \frac{D}{d_1 d_2} \exp \left[ -\frac{r^2}{\sigma^2} - \sigma^2 p^2 \right],$$

$$\Phi_P^W(\mathbf{r}, \mathbf{p}) = \frac{16}{3} \frac{D}{d_1 d_2} \left( \frac{r^2}{\sigma^2} - \frac{3}{2} + \sigma^2 p^2 \right) \\ \times \exp \left[ -\frac{r^2}{\sigma^2} - \sigma^2 p^2 \right],$$

$$r = r_c - r_{\bar{c}} \\ p = \frac{p_c - p_{\bar{c}}}{2}$$

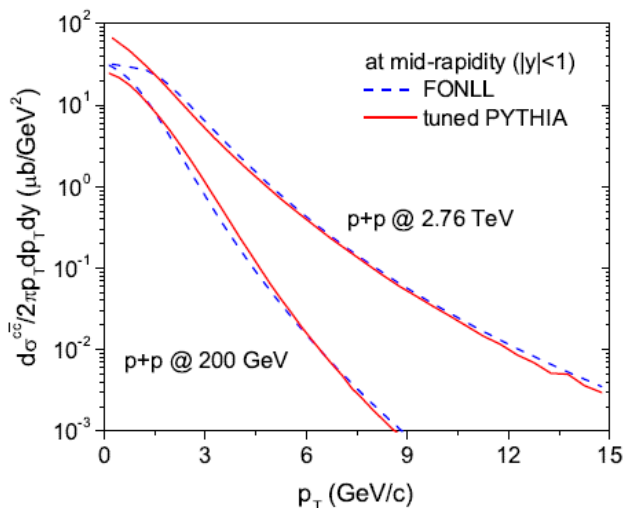
D : degeneracy of  $\Phi$   
 $d_1$  : degeneracy of c  
 $d_2$  : degeneracy of cbar  
 $\sigma \sim$  radius of  $\Phi$

Where  $\sigma$  reproduces the rms radius of the vacuum c cbar state  $|\Phi_i\rangle$

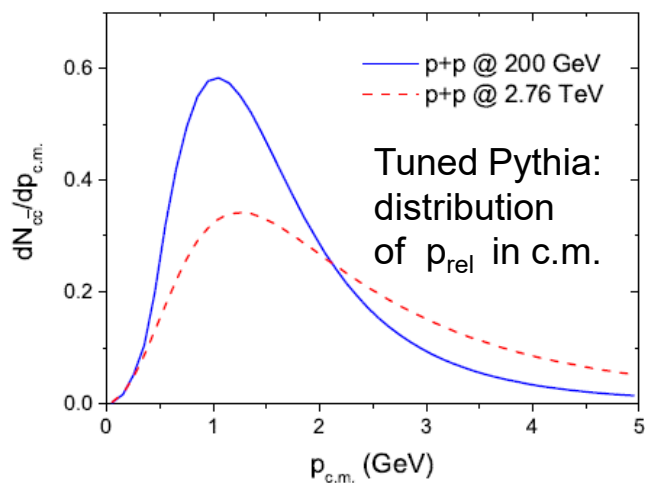
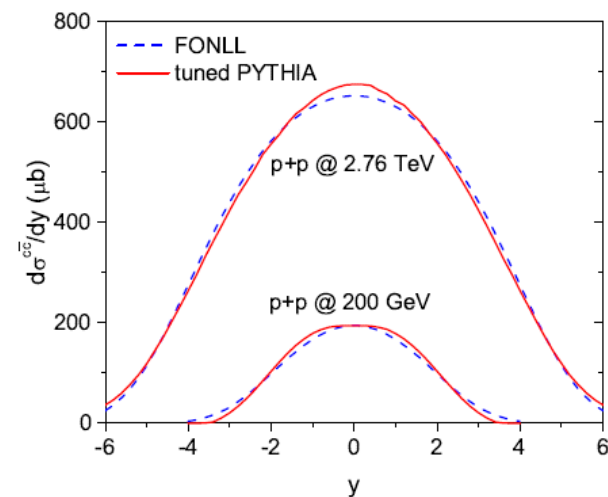
$$\Phi = J/\psi(1S), \quad \chi_c(1P), \quad \psi'(2S)$$

# Wigner Density Formalism

The (Innsbruck) tuned PYTHIA reproduces FONLL calculation  
but in addition it keeps the  $c\bar{c}$  correlation (not known in FONLL)

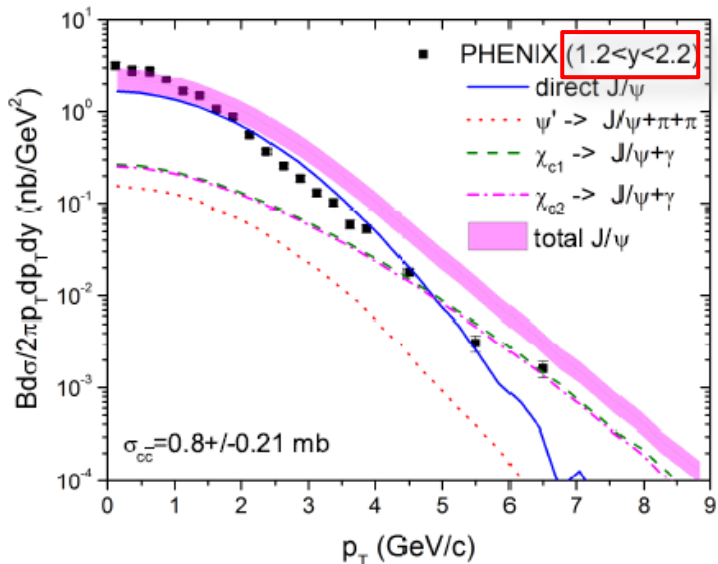
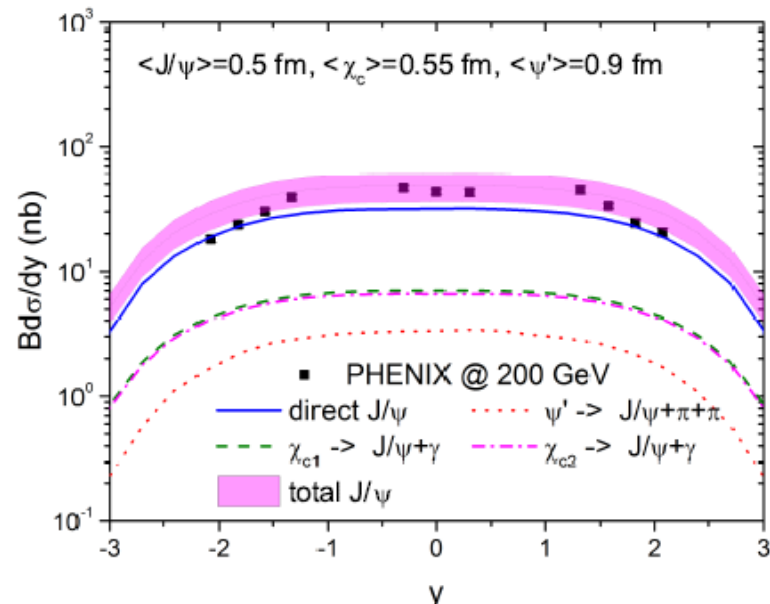
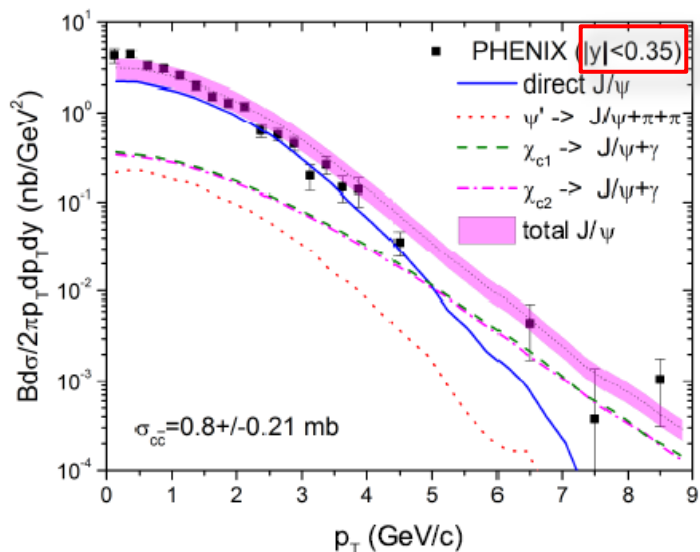


Distribution of  
charmed quarks



quite different relative momenta  
at RHIC and LHC

# pp: comparison with Phenix data

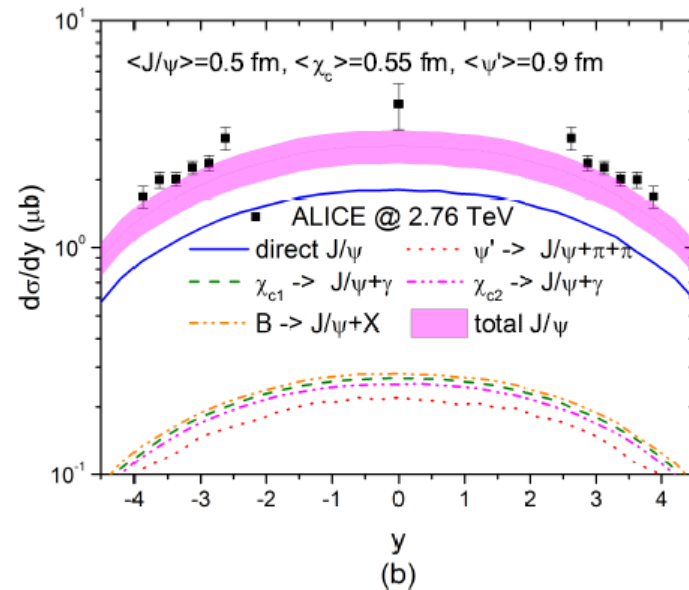
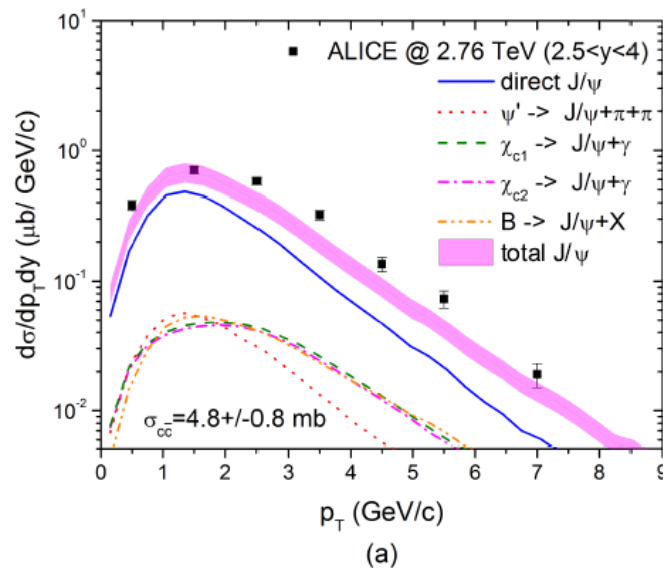


Good agreement for  
rapidity spectrum  
pt spectrum at  $|y| < 0.35$   
pt spectrum at  $1.25 < |y| < 2.2$

Feeding at RHIC not very important

# pp: comparison with ALICE data

same charmonia radii as at RHIC



Important contribution of feeding

The observed  $J/\psi$  data in pp at RHIC and LHC can be well described by Wigner dens.

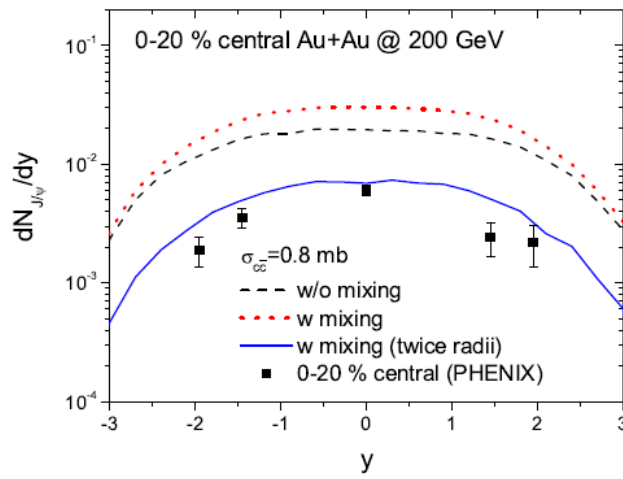


# AA collisions

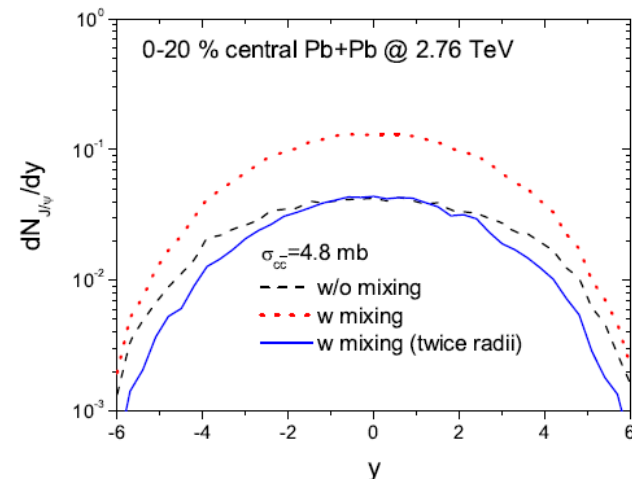
# AA: without any QGP

Without the formation of a QGP we expect a (large) **enhancement of the  $J/\psi$  production** because  $c$  and  $cbar$  **from different vertices** can form a  $J/\psi$ .

enhancement **46%**



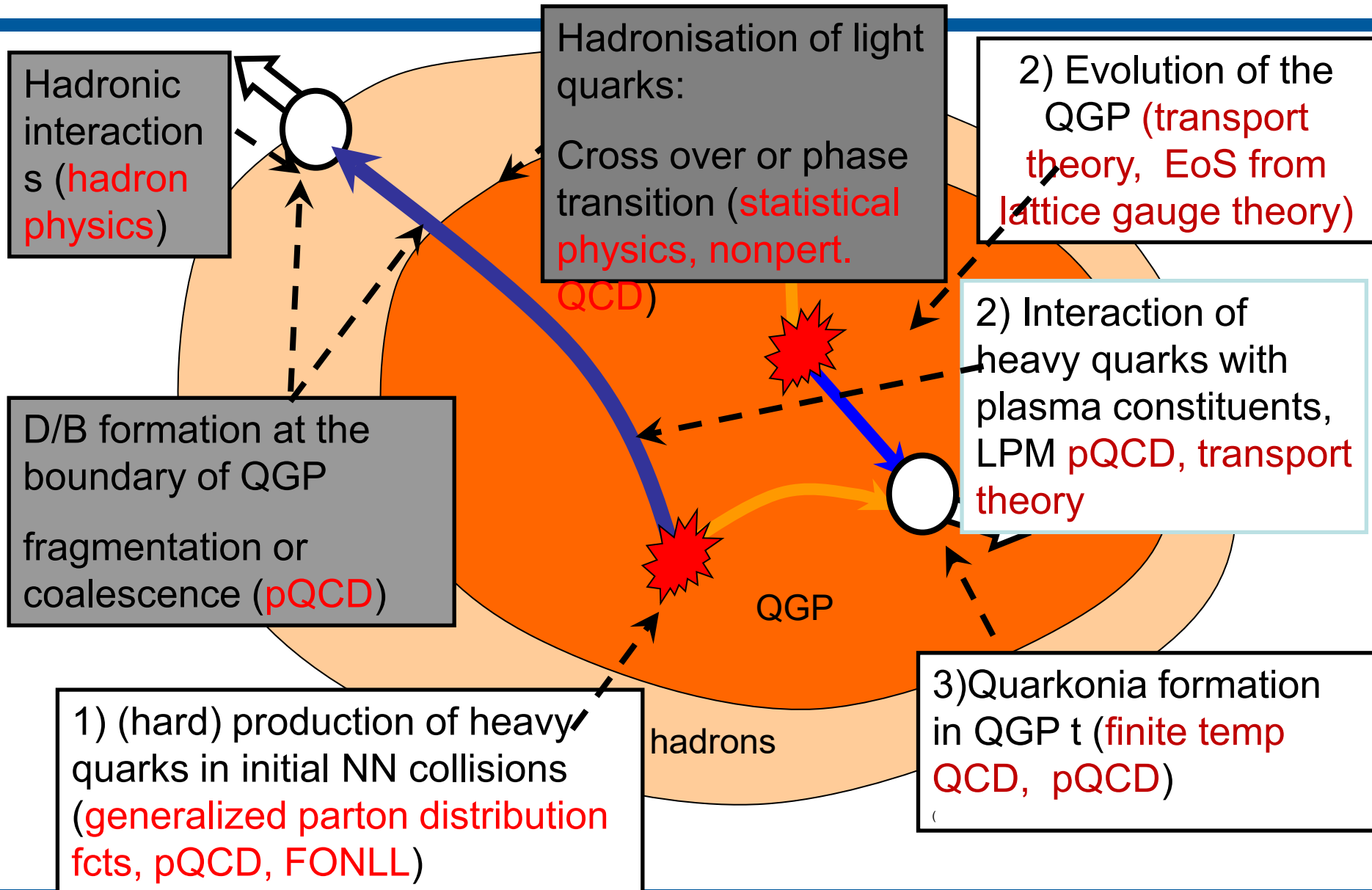
enhancement **270%**



**but experiments show suppression**

Reason:  $J/\psi$  production in HI collisions is a very complex process

# Complexity of heavy quark physics in HI reactions



# The different processes which influences the $J/\psi$ yield

- Creation of heavy quarks (shadowing)
- $J/\psi$  are first unstable in the quark gluon plasma and are created later
- $c$  and  $\bar{c}$  interact with the QGP
- $c$  and  $\bar{c}$  interact among themselves ( $\leftarrow$  lattice QCD)
- If QGP arrives at the dissociation temperature  $T_{\text{diss}}$ , stable  $J/\psi$  are possible
- $J/\psi$  creation ends when the QGP thermalizes
- $J/\psi$  can be further suppressed or created by hadronic interaction (task for the future  $\rightarrow$  Torres-Rincon)
- There may be in addition  $J/\psi$  from the corona

The model we developed follows the time evolution of all  $c$  and  $\bar{c}$  quarks based, as our pp calculation, on the Wigner density formalism

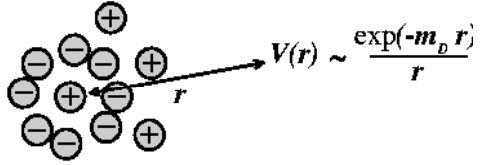
assumes that before and after the  $J/\psi$  formation

the  $c$  and  $\bar{c}$  interact with the medium as those observed finally as D-mesons

the  $c$  and  $\bar{c}$  interact among themselves

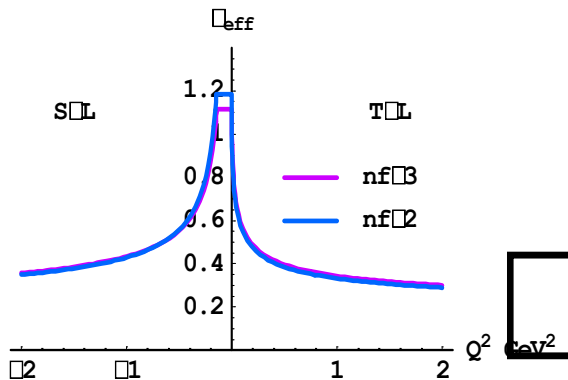
uses EPOS2 to describe the expanding QGP

The interaction between HQ and q and g is described by Born type diagrams

$$\frac{d\sigma_F}{dt} = \frac{g^4}{\pi(s - M^2)^2} \left[ \frac{(s - M^2)^2}{(t - \kappa m_D^2)^2} + \frac{s}{t - \kappa m_D^2} + \frac{1}{2} \right]$$


q/g is randomly chosen from a Fermi/Bose distribution with the hydro cell temperature

coupling constant and infrared screening are input



If  $t$  is small ( $\ll T$ ) : Born has to be replaced by a **hard thermal loop (HTL)** approach

For  $t > T$  Born approximation is (almost) ok

(Braaten and Thoma PRD44:1298,2625) for QED: Energy loss indep. of the **artificial scale**  $t^*$  which separates the regimes

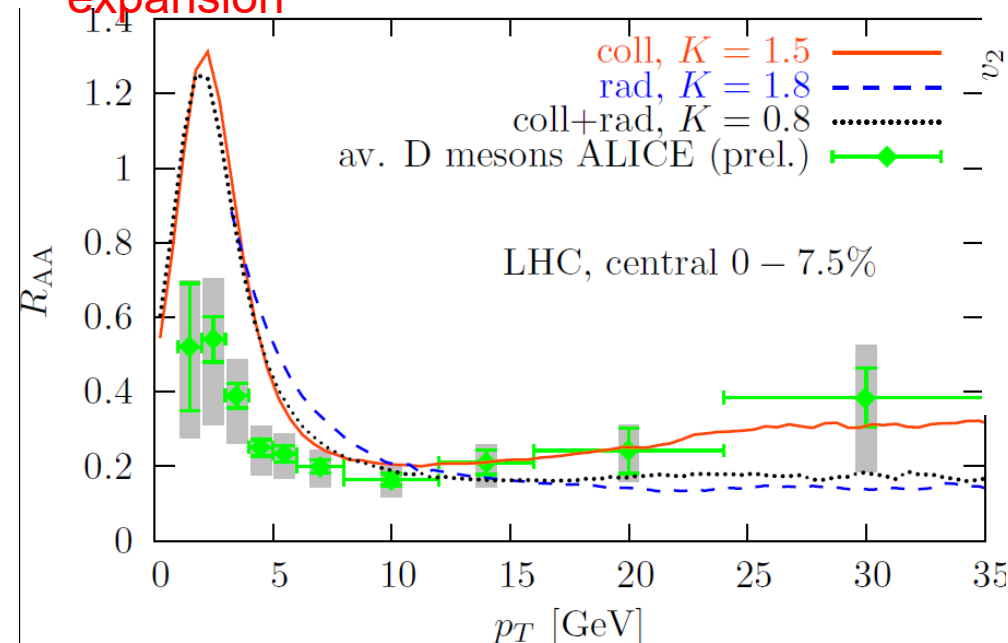
Extension to QCD (PRC78:014904)

Peshier 0801.0595  
based on universality  
constraint of Dokshitzer

$$\kappa \approx 0.2$$

# D meson result

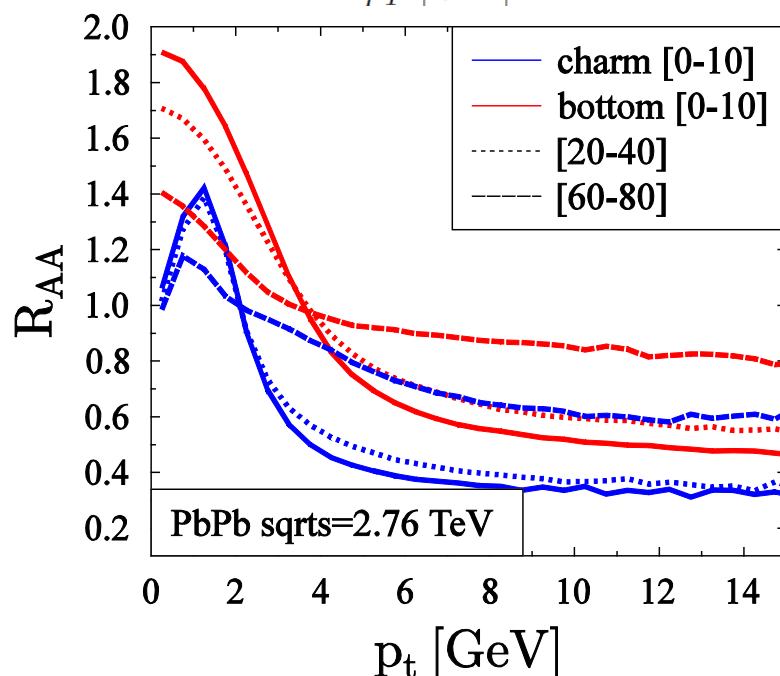
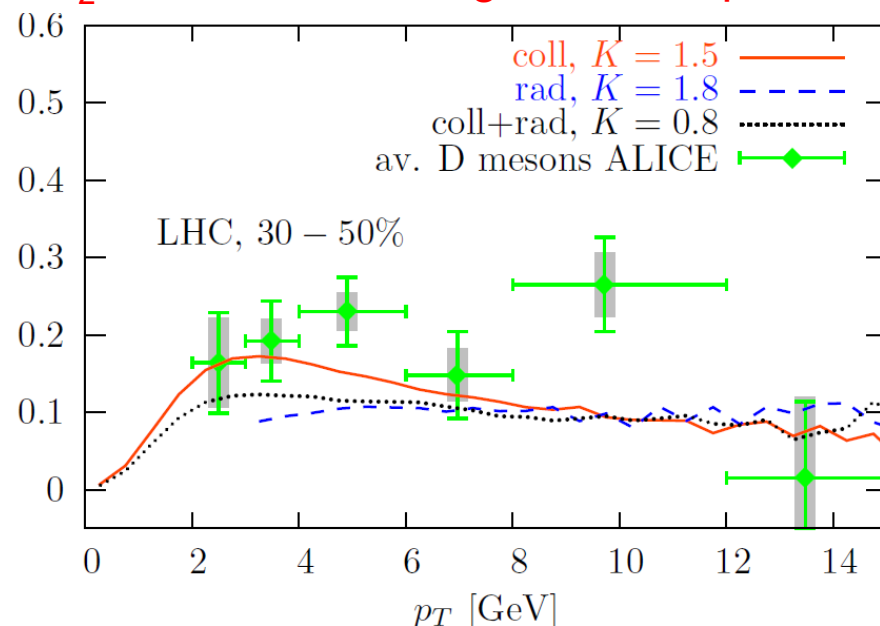
Energy loss tests the initial phase of the expansion



3 options :  
 Collisions only  $K$  factor = 1.5  
 Collision and radiation  $K = 0.8$   
 Radiation only  $K = 1.8$

$R_{AA}$  and  $v_2$  for coll and  
 coll + radiative about the same  
 B much more suppressed

$v_2$  tests the late stage of the expansion



# J/ψ creation in heavy ion collisions

Starting point: [von Neumann equation](#) for the density matrix of all particles

$$\partial \rho_N / \partial t = -i[H, \rho_N] \quad \text{with} \quad H = \sum_i K_i + \sum_{i>j} V_{ij}$$

gives the probability that at time  $t$  the state  $\Phi$  is produced:

$$P^\Phi(t) = \text{Tr}[\rho^\Phi \rho_N(t)] \quad \rho^\Phi = |\Psi^\Phi\rangle\langle\Psi^\Phi|$$

This is the solution if we could calculate the quantal  $\rho^N(t)$

In our semiclassical approach (correlations are lost) preferable to calculate the rate

$$\Gamma^\Phi(t) = \frac{dP^\Phi}{dt} = \frac{d}{dt} \text{Tr}[\rho^\Phi \rho_N(t)] \quad P^\Phi(T) = \int_0^T \Gamma^\Phi(t) dt$$

For time independent  $\rho^\Phi$

$$\Gamma^\Phi = \text{Tr}(\rho^\Phi d\rho^N(t)/dt) = -i \text{Tr}(\rho^\Phi [H, \rho^N(t)]) = -i \text{Tr}(\rho^\Phi [U_{12}, \rho^N])$$

$$U_{12} = \sum_{j \leq 3} (V_{1j} + V_{2j})$$

# J/ψ creation in heavy ion collisions

Heavy ion studies (BUU,QMD,PHSD) have shown that we obtain very satisfying results if we assume

$$W = \langle W^{\text{classic}} \rangle$$

We assume in addition that heavy quarks and QGP partons interact by collisions only

$$\frac{dP^\Phi(t)}{dt} = \prod_j^N \int d^3\mathbf{r}_j d^3\mathbf{p}_j W^\Phi \frac{d}{dt} W_N^c(t).$$

with

$$\begin{aligned} \frac{\partial}{\partial t} W_N^c(t) &= \sum_i v_i \cdot \partial_{r_i} W_N^c(\{\mathbf{r}\}, \{\mathbf{p}\}, t) \\ &+ \sum_{j \geq i} \sum_n \delta(t - t_{ij}(n)) \\ &\cdot (W_N^c(\{\mathbf{r}\}, \{\mathbf{p}\}, t + \epsilon) - W_N^c(\{\mathbf{r}\}, \{\mathbf{p}\}, t - \epsilon)). \end{aligned} \quad (19)$$

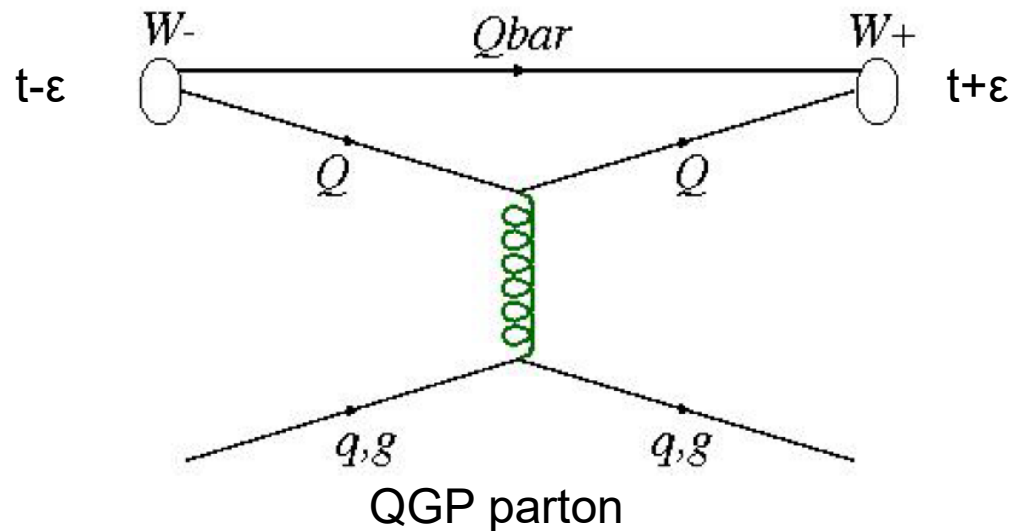


# J/ψ creation in heavy ion collisions

If the collisions are point like in time and if  $W^\Phi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{p}_1, \mathbf{p}_2)$  is time independent

$$\Gamma^\Phi(t) = \sum_{i=1,2} \sum_{j \geq 3} \delta(t - t_{ij}(n)) \prod_{k=1}^N \int d^3\mathbf{r}_i d^3\mathbf{p}_i$$

- $W^\Phi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{p}_1, \mathbf{p}_2)$
- $[W_N(\{\mathbf{r}, \mathbf{p}\}; t + \epsilon) - W_N(\{\mathbf{r}, \mathbf{p}\}; t - \epsilon)]$



# Our approach and open quantum systems

Von Neuman eq.

$$\partial \rho_N / \partial t = -\frac{i}{\hbar} [H, \rho_N] \quad H = H_{1,2} + H_{N-2} + U_{1,2} \quad U_{1,2} = \sum_j V_{1,j} + \sum_j V_{2,j}$$

Prob to find quarkonium  $P^\Phi(t) = \text{Tr}[\rho^\Phi \rho_N(t)]$  with  $[\rho^\Phi, H_{1,2}] = 0$   $[\rho^\Phi, H_{N-2}] = 0$

Quarkonium rate  $\frac{dP^\Phi(t)}{dt} = \Gamma^\Phi(t) = \frac{-i}{\hbar} \text{Tr}[\rho^\Phi [U_{1,2}, \rho_N(t)]]$

$$\partial \rho_N(t) / \partial t = -\frac{i}{\hbar} \sum_j [K_j, \rho_N(t)] - \frac{i}{\hbar} \sum_{k>j} [V_{jk}, \rho_N(t)].$$

Interaction: coll. heavy quarks –partons:

$$-\frac{i}{\hbar} \sum_{k>j} [V_{jk}, \rho_N(t)] \equiv \langle \sum_{k>j} \sum_n \delta(t - t_{jk}(n)) \cdot (W_N^c(\{\mathbf{r}\}, \{\mathbf{p}\}, t + \epsilon) - W_N^c(\{\mathbf{r}\}, \{\mathbf{p}\}, t - \epsilon)) \rangle.$$

yields  $\frac{dP^\Phi(t)}{dt} = \Gamma^\Phi(t) = h^3 \frac{d}{dt} \int \prod_j^N d^3 r_j d^3 p_j W_{12}^\Phi W_N^c(t) = h^3 \int \prod_i^N d^3 \mathbf{r}_j d^3 \mathbf{p}_j W_{12}^\Phi \frac{\partial}{\partial t} W_N^c(t)$

Lindblad eq. in the quantal Brownian motion regime  $\hbar_E \ll \hbar_S, \hbar_R$

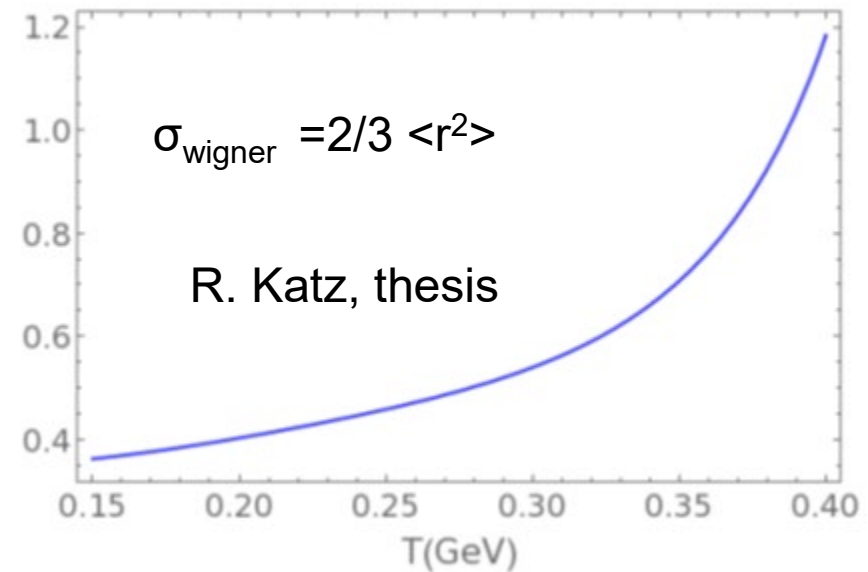
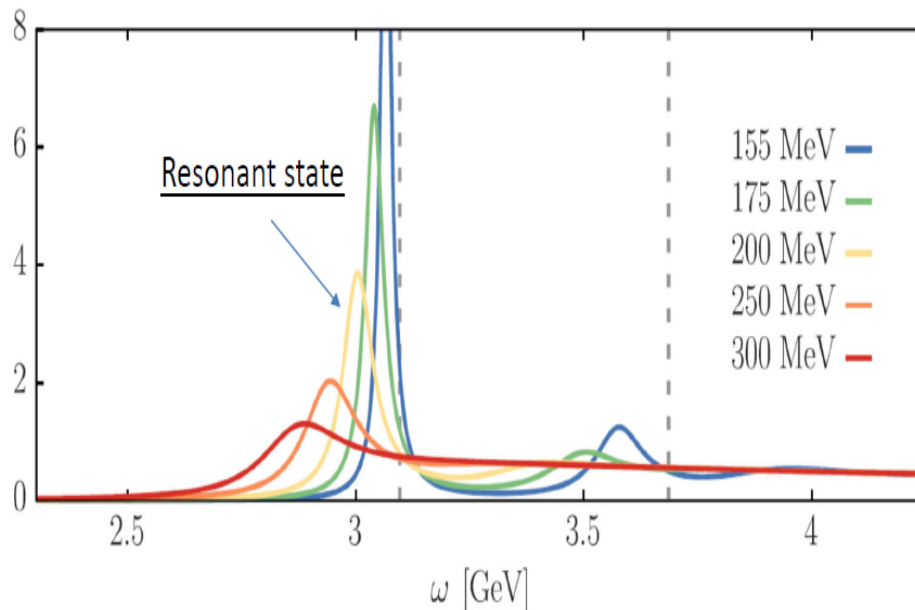
$$\frac{d}{dt} \rho(t) = -i \left[ \frac{p^2}{M} + \Delta H, \rho \right] + \sum_n \int \frac{d^3 k}{(2\pi)^3} \left[ C_n(\vec{k}) \rho C_n^\dagger(\vec{k}) - \frac{1}{2} \left\{ C_n^\dagger(\vec{k}) C_n(\vec{k}), \rho \right\} \right]$$

Miura, Akamatsu, [2205.15551](https://arxiv.org/abs/2205.15551)

# J/ψ creation in heavy ion collisions

Lattice calc: In an expanding QGP  $W^\Phi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{p}_1, \mathbf{p}_2)$  depends  
on the temperature and hence on time

Parametrization of the lattice results (Lafferty and Rothkopf PRD 101,056010)



This creates an additional rate, called local rate.

# Local Rate

Lattice :  $J/\psi$  wavefct is a function of the local QGP temperature

The QGP temperature decreases during the expansion

→  $J/\psi$  wavefct becomes time dependent

creates for  $T < T_{\text{diss}} = 400 \text{ MeV}$  a local  $J/\psi$  prod. rate

$$\begin{aligned}\Gamma_{loc} &= (2\pi\hbar)^3 \int d^3r d^3p W_{Q\bar{Q}}(\mathbf{r}, \mathbf{p}, t) \dot{W}_{\Phi}(\mathbf{r}, \mathbf{p}, T(t)). \\ &= \int d^3r d^3p \frac{16}{(\pi)^3} \dot{\sigma}(T(t)) \left( \frac{\mathbf{r}^2}{\sigma^3(T)} - \frac{\sigma(T)\mathbf{p}^2}{\hbar^2} \right) e^{-(\frac{\mathbf{r}^2}{\sigma^2} + \frac{\sigma^2\mathbf{p}^2}{\hbar^2})}\end{aligned}$$

Total  $J/\psi$  multiplicity at time  $t$  is then given by

$$P_{Q\bar{Q}}(t) = P^{\text{prim}}(t_{\text{init}}^{Q,\bar{Q}}) + \int_{t_{\text{init}}^{Q,\bar{Q}}}^t (\Gamma_{\text{coll},Q\bar{Q}}(t') + \Gamma_{\text{loc},Q\bar{Q}}(t')) dt'$$

For  $t \rightarrow \infty$   $P(t)$  is the observable  $J/\psi$  multiplicity

# Present interaction of c and cbar in the QGP

$V(r)$  = attractive potential between c and cbar (PRD101,056010)

We work in leading order in  $\gamma^{-1}$

$$\mathcal{L} = -\gamma^{-1}mc^2 - V(r) \quad H = \sqrt{m^2 + p_r^2 + \frac{p_\theta^2}{r^2}} + V(r) \quad p^2 = p_r^2 + p_\theta^2/r^2$$

$$\text{Time evolution equation:} \quad \gamma^{-1} = \sqrt{1 - v^2/c^2} \quad \frac{\partial \mathcal{L}}{\partial v_i} = p_i = \gamma m v_i$$

$$\dot{r} = \frac{\partial H}{\partial p_r} = \frac{p_r}{\sqrt{m^2 + p_r^2 + \frac{p_\theta^2}{r^2}}}$$

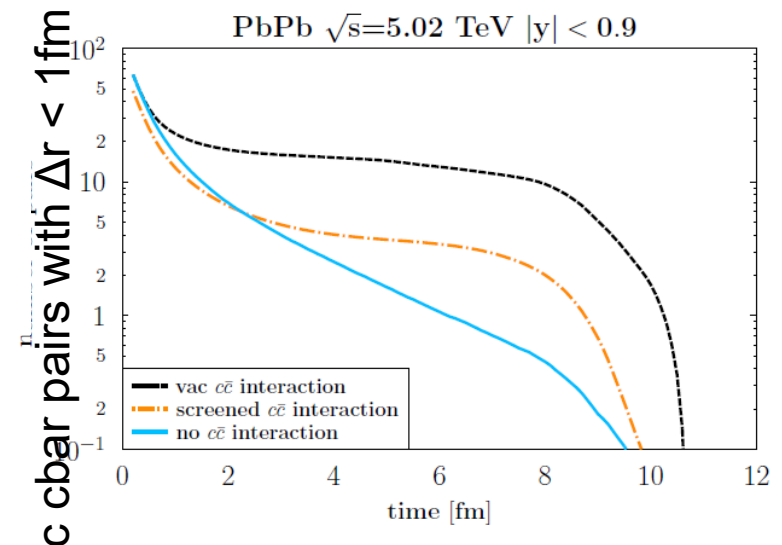
$$\dot{\theta} = \frac{\partial H}{\partial p_\theta} = \frac{p_\theta}{r^2 \sqrt{m^2 + p_r^2 + \frac{p_\theta^2}{r^2}}}$$

$$\dot{p}_r = -\frac{\partial H}{\partial r} = \frac{p_\theta^2}{r^3 \sqrt{m^2 + p_r^2 + \frac{p_\theta^2}{r^2}}} - \frac{\partial V}{\partial r}$$

$$= \frac{p_\theta \dot{\theta}}{r} - \frac{\partial V}{\partial r}$$

$$\dot{p}_\theta = -\frac{\partial H}{\partial \theta} = 0 \rightarrow p_\theta = \text{const} = L$$

position and momentum of each c cbar pair evolve according to these equations



# new description of c and cbar potential interaction

Not used in the present calculation

Extension to a real relativistic two body kinematics:

Energy and time constraints reduce 8 dim  $\rightarrow$  6+1 dim phase space

energy constraints

$$\phi_a = \frac{1}{2}(p_{a\mu}p_a^\mu - m_a^2 + \Phi) \approx 0$$

generalized Poisson brackets

$$\{A, B\} = \sum_k \frac{\partial A}{\partial x_k^\mu} \frac{\partial B}{\partial p_{k\mu}} - \frac{\partial B}{\partial x_k^\mu} \frac{\partial A}{\partial p_{k\mu}}$$

which gives the time evolution equations

$$\dot{x}_a^\mu = \{x_a^\mu, \phi_a\} \quad ; \quad \dot{p}_a^\mu = \{p_a^\mu, \phi_a\}$$

to know what the dot means we need time fixations to the system time  $\tau$

$$\chi_1 = \frac{1}{2}(x_1 - x_2)^\mu U_\mu \quad ; \quad \chi_2 = \frac{1}{2}(x_1 + x_2)^\mu U_\mu - \tau = 0$$

where U is the center of mass velocity

for details: Marty et al. PRC87,034912

# new description of c and cbar potential interaction

Fiziev and Todorov (PRD63,104007)

approximation which allows for a separation of CM and relative motion

$$\phi = H = \frac{1}{2\Lambda}(p_{rel}^2 - \mu^2 + \Phi)$$

$$p_{rel}^{cm} = \begin{pmatrix} \frac{s-m_1^2-m_2^2}{2\sqrt{s}} \\ \mathbf{p}_{rel}^{cm} = \nu_2 \mathbf{p}_1^{cm} - \nu_1 \mathbf{p}_2^{cm} \end{pmatrix} \quad \text{with } p_{rel}^{cm} p_{rel}^{cm} = \frac{m_1^2 m_2^2}{s} = \mu_{rel}^2 \quad \begin{aligned} \nu_1 - \nu_2 &= \frac{m_1^2 - m_2^2}{s} \\ \nu_1 + \nu_2 &= 1 \end{aligned}$$

H can be rewritten (for Coulomb)

with the time evolution eqs.

$$H = \frac{1}{2\lambda} \left( u_r^2 + \frac{J^2}{r^2} + 1 - \left( \epsilon^2 + \frac{e^2}{r} \right)^2 \right)$$

J: angular momentum

$\epsilon$ : const

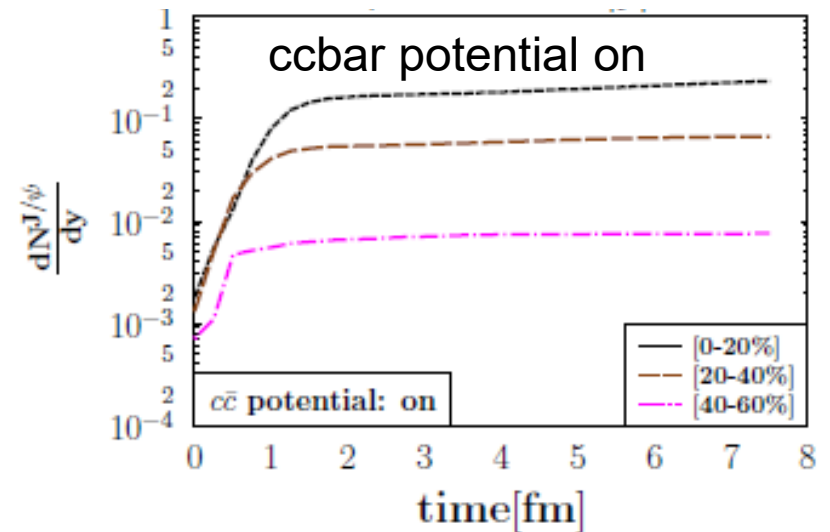
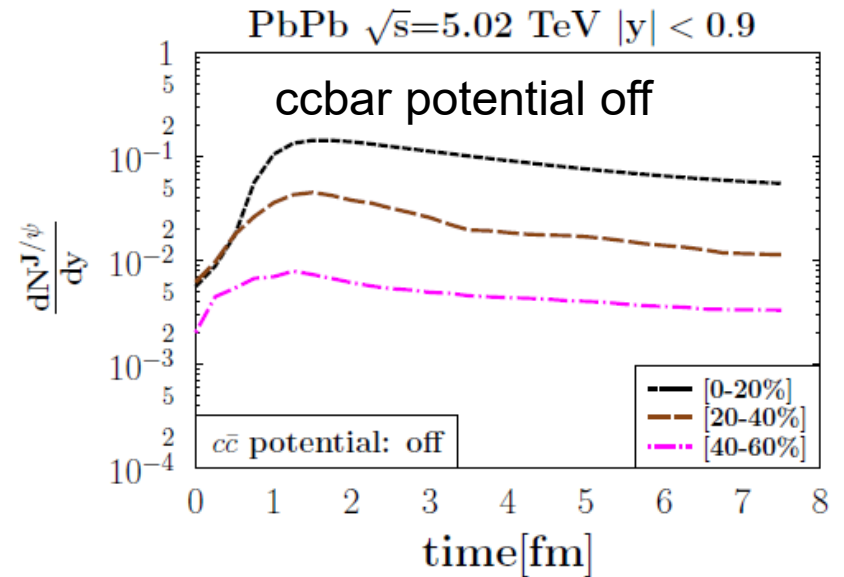
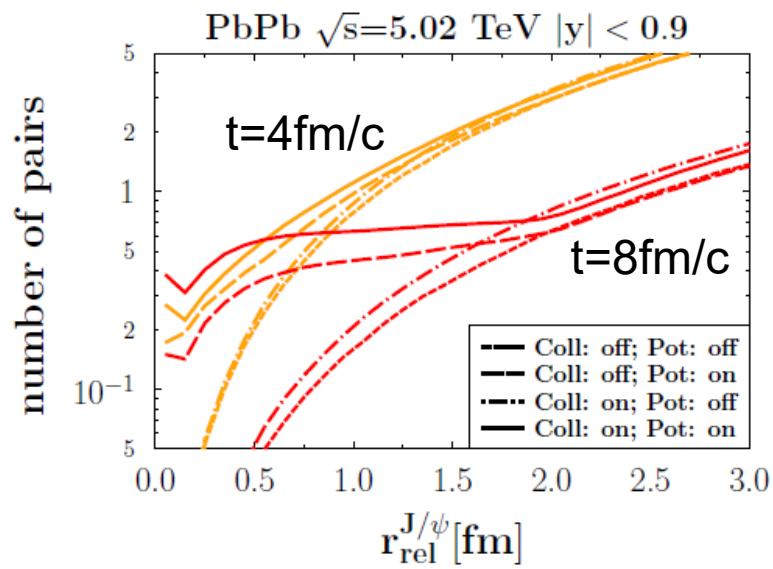
$$\begin{aligned} \dot{r} &= \frac{\partial H}{\partial u_r} = \frac{u_r}{\lambda} \\ \dot{u}_r &= -\frac{\partial H}{\partial r} = \frac{J^2}{\lambda r^3} - \frac{e^2(\epsilon^2 + \frac{e^2}{r})}{\lambda r^2} \\ \dot{\phi} &= \frac{\partial H}{\partial J} = \frac{J}{\lambda r^2} \\ \dot{J} &= -\frac{\partial H}{\partial \phi} = 0 \end{aligned}$$

# Results

Qq and Qg collisions shift  $p_T$  spectra to lower values

(as for D mesons)

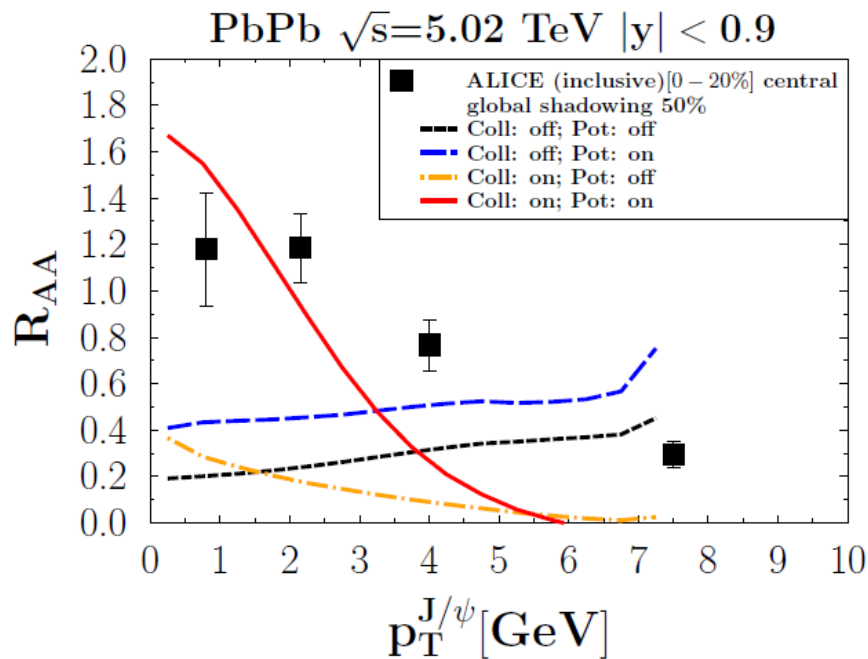
QQbar potential interaction increases the production rate



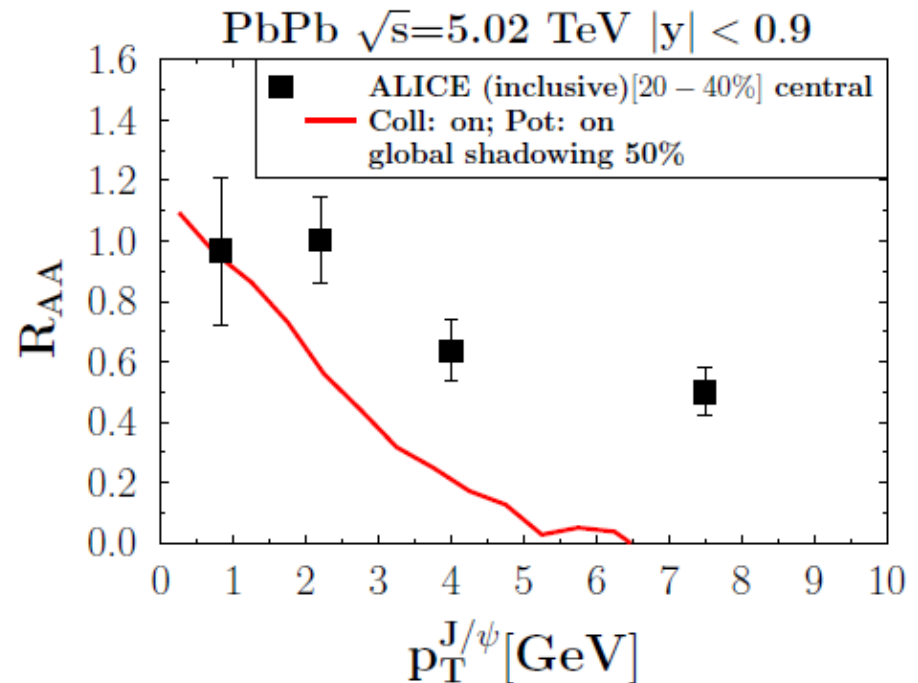


# Comparison with ALICE data

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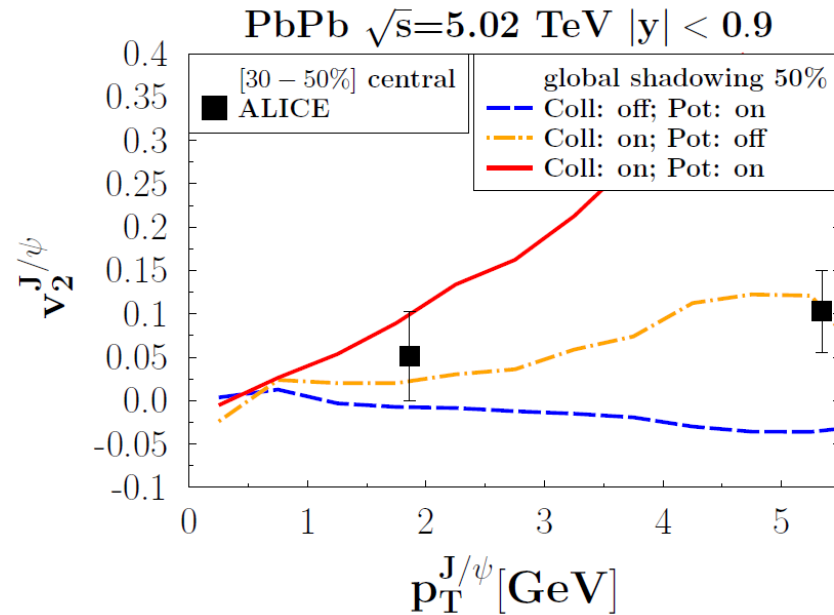
[20-40%]



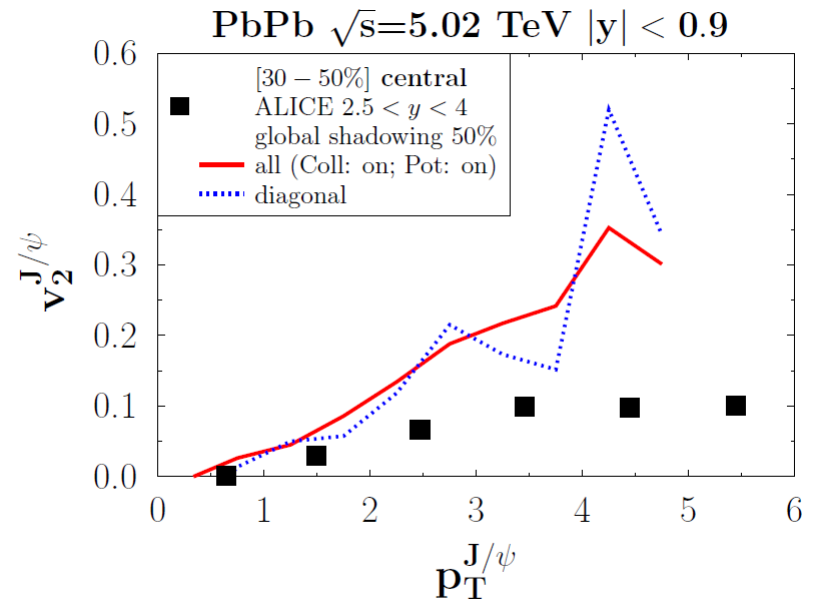
Caution: we compare inclusive ALICE data with calculation of direct prod.

# Comparison with ALICE data

[30-50%]



[30-50%]

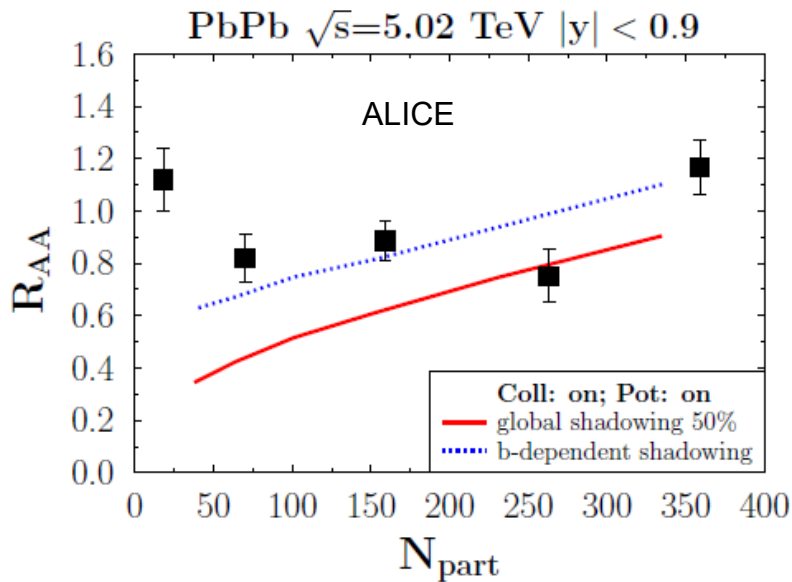


caution:

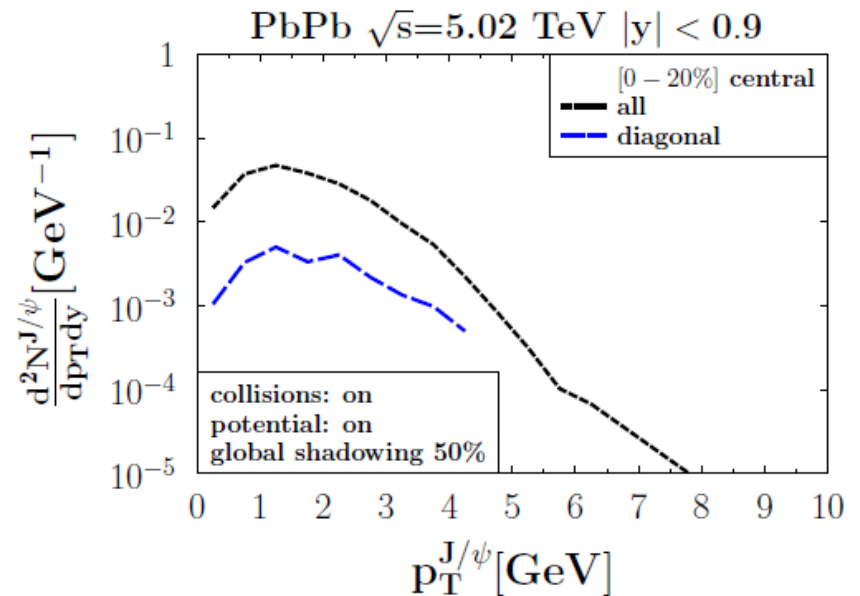
comparison of mid and forward rap

# Comparison with ALICE data

Centrality dependence



importance of c and cbar from difference vertices



# Summary

New approach **which follows each  $c$  and  $\bar{c}$  from creation until detection as  $J/\psi$**

(no rate equation, no Fokker Planck eq., no thermal assumptions)

$c$  and  $\bar{c}$  are created in initial hard collisions (controlled by pp data)

when entering the QGP  $J/\psi$  become unstable

$c$  and  $\bar{c}$  interact by potential interaction (lattice potential)

$c$  and  $\bar{c}$  interact by collisions with  $q, g$  from QGP

When  $T < T_{\text{diss}} = 400 \text{ MeV}$   $J/\psi$  can be formed (and later destroyed)

described by Wigner density formalism (as in pp)

Preliminary results agree reasonably with ALICE data for  $R_{AA}$  as well as for  $v_2$ .

The later production (over) compensates the expected multiplicity increase (with respect to pp) due to  $c$  and  $\bar{c}$  from different vertices

Has many common features with **open quantum system** approach (however bottom up)

A lot remains to be done.

- Follow the color structure, excited states, corona  $J/\psi$
  - Relativistic kinematics, hadronic expansion
- Collisions of preformed ( $r < \text{interaction range}$ )  $J/\psi$  with QGP partons