Nuclear ab-initio Theories and Neutrino Physics

February 26 – March 30
INT Seattle

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From dilute matter to the equilibrium point in the energy-density-functional theory
Present collaborators along this research line

- **ENSAR2, JRA TheoS** (Theoretical Support for Nuclear Facilities in Europe)
  Task: Development of suitable effective interactions in mean-field and BMF theories

- **International Laboratory LIA COLL-AGAIN** (France-Italy collaborations)

- **J. Bonnard, A. Boulet, U. van Kolck, D. Lacroix, O. Vasseur** (IPN Orsay)

- **J. Yang** (George Washington University), 3 years spent at IPN

- **G. Colò, X. Roca-Maza** (Univ. of Milano)
Energy Density Functional (EDF) theory (functionals derived in most cases from effective phenomenological interactions) since several decades...

Nuclear many-body problem with effective interactions

Energy Density Functional (EDF) theory (functionals derived in most cases from effective phenomenological interactions) ... since several decades

Mean-field models and beyond

Double counting, divergences, ...

Work on EDF designed for beyond-mean-field models Nuclear matter

Bridging with EFT/ab initio (borrowing concepts and techniques - less phenomenological)
Starting point. Work on EDF designed for beyond-mean-field models. Beyond mean field: second order in the Dyson perturbative many-body expansion for nuclear matter with Skyrme-type interactions.

Divergences, double counting -> regularization procedures and parameters adjustment (for ‘usual’ nuclear density scales)
Properties of matter: relevant for constraining energy density functionals for finite nuclei and neutron stars

- Neutron-rich matter and pure neutron matter
- Physics of isospin asymmetric systems
- Very low-density neutron matter
- Surface properties of neutron-rich nuclei with a diffuse density
- Outer crust of neutron stars
- Analogy with ultracold atomic gases at unitarity (large scattering length)
• Around the saturation point and beyond.

The structure of neutron stars may be calculated by solving the Tolmann-Oppenheimer-Volkoff equations. Pressure (first derivative of the EOS) enters in such equations. The total radius is provided by the point where the pressure vanishes:

**neutron star mass/radius**
Equation of state of nuclear matter with a Skyrme-type interaction.

The perturbative many-body problem:

- Moghrabi, Grasso, Colo’, Van Giai, PRL 105, 262501 (2010)
- Yang, Grasso, Roca-Maza, et al., PRC 94, 034311 (2016)
- Yang, Grasso, and Lacroix, PRC 96, 034318 (2017)
- Yang, Grasso, et al., PRC 95, 054325 (2017)

\[ k_F = (3/2 \pi^2 \rho)^{1/3} \quad \text{SM} \]
\[ k_F = k_N = (3\pi^2 \rho)^{1/3} \quad \text{NM} \]

This second-order contribution diverges \(\rightarrow\)

**For ex. the square of the Skyrme \(t_0\) term has a \(k_F^4\) dependence** and is the sum of a finite part plus a term **linearly dependent on the cutoff** (on the transferred momentum \(q\)) \(\rightarrow\) **REGULARIZATION**
Skyrme interaction for matter (no spin orbit at the mean-field level)

\[ v = t_0 (1 + x_0 P_\sigma) + \frac{1}{2} t_1 (1 + x_1 P_\sigma) (k'^2 + k^2) + t_2 (1 + x_2 P_\sigma) k' \cdot k + \frac{1}{6} t_3 (1 + x_3 P_\sigma) \rho^\alpha \]

Spin-exchange operator \[ P_\sigma = \frac{1}{2} (1 + \sigma_1 \cdot \sigma_2) \]
Second-order contribution to the EOS (symmetric matter)

$$\int d^3k_1 \int d^3k_2 \int d^3q (v G v)$$

$$G = \frac{-1}{\epsilon_1' + \epsilon_2' - \epsilon_1 - \epsilon_2}, \quad \epsilon_i^{(')} = \frac{\hbar^2 k_i^{(')} 2}{2m_i^*}$$

$$k_1' = q + k_1, \quad k_2' = k_2 - q,$$

$$|k_1| < k_{F1}, \quad |k_2| < k_{F2}, \quad |q + k_1| > k_{F1}, \quad |k_2 - q| > k_{F2}$$

In symmetric matter, neutron and proton Fermi momenta are the same:

$$k_F = \left(\frac{3\pi^2}{2}\rho\right)^{1/3}$$
EOS of symmetric matter and cutoff regularization

- **First order**

\[
\frac{E_S^{(1)}}{A} = \frac{3}{10} \frac{\hbar^2}{m} \left( \frac{3\pi^2}{2} \right)^{\frac{2}{3}} \rho^3 + \frac{3}{8} t_0 \rho + \frac{3}{80} \left( \frac{3\pi^2}{2} \right)^{\frac{2}{3}} \Theta_S \rho^3 + \frac{1}{16} t_3 \rho^{\alpha+1}
\]

\[
\Theta_S = 3t_1 + t_2 (5 + 4x_2)
\]

- **Second order**

Convenient change of variables: using the incoming and outgoing relative momenta \( k \) and \( k' \)

\[
k = \frac{k_1 - k_2}{2}, \quad k' = \frac{k'_1 - k'_2}{2} = \frac{k_1 - k_2}{2} + q
\]

Then the propagator can be simplified and written as

\[
G = \frac{-m^*}{\hbar^2(k'^2 - k^2)}
\]
Second-order contribution for symmetric matter (without the spin-orbit and the tensor terms). Sum of the two following terms (cutoff on $k'$)

\[
\frac{E_{l=0}^{S(2)}}{A} = - \frac{mk_F^4}{110880\hbar^2\pi^4} \left\{ -6534 + 1188\ln[2] + 3564\lambda - 19602\lambda^3 - 5940\lambda^5 \\
+ (1782 - 20790\lambda^4)\ln[\frac{\lambda-1}{\lambda+1}] + (24948\lambda^5 - 5940\lambda^7)\ln[\frac{\lambda^2-1}{\lambda^2}] \\
- 14696 + 2112\ln[2] - 5280\lambda - 2860\lambda^3 \\
- 48840\lambda^5 - 18480\lambda^7 + (2640 - 55440\lambda^6)\ln[\frac{\lambda-1}{\lambda+1}] \\
+ (71280\lambda^7 - 18480\lambda^9)\ln[\frac{\lambda^2-1}{\lambda^2}] \\
- 9886 + 1128\ln[2] - 2520\lambda + 147\lambda^3 - 3654\lambda^5 \\
- 35280\lambda^7 - 15120\lambda^9 + (1260 - 41580\lambda^8)\ln[\frac{\lambda-1}{\lambda+1}] + (55440\lambda^9 - 15120\lambda^{11})\ln[\frac{\lambda^2-1}{\lambda^2}] \right\} + \frac{k^2}{f} \tilde{T}_{03} \tilde{T}_1 + \frac{4}{f} \tilde{T}_{03}^2 \tilde{T}_1 + \frac{4}{f} \tilde{T}_{1}^2 \tilde{T}_1
\]

\[
\frac{E_{l=1}^{S(2)}}{A} = - \frac{mk_F^8}{73920\hbar^2\pi^4} \left\{ -1033 + 156\ln[2] - 420\lambda + 140\lambda^3 - 840\lambda^5 \\
- 5880\lambda^7 - 2520\lambda^9 + (-210 + 6930\lambda^8)\ln[\frac{\lambda-1}{\lambda+1}] \\
+ (9240\lambda^9 - 2520\lambda^{11})\ln[\frac{\lambda^2-1}{\lambda^2}] \right\}
\]

Asymptotic behavior:

\[ E_{l=0,\text{poly}}^{\text{sym}(2)} = -\frac{18m k_s^4}{4\hbar^2 \pi^4} \left[ \frac{k_s^4 \tilde{T}_1^2}{300} \lambda^5 + \left( \frac{k_s^2 \tilde{T}_0 \tilde{T}_1}{108} + \frac{k_s^4 \tilde{T}_1^2}{240} \right) \lambda^3 + \left( \frac{\tilde{T}_0^2}{12} + \frac{k_s^2 \tilde{T}_0 \tilde{T}_1}{60} + \frac{k_s^4 \tilde{T}_1^2}{140} \right) \lambda \right] 
+ \frac{4k_s^2 \tilde{T}_0 \tilde{T}_1 (-167+24ln[2]) + k_s^4 \tilde{T}_1^2 (-4943+564ln[2]) + 297\tilde{T}_0^2 (-11+2ln[2])}{50k_s^2} 
- \left( \frac{\tilde{T}_0^2}{240} + \frac{k_s^2 \tilde{T}_0 \tilde{T}_1}{140} + \frac{k_s^4 \tilde{T}_1^2}{270} \right) / \lambda + O(\lambda^{-2}) \]

\[ E_{l=1,\text{poly}}^{\text{sym}(2)} = -\frac{18m k_s^8}{4\hbar^2 \pi^4} \left[ \frac{1}{720} \lambda^3 + \frac{1}{560} \lambda + \left( \frac{-1033+156ln[2]}{332640} \right) \right] \tilde{T}_2^2. \]
Combinations of Skyrme parameters

\[
\tilde{T}_{03}^2 = \left[ t_0(1-x_0) + \frac{1}{6} t_3(1-x_3) \rho^\alpha \right]^2 + \left[ t_0(1+x_0) + \frac{1}{6} t_3(1+x_3) \rho^\alpha \right]^2
\]

\[
\tilde{T}_1^2 = \frac{1}{4} t_1^2 \left[ (1-x_1)^2 + (1+x_1)^2 \right] = \frac{1}{2} t_1^2 (1+x_1^2)
\]

\[
\tilde{T}_{03} \tilde{T}_1 = \frac{t_1}{2} \left[ [t_0(1-x_0) + \frac{1}{6} t_3(1-x_3) \rho^\alpha](1-x_1) + [t_0(1+x_0) + \frac{1}{6} t_3(1+x_3) \rho^\alpha](1+x_1) \right]
\]

\[
\tilde{T}_2^2 = \left[ t_2^2 (1-x_2)^2 + 9 t_2^2 (1+x_2)^2 \right]/9
\]

\[
= \frac{2}{9} t_2^2 (5 + 8x_2 + 5x_2^2).
\]
Double counting and ultraviolet divergence (equation of state of symmetric matter)

(a) Second-order EOS of symmetric matter computed for several values of the cutoff $\Lambda$ and compared with the mean-field EOS; (b) second-order correction to the energy per particle for symmetric matter. The used parameters are those of SLy5.

Double counting and ultraviolet divergence (pressure and incompressibility)

\[ P(\rho, \Lambda) = \rho^2 \frac{d}{d\rho} \frac{E}{A}(\rho, \Lambda) \]

\[ K(\rho, \Lambda) = 9\rho^2 \frac{d^2}{d\rho^2} \frac{E}{A}(\rho, \Lambda) \]

(a) Second-order pressure; (b) second-order incompressibility modulus. The used parameters are those of SLy5.

Cutoff-regularized and readjusted EOSs. Simultaneous fit for symmetric, asymmetric and neutron matter (benchmark: SLy5 mean field)

\[
\frac{\rho_n - \rho_p}{\rho_n + \rho_p} = 0.5
\]

Pressure and incompressibility (not entering in the fit)

Pressure (a) and incompressibility modulus (b) computed with the parameters of the simultaneous fit and compared with the mean-field curves.

Remaining at leading order in the perturbative expansion … new functionals for nuclear matter
YGLO functional 
(resummation at leading order)
Low-density for neutron matter (EFT satisfies this regime -> Hammer, Furnstahl, NPA 678, 277 (2000))

Lee-Yang expansion in \((ak_N)\). Low-density EOS

Lee and Yang, Phys. Rev. 105, 1119 (1957)

\[
\frac{E}{N} = \frac{\hbar^2 k_N^2}{2m} \left[ \frac{3}{5} + \frac{2}{3\pi} (k_Na) + \frac{4}{35\pi^2} (11 - 2\ln 2) (k_Na)^2 \right]
\]

<table>
<thead>
<tr>
<th>Skyrme term</th>
<th>kN dependence in the EOS</th>
</tr>
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<tbody>
<tr>
<td>(t_0)</td>
<td>(k_N^3)</td>
</tr>
<tr>
<td>(t_3)</td>
<td>(k_N^{3\alpha+3})</td>
</tr>
<tr>
<td>(t_1) and (t_2)</td>
<td>(k_N^5)</td>
</tr>
</tbody>
</table>

\(\alpha = 1/3\)
We have to constrain the parameters in the following way:

\[ t_0(1 - x_0) = 4\pi \hbar^2 a/m. \]

\[ t_3(1 - x_3) = \frac{\hbar^2}{m} \frac{144}{35} (3\pi^2)^{1/3} (11 - 2\ln 2)a^2. \]

\[ t_0 = \frac{-9849.45}{1 - x_0} \text{MeV fm}^3, \]

\[ t_3 = \frac{1812705.02}{1 - x_3} \text{MeV fm}^4. \]
It is possible to constrain the low-density behavior of neutron matter, with $\alpha=1/3$, and to adjust $x_0$ and $x_3$ for reproducing a reasonable EOS for symmetric matter (at ordinary densities).

But the EOS of neutron matter is completely wrong at ordinary scales of densities.

Yang, Grasso, Lacroix, PRC 94 , 031301(R) (2016)
Neutron matter at ‘usual’ density scales. Example of Lyon-Saclay forces adjusted on the neutron EOS.

\[
\frac{E}{N} = \frac{\hbar^2 k_N^2}{2m} \left[ \frac{3}{5} + \frac{2}{3\pi} (k_N a) + \frac{4}{35\pi^2} (11 - 2ln2)(k_N a)^2 \right]
\]


Neutron matter energy divided by the free gas energy.
Some indications from second-order calculations: the second-order contribution has the required $k_F^4$ term (second term of Lee-Yang exp.)

… but only second order is not enough (if one wants to keep the correct value of the scattering length)

Resummation techniques
- Steele, arXiv: nucl-th/0010066v2
- Kaiser, NPA 860, 41 (2011)
- Schaefer, NPA 762, 82 (2005)

Effective field theories capable of describing systems with anomalously large scattering lengths require summing an infinite number of Feynman diagrams at leading order …
Guided by:
1) The fact that the second-order $t_0$ contribution leads to the correct dependence on the Fermi momentum in neutron matter;
2) The resumed formulae;
3) Good properties of Skyrme functionals

A hybrid functional, YGLO (Yang, Grasso, Lacroix, Orsay): Matching the low-density limit with the Lee-Yang expansion of the energy

$$
\nu = \frac{B_\beta \rho^2}{1 - R_\beta \rho^{1/3} + C_\beta \rho^{2/3}} + D_\beta \rho^{8/3} + F_\beta \rho^{\alpha+2}.
$$

Beta = 1 -> symmetric matter
Beta = 0 -> neutron matter
YGLO functional: Inspired by resumed expressions (resumed functional) (EFT)

EOS for symmetric and neutron matter:

Constrained by the first two terms of Lee Yang formula (scattering length)

\[ \frac{E}{A} = K_\beta + \frac{B_\beta}{1 - R_\beta \rho^{1/3} + C_\beta \rho^{2/3}} + D_\beta \rho^{5/3} + F_\beta \rho^{\alpha+1} \]

Resumed expression

Mimic velocity- and density-dependent terms

Other parameters adjusted on QMC results at extremely low densities and on Friedman et al. or Akmal et al. EOSs at higher densities

Yang, Grasso, Lacroix, PRC 94, 031301(R) (2016)
B and R are fixed by imposing to recover the Lee-Yang formula (the analog for symmetric matter may be found in Fetter-Walecka book)

\[ B_\beta = 2\pi \frac{\hbar^2}{m} \frac{(\nu - 1)}{\nu} a, \quad R_\beta = \frac{6}{35\pi} \left(\frac{6\pi^2}{\nu}\right)^{\frac{1}{3}} (11 - 2 \ln 2) a, \]

\( \nu = 2 \ (4) \) is the degeneracy for \( \beta = 0 \) (1)
The other adjusted parameters

YGLO functional. In all cases, $\alpha = 0.7$.

<table>
<thead>
<tr>
<th></th>
<th>$C_\beta$ (fm$^2$)</th>
<th>$D_\beta$ (MeV fm$^5$)</th>
<th>$F_\beta$ (MeV fm$^{3+3\alpha}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta = 0$ (FP)</td>
<td>100.87</td>
<td>-9264.18</td>
<td>9571.90</td>
</tr>
<tr>
<td>$\beta = 0$ (Akmal)</td>
<td>70.19</td>
<td>-8377.83</td>
<td>8743.85</td>
</tr>
<tr>
<td>$\beta = 1$ (FP)</td>
<td>8.188</td>
<td>-6624.87</td>
<td>6995.46</td>
</tr>
</tbody>
</table>

Benchmark data are (i) for neutron matter, the QMC AV4 results of Ref. [17] for values of $|ak_N| < 10$ ($\rho < 0.05$ fm$^{-3}$), and two different sets of results for $|ak_N| > 10$: the Friedman et al. results (FP) of Ref. [18] or the Akmal et al. results (stiffer EOS) of Ref. [19] [we call here the corresponding parameter sets YGLO (FP) and YGLO (Akmal), respectively]. (ii) For symmetric matter, the FP results and those of Akmal et al. are very close from each others and we made a fit using only the FP points.
YGLO. Very low-density behavior of neutron matter

Energy divided by the free gas energy

Yang, Grasso, Lacroix, PRC 94, 031301(R) (2016)
Asymmetric matter

Parabolic approximation

\[ \frac{E_\delta}{A}(\rho) = \frac{E_{SM}}{A}(\rho) + S(\rho)\delta^2 \]

\[ \delta = \frac{(\rho_N - \rho_P)}{\rho_N + \rho_P} \]

Neutron density

Proton density
Asymmetric matter

EOSs from Akmal et al. [19] (blue diamonds) and Friedman et al. (purple circles) in symmetric and neutron matter compared to the YGLO (Akmal) (red dot-dashed curve) and YGLO (FP) (blue dashed curve) results. The different gray dotted curves correspond to the YGLO(FP) EOSs obtained for different asymmetry $\delta$ from 0.1 to 0.9 by steps of 0.1 (see text).
Neutron skin thickness (difference between rms radii of neutrons and protons)

Dipole polarizability versus neutron skin thickness

Dipole polarizability times symmetry energy versus neutron skin thickness

Roca-Maza et al, PRC 92, 064304 (2015)
Symmetry energy and its slope \( L = 3 \rho_0 \left( \frac{dS}{d\rho} \right)_{\rho = \rho_0} \)

Strong correlation observed between the neutron skin thickness and the slope \( L \) of the symmetry energy (see for instance: Warda et al. PRC 80, 024316 (2009), Centelles et al. PRL 102, 122502 (2009) ->

This correlation is thus expected to exist between the electric dipole polarizability times the symmetry energy and the slope of the symmetry energy.

Recent experimental determinations of the electric dipole polarizability:

- \(^{208}\text{Pb}\) (polarized proton inelastic scattering at forward angles, RCNP) (Tamii et al. PRL107, 062502 (2011)). Combining all available data: \( \alpha_D = 20.1 \pm 0.6 \text{ fm}^3 \)

- \(^{120}\text{Sn}\) (polarized proton inelastic scattering at forward angles, RCNP) (Hashimoto et al. PRC 92, 031305 (2015)). Combining all available data: \( \alpha_D = 8.93 \pm 0.36 \text{ fm}^3 \)

- \(^{68}\text{Ni}\) (Coulomb excitation in inverse kinematics and invariant mass in one- and two-neutron decay channels, GSI) (Wieland et al, PRL 102, 092502 (2009); Rossi et al. PRL 111, 242503 (2013)). \( \alpha_D = 3.40 \pm 0.23 \text{ fm}^3 \)
Using the experimental values of the electric dipole polarizability in the three nuclei

$^{208}\text{Pb} \rightarrow J = (24.5 \pm 0.8) + (0.168 \pm 0.007) \ L$

$^{68}\text{Ni} \rightarrow J = (24.9 \pm 2.0) + (0.19 \pm 0.02) \ L$

$^{120}\text{Sn} \rightarrow J = (25.4 \pm 1.1) + (0.17 \pm 0.01) \ L$

Roca-Maza et al, PRC 92, 064304 (2015)
Symmetry energy and its slope

Lines delimit the phenomenological areas constrained by the experimental determination of the electric dipole polarizability.
No resummation. Imposing a Lee-Yang regime at all densities at leading order
Without resummation, how to handle the different density scales?

A Lee-Yang type expression for the EOS of neutron matter-> if the low-density regime is always satisfied

\[
\frac{E}{N} = \frac{\hbar^2 k_F^2}{2m} \left[ \frac{3}{5} + \frac{2}{3\pi} (k_F a) + \frac{4}{35\pi^2} (11 - 2 \ln 2)(k_F a)^2 \right. \\
\left. + \frac{1}{10\pi} (k_F r_s)(k_F a)^2 + 0.019(k_F a)^3 \right]
\]

We choose to keep terms containing only the s-wave scattering length. The next term in the Lee-Yang expansion contains the p-wave scattering length.

Grasso, Lacroix, Yang, Phys. Rev. C 95, 054327 (2017)
Neutron-neutron scattering length.

Low-density regime: \(|a k_F| < 1\).

We impose a low-density constraint: - a \(k_F=1 \rightarrow\)

- \(a = -18.9 \text{ fm up to a max momentum so that } 18.9 k_F=1.\)
- Beyond this value, we tune the scattering length so that \(-a = 1/k_F\)
Neutron-neutron scattering length

Grasso, Lacroix, Yang, PRC 95, 054327 (2017).
Interdisciplinary bridges

Analogy with atomic gases close to Feshbach energy in the case of a density-dependent scattering length
We introduce a Skyrme-type functional containing only s-wave terms and leading, at the mean-field level, to a neutron matter EOS given by the LY expression, with the relations:

\[ t_0(1 - x_0) = \frac{4\pi \hbar^2}{m} a, \]
\[ t_3(1 - x_3) = \frac{144\hbar^2}{35m} (3\pi^2)^{1/3} (11 - 2 \ln 2) a^2, \]
\[ t_1(1 - x_1) = \frac{2\pi \hbar^2}{m} (a^2 r_s + 0.19\pi a^3), \]

The power of the density-dependent term is chosen equal to 1/3

Grasso, Lacroix, Yang, PRC 95, 054327 (2017).
We require that:

(i) The functional correctly describes neutron matter at all density scales

(ii) The functional leads to a reasonable EOS for symmetric matter around the equilibrium point

This may be obtained by imposing a low-density regime everywhere (with a density-dependent neutron-neutron scattering length)
The parameters $x_i$ do not enter in the EOS of symmetric matter.

We may thus adjust the parameters $t_i$ to have a reasonable EOS of symmetric matter and tune the neutron-neutron scattering length by imposing, at each density scale, a low-density constraint.

**Symmetric matter, two cases**
- $t_0-t_3$
- $t_0-t_3-t_1$

Grasso, Lacroix, Yang, Phys. Rev. C 95, 054327 (2017)
Density dependence of the parameters $x_0$ and $x_3$

![Graph showing the dependence of $x_0$ and $x_3$ on density.]

Typical Skyrme values at densities around the saturation point

Grasso, Lacroix, Yang, Phys. Rev. C 95, 054327 (2017)
First two terms of the Lee-Yang expansion. EOS of neutron matter

LY with $-18.9$ fm

First two terms

Huge discrepancy

SLy5 mean field

SkP mean field

SIII mean field

Grasso, Lacroix, Yang, Phys. Rev. C 95, 054327 (2017)
Including the s-wave $k_F^5$ terms and adjusting the effective range.

Grasso, Lacroix, Yang, PRC 95, 054327 (2017).
Low-density behavior

Grasso, Lacroix, Yang, Phys. Rev. C 95, 054327 (2017)
Adding spin-orbit and pairing to our functionals

Adjusting to preudodata: using the average of the results shown in the figure below (except Brueckner HF Bonn A)

Dots: Green’s function and auxiliary field diffusion QMC
- Maris et al., PRC 87, 054318 (2013)
- Gandolfi et al., PRL 106, 012501 (2011)
- 2-body AV8’, Pudliner 1997
- 3-body UIX, Pudliner 1995
- 3-body IL7, Pieper 2008

Squares: configuration-interaction (Maris et al)

Pentagones: no-core shell model and coupled cluster (Potter et al. PLB, 739, 445 (2014))

Bonnard, Grasso, Lacroix, in progress
Adding spin-orbit and pairing to our functionals

Adjusting to pseudodata: using the average of the results shown in the figure below (except Brueckner HF Bonn A)

Additional parameters in finite-size systems:

- Harmonic shell closures $N=8, 20$ (no spin orbit, no pairing) (disentangle density-dep. and velocity-dep. Terms for $k_F^5$)

- Spin orbit coupling constant: adjusting to $N \pm 1$

Pairing strength (density-dependent mixed surface-volume interaction): mid-shell systems 12, 14, 16

- Rest will be predictions
Lee-Yang inspired functional. HF calculations (no spin orbit, no pairing). Lee-Yang regime with - a $k_F = \Lambda$

Original functional

Modifying $\Lambda$ or $r_s$, but the EOS is deteriorated

The $k_F^5$ term in the EOS may come from velocity-dependent terms as well as from density-dependent terms $\rightarrow W$ is the mixing parameter

$W = 1.00, \Lambda = 1.00, r_s = -4.50$ fm
$\Lambda = 1.00, r_s = -2.95$ fm
$\Lambda = 0.84, r_s = -4.50$ fm
$W = 0.43, \Lambda = 1.00, r_s = -4.50$ fm

average
After adjustment of spin-orbit and pairing

\[ \varepsilon_{pp}(\vec{r}) = V_{pp} \left(1 - \frac{1}{2} \frac{\rho(\vec{r})}{\rho_c}\right) \tilde{\rho}(\vec{r}) \]

Bonnard, Grasso, Lacroix, in progress
Root-mean-square radius

Bonnard, Grasso, Lacroix, in progress
Pairing potential

Bonnard, Grasso, Lacroix, in progress
Conclusions

• New functionals valid at all density scales for neutron matter and at densities around saturation for symmetric matter

- YGLO (resummation from EFT and good properties of Skyrme forces : a hybrid functional)

- without resummation -> density-dependent neutron-neutron scattering length

- not only nuclear matter. Towards finite-size systems: preliminary results for neutron drops