Rigid rotating NS as binary-neutron star-merger remnant

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Classic binary-neutron-star EM counterparts

- Short Gamma-ray burst
- Broadband sGRB afterglows: From X-ray to radio
- UV/optical/IR kilo-nova peaks at ~ 1 day
- Ejecta-ISM driven afterglows



Magnetar-powered EM signals

- Engine-fed kilonova (Mergernova) (Yu et al. 2013, Ai et al. 2022)
- Ejecta-ISM shock powered bright afterglow (Gao et al. 2013)
- (Short-GRB-less) X-ray internal plateau emission (Zhang 2013)
- Late-time X-ray flares (Zhang 2006, Piro et al. 2019)
- Fast radio burst induced by the collapse of the post-merger NS (Zhang 2014, Falcke & Rezzolla 2014)



(Gao et al. 2013)

Magnetar-powered X-ray Internal Plateau



- X-ray plateau followed by a sharp decay ($F \propto 1/t^{>3}$)
- A long-live central engine is required to power the plateau
- Any external shock emission cannot have a decay slope steeper than 3 (Kumar & Panaitescu 2000; Kobayashi & Zhang 2007)
- The most straightforward interpretation: NS collapsing to BH

Magnetar-powered (engine-fed) kilonova



- For the kilonova associated with GW170817 $L_p \sim 10^{42} {\rm erg/s}$ may be produced with short-lived Hyper-massive NS
- Some kilonova candidates have $L_p \sim 10^{43}$ erg/s. need long-lived magnetar as the central engine



Rigid rotating NS as BNS merger remnant

• Two types of mass:

Gravitational mass (M) vs. baryonic mass (M_b)

• Baryonic mass is conserved during the merger

$$M_{1} + M_{2} = M_{tot} = 2.74 M_{\odot}$$

$$M_{b,1} + M_{b,2} = M_{b,rem} + M_{ej}$$



•	Table 1 The 10 EoSs Investigated in This Paper									
$M_{rem,0}$		$M_{ m TOV} \ (M_{\odot})$	P _{k,min} ms	$M_{ m b,tot}$ (M_{\odot})	$M_{ m b,rem} \ (M_{\odot})$	$M^k_{ m rem} \ (M_\odot)$	P_k ms	$1 + \chi^k_{\mathrm{TOV}}$	$1 + \chi_{\max}$	Product Type
	SLy	2.05	0.55	$3.01\substack{+0.05 \\ -0.01}$	$2.95\substack{+0.06 \\ -0.02}$			1.039	1.184	BH
	WFF1	2.14	0.47	$3.07\substack{+0.05 \\ -0.01}$	$3.01\substack{+0.06 \\ -0.02}$	$2.51\substack{+0.03 \\ -0.01}$	0.52	1.051	1.201	SMNS
GW170817	WFF2	2.20	0.50	$3.04\substack{+0.05 \\ -0.01}$	$2.98\substack{+0.06 \\ -0.02}$	$2.51\substack{+0.04 \\ -0.01}$	0.58	1.048	1.192	SMNS
	Ap4	2.22	0.51	$3.03\substack{+0.05 \\ -0.01}$	$2.97\substack{+0.06 \\ -0.02}$	$2.52\substack{+0.03 \\ -0.01}$	0.60	1.047	1.194	SMNS
(Ai et al. 2020 APJ)	BSk21	2.28	0.60	$2.99\substack{+0.05\\-0.01}$	$2.93\substack{+0.06 \\ -0.02}$	$2.54\substack{+0.03 \\ -0.02}$	0.74	1.044	1.205	SMNS
	AP3	2.39	0.55	$3.01\substack{+0.05 \\ -0.01}$	$2.95\substack{+0.06 \\ -0.02}$	$2.54\substack{+0.03 \\ -0.02}$	0.70	1.049	1.202	SMNS
	DD2	2.42	0.65	$2.99\substack{+0.05\\-0.01}$	$2.93\substack{+0.06 \\ -0.02}$	$2.55\substack{+0.04 \\ -0.01}$	0.82	1.042	1.208	SMNS
	MPA1	2.48	0.59	$3.00\substack{+0.05\\-0.01}$	$2.94\substack{+0.06\\-0.02}$	$2.54\substack{+0.04 \\ -0.01}$	0.76	1.048	1.208	SNS
	Ms1	2.77	0.72	$2.95\substack{+0.05 \\ -0.01}$	$2.89\substack{+0.06\\-0.02}$	$2.56\substack{+0.04 \\ -0.01}$	1.00	1.043	1.207	SNS
	Ms1b	2.78	0.71	$2.96\substack{+0.05\\-0.01}$	$2.90\substack{+0.06\\-0.02}$	$2.56\substack{+0.04 \\ -0.01}$	0.99	1.042	1.212	SNS

Rigid rotating NS as NS-NS merger remnant

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 $M_1 + M_2$

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• Baryonic mass is conserved during the merger

 $M_{rem.0}$

Universal relation For non(slowly)-rotating NSs $M_b = M + 0.080M^2$

$$M_{b,1} + M_{b,2} = M_{b,rem} + M_{ej}$$

Universal relation For Keplerian rotating NSs $M_b = M + 0.064M^2$

	Non-rotating NS		Rotating NS			
	$M_b - M_g$ relation	Residual error ^A	$M_b - M_g$ relation	Residual error^{A}		
Lattimer & Yahil (1989) [20]	$M_b = M_g + 0.084 \times M_g^2$	4.1% (1.7%)	_	_	7	
Timmes <i>et al.</i> (1996) [17]	$M_b = M_g + 0.075 \times M_g^2$	5.8% (1.5%)	_	_	0 ^B	
Lattimer & Prakash (2001) [31]	$ \begin{array}{l} (M_b-M_g)/M_g=0.6\beta/(1\!-\!0.5\beta), \\ \text{where } \beta=GM_g/Rc^2 \end{array} $	2.8%~(0.92%)	_	_	14	
Coughlin <i>et al.</i> (2017) [32]	$M_b/M_g = 1 + 0.89 \times (M_g/R)^{1.2}$	$2.6\% \; (0.56\%)$	_	_	19	
This work	_	_	Maximally rotating NSs	_	-	
	$M_b = M_g + R_{1.4}^{-1} \times M_g^2$	1.8%~(1.1%)	$M_b = M_g + 0.078 R_{1.4}^{-1} \times M_g^2$	1.3%~(0.74%)	10	
	$M_b = M_g + 0.080 \times M_g^2$	5.0%~(1.5%)	$M_b = M_g + 0.064 \times M_g^2$	3.3%~(1.2%~)	10	
	$M_b = M_g + A_1 \times M_g^2 + A_2 \times M_g^3$	$0.45\% \ (0.16\%)$	$M_b = M_g + 0.056 \times M_g^2 + 0.003 \times M_g^3$	3.5%~(1.0%)	10	
	_	_	General NSs with arbitrary rotation	—	-	
	_	_	$M_b = M_g + R_{1.4}^{-1} e^{-\frac{1}{4\mathcal{P}}} \times M_g^2$	3.3% (1.0%)	10	
	_	_	$M_b = M_g + 0.073 \times M_g^2$	6.0%~(1.6%)	10	
	_	_	$M_b = M_g + 0.078 \times M_g^2 + 0.002 \times M_g^3$	4.0% (0.95%)	10	

(Gao et al. 2020 Frontiers of Physics)

^AThe maximum residual error of the transformation between M_b and M_g , with the average residual error showing in the brackets.

^BTimmes *et al.* [17] claims that the M_b-M_g relations used in their paper is based on private communications with J. M. Lattimer.

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 $M_{1} + M_{2}$ $M_{b,1} + M_{b,2} = M_{b,rem} + M_{ej}$ $M_{rem,0}$

• Define
$$\chi_{max} = (M_{max} - M_{TOV})/M_{TOV}$$

 $\chi_{TOV} = (M - M_{TOV})/M_{TOV}$, for $M = M(P = P_k, M_{\infty} = M_{TOV})$

(Ai et al. 2020 APJ)

• $\chi_{max} \approx 0.2$; $\chi_{TOV} \approx 0.05$

$$\begin{split} M_{rem,0} &> (1 + \chi_{max}) M_{TOV} \rightarrow BH \\ (1 + \chi_{TOV}) M_{TOV} < M_{rem,0} < (1 + \chi_{max}) M_{TOV} \rightarrow SMNS \\ M_{rem,0} &< (1 + \chi_{TOV}) M_{TOV} \rightarrow SNS \end{split}$$

1.2LS220 ${
m BHB}\Lambda \phi$ DD2SFHo 1.0 $P_0 \, [\mathrm{ms}]$ 0.8(Radice et al. 2018) 0.62.53.02.03.51.5 $M_b [M_{\odot}]$



GW170817



- If a BH was formed directly after the HMNS, We have $M_{TOV} < 2.09^{+0.11}_{-0.09} M_{\odot}$
- If a SMNS was formed after the differentially rotating phase and finally collapses into a BH, We have $2.09^{+0.11}_{-0.09}M_{\odot} < M_{TOV} < 2.43^{+0.10}_{-0.08}M_{\odot}$

• If a SNS was formed, We have $M_{TOV} > 2.43^{+0.10}_{-0.08} M_{\odot}$. (2 σ)

Constraints on the NS Properties in the MNS Cases



Following the spin period evolution of a SMNS, given its lifetime and M_{TOV} , constraints can be put on B (EM radiation) and ϵ (GW radiation).

Low B, NS hides in the center? High B NS but quickly collapses or GW dominated spin-down? (Ai, Gao & Zhang 2020, The Astrophysical Journal)

(Ai et al. 2018, The Astrophysical Journal)

What's the merger product of GW170817?

• Hyper-massive NS \rightarrow BH?

 $M_{TOV} < 2.1 M_{\odot}$, close the mass of observed massive pulsars?

PSR J1614-2230: $1.97 \pm 0.04 M_{\odot}$ (Demorest et al. 2010) PSR J0348+0432: $2.01 \pm 0.04 M_{\odot}$ (Antoniadis et al. 2013) PSR J0740+6620: $2.14^{+0.10}_{-0.09} M_{\odot}$ (Cormartie et al. 2019) **30% SGRBs have X-ray internal plateaus?**

• Hyper-massive NS \rightarrow Super-massive NS (\rightarrow BH)?

short-lived SMNS? $M_{TOV} \sim 2.1 M_{\odot}$

long-lived SMNS? High B, but GW dominated spin-down (\checkmark) stable NS? High B, but GW dominated spin-down (\checkmark)